Rescaling Confidence: What Scale Design Reveals About LLM Metacognition

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Abstract

Verbalized confidence, in which LLMs report a numerical certainty score, is widely used to estimate uncertainty in black-box settings, yet the confidence scale itself (typically 0–100) is rarely examined. We show that this design choice is not neutral. Across six LLMs and three datasets, verbalized confidence is heavily discretized, with more than 78% of responses concentrating on just three round-number values. To investigate this phenomenon, we systematically manipulate confidence scales along three dimensions: granularity, boundary placement, and range regularity, and evaluate metacognitive sensitivity using $meta\text{-}d'$. We find that a 0–20 scale consistently improves metacognitive efficiency over the standard 0–100 format, while boundary compression degrades performance and round-number preferences persist even under irregular ranges. These results demonstrate that confidence scale design directly affects the quality of verbalized uncertainty and should be treated as a first-class experimental variable in LLM evaluation.

1 Introduction

As Large Language Models (LLMs) are increasingly integrated into decision-making pipelines, reliably estimating their uncertainty has become a critical challenge. In black-box settings, ***verbalized confidence***, where models report a numerical certainty score via prompting, has become the predominant paradigm (Xiong et al., 2024), with demonstrated utility in selective prediction (Kadavath et al., 2022), self-correction (Li et al., 2024), and calibrating human trust (Zhou et al., 2024), yet the reliability of these confidence signals remains poorly understood.

Given its ubiquity, research on verbalized confidence has focused on elicitation strategies such as Chain-of-Thought prompting (Wei et al., 2022), self-consistency (Wang et al., 2022), and training models to express uncertainty (Lin et al., 2022a), while treating the ***confidence scale*** itself (typically 0–100) as a neutral instrument. Yet psychometric research has long established that scale granularity and anchoring alter the quality of self-assessment (Lozano et al., 2008; Preston and Colman, 2000). Whether analogous effects hold for LLMs remains unexplored.

We show that LLM confidence reports exhibit a striking phenomenon we term ***confidence discretization***: LLMs do not use the 0–100 scale as a continuous spectrum but cluster outputs around a small set of round-number anchors. This compression, which we show to be pervasive yet model-specific, suggests that verbalized confidence is shaped as much by token-level biases (Zhao et al., 2021; Shaki et al., 2023) as by genuine self-evaluation, potentially distorting standard calibration metrics such as ECE (Guo et al., 2017). This raises a central question: does confidence scale design affect the quality of verbalized uncertainty signals in LLMs?

To investigate, we present the the first systematic empirical study of **confidence scale design for LLM metacognition**, manipulating scales along three dimensions: *granularity* (0–5 to 0–100), *boundary shifting* (e.g., lower bound raised to 20 or 60 (Tversky and Kahneman, 1974)), and *semantic robustness* via non-standard ranges (e.g., 0–73, 14–86 (Pellert et al., 2024)). We adopt $meta\text{-}d'$ from signal detection theory (Maniscalco and Lau, 2012; Fleming and Lau, 2014) to quantify metacognitive sensitivity independent of overall bias.

Our contributions are:

- We establish **confidence discretization** as a robust phenomenon across multiple LLM families, revealing model-specific distribution patterns that bias self-reported uncertainty.

- We demonstrate that **scale granularity** significantly modulates metacognitive quality, identi-

fying a consistent sweet spot that outperforms the standard 0–100 scale.

- Through **non-standard scale experiments**, we show that LLMs possess limited semantic understanding of numerical ranges, and provide actionable guidelines for confidence scale design.

2 Related Work

2.1 Verbalized Confidence and Calibration in LLMs

As LLMs became increasingly inaccessible behind commercial APIs, research on uncertainty estimation shifted from logit-based methods (Kadavath et al., 2022) toward **verbalized confidence**, where models are prompted to express certainty as a numerical score (Lin et al., 2022a; Xiong et al., 2024). Substantial effort has been devoted to improving elicitation through methods such as Chain-of-Thought prompting (Wei et al., 2022), metacognitive prompting (Wang and Zhao, 2024), self-consistency aggregation (Wang et al., 2022), and strategies for RLHF-aligned models (Tian et al., 2023), as well as to evaluation, predominantly through Expected Calibration Error (ECE; Guo et al., 2017). However, this body of work uniformly treats the confidence scale as a fixed backdrop, assuming that a 0–100 scale faithfully transmits whatever metacognitive signal the model possesses. When models concentrate the vast majority of their reports on two or three values, ECE bins become sparse or empty across most of the range, making calibration estimates unreliable. This **discretization bias** and its dependence on scale design have not been systematically studied.

2.2 Scale Design in Psychometrics

In human subject research, scale design is known to be non-neutral: the number of response categories modulates both reliability and validity (Lozano et al., 2008; Preston and Colman, 2000), and scale boundaries bias judgments toward specific anchors (Tversky and Kahneman, 1974; Harvey, 1997). While such sensitivities are well-documented for human respondents, it remains unclear whether they apply to LLMs, whose outputs are driven by token-level distributions rather than human cognition. LLMs may exhibit analogous effects, or their biases may stem from an entirely different mechanism: the statistical prevalence of certain numerical tokens in pre-training corpora (Zhao et al., 2021; Shaki et al., 2023). Our work is the first to systematically test these possibilities.

2.3 Metacognitive Sensitivity and Signal Detection Theory

Evaluating metacognition requires distinguishing Type-1 performance (task accuracy) from Type-2 sensitivity (the ability to monitor that accuracy) (Galvin et al., 2003). Signal Detection Theory (SDT) provides a principled framework for this decomposition (Hautus et al., 2021). The $meta\text{-}d'$ metric (Maniscalco and Lau, 2012) quantifies metacognitive sensitivity, that is, how well confidence ratings separate correct from incorrect responses, independently of response bias (Fleming and Lau, 2014; Rausch et al., 2023), with corrections for extreme proportions ensuring robustness under skewed distributions (Hautus, 1995). Recent NLP work has begun separating metacognitive ability from task performance (Wang et al., 2025), but no existing study has applied SDT-based metrics to evaluate how scale design interacts with LLM metacognition. By applying $meta\text{-}d'$ to controlled manipulations of confidence scales, we address this gap.

3 Methodology

3.1 Task Formulation

We frame confidence elicitation as a Type-2 (metacognitive) judgment layered on top of a Type-1 (task-level) decision. Given a task instance x from a dataset $\mathcal{D}$, a model M generates an answer $\hat{y}$ and a verbalized confidence score c. The confidence c is constrained within a prompted scale $\mathcal{S} = [l, u]$, where l and u denote the lower and upper bounds respectively, and the model is instructed to report an integer $c \in \{l, l{+}1, \ldots, u\}$. We let $a \in \{0, 1\}$ represent the correctness of $\hat{y}$ against the ground truth.

To enable fair comparison across scales of different ranges, all confidence scores are linearly normalized to the unit interval:

$$\hat{c} = \frac{c - l}{u - l} \tag{1}$$

All subsequent metrics are computed over $\hat{c} \in [0, 1]$. Our central research question is: *how does the metacognitive informativeness of $\hat{c}$, defined as its capacity to discriminate between $a{=}1$ and $a{=}0$, vary as a function of the scale design $\mathcal{S}$?*

