

EVOLVING ALIGNMENT *via* ASYMMETRIC SELF-PLAY

Scalable Preference Fine-Tuning Beyond Static Human Prompts

Anonymous authors

Paper under double-blind review

ABSTRACT

Current RLHF approaches for aligning large language models (LLMs) typically assume a fixed prompt distribution, which is sub-optimal and limits the generalization capabilities for language models. To address this issue, we introduce a general framework that casts alignment as an asymmetric game between two players: (i) **a creator** that generates increasingly informative prompt distributions using the reward model, and (ii) **a solver** that learns to produce more preferred responses on prompts produced by the creator. This framework of *Evolving Alignment via Asymmetric Self-Play* (**eva**), results in a simple and efficient approach that can utilize any existing RLHF algorithm. **eva** outperforms state-of-the-art methods on widely-used benchmarks, without the need of any additional human crafted prompts. Specifically, **eva** improves the win rate of GEMMA2-9B-IT on Arena-Hard from 51.6% to 60.1% with DPO, from 55.7% to 58.9% with SPPO, from 52.3% to 60.7% with SimPO, and from 54.8% to 60.3% with ORPO, surpassing its 27B version and matching `claude-3-opus`. This improvement is persistent even when new human crafted prompts are introduced. Finally, we show **eva** is effective and robust under various ablation settings.

What I cannot create, I do not understand.

– Richard P. Feynman

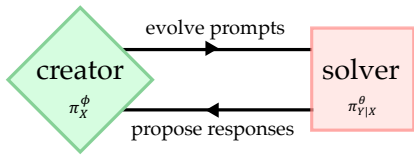


Figure 1: **eva**: Open-Ended RLHF *via* Asymmetric Self-Play. The creator is the prompt generation policy π_X and the solver is the response policy $\pi_{Y|X}$.

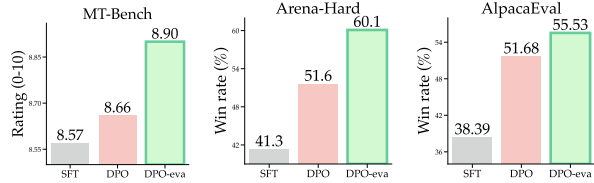


Figure 2: **Results**: Our method **eva** achieves concrete performance gain especially on *hard* alignment benchmarks, without relying on any additional human prompts. Here, we report results for DPO-**eva**; see more in §4.1.

1 INTRODUCTION

Long-lived artificial intelligence must deal with an ever-evolving, open-ended world, yet currently face constraints in both the *scale* and *quality* of available data, and the *growth rate* at which new, useful information is created. High quality human data, crucial for scaling large language model (LLM) based intelligence, is projected to run out in the next few years (Villalobos et al., 2024); the quality of such data is also expected to stagnate: as LLMs become more capable, they need to solve increasingly complex or new challenges, requiring training data beyond abilities of humans to create. This necessitates a new fundamental mechanism for self-improving, where models can continuously self-generate and self-solve harder problems. We thereby investigate the research question below:

*Can language models self-create new, learnable tasks to work on,
to self-improve to generalize better for human preferences alignment?*

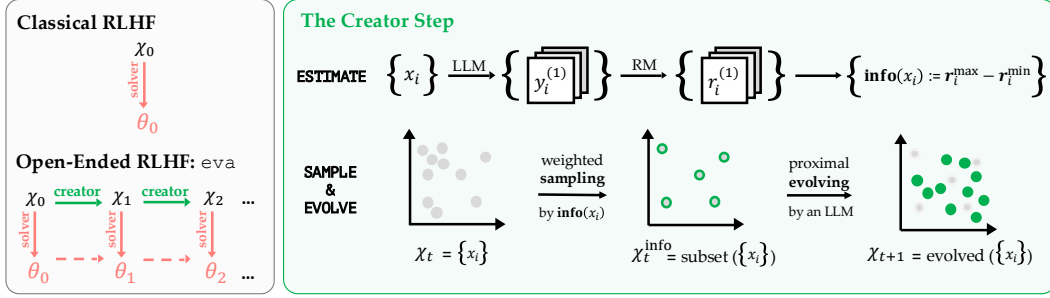


Figure 3: **Pipeline:** We generalize classical RLHF with open-ended RLHF, optimized with a creator-solver game for self-improving language models. Our proposed **eva** strategically evolves prompt distributions with a creator policy, which synthesizes prompts with an easy-to-implement *estimate, sample then evolve* procedure; specifically, it estimates the informativeness for each prompt by how contrastive the self-generated responses are to the prompt, from the reward signals it receives. The creator evolves new prompts from highly informative prompts, which the solver uses for continual training. Both the solver and creator policy can share the same network or operate independently. See more on our minimax-regret objective that drives the above design in § 3.

Many preference optimization algorithms (Christiano et al., 2017; Rafailov et al., 2023; Zhao et al., 2023; Wu et al., 2024; Liu et al., 2023a; Guo et al., 2024) have been proposed to improve the alignment of language models, however, they all default to fixed prompt training distributions. Such fixed training paradigm inevitably leads to: (i) *generalization issues* (models may underperform or hack on instructions that are insufficiently represented within the fixed set) and (ii) *efficiency issues* (data annotation and model training are costly, however not all prompt provide the same utility; it is wasteful to invest in sub-optimal fixed set, while identifying informative prompts through human efforts is expensive and time-consuming) (Team et al., 2023; 2024b; Dubey et al., 2024).

The objective thereby should not only be to optimize over a specific, static distribution of prompts, yet to develop an agent that can autonomously evolve the training data distribution for self-improvement, to align well across unseen, novel environments or tasks (instantiated by prompts).

Thus, we develop **eva** (Evolving Alignment *via* Asymmetric Self-Play), as illustrated in Figure 1. Central to our approach is a game with the minimax-regret objective, achieved through alternating optimization between creating prompts and solving them. The interplay encourages evolving curricula (Parker-Holder et al., 2022), potentially benefits both generalization and efficiency (see also § 3.4). Orthogonal to many recent self-play studies in LLM alignment (Munos et al., 2023; Choi et al., 2024; Wu et al., 2024), **eva** is *asymmetric* (Sukhbaatar et al., 2017), with two policies of different goals:

- **Creator:** evolves the prompt distribution for alignment.
- **Solver:** produces responses and optimizes alignment based on the evolving prompts.

Our main contributions are summarized as:

- **A new principle:** We propose a generalized **Open-Ended RLHF** objective for aligning language models, which seeks to jointly optimize the prompt distribution and the response policy, thus incentivizes models to self-improve to generalize well on new, unseen tasks beyond the initial training prompt distribution for alignment, as in Definition 1.
- **A new algorithm:** To optimize the objective, we design a practical algorithm *via* asymmetric self-play, which is implemented through alternating optimization in a **creator-solver game**, and can be easily plugged into any existing alignment pipeline, as in Algorithm 1.
- **State-of-the-art performance:** We empirically validate our method on public alignment benchmarks and present general strong performance improvement when plugged in with different preference optimization algorithms (*i.e.*, DPO, SPPO, SimPO, ORPO). We also conduct extensive ablation studies that provide additional insights on the choice of informativeness metric, reward model, and training schedules, as in § 4.

eva is easy to implement. We hope it can serve as a scalable method for the research community to build open-ended, robust, and self-improving language agents, that align with human values.

2 PRELIMINARIES

We hereby review major concepts, which we later in § 3 use *regret* and the proxy by *advantage* to identify informative prompts, leading to learning curricular implicitly maximizing *contrastive ratio*.

Alignment by RLHF. Classical RLHF (Ouyang et al., 2022) optimizes on a fixed distribution \mathcal{D} :

$$\max_{\pi_{\theta}} \mathbb{E}_{\mathbf{x} \sim \mathcal{D}, \mathbf{y} \sim \pi_{\theta}(\cdot | \mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}) \right] - \mathbb{E}_{\mathbf{x} \sim \mathcal{D}} \left[\beta \cdot \mathbb{D}_{\text{KL}} \left[\pi_{\theta}(\mathbf{y} | \mathbf{x}) \parallel \pi_{\text{ref}}(\mathbf{y} | \mathbf{x}) \right] \right], \quad (1)$$

where \mathbf{x} and \mathbf{y} denote the prompts and responses, and $r(\cdot, \cdot)$ is the reward function.

