Skim and Skip: Hierarchical Adaptive Inference for Efficient Multimodal Retrieval

Abstract

Universal multimodal retrieval (UMR) increasingly adopts multimodal large language models (MLLMs) as unified embedding backbones, but their strong retrieval performance comes at substantial inference cost. Existing methods typically rely on uniformly dense inference, where all input tokens are processed through the entire model and matched using the final-layer [EOS] representation. However, this paradigm overlooks two key forms of heterogeneity in multimodal retrieval: token contributions to the final retrieval embedding are highly uneven, and different queries require markedly different amounts of inference depth. To address this, we propose **Skim and Skip (SAS)**, a hierarchical adaptive inference framework for efficient multimodal retrieval. SAS first performs token-level evidence selection to preserve only the input information most relevant to the final retrieval embedding, and then performs depth-adaptive inference to determine whether the current representation is already sufficient for reliable matching. Experiments on 12 MMEB retrieval tasks show that SAS retains around 99% of the original retrieval performance while achieving up to **1.64×** end-to-end speedup and nearly **3×** FLOPs reduction.

1 Introduction

Multimodal large language models (MLLMs) are increasingly used as unified backbones for multimodal retrieval (Jiang et al., 2024b; Zhang et al., 2025b; He et al., 2026). Benefiting from large-scale cross-modal pretraining, MLLM-based retrievers have achieved strong performance across zero-shot, fine-grained, and universal retrieval settings (Liu et al., 2024; Jiang et al., 2024b; He et al., 2026; Li et al., 2026; Huang et al., 2026a). However, this performance comes at substantial inference cost, as existing methods typically process every query with all tokens through the full depth of the model (Lyu et al., 2025; Xiao et al., 2026).

Figure 1: **Motivation of Skim and Skip (SAS).** Conventional MLLM retrieval applies uniformly dense inference to all tokens across all layers, resulting in high latency. In contrast, SAS performs hierarchical adaptive inference: it first filters retrieval-relevant information (*Skim*) and then allocates depth based on representation maturity (*Skip*), allowing easy queries to exit early while reserving deeper computation for harder ones.

The high inference cost primarily arises from two core computational factors: input information width and information processing depth. First, multimodal inputs—comprising visual and textual tokens—are long and processed uniformly, despite being inherently uneven, redundant, and noisy, which degrades the quality of the final retrieval embedding. Second, different queries require varying levels of reasoning depth, yet existing approaches often apply a fixed processing budget. Therefore, efficient retrieval hinges on two tightly coupled questions: which portions of the input are truly informative for constructing the representation, and how much computation is necessary for that representation to become sufficiently reliable.

Existing acceleration methods typically address these two issues in isolation. Token reduction methods focus on compressing the input sequence (Yang

et al., 2024; Chen et al., 2024; Li et al., 2026; Wu et al., 2026; Deniz et al., 2025; He and Chen, 2026), while depth reduction methods focus on executing fewer layers (Lyu et al., 2025; Yoo et al., 2026; Huang et al., 2026b; Yang et al., 2026). On the one hand, standard pruning strategies developed for multimodal tasks such as VQA are poorly suited to retrieval. Existing token reduction methods for visual and textual inputs largely overlook the critical role of the EOS embedding, which serves as the final representation in retrieval, leading to severe performance degradation even at low compression ratios. Moreover, naive depth reduction also harms performance: while easy queries already achieve 55.0% Hit@1 at intermediate layer 22, hard queries reach only 7.2% on MSCOCO, indicating substantial variability in required reasoning depth. On the other hand, jointly learning what information to preserve and when the current representation is sufficient for retrieval is inherently challenging, as it deviates from standard training with full-token supervision.

Motivated by this view, we propose **Skim and Skip (SAS)**, a hierarchical adaptive inference framework for efficient multimodal retrieval. SAS consists of two stages. **Skim** performs [EOS]-centric cross-modal information selection, preserving only the input information most relevant to the final retrieval embedding. **Skip** performs adaptive depth allocation, deciding whether the current representation is already mature enough for reliable retrieval. To motivate this design, we revisit the assumptions behind uniformly dense inference in Section 2, and then present SAS in Section 3.

Our main contributions are as follows:

• We identify two key forms of heterogeneity overlooked by uniform dense inference in MLLM retrieval: uneven token contributions to the final retrieval representation, and varying depth requirements across queries.

• We propose **Skim and Skip (SAS)**, a hierarchical adaptive inference framework that unifies [EOS]-centric cross-modal information selection and adaptive depth allocation for multimodal retrieval.

• We evaluate SAS on 12 multimodal retrieval benchmarks spanning five task types. SAS retains 99% of the dense model's retrieval performance while achieving up to 1.64× end-to-end speedup and nearly 3× FLOPs reduction.

Top-k	Shallow (L0)	Middle (L14)	Deep (L27)
Top-10	69.6%	**77.8%**	58.3%
Top-20	86.3%	**87.9%**	75.1%

Table 1: Average [EOS] attention on 11 MMEB tasks.

Drop Ratio	CIRR	FashionIQ	NIGHTS	OVEN
0%	0.572	0.197	0.685	0.645
10%	0.591	0.204	0.659	0.647
20%	0.577	0.191	0.667	0.648
30%	0.586	0.194	0.660	0.633

Table 2: Negligible impact of random drops.

2 Revisiting Uniform Dense Inference in MLLM Retrieval

In MLLM-based retrieval, most approaches follow a uniformly dense inference paradigm, processing every query with the full set of input tokens through the entire model. While effective, this design implicitly assumes that all input information warrants equal computation and that all queries require the same amount of reasoning depth. To revisit this paradigm, we study it from two perspectives: whether all tokens contribute equally to the final [EOS] retrieval embedding, and whether all queries require the same inference depth before a reliable retrieval representation is formed.

2.1 Are All Tokens Equally Informative?

We first examine how the [EOS] token aggregates retrieval evidence. Specifically, we analyze the attention from [EOS] to all input tokens across layers of VLM2Vec-V2.0. As shown in Table 1, at the middle layer (L14), where cross-modal interaction is strongest, the top-10 tokens capture 77.8% of the total [EOS] attention mass and the top-20 capture 87.9%. These results suggest that the final [EOS] embedding is driven primarily by a small subset of tokens, while the majority contribute little.

This view is reinforced by random token removal experiments. We randomly drop different proportions of tokens across multiple retrieval tasks (Table 2) and find that performance remains largely stable under 10–30% pruning, with slight gains on some tasks. This suggests that retrieval evidence is inherently sparse, some tokens may even introduce distracting or irrelevant signals. Efficient retrieval inference should therefore identify the information that materially contributes to the final [EOS] retrieval embedding and preserve only that evidence

(a) Per-layer retrieval performance across five tasks.