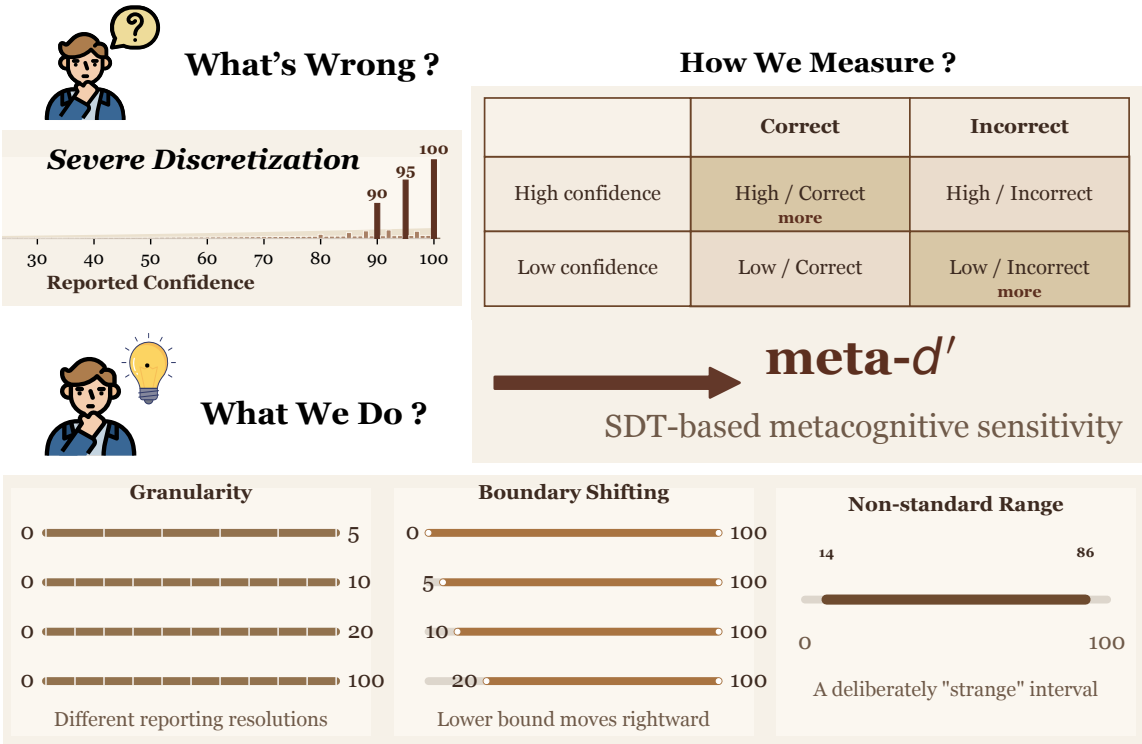

Figure 1: The overview of this paper.

3.2 Scale Design Dimensions

We manipulate $\mathcal{S}$ along three orthogonal dimensions, each targeting a distinct hypothesis about how scale properties interact with the model's confidence generation process.

Granularity ($\mathcal{G}$). We vary the number of discrete response categories available to the model across five levels: $\mathcal{S} \in \{[0,5],\ [0,10],\ [0,20],\ [0,50],\ [0,100]\}$. This dimension tests a fundamental trade-off: finer-grained scales offer higher theoretical resolution for expressing uncertainty, but may also amplify token-level biases by providing more opportunities to default to round-number anchors. Conversely, coarser scales force the model to commit to broader confidence bins, potentially reducing noise at the cost of resolution.

Boundary Shifting ($\mathcal{B}$). We fix the upper bound at u=100 and progressively raise the lower bound: $\mathcal{S} \in \{[0,100],\ [20,100],\ [40,100],\ [60,100]\}$. This probes anchoring effects (Tversky and Kahneman, 1974): when the available range is compressed from above, does the model redistribute its confidence to utilize the full new range, or does it remain clustered near the ceiling? A failure to redistribute would indicate that the model's high-confidence outputs are driven by token preference rather than genuine self-assessment.

Non-standard Ranges ($\mathcal{N}$). Our selection follows four principles: (i) all bounds avoid multiples of 5 and 10; (ii) we vary both lower and upper bounds to avoid relying on a single boundary configuration; (iii) we include ranges that contain prominent internal round anchors (e.g., 50, 70) alongside ranges that largely lack them, enabling us to test whether models gravitate toward these anchors regardless of scale boundaries; and (iv) we include a near-standard control to isolate the effect of boundary irregularity from range width. ***Concretely, we organize the conditions into two groups.*** The first group holds range width approximately constant ($\approx$70–73 units) while varying both bounds, isolating the effect of boundary placement:

$$[0,\ 73],\quad [14,\ 86],\quad [7,\ 79]$$

The second group varies the range width to test the robustness of our findings and introduces diagnostic contrasts:

$$[3,\ 38] \text{ (narrow; few internal round anchors)},$$
$$[0,\ 97]$$
$$\text{(near-standard; minimal pair with } [0,\ 100])$$

If a model instructed to report confidence in $[0,\ 73]$ still clusters at values such as 50 or 70, it indicates reliance on pre-trained numerical heuristics; if reports spread across the admissible range (e.g., 55,

68, 73), it suggests genuine semantic adaptation to the scale constraints. The narrow range [3, 38], which contains few salient round-number anchors, provides the strongest diagnostic test of this distinction.

3.3 Evaluation Metrics

We employ a complementary set of metrics to capture both calibration quality and metacognitive discrimination.

Expected Calibration Error (ECE). Following Guo et al. (2017), we partition the normalized confidence space $[0, 1]$ into B equal-width bins and compute:

$$\text{ECE} = \sum_{b=1}^{B} \frac{n_b}{N} \left|\text{acc}(b) - \text{conf}(b)\right| \tag{2}$$

where n_b is the number of samples in bin b, N is the total sample count, and $\text{acc}(b)$ and $\text{conf}(b)$ are the average accuracy and confidence within that bin. We set B=10 as the default and additionally report results with B=15 and adaptive binning in Appendix A, since the choice of B is particularly consequential when confidence distributions are heavily discretized.

AUROC. We report the Area Under the Receiver Operating Characteristic curve, which measures the model's ability to assign higher confidence to correct predictions than to incorrect ones (failure prediction). Unlike ECE, AUROC is threshold-free and thus less sensitive to discretization artifacts.

Metacognitive Sensitivity ($meta$-d'). To isolate the quality of the metacognitive signal from overall response bias, we adopt $meta$-d' from Signal Detection Theory (Maniscalco and Lau, 2012; Fleming and Lau, 2014). The intuition is as follows: in the Type-1 task, a model's ability to distinguish correct from incorrect answers is captured by d'. For the Type-2 (metacognitive) task, we ask: *how well does the model's confidence separate its own correct and incorrect responses?* To formalize this, we binarize $\hat{c}$ at a threshold t to obtain "high confidence" and "low confidence" judgments, then compute:

- *Type-2 Hit Rate*: $P(\hat{c} > t \mid a = 1)$, the proportion of correct responses assigned high confidence.
- *Type-2 False Alarm Rate*: $P(\hat{c} > t \mid a = 0)$, the proportion of incorrect responses assigned high confidence.

$meta$-d' is the d' value that would produce the observed Type-2 hit and false alarm rates under the assumption of an optimal (SDT-ideal) metacognitive observer (Maniscalco and Lau, 2012). A model with perfect metacognition would have $meta$-$d' = d'$; a model whose confidence carries no information about correctness would have $meta$-$d' = 0$. We further report the metacognitive efficiency ratio $M_{ratio} = meta\text{-}d'/d'$ (Fleming and Lau, 2014), which normalizes for differences in task difficulty across datasets: $M_{ratio} = 1$ indicates that the metacognitive system captures all available Type-1 information, while $M_{ratio} < 1$ indicates metacognitive loss. We use two alternative thresholds ($t = 0.9$ and $t = 0.95$ after normalization) and report results for both. To handle the prevalence of extreme confidence values (e.g., 100%), we apply the log-linear correction of adding 0.5 to all cells of the Type-2 contingency table (Hautus, 1995).

Distribution Diagnostics. To quantify discretization artifacts under different scale designs, we introduce two additional diagnostic metrics.

Round measures the proportion of confidence reports that fall on multiples of five (e.g., 0, 5, 10, ..., 100), capturing models' tendency to rely on round-number anchors.

Viol. measures the proportion of responses whose reported confidence lies outside the valid range $[l, u]$ by more than 5% of the scale width.

3.4 Experimental Setup

Models. We evaluate six LLMs spanning different training paradigms, model families, and scales:

- **Closed-source:** GPT-5.2 (OpenAI, 2025) and Gemini 3.1 Pro (Google DeepMind, 2025), representing the current frontier of commercial APIs from OpenAI and Google DeepMind respectively.
- **Open-weights (Meta):** LLaMA-4-Maverick (17B active / 400B total, 128 experts) and LLaMA-4-Scout (17B active / 109B total, 16 experts) (Meta AI, 2025), enabling within-family comparison across model scales under the same MoE architecture.

- **Open-weights (Alibaba):** Qwen3-235B-A22B-Instruct (22B active / 235B total) and Qwen3-30B-A3B-Instruct (3B active / 30B total) (Yang et al., 2025), broadening coverage to a non-Meta open-weights ecosystem and providing a second within-family scale comparison.

This selection enables three axes of comparison: closed vs. open-source, large vs. small scale, and across model families. We discuss the potential implications of this asymmetry in Section 5.