Reward. Let the *optimal policy* of Eq. 1 be $\pi^*(\cdot)$ and $Z(\cdot)$ be the partition function, we have:

$$r(\mathbf{x}, \mathbf{y}) = \beta \cdot \log \frac{\pi^*(\mathbf{y} | \mathbf{x})}{\pi_{\text{ref}}(\mathbf{y} | \mathbf{x})} + \beta \cdot \log Z(\mathbf{x}). \quad (2)$$

Regret. Let $r^*(\mathbf{x}) = \max_{\mathbf{y}'} r(\mathbf{x}, \mathbf{y}')$ be the optimal reward achievable at \mathbf{x} , the *regret* to take \mathbf{y} is:

$$\text{Regret}(\mathbf{x}, \mathbf{y}) = r^*(\mathbf{x}) - r(\mathbf{x}, \mathbf{y}). \quad (3)$$

Advantage. The *advantage* function quantifies how much better a response \mathbf{y} is w.r.t. a baseline:

$$A(\mathbf{x}, \mathbf{y}) = r(\mathbf{x}, \mathbf{y}) - \mathbb{E}_{\mathbf{y}' \sim \pi(\mathbf{y}' | \mathbf{x})} [r(\mathbf{x}, \mathbf{y}')]. \quad (4)$$

Variants of advantage (e.g., the worst-case advantage A_{\min}^*) are related to regret, as shown in Table 2.

Direct preference optimization. The DPO (Rafailov et al., 2023) objective for RLHF is:

$$\mathcal{L}_{\beta}^{\text{DPO}}(\pi_{\theta}) = \sum_{(\mathbf{y}_+, \mathbf{y}_-, \mathbf{x}) \in \mathcal{D}} -\log \left[\sigma \left(\beta \cdot \Delta_{\theta; \text{ref}}^{\mathbf{x}} \right) \right], \quad (5)$$

where we use $+$, $-$ to denote chosen and rejected responses, and denote the **contrastive ratio** as:

$$\Delta_{\theta; \text{ref}}^{\mathbf{x}} := \log \frac{\pi_{\theta}(\mathbf{y}_+ | \mathbf{x})}{\pi_{\text{ref}}(\mathbf{y}_+ | \mathbf{x})} - \log \frac{\pi_{\theta}(\mathbf{y}_- | \mathbf{x})}{\pi_{\text{ref}}(\mathbf{y}_- | \mathbf{x})}. \quad (6)$$

By reward reparameterization with Eq. 2, advantage also relates to contrastive ratio, as in § 3.4.

3 METHOD

Algorithm overview. On a high level, **eva** extends classical RLHF to open-ended RLHF via a creator that adapts prompt distributions with an easy-to-implement *estimate, sample then evolve* procedure, mimicing the *minimax-regret* policy of asymmetric self-play games, as detailed in §3.3.

Algorithm 1 **eva**: Evolving Alignment via Asymmetric Self-Play

Input: initial policy π_{θ_0} , initial prompt set \mathcal{X}_0

1: **for** iteration $t = 1, 2, \dots$ **do**

∇ /* **creator step** */

2: *estimate informativeness:* $\mathcal{X}_t \leftarrow \mathcal{X}_t \cup \{\mathbf{info}(\mathbf{x}_i)\}$

sample subset: $\mathcal{X}_t^{\text{info}} \leftarrow \mathbf{sample}(\mathcal{X}_t)$

self-evolve prompts: $\mathcal{X}_t' \leftarrow \mathbf{evolve}(\mathcal{X}_t^{\text{info}})$

∇ /* **solver step** */

3: *self-generate responses:* $\forall \mathbf{x}_i \in \mathcal{X}_t', \text{ generate } \{\mathbf{y}_i^{(j)}\} \sim \pi_{\theta_{t-1}}(\cdot | \mathbf{x}_i)$

4: *annotate rewards:* $\mathcal{X}_t' \leftarrow \mathcal{X}_t' \cup \{(\mathbf{y}_i^{(j)}, r_i^{(j)})\}$

5: *preference optimization:* $\theta_t \leftarrow \theta_{t-1} - \eta \nabla_{\theta} \mathcal{L}_{\mathcal{X}_t'}(\theta)$

6: **end for**

7: **return** final solver policy π_{θ_T}

Section overview. We aim to develop language models that can *self-improve to generalize well on new, unseen tasks* beyond the initial training prompt distribution for alignment. In §3.1, we present the limitations of classical RLHF and generalize it to the new objective of open-ended RLHF. In §3.2, we introduce the creator-solver game to tractably optimize the objective. In §3.3, we detail the practical algorithm, compatible with any preference optimization method as the solver, with our designed creator in the loop. Lastly in §3.4, we present various interpretations for **eva**.

3.1 THE PRINCIPLE: OPEN-ENDED RLHF FOR JOINT SELF-IMPROVEMENT

Intuition. Classical RLHF (*cf.*, Eq. 1) optimizes over a *static* prompt distribution, meaning that the agent is only aligned to a fixed reference point, making it brittle when it is evaluated on new problems from the ever-changing real world. Our Open-Ended RLHF breaks away from this static framework, with the goal to develop an agent that *generalizes* well across *unseen, novel* environments (where the tasks entailed in prompts may not have been explicitly encountered during training). To achieve this, we must design a new objective that moves beyond optimizing over a fixed dataset \mathcal{D} .

Formalization. We thus formally introduce *optimizable* prompt generation policy $\pi_\phi(\mathbf{x})$, which is *jointly* optimized with the response policy $\pi_\theta(\mathbf{y} \mid \mathbf{x})$, as follows:

Definition 1 (Open-Ended RLHF) We define evolving alignment^a as the open-ended joint optimization on the prompt and response policy for alignment w.r.t the joint reference policy:

$$\max_{\phi, \theta} J_{\phi, \theta}(\pi_{ref}) := \mathbb{E}_{\mathbf{x} \sim \pi_\phi(\cdot), \mathbf{y} \sim \pi_\theta(\cdot \mid \mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}) \right] - \beta \cdot \mathbb{D}_{KL} \left[\pi_{\phi, \theta}(\mathbf{x}, \mathbf{y}) \parallel \pi_{ref}(\mathbf{x}, \mathbf{y}) \right], \quad (7)$$

where $\pi_{\phi, \theta}(\mathbf{x}, \mathbf{y}) := \pi_\phi(\mathbf{x}) \cdot \pi_\theta(\mathbf{y} \mid \mathbf{x})$ and $\pi_{ref}(\mathbf{x}, \mathbf{y}) := p_{ref}(\mathbf{x}) \cdot \pi_{ref}(\mathbf{y} \mid \mathbf{x})$.

^aThis generalizes RLHF (Eq. 1), which is recovered when π_ϕ is static as p_{ref} . To see this, expand Eq. 7:

$$\max_{\phi, \theta} \mathbb{E}_{\mathbf{x} \sim \pi_\phi(\cdot), \mathbf{y} \sim \pi_\theta(\cdot \mid \mathbf{x})} [r(\mathbf{x}, \mathbf{y})] - \mathbb{E}_{\mathbf{x} \sim \pi_\phi(\cdot)} [\beta \cdot \mathbb{D}_{KL} [\pi_\theta(\mathbf{y} \mid \mathbf{x}) \parallel \pi_{ref}(\mathbf{y} \mid \mathbf{x})]] - \beta \cdot \mathbb{D}_{KL} [\pi_\phi(\mathbf{x}) \parallel p_{ref}(\mathbf{x})].$$

Here, $p_{ref}(\mathbf{x})$ represents an idealized, potentially intractable probability measure over all possible tasks (instantiated *via* prompts) in the wild, as a conceptual reference that encompasses the full diversity and complexity of tasks agents may encounter, serving as a guiding target for alignment. Additionally, the *joint optimization* ensures that the task distribution and the agent’s response policy are updated in tandem, enabling adaptation to increasingly complex tasks, thereby promoting generalization.

3.2 THE MECHANISM: ASYMMETRIC SELF-PLAY *via* THE CREATOR V.S. SOLVER GAME

Intuition. It is hard to directly optimize Eq. 7, due to (i) the **intractability** of the unspecified reference (Dennis et al., 2020); (ii) the **instability** of joint differentiation (Goodfellow et al., 2014). We present an *alternating optimization* solution by casting it as an asymmetric creator-solver game.