(b) Easy/Medium/Hard stratification (MSCOCO t→i).

Figure 2: Evidence against uniform depth allocation.

for subsequent reasoning.

Importantly, this token selection problem cannot be reduced to a modality-specific heuristic. Token composition varies substantially across tasks. Such variability makes fixed modality-dependent rules brittle. Instead, retrieval-oriented token selection should rely on a unified cross-modal criterion that directly measures a token's relevance to the final [EOS] representation.

2.2 Do All Queries Require the Same Inference Depth?

We next examine whether all queries require the same inference depth. Layer-wise probing on VLM2Vec-V2.0 shows that retrieval signals do not emerge only at the final layer, but develop progressively in intermediate and late layers (Figure 2a). For example, on VisDial, the model already reaches 50.9% Hit@1 at layer 22, compared to 82.1% at the final layer, indicating that intermediate layers already encode substantial retrieval-relevant semantics before full-depth inference is completed.

However, the benefit of deeper computation is far from uniform across queries. To examine this heterogeneity, we partition queries into Easy, Medium, and Hard groups according to the final-layer Top-1/Top-2 similarity margin, and compare their layer-wise retrieval performance (Figure 2b). On MSCOCO text-to-image retrieval, Easy queries already achieve 55.0% Hit@1 at layer 22, whereas Hard queries reach only 7.2%. This disparity shows that retrieval representations mature at very different rates across samples.

At the same time, the presence of useful intermediate-layer signals does not by itself yield a practical adaptive-depth mechanism. Standard retrieval backbones are supervised only at the fi-

nal layer, so intermediate representations, although informative, are not explicitly trained to function as standalone retrieval embeddings. Converting this latent depth redundancy into real inference savings therefore requires two steps: first, activating retrieval capability at a target intermediate layer through additional supervision; and second, deciding whether inference can terminate there based on the maturity of the current representation.

3 Methodology

The analysis in Section 2 shows that efficient multimodal retrieval requires two coupled decisions: what information to preserve and how much computation to allocate. Motivated by this view, we propose **Skim and Skip (SAS)**, a hierarchical adaptive inference framework for multimodal retrieval. For each query, SAS first applies **Skim** to retain the input information most relevant to the final [EOS] retrieval embedding, and then applies **Skip** to determine whether the current representation is already mature enough for early termination. Accordingly, Skim addresses *information selection*, while Skip addresses *depth allocation*.

3.1 Skim: [EOS]-centric Cross-modal Information Selection

The goal of **Skim** is to retain only the input information that materially contributes to the final [EOS] retrieval embedding, so that subsequent computation is concentrated on informative tokens. Because visual and textual token composition varies substantially across retrieval tasks, token selection must be defined under a unified cross-modal criterion. Rather than relying on local saliency or heuristic thresholds, Skim measures token importance by the

Figure 3: **Overview of SAS.** SAS treats retrieval inference as progressive evidence accumulation. **Left: Token-level evidence selection.** At the skim layer l_s, the Influence-Aware Filter estimates each token's marginal influence on the [EOS] embedding and removes low-contribution tokens, preserving only evidence-bearing information. **Right: Layer-level evidence sufficiency.** At the decision layer l_d, a learned sufficiency classifier determines whether the accumulated evidence is adequate for reliable retrieval; sufficiently mature queries exit early, while the rest continue to deeper layers.

perturbation that removing a token would induce on the [EOS] representation.

In practice, we first apply pooling to the ViT-encoded visual tokens to shorten the initial visual sequence before it is fed into the LLM. We then perform cross-modal token selection at layer l_s.

Local Perturbation of Token Removal. Consider attention head h at layer l. Let $o_{l,h}(e)$ denote the attention output at the [EOS] position, and let $\alpha_{l,h}(e \to j)$ denote the attention weight from [EOS] to token j. The output at [EOS] is

$$o_{l,h}(e) = \sum_i \alpha_{l,h}(e \to i)\, v_{l,h,i}, \qquad (1)$$

where $v_{l,h,i}$ is the value vector of token i.

If token j is removed, the attention weights over the remaining tokens are re-normalized, perturbing the head output at [EOS]. The resulting exact perturbation is

$$\Delta o_{l,h}(e) = \frac{\alpha_{l,h}(e \to j)}{1 - \alpha_{l,h}(e \to j)}\Big(o_{l,h}(e) - v_{l,h,j}\Big). \qquad (2)$$

This expression captures the immediate effect of token removal on the [EOS] representation at the current layer. Importantly, the perturbation depends

not only on the attention mass assigned to token j, but also on the discrepancy between its value vector and the aggregated head output. Attention alone is therefore insufficient to characterize a token's retrieval contribution.

A Computable Upper Bound on Token Influence. The local perturbation first affects a single attention head and then propagates through the output projection $W_O^{l,h}$ to subsequent layers. To quantify its downstream impact, we consider the magnitude of the projected perturbation, $\|W_O^{l,h}\Delta o_{l,h}(e)\|_2$.

Computing this quantity exactly during inference is inefficient. Instead, we upper-bound it using the spectral norm $\sigma_O^{l,h}$ of $W_O^{l,h}$:

$$\|W_O^{l,h}\Delta o_{l,h}(e)\|_2 \leq \sigma_O^{l,h} \frac{\alpha_j}{1 - \alpha_j}$$
$$\times \Big(\|o_{l,h}(e)\|_2 + \|v_{l,h,j}\|_2\Big), \qquad (3)$$

where α_j abbreviates $\alpha_{l,h}(e \to j)$.

To obtain an inference-time computable score, we further bound $\|o_{l,h}(e)\|_2$ and $\|v_{l,h,j}\|_2$ using the spectral norm $\sigma_V^{l,h}$ of the value projection $W_V^{l,h}$ and its bias term $\mathbf{b}_V^{l,h}$. Aggregating the resulting bound over all H heads yields the following influence

score for token j at layer l:

$$\psi_l(j) = \sum_{h=1}^{H} \sigma_O^{l,h} \frac{\alpha_j}{1-\alpha_j} \cdot \left[\sigma_V^{l,h}\big(S_{l,h} + \|\mathbf{h}_l[j]\|_2\big) + 2\|\mathbf{b}_V^{l,h}\|_2 \right], \tag{4}$$

where

$$S_{l,h} := \sum_i \alpha_{l,h}(e \to i)\, \|\mathbf{h}_l[i]\|_2, \tag{5}$$

and $\mathbf{h}_l[j]$ is the input hidden state of token j at layer l. The full derivation is provided in Appendix B.

This score can be interpreted as a computable upper bound on the perturbation that removing token j may induce on the subsequent evolution of the [EOS] representation. A larger score indicates greater importance to the final retrieval embedding, while a smaller score suggests that the token can be removed with limited effect.