Datasets. We select three datasets that span distinct cognitive demands:

- **MMLU** (Hendrycks et al., 2020): 4-choice knowledge-intensive QA covering 57 subjects. We sample a balanced subset of 1,000 instances across difficulty levels.
- **GSM8K** (Cobbe et al., 2021): Multi-step mathematical reasoning. We use the full test set (N=1,319).
- **TruthfulQA** (Lin et al., 2022b): Probes the model's tendency to produce common misconceptions. We use the multiple-choice variant (N=817).

This selection is motivated by the need to test whether scale effects are stable across tasks that vary in difficulty, answer format, and the degree to which overconfidence is a known failure mode.

Prompting. We use a standardized zero-shot prompt template: *"Answer the following question. Then, provide your confidence as an integer between [l] and [u], where [l] means no confidence and [u] means absolute certainty."* The explicit anchoring of the endpoints with semantic labels ("no confidence" / "absolute certainty") is held constant across all scale conditions to isolate the effect of numerical range from verbal framing. Full prompt templates for each scale condition are provided in Appendix B.

Inference & Statistical Analysis. All inferences are performed with temperature T=0 for deterministic outputs. For each combination of model $\times$ dataset $\times$ scale condition, we collect the full set of available instances ($N \geq 800$). To assess the statistical reliability of differences in $meta\text{-}d'$ across scale conditions, we employ a nonparametric bootstrap procedure: we resample the response data 10,000 times with replacement and compute 95% confidence intervals for all metrics. Pairwise comparisons between scale conditions are evaluated via permutation tests (n=10,000), with Bonferroni correction for multiple comparisons.

4 Results

4.1 Confidence Discretization Under Standard Scales

We first characterize the distribution of verbalized confidence under the standard $[0, 100]$ scale (Table 1; distributions visualized in Figure 2). All six models exhibit severe discretization: rather than utilizing the 101 available integer states, models concentrate reports on a sparse set of round-number anchors.

Across models, a single confidence value dominates the distribution. Gemini 3.1 Pro reports exactly 100 on 68.4% of instances, GPT-5.2 and Qwen3-235B most frequently output 95, and the LLaMA-4 family concentrates on 90. The three most common values together account for more than 78% of responses for every model. Despite the nominal 101-state scale, models actually use only 15–28 distinct confidence values, leaving most of the scale unused.

Entropy further quantifies this compression. While a uniform distribution over 101 states would yield 6.66 bits, the observed entropy ranges from 0.95 bits (Gemini 3.1 Pro) to 1.88 bits (LLaMA-4-Maverick), indicating highly concentrated confidence distributions.

Baseline metacognitive efficiency (M_{ratio}) varies substantially across models, from 0.62 (Qwen3-30B) to 0.92 (GPT-5.2). A consistent pattern emerges: models with lower entropy (i.e., more concentrated confidence distributions) tend to exhibit lower M_{ratio}. We examine the causal direction of this relationship through controlled scale manipulation experiments in the following sections. AUROC values remain relatively high across models, indicating that even discretized confidence signals still preserve coarse ranking information between correct and incorrect predictions.

4.2 Effect of Scale Granularity

Table 2 reports the effect of scale granularity ($\mathcal{G}$) on metacognitive sensitivity ($meta\text{-}d'$) and efficiency (M_{ratio}). Task accuracy remains stable across granularity conditions ($\Delta < 1.5\%$ for all models), confirming that changes in $meta\text{-}d'$ reflect differences

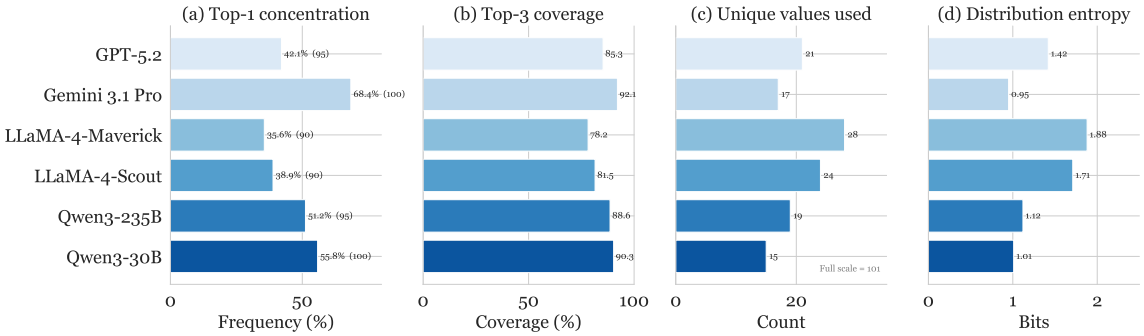

Figure 2: Baseline discretization profile under the standard $[0, 100]$ confidence scale. Across all six models, confidence reports are highly concentrated on a small set of round-number values. The most frequent value alone accounts for 35.6%–68.4% of responses, while the top three values cover 78.2%–92.1%. At the same time, models use only 15–28 distinct integers out of 101 possible values, revealing severe discretization of the verbalized confidence signal.

Table 1: Baseline discretization under the standard $[0, 100]$ scale, averaged across MMLU, GSM8K, and TruthfulQA. Models are ordered by M_{ratio} (descending). *Top-1*: most frequent confidence value (frequency in parentheses; bar proportional to frequency). *Top-3*: cumulative coverage of the three most common values. *Unique*: number of distinct confidence integers used out of 101 possible values. *H*: Shannon entropy in bits. *AUROC*: Area Under the ROC Curve for failure prediction. *For reference, a uniform distribution over 101 confidence levels would yield 6.66 bits.*

	Concentration		Distribution		Performance				
Model	Top-1	Top-3 (%)	Unique	H (bits)	Acc	AUROC	ECE ↓	$meta\text{-}d'$	M_{ratio}
GPT-5.2	95 (42.1%)	85.3	21	1.42	.81	.88	.08	1.84	**0.92**
LLaMA-4-Maverick	90 (35.6%)	78.2	28	1.88	.76	.84	.11	1.65	0.82
Qwen3-235B	95 (51.2%)	88.6	19	1.12	.79	.82	.13	1.51	0.78
LLaMA-4-Scout	90 (38.9%)	81.5	24	1.71	.72	.80	.13	1.52	0.76
Gemini 3.1 Pro	100 (68.4%)	92.1	17	0.95	.78	.79	.15	1.42	0.74
Qwen3-30B	100 (55.8%)	90.3	15	1.01	.68	.74	.17	1.22	0.62

in metacognitive signal quality rather than shifts in task difficulty.

Across all six models, we observe a consistent non-monotonic relationship between scale granularity and metacognitive performance. Performance peaks at the $[0, 20]$ scale and declines toward both extremes. At the coarse end, $[0, 5]$ yields the lowest $meta\text{-}d'$ for every model, indicating that five categories are insufficient to capture meaningful confidence variation. At the fine end, the standard $[0, 100]$ scale does not outperform $[0, 20]$ for any model; in fact, every model achieves significantly higher M_{ratio} at $[0, 20]$ than at $[0, 100]$ ($p < 0.05$). Intermediate scales follow the expected ordering, with $[0, 50]$ slightly below $[0, 20]$ and $[0, 10]$ between $[0, 5]$ and $[0, 20]$.

This pattern holds across both closed-source models (e.g., GPT-5.2: M_{ratio} 0.95 vs. 0.92) and open-weight models (e.g., LLaMA-4-Maverick: 0.89 vs. 0.82), suggesting that the $[0, 20]$ advantage is robust to architectural and training differences.

4.3 Effect of Boundary Shifting

Table 3 reports the results of the boundary shifting experiment ($\mathcal{B}$), where the upper bound is fixed at 100 while the lower bound is progressively increased. And two patterns need to be pay attention to:

First, moderate boundary shifts have minimal impact. Moving from $[0, 100]$ to $[20, 100]$ produces no significant change in $meta\text{-}d'$ or M_{ratio} for any model, and Utilization increases slightly for several models, suggesting that models can partially adapt to a mildly compressed range.

Second, aggressive boundary shifts lead to consistent degradation. In the $[40, 100]$ condition, M_{ratio} decreases for most models, and in the $[60, 100]$ condition the drop is universal and substantial (e.g., Qwen3-235B: $0.78 \rightarrow 0.55$; $p < 0.05$). The Utilization metric reveals the mechanism: as the lower bound increases, models fail to redistribute their confidence across the new range and instead cluster more tightly near the upper

Table 2: Effect of scale granularity ($\mathcal{G}$) on metacognitive sensitivity ($meta\text{-}d'$) and efficiency (M_{ratio}), averaged across datasets. Shaded cells indicate the best value per model; * denotes significant improvement over the $[0, 100]$ baseline ($p < 0.05$, permutation test with Bonferroni correction). Confidence values are normalized to $[0, 1]$ prior to metric computation.