- Intuitively, the creator can guide the solver by a prompt curriculum with *increasing complexity*, ensuring the learning is efficient and general to handle the diversity in the wild.
- Mathematically, this resembles RL optimization *via* expectation-maximization (Dayan and Hinton, 1997; Singh et al., 2023), where ϕ for the prompt distribution is fixed at each step.

Formalization. We formalize the alternating optimization as an asymmetric game as follows:

- **Creator** : the prompt player $\pi_{\mathcal{X}}$ that strategically generate prompts for the solver.
- **Solver** : the response player $\pi_{\mathcal{Y} \mid \mathcal{X}}$ (or π) that learn to generate preferred responses.

We use the *minimax regret* approach (Savage, 1951; Hejna et al., 2023), where the solver minimizes and the creator maximizes regret¹, *i.e.*, the difference in the reward of the current and optimal policy:

$$\text{Regret}(\mathbf{x}, \pi) = \mathbb{E}_{\mathbf{y}' \sim \pi(\mathbf{y}' \mid \mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}') \right] - \mathbb{E}_{\mathbf{y}' \sim \pi^*(\mathbf{y}' \mid \mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}') \right]. \quad (8)$$

¹The expression here is oversimplified by omitting the KL term; please see Appendix G for details.

At the equilibrium (Nash et al., 1950), prior works (Dennis et al., 2020) have shown:

Remark 1 (Minimax Regret) *If the solver-creator game reaches an equilibrium, the solver follows a minimax regret strategy, i.e., it optimizes to perform well under all cases:*

$$\pi^* \in \arg \min_{\pi \in \Pi_{\mathcal{Y}|\mathcal{X}}} \max_{\pi_{\mathcal{X}} \in \Pi_{\mathcal{X}}} \mathbb{E}_{\mathbf{x} \sim \pi_{\mathcal{X}}} [\text{Regret}(\mathbf{x}, \pi)]. \quad (9)$$

To illustrate, our open-ended RLHF allow for the creation of an evolving prompt distribution that challenges the agent progressively for better generalization; the introduced minimax regret objective further adds *robustness* on top of such evolving curricula by *incentivizing agents to perform well in all cases*. However, without access to the true optimal policy, we must approximate the regret. We thereby design the advantage-based proxy, which is used to measure the prompt informativeness:

Definition 2 (Informativeness Proxy) *We measure the informativeness of a prompt by the (absolute) empirical worst-case optimal advantage, approximating the minimax regret:*

$$\text{info}(\mathbf{x}) \leftarrow \hat{A}_{\min}^* := |\min_{\mathbf{y}} r(\mathbf{x}, \mathbf{y}) - \max_{\mathbf{y}'} r(\mathbf{x}, \mathbf{y}')|, \quad (10)$$

which is estimated by sampling multiple responses for \mathbf{x} from the solver and calculating gap between the maximal reward (from the best \mathbf{y}) and the minimal reward (from the worst \mathbf{y}).

We then use the informativeness proxy to guide the creator for prompt generation, which has a few useful properties under different interpretations, as in § 3.4. Together, we define a mechanism that the solver learns to improve, as the creator keeps challenging the solver on its current weaknesses.

3.3 THE PRACTICAL ALGORITHM

We now illustrate **eva** of Algorithm 1 (cf., Fig 3), with specifications in Appendix A.

3.3.1 THE CREATOR STEP: ESTIMATE, SAMPLE THEN EVOLVE

Plainly, the creator finds most useful prompts and generate variants of them for preference optimization. One may relate this to **evolution strategies** (Schwefel, 1977) which find the most promising species, then mutate and crossover, or to **curriculum RL** (Parker-Holder et al., 2022) which finds environments with high-regret levels, then edits within some distance. As in Section 3.2, we do not seek a differentiable creator in this work. The creator is implemented in three steps as in Figure 3.

Step 1: info(\cdot) – *estimate the informativeness.* For each \mathbf{x} in the prompt set \mathcal{X}_t , we generate responses, annotate rewards and estimate a informativeness metric to \mathbf{x} by Eq. 10 (see also Table 2).

Step 2: sample(\cdot) – *weighted sampling for an informative subset.* By using the informativeness metric as the weight, we sample a informative prompt subset $\mathcal{X}_t^{\text{info}}$ to be evolved later.

Step 3: evolve(\cdot) – *evolving for a proximal region of high-advantage prompts.* Our algorithm is agnostic to and does not rely on any specific evolving method. We take EvolInstruct (Xu et al., 2023a) as an off-the-shelf method, which conducts in-depth (i.e., adding constraints, deepening, concretising, complicating) and in-breadth evolving (i.e., mutation) for prompts. Specifically, we iterate over each prompt in the $\mathcal{X}_t^{\text{info}}$, where each one is evolved to multiple variations, then optionally mix the newly generated prompts with a uniformly sampled buffer from \mathcal{X}_t to create \mathcal{X}_t' .

3.3.2 THE SOLVER STEP: SOLVE THEN OPTIMIZE

This step is the classical preference optimization (Rafailov et al., 2023), where responses are generated and the gradient descent is performed. Take the pointwise reward model setting as an example, for every prompt, we sample n responses with reward annotated for each; we take the responses with the maximal and the minimal reward to construct the preference pairs, then optimize upon.

Put together, **eva** can unify existing iterative optimization pipeline (Tran et al., 2023) with a new creator module, which can either share the same network as the solver policy or operate independently.

3.4 UNDERSTANDING **eva** IN DIFFERENT INTUITIVE WAYS

Learning potential. Our metric intuitively identifies the learning potential of a prompt by measuring the gap between the best and worst response to it from the solver. We reason, that prompts eliciting *both* high-reward and low-reward outcomes, reflect *learnable* tasks where the model is capable of improving but has not yet mastered, thereby implying learning potential (cf., Jiang et al. (2021b)).

Worst-case guarantees. The minimax-regret objective, by design, leads to solvers that perform robustly across the prompt space, thus gives the worst-case guarantee. While exact equilibrium may not be attainable with approximation, our empirical results in § 4.2.1 demonstrate robustness.

Auto-curricula for the players. We visualize curriculum induced by **eva** in § E. With the stochastic policy, the advantage may be heuristically understood as the reward difference between a *base solver* and a *reference solver*. Rather than optimizing separate solvers (Dennis et al., 2020), we sample multiple times from the same policy to create the pair. In this way, the creator is incentivized to produce new prompts that are just out of the comfort zone of solvers (Chaiklin et al., 2003):

- For overly challenging prompts, both solutions perform poorly, leading to a low proxy.
- For overly easy prompts, the base solution already performs well, again giving a low proxy.
- The optimal strategy is to find prompts that are just beyond the solver’s current capability.

Auto-curricula inherent to Contrastive Optimization. Contrastive preference optimization generalizes DPO and a family of algorithms (cf., Hejna et al. (2023); Rafailov et al. (2023); Tang et al. (2024)), many of whose losses monotonically decrease as the contrastive ratio increases. Here, by Eq. 2 and Eq. 6, the *contrastive ratio* can be written via the *advantage-based proxy*:

$$A_{\min}^*(\mathbf{x}) = \beta \cdot \Delta_{\theta^*, \text{ref}}^{\mathbf{x}}. \quad (11)$$

By our proxy, we implicitly incentivize the creator to generate prompts that *bring the most contrastive responses*, which decrease the loss the most. This matches the curriculum learning literature, which prioritizes (in **eva**, *generatively* prioritizes) examples with smaller losses for better convergence and generalization (Bengio et al., 2009). We hence suggest the *Contrastive Curriculum Hypothesis*: in contrastive preference optimization, prioritizing prompts with higher contrastive ratio improves sample efficiency and generalization. We show initial empirical results on this in § 4.2.1 and § 4.2.4.

4 EXPERIMENTS

Datasets and models for training. We use **UltraFeedback** (Cui et al., 2023) as the training dataset, which contains diverse high-quality prompts that are primarily human-generated. We use the instruction-finetuned GEMMA-2-9B (Team et al., 2024b) as the primary model, which is a strong baseline for models of its size. Detailed experimental setting can be found in § A.

Evaluation settings. We choose: (i) **AlpacaEval 2.0** (Dubois et al., 2024), which assesses general instruction following with 805 questions; (ii) **MT-Bench** (Zheng et al., 2023), which evaluates multi-turn instruction following with 80 hard questions in 8 categories; (iii) **Arena-Hard** (Li et al., 2024b), which is derived from 200K user queries on Chatbot Arena with 500 challenging prompts across 250 topics. We use gpt-4-1106 as the judge and gpt-4-0314 as the baseline for win rate.

