PANOPTAG: Simultaneously Tagging All Jets in a Particle Collision Event

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Abstract

Jet tagging, identifying the origin of jets produced in particle collisions, is a critical classification task in high-energy physics. Despite the revolutionary impact of deep learning on jet tagging, the paradigm has remained unchanged: jets are classified independently, one at a time. This approach ignores correlations, overlaps, and wider event context between jets. We introduce PANOPTAG, which simultaneously tags all jets in an event using an encoder-decoder architecture where jet kinematics serve as queries that cross-attend to particle flow object embeddings. We evaluate PANOPTAG on heavy-flavor (b/c)-tagging and demonstrate significant performance improvements over state-of-the-art single-jet baselines, while maintaining the topology independence required for conventional calibration techniques.

1 Introduction

Particle colliders, such as the Large Hadron Collider (LHC) at CERN, accelerate beams of protons to nearly the speed of light and bring them to collide tens of millions of times per second. Each collision event produces complex sprays of outgoing particles that traverse a layered detector system [3, 12] used to reconstruct particle trajectories, momenta, energies, and identities.

A central object in this reconstruction chain is a jet [42, 39], a collimated spray of particles originating from quarks or gluons. Jets are ubiquitous in collider analyses and as such determining the origin of each jet, dubbed jet tagging, is a key classification task that underpins both precision measurements and searches for new physics. A jet is naturally represented as a variable-size set of its reconstructed constituent particles, called particle flow objects (PFOs). Modern deep learning methods [16, 36] that operate directly on low-level constituent PFOs have become standard, with the prevailing state-of-the-art treating jets as unordered sets or "particle clouds" [34].

Within this paradigm, Particle Flow Networks [21] adapted the Deep Sets [44] formulation, ParticleNet [32] introduced dynamic graph construction with EdgeConv from DGCNN [43], and the Particle Transformer (ParT) [34] uses attention augmented with pairwise kinematic information. Symmetry-aware models like LGATr [41, 7] incorporate Lorentz equivariance within the Geometric Algebra Transformer [8] framework. Alongside these, unsupervised [19], self-supervised [37], and fully-supervised pretraining methods [28, 14, 24, 6] have been explored for representation learning. In addition, both CMS and ATLAS collaborations at the LHC have deployed increasingly sophisticated deep-learning-based taggers [29, 1, 4], underscoring that continued progress in jet tagging is a key enabler for the LHC physics program.

In this work, we introduce PANOPTAG, a new paradigm that reframes jet tagging as an event-level, multi-jet inference problem. Instead of classifying each jet in isolation, PANOPTAG processes the full set of reconstructed jets and particles once with a DETR-inspired [11] encoder–decoder architecture, assigning labels to all jets simultaneously. A permutation equivariant backbone generates embeddings

Figure 1: A high-level overview of the PANOPTAG architecture. PFOs are processed through the Event Encoder to produce embeddings, which serve as keys and values in a cross-attention mechanism. Simultaneously, jet kinematics are passed through an MLP to produce jet embeddings that act as queries, with the outputs after classification heads predicting class labels.

for all PFOs in the event. Jet kinematics are then used as queries in a decoder that cross-attends to the particle embeddings, producing one latent representation per jet, which is mapped to label probabilities (Fig. 1). This design allows information to be shared coherently across jets, while letting each jet focus on the subset of particles most informative for its identity. Evaluated on heavy-flavor identification, PANOPTAG achieves remarkably higher performance than existing state-of-the-art single-jet baselines, with gains that generalize beyond topologies included in training.

2 Model Architecture

The model consists of an Event Encoder (EE) block that processes all PFOs to compute contextual embeddings, and a Jet Query Decoder (JQD) block that cross-attends per-jet kinematic embeddings to these PFO embeddings to produce per-jet classification logits.

2.1 Event Encoder Block

The EE combines local and global feature extraction. PFO input features $\mathbf{X} \in \mathbb{R}^{B \times N \times d_{\mathrm{in}}}$ are first projected to the model dimension d_h via an input MLP. Local geometric structure is captured through sequential EdgeConv [43] layers. The first layer constructs k-nearest neighbor graphs in the PFO coordinate space (pseudorapidity η and azimuthal angle ϕ). EdgeConv computes edge features as $\mathbf{e}_{ij} = [\mathbf{x}_j - \mathbf{x}_i, \mathbf{x}_i]$ for all $j \in \mathcal{N}_i$, passed through an MLP and aggregated via max pooling:

$$\mathbf{x}_i^{\mathrm{EdgeConv}} = \max_{j \in \mathcal{N}_i} \left(\mathrm{MLP}(\mathbf{e}_{ij}) \right). \tag{1}$$

Subsequent EdgeConv layers use Euclidean distances in the learned feature space. This hierarchical design is motivated by [22, 28], where incorporating local features is shown to improve performance. The addition of EdgeConv layers creates a latent representation that is better aware of distances and topology, which is important since PANOPTAG needs to both learn geometric correlations between particles and associate individual PFOs to jets.