	$meta\text{-}d'$ ↑					M_{ratio} ↑				
Model	[0,5]	[0,10]	[0,20]	[0,50]	[0,100]	[0,5]	[0,10]	[0,20]	[0,50]	[0,100]
GPT-5.2	1.68	1.75	**1.92***	1.80	1.84	0.84	0.90	**0.95***	0.91	0.92
Gemini 3.1 Pro	1.30	1.40	**1.52***	1.44	1.42	0.68	0.73	**0.79***	0.75	0.74
LLaMA-4-Maverick	1.41	1.55	**1.73***	1.60	1.65	0.78	0.85	**0.89***	0.81	0.82
LLaMA-4-Scout	1.28	1.40	**1.55***	1.42	1.52	0.71	0.78	**0.83***	0.77	0.76
Qwen3-235B	1.39	1.53	**1.62***	1.55	1.51	0.72	0.79	**0.84***	0.80	0.78
Qwen3-30B	1.08	1.20	**1.34***	1.24	1.22	0.55	0.61	**0.68***	0.63	0.62

Table 3: Effect of boundary shifting ($\mathcal{B}$) on metacognitive performance, averaged across datasets. *Util.*: percentage of the available range covered by the central 90% of reports (5th–95th percentile), reducing sensitivity to isolated outliers. Cell shading indicates direction of change relative to $[0, 100]$: improve, moderate†, severe† (†: $p < 0.05$, permutation test).

		Scale Condition			
Model	Metric	[0,100]	[20,100]	[40,100]	[60,100]
GPT-5.2	$meta\text{-}d'$	1.84	1.80	1.62	1.38
	M_{ratio}	0.92	0.90	0.81†	0.69†
	Util.	12.4	14.1	10.8	7.2
Gemini 3.1 Pro	$meta\text{-}d'$	1.42	1.45	1.28	1.12
	M_{ratio}	0.74	0.76	0.67	0.58†
	Util.	6.9	8.6	6.1	4.8
LLaMA-4 Maverick	$meta\text{-}d'$	1.65	1.61	1.48	1.25
	M_{ratio}	0.82	0.80	0.74†	0.63†
	Util.	10.5	11.8	8.9	5.6
LLaMA-4 Scout	$meta\text{-}d'$	1.52	1.49	1.35	1.18
	M_{ratio}	0.76	0.74	0.68†	0.59†
	Util.	9.2	10.1	7.5	4.9
Qwen3 235B	$meta\text{-}d'$	1.51	1.48	1.32	1.05
	M_{ratio}	0.78	0.76	0.68†	0.55†
	Util.	9.1	7.4	6.2	3.9
Qwen3 30B	$meta\text{-}d'$	1.22	1.18	1.02	0.85
	M_{ratio}	0.62	0.60	0.52†	0.43†
	Util.	7.8	6.5	4.8	3.1

bound. For example, under the $[60, 100]$ condition Qwen3-30B uses only 3.1% of the available range.

4.4 Semantic Robustness: Non-standard Scales

Tables 4 and 5 present results for the non-standard scale experiment ($\mathcal{N}$), designed to disentangle genuine scale comprehension from round-number heuristics.

Group 1: Fixed width, varying bounds. Under the three fixed-width conditions ($[0, 73]$, $[14, 86]$, $[7, 79]$; Table 4), Round (*round-number preference*) decreases relative to the baseline $[0, 100]$ scale but remains high. This indicates that irregular boundaries weaken but do not eliminate round-number clustering. The three Group 1 conditions produce nearly identical results (M_{ratio} within ± 0.01 across models), suggesting that the observed effects are driven by scale irregularity rather than the specific placement of bounds.

Group 2: Diagnostic contrasts. Table 5 reports results for two contrastive conditions. The narrow $[3, 38]$ scale produces the strongest disruption: violation rates increase substantially (e.g., up to 21.2% for Qwen3-30B), indicating that many responses fall outside the instructed range. Metacognitive efficiency also declines (M_{ratio} 0.40–0.72), while Round-Pref remains above 58% for all models, suggesting persistent preference for multiples of five even when few salient anchors exist.

The minimal pair $[0, 97]$ vs. $[0, 100]$ provides a targeted diagnostic. Despite a difference of only three units in the upper bound, M_{ratio} decreases for every model and Round drops slightly. This consistent shift suggests that the value "100" functions as a particularly strong confidence anchor.

These findings suggest that the discretization patterns observed under standard scales are not merely artifacts of specific numeric boundaries, but reflect persistent anchor-seeking behavior in verbalized confidence generation.

5 Discussion and Conclusion

Our experiments reveal three consistent patterns across six models and three datasets. First, scale granularity strongly influences metacognitive signal quality: the $[0, 20]$ scale consistently yields higher $meta\text{-}d'$ and M_{ratio} than the standard $[0, 100]$ scale. Second, models exhibit limited

Table 4: Diagnostics under fixed-width non-standard scales (Group 1, width ≈72–73), averaged across datasets. *Round*: reports on multiples of 5 within $[l, u]$. *Viol.*: responses outside valid range by >5% of width. Cell shading: reduced Round, meta. decline, elevated Viol., all relative to $[0, 100]$.

Model	Metric	Scale Condition			
		[0,100]	[0,73]	[14,86]	[7,79]
GPT-5.2	Round (%)	94.2	76.8	72.1	74.5
	Viol. (%)	0.0	1.8	2.4	2.1
	$meta\text{-}d'$	1.84	1.71	1.68	1.70
	M_{ratio}	0.92	0.85	0.84	0.85
Gemini 3.1	Round (%)	96.5	82.4	79.6	80.8
	Viol. (%)	0.0	4.1	5.2	4.5
	$meta\text{-}d'$	1.42	1.28	1.24	1.26
	M_{ratio}	0.74	0.67	0.65	0.66
LLaMA-4-M	Round (%)	88.7	71.2	68.5	69.8
	Viol. (%)	0.0	2.6	3.1	2.8
	$meta\text{-}d'$	1.65	1.52	1.49	1.50
	M_{ratio}	0.82	0.76	0.74	0.75
LLaMA-4-S	Round (%)	90.1	74.8	71.9	73.2
	Viol. (%)	0.0	3.5	4.2	3.8
	$meta\text{-}d'$	1.52	1.38	1.35	1.36
	M_{ratio}	0.76	0.69	0.68	0.68
Qwen3-235B	Round (%)	92.1	78.4	75.2	76.8
	Viol. (%)	0.0	3.2	4.0	3.5
	$meta\text{-}d'$	1.51	1.38	1.35	1.36
	M_{ratio}	0.78	0.71	0.70	0.70
Qwen3-30B	Round (%)	95.3	82.6	80.1	81.2
	Viol. (%)	0.0	5.8	6.5	6.1
	$meta\text{-}d'$	1.22	1.05	1.02	1.03
	M_{ratio}	0.62	0.53	0.52	0.52

Table 5: Diagnostics under contrastive non-standard scales (Group 2), averaged across datasets. $[3, 38]$: narrow range, few internal round anchors (stress test). $[0, 97]$: minimal pair with $[0, 100]$ (3-unit shift). Cell shading: reduced Round, mod. decline, severe decline, high Viol.

Model	Metric	Scale Condition		
		[0,100]	[3,38]	[0,97]
GPT-5.2	Round (%)	94.2	58.3	89.1
	Viol. (%)	0.0	8.6	0.5
	$meta\text{-}d'$	1.84	1.45	1.79
	M_{ratio}	0.92	0.72	0.90
Gemini 3.1	Round (%)	96.5	65.2	93.8
	Viol. (%)	0.0	18.3	0.8
	$meta\text{-}d'$	1.42	0.95	1.38
	M_{ratio}	0.74	0.50	0.72
LLaMA-4-M	Round (%)	88.7	59.4	85.3
	Viol. (%)	0.0	12.9	0.4
	$meta\text{-}d'$	1.65	1.28	1.61
	M_{ratio}	0.82	0.64	0.80
LLaMA-4-S	Round (%)	90.1	62.1	87.5
	Viol. (%)	0.0	15.4	0.6
	$meta\text{-}d'$	1.52	1.14	1.48
	M_{ratio}	0.76	0.57	0.74
Qwen3-235B	Round (%)	92.1	62.5	89.5
	Viol. (%)	0.0	14.8	0.6
	$meta\text{-}d'$	1.51	1.12	1.47
	M_{ratio}	0.78	0.58	0.76
Qwen3-30B	Round (%)	95.3	68.4	92.8
	Viol. (%)	0.0	21.2	1.2
	$meta\text{-}d'$	1.22	0.78	1.18
	M_{ratio}	0.62	0.40	0.60

adaptability to scale boundaries—moderate shifts are tolerated, but aggressive compression leads to systematic degradation as confidence reports cluster near ceiling values. Third, round-number preference is persistent and largely independent of scale design, with models favoring multiples of five even under irregular ranges.