Optimization algorithms. We focus on direct preference optimization and consider the following:

- **With reference policy:** DPO (Rafailov et al., 2023), SPPO (Wu et al., 2024).
- **Without reference policy:** SimPO (Meng et al., 2024), ORPO (Hong et al., 2024).

Reward models as preference oracles. We use ARMORM-8B (Wang et al., 2024) as our default reward model as the human-preference proxy, and consider the following for ablation studies:

- **Pointwise:** ARMORM-8B (Wang et al., 2024), SKYWORKRM-27B (Liu and Zeng, 2024).
- **Pairwise:** PAIRRM-0.4B (Jiang et al., 2023), PAIRRM-8B (Dong et al., 2024a).

4.1 MAIN RESULTS

In general, **eva** brings notable gains in alignment without relying on any human-crafted data, thus offering more efficiency. In the base setup, building on the one-iteration finetuned model ($\theta_{0 \rightarrow 1}$), **eva** adds a creator to self-evolve the prompt set of the initial iteration and uses any preference optimization algorithm for an additional open-ended RLHF iteration, resulting in $\theta_{1 \rightarrow \bar{1}}$ ².

eva achieves self-improvement. As shown in red rows in Table 1, **eva** yields notable performance improvement over $\theta_{0 \rightarrow 1}$ across different optimization algorithms, especially on the harder Arena-Hard benchmark, which is recognized to be more challenging and distinguishable among others due to the complexity of its prompts and its fairer scoring system (Li et al., 2024b; Meng et al., 2024). Specifically, **eva** brings 8.4% gain with SimPO as the solver, and 8.5% gain with DPO as the solver, surpassing its 27B version and matching `claude-3-opus-240229` as reported on the [AH leaderboard](#), while using fully self-automated prompt generation for alignment. Interestingly, **eva** brings the least gains on AlpacaEval 2.0, a simpler evaluation benchmark. This indicates **eva** improves the most for challenging tasks.

eva can surpass human-crafted prompts. We further show that **eva**-prompt-trained models ($\theta_{1 \rightarrow \bar{1}}$) can match and even outperform those trained on additional new prompts from UltraFeedback ($\theta_{1 \rightarrow 2}$) (which we denoted as human prompts), while being much cheaper and more efficient. Additionally, on MT-Bench, training with new human prompts typically show decreased performance in the first turn and only modest gains in the second turn. In contrast, **eva** notably enhances second-turn performance. We hypothesize that **eva** evolves novel, learnable prompts that include characteristics of second-turn questions, reflecting emergent skills like handling follow-up interactions.

Model Family (\rightarrow)	GEMMA-2-9B-IT					
	Arena-Hard		MT-Bench		AlpacaEval 2.0	
Benchmark (\rightarrow)						
Method (\downarrow) / Metric (\rightarrow)	WR (%)	avg. score	1 st turn	2 nd turn	LC-WR (%)	WR (%)
θ_0 : SFT	41.3	8.57	8.81	8.32	47.11	38.39
$\theta_{0 \rightarrow 1}$: DPO	51.6	8.66	9.01	8.32	55.01	51.68
$\theta_{1 \rightarrow \bar{1}}$: + eva	60.1 (+8.5)	8.90	9.04	8.75 (+0.43)	55.35	55.53
$\theta_{1 \rightarrow 2}$: + new human prompts	59.8	8.64	8.88	8.39	55.74	56.15
$\theta_{0 \rightarrow 1}$: SPPO	55.7	8.62	9.03	8.21	51.58	42.17
$\theta_{1 \rightarrow \bar{1}}$: + eva	58.9 (+3.2)	8.78	9.11	8.45 (+0.24)	51.86	43.04
$\theta_{1 \rightarrow 2}$: + new human prompts	57.7	8.64	8.90	8.39	51.78	42.98
$\theta_{0 \rightarrow 1}$: SimPO	52.3	8.69	9.03	8.35	54.29	52.05
$\theta_{1 \rightarrow \bar{1}}$: + eva	60.7 (+8.4)	8.92	9.08	8.77 (+0.42)	55.85	55.92
$\theta_{1 \rightarrow 2}$: + new human prompts	54.6	8.76	9.00	8.52	54.40	55.72
$\theta_{0 \rightarrow 1}$: ORPO	54.8	8.67	9.04	8.30	52.17	49.50
$\theta_{1 \rightarrow \bar{1}}$: + eva	60.3 (+5.5)	8.89	9.07	8.71 (+0.41)	54.39	50.88
$\theta_{1 \rightarrow 2}$: + new human prompts	57.2	8.74	9.01	8.47	54.00	51.21

Table 1: **Main results.** Our **eva** achieves notable alignment gains and can surpass human prompts on major benchmarks across a variety of representative direct preference optimization algorithms.

4.2 ABLATION STUDIES

We conduct in-depth ablation studies on **eva**, with findings below to be elaborated on later:

- § 4.2.1 - **informativeness metric**: our *regret*-based metric outperforms other alternatives.
- § 4.2.2 - **sample-then-evolve procedure**: our method outperforms greedy selection.
- § 4.2.3 - **scaling w/ reward models**: the alignment gain of **eva** scales with reward models.
- § 4.2.4 - **continual training**: our method has monotonic gain with incremental training; the *evolved data and schedule* by **eva** serves as an *implicit regularizer* for better local minima.

²Unless stated otherwise, each iteration uses 10K prompts (*i.e.*, 1/6 partition from UltraFeedback in classical training). We denote $\theta_{t \rightarrow t+1}$ as the model trained with new human prompts based on the t -th checkpoint, and $\theta_{t \rightarrow \bar{t}}$ as the model trained with evolved prompts from the t -th checkpoint w/o adding any new human prompts.

4.2.1 THE CHOICE OF INFORMATIVENESS METRICS: $\text{INFO}(\cdot)$

Metric	$\text{info}(\mathbf{x})$	Related Interpretations
A_{\min}^* : worst-case optimal advantage	$ \min_{\mathbf{y}} r(\mathbf{x}, \mathbf{y}) - \max_{\mathbf{y}'} r(\mathbf{x}, \mathbf{y}') $	minimax regret (Savage, 1951)
A_{avg}^* : average optimal advantage	$ \frac{1}{N} \sum_{\mathbf{y}} r(\mathbf{x}, \mathbf{y}) - \max_{\mathbf{y}'} r(\mathbf{x}, \mathbf{y}') $	Bayesian regret (Banos, 1968)
A_{dis}^* : dueling optimal advantage	$ \max_{\mathbf{y} \neq \mathbf{y}^*} r(\mathbf{x}, \mathbf{y}) - \max_{\mathbf{y}'} r(\mathbf{x}, \mathbf{y}') $	dueling regret (Wu and Liu, 2016)

Table 2: The reward-advantage-based metrics that serve as the informativeness proxies for prompts.

Model Family (\rightarrow)	GEMMA-2-9B-IT					
Benchmark (\rightarrow)	Arena-Hard	MT-Bench			AlpacaEval 2.0	
Method (\downarrow) / Metric (\rightarrow)	WR (%)	avg. score	1 st turn	2 nd turn	LC-WR (%)	WR (%)
$\theta_{0 \rightarrow 1}$: DPO	51.6	8.66	9.01	8.32	55.01	51.68
$\theta_{1 \rightarrow 1}$: + eva (uniform)	57.5	8.71	9.02	8.40	53.43	53.98
$\theta_{1 \rightarrow 1}$: + eva ($\text{var}(\mathbf{r})$)	54.8	8.66	9.13	8.20	54.58	52.55
$\theta_{1 \rightarrow 1}$: + eva ($\text{avg}(\mathbf{r})$)	58.5	8.76	9.13	8.40	55.01	55.47
$\theta_{1 \rightarrow 1}$: + eva ($1/\text{avg}(\mathbf{r})$)	56.7	8.79	9.13	8.45	55.04	54.97
$\theta_{1 \rightarrow 1}$: + eva ($1/A_{\min}^*$)	52.3	8.64	8.96	8.31	53.84	52.92
$\theta_{1 \rightarrow 1}$: + eva (A_{avg}^*) (our variant)	60.0	8.85	9.08	8.61	56.01	56.46
$\theta_{1 \rightarrow 1}$: + eva (A_{dis}^*) (our variant)	60.0	8.86	9.18	8.52	55.96	56.09
$\theta_{1 \rightarrow 1}$: + eva (A_{\min}^*) (our default)	60.1 (+8.5)	8.90	9.04	8.75 (+0.43)	55.35	55.53

Table 3: **Choice of informativeness metric matters.** Our metric by *advantage* achieves the best performances, comparing with others as weights to sample for evolving. See also § F for visualization.

