Using Extractable Symbolic Programs to Evaluate Mathematical Reasoning

Abstract

Existing math datasets evaluate the reasoning abilities of large language models (LLMs) by either using the final answer or the intermediate reasoning steps derived from static examples. However, the former approach fails to surface model's uses of shortcuts and wrong reasoning while the later poses challenges in accommodating alternative solutions. In this work, we seek to use symbolic programs as a means for automated evaluation if a model can consistently produce correct final answers across various inputs to the program. We begin by extracting programs for popular math datasets (GSM8K and Math) using GPT4-o. For those executable programs verified using the original input-output pairs, they are found to encapsulate the proper reasoning required to solve the original text questions. We then prompt GPT4-o to generate new questions using alternative input-output pairs based the extracted program. We apply the resulting datasets to evaluate a collection of LLMs. In our experiments, we observe significant accuracy drops using our proposed evaluation compared with original static examples, suggesting the fragility of math reasoning in state-of-the-art LLMs.

1 Introduction

Mathematical reasoning is a fundamental skill essential for numerous complex applications, leading to a recent growing research effort on advancing large language models (LLMs) in this area. Thus, proper evaluation of LLMs' mathematical reasoning is crucial. Most previous studies have primarily evaluated LLMs using static datasets, such as GSM8K (Cobbe et al., 2021) and MATH (Hendrycks et al., 2021). Typically, evaluations focus solely on the final answers, overlooking reasoning flaws (Lewkowycz et al., 2022) and potential data contamination issues. Despite impressive results, LLMs can reply on shortcuts rather than true reasoning, displaying high sensitivity to input

tokens (Li et al., 2024b,a). Alternatively, some works (Sawada et al., 2023; Golovneva et al., 2023) use model-based techniques to assess the reasoning quality, but these can suffer from model biases, limiting accommodation for alternative solutions.

In this paper, we present a focused study on evaluating mathematical reasoning which can be concisely encapsulated by symbolic programs, *i.e.,* Python programs. For such cases, we can automatically generate a diverse set of new test cases (input-output pairs) by varying the valid inputs fed into the program. Thus, if LLMs truly employ the appropriate reasoning process (as embodied by the programs) to solve the original question, they should also be able to consistently solve all new test cases. This approach allows us to evaluate the reasoning quality directly by examining the final answers, without ruling out alternatives.

To avoid costly manual annotations, we use the state-of-the-art LLM (GPT4-o) to generate Python programs for GSM8K and MATH. We retain only those questions with *extractable* programs, which can be automatically validated for our evaluation. This means the programs can be executed to produce the original gold answers. Upon manual inspection, 92% and 83% of the programs from GSM8K and MATH genuinely demonstrate the correct reasoning process required to solve the original questions. We then prompt GPT4-o to propose alternative valid inputs based on the extracted program and the original question. These inputs are then used to generate new input-output pairs derived from the program. Finally, GPT4-o is tasked to update the original question using these proposed inputs to create new test cases for evaluation.

Our experiments show that model performances drop drastically when evaluated on perturbed questions. For example, on original questions that GPT-4-Turbo answers correctly, only 48% of the time, the same model can answer all perturbed questions correctly, too. This suggests that GPT-4-Turbo, one

Figure 1: Pipeline of ReasonAgain, and a running example perturbed by ReasonAgain.

of the most capable large language models available, only truly understands the reasoning paths of less than half of the math questions. In other words, we show that existing evaluation methods on math questions are over-optimistic, and our proposed ReasonAgain is a better alternative.

2 Methods

Assessing the reasoning capabilities of large language models (LLMs) presents significant challenges, primarily because the reasoning process is not consistently articulated, and standardizing its representation is difficult. Moreover, multiple reasoning paths may exist to arrive at the same solution. Consequently, it is impractical to simply output the reasoning process and evaluate its correctness directly. Typically, the accuracy of reasoning is assessed through question-answering formats, such as verifying the accuracy of an answer to a mathematical problem. However, this paper contends that relying solely on a single question-answer pair is inadequate for genuinely assessing reasoning capabilities because: 1) an incorrect reasoning path may coincidentally yield the correct answer, and 2) potential data contamination could enable models to memorize answers without engaging in a legitimate reasoning process. To effectively evaluate the reasoning abilities of LLMs, we introduce ReasonAgain, which conceptualizes the reasoning process within Python code and automatically generates five additional perturbations of

the same question. These perturbations retain the original reasoning process but feature different input values, thereby testing whether the model genuinely employs a correct reasoning process. The pipeline of ReasonAgain is illustrated in Figure 1.