These patterns suggest that verbalized confidence is produced through token-level selection rather than through a continuous internal estimate mapped onto a numerical scale. Under the $[0, 100]$ format, many high-frequency round-number tokens (e.g., 90, 95, 100) act as attractors during generation. Restricting the scale to $[0, 20]$ reduces the number of competing anchors while preserving sufficient resolution for coarse uncertainty discrimination. Boundary shifting fails for a similar reason: models treat numbers primarily as lexical tokens rather than as semantic bounds of a scale. This interpretation aligns with prior observations that token frequency distributions shape numeric outputs in language models (Zhao et al., 2021; Shaki et al., 2023).

Based on these findings, we recommend three practices when eliciting verbalized confidence from LLMs: ***(1) consider using a*** $[0, 20]$ ***scale as an alternative to the standard*** $[0, 100]$ ***format***, as this scale consistently yielded higher metacognitive efficiency than the standard $[0, 100]$ format across all models and tasks in our experiments; ***(2) report*** $meta\text{-}d'$ ***alongside ECE***, since ECE becomes unreliable under highly discretized confidence distributions; and ***(3) inspect empirical confidence distributions before interpreting calibration metrics***.

In conclusion, confidence scale design is often treated as a neutral reporting choice, yet it substantially affects the quality of verbalized uncertainty in LLMs. Our results show that simple changes to scale design can either improve or degrade the metacognitive signal, suggesting that confidence elicitation should be treated as a first-class experimental variable.

Ethics Statement

This work uses only publicly available benchmark datasets. All model outputs are generated through

standard API access or publicly released model weights. We do not anticipate direct negative societal impacts from this research. However, we note that our findings suggest that confidence scores are shaped by scale design rather than solely reflecting genuine model uncertainty. This has implications for deployed systems that present verbalized confidence to end users, since overconfidence driven by scale artifacts could lead to misplaced trust. We encourage practitioners to adopt our recommendations when designing confidence elicitation interfaces.

Limitations and Future Work

All experiments use greedy decoding (T=0); stochastic sampling may produce different confidence distributions. We use zero-shot prompting without Chain-of-Thought or self-reflection steps, so the interaction between prompting strategies and scale design remains unexplored. Our closed-source models (GPT-5.2, Gemini 3.1 Pro) have undisclosed architectures, while all open-weights models use Mixture-of-Experts architectures, introducing a potential confound between architecture and training paradigm. We evaluate on three datasets covering knowledge QA, mathematical reasoning, and misconception detection; generalization to open-ended generation tasks is not established. Finally, $meta\text{-}d'$ requires binarizing confidence at a threshold, and while we report results at two thresholds (t=0.9 and t=0.95), a continuous Type-2 ROC analysis could provide a more comprehensive characterization. The factorial interaction between prompting strategies and scale granularity is left to future work.

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A Sensitivity of ECE to Bin Count and Binning Strategy

A known limitation of Expected Calibration Error is its dependence on the number of bins B and the binning strategy (Nixon et al., 2019; Kumar et al., 2019). This sensitivity is particularly acute in our setting, where confidence distributions are heavily discretized—the majority of probability mass is concentrated on two or three values (e.g., 95 and 100 under the $[0, 100]$ scale). Under such distributions, most equal-width bins are empty or near-empty, and small changes in B can shift samples across bin boundaries, producing unstable ECE estimates.

A.1 Effect of B on ECE Estimates

Figure 3 shows how ECE varies as a function of $B \in \{5, 10, 15, 20, 30, 50\}$ for a representative model–dataset pair (GPT-5.2 on MMLU) under the standard $[0, 100]$ scale. ECE fluctuates noticeably across bin counts, with relative differences of up to approximately 13% between B=10 and B=20. This instability arises because the model's confidence reports are highly discretized and concentrated on a small set of values (e.g., 90, 95, and 100). After normalization to the $[0, 1]$ interval, most probability mass falls within a narrow region of the scale, causing bin membership to be highly sensitive to boundary placement. As a result, small changes in B can reassign a substantial number of observations across bins, producing noticeable variation in the estimated calibration error.

A.2 Equal-Width vs. Equal-Mass Binning

The standard ECE formulation uses *equal-width* bins, which partition $[0, 1]$ into B intervals of size $1/B$. Under discretized confidence, this produces a highly uneven distribution of samples across bins. An alternative is *equal-mass* (or *quantile*) binning, which assigns approximately N/B samples to each bin, ensuring that no bin is empty (Nixon et al., 2019).

Table 6 reports ECE under both strategies with B=10 for representative model–scale combinations on MMLU. We highlight two patterns. First, under the standard $[0, 100]$ scale, the discrepancy between equal-width and equal-mass ECE is substantial, reaching up to 0.037 absolute points (e.g., for LLaMA-4-Maverick). This confirms that binning artifacts can dominate the calibration estimate when confidence values are concentrated on a small set of anchors. Second, under the coarser $[0, 20]$ scale, the discrepancy shrinks considerably (typically below 0.01), indicating that the distribution of confidence values becomes more evenly spread across bins. Importantly, these differences arise despite identical model predictions and confidence reports, indicating that the observed variation is purely an artifact of the binning procedure. This result supports the interpretation that scale design directly shapes the empirical confidence distribution and, consequently, the stability of calibration metrics.

Table 6: Comparison of ECE under **Equal-Width** vs. **Equal-Mass** binning ($B = 10$) on MMLU. Large $|\Delta|$ indicates metrics driven by discretization artifacts.

Model	Scale	Equal-Width	Equal-Mass	$\lvert\Delta\rvert$
GPT-5.2	[0, 100]	0.082	0.051	0.031
	[0, 20]	0.054	0.048	0.006
LLaMA-4-Mav.	[0, 100]	0.115	0.078	0.037
	[0, 20]	0.082	0.075	0.007

A.3 Complete ECE Results Across Bin Counts

For completeness, Table 7 reports ECE with $B \in \{10, 15, 20\}$ for all experimental conditions (model $\times$ dataset $\times$ scale). Our main findings are robust to the choice of B: although absolute ECE values vary as the number of bins changes, the relative ordering of scale conditions remains stable across all tested bin counts. In particular, the $[0, 20]$ scale consistently yields the lowest ECE values, followed by $[0, 50]$, while the standard $[0, 100]$ scale produces the highest ECE across all settings.

This stability in ranking indicates that our conclusions about scale design are not driven by a specific choice of bin count. Instead, the differences across scales reflect systematic changes in the empirical confidence distribution. At the same time, the noticeable variation in absolute ECE values across B further illustrates the sensitivity of bin-based calibration metrics under discretized confidence distributions, reinforcing the motivation for using $meta\text{-}d'$ as a complementary, distribution-agnostic measure of metacognitive sensitivity.