Advantage as the informativeness metric outperforms baselines. As in Table 3, **eva** offers an effective curriculum by the advantage-based proxy as the informativeness metric (bottom row):

- Comparing w/ *uniform evolving* (brown): Existing baselines generate prompts in a uniform manner (Yuan et al., 2024) w/o informativeness measure (*cf.*, the principle of insufficient reason (Keynes, 1921; Tobin et al., 2017)). **eva** concretely outperforms, corroborating Das et al. (2024) that uniform learners can suffer sub-optimality gaps.
- Comparing w/ *other heuristics* (blue): Prior practices (Team et al., 2023) tried heuristics like prioritizing prompts w/ the most variance in its rewards or w/ the lowest/highest average. We find our advantage based methods (red) outperforms those heuristics; see § F for more.
- Comparing w/ the *inverse advantage* (purple): Contrary to curriculum learning, a line of works conjecture that examples w/ higher losses may be prioritized (Jiang et al., 2019; Kawaguchi and Lu, 2020), which can be done by inverting our metric. We find it significantly *hurt* the alignment gain, corroborating Mindermann et al. (2022) that those examples are often noisy, unlearnable or irrelevant, meaning our curriculum is effective and practical.
- Among our *advantage variants* (red): We designed variants of our default advantage-based metric, as in Table 2; the default A_{\min}^* remains competitive among its peers. Together, the advantage-based principle provides a robust guideline for prompt sampling and evolving.

The lesson is that we must be selective about which are the promising to evolve, otherwise unlearnable, noisy or naïve prompts may hinder learning. Our regret-inspired metric represents a solid baseline.

4.2.2 THE EFFECT OF THE SAMPLE-THEN-EVOLVE PROCEDURE

The design of $\text{evolve}(\cdot)$ in **eva is effective.** As in Table 4, we show:

- Removing the $\text{evolve}(\cdot)$ step: if we only do subset sampling or ordered selection, we still have gain, but not as much as w/ evolving (*e.g.*, **eva** brings 4.8% additional wins on AH).
- Altering the $\text{sample}(\cdot)$ step: if we greedily select prompts by the metric instead of using them as weights for importance sampling, the performance will be weaker as we evolve.

This shows that simply adaptive training within a fixed prompt distribution is unsatisfactory; our open-ended RLHF with *generative* prompt exploration gives a substantial headroom for self-improvement.

Benchmark (\rightarrow)	Arena-Hard	MT-Bench			AlpacaEval 2.0	
Method (\downarrow) / Metric (\rightarrow)	WR (%)	avg. score	1 st turn	2 nd turn	LC-WR (%)	WR (%)
$\theta_{0 \rightarrow 1}$: DPO	51.6	8.66	9.01	8.32	55.01	51.68
$\theta_{1 \rightarrow \bar{1}}$: [no evolve]-greedy	56.1	8.68	8.98	8.38	54.11	53.66
$\theta_{1 \rightarrow \bar{1}}$: [no evolve]-sample	55.3	8.69	9.00	8.38	54.22	54.16
$\theta_{1 \rightarrow \bar{1}}$: + eva -greedy (our variant)	59.5	8.72	9.06	8.36	54.52	55.22
$\theta_{1 \rightarrow \bar{1}}$: + eva -sample (our default)	60.1	8.90	9.04	8.75	55.35	55.53

Table 4: **Effect of evolving.** The blue are those training w/ only the informative subset and w/o evolving; we denote -sample for the default weighted sampling procedure in Algo 1, while using -greedy for the variant from the classical active data selection procedure (cf., a recent work (Muldrew et al., 2024) and a pre-LLM work (Kawaguchi and Lu, 2020)), which selects data by a high-to-low ranking via the metric greedily. We show evolving brings a remarkable alignment gain (the red v.s. the blue); and as we evolve, sampling is more robust than being greedy (cf., Russo et al. (2018)).

4.2.3 SCALING POINTWISE AND PAIRWISE REWARD MODELS

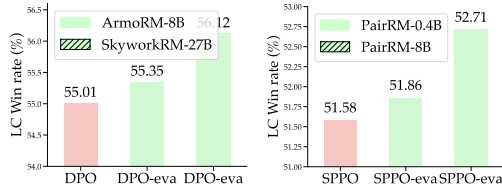


Figure 4: **eva scales with quality of reward models**, under pointwise RMs w/ DPO (left) and pairwise RMs w/ SPPO (right). Note SPPO handles general preferences thus requires pairwise RMs, and DPO relies on the Bradley-Terry assumption, for which pointwise RMs are suitable.

Figure 4 presents the length-controlled win rate of **eva** on AlpacaEval using pointwise and pairwise reward models of varying scales. The results give a clear trend: as the quality of reward models improve, **eva** brings higher alignment gain. The scaling observation shows the effectiveness of **eva** in exploiting more accurate reward signals to choose informative prompts for better alignment. One takeaway is interaction w/ the external world is essential for intelligence. The more accurate reward signals observed, the better the agent incentivize themselves to improve (cf., Silver et al. (2021)).

4.2.4 EVA IMPROVES BOTH SAMPLE EFFICIENCY AND GENERALIZATION

We then continuously run the default *incremental training* (i.e., training from the last checkpoint w/ the evolved set in each iteration), as in Fig 5, **eva** presents *monotonic performance gain* over iterations, and surpasses that trained w/ new human prompts, implying the generalization benefit³.

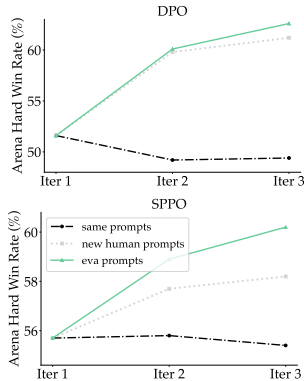


Figure 5: **Continual training.** **eva** stays robust w/ more iterations in incremental training.

The solutions found by **eva** cannot be recovered by training longer w/ a fixed distribution (the dashed), nor by naively sourcing new prompts w/o examining informativeness (the gray dotted), thus our generative data schedule is effective.

In Table 5, we ablate **eva** in *scratch training*, i.e., training w/ the full set (the evolved and the original data). **eva** is competitive in incremental training, thus *learns more effective with less data* – a nice bonus via minimax regret (Jiang et al., 2021a).

Benchmark (\rightarrow)	Arena-Hard	MT-Bench	AlpacaEval 2.0
Method (\downarrow) / Metric (\rightarrow)	WR (%)	avg. score	LC-WR (%)
θ_0 : SFT	41.3	8.57	47.11
$\theta_{0 \rightarrow 1}$: DPO	51.6	8.66	55.01
$\theta_{0 \rightarrow \bar{1}}$: eva (scratch)	59.8	8.88	54.59
$\theta_{1 \rightarrow \bar{1}}$: eva (incremental)	60.1	8.90	55.35

Table 5: **Ablation on incremental v.s. scratch training.**

³Behaviors of the dashed/dotted lines relate to *loss of plasticity* (Ash and Adams, 2019; Dohare et al., 2023; Abbas et al., 2023; Xue et al., 2024). Classical works resolve it by the optimization view (e.g., weight perturbing), whereas **eva** provides a fresh data view, potentially mimicking an **implicit regularizer for better generalization**.

5 RELATED WORKS

Self-improving algorithms and iterative optimization. This line of work focuses on iteratively generating samples from the response policy and continuously re-training the policy by selected self-generated samples. Major works include ReST (Gulcehre et al., 2023; Singh et al., 2023), STaR (Zelikman et al., 2022), RFT (Yuan et al., 2023), RAFT (Dong et al., 2023), self-improving LLMs (Huang et al., 2022; Yuan et al., 2024); in the context of preference optimization, iterative DPO (Xu et al., 2023b; Tajwar et al., 2024; Tran et al., 2023; Xiong et al., 2024; Pang et al., 2024) has proven effective. Most works focus on self-training by improving in $\mathcal{Y} \mid \mathcal{X}$, while we *jointly optimize* both responses and prompts via generative exploration in the $(\mathcal{X}, \mathcal{Y})$ space. Among them, we also distinctly present a game-theoretic framework with the minimax-regret principle as the guidance.