Unified Cross-modal Selection. At skim layer l_s, we rank all tokens by their influence scores and remove those with the lowest values, preserving the tokens most important to the final [EOS] retrieval embedding. Because the score is defined directly by a token's effect on [EOS], visual and textual tokens can be ranked under the same criterion.

Moreover, the influence score is computed from attention weights and hidden states that are already available in the forward pass, introducing negligible overhead.

3.2 Skip: Adaptive Depth Allocation by Representation Maturity

The goal of **Skip** is to determine whether the current depth is already sufficient for reliable retrieval and to allocate additional computation only when necessary. This is non-trivial because standard retrieval backbones are supervised only on the final-layer [EOS] embedding. As a result, intermediate layers may already contain retrieval signals, but are not explicitly trained to serve as standalone retrieval embeddings.

To address this, Skip adopts a two-stage training paradigm: we first activate retrieval capability at the target decision layer, and then train a lightweight assessor to decide whether inference can stop there.

Stage I: Activating Intermediate Retrieval Capability. To equip the target layer l_d with standalone retrieval capability, we supervise its representation

with both feature-level distillation and contrastive learning. Intuitively, this stage encourages the intermediate embedding to both align with the final-layer semantic space and remain discriminative for retrieval.

Specifically, we treat the final-layer embedding $e^{(L)}$ as the teacher and the embedding at layer l_d, denoted by $e^{(l_d)}$, as the student. We first align them using mean squared error:

$$\mathcal{L}_{distill} = \mathbb{E}_{(q,c)\sim\mathcal{D}} \left[\|e_q^{(L)} - e_q^{(l_d)}\|_2^2 + \|e_c^{(L)} - e_c^{(l_d)}\|_2^2 \right]. \tag{6}$$

This term reduces the distribution gap between intermediate and final representations.

To ensure retrieval discriminability, we further apply InfoNCE supervision (Oord et al., 2018) to the intermediate embedding:

$$\mathcal{L}_{con}^{(l_d)} = -\frac{1}{N} \sum_{i=1}^{N} \log \frac{\exp(\text{sim}(e_{q_i}^{(l_d)}, e_{c_i}^{(l_d)})/\tau)}{\sum_{j=1}^{N} \exp(\text{sim}(e_{q_i}^{(l_d)}, e_{c_j}^{(l_d)})/\tau)}, \tag{7}$$

where $\text{sim}(\cdot, \cdot)$ denotes cosine similarity and τ is a temperature parameter.

We combine the two objectives with a dynamic weight:

$$\mathcal{L}_{inter}(t) = \lambda(t)\mathcal{L}_{con}^{(l_d)} + (1 - \lambda(t))\mathcal{L}_{distill}, \tag{8}$$

where $\lambda(t)$ increases monotonically during training. Early training emphasizes semantic alignment, while later training shifts toward retrieval discriminability.

To preserve final-layer performance, we retain the standard contrastive objective at layer L. The overall Stage-I loss is

$$\mathcal{L}_{\text{StageI}} = \mathcal{L}_{con}^{(L)} + \gamma \mathcal{L}_{inter}(t), \tag{9}$$

where γ controls the strength of the intermediate supervision. After this stage, layer l_d is explicitly trained as a usable retrieval representation, rather than remaining only a latent carrier of retrieval signals.

Stage II: Learning a Depth Sufficiency Assessor. Once the intermediate representation at layer l_d becomes sufficiently mature, we train a depth assessor to determine whether it is already sufficient for reliable retrieval. In this stage, the backbone is frozen and only a lightweight decision module is optimized.

The assessor does not predict the retrieval result itself. Instead, it predicts whether the current representation has accumulated enough evidence for

Model	Avg. (Ret.)	Time ↓	FLOPs ↓	Speedup ↑	Exit Rate ↑	Vis. Tok. ↓	Txt. Tok. ↓
Qwen2.5-VL-3B + CL	68.9 (100%)	678.4s	100%	1.00×	0%	100%	100%
Qwen2.5-VL-3B + SAS	**68.0 (99%)**	**471.3s** ↓30.5%	**36.6%** ↓63.4%	**1.44×**	**20%** ↑20%	**25%** ↓75%	**50%** ↓50%
Qwen2.5-VL-7B + CL	71.7 (100%)	1058.0s	100%	1.00×	0%	100%	100%
Qwen2.5-VL-7B + SAS	**70.9 (99%)**	**644.2s** ↓39.1%	**33.7%** ↓66.3%	**1.64×**	**26%** ↑26%	**25%** ↓75%	**50%** ↓50%

Table 3: Efficiency analysis of Qwen2.5-VL-3B/7B with standard contrastive learning (CL) and their SAS-accelerated counterparts. Avg. (Ret.) reports the mean Hit@1 and the corresponding performance retention rate relative to the CL baseline. Exit Rate indicates the proportion of early-exited samples, while Vis./Txt. Tok. denote the ratios of retained visual and textual tokens after skimming.

reliable matching, or whether deeper refinement is still needed. We formulate this as a binary classification problem over whether the sample should terminate at layer l_d.

The assessor uses three types of features. First, *uncertainty scalars*, including the Top-1 similarity score and the Top-1/Top-2 similarity margin from intermediate retrieval results, capture ranking confidence. Second, *modality indicators* distinguish text, image, and multimodal inputs, allowing the classifier to adapt to task-dependent distribution shifts. Third, *semantic features* are obtained by projecting the intermediate `[EOS]` representation to encode the current semantic context. Full architectural and training details are provided in Appendix C.

4 Experiment

Implementation Details. We instantiate SAS on top of Qwen2.5-VL-Instruct (3B and 7B) (Bai et al., 2025), and additionally evaluate its generality on the LLaVA-style training architecture (Liu et al., 2023). Stage I is conducted on 8 NVIDIA H100 GPUs with LoRA (Hu et al., 2022) ($r = 16$) for parameter-efficient fine-tuning. We train on the retrieval subset of MMEB (Jiang et al., 2024b) for 5,000 steps with a learning rate of 5×10^{-5}, a global batch size of 1,024, and a contrastive temperature of $\tau = 0.02$. Stage II is performed on a single NVIDIA A100 GPU, where we freeze the backbone and train the termination classifier for 1,000 steps using Focal Loss (Lin et al., 2017) with $\alpha = 0.8$ and $\gamma = 3.0$, a learning rate of 5×10^{-4}, and a batch size of 512. $\lambda(t)$ is initialized at 0 and annealed to 1.0 with a cosine schedule, gradually shifting the objective from distillation-based alignment to contrastive discrimination. We apply Vision Pooling at layer 1, Influence-Aware Token Filtering at layer 10 (l_s), and place adaptive depth allocation at layer 12 (l_d). For text tokens, we prune 50% of the sequence while preserving a 16-token guardrail.