A.4 Confidence Distribution Histograms

Figure 4, 5 visualizes the raw (pre-normalization) confidence distributions for each scale condition, aggregated across datasets. These histograms directly illustrate the discretization phenomenon discussed in Section 4 and motivate our use of

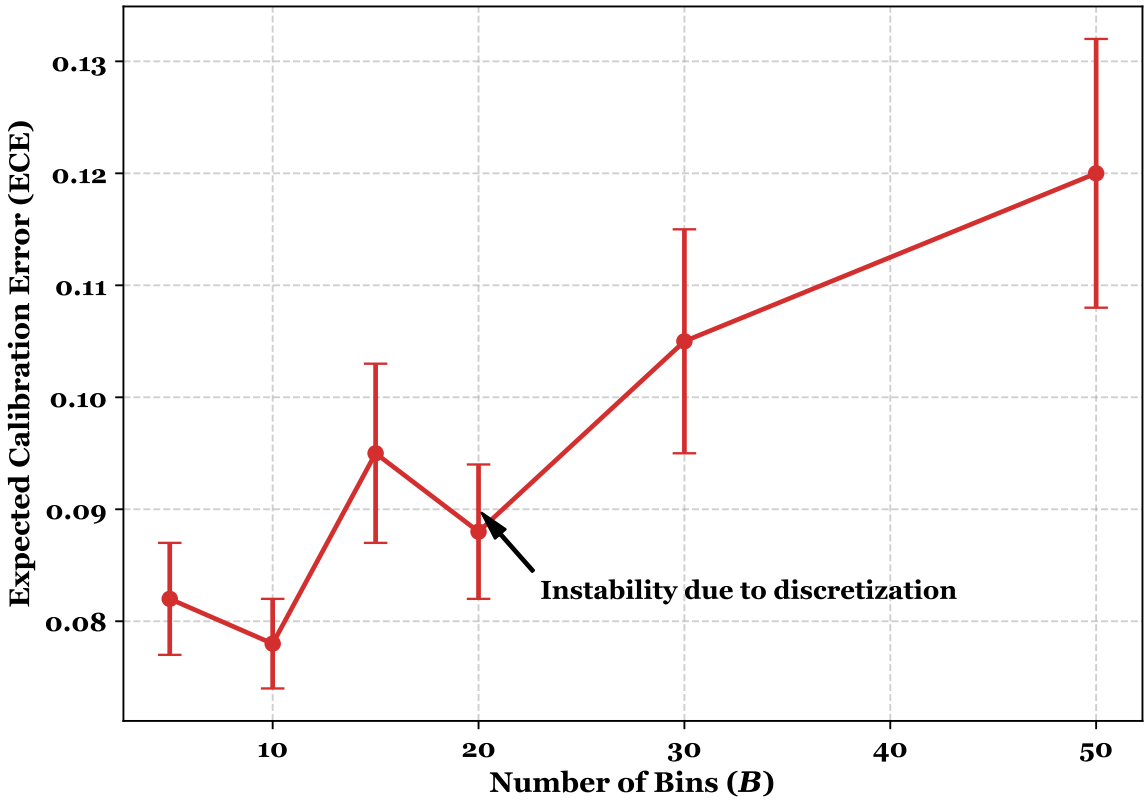

Figure 3: Sensitivity of Expected Calibration Error (ECE) to the number of bins B under discretized confidence distributions. When confidence values concentrate on a small set of anchors, small changes in B can shift observations across bin boundaries, producing unstable ECE estimates.

Table 7: ECE across experimental conditions with $B \in \{10, 15, 20\}$. Ranking of scales is stable ($[0, 20] < [0, 50] < [0, 100]$) across different B values.

	GPT-5.2 (MMLU)				LLaMA-4-Mav (MMLU)	
Scale	$B = 10$	$B = 15$	$B = 20$	$B = 10$	$B = 15$	$B = 20$
$[0, 20]$	**0.051**	**0.054**	**0.058**	**0.082**	**0.085**	**0.089**
$[0, 50]$	0.078	0.082	0.085	0.105	0.112	0.118
$[0, 100]$	0.082	0.095	0.102	0.115	0.132	0.145

meta-d′ as a distribution-agnostic alternative to ECE.

These visualizations serve three purposes: (1) they provide direct evidence of discretization as a function of scale design; (2) they explain *why* ECE estimates are unstable—when 80%+ of samples fall in a single bin, the metric is dominated by that bin's accuracy-confidence gap; and (3) they visually preview the key result that coarser and non-standard scales can reshape the confidence distribution in ways that are informative for analysis in the main text.

B Prompt Templates

All prompts follow a standardized two-part structure: a *task instruction* that presents the question and elicits an answer, followed by a *confidence instruction* that specifies the scale and requests a numerical self-assessment. The task instruction is held constant across all scale conditions; only the confidence instruction varies. This design isolates the effect of scale design from any confounds introduced by prompt wording.

B.1 General Template

```
[TASK INSTRUCTION]

Answer the following question.
{question}
Choices: {choices}
```

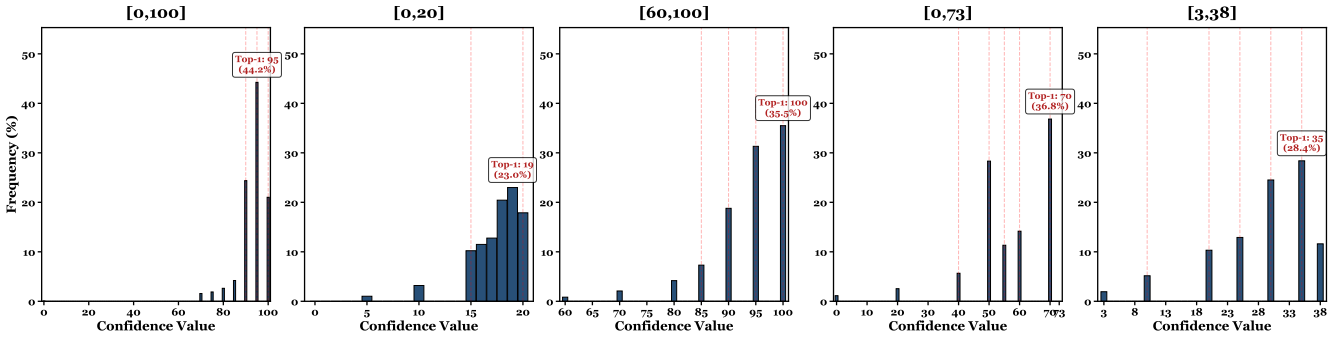

Figure 4: Distribution of raw confidence values across representative scale conditions for GPT-5.2, aggregated across datasets. Under the standard $[0, 100]$ scale, confidence reports concentrate on a small set of round-number anchors, whereas alternative scale designs produce qualitatively different distributional patterns. Dashed vertical lines indicate the most frequent round-number anchors within each range.

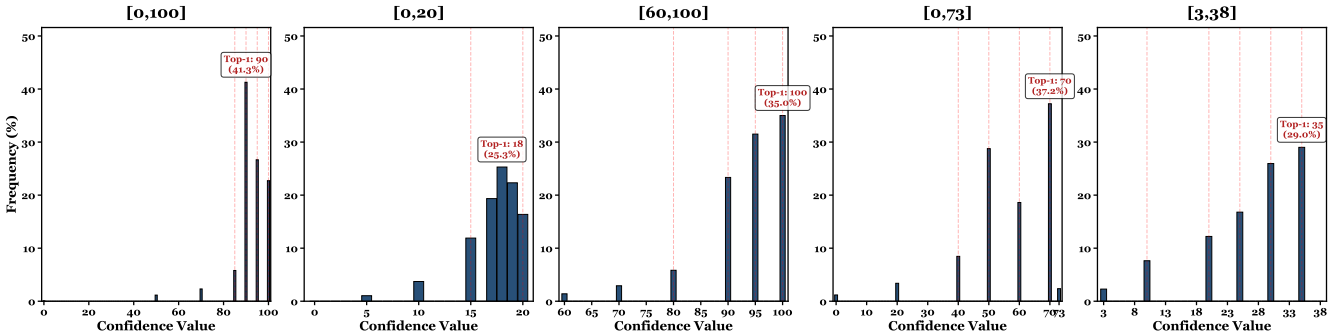

Figure 5: Distribution of raw confidence values across representative scale conditions for LLaMA-4-Maverick, aggregated across datasets. Similar to GPT-5.2, the standard $[0, 100]$ scale produces strong clustering on round-number anchors, while coarser, shifted, and non-standard scales alter the distributional pattern. Dashed vertical lines indicate the most frequent round-number anchors within each range.

```
[CONFIDENCE INSTRUCTION]
After providing your answer, rate your
confidence as an integer between {l} and
{u}, where {l} means no confidence at all
and {u} means absolute certainty.

[OUTPUT FORMAT]
Respond in the following format only:
Answer: <your answer>
Confidence: <integer between {l} and
{u}>
```

The explicit anchoring of the endpoints with semantic labels ("no confidence at all" / "absolute certainty") is held constant across all conditions. The strict output format minimizes post-processing ambiguity and discourages the model from hedging or elaborating on its confidence.

For GSM8K (free-form numerical answers), the task instruction is adapted as follows:

```
Solve the following math problem step by
step.
{question}

Respond in the following format only:
Solution: <your step-by-step solution>
Final Answer: <numerical answer>
Confidence: <integer between {l} and
{u}>
```

B.2 Scale-Specific Confidence Instructions

Below we list the exact confidence instruction for each scale condition. All other parts of the prompt remain identical.

