SELF-DEMOS: Eliciting Out-of-Demonstration Generalizability in Large Language Models

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Abstract

Large language models (LLMs) have shown promising abilities of in-context learning (ICL), adapting swiftly to new tasks with only few-shot demonstrations. However, current few-shot methods heavily depend on high-quality, query-specific demos, which are often lacking. When faced with *out-of-demonstration* (OOD[1]) queries, methods that rely on hand-crafted demos or external retrievers might fail. To bridge the gap between limited demos and OOD queries, we propose **SELF-DEMOS**, a novel prompting method that elicits the inherent generalizability in LLMs by query-aware demo generation. The generated demos strategically interpolate between existing demos and the given query, transforming the query from OOD to ID. To evaluate the effectiveness of our approach, we manually constructed **OOD-Toolset**, a dataset in the tool-using scenario with over 300 real-world APIs and 1000 instances, each consisting of three tool-use cases as demos and an OOD query. Thorough experiments on our dataset and two public math benchmarks have shown that our method can outperform state-of-the-art baselines in the OOD setting. Moreover, we conduct a range of analyses to validate SELF-DEMOS's generalization and provide more insights.

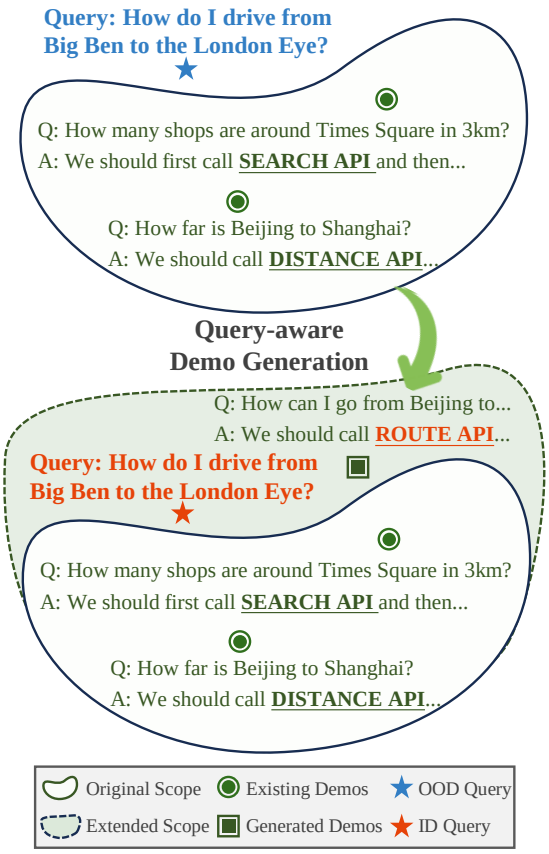


Figure 1: An example of how query-aware demo generation works. In the tool-using scenario, there is a gap between the user query and the available tool-use cases in the original scope since they require different APIs. This can lead to errors if the LLM is unfamiliar with the ROUTE API. After interpolating new demos between the existing ones and the OOD query, LLMs can perform better in the extended scope.

1 Introduction

Large language models (LLMs) have achieved impressive performance across a wide range of tasks, ranging from mathematical reasoning to tool using (Brown et al., 2020a; Kojima et al., 2022; Qin et al., 2023; Xi et al., 2023). The models learn to perform unseen downstream tasks simply by conditioning on a prompt containing input-output pairs (i.e., *few-shot demonstrations*, Brown et al., 2020a). This paradigm, also known as in-context learning (ICL), has been found its effectiveness considerably influenced by the quality and relevance of the demos provided (Liu et al., 2022; Dong et al., 2023). Thus, how to provide high-quality demos becomes an essential challenge in LLM applications.

The leading few-shot techniques typically hinge on hand-crafted task-specific demos or extensive demo libraries (Wei et al., 2022c; Liu et al., 2022;

[1]OOD refers to "Out-of-Demonstration" in this paper, not the commonly understood "Out-of-Distribution". Similarly, ID stands for "In-Demonstration".

Rubin et al., 2022). However, crafting demos for each unique query is impractical, and the demo libraries are also unable to cover all the potential queries. The issue arises when faced with out-of-demonstration (OOD) queries, resulting in poorer performance due to the gap between existing demos and new queries.

An alternative strategy is prompting the LLMs to self-generate relevant demos, thereby guiding themselves toward resolving the query (Kim et al., 2022; Chen et al., 2023b; Yasunaga et al., 2023). However, these works often overlook a critical point: instead of blindly recalling relevant demos based on queries, we can perform interpolation between existing demos and queries, as depicted in Figure 1. By strategically interpolating, we can derive more relevant and accurate demos from existing ones, which have proven helpful for the final response (Liu et al., 2022; Halawi et al., 2023). Specifically, we introduce **SELF-DEMOS**, a novel prompting method that may fully elicit the model's potential out-of-demonstration generalizability. Unlike previous works, we developed a complete workflow incorporating pre- and post-processing steps around the demo generation. Before the demos are generated, we first prompt the model to *"give a general understanding of the user query"*, thus reducing the cognitive load in subsequent steps. Then, we generate query-aware demos and select the most high-quality ones through *Best-of-N sampling* (Stiennon et al., 2020). These selected demos will be used for the final response along with the initial available demos.