Evaluation. We evaluate SAS on the retrieval split of MMEB, covering 12 benchmarks from five representative multimodal retrieval task types. Following standard practice, we report Hit@1 as the accuracy metric and measure end-to-end inference latency on a single NVIDIA A100 GPU.

5 Main Results

We analyze the results from two perspectives: (1) efficiency relative to our reproduced dense models, and (2) retrieval performance compared with representative baselines.

5.1 Efficiency Comparison

To isolate the effect of SAS, we train dense 3B and 7B baselines under the same setting but without any adaptive acceleration, and use them as strict references for efficiency–accuracy comparison.

Efficiency–Accuracy Trade-off. As shown in Table 3, SAS substantially reduces computation while preserving retrieval quality. Compared with the dense models, SAS retains nearly 99% of the original performance (e.g., 71.7% → 70.9% for 7B, and 68.9% → 68.0% for 3B), while reducing FLOPs by nearly **3×**. This supports our claim that a considerable portion of token- and depth-level computation in dense MLLM retrieval is redundant and can be removed adaptively.

Revisiting the Parameter–Latency Trade-off. A notable finding is that the SAS-accelerated 7B model is even faster than the dense 3B model in end-to-end latency. In addition to outperforming the dense 3B model by about 2.0% in retrieval accuracy, the accelerated 7B model also achieves lower inference time. We attribute this to stronger representation quality in the larger model, which enables more reliable identification of easy queries and therefore more frequent early termination at l_d. This result suggests that, under adaptive inference, a larger model can simultaneously maintain better

Methods	$q^t \to c^i$				$q^i \to c^t$		$q^i \to c^i$	$q^t \to (c^i, c^t)$		$(q^i, q^t) \to c^i$		$(q^i, q^t) \to (c^i, c^t)$	Avg.
	VisDial	VN	COCO	Wiki-SS	VN	COCO	NIGHTS	WebQA	EDIS	CIRR	FIQ	OVEN	
UniIR (Wei et al., 2024)	42.2	74.3	68.5	12.2	76.8	72.1	66.2	89.6	79.2	51.3	40.2	69.4	61.8
GME (Zhang et al., 2024a)	48.1	74.7	68.1	73.9	78.3	63.1	67.0	88.8	91.8	44.2	32.9	72.3	66.9
VLM2Vec-2B (Jiang et al., 2024b)	74.3	73.1	73.4	54.2	73.7	68.5	66.3	85.9	81.2	46.8	14.0	68.3	65.0
VLM2Vec-7B (Jiang et al., 2024b)	81.9	80.5	77.2	62.3	81.2	73.9	67.6	88.3	85.7	51.1	17.1	66.5	69.4
VLM2Vec-V2.0 (Meng et al., 2025)	82.7	74.5	75.3	66.9	78.2	71.4	68.6	90.6	84.1	57.5	19.5	64.3	69.6
LamRA-Qwen2-7B (Liu et al., 2024)	61.3	70.4	72.2	69.7	83.9	73.7	65.6	81.0	85.9	51.7	42.0	82.0	70.0
LamRA-Qwen2.5-7B (Liu et al., 2024)	62.5	70.1	65.7	67.0	74.2	71.1	64.4	85.7	78.7	44.7	33.4	84.8	66.9
LLaVA-7B + CL	81.6	88.9	76.3	59.7	80.1	75.4	68.7	75.9	83.1	58.3	17.4	50.8	68.0
LLaVA-7B + SAS (ours)	81.6	75.6	76.3	57.3	80.0	73.5	69.7	87.2	75.2	56.2	17.4	54.5	67.1
Qwen2.5-VL-3B + CL	83.3	73.8	76.2	61.3	76.5	73.7	62.0	89.6	90.3	59.3	19.9	61.0	68.9
Qwen2.5-VL-3B + SAS (ours)	83.9	71.3	76.5	55.1	76.2	72.2	68.2	90.7	85.8	54.8	20.5	60.6	68.0
Qwen2.5-VL-7B + CL	83.9	77.4	78.4	71.1	78.6	73.9	68.0	90.5	93.0	54.1	25.0	66.8	71.7
Qwen2.5-VL-7B + SAS (ours)	84.6	75.1	77.8	64.5	78.8	74.4	68.0	90.1	90.0	59.7	22.5	65.6	70.9

Table 4: Performance comparison among Qwen2.5-VL-3B/7B with contrastive learning (CL), our SAS-accelerated variants, and state-of-the-art retrieval methods. All results are reported in Hit@1.

accuracy and achieve lower latency than a smaller dense counterpart.

5.2 Performance Comparison

Table 4 compares SAS with representative baselines, including dual-encoder retrievers and recent fine-tuned MLLM-based methods.

Despite aggressive token reduction and adaptive depth allocation, SAS remains highly competitive across diverse retrieval tasks. Our 7B model achieves an average Hit@1 of 70.9%, outperforming strong recent MLLM-based retrieval baselines. This shows that adaptive sparse inference can significantly improve efficiency without compromising the representational strength of large retrieval models.

SAS is particularly effective on tasks requiring fine-grained semantic matching. On benchmarks such as VisDial and WebQA, it consistently performs better than prior methods. We attribute this to the complementary roles of Skim and Skip: Skim suppresses irrelevant information to sharpen semantic focus, while Skip preserves deeper reasoning for genuinely difficult queries.

6 Discussion and Ablation

6.1 Qualitative Analysis of Influence-Aware Token Scoring

To better understand the behavior of the influence score $\psi_l(j)$ used in Skim, we visualize both its distributional behavior and its instance-level spatial selection pattern on the OVEN dataset, based on SAS-3B under 75% visual-token reduction, collecting score statistics from 1,000 queries (112,554 visual tokens in total).

As shown in Figure 4a, the proposed influence score yields a much clearer separation between kept and pruned tokens, with limited distributional overlap. In contrast, raw [EOS] attention collapses most tokens into a narrow range near zero, making the two groups barely distinguishable. This suggests that raw attention, as an instantaneous per-head signal, does not provide a stable pruning boundary. By aggregating perturbation effects across heads and accounting for downstream propagation, the influence score more faithfully captures each token's marginal contribution to the retrieval embedding.

Figure 4b presents a representative spatial score map. The influence score highlights broader and more spatially coherent high-score regions, whereas raw attention responds only to a few isolated peaks. This indicates that retrieval-relevant evidence is often distributed across multiple tokens that jointly shape the [EOS] representation, rather than concentrated in a small number of extreme attention maxima—a pattern that generic attention-based pruning can easily miss.