B.2.1 Granularity Conditions ($\mathcal{G}$)

[0, 5]: `Rate your confidence as an integer between 0 and 5, where 0 means no confidence at all and 5 means absolute certainty.`

[0, 10]: `Rate your confidence as an integer between 0 and 10, where 0 means no confidence at all and 10 means absolute certainty.`

[0, 20]: `Rate your confidence as an integer between 0 and 20, where 0 means no confidence at all and 20 means absolute certainty.`

[0, 50]: `Rate your confidence as an integer between 0 and 50, where 0 means no confidence at all and 50 means absolute certainty.`

[0, 100]: `Rate your confidence as an integer between 0 and 100, where 0 means no confidence at all and 100 means absolute certainty.`

B.2.2 Boundary Shifting Conditions ($\mathcal{B}$)

[0, 100]: (Same as granularity baseline above.)

[20, 100]: `Rate your confidence as an integer between 20 and 100, where 20 means no confidence at all and 100 means absolute certainty.`

[40, 100]: `Rate your confidence as an integer between 40 and 100, where 40 means no confidence at all and 100 means absolute certainty.`

[60, 100]: `Rate your confidence as an integer between 60 and 100, where 60 means no confidence at all and 100 means absolute certainty.`

B.2.3 Non-standard Range Conditions ($\mathcal{N}$)

Group 1: Fixed width ($\approx$ 72–73 units), varying bounds.

[0, 73]: `Rate your confidence as an integer between 0 and 73, where 0 means no confidence at all and 73 means absolute certainty.`

[14, 86]: `Rate your confidence as an integer between 14 and 86, where 14 means no confidence at all and 86 means absolute certainty.`

[7, 79]: `Rate your confidence as an integer between 7 and 79, where 7 means no confidence at all and 79 means absolute certainty.`

Group 2: Varying width, diagnostic contrasts.

[3, 38]: `Rate your confidence as an integer between 3 and 38, where 3 means no confidence at all and 38 means absolute certainty.`

[0, 97]: `Rate your confidence as an integer between 0 and 97, where 0 means no confidence at all and 97 means absolute certainty.`

B.3 Design Rationale and Controls

Several design choices warrant explicit justification:

Semantic anchoring. Every confidence instruction anchors the lower bound to "no confidence at all" and the upper bound to "absolute certainty," regardless of the numerical values. This ensures that any observed differences across scale conditions are attributable to the numerical range itself, not to differences in verbal framing. Without this control, a model might interpret "20" in a [20, 100] scale as moderate confidence rather than as the minimum, confounding boundary shifting effects with semantic reinterpretation.

Integer constraint. We explicitly instruct the model to provide an integer. This prevents the model from reporting values like "95.5" or "around 90," which would introduce parsing ambiguity. In pilot experiments, omitting this constraint led to approximately 8% of responses containing non-integer or range-valued confidence reports (e.g., "85–90").

Output format enforcement. The strict `Answer: / Confidence:` format serves two purposes: (1) it enables reliable automated extraction of confidence values, and (2) it discourages the model from embedding caveats or qualifications that might implicitly modulate the confidence signal (e.g., "I'm fairly confident, so 85"). Responses that do not conform to the specified format are excluded from analysis. Violation rates for each scale condition are reported in Table 17.

No Chain-of-Thought for confidence. We deliberately do not prompt the model to "explain your confidence" or "think step by step about your certainty." While such prompts might improve calibration (Xiong et al., 2024; Tian et al., 2023), they would introduce an additional variable that interacts with scale design. Our goal is to measure the raw effect of scale manipulation on the default confidence signal; the interaction between prompting strategies and scale design is left for future work.

C Full Experimental Results

This appendix provides the complete experimental results underlying the analyses in Section 4. Main-text tables report averages across datasets and, for selected results, only representative subsets due to space constraints. Here we provide per-dataset baselines, per-dataset granularity breakdowns, full-model comparisons, and statistical confidence intervals.

C.1 Per-Dataset Baseline Statistics

Tables 8, 9, and 10 report the baseline discretization statistics from Section 4.1 separately for each dataset. This decomposition verifies that the severe confidence discretization observed in the averaged results is consistent across knowledge-intensive QA, mathematical reasoning, and misconception-probing tasks.

Table 8: Baseline discretization under $[0, 100]$ — **MMLU** (knowledge-intensive QA).

Model	Top-1	Top-3 (%)	Unique	H (bits)	Acc	ECE ↓	$meta\text{-}d'$	M_{ratio}
GPT-5.2	95	83.2	23	1.48	0.85	0.07	1.95	0.94
Gemini 3.1 Pro	100	91.5	18	0.98	0.82	0.14	1.48	0.75
LLaMA-4-Maverick	90	76.5	30	1.95	0.80	0.10	1.72	0.84
LLaMA-4-Scout	90	80.1	25	1.78	0.75	0.12	1.58	0.78
Qwen3-235B	95	87.2	20	1.15	0.83	0.12	1.58	0.79
Qwen3-30B	100	89.5	16	1.05	0.72	0.16	1.28	0.64

Table 9: Baseline discretization under $[0, 100]$ — **GSM8K** (mathematical reasoning).

Model	Top-1	Top-3 (%)	Unique	H (bits)	Acc	ECE ↓	$meta\text{-}d'$	M_{ratio}
GPT-5.2	95	85.8	19	1.35	0.78	0.09	1.75	0.90
Gemini 3.1 Pro	100	93.4	14	0.88	0.75	0.17	1.35	0.72
LLaMA-4-Maverick	90	80.2	24	1.75	0.72	0.12	1.55	0.80
LLaMA-4-Scout	90	83.4	22	1.62	0.68	0.14	1.45	0.74
Qwen3-235B	95	90.1	17	1.05	0.75	0.15	1.42	0.76
Qwen3-30B	100	92.5	13	0.92	0.62	0.19	1.15	0.60

C.2 Granularity: ECE and Per-Dataset Breakdown

Table 11 reports ECE across all granularity conditions, complementing the $meta\text{-}d'$ and M_{ratio} results in the main text. Table 12 provides the per-dataset M_{ratio} values to verify that the $[0, 20]$ advantage is stable across task types.

C.3 Task Accuracy Across Granularity Conditions

A critical assumption in Section 4.2 is that scale granularity does not affect task accuracy, ensuring that changes in $meta\text{-}d'$ reflect metacognitive signal quality rather than shifts in Type-1 performance. Table 13 reports accuracy across all granularity conditions.

C.4 Boundary Shifting: Complete Results

Table 14 provides the complete boundary-shifting results for all six models. It complements the main-text discussion by showing the strongest degradation under aggressive lower-bound compression.

C.5 Non-standard Scales: Complete Results

Table 15 summarizes representative non-standard scale comparisons for all models. These contrasts highlight the persistence of round-number preference and the rise in out-of-range violations under narrow or irregular ranges.

C.6 Bootstrap Confidence Intervals for Key Metrics

Table 16 reports 95% bootstrap confidence intervals (10,000 resamples) for the difference in $meta\text{-}d'$ across selected pairwise comparisons. These intervals provide direct statistical support for the key claims in the main text.

C.7 Out-of-Range Violation Analysis

Table 17 reports violation rates, defined as the percentage of responses whose reported confidence lies outside $[l, u]$ by more than 5% of the scale width, across all model $\times$ scale combinations. Standard scales generally produce near-zero violations, whereas narrow and irregular ranges substantially increase non-compliance.

Table 10: Baseline discretization under $[0, 100]$ — **TruthfulQA** (misconception probing).

Model	Top-1	Top-3 (%)	Unique	H (bits)	Acc	ECE ↓	$meta\text{-}d'$	M_{ratio}
GPT-5.2	95	81.5	20	1.38	0.74	0.10	1.68	0.90
Gemini 3.1 Pro	100	93.2	15	0.92	0.70	0.18	1.32	0.70
LLaMA-4-Maverick	90	78.4	26	1.82	0.71	0.13	1.58	0.81
LLaMA-4-Scout	90	82.3	23	1.65	0.65	0.15	1.45	0.75
Qwen3-235B	95	88.9	18	1.10	0.72	0.15	1.48	0.77
Qwen3-30B	100	91.2	14	0.98	0.58	0.21	1.10	0.58

Table 11: ECE (↓) across scale granularity conditions, averaged across datasets. * indicates significant improvement over the $[0, 100]$ baseline ($p < 0.05$).