Encapsulating the reasoning process. To explicitly represent the reasoning process of a math question, we first ask the pivot LLM to generate the parameters of questions.

> **Generate Parameters of the Question**
>
> Identify numerical values in the given question, then replace some of them with Python parameters that are either int or float, so that the resulting abstract question is still answerable with the same general solution as the original question. Follow the the provided examples.
>
> {Few-shots examples}
>
> {Question}

Then we use the generated parameter names to replace all the values in the question, and ask the LLM to generate a Python function that uses the generated parameters as the input to solve the question.

> **Generate Python Function of the Question**
>
> Write a Python program to solve the given abstract math question. Your program must contain a function called 'answer' that accepts the input parameters as specified in the question.
>
> {Few-shots examples}
>
> {Question with parameters.}

After generating Python code for all the ques-

tions, to ensure the quality of the code, we first filter out all the code that cannot be compiled. Then we run the code by inputting the original parameter values, and we only keep the code that can output the correct answer.

Generate the perturbations of the question. To generate the perturbations of the question, we first ask the model to generate 5 kinds of new parameter values given the original parameters using the following prompt.

Prompt for Generating Alternative Parameter Values

Here is a math question with the parameter and parameter values. Please perturb the value of parameters into different values. Output five kinds of new values in the same format as the given parameters in five lines without index.

Question: {Question}

Parameters: {Parameters}

After getting the new parameter values, we ask the model to update all the values in the question to generate the corresponding new questions.

Prompt for Generating New Questions

Here is a math question with old parameter values, and five kinds of new parameter values. Please rewrite the question five times to update all the parameters from old value to each corresponding new value in five lines without index.

Question: {Question}

Old Parameters: {Parameters}

New Parameters: {New Parameters}

New Questions:

To get the answers for each new questions, we run the Python code for each set of new parameter value, and use the output of the code as the gold answer. To examine the robustness of models' reasoning capability, we ask the models to answer the new questions, and compare the output with the gold answer.

3 Experiments

3.1 Experiment Settings

Datasets. We sample 2k questions from GSM8k (Cobbe et al., 2021) and 1k questions from MATH (Hendrycks et al., 2021). As discussed in Section 2, we first ask the model to generate the Python code for each question, and then we filter out all the problematic code that cannot be compiled or fail to return the correct gold answer. After filtering, in total, we have 1121 cases from GSM8k, and 268 cases from MATH. For each case, we use `ReasonAgain` to generate 5 perturbations as

the new test cases, which gives us 5605 cases for GSM8k, and 1072 cases for MATH. We use GPT-4o (OpenAI et al., 2024) as the pivot LLM to generate all the parameters, code, and perturbations.

Baselines. We evaluate 4 LLMs in this paper: GPT-4-Turbo (OpenAI et al., 2024), GPT-4o (OpenAI et al., 2024), LLama-3.1-8B (Dubey et al., 2024), and Qwen-2.5-7B (Team, 2024) using the following different settings: direct, few-shot Chain-of-thought (CoT) (Wei et al., 2022), and few-shot Chain-of-thought + self-consistency (CoT+SC) (Wang et al., 2022).

Direct: We ask the model to directly answer the question without providing any examples using the following prompts.

Prompt for Generating Alternative Parameter Values

Answer the math question below. Only output the answer without units and any context words.

Question: {Question}

Answer:

Few-shot CoT: We follow the same CoT template and the same 8-shot math examples from Wei et al. (2022). Temperature is set to 0.

Few-shot CoT+SC: Following Wang et al. (2022), temperature is set to 0.7, and we run each query 5 times. The majority of the outputs will be used as the final answer.

Evaluation Metrics. We report Exact Match accuracy (EM) for all the experiments. Predicted answers are parsed by CoT format, and we round both gold answers and predicted answers before checking if the values are same.