We further ablate two design choices behind Skim. The selection layer l_s determines when evidence filtering is applied: pruning too early (layers 6–8) removes tokens before cross-modal representations have sufficiently matured, while pruning too late (layer 13) leaves little room before the depth sufficiency check. Setting $l_s = 10$ achieves the best trade-off, full results are provided in Appendix D. We also compare Skim against alternative pruning strategies in Appendix E. Under 75% visual and 50% textual reduction, SAS retains 68.0% performance, whereas vision-only methods (FastV, and DART) drop to 39.3–60.6%, and random text prun-

(a) Score distribution.   (b) Spatial score map.

Figure 4: Qualitative comparison of influence-aware scoring vs. raw [EOS] attention.

Figure 5: Performance under different l_d choices.

| Components | | Performance | Efficiency | |
Skim	Skip	Avg. ↑	FLOPs ↓	Speedup ↑
✗	✗	68.9	100.0%	1.00×
✓	✗	68.0	42.2%	1.26×
✗	✓	68.1	87.9%	1.17×
✓	✓	**68.0**	**36.6%**	**1.44×**

Table 5: Ablation Study of SAS Components.

ing falls to 58.3%.

6.2 Exit Layer Selection

The exit layer l_d determines where the depth sufficiency check is applied. A shallower exit saves more computation but may act on immature representations, whereas a deeper exit is more reliable but reduces the opportunity for early termination.

Figure 5 compares per-layer retrieval performance for SAS variants trained with $l_d \in \{8, 12, 16, 20\}$. Supervising a specific layer consistently boosts retrieval performance at that depth (marked by ⋆), confirming that Stage I effectively activates retrieval capability at the target layer. Among all choices, $l_d = 12$ gives the best trade-off: the intermediate layer reaches 50.6% average Hit@1, while the final layer achieves 69.4%. Earlier exits produce weaker intermediate retrieval representations, while overly late exits reduce the practical benefit of adaptive termination. In particular, setting $l_d = 13$ performs poorly , likely because too little depth remains after the selection layer.

The full quantitative comparison is provided in Figure 5. We further verify this effect through embedding-space visualization in Appendix G: after Stage I training, queries and their ground-truth candidates form much more coherent semantic clusters at l_d, whereas they are clearly separated before training. Additional comparisons of different supervision strategies are also included there.

6.3 Component Analysis

Table 5 reports a progressive ablation of the two hierarchical decisions in SAS. Evidence selection alone brings a 1.26× speedup with minimal performance loss (68.0% vs. 68.9%), indicating substantial token redundancy, while depth adaptation alone yields a 1.17× speedup, suggesting that many queries can terminate before the final layer. Combining the two leads to a 1.44× speedup at the same 68.0% accuracy, showing that token selection and depth allocation address complementary sources of computation and work effectively together.

7 Conclusion

In this paper, we introduce **Skim and Skip (SAS)**, a hierarchical adaptive inference framework designed for universal multimodal retrieval. To overcome the computational bottlenecks inherent in standard dense retrieval, SAS reconfigures the inference paradigm by integrating two complementary strategies: *Influence-Aware Token Filtering*, which effectively prunes redundant tokens to mitigate quadratic complexity, and *Difficulty-Aware Early Exit*, which allows easy samples to terminate at intermediate layers. Comparisons with SOTA dense MLLM backbones across multiple benchmarks demonstrate that SAS significantly enhances inference efficiency while maintaining superior retrieval performance, fully validating the rationality and effectiveness.

Limitations

Despite the encouraging results, we have not yet fully optimized the framework along two practical dimensions.

First, our current prototype uses standard dense attention kernels. Token skimming produces variable-length sequences. These irregular shapes are not always hardware-friendly. As a result, wall-clock gains can fall short of the theoretical FLOPs reduction. This is primarily an engineering gap. SAS is compatible with hardware-aware execution strategies. Examples include length-bucketed batching, fused indexing operators, and kernels that better support sparse or variable-length attention. We expect these improvements to narrow the theory–practice discrepancy.

Second, we evaluate SAS only on retrieval and embedding workloads. We have not validated it on multimodal generation tasks. Extending to VQA or captioning raises additional systems constraints. In particular, KV-cache handling becomes more complex under varying token lengths. It also calls for more systematic choices of pruning and exit locations across backbones. Nevertheless, SAS introduces lightweight control without modifying the backbone. This design is data- and compute-efficient. We therefore expect that limited additional calibration, with small-scale task data or modest extra tuning compute, can enable robust configurations for generative settings.

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A Detailed Related Work

A.1 Multimodal Retrieval

Multimodal retrieval has evolved from dual-encoder models such as CLIP (Radford et al., 2021) toward MLLM-based universal embedding frameworks. Early efforts such as E5-V (Jiang et al., 2024a), VLM2Vec (Jiang et al., 2024b), and GME (Zhang et al., 2024a) demonstrated that MLLMs can be repurposed as strong zero-shot retrievers, while LamRA (Liu et al., 2024) further improved alignment through retrieval-oriented tuning. More recent works continue to strengthen MLLM retrieval through universal embeddings (Li et al., 2026; He et al., 2026), flexible late interaction (Xiao et al., 2026), bottleneck representations (Sun et al., 2026), and reasoning-enhanced retrieval features (Cui et al., 2025; Zhang et al., 2026). For fine-grained scenarios, ColPali (Faysse et al., 2024) introduced multi-vector document representations derived directly from page images.

Beyond architectural design, another line of work improves retrieval representations through data scaling and training strategies. This includes expanding multimodal supervision via synthetic data (Zhou et al., 2024; Chen et al., 2025), as well as improving contrastive learning with modality-aware curation (Kong et al., 2025), smart hard-negative mining (Thirukovalluru et al., 2025), and hardness-aware optimization (Lan et al., 2025). Benchmark efforts such as MMEB-V3 (Huang et al., 2026a) further highlight the remaining performance gaps of omni-modality embedding models. However, these approaches generally retain uniform dense inference at test time, applying the same amount of computation to all queries regardless of difficulty. In contrast, our work focuses on adaptive inference for multimodal retrieval by dynamically adjusting computation according to the query's information content and depth requirement.

A.2 Token Compression and Adaptive Computation

To reduce the computational cost of long multimodal sequences, prior work has extensively studied token compression, especially on the vision side. Attention-based methods such as FastV (Chen et al., 2024), SparseVLM (Zhang et al., 2024b), and ADSC (Deniz et al., 2025) rank tokens by importance scores, but often remain sensitive to local attention patterns. Similarity-based methods, including ToMe (Bolya et al., 2022), VisionZip (Yang

et al., 2024), and DART (Wen et al., 2025), merge or select representative tokens based on feature similarity, but are often weakly coupled to downstream retrieval objectives. More recent approaches incorporate stronger adaptivity through text conditioning, hierarchical reduction, or energy-aware scoring, as in CDPruner (Zhang et al., 2025a), GridPrune (Duan et al., 2025), HoloV (Zou et al., 2025), HiDrop (Wu et al., 2026), and EAdaPrune (He and Chen, 2026). Nevertheless, these methods mainly focus on reducing token count, typically under a predefined compression budget. Recent analysis also shows that visual token pruning can fail when relevant evidence shifts during inference (Kim et al., 2026).