Following local feature extraction, global context is captured through Induced Self-Attention Blocks (ISABs) from Set Transformers [23]. Each ISAB introduces learnable inducing points $\mathbf{I} \in \mathbb{R}^{M \times d_h}$, first attending to the full PFO set as $\mathbf{H} = \mathrm{MAB}(\mathbf{I}, \mathbf{X}^{\mathrm{local}})$, then PFOs attend back as $\mathbf{X}^{\mathrm{ISAB}} = \mathrm{MAB}(\mathbf{X}^{\mathrm{local}}, \mathbf{H})$. This reduces complexity from $\mathcal{O}(N^2)$ to $\mathcal{O}(MN)$, which is important since collision events can contain $\mathcal{O}(1000)$ PFOs. Each MAB implements scaled dot-product attention without positional encoding to ensure permutation equivariance, with residual connections and layer normalization [5]. Both local and global features are accumulated with skip connections.

2.2 Jet Query Decoder Block

The JQD generates per-jet predictions by cross-attending jet-specific query embeddings to the contextual PFO embeddings. Each jet is represented by its kinematic properties (p_{T}, η, ϕ, m),

	All Classes		*b*-jets		*c*-jets	
	Accuracy	AUC	$\text{Rej}_{50\%}$	$\text{Rej}_{80\%}$	$\text{Rej}_{50\%}$	$\text{Rej}_{80\%}$
ParticleNet	0.910	0.9742	10,003	194	157	18
ParT	0.913	0.9744	13,757	232	176	18
PANOPTAG	**0.9350 ± 0.0009**	**0.9787 ± 0.0007**	**18,087**	**383**	**252**	**24**

Table 1: Jet tagging performance on the heavy-flavor tagging dataset for all processes. Higher is better. Best results in **boldface**.

embedded via an MLP: $\mathbf{Z}_0 = \text{MLP}_{\text{jet}}(\mathbf{J})$, where $\mathbf{J} \in \mathbb{R}^{B \times M_{\text{jets}} \times 4}$. The decoder consists of L_{dec} cross-attention layers computing $\mathbf{Z}_{l+1}, \mathbf{A}_{l+1} = \text{MAB}(\mathbf{Z}_l, \mathbf{H}_c)$, with mask-aware attention to prevent attention to padded PFOs. A final classification head projects jet embeddings to per-class logits.

3 Heavy-Flavor Tagging Experiment

Existing jet-tagging benchmarks [18, 20, 33] provide data in a jet-centric format with no access to full event context. Since PANOPTAG operates at the event level, we simulate dedicated datasets.

3.1 Dataset

Samples are simulated with PYTHIA [40] for event generation, parton showering, and hadronization, and DELPHES [13] for detector simulation using the default ATLAS configuration. Jets are clustered from reconstructed PFOs via the anti-k_{T} algorithm [10] with $R = 0.4$ and $p_{\text{T}} > 20$ GeV using FASTJET [9, 38]. Unlike the ATLAS and CMS heavy-flavor tagging studies which consider only $t\bar{t}$ production, we also include single-top, tW, ZH, and $t\bar{t}H$ to ensure PANOPTAG does not memorize features of a particular topology. We train only on single-top, $t\bar{t}$, and $t\bar{t}H$, reserving ZH and tW for out-of-distribution validation. For each topology, we simulate 1M events, yielding ∼30M jets in three classes: light jets (55%), b-jets (33%), and c-jets (12%). The leading 128 PFOs and 10 jets are kept per event. Each PFO uses 14 input features spanning kinematics, particle identification, and trajectory displacement. The baselines use the same jets but with PFO constituents restricted to those used in jet clustering.

3.2 Setup

A training-validation-testing split of 750k-100k-150k events is used, with additional 150k ZH and tW events for testing. The nominal model contains 2 EdgeConv layers and 3 ISAB layers, with $d_h = 256$, $m = 48$ inducing points, $n_h = 32$ attention heads, $k = 20$ nearest neighbors, GELU [15] activations, and 3.42M learnable parameters. We use ADAMW [26] with weight decay 10^{-3} to minimize the weighted focal cross-entropy [25] loss with $\gamma = 1$. The learning rate warms up linearly over one epoch from 10^{-6} to 2×10^{-4}, followed by cosine annealing [27] with warm restarts every 15 epochs, training for 30 epochs with batch size 512. The model is implemented in PyTorch [30].