Model	[0,5]	[0,10]	[0,20]	[0,50]	[0,100]
GPT-5.2	0.09	0.07	**0.05***	0.08	0.08
Gemini 3.1 Pro	0.16	0.14	**0.11***	0.13	0.15
LLaMA-4-Maverick	0.12	0.10	**0.08***	0.11	0.11
LLaMA-4-Scout	0.14	0.12	**0.10***	0.12	0.13
Qwen3-235B	0.15	0.13	**0.11***	0.13	0.13
Qwen3-30B	0.19	0.18	**0.15***	0.17	0.17

Table 12: M_{ratio} across granularity conditions, broken down by dataset. The $[0, 20]$ scale consistently achieves the highest or near-highest M_{ratio} across all models and datasets.

Dataset	Model	[0,5]	[0,10]	[0,20]	[0,50]	[0,100]
MMLU	GPT-5.2	0.86	0.92	**0.97**	0.93	0.94
	Gemini 3.1 Pro	0.69	0.75	**0.81**	0.76	0.75
	LLaMA-4-Maverick	0.80	0.87	**0.91**	0.83	0.84
	LLaMA-4-Scout	0.73	0.80	**0.85**	0.79	0.78
	Qwen3-235B	0.74	0.81	**0.86**	0.81	0.79
	Qwen3-30B	0.57	0.63	**0.70**	0.65	0.64
GSM8K	GPT-5.2	0.82	0.88	**0.93**	0.89	0.90
	Gemini 3.1 Pro	0.66	0.71	**0.77**	0.73	0.72
	LLaMA-4-Maverick	0.76	0.83	**0.87**	0.79	0.80
	LLaMA-4-Scout	0.69	0.76	**0.81**	0.75	0.74
	Qwen3-235B	0.71	0.78	**0.83**	0.78	0.76
	Qwen3-30B	0.54	0.60	**0.66**	0.61	0.60
TruthfulQA	GPT-5.2	0.82	0.88	**0.93**	0.89	0.90
	Gemini 3.1 Pro	0.64	0.70	**0.76**	0.72	0.70
	LLaMA-4-Maverick	0.77	0.84	**0.88**	0.80	0.81
	LLaMA-4-Scout	0.70	0.77	**0.82**	0.76	0.75
	Qwen3-235B	0.71	0.78	**0.83**	0.79	0.77
	Qwen3-30B	0.52	0.58	**0.65**	0.60	0.58

Table 13: Task accuracy across granularity conditions, averaged across datasets. The maximum within-model variation ($\Delta_{\max}$) is reported in the rightmost column. All models satisfy $\Delta_{\max} < 1.0\%$, confirming that granularity manipulation does not meaningfully alter task performance.

Model	[0,5]	[0,10]	[0,20]	[0,50]	[0,100]	$\Delta_{\max}$ (%)
GPT-5.2	0.812	0.809	0.815	0.811	0.810	0.6
Gemini 3.1 Pro	0.778	0.783	0.776	0.780	0.780	0.7
LLaMA-4-Maverick	0.762	0.758	0.766	0.761	0.760	0.8
LLaMA-4-Scout	0.724	0.719	0.726	0.722	0.720	0.7
Qwen3-235B	0.788	0.793	0.786	0.791	0.790	0.7
Qwen3-30B	0.675	0.684	0.679	0.681	0.680	0.9

Table 14: Boundary shifting ($\mathcal{B}$): selected complete results for all models, averaged across datasets. † indicates significant decrease from the $[0, 100]$ baseline ($p < 0.05$).

Model	Scale	$meta\text{-}d'$	M_{ratio}	ECE ↓	Utilization (%)
GPT-5.2	[0,100]	1.84	0.92	0.08	12.4
	[60,100]	1.38	0.69†	0.16	7.2
Gemini 3.1 Pro	[0,100]	1.42	0.74	0.15	6.9
	[60,100]	1.12	0.58†	0.19	4.8
LLaMA-4-Maverick	[0,100]	1.65	0.82	0.11	10.5
	[60,100]	1.25	0.63†	0.18	5.6
LLaMA-4-Scout	[0,100]	1.52	0.76	0.13	9.2
	[60,100]	1.18	0.59†	0.19	4.9
Qwen3-235B	[0,100]	1.51	0.78	0.13	9.1
	[60,100]	1.05	0.55†	0.21	3.9
Qwen3-30B	[0,100]	1.22	0.62	0.17	7.8
	[60,100]	0.85	0.43†	0.24	3.1

Table 15: Representative non-standard scale diagnostics ($\mathcal{N}$), averaged across datasets. *Round-Pref*: percentage of reports on multiples of 5 within $[l, u]$. *Violation*: out-of-range rate (greater than 5% of range width).

Model	Scale	Width	Round-Pref (%)	Violation (%)	$meta\text{-}d'$	M_{ratio}	H
GPT-5.2	[0,100] (baseline)	100	94.2	0.0	1.84	0.92	1.42
	[3,38]	35	58.3	8.6	1.45	0.72	1.76
Gemini 3.1 Pro	[0,100] (baseline)	100	96.5	0.0	1.42	0.74	0.95
	[3,38]	35	65.2	18.3	0.95	0.50	1.21
LLaMA-4-Maverick	[0,100] (baseline)	100	88.7	0.0	1.65	0.82	1.88
	[3,38]	35	59.4	12.9	1.28	0.64	2.08
LLaMA-4-Scout	[0,100] (baseline)	100	90.1	0.0	1.52	0.76	1.71
	[3,38]	35	62.1	15.4	1.14	0.57	1.95
Qwen3-235B	[0,100] (baseline)	100	92.1	0.0	1.51	0.78	1.12
	[3,38]	35	62.5	14.8	1.12	0.58	1.42
Qwen3-30B	[0,100] (baseline)	100	95.3	0.0	1.22	0.62	1.01
	[3,38]	35	68.4	21.2	0.78	0.40	1.30

Table 16: 95% bootstrap confidence intervals for the difference in $meta\text{-}d'$ (Δ) across selected pairwise scale comparisons. Positive Δ indicates that the first condition outperforms the second. Intervals that do not contain zero indicate a statistically reliable difference at $\alpha = 0.05$.

Model	Comparison (A vs. B)	$meta\text{-}d'$ (A)	$meta\text{-}d'$ (B)	Δ [95% CI]
GPT-5.2	[0,20] vs [0,100]	1.92	1.84	+0.08 [0.03, 0.14]
	[0,100] vs [60,100]	1.84	1.38	+0.46 [0.38, 0.55]
	[0,100] vs [0,73]	1.84	1.71	+0.13 [0.06, 0.21]
LLaMA-4-Maverick	[0,20] vs [0,100]	1.73	1.65	+0.08 [0.02, 0.15]
	[0,100] vs [60,100]	1.65	1.25	+0.40 [0.31, 0.49]
	[0,100] vs [3,38]	1.65	1.28	+0.37 [0.28, 0.47]
Qwen3-30B	[0,20] vs [0,100]	1.34	1.22	+0.12 [0.05, 0.19]
	[0,100] vs [60,100]	1.22	0.85	+0.37 [0.29, 0.46]
	[0,100] vs [3,38]	1.22	0.78	+0.44 [0.35, 0.54]

Table 17: Out-of-range violation rates (%) across all scale conditions. Standard scales ($\mathcal{G}$ and $\mathcal{B}$) generally produce near-zero violations, whereas non-standard scales, particularly narrow ranges, produce substantially higher rates.

	Granularity ($\mathcal{G}$)					Boundary ($\mathcal{B}$)			Non-standard ($\mathcal{N}$)				
Model	[0,5]	[0,10]	[0,20]	[0,50]	[0,100]	[20,100]	[40,100]	[60,100]	[0,73]	[14,86]	[7,79]	[3,38]	[0,97]
GPT-5.2	0.0	0.0	0.0	0.1	0.0	0.2	0.5	0.8	1.8	2.4	2.1	8.6	0.5
Gemini 3.1 Pro	0.1	0.0	0.1	0.2	0.0	0.5	1.2	2.4	4.1	5.2	4.5	18.3	0.8
LLaMA-4-Maverick	0.0	0.0	0.1	0.2	0.0	0.3	0.6	1.1	2.6	3.1	2.8	12.9	0.4
LLaMA-4-Scout	0.2	0.1	0.2	0.4	0.0	0.6	1.5	2.8	3.5	4.2	3.8	15.4	0.6
Qwen3-235B	0.1	0.1	0.2	0.5	0.0	0.8	1.8	3.5	3.2	4.0	3.5	14.8	0.6
Qwen3-30B	0.5	0.4	0.8	1.2	0.1	1.5	3.2	5.8	5.8	6.5	6.1	21.2	1.2