Microlensing Detection and Inference via Learned Bayes Factors

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Abstract

We present a unified framework for gravitational microlensing event detection and parameter inference. Traditional pipelines use deterministic hard cuts on photometric statistics, systematically missing low-magnification events in the finite-source regime. We instead frame detection as Bayesian model comparison using Evidence Networks, which learn calibrated Bayes factors from binary-labeled simulations, and combine this with Neural Posterior Estimation (NPE) for amortized parameter inference. Both share a transformer encoder that handles irregularly-sampled time series without imputation. On simulated Roman Space Telescope data, our Evidence Network achieves 99.9% detection efficiency with no false positives among 5,000 Gaussian-noise realizations (a 95% upper bound on the false-positive rate of 6×10^{-4}). Gains are most dramatic in the extreme finite-source regime ($\rho \gtrsim 5$), where detection rates reach $\sim 95\%$ versus $\sim 50\%$ for hard cuts, precisely the short-duration free-floating planet events most constraining for formation scenarios. Our NPE provides calibrated posteriors, working towards real-time analysis at survey scale.

1 Introduction

The Nancy Grace Roman Space Telescope will survey over 200 million stars toward the Galactic bulge at 15-minute cadence, detecting $\sim$1,400 bound exoplanets [Penny et al., 2019] and $\sim$250 free-floating planets (FFPs) [Johnson et al., 2020] via gravitational microlensing, with lens mass and distance measurements achievable for a significant fraction of hosts [Terry et al., 2025]. FFPs are expected to outnumber bound terrestrial planets by a factor of 20 or more [Sumi et al., 2023], and the recent first direct mass measurement of an FFP via microlensing parallax [Dong et al., 2026] underscores the maturity of this technique. Characterizing the low-mass end of the FFP mass function requires sensitivity to short-duration, low-magnification events in the finite-source regime.

Realizing this science demands solving two coupled challenges: *detection* of microlensing signals amid billions of light curves, and *inference* of physical parameters for detected events. Current pipelines address these sequentially. Detection relies on deterministic *hard cuts*—threshold-based criteria such as $\Delta\chi^2 \geq 300$ with $N_{\text{consec}} \geq 6$ consecutive 3σ points [Johnson et al., 2020], or summed-significance variants [Sumi et al., 2011, Mroz et al., 2017]. Hard cuts are ad hoc, provide no probabilistic interpretation, and systematically miss low-magnification events. Inference then employs Markov Chain Monte Carlo (MCMC), which is computationally expensive and does not amortize across observations.

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Figure 1: Joint architecture for microlensing detection and inference. A shared transformer encoder processes irregularly-sampled light curves into a fixed-dimensional summary $\mathbf{s}$. The detection head outputs calibrated Bayes factors $\log_{10} K$ via Evidence Networks, while the inference head uses a masked-autoregressive normalizing flow to estimate the full posterior $p(\boldsymbol{\theta}|\mathbf{x})$.

We present a unified neural framework combining *Evidence Networks* [Jeffrey and Wandelt, 2024] for Bayes factor estimation with *Neural Posterior Estimation* (NPE) [Papamakarios and Murray, 2018, Greenberg et al., 2019] for amortized posterior inference. Both share a transformer encoder for irregularly-sampled time series. Prior work has applied NPE to binary microlensing [Zhang et al., 2021], transformer embeddings for single-lens inference on irregular time-series data [Smyth et al., 2025], and normalizing flows with reversible-jump MCMC for microlensing model selection [Keehan et al., 2022]. Our framework extends these by unifying detection and characterization without requiring MCMC at inference time.

Our key contributions are: **(i)** a unified probabilistic framework performing both detection and inference within a Bayesian formalism; **(ii)** principled model comparison via Evidence Networks that recover calibrated Bayes factors from binary labels alone, replacing ad hoc $\Delta\chi^2$ thresholds; and **(iii)** improved detection completeness in the finite-source regime ($\sim$95% vs. $\sim$50% for hard cuts), where short-duration FFP events are most prevalent.