3.2 Main Results

We show our main experiment results using our proposed `ReasonAgain` evaluation pipeline in Fig. 1. We observe a substantial performance drop across all models on both GSM8K and MATH. For direct inference, models drop 10%-15%, regardless of model sizes and capabilities. Such a drop is not mitigated by chain-of-thought and self-consistency inference methods, where we observe a similar 10% to 20% drop after our perturbation. In the normalized accuracy results, we show that models often demonstrate false hopes in their performances: they only answer 50% to 80% of the perturbed questions correctly on the questions they initially answered correctly. A more concerning finding is that models only truly understand at most half of

Model	Prompt	GSM8K					MATH				
		Accu.		Normalized Accu.			Accu.		Normalized Accu.		
		Before	After	Before	After	% of Correct	Before	After	Before	After	% of Correct
Llama3.1-8B	Direct	21.59	7.05	100	34.27	5.39	20.88	14.30	100	32.31	9.62
	CoT	88.26	69.62	100	75.31	48.63	71.49	44.02	100	54.04	33.71
	CoT+SC	85.75	68.01	100	71.95	39.92	69.48	43.13	100	53.06	25.43
Qwen2.5-7B	Direct	38.44	22.20	100	42.78	13.29	35.34	19.52	100	38.41	13.64
	CoT	60.04	49.48	100	63.79	30.44	38.96	25.30	100	46.19	17.53
	CoT+SC	61.23	50.12	100	45.97	29.66	40.56	26.43	100	44.95	16.83
GPT4o	Direct	66.57	52.93	100	72.89	48.86	57.83	37.27	100	56.25	36.11
	CoT	93.73	75.68	100	**79.52**	**58.80**	84.34	**50.76**	100	55.62	34.29
	CoT+SC	94.44	74.87	100	78.05	55.12	82.33	50.36	100	55.41	27.80
GPT4-Turbo	Direct	45.43	35.04	100	56.13	26.63	47.39	31.16	100	45.76	22.88
	CoT	54.75	43.49	100	70.02	48.12	36.14	28.19	100	**61.78**	**42.22**
	CoT+SC	51.52	40.95	100	71.23	50.09	55.02	37.59	100	55.62	32.85

Table 1: Performance of LLMs on GSM8K, MATH and corresponding perturbations generated by `ReasonAgain`. "Normalized Accu." refers to the performance on the subset of the test cases that the model answers correctly before perturbation. "Before" refers to the performance on the original dataset. "After" refers to the performance on the perturbations. "% of Correct" refers to the percentage of the cases that the model solves all the perturbations correctly.

the questions, and sometimes even less than 30%, as suggested by the "% of Correct" results. Combining these findings, we argue that `ReasonAgain` is an effective method for evaluating the true capabilities of models on mathematical reasoning, and current models' performances are overestimated by previous evaluation methods.

3.3 Human Evaluation

To evaluate if the generated code is reliable, we sample 200 cases from GSM8K and MATH (100 each), and ask three human experts to annotate the correctness of the generated perturbations of these 200 cases. The annotators are asked to understand the generated code, and check the correctness of the gold answers of perturbations. We observe 8 of the 100 cases from GSM8K and 17 of the 100 cases from MATH are problematic, mainly because some positive parameters being negative or the model cannot generate the correct code.

4 Related Work

Many works have discussed language model bias and inconsistency during reasoning (Li et al., 2024b,a; Zhou et al., 2024) and adversarial and contrastive evaluation (Gardner et al., 2020; Patel et al., 2021; Yu et al., 2024). To this end, our work provides a novel way for automatic mathematical consistency evaluation. At the same time, while some works have decomposed methods to solve or evaluate math questions (Hao et al., 2023; Madaan et al., 2023; Gao et al., 2023; Xia et al., 2024), our work points out that better language modeling is also needed to achieve consistent reasoning.

5 Conclusion

In this work, we propose `ReasonAgain`, a novel evaluation method to benchmark large language models' true capabilities on mathematical reasoning. `ReasonAgain` employs a programmatic perturbation method that changes the numbers in the original math questions and derives the corresponding gold answers. We then evaluate models on such perturbed questions. Experiments show that all models perform drastically worse on these perturbed questions, suggesting that 1) existing models do not truly understand the reasoning process of math questions, even though they sometimes predict the correct answer; 2) existing evaluation methods are inadequate, and current perceptions of model performances on math reasoning are over-optimistic. `ReasonAgain` can be the better alternative for evaluating model reasoning capabilities.

Limitations

Our work has several limitations.

Imperfect Programs. As pointed out in §3.3, some mistakes exist in the current generated programs, which leads to partially incorrect gold labels in some perturbed questions. We will explore better filtering mechanisms in later versions. However, such mistakes do not impact our overall conclusion, as model performances are much lower than the upper bounds.

Limited Program Coverage. Our program generation is limited by a conceptualization process proposed in Zhou et al. (2024), which does

not work well on certain types of math questions, such as geometry-related ones. As a result, ReasonAgain only works on a subset of all existing math questions.

Limited Reasoning Types. Our general formulation can be applied to other reasoning types, such as multiple-choice questions. However, we only focus on math questions in this work.

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