To evaluate our approach's efficacy in the OOD context, we manually construct **OOD-Toolset**, a dataset tailored for tool-using scenarios as delineated by Tang et al. (2023). Our dataset includes over 300 real-world APIs and 1000 instances, each consisting of three tool-use cases as demos and an OOD query. Moreover, we benchmarked our method with two public mathematical datasets, GSM8K (Cobbe et al., 2021) and MATH (Hendrycks et al., 2021), to validate its adaptability. The primary experimental findings reveal that SELF-DEMOS outperforms state-of-the-art baselines in solving OOD queries. We also conducted ablation studies and other extensive experiments to gain more insights into our method. Collectively, our analyses show that we have found a more efficient way to elicit the potential OOD generalizability in LLMs.

Our contributions are summarized as follows:

1. We proposed SELF-DEMOS, a novel prompting method to elicit the out-of-demonstration (OOD) generalizability in LLMs.

2. We manually constructed OOD-Toolset, a tool-using dataset for better verifying the potential OOD generalizability in LLMs.

3. We conducted extensive experiments to validate SELF-DEMOS's effectiveness and generalization under different settings.

2 Related Work

2.1 In-Context Learning

The rise of LLMs such as ChatGPT (OpenAI, 2022) and LLaMA (Touvron et al., 2023) has revolutionized the field. With the model size scaling, LLMs demonstrate remarkable capabilities of ICL (Brown et al., 2020b; Wei et al., 2022b), which learns to perform tasks by specific instructions and demonstrations. Additionally, insights from scaling laws (Wei et al., 2022b) also highlight the LLMs' potential for out-of-distribution generalization. It refers to the challenge where model inputs deviate from their training distribution (Wang et al., 2023a). If stimulated effectively, this generalization capability can empower LLMs to address queries outside the training corpus (Collins et al., 2022), enhancing utility in dynamic and open-ended scenarios.

2.2 Optimizing Demonstrations for ICL

The performance of LLMs may be influenced by the quantity, relevance, diversity, and truthfulness of demonstrations (Chen et al., 2023a; Levy et al., 2023; Min et al., 2022; Halawi et al., 2023). There are two primary paradigms to optimize demonstrations and steer models towards generalization.

Demo Retrieval for ICL. LLMs are sensitive to the choice of demonstrations. Therefore, researchers have focused on using retrieval modules to find the most representative demos for ICL. One effective strategy is leveraging existing retrievers based on semantic similarity metrics between the available demos and queries (Liu et al., 2022; Agrawal et al., 2023; Gao et al., 2023; Luo et al., 2023). Another method employs ranking scores derived from fine-tuned language models (Rubin et al., 2022; Shi et al., 2022).

Demo Generation for ICL. Rather than extracting existing demos, demo generation aims to self-generate exemplars that closely align with the in-

put. Kim et al. (2022) initially employed language models to produce demos from pre-defined labels. Subsequent works adopted a two-stage approach of generating and selecting demos (Li et al., 2022; Zhang et al., 2023; Shao et al., 2023). In contrast, our work leverages the intrinsic capabilities of LLMs to identify superior demos via best-of-N sampling.

Besides, there are approaches akin to ours. Chen et al. (2023b) adopt multi-steps to construct demonstration pairs, while Yasunaga et al. (2023) prompt LLMs to recall relevant demos before answering. However, our method stands out by combining pre- and post-processing steps around demo generation to guarantee the high quality of generated demos.

2.3 Eliciting LLMs' Power with Prompts

Efforts to enhance LLMs include finetuning with specific instructions (Wei et al., 2022a) and employing prompting strategies like Chain-of-Thought (CoT) (Wei et al., 2022c). Our approach adopts the prompt-based strategy and draws inspiration from studies of the "self" series (Madaan et al., 2023; Wang et al., 2023b; Chen et al., 2023b). The essence of "self" is to leverage the model's inherent power, without external modules. Our method positions the LLM itself as an analyzer, generator, and selector, aiming to elicit its intrinsic generalizability to resolve OOD queries.

3 Methodology

In this section, we first introduce the construction process of OOD-Toolset. Next, we provide a detailed description of the SELF-DEMOS method, which is illustrated in Figure 2.

3.1 OOD-Toolset Construction

Recent works are evaluated on benchmarks such as BIG-Bench (Srivastava et al., 2022) and GSM8K (Cobbe et al., 2021). However, since these datasets may have been inadvertently included in the training data of LLMs, there is a risk of overestimating their ability to generalize to OOD query (Zhou et al., 2023). To mitigate this, we chose the tool-using scenarios that are less likely to occur during model training for assessment. Specifically, we constructed the dataset following the two steps:

Data Collection. Our original data derives from the tool-use corpus created by ToolAlpaca (Tang et al., 2023). It was composed of a wide range of real-world APIs complete with API descriptions, usage specifications, and multiple simulated tool-use cases. However, despite the dataset's comprehensiveness, we noted that the initial AI-generated tool-use cases contain some errors, such as ambiguous queries and incorrect API calls in response. These minor errors may prevent accurate judgment in our evaluation. Therefore, we engaged human annotators to manually refine the corpus, producing a high-quality version for more reliable assessment. Additional details and an example of OOD-Toolset are provided in Appendix A.