2 Method

Data and augmentation. We model finite-source point-lens (FSPL) microlensing events with five parameters $\boldsymbol{\theta} = (t_0, u_0, t_E, \rho, f_s)$: time of closest approach, impact parameter (in units of the Einstein radius θ_E), Einstein crossing time, normalized source radius $\rho \equiv \theta_s/\theta_E$ (where θ_s is the angular source size), and source flux fraction f_s such that the observed flux is $F(t) = f_s A(t, \boldsymbol{\theta}) + (1 - f_s)$ with A the magnification and $1 - f_s$ the blended light from unresolved stars. We adopt box-uniform priors: $t_0 \in [0, 20]$ days, $u_0 \in [0, 1.5]$, $\log_{10}(t_E/\text{day}) \in [-1, 1.3]$, $\log_{10} \rho \in [-2, 1]$, $f_s \in [0.1, 1.0]$. Light curves are simulated using VBMicrolensing [Bozza et al., 2018] at Roman's 15-minute cadence over a 20-day window. To build robustness, we apply on-the-fly augmentation: 0–3 seasonal gaps (1–10 days each), random dropout (0–60%), and Gaussian noise ($\sigma \in [0.001, 0.02]$). Each light curve is represented as a padded sequence of length $L = 1000$ with three channels per timestep: $(t_i^{\text{norm}}, F_i, \sigma_i)$. We apply recoverability filters to exclude unrecoverable events: at least 5 points within $1.5\, t_E$ of t_0, at least 5 points beyond $3.0\, t_E$ from t_0 (for baseline establishment), and peak signal-to-noise ratio > 5.

Shared transformer encoder. Both the Evidence Network and NPE share a transformer encoder [Vaswani et al., 2023] that maps variable-length input $\mathbf{X} \in \mathbb{R}^{L \times 3}$ to a fixed summary $\mathbf{s} \in \mathbb{R}^{256}$ (Figure 1). The architecture consists of an input projection, sinusoidal positional encoding, and 6 transformer layers with 8-head self-attention ($d_{\text{model}} = 256$, $d_{\text{ff}} = 512$). A learnable CLS token aggregates information via self-attention; padded positions are masked. This design naturally handles irregular sampling without interpolation.

Evidence Networks for detection. We frame detection as Bayesian model comparison. Given data $\mathbf{x}$, the Bayes factor $K = p(\mathbf{x}|\mathcal{M}_1)/p(\mathbf{x}|\mathcal{M}_0)$ quantifies evidence for the signal hypothesis $\mathcal{M}_1$ relative to noise $\mathcal{M}_0$. Unlike $\Delta\chi^2$ statistics—which are often used as a proxy for model comparison without rigorous Bayesian justification and fail to penalize model complexity—Bayes factors incorporate Occam's razor via marginalization over parameters.

Evidence Networks [Jeffrey and Wandelt, 2024] learn $\log_{10} K$ from binary-labeled data using the leaky parity-odd power (l-POP) exponential loss:

$$\mathcal{L}(f(\mathbf{x}), m) = \exp\left[\left(\tfrac{1}{2} - m\right) J_\alpha(f(\mathbf{x}))\right], \quad J_\alpha(z) = z + z|z|^{\alpha-1} \tag{1}$$

where $m \in \{0, 1\}$ is the binary label and $f(\mathbf{x})$ is the network output. For the optimal f^*, we have $\log_{10} K = J_\alpha(f^*(\mathbf{x}))$. The network consists of the shared transformer followed by a 3-layer MLP ($[256, 128, 1]$). It is trained on 100,000 light curves with equal signal/noise fractions.

Neural posterior estimation. For detected events, we estimate $p(\boldsymbol{\theta}|\mathbf{x})$ using NPE with a Masked Autoregressive Flow [Papamakarios et al., 2018] conditioned on the transformer summary $\mathbf{s}$, implemented via the sbi library [Boelts et al., 2025]. The flow is trained on 80,000 simulated pairs by maximizing $\mathbb{E}[\log p_\psi(\boldsymbol{\theta}|g_\phi(\mathbf{x}))]$. At test time, drawing 10,000 posterior samples requires $\sim$100 milliseconds—approximately $10^3\times$ faster than MCMC on the same hardware.