Prompt synthesis for language models. Existing works include Self-Instruct (Wang et al., 2022), WizardLM (Xu et al., 2023a; Luo et al., 2023), Self-Align (Sun et al., 2024), Glan (Li et al., 2024a), EvoPrompt (Guo et al., 2023), Magpie (Xu et al., 2024) and others (Long et al., 2024). **eva** is an orthogonal contribution since any synthesis method can be plugged in as the `evolve(.)` for the creator. Importantly, our work presents a new reward-related metric to endow prompt the notion of informativeness, with new implications as in § 3.4. We also focus on preference optimization algorithms, while those existing works primarily use synthesized prompts in an SFT-only way.

Self-play and curriculum RL. Agents trained on a fixed data distribution are often brittle and may struggle to adapt to the real world (Hughes et al., 2024a). Self-play (Samuel, 1959; Goodfellow et al., 2014; Silver et al., 2016) addresses this by having the agent learn through self-interaction, thus creating more diverse experiences and automatic curricula. In asymmetric self-play, the paradigm centers on “Alice proposing a task, and Bob doing it” (Sukhbaatar et al., 2017; Samvelyan et al., 2023; Beukman et al., 2024; Dennis et al., 2020). We revive the classical asymmetric self-play principle (Sutton et al., 2011) in optimizing language models. Unlike traditional curriculum RL (Parker-Holder et al., 2022), which usually renders environments from specified levels (Dennis et al., 2020), our approach is *generative* by nature, as we directly generate contexts from the auto-regressive language models.

Self-play in RLHF. A growing line of research frames RLHF as a *symmetric* self-play game, where both players are response players (Munos et al., 2023; Wu et al., 2024; Choi et al., 2024; Rosset et al., 2024). However, these methods still rely on a fixed prompt distribution thus is sub-optimal. In contrast, we solve this by *asymmetric* self-play, enabling evolving prompt distributions for more generalizable language agents. During our work, we notice one concurrent paper adopting the asymmetric two-player setup (Zheng et al., 2024), however (i) it applies to adversarial attack tasks instead of general alignment benchmarks, (ii) it is incompatible w/ direct preference optimization, and (iii) it relies on the maxmin principle (which is known to be producing unlearnable environments (Dennis et al., 2020)) instead of the minimax *regret* principle (Fan, 1953; Savage, 1951) as we do. We also first precisely defined the new problem of open-ended RLHF, which generalizes over classical RLHF.

6 CONCLUDING REMARKS

Limitations and future directions. **eva** defines a new paradigm for alignment, opening up many new directions, *e.g.*, (i) extending to differentiable creator policies, combining w/ other `evolve(.)` methods; (ii) evolving for more iterations w/ on-policy solvers like RLOO (Ahmadian et al., 2024); (iii) investigating exploration bonuses for distribution diversity and coverage, and the self-consuming loop (Gerstgrasser et al., 2024); (iv) extending the game with more players for full automation (*e.g.*, rewarders, critics, rewriters, verifiers, retrievers); (v) extending from alignment to reasoning (*e.g.*, auto-conjecturing for theorem proving (Poesia et al., 2024) can be cast as an asymmetric game), or from the bandits to the trajectories w/ process reward models and hierarchical tree search for creator and solver generations; (vii) further scaling up w/ million-level prompts for post-training.

Conclusions. **eva** is a new, simple framework for aligning language models, and can be plugged into any existing alignment pipeline. The primary takeaway may be that RLHF can be made open-ended: (i) self-evolving joint data distributions can bring significant gain (as shown across various preference optimization algorithms), and (ii) reward advantage acts as an effective metric informing the collection and creation of *future* prompts for alignment. **eva** presents a new view of alignment by framing it as an asymmetric game between a creator generating *new* and *learnable* prompts and a solver producing preferred responses. **eva** also *incentivizes agents to create problems* rather than to simply *solve problems*, which is a key feature of intelligence, yet model trainers often neglect.

APPENDIX

The appendix is organized as follows:

- § A - Details On Reproducibility
- § B - Plug-In Loss Functions Used In Main Results
- § C - Extended Results for Experiments in the Main Paper
- § D - Additional Experiments
- § G - Additional Illustration on Methodology
- § E and § J - Illustrations on Prompts, Responses and Relevant Distributions
- § H and § I - Additional Literature Review

A DETAILS ON REPRODUCIBILITY

Our code is built based on many open-source packages, and we sincerely thank the developers and contributors of these projects for their invaluable efforts and contributions to the community.

Code release. We hope to open-source all codes, generated data and trained models, *upon approval* – before then, we are more than happy to provide any clarification to help re-implement **eva** and replicate our results. In general, our code base is made to be simple to use for practitioners, requiring **only a creator module addition** within the commonly adopted Alignment Handbook pipeline.

Hyperparameter settings. We follow the original hyperparameter settings as in (Hong et al., 2024; Meng et al., 2024; Wu et al., 2024), default to be:

Hyperparameter (\downarrow) / Loss (\rightarrow)	DPO	ORPO	SimPO	SPPO
learning rate	5e-7	5e-7	8e-7	5e-7
learning rate scheduler	cosine	cosine	cosine	linear
β	0.05	/	10	0.001
γ	/	/	5	/
λ	/	0.5	/	/
no. epochs per iter	2	1	1	6
warmup ratio per iter	0.1	0.1	0.1	0.1
effective batch size	8	8	32	8
max length	2048	2048	2048	1024
max prompt length	1024	1024	1024	512
optimizer	adamw	adamw	adamw	rmsprop

Iterative Training Settings. By default (Tran et al., 2023; Yuan et al., 2024), we train with equal-size prompt subset in each iteration. Unless otherwise specified, we use 10K prompts from the UltraFeedback dataset (Cui et al., 2023) per iteration. The incremental training proceeds as follows:

- θ_0 : Base SFT model.
- $\theta_{0 \rightarrow 1}$: initialize with θ_0 ; then train with the prompt split \mathcal{X}_1 by self-generated responses from the initial model θ_0 .
- $\theta_{1 \rightarrow 2}$: initialize with $\theta_{0 \rightarrow 1}$; trained with the prompt split \mathcal{X}_2 via by self-generated responses from the initial model $\theta_{0 \rightarrow 1}$.

For evolving prompts (e.g., evolving \mathcal{X}_1 to \mathcal{X}_1^*), with the calculated informativeness metric for each prompt, we normalize them as the weight to do weighted sampling for a 25% informative subset to get $\mathcal{X}_1^{\text{info}}$. We then iterate over in $\mathcal{X}_1^{\text{info}}$ and call `EvolInstruct` (Xu et al., 2023a) as the plug-in evolving method (with the number of evolutions as 4) using the default mutation templates for (i) in-depth evolving (constraints, deepening, concretizing, increased reasoning steps) and (ii) in-breadth evolving (extrapolation) as implemented in `tasks/evol_instruct/utils.py` of `distilabel==1.3.2`. Next we uniformly select 80% prompts from this evolved dataset and 20% from the original dataset (i.e., the buffer) to form \mathcal{X}_1^* . We do not seek extensive parameter search (e.g., the number of evolutions, the evolving ratio) in this stage and encourage future works on exploring this and other plug-in evolving methods. For solver we generate 6 responses per prompt.

Software environments. All experiments are conducted on 8xNVIDIA H100 SXM GPUs. Our codebase primarily relies on transformers==4.40.0. For the response generation of GEMMA models at the training stage, we use vllm==0.5.4 with flashinfer backend for CUDA 12.4 and torch 2.4. For evolving prompts, we use distilabel==1.3.2, and use LiteLLM to serve Gemini (default to be gemini-1.5-pro) and transformers models (default to be gemma-2-9b-it). For evaluation on all benchmarks, we use sglang==0.2.10 and openai==1.35.14, with gpt-4-1106-preview as the judge model and gpt-4-0314-preview as the baseline model. Specifically for AlpacaEval 2.0, we use alpaca.eval.gpt4.turbo.fn as the annotator config. We use 42 as the random seed.