3.3 Baselines

We compare against ParticleNet [32] and ParT [34], using existing implementations from the WEAVER [31] framework. All models are trained end-to-end on the same dataset, with the same input features, optimizer, loss, and LR schedule. The key difference is that baselines input jets one-at-a-time with relative coordinates $(\Delta\eta, \Delta\phi)$.

3.4 Results

We report classification accuracy, AUC, and the background rejection $\text{Rej}_{X\%} \equiv 1/\text{FPR}$ at TPR = $X\%$, reported separately for each signal (b/c) jet category at operating points of 50% and 80%. Background rejection directly maps onto discovery sensitivity at the LHC: doubling it corresponds to an approximately 40% gain in discovery potential.

Figure 2: Background rejection versus b-jet (left) and c-jet (center-left) tagging efficiency for PANOPTAG, ParT, and ParticleNet, with ratio panels below. (Center-right) In-distribution ($t\bar{t}$) versus out-of-distribution (ZH) comparison. (Right) ΔR to nearest b/c jet for mistagged light jets compared to the inclusive distribution.

Table 1 and Fig. 2 summarize the results. PANOPTAG delivers the best performance on every metric, outperforming ParT by a wide margin. Overall accuracy increases by 2.2% and 2.5% compared to ParT and ParticleNet, respectively. For background rejection, PANOPTAG improves upon ParticleNet and ParT by a factor of 1.8 (2.0) and 1.7 (1.6) respectively for b-jets, and 1.6 (1.3) and 1.4 (1.3) for c-jets at 50% (80%) signal efficiency. The performance gains persist when evaluating on topologies not included during training: PANOPTAG maintains its improvement on the ZH process, demonstrating generalization beyond the training distribution.

To investigate the source of these gains, we study the $\Delta R \equiv \sqrt{\Delta\eta^2 + \Delta\phi^2}$ distance distribution of light jets to the nearest heavy-flavor jet. Relative to the inclusive spectrum, ParticleNet mistags are strongly biased toward smaller ΔR, indicating ambiguities when a light jet lies close to a true b/c jet and constituent overlap makes classification challenging. PANOPTAG shows a much smaller bias, following the inclusive distribution more closely, suggesting it suppresses proximity-driven mistags.

3.5 Calibration

Although jet classification is performed jointly within each event, compatibility with standard per-jet efficiency calibrations—typically derived from $t\bar{t}$ control samples—requires that per-jet flavour probabilities remain statistically independent. To validate this, we perform a perturbative test: for each event, a randomly selected b-jet and its associated PFOs are replaced by a light-flavour jet drawn from a cross-event cache, and model inference is re-evaluated. The resulting accuracy of 0.9348 and AUC of 0.9780 are consistent with Table 1 within training-seed uncertainties. Further tests of conditional independence of b-jet probabilities and compatibility with conventional calibration strategies is left to future work. This result is a natural consequence of the topology independence.

4 Discussion and Conclusion

We introduce PANOPTAG, a new paradigm presenting an event-level formulation of jet tagging. All jets in an event are simultaneously tagged by using each jet's kinematics as a learnable query that cross-attends to particle embeddings. On heavy-flavor tagging, PANOPTAG yields performance gains over state-of-the-art single-jet baselines while being topology-agnostic—enabling the standard approach of efficiency measurement and calibration using $t\bar{t}$ or $Z(\to \mu\mu)$ + Jets control samples.

These results support a broader conclusion: treating jets as a set of correlated objects and enforcing a shared event representation is a productive modeling direction, motivated by the physical reality that jets within an event are constrained by global energy-momentum conservation, characteristic production topologies, and even partial overlap. The PANOPTAG formulation is a general recipe that can be repurposed for pileup-jet identification [2], jet regression [17], background subtraction [35], and more, making it a candidate for a high-energy physics foundation model. The event-level perspective is also attractive from a fast-inference standpoint, as the particle representation is computed once per event and reused across all jets. Finally, PANOPTAG is compatible with alternative backbones (e.g. Lorentz-equivariant layers) and is a natural target for self-supervised pretraining with masking, denoising, or contrastive objectives; PANOPTAG improves upon state-of-the-art performance today, while providing a template for extending collider machine learning toward unified, event-level solutions for a broad class of jet analyses tomorrow.

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