3   Results

Detection Performance We evaluate on a test set of 5,000 simulated events with realistic augmentation. Using a threshold of $\log_{10} K > 0.8$ (chosen for zero false positives on the validation set), the Evidence Network detects **4,996 of 5,000 signals (99.9%)** with no false positives on the 5,000 Gaussian-noise realizations—a one-sided Clopper–Pearson 95% upper bound on the false-positive rate of 5.99×10^{-4}, valid within the simulator's support (Section 4). This operating point lies on a broad plateau, not a knife edge: signal and noise $\log_{10} K$ distributions are cleanly separated (AUROC $= 0.9995$). For comparison, we compute hard-cut statistics using the *true* injected parameters—an oracle upper bound, since in practice one must fit the model, incurring optimization failures and local minima that would further degrade detection rates. Even with this advantage, hard cuts achieve only 95.9% [Johnson et al., 2020], 93.9% [Sumi et al., 2011], and 95.4% [Mroz et al., 2017].

Detection Efficiency vs. Physical Parameters Figure 2 shows detection efficiency as a function of each FSPL parameter. The advantage is most pronounced in the extreme finite-source regime ($\rho \gtrsim 5$), where efficiency remains $\sim$95% compared to $\sim$50% for hard cuts. This regime dominates short-duration events from low-mass FFPs—precisely the population most constraining for formation and ejection scenarios. Hard cuts fail because finite-source events have lower peak magnification despite distinctive morphological signatures (Figure 3); the Evidence Network extracts evidence from the full temporal structure.

Posterior Calibration We assess NPE calibration on the 4,996 detected events using the TARP diagnostic [Lemos et al., 2023]. Expected coverage closely tracks the credibility level across all parameters, confirming well-calibrated, unbiased posteriors. We additionally validate the Evidence Network on a toy model—detecting Gaussian bumps in white noise—where the Bayes factor admits a closed-form solution. The network is trained on binary signal/noise labels only, with no access to the analytic $\log K$ values. Despite this, it achieves near-oracle discriminative performance (AUC $= 0.725$ vs. oracle 0.726), demonstrating that Evidence Networks recover calibrated Bayes factors from binary labels alone without requiring explicit likelihood computation.

4   Discussion and Conclusion

Our unified framework replaces ad hoc hard cuts with calibrated Bayes factors via Evidence Networks, combined with amortized posterior inference via NPE—all sharing a single transformer encoder that handles irregular sampling without imputation.

Limitations. Our training assumes Gaussian photometric noise and does not model astrophysical false positives (stellar flares, eclipsing binaries, pulsating variables); the false-positive bound above is therefore valid only within this idealized noise model, and injecting or learning realistic contaminants during training is the most important next step [Legin et al., 2023]. The 20-day observation window

Figure 2: Detection efficiency as a function of FSPL parameters. The Evidence Network (blue) dramatically outperforms literature hard cuts in the extreme finite-source regime ($\rho \gtrsim 5$), recovering nearly twice as many events. Hard-cut statistics use oracle (true) parameters, so the comparison is conservative.

Figure 3: Six representative events detected by the Evidence Network ($\log_{10} K > 0.8$) but missed by all three literature hard cuts. These finite-source events ($\rho \gtrsim 2$) have low peak magnification despite distinctive morphological signatures (red curves), making them invisible to threshold-based statistics. The network extracts evidence from the full temporal structure rather than relying on peak flux alone.

limits applicability to longer-duration events from more massive lenses. Additionally, SBI methods can be sensitive to distributional shifts [Filipp et al., 2024]; the box-uniform priors above should ultimately be replaced by galactic population models.

Related approaches and outlook. Differentiable simulators (`microJAX` [Miyazaki and Kawahara, 2025], `microlux` [Ren and Zhu, 2025]) enable gradient-based inference via HMC [Ren et al., 2026]; these are complementary to SBI, which works with any black-box simulator and amortizes across observations. Natural next steps include binary lens models, hierarchical population inference, multi-band data, and other irregularly-sampled transients. Code: `https://github.com/NolanSmyth/evidence_networks_sbi_microlensing`

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