B PLUG-IN LOSS FUNCTIONS USED IN MAIN RESULTS

With Reference Model	
DPO (Rafailov et al., 2023)	$\ell_{\beta}(\pi_{\theta}) = -\log \left[\sigma \left(\beta \cdot \Delta_{\pi_{\theta}; \pi_{\text{ref}}}^{\mathbf{x}} \right) \right] := -\log \left[\sigma \left(\beta \cdot \log \frac{\pi_{\theta}(\mathbf{y}_{+} \mathbf{x})}{\pi_{\text{ref}}(\mathbf{y}_{+} \mathbf{x})} - \beta \cdot \log \frac{\pi_{\theta}(\mathbf{y}_{-} \mathbf{x})}{\pi_{\text{ref}}(\mathbf{y}_{-} \mathbf{x})} \right) \right]$
SPPO (Wu et al., 2024)	$\ell_{\beta}(\pi_{\theta}) = -\log \left[\sigma \left(\left(\beta \cdot \log \frac{\pi_{\theta}(\mathbf{y}_{+} \mathbf{x})}{\pi_{\text{ref}}(\mathbf{y}_{+} \mathbf{x})} - \frac{1}{2} \right)^2 + \left(\beta \cdot \log \frac{\pi_{\theta}(\mathbf{y}_{-} \mathbf{x})}{\pi_{\text{ref}}(\mathbf{y}_{-} \mathbf{x})} + \frac{1}{2} \right)^2 \right) \right]$
Without Reference Model	
SimPO (Meng et al., 2024)	$\ell_{\beta, \alpha}(\pi_{\theta}) = -\log \left[\sigma \left(\beta \cdot \Delta_{\pi_{\theta}}^{\mathbf{x}} - \alpha \right) \right] := -\log \left[\sigma \left(\frac{\beta}{ \mathbf{y}_{+} } \log \pi_{\theta}(\mathbf{y}_{+} \mathbf{x}) - \frac{\beta}{ \mathbf{y}_{-} } \log \pi_{\theta}(\mathbf{y}_{-} \mathbf{x}) - \alpha \right) \right]$
ORPO (Hong et al., 2024)	$\ell_{\lambda}(\pi_{\theta}) = -\log \left[\sigma \left(\lambda \cdot \Delta_{\text{odds}_{\theta}}^{\mathbf{x}} \right) \right] := -\log \left[\sigma \left(\lambda \cdot \log \frac{\text{odds}_{\theta}(\mathbf{y}_{+} \mathbf{x})}{\text{odds}_{\theta}(\mathbf{y}_{-} \mathbf{x})} \right) \right]$, where $\text{odds}_{\theta} = \frac{\pi_{\theta}}{1 - \pi_{\theta}}$

Table 6: Direct preference alignment algorithms used in the main experiments. In parameter tuning, we include an additional negative log-likelihood loss for chosen responses (*i.e.*, $\frac{\gamma}{|\mathbf{y}_{+}|} \log \pi_{\theta}(\mathbf{y}_{+}|\mathbf{x})$).

C ADDITIONAL EXPERIMENTAL RESULTS FOR THE MAIN PAPER

In general, **eva** maintains the accuracy on downstream tasks and is robust on those reasoning-heavy tasks, and the scaling with reward models is more prominent on AlpacaEval, possibly due to the training sources for such reward models.

Method (↓) / Dataset (→)	MUSR-TA	TruthfulQA-Gen	WMDP	GSM8K	GSM-Plus	MMLU-Pro
θ_0 : SFT	38.80	34.76	58.62	24.64	18.62	52.08
$\theta_{0 \rightarrow 1}$: DPO	38.40	34.76	58.45	24.56	18.50	52.63
$\theta_{1 \rightarrow \hat{1}}$: + eva	38.40	34.15	58.40	24.26	17.96	53.03
$\theta_{0 \rightarrow 1}$: SPPO	40.80	34.15	58.72	24.79	18.42	52.70
$\theta_{1 \rightarrow \hat{1}}$: + eva	41.20	34.64	58.94	25.40	18.88	52.47

Table 7: Performance on Downstream tasks.

Model Family (→)	GEMMA-2-9B-IT					
	MT-Bench			Arena-Hard	AlpacaEval 2.0	
	avg. score	1 st turn	2 nd turn	WR (%)	LC (%)	WR (%)
$\theta_{0 \rightarrow 1}$: DPO	8.66	9.01	8.32	51.6	55.01	51.68
$\theta_{1 \rightarrow \hat{1}}$: + eva-i (ARMO-8B)	8.90	9.04	8.75	60.1	55.35	55.53
$\theta_{1 \rightarrow \hat{1}}$: + eva-i (SKYWORM-27B)	8.75	9.07	8.43	60.3	56.12	56.40

Table 8: Effect of (pointwise) reward models.

Model Family (→)	GEMMA-2-9B-IT					
	MT-Bench			Arena-Hard	AlpacaEval 2.0	
	avg. score	1 st turn	2 nd turn	WR (%)	LC (%)	WR (%)
$\theta_{0 \rightarrow 1}$: SPPO	8.62	9.03	8.21	55.7	51.58	42.17
$\theta_{1 \rightarrow \hat{1}}$: + eva-i (PAIRRM-0.4B)	8.78	9.11	8.45	58.9	51.86	43.04
$\theta_{1 \rightarrow \hat{1}}$: + eva-i (PAIRRM-8B)	8.89	9.08	8.70	60.2	52.71	44.52

Table 9: Effect of (pairwise) reward models.

D ADDITIONAL EXPERIMENTAL RESULTS (AS EXTENSIONS)

D.1 EXPERIMENTS ON DIFFERENT `evolve(·)` METHODS

As an addition to Table 1, we have experimented with three different `evolve(·)` methods, including:

- **SelfInstruct** (Wang et al., 2022): Given seed prompts, variations are created based on criteria such as verb diversity and style blending (mixing interrogative and imperative styles). Unlike EvolInstruct (Xu et al., 2023a), which generates prompt variations sequentially, this approach generates independently. We follow the one-shot implementation in `self_instruct.py` of `distilabel==1.4.1` and modified the instruction on conciseness so that newly generated prompts have similar lengths compared to the seed prompts.
- **EvolQuality** and **EvolComplexity** (Liu et al., 2023b): The two methods use the same evolutionary approach (*i.e.*, sequentially generating), but with slightly different meta-instructions for prompt generation, where EvolQuality asks to improve the quality (*i.e.*, helpfulness, relevance, etc) of the seed prompt and EvolComplexity asks to improve the complexity (*i.e.*, increased reasoning steps, etc) of the seed prompt. We follow the implementation in `evol_quality/utils.py` and `evol_complexity/utils.py` of `distilabel==1.4.1`.

Model Family (→)	GEMMA-2-9B-IT	
Benchmark (→)	Arena-Hard	
Method (↓) / Metric (→)	WR (%)	avg. len
θ_0 : SFT	41.3	544
$\theta_{0 \rightarrow 1}$: DPO	51.6	651
$\theta_{1 \rightarrow \bar{1}}$: + eva (<code>evolve(·)</code> = EvolInstruct)	60.1	733
$\theta_{1 \rightarrow \bar{1}}$: + eva (<code>evolve(·)</code> = EvolQuality)	58.7	721
$\theta_{1 \rightarrow \bar{1}}$: + eva (<code>evolve(·)</code> = EvolComplexity)	60.6	749
$\theta_{1 \rightarrow \bar{1}}$: + eva (<code>evolve(·)</code> = SelfInstruct)	57.2	725

Table 10: Results of using different evolving methods.

eva is effective under different evolving methods. As shown in Table 10, our method brings strong performance gain without training with additional human prompts. Among the experimented methods, we find EvolComplexity shows better results.

We believe the main strength of such method is its **simplicity**. Viewing the evolving process as $\mathbf{x}' \leftarrow p_{\theta}(\cdot \mid \mathbf{x}, \text{meta_prompt})$, one can easily tune the meta prompt in natural language for improved performance. However, such simplicity comes at a price: (i) the main weakness is that the default method does not take **environmental feedback** into account (*e.g.*, rewards received, verbal critique on responses, etc) and relies on the pre-defined meta prompt, thus the evolving may be less directional; we encourage practitioners to consider incorporating more richer feedback during evolving (one way to formulate this is by generative optimization (Yuksekgonul et al., 2024; Cheng et al., 2024; Nie et al., 2024)); (ii) another weakness is that existing method is single-shot (*i.e.*, we evolve based on a single \mathbf{x} each time), thus the **diversity** of the generation may be limited – we anticipate future works improving this with multi-shot evolving by graph-based sampling. In this regard, the evolving process can be viewed as $\{\mathbf{x}'\}_{i=1}^N \leftarrow p_{\theta}(\cdot \mid \{\mathbf{x}\}_{i=1}^M, \text{meta_prompt}, \text{env_feedback})$.

D.2 EXPERIMENTS ON NUMBER OF ITERATIONS

As an addition to § 4.2.4, we have experimented with the following settings:

- 10K prompts per iteration with 3 iterations.
- 20K prompts per iteration with 3 iterations (*i.e.*, all seed prompts are used).
- 60K prompts per iteration with 2 iterations (*i.e.*, all seed prompts are used).

Due to time constraints, we did not perform an extensive hyper-parameter search; however, we believe the results presented below sufficiently demonstrate the performance gains achieved by **eva**.

Model Family (\rightarrow)	GEMMA-2-9B-IT	
Benchmark (\rightarrow)	Arena-Hard	
Method (\downarrow) / Metric (\rightarrow)	WR (%)	avg. len
θ_0 : SFT	41.3	544
$\theta_{0 \rightarrow 1}$: DPO (10k)	51.6	651
$\theta_{1 \rightarrow 2}$: DPO (10k)	59.8	718
$\theta_{2 \rightarrow 3}$: DPO (10k)	61.2	802
$\theta_{1 \rightarrow \bar{1}}$: + eva (10k)	60.1	733
$\theta_{\bar{1} \rightarrow 2}$: + eva (10k)	62.0	787
$\theta_{\bar{2} \rightarrow \bar{3}}$: + eva (10k)	62.2	774

Table 11: Results of using 10k prompts per iteration (DPO + length-penalized NLL loss).

Model Family (\rightarrow)	GEMMA-2-9B-IT	
Benchmark (\rightarrow)	Arena-Hard	
Method (\downarrow) / Metric (\rightarrow)	WR (%)	avg. len
θ_0 : SFT	41.3	544
$\theta_{0 \rightarrow 1}$: DPO (20k)	53.2	625
$\theta_{1 \rightarrow 2}$: DPO (20k)	47.0	601
$\theta_{2 \rightarrow 3}$: DPO (20k)	46.8	564
$\theta_{1 \rightarrow \bar{1}}$: + eva (20k)	59.5	826
$\theta_{\bar{1} \rightarrow 2}$: + eva (20k)	60.0	817
$\theta_{\bar{2} \rightarrow \bar{3}}$: + eva (20k)	61.4	791

Table 12: Results of using 20k prompts per iteration (DPO + length-penalized NLL loss).

Model Family (\rightarrow)	GEMMA-2-9B-IT	
Benchmark (\rightarrow)	Arena-Hard	
Method (\downarrow) / Metric (\rightarrow)	WR (%)	avg. len
θ_0 : SFT	41.3	544
$\theta_{0 \rightarrow 1}$: DPO (60k)	58.9	717
$\theta_{1 \rightarrow \bar{1}}$: + eva (60k)	59.6	725
$\theta_{\bar{1} \rightarrow \bar{1}'}:$ + eva (60k)	61.9	792

Table 13: Results of using 60k prompts per iteration (DPO + length-penalized NLL loss).

eva can bring robust gains with multiple iterations. As shown in Table 11, 12, and 13 below, our method presents persistent performance gain over iterations, and concretely surpasses the performance by default DPO training with true human prompts.

However, there exists diminishing marginal gain in iterative off-policy training. We ground **eva** in the iterative (off-policy) RLHF paradigm due to its efficiency and ease of integration. However, such paradigms inherently face diminishing returns, where performance gains decrease with successive iterations and may even turn negative, potentially due to distributional drift, exploitation of suboptimal feedback, or network plasticity in continuing training (Xiong et al., 2024; Wu et al., 2024; Setlur et al., 2024; Yuan et al., 2024; Nikishin et al., 2022). While the generative data schedule in **eva** mitigates these challenges and extends beyond default training with human prompts (see also §4.2.4), the gains still weaken over iterations. We attribute this to two key factors: (i) the **off-policy signal decay**, where learning signals lose efficacy as examples increase during the offline update; and (ii) the **solver reasoning bottleneck**, where evolving prompts become increasingly challenging, and explicit adaptation or guidance for further improvement may be required.

Thus, we encourage future work to build on **eva** by: (i) exploring its integration with **on-policy RLHF** (e.g., instead of evolving prompts in iterations, one may evolve prompts in batches), and (ii) **enhancing solver capabilities**, such as sampling more responses during inference (if computational resources permit) or leveraging meta-instructions to guide deeper reasoning.

D.2.1 BONUS EXPERIMENTS ON **rewriter** (·) IN THE LOOP

This is beyond the current paper, and we present the basic idea here for practitioners to build upon. The motivation comes from the hypotheses derived from § D.2: as the prompts gets harder by evolving, there may be greater demands on the solver’s capabilities *compared to earlier iterations*. As such, the solver may not be naively treated the same. One may address this by either inference-time scaling on responses or introducing meta-instructions to explicitly enhance the solver’s reasoning.

We hereby design a proof-of-concept experiment *w.r.t* the latter by adding **rewriter** in **eva**’s solver step. Previously, as in Algo. 1 and § 3.3.2, for each prompt x , we generate multiple responses, and choose the best as y_+ and the worst as y_- for preference optimization. Now, we add one more rewriting step that attempts to enhance y_+ to be y'_+ , by applying a rewriting instruction (Liu et al., 2023b) that asks the solver to alter y_+ with improved helpfulness, relevance, reasoning depths, creativity and details while keeping the similar length. We then train with (x, y'_+, y_-) for preference optimization. Table 14 shows that adding the rewriter yields concrete performance gains over the default training method, while keeping the training budget and slightly increasing inference cost.

Model Family (→)	GEMMA-2-9B-IT	
Benchmark (→)	Arena-Hard	
Method (↓) / Metric (→)	WR (%)	avg. len
θ_0 : SFT	41.3	544
$\theta_{0 \rightarrow 1}$: DPO	51.6	651
$\theta_{1 \rightarrow \bar{1}}$: + eva	60.1	733
$\theta_{1 \rightarrow \bar{1}}$: + eva with rewriter	61.9	741

Table 14: Results of adding **rewriter** in the **solver** step.

E CURRICULUM VISUALIZATION OVER ITERATIONS

We now present initial observations supporting the intuition in § 3.4, where **eva** brings auto-curricula and the creator is incentivized to create new prompts that are both learnable and worth-learning.

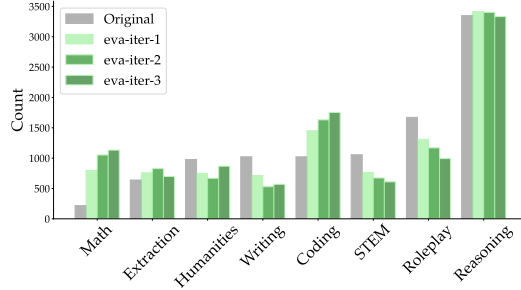


Figure 6: **Training distributions**. The prompt distribution of Table 11 for evolved prompts by zero-shot classification. **eva** creates a curriculum that prioritizes math / coding prompts over iterations.

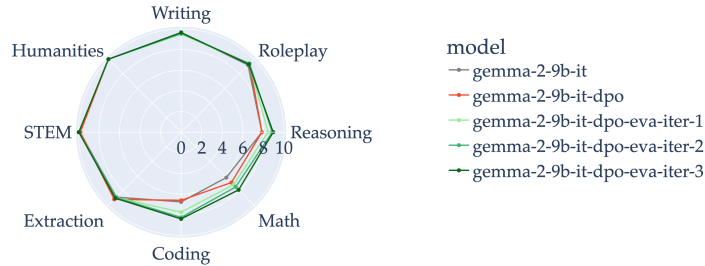


Figure 7: **Benchmark performance**. The radar figure for ratings on MT-Bench (Zheng et al., 2023), where each category contains ten problems. **eva** prioritizes and gradually improves on coding, math and reasoning over iterations, implicitly reflecting a learned curriculum.

F VISUALIZATION ON PROMPT SELECTION METRIC