A complementary line of work studies adaptive computation through early exit or layer skipping. In language models, methods such as FastBERT (Liu et al., 2020), DeeBERT (Xin et al., 2020), and ADEPT (Yoo et al., 2026) dynamically reduce inference depth based on prediction confidence. Related ideas have also been explored in retrieval-augmented and multimodal settings (Huang et al., 2026b; Yang et al., 2026). However, directly transferring these techniques to multimodal retrieval is non-trivial, since retrieval depends on the stability of continuous embeddings rather than discrete label predictions. Different from prior work that treats token reduction and depth reduction separately, our method formulates efficient multimodal retrieval as a unified adaptive inference problem that jointly decides what information to keep and how deeply it should be processed.

B Theoretical Analysis of Influence-Aware Token Skimming

In this section, we provide the complete derivation for the Influence-Aware Token Filtering score $\psi_l(j)$ (Eq. (4) in the main text) and the bounding analysis for retrieval stability under token pruning.

B.1 Derivation of Influence Score

Problem Formulation and Notation. We consider a Transformer-based MLLM backbone with L layers. For a specific query encoding process, we focus on the self-attention mechanism at layer l with H heads. Let $\mathbf{h}_l[i] \in \mathbb{R}^D$ denote the hidden state of token i at layer l, and let e denote the index of the [EOS] token used for pooling the final query embedding. For a specific head h, the projection matrices are defined as $W_Q^{l,h}, W_K^{l,h}, W_V^{l,h} \in \mathbb{R}^{d \times D}$,

and the output projection matrix as $W_O^{l,h} \in \mathbb{R}^{D \times d}$, where $d = D/H$. Crucially, we incorporate the bias term for the value projection, denoted as $\mathbf{b}_V^{l,h} \in \mathbb{R}^d$. Accordingly, the value vector for token i is computed as:

$$\mathbf{v}_{l,h,i} = W_V^{l,h}\mathbf{h}_l[i] + \mathbf{b}_V^{l,h}, \qquad (10)$$

and the attention weight from the [EOS] token to token i is denoted by $\alpha_{l,h}(e \to i)$.

Local Perturbation Analysis. Consider the self-attention output at the [EOS] position for a single head h at layer l. The original output $\mathbf{o}_{l,h}(e)$ is a weighted sum of value vectors:

$$\mathbf{o}_{l,h}(e) = \sum_i \alpha_{l,h}(e \to i)\mathbf{v}_{l,h,i}. \qquad (11)$$

When a token j is removed (skimmed), the attention mechanism re-normalizes the weights of the remaining tokens. Assuming the pre-softmax logits remain unchanged for the surviving tokens, the new attention weight for any remaining token i ($i \neq j$) becomes:

$$\alpha'_{l,h}(e \to i) = \frac{\alpha_{l,h}(e \to i)}{1 - \alpha_{l,h}(e \to j)}. \qquad (12)$$

The perturbed output $\mathbf{o}'_{l,h}(e)$ after removing token j is:

$$\mathbf{o}'_{l,h}(e) = \sum_{i \neq j} \frac{\alpha_{l,h}(e \to i)}{1 - \alpha_{l,h}(e \to j)}\mathbf{v}_{l,h,i}. \qquad (13)$$

The exact perturbation vector $\Delta\mathbf{o}_{l,h}(e) = \mathbf{o}'_{l,h}(e) - \mathbf{o}_{l,h}(e)$ is derived as follows:

$$\begin{aligned}
\Delta\mathbf{o}_{l,h}(e) &= \frac{\sum_{i \neq j} \alpha_{l,h}(e \to i)\mathbf{v}_{l,h,i}}{1 - \alpha_{l,h}(e \to j)} - \mathbf{o}_{l,h}(e) \\
&= \frac{\mathbf{o}_{l,h}(e) - \alpha_{l,h}(e \to j)\mathbf{v}_{l,h,j}}{1 - \alpha_{l,h}(e \to j)} - \mathbf{o}_{l,h}(e) \\
&= \frac{\alpha_{l,h}(e \to j)}{1 - \alpha_{l,h}(e \to j)}(\mathbf{o}_{l,h}(e) - \mathbf{v}_{l,h,j}).
\end{aligned}$$
$$(14)$$

This recovers Eq. (2) presented in the main text.

Upper Bound on Influence Score. To efficiently select tokens for pruning, we derive a computable upper bound for the magnitude of the perturbation projected by $W_O^{l,h}$. We utilize the spectral norms of the weight matrices, denoted as $\sigma_V^{l,h} = \|W_V^{l,h}\|_2$ and $\sigma_O^{l,h} = \|W_O^{l,h}\|_2$.

First, we bound the term $\|\mathbf{o}_{l,h}(e) - \mathbf{v}_{l,h,j}\|_2$ using the triangle inequality:

$$\|\mathbf{o}_{l,h}(e) - \mathbf{v}_{l,h,j}\|_2 \leq \|\mathbf{o}_{l,h}(e)\|_2 + \|\mathbf{v}_{l,h,j}\|_2. \quad (15)$$

We expand the norm of the value vector $\mathbf{v}_{l,h,j}$:

$$\begin{aligned}\|\mathbf{v}_{l,h,j}\|_2 &= \|W_V^{l,h}\mathbf{h}_l[j] + \mathbf{b}_V^{l,h}\|_2 \\ &\leq \sigma_V^{l,h}\|\mathbf{h}_l[j]\|_2 + \|\mathbf{b}_V^{l,h}\|_2.\end{aligned} \quad (16)$$

Next, we expand the norm of the original output $\mathbf{o}_{l,h}(e)$. Noting that $\sum_i \alpha_{l,h}(e \rightarrow i) = 1$, the bias term sums directly:

$$\begin{aligned}\|\mathbf{o}_{l,h}(e)\|_2 &= \left\|\sum_i \alpha_{l,h}(e \rightarrow i)(W_V^{l,h}\mathbf{h}_l[i] + \mathbf{b}_V^{l,h})\right\|_2 \\ &\leq \sigma_V^{l,h}\sum_i \alpha_{l,h}(e \rightarrow i)\|\mathbf{h}_l[i]\|_2 + \|\mathbf{b}_V^{l,h}\|_2 \\ &= \sigma_V^{l,h}S_{l,h} + \|\mathbf{b}_V^{l,h}\|_2, \quad (17)\end{aligned}$$

where we defined $S_{l,h} := \sum_i \alpha_{l,h}(e \rightarrow i)\|\mathbf{h}_l[i]\|_2$.

Substituting these bounds back into the perturbation equation:

$$\begin{aligned}&\|W_O^{l,h}\Delta\mathbf{o}_{l,h}(e)\|_2 \\ &\leq \sigma_O^{l,h}\frac{\alpha_{l,h}(e \rightarrow j)}{1 - \alpha_{l,h}(e \rightarrow j)}(\|\mathbf{o}_{l,h}(e)\|_2 + \|\mathbf{v}_{l,h,j}\|_2) \\ &\leq \sigma_O^{l,h}\frac{\alpha_{l,h}(e \rightarrow j)}{1 - \alpha_{l,h}(e \rightarrow j)}\left[\left(\sigma_V^{l,h}S_{l,h} + \|\mathbf{b}_V^{l,h}\|_2\right)\right. \\ &\quad \left. + \left(\sigma_V^{l,h}\|\mathbf{h}_l[j]\|_2 + \|\mathbf{b}_V^{l,h}\|_2\right)\right] \\ &= \sigma_O^{l,h}\frac{\alpha_{l,h}(e \rightarrow j)}{1 - \alpha_{l,h}(e \rightarrow j)} \\ &\quad \cdot \left(\sigma_V^{l,h}\left(S_{l,h} + \|\mathbf{h}_l[j]\|_2\right) + 2\|\mathbf{b}_V^{l,h}\|_2\right). \quad (18)\end{aligned}$$

Summing this upper bound across all H heads yields the final Influence Score $\psi_l(j)$, as used in the token filtering algorithm.

B.2 Theoretical Interpretation: Connection to Integrated Gradients

The derived influence score $\psi_l(j)$ aligns theoretically with feature attribution methods. Specifically, the importance of a token h_j to the output function F can be formalized using Integrated Gradients (IG):

$$IG_j(F) = (h_j - 0) \times \int_{\alpha=0}^{1}\frac{\partial F(\alpha h_j)}{\partial h_j}d\alpha. \quad (19)$$

In the context of the attention mechanism, assuming a single-step linear approximation ($\alpha = 1$) and the "Attention-as-Gradient" hypothesis, the gradient flow is proportional to the attention weight weighted by the value projection. Consequently, the perturbation term in Eq. 14 can be viewed as:

$$\|\Delta o_{l,h}(e)\| \approx \|\underbrace{\alpha_{l,h}(e \rightarrow j) \cdot v_{l,h,j}}_{\text{Attribution}}\|. \quad (20)$$

Therefore, our filtering strategy $\min_j \psi_l(j)$ is closely related to pruning the token with the minimal first-order contribution to the layer's output.

B.3 Global Stability Analysis via Neural ODEs

While the derivation above guarantees minimal *local* perturbation, we further demonstrate that this error does not propagate catastrophically. We view the residual connections in the MLLM backbone as an Euler discretization of a continuous Ordinary Differential Equation (ODE):

$$h_{l+1} = h_l + f(h_l) \iff \frac{dh(t)}{dt} = f(h(t), t) \quad (21)$$

Let $h(t)$ represent the trajectory of the full token sequence and $\tilde{h}(t)$ represent the trajectory after pruning a token at time t_l. The initial discrepancy introduced by pruning is bounded by our influence score: $\|\tilde{h}(t_l) - h(t_l)\| \leq \epsilon = \min_j \psi_l(j)$.

Assuming the network dynamics function f (Transformer block) is K-Lipschitz continuous (satisfied by bounded activation functions and LayerNorm), the divergence between the trajectories at the final time T (Layer L) is governed by **Gronwall's Inequality**:

$$\|\tilde{h}(T) - h(T)\| \leq \|\tilde{h}(t_l) - h(t_l)\| \cdot e^{K(T-t_l)}. \quad (22)$$

This inequality suggests that the error introduced by our skimming strategy remains bounded under the stated assumptions. By minimizing the initial perturbation $\|\tilde{h}(t_l) - h(t_l)\|$ via our Influence Score, the deviation in the final retrieval embedding can be kept under control, rather than growing chaotically.

C Implementation Details of Termination Classifier

In this section, we provide the technical specifications for the Termination Classifier $g(\cdot)$ utilized in Stage II.

C.1 Input Feature Construction

The classifier aggregates information from three distinct sources. We specifically design these features to capture inference uncertainty, input modality, and semantic context:

- **Confidence & Uncertainty Scalars ($\mathbf{x}_{stat} \in \mathbb{R}^{27}$):** We extract 27 scalar statistics from the intermediate layer's output. Crucially, to explicitly inform the classifier about ranking stability, we include:

  (1) **Top-1 Similarity Score:** The cosine similarity of the highest-ranked candidate, serving as a proxy for absolute confidence.

  (2) **Top-1/Top-2 Margin:** The difference between the similarity scores of the top-1 and top-2 candidates. A larger margin typically indicates a decisive prediction, while a narrow margin suggests potential ambiguity.

Other metrics include attention entropy, token density, and maximum attention scores. To rectify the highly skewed, long-tail distribution of these values (e.g., entropy varies significantly across layers), we apply a signed Log1p transformation followed by Layer Normalization:

$$\hat{\mathbf{x}}_{stat} = \text{LayerNorm}(\text{sign}(\mathbf{x}_{stat}) \cdot \ln(1 + |\mathbf{x}_{stat}|)). \tag{23}$$

- **Modality Embedding ($\mathbf{x}_{mod} \in \mathbb{R}^{4}$):** A learnable embedding layer maps the discrete modality index (representing text-only, image-only, or multimodal inputs) to a 4-dimensional continuous vector. This allows the classifier to adapt its decision boundary biases according to the specific input data type.

- **Semantic Projection ($\mathbf{x}_{sem} \in \mathbb{R}^{64}$):** To incorporate semantic context without incurring high computational costs, the high-dimensional backbone embedding $\mathbf{e}_{l_{exit}}$ ($D = 3584$ for Qwen2.5-VL) is projected to a lower dimension via a non-linear head:

$$\mathbf{x}_{sem} = \text{ReLU}(\text{LayerNorm}(\mathbf{W}_p \mathbf{e}_{l_{exit}} + \mathbf{b}_p)), \tag{24}$$

where the projection dimension is set to 64.

C.2 Network Architecture

The processed features are concatenated into a single vector $\mathbf{h}_{in} \in \mathbb{R}^{95}$ and fed into the classifier.

The architecture is a Multi-Layer Perceptron (MLP) defined as:

$$p_{exit} = \text{Sigmoid}(\text{MLP}_{\text{LN}}(\mathbf{h}_{in})). \tag{25}$$

Specifically, MLP_{LN} consists of two hidden layers with dimensions 128 and 64, respectively. We consistently employ Layer Normalization instead of Batch Normalization after each linear transformation, followed by ReLU activation and Dropout ($p = 0.2$). This design ensures that normalization statistics are computed independently for each instance, enhancing robustness against batch-size variations and distribution shifts during inference.

C.3 Training Objective

Since samples that are already sufficient at intermediate layers and those requiring deeper computation are typically imbalanced, we optimize the classifier using Focal Loss (Lin et al., 2017):

$$\mathcal{L}_{focal} = -\alpha(1 - p_t)^{\gamma} \log(p_t), \tag{26}$$

where p_t represents the estimated probability for the ground-truth class. This loss reduces the dominance of easy-to-classify samples, focusing training on boundary cases where the sufficiency decision is most ambiguous. We set $\alpha = 0.8$ and $\gamma = 3.0$ in all experiments.

D Hyperparameter Sensitivity: Pivot Layer Selection

D.1 Selection of the Selection Layer (l_s)

A key design choice in SAS is the position of the selection layer l_s, where Influence-Aware Token Filtering is applied. Choosing l_s requires balancing computational savings against representational maturity:

- **Too early ($l_s < 8$):** Multimodal representations may not yet be sufficiently mature. Pruning at this stage risks removing tokens that appear locally redundant but are still important for deeper cross-modal aggregation.

- **Too late ($l_s > 12$):** Although safer, delayed pruning preserves redundant tokens for too many layers and weakens the efficiency gains.

To identify an appropriate l_s, we conduct an ablation study on Qwen2.5-VL-3B trained for 2,000 steps on MMEB. We vary the selection layer over $l_s \in \{6, 8, 10, 11, 12, 13\}$ and measure retrieval performance (Hit@1) at both the intermediate layer (L_{12}) and the final layer (L_{36}).

Selection (l_s)	Retrieval Performance (Hit@1)	
	Inter. (L_{12})	Final (L_{36})
6	39.5%	66.3%
8	39.3%	66.4%
10	**44.4%**	**69.2%**
11	44.4%	68.1%
12	45.4%	68.7%
13	5.3%	68.2%

Table 6: **Impact of selection layer choice.** Retrieval performance at the intermediate and final layers under different l_s settings. $l_s = 10$ achieves the best balance.

Method	Avg. ↑	Vis. R. ↑	Text R. ↑	FLOPs ↓
DenseRet-3B	68.9	0%	0%	100%
Vision Pruning Baselines				
+ VisionZip	39.3	75%	0%	48.5%
+ FastV	60.6	75%	0%	51.3%
+ DART	59.0	75%	0%	51.3%
Text Pruning Baseline				
+ Random	58.3	0%	50%	76.9%
Ours				
+ SAS	**68.0**	**75%**	**50%**	**36.6%**

Table 7: Comparison with vision and text token pruning strategies. Vis. R. and Text R. denote the reduction rates of visual and textual tokens, respectively.

Analysis. As shown in Table 6, applying pruning too early (layers 6 or 8) noticeably degrades final performance (around 66.3%–66.4% versus 69.2%), confirming that early representations are still too unstable for aggressive reduction.

Notably, $l_s = 10$ gives the best overall result, outperforming even later choices such as $l_s = 12$. We conjecture that selecting tokens at layer 10 leaves a useful buffer before the first depth sufficiency check at $l_d = 12$, allowing the remaining tokens to re-distribute attention and consolidate cross-modal semantics after pruning. By contrast, when filtering is applied too close to the first depth decision, the model has insufficient room to recover from the perturbation introduced by token removal. We therefore set $l_s = 10$ in all main experiments.

E Token Pruning Strategy Comparison

We compare SAS with existing token pruning strategies applied to the DenseRet backbone, including vision-centric methods (VisionZip, FastV, DART) and a text-centric baseline (Random Text Pruning).

As shown in Table 7, vision-optimized meth-

Table 8: **Impact of decision layer choice.** Average Hit@1 at the selected decision layer l_d and at the final layer. We choose l_d=12 in the main experiments.

l_d	Hit@1 at l_d	Hit@1 at L_{36}
8	47.7	66.8
10	50.9	69.4
11	50.5	68.2
12	**50.6**	**69.4**
13	18.8	67.7

ods cause severe degradation (e.g., VisionZip: 68.9% → 39.3%), as they prioritize local visual salience without reference to the retrieval objective. Random text pruning (58.3%) indiscriminately removes tokens critical for semantic alignment. SAS sustains 68.0% performance at substantially higher reduction ratios (75% visual, 50% textual) because its influence metric specifically preserves tokens with high marginal contribution to the [EOS] retrieval embedding.

F Exit Layer Ablation

Table 8 reports the average Hit@1 at the selected decision layer and at the final layer under different choices of l_d. Although $l_d = 10$ and $l_d = 12$ achieve comparable final-layer performance, we use $l_d = 12$ in the main experiments because it provides a more stable decision point after token selection and better practical early-exit behavior.

G Detailed Ablation on Supervision Strategies

This section provides the detailed numerical comparison of different intermediate supervision strategies. Table 9 reports the retrieval accuracy (Hit@1) at both the intermediate exit layer (L_{12}) and the final layer (L_{last}). Further analysis reveals the limitations of single objectives. Applying solely $\mathcal{L}_{con}$ leads to under-fitting (49.4%) due to optimization difficulties at shallow layers, while solely $\mathcal{L}_{distill}$ over-regularizes the network, suppressing the final layer's potential (L_{last} drops to 69.2%). In contrast, our Hybrid Strategy resolves this dilemma, securing high utility for early exiting (57.2%) while boosting the final layer's peak performance to **69.5%**.

H More Visualization Results

(a) Before training

(a) Before training

Figure 6: t-SNE visualizations on CIRR

Figure 9: t-SNE visualizations on VisualNews_i2t

(b) After training

(b) After training

(a) Before training

(a) Before training

Figure 7: t-SNE visualizations on NIGHTS

Figure 10: t-SNE visualizations on VisDial

(b) After training

(b) After training

(a) Before training

(a) Before training

Figure 8: t-SNE visualizations on OVEN

Figure 11: t-SNE visualizations on MSCOCO_t2i

(b) After training

(b) After training

Table 9: **Impact of Intermediate Supervision Strategies.** Comparison of Hit@1 accuracy at the intermediate (L_{12}) and final (L_{last}) layers.

Training Strategy	Exit (L_{12})	Final (L_{last})
Baseline (No Loss)	0.01	68.9
$+\mathcal{L}_{con}$ Only	49.4	69.0
$+\mathcal{L}_{distill}$ Only	**57.4**	69.2
Hybrid (Ours)	57.2	**69.5**

(a) Before training

(b) After training

Figure 12: t-SNE visualizations on Wiki-SS-NQ