OOD Setting. We retained the user's queries and corresponding API calls from tool-use cases as input-output pairs for the evaluation. In addition, we kept the API descriptions and usage specifications from the refined corpus as context for LLMs. For each test instance, we provided three cases from the same API as initial available few-shot demos (also referred to as *seed demos* (D_{seed})). Notably, in the OOD setting, the sub-APIs in seed demos differ from those needed in the final query.

Take the MAP tool for example, which contains three sub-APIs: DISTANCE, ROUTE, and SEARCH API. For instance, if the DISTANCE and SEARCH APIs serve as seed demos, the user's query might pertain to the ROUTE API. This design tests the model's ability to understand and apply tool-using patterns across different functions, allowing us to explore the OOD generalizability in LLMs.

3.2 SELF-DEMOS

We executed the whole workflow by prompting the model itself. The prompt template for each step is illustrated in Appendix B.

Query Understanding. The first step involves comprehensive query understanding. Given the model $\mathcal{M}$ and a query q, we employ a zero-shot method:

$$u = \mathcal{M}(p_1 \,||\, q), \tag{1}$$

where p_1 is the prompt for query understanding, $||$ denotes concatenation, and u is the generated understanding. Through this pre-processing step, we narrow the gap between seed demos and the target query, transitioning from the generic MAP API to the more specific ROUTE sub-API. Furthermore, this step resembles a chain-of-thought process (Wei et al., 2022c), which may reduce the cognitive load in subsequent steps. This is helpful to enhance the relevance and accuracy of the generated demos.

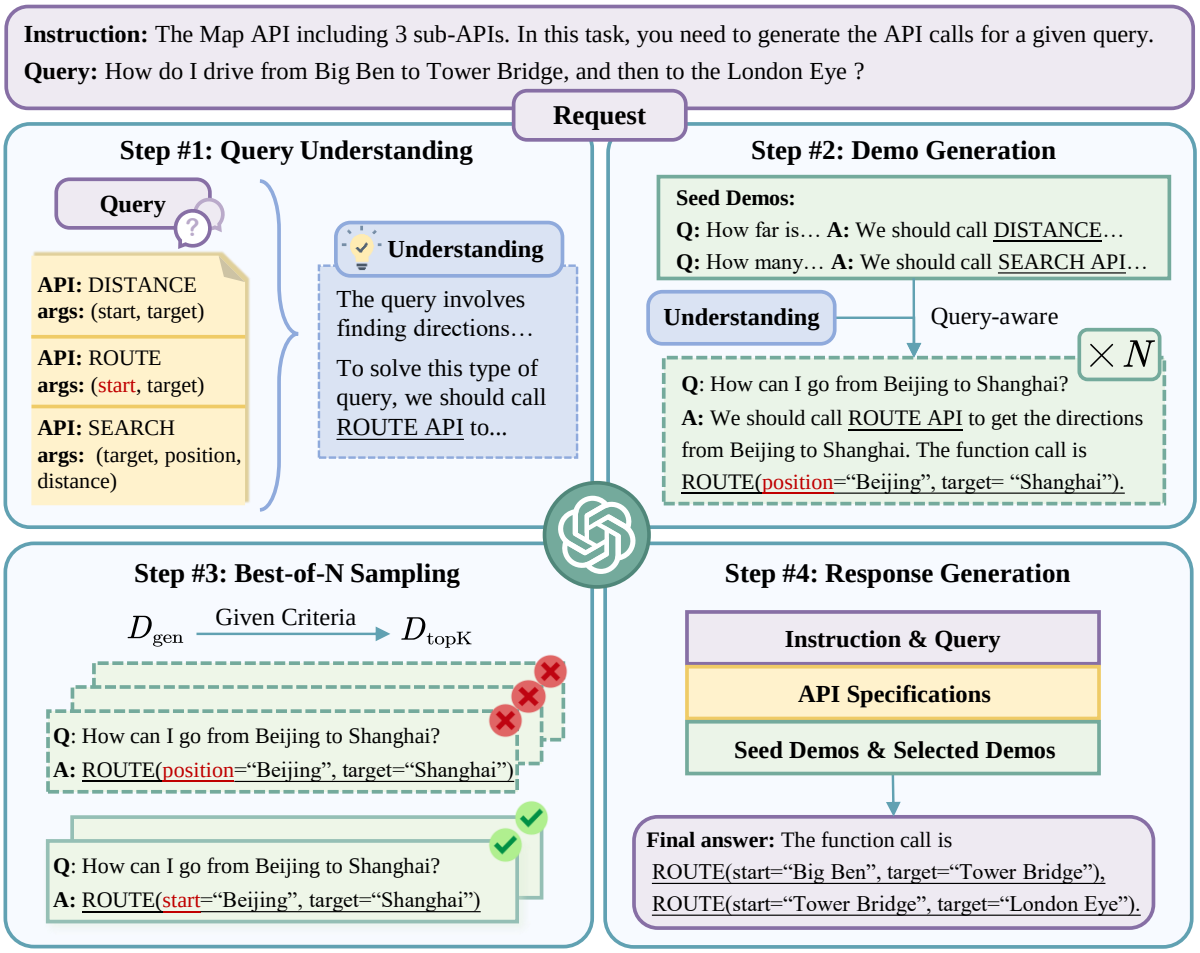


Figure 2: An overview of the proposed SELF-DEMOS prompting method in tool-using scenario.

Query-aware Demo Generation. Based on the distilled understanding u and seed demos D_{seed}, we generate query-aware demos as:

$$D_{\text{gen}} = \{d_1, d_2, ..., d_N\} = \mathcal{M}(p_2 \mid\mid q, u, D_{\text{seed}}), \tag{2}$$

where p_2 is the prompt for demo generation, D_{gen} is the set of generated demos, and N is the number of demos to be generated. The seed demos, while not directly linked to the specific query, showcase potential tool-using patterns of MAP API, offering guidance for the generation. We call the model N times to generate N demos separately, alleviating the difficulty of a single try and avoiding the model falling into consecutive errors in one response. In this phase, we extend the original scope of the demos to a broader boundary.

Best-of-N Sampling. It has been argued that LLMs are unlikely to self-critique their outputs without an external validator (Stechly et al., 2023; Valmeekam et al., 2023). Consequently, we assume that while models might not calibrate and refine outputs, they could still discern the superior output from a variety. Therefore, we employ a Best-of-N sampling strategy, where the model is prompted to select the best K demos from the N generated demos based on special criteria:

$$D_{\text{topK}} = \mathcal{M}(p_3 \mid\mid D_{\text{gen}}, C, K), \tag{3}$$

where p_3 is the prompt for sampling, D_{topK} is the subset of K demos sampled from the generated ones, conditioned on criteria C.

This process is inspired by preference learning, where multiple samples are generated and the one with the highest reward model score is chosen (Stiennon et al., 2020). It is worth noting that our criteria, which include the demos' accuracy, relevance, and potential helpfulness for the final response, are given to the model via prompts. This is where SELF-DEMOS differs from methods such as Synthetic Prompting (Shao et al., 2023), which also selects demos after generation. Because our sampling criteria are more nuanced and do not rely on an external retriever.

Response Generation. Finally, we leverage the sampled demos D_{topK} and the initial seed demos D_{seed} to generate the final response:

$$r = \mathcal{M}(p_4 \,||\, D_{\text{seed}} \cup D_{\text{topK}}, q), \tag{4}$$

where p_4 is the prompt for response generation, $\cup$ denotes the concatenation of two sets and the r is the final response. The concatenation ensures that the model benefits from the query-specific demos in D_{topK}, while also incorporating the beneficial diversity and quality of D_{seed} (Levy et al., 2023; Halawi et al., 2023).

4 Experiments

To evaluate the effectiveness of SELF-DEMOS, we conduct extensive experiments for comparison and analysis.

4.1 Experimental Setups

Foundation Models. We use GPT-3.5 (the `gpt-3.5-turbo-0613` version) for most of our experiments, with only one additional experiment using the Llama-2-Chat model family, to validate the generalization of SELF-DEMOS across different model sizes. For all LLMs, we set the parameter $temperature = 0$ for stable responses except for the sampling step, where we set $temperature = 0.8$ to introduce diversity.

Tasks & Datasets. We evaluate the proposed method in two reasoning-intensive tasks: tool-using and mathematical problem-solving.

In the tool task, we developed the OOD-Toolset for evaluation. Details of the construction process are described in section 3.1. In the math task, we employed two public datasets: GSM8K (Cobbe et al., 2021), featuring elementary math word problems, and MATH (Hendrycks et al., 2021), containing complex problems from high school competitions. We evaluate the entire GSM8K testing set and a randomly selected subset from the MATH testing set. Distinct OOD settings are designed for math tasks. For GSM8K, we manually created several outlier samples, ensuring that the testing set did not contain problems with similar contexts. For MATH, since the problems were categorized into seven subjects and five difficulty levels, we used problems from different subjects but the same level to meet the OOD condition. The dataset statistics are presented in Table 1.

Evaluation Metric. In the report for the math tasks, we present the exact match accuracy for each problem. For the tool task, which may require multiple API calls in one case, we assess accuracy using both exact and partial matches. Partial matches are awarded half the score if the model's response includes only part of the required API calls.

4.2 Baselines

We compare SELF-DEMOS with the following baselines, including two methods that are designed for demo generation:

Zero-shot and Zero-shot + CoT (Brown et al., 2020a; Kojima et al., 2022). Prompt the model with the task description, test input, and no demonstration. Besides, the CoT method integrates a trigger prompt *"let's think step by step"*.

Few-shot (Wei et al., 2022c). Employ a fixed set of seed demos we constructed for each OOD query. For the GSM8K and MATH datasets, which include solutions with labeled reasoning steps, the demos also feature CoT steps to enhance the model's problem-solving capabilities.

Self-ICL (Chen et al., 2023b). A multi-step framework for zero-shot in-context learning by prompting the LLM itself to generate pseudo-inputs and labels. Unlike us, they generate Q&A separately and then merge them into demos, with no other pre- and post-processing steps. We have also adapted it into a few-shot variant to make it comparable.

Analogical Prompting (Yasunaga et al., 2023). A single-step prompting method that guides LLM to recall relevant demos and knowledge before solving a given problem. Here we let it generate demos for the vanilla version and our few-shot variant.

4.3 Main Results

Table 2 shows the performance of each method on three datasets. We can find that: (1) The better performance of few-shot over zero-shot (+ CoT) shows the LLM's capacity to discern and apply underlying patterns from seed demos to OOD queries, indicating a degree of inherent generalizability. Furthermore, the OOD-Toolset measures this ability more accurately than the two public math datasets, validating the necessity of creating unseen scenarios and OOD structures of instances. (2) Only a few-shot method does not fully unlock the model's

Dataset Name	Size	Demo Source	Avg. #tokens of Query	Avg. #tokens of Demo	Avg. #tokens of Context (Few-shot)
OOD-Toolset	1057	Same tool, different sub-APIs	35.5	53.8	496.0
GSM8K	1319	Manually created outliers	59.0	136.8	526.1
MATH	1000	Same level, different subjects	69.1	291.9	1002.1

Table 1: Statistics of three datasets in the OOD setting.

Prompting Method	OOD-Toolset		GSM8K	MATH	Average
	Exact Acc	Part Acc	Acc	Acc	
Zero-shot	64.5	68.4	75.0*	33.0*	60.2
Zero-shot + CoT	66.1	70.9	75.8*	33.9*	61.7
Few-shot	71.9	76.6	76.2	35.1	65.0
Self-ICL (Zero-shot)	67.0	71.1	76.6	34.6	62.3
Self-ICL (Few-shot)	71.5	76.0	78.0	**37.9**	65.9
Analogical Prompting (Zero-shot)	67.8	72.0	77.8*	37.3*	63.7
Analogical Prompting (Few-shot)	71.1	75.4	75.7	36.3	64.6
SELF-DEMOS (ours)	**75.1**	**79.4**	**78.2**	**37.9**	**67.7**

Table 2: Main results of different prompting methods on three datasets. All the results are with GPT-3.5-Turbo. The best performance for each task is in **bold**. The (*) indicates that results are from Yasunaga et al. (2023).

capability. In contrast, the methods with demo generation, especially SELF-DEMOS, present superior performance, underscoring their potential to serve as a reliable prompting strategy in OOD scenarios. (3) Self-ICL, which generates Q&A separately, serves a similar purpose to our Best-of-N Sampling step by enhancing the accuracy of generated demos. Thus, it yields performance that is closest to our method. However, this framework may also lead to mismatches of Q&A pairs, i.e., the model fails to answer the questions it generates, which may affect subsequent responses. (4) Seed demos bring little benefit to the Analogical Prompting method and may even be harmful. This could be because the additional demos are irrelevant to the instructions of analogical reasoning, which require the model to do multiple tasks. The seed demos fail to guide the model in different tasks and may distract the model from the whole process.

4.4 Ablation Study

Table 3 presents the results of our ablation study. We compare a range of pre- and post-processing methods and their influence.

Pre-processing Methods. We performed the following settings: no pre-processing before generating demos, directly answering the query before generating, and query understanding before generating.

Pre- & Post-processing Method	OOD-Toolset
w/o Pre-processing	72.9 / 77.5
+ Directly Answering	72.3 / 77.0
+ Query Understanding	**75.1 / 79.4**
w/o Post-processing	74.1 / 78.7
+ Self-Critique	74.3 / 78.8
+ Best-of-N Sampling	**75.1 / 79.4**
+ Best-of-N Sampling & Self-Critique	74.6 / 79.0

Table 3: Ablation study of pre- & post-processing methods on **OOD-Toolset**. The upper rows show the impact of different pre-processing steps, with the other steps remaining consistent with the original. The following rows show the impact of post-processing steps, again keeping all other steps consistent with the original.

The result shows that either no pre-processing or directly answering will compromise performance. Notably, the absence of pre-processing tends to yield homogenous outputs despite our introduction of randomness, potentially due to the model's challenge in reconciling the demanded relevance and diversity. Direct answer generation also diminishes performance, as initial errors propagate, leading to more erroneous or ambiguous answers in subsequent steps. Hence, a robust pre-processing strategy enhances model performance by ensuring diverse and correct initial responses.

Post-processing Methods. We performed the following settings: no post-processing after generating two demos, self-critique after generating two, sampling the best two demos after generating five, and self-critique after sampling. In the self-critique step, we prompt the model to verify and refine the D_{gen} or D_{TopK} according to the same criteria C. However, the result indicates that LLMs are no better at verifying their own outputs, echoing the findings of Stechly et al. (2023). This also discourages us from constantly improving the quality of demos through iterative verification.

5 Discussion

5.1 Consistency when Model Scaling

Figure 3 presents the results on varying sizes of the foundation model, ranging from Llama-2-7B-Chat to Llama-2-70B-Chat. According to the results, analogical reasoning did not work on smaller models, likely due to their limited capacity to follow hard instructions. The Self-ICL method encountered similar issues, with the small models' inability to provide accurate demos compromising their effectiveness. In contrast, our method, which incorporates extra processing steps around demo generation and lowers the task difficulty, proved more adaptable even when the model is weaker (∼10B parameters). It suggests that our approach can be more effective for resource-limited or mobile scenarios.

5.2 Effectiveness Toward Complex Tasks

In the main results, we can observe that both Self-ICL and SELF-DEMOS have shown a considerable improvement on the most challenging MATH datasets. This may suggest that the methods of generating demos in advance are more effective for complex tasks, as we will detail here.

Table 4 presents the full results on the MATH dataset across different complexity levels. Analogical Prompting, as a single-step prompting method, is most effective for simple problems, showing an entirely different trend from the other methods. This aligns with our previous analysis that high model ability is required for analogical reasoning. In contrast, Self-ICL and our method significantly gain in more complex problems. With its greater focus on the relevance and correctness of demos, SELF-DEMOS outperforms others in solving the most difficult level 5 problems.

Level	Prompting Method			
	FS	Self-ICL + FS	Analog + FS	SELF-DEMOS
1	70.2	71.3 (↑ 1.6)	**80.9** (↑ 15.2)	74.5 (↑ 6.1)
2	58.9	61.9 (↑ 5.1)	**63.1** (↑ 7.1)	58.3 (↓ 1.0)
3	37.4	38.7 (↑ 3.5)	**39.9** (↑ 6.7)	39.1 (↑ 4.5)
4	28.0	**34.7** (↑ 23.9)	24.0 (↓ 14.3)	**34.7** (↑ 23.9)
5	12.4	13.8 (↑ 11.3)	11.6 (↓ 6.4)	**14.6** (↑ 17.7)

Table 4: Evaluating prompting methods on the **MATH** dataset at different complexity levels. The **Level** corresponds to problem complexity, with higher values indicating greater difficulty. The percentage of performance improvements / declines compared to the few-shot method (FS) is denoted by (↑) / (↓).

5.3 Comparing with Demo Retrieval

A key motivation for our idea is to provide relevant demos for problem-solving, without using an external retriever or demo library. So, is our approach comparable enough to retrieval-based solutions? To answer this question, we created two baselines that retrieve exemplars relevant to the given query from external data (i.e., the training set of GSM8K and MATH, which includes labeled Q&A pairs). Table 5 shows the results of these methods on two math datasets.

Undoubtedly, the retrieval-based methods perform well, with the dense retriever achieving the highest scores due to its effective representation of latent semantics (Karpukhin et al., 2020). Besides, SELF-DEMOS also shows competitive performance, especially on the MATH dataset. This could be due to more complex questions in the MATH dataset, resulting in intricate semantic connections that cannot be easily captured by a statistical algorithm like BM25 (Robertson et al., 2009). In contrast, the GSM8K dataset has more uniform and centrally distributed questions, making it more suitable for retrieval-based approaches. Overall, our approach can still be a good option when resources are limited and retrieval is less feasible.

5.4 Number of Demonstrations Matters

We examine the impact of varying the number of self-generated demos (N) and selected demos (K) in the tool-using task. The details are shown in Figure 4a. Notably, the model performs better when selecting two demos. We suspect that a singular demo is insufficient to grasp all using patterns of an API. Additional samples ($K = 3$) may introduce noise and instabilities and hinder model learning. Our configuration ($K = 2, N = 5$) not only maximizes accuracy but also ensures efficiency in com-

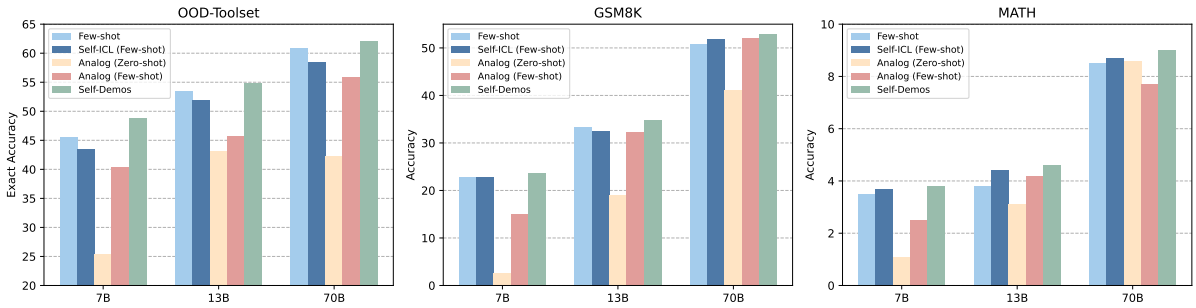
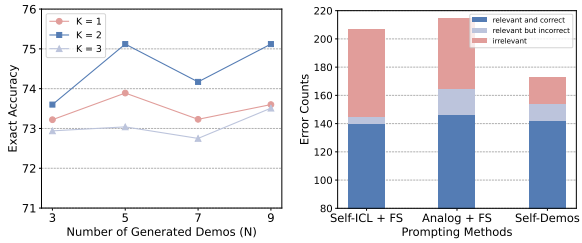


Figure 3: Performance comparison on Llama-2-Chat model family. SELF-DEMOS consistently improves performance across multiple model sizes from 7B, 13B to 70B parameters.

Demonstrating Method	Dataset	
	GSM8K	MATH
Demo Retrieval (Sparse)	79.5	37.0
Demo Retrieval (Dense)	**79.7**	**38.1**
Demo Generation (SELF-DEMOS)	78.2	37.9

Table 5: Comparison with demo retrieval methods on the **GSM8K** and **MATH** datasets. The (Sparse) means sparse retrieval using the BM25 algorithm, and the (Dense) means dense retrieval using `text-embedding-ada-002` API to generate sentence embedding and apply cosine similarity. Both baselines retrieve the Top 5 similar samples from the training set as demonstrations.



(a) (b)

Figure 4: (a) Comparison of the method with varying numbers of self-generated demonstrations (N) and selected training exemplars (K). (b) Error distribution of different methods. Demos yielding incorrect answers can be categorized into three types based on relevance and accuracy. Both results are on the **OOD-Toolset**.

putational costs. In our experiments, we further observed a tendency for the model to preferentially select demos positioned towards the front, indicating the phenomenon of position bias (Ko et al., 2020; Nori et al., 2023).

5.5 Error Analysis

Furthermore, we manually analyze the errors of SELF-DEMOS, comparing with the two baselines of demo generation. Errors were categorized into three distinct types: (1) **Irrelevant demos**: These exemplars are generated in a similar distribution and fail to interpolate between seed demos and given queries. (2) **Relevant but incorrect demos**: This category includes syntactical errors and redundant or inaccurate parameters. The issues contribute to false information propagation and interfere with the final output. (3) **Relevant and correct demons**: Even with correct demonstrations, errors can occur due to the model's inherent limitations and the generalization gap. Based on Figure 4b, all three methods have similar results in Category 3 with approximately 140 errors. However, SELF-DEMOS stands out by greatly lowering the errors in the first two categories. This suggests that SELF-DEMOS is better at generating relevant exemplars, which improves generalization across novel and unseen tasks.

6 Conclusion

This paper focuses on addressing the challenge of out-of-demonstration (OOD) queries in few-shot learning scenario. We present a novel prompting method, SELF-DEMOS, which elicits the OOD generalizability in LLMs by generating query-aware demos. Our method strategically interpolates between existing demonstrations and the OOD queries, effectively transforming them into in-demonstration (ID) queries. In an OOD setting, SELF-DEMOS achieved state-of-the-art results on the proposed OOD-Toolset and two public mathematical benchmarks. For future works, we aim to explore the scalability of the SELF-DEMOS method across diverse domains and to integrate unsupervised learning techniques to refine the quality of generated demos further.

Limitations

We summarize the limitations of our method as follows: (1) SELF-DEMOS is designed to resolve the out-of-demonstration queries, which can steadily improve downstream task performance, but the process involves additional costs. Users can trade off based on the task scenario. In addition, most of our prompts in different steps remain constant and can be orthogonalized with techniques such as prompt compression to save overhead. (2) Our method has some requirements for the model's ability. Although we have done empirical experiments and demonstrated our method is effective on small models ($\sim$10B parameters), it still requires models to have a certain degree of instruction following ability.

Ethics Statement

In this paper, we have followed ethical standards and principles to ensure the accuracy and validity of our research. The dataset was manually cleansed to ensure the removal of any sensitive or personal information. The human-annotated data is collected and used in compliance with relevant ethical guidelines. During the data construction process, we followed ToolAlpaca's terms under the Apache License 2.0 (Tang et al., 2023).

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Appendix

A Details of OOD-Toolset

The raw data from ToolAlpaca (Tang et al., 2023) including the training and testing sets, comprises

468 tool APIs and 4,369 tool-use cases. Due to the lack of verification of content generated by GPT-3.5, the toolset may have specific errors, such as empty values, outdated information, and incomplete data. To address these issues, we implemented a data cleansing process in the following steps:

Rule-based Cleaning We structured the raw data into a dictionary with keys for `Name`, `Description`, `Function_Description`, and `Instances`. `Name` identifies the tool and `Description` outlines its purpose. `Function_Description` clarifies the API calls and parameter interfaces, `Instances` consists of user queries and corresponding function call lists.

- We filtered entries lacking function descriptions, not following JSON format, and with more than three function calls due to complexity.
- To enhance the relevance and quality of our dataset, we filtered entries not directly related to the main function and tools with two or fewer instances or functions.
- We removed unused functions to reduce redundancy and noise.

After rule-based cleaning, a total of 322 tools and 2,788 instances remained.

Manual Data Cleaning In our single-turn calling scenarios, essential information for function calls needed explicit mention in the query. Our data cleaning process involved:

- The query should identify the subject clearly and avoid ambiguous pronouns and terms, such as 'today' or 'tomorrow' to prevent confusion.
- We checked and corrected logical errors in the data, such as incorrect function call.
- We confirmed the consistency of parameter values with their data types as defined in the function specifications.

After the second cleaning round, the dataset comprised 321 tools and 2,625 instances.

Query and Demonstration Construction After conducting two rounds of data cleaning, we proceeded to generate queries and corresponding demonstrations. Instance difficulty correlates with the length of its function calls and parameter lists. We ranked each tool's instances by length, choosing the longest as our query. Then, we randomly chose three instances that perform different functions to demonstrate. We aimed to conduct four queries for each tool, excluding instances with insufficient functional diversity.

Following this process, we obtained a final set of 1,057 queries, forming our testing set. Table 6 presents an example of OOD-Toolset.

API Name: Map
Description: Map API is used for calculating distances, planning routes, and locating points.
Usage specifications: DISTANCE: Calculate the distance between two points. Parameters: {"start": "Required. String. The starting point for the distance calculation.", "target": "Required. String. The destination point for the distance calculation."} ROUTE: Generate a travel route between two points. Parameters: {"start": "...", "target": "..."} SEARCH: Locate nearby points within a set distance. Parameters: {"target": "...", "position": "...", "distance": "..."}
Tool-use Cases: Query: How can I go from Beijing to Shanghai? Function call: ROUTE(start="Beijing", target="Shanghai") Query: How many shops are around Times Square in 3km? Function call: SEARCH(target="shop", position="Times Square", distance="3km") ...

Table 6: An instance of OOD-Toolset, composed of four parts: API name, description, usage specifications, and tool-use cases.

B Prompt Templates

Table 7, 8, 9, and 10 present the prompt templates of SELF-DEMOS for each step in tool-using tasks. Table 11, 12, 13, and 14 present the prompt templates of SELF-DEMOS for each step in mathematical problem-solving tasks.

The {tool_name} API is used for {description}. In this task, you need to give a general understanding of the user query and determine which function should be called to solve the query.

 # Tool Specification:
{specification}

 # User Query:
{query}

 # Instruction:
Generate a general understanding here. In particular, you need to explicitly indicate the name of the function that should be called.

Table 7: Prompt template for Query Understanding (Step 1) on the OOD-Toolset.

The {tool_name} API is used for {description}. In this task, you need to give an example of when to use the API based on the specification.

 # Tool Specification:
{specification}

 # Demonstration:
{minimal_demos}

 # Instruction:
Generate an example of how to use the {function_mentioned_in_step1} function.
- After "Query: ", describe the user query.
- After "Function Calls: ", give the function calls in the format of ["function_name(parameter=value)"].

Table 8: Prompt template for Query-aware Demo Generation (Step 2) on the OOD-Toolset.

The {tool_name} API is used for {description}. Here are some examples of how to use the API. In this task, you must check the examples for correctness and select one or two best examples to keep.

 # Tool Specification:
{specification}

 # Check List:
- Syntax errors: the function calls should conform to the format like "function_name(parameter=value)".
- Redundant parameters: the function calls must conform to the parameter list in the tool specification.
- Value passing errors: the values of parameters should be of the correct type and reasonable.
- Unsolvable errors: the query should be solvable with the given function.

 # Examples to be Checked:
{generated_demos}

 # Instruction:
Select one or two best examples to keep. If there are not enough correct examples, just keep one.
For your output:
- After "Selection: ", give the serial numbers of your choice in the format of <x>, <y>.
- After "Explanation: ", give the reason why you keep the examples.

Table 9: Prompt template for Best-of-N Sampling (Step 3) on the OOD-Toolset.

The {tool_name} API is used for {description}. In this task, you must generate the function calls for a given query.

 # Tool Specification:
{specification}

 # Demonstration:
{minimal_demos}
{selected_demos}

 # Instruction:
Solve the following user query.
Query: {query}
Function calls: Give your answer in the format of ["function_name(parameter=value)"].

Table 10: Prompt template for Response Generation (Step 4) on the OOD-Toolset.

In this task, you need to give a general understanding of mathematical problems, which can be applied to all similar questions in the same scenario.

 # Problem:
{question}

 # Instruction:
Give a general understanding of this problem in one line. Highlight the general solution methodologies to solve this type of problem. Focus on the problem-solving approach without delving into specific numerical values or answers.
You can refer to this template for your understanding: This problem involves...To solve this type of problem...

Table 11: Prompt template for Query Understanding (Step 1) on the GSM8K and MATH datasets.

In this task, you need to recall mathematical problems. When presented with a math problem, recall another relevant problem as an example. The example should help answer the initial problem.

 # Problem:
The initial problem:
{question}

The understanding you can refer to:
{understanding}

Demonstration:
{minimal_demos}

 # Instruction:
Recall one example of a math problem relevant to the initial problem. The example should be distinct from the initial problem (e.g., involving different numbers and names).
- After "Question: ", describe the problem you generate in one line.
- After "Answer: ", Explain the step-by-step solution and enclose the ultimate answer in \boxed{}.

Table 12: Prompt template for Query-aware Demo Generation (Step 2) on the GSM8K and MATH datasets.

In this task, you need to check the correctness of these math Q&A pairs and select one or two best examples to keep for answering the initial problem.

 # The initial problem:
`{Question}`

 # Check List:
- The calculation process in the solution must be correct and without ambiguity.
- The examples should be relevant and helpful in solving the initial problem.

 # Examples to be checked:
`{generated_demos}`

 # Instruction:
Select one or two best examples to keep. If there are not enough correct and helpful examples, just keep one.
For your answer:
- After "Selection: ", give the serial numbers of your choice in the format of <x>, <y>.
- After "Explanation: ", give the reason why you keep this example.

Table 13: Prompt template for Best-of-N Sampling (Step 3) on the GSM8K and MATH datasets.

Your task is to tackle mathematical problems step by step. You can refer to these demonstrations to give your reasoning process.

 # Demonstration:
`{minimal_demos}`
`{selected_demos}`

 # Instruction:
Solve the following problem step by step.
Question: `{Question}`
Answer: Explain the step-by-step solution and enclose the ultimate answer in \boxed{} here.

Table 14: Prompt template for Response Generation (Step 4) on the GSM8K and MATH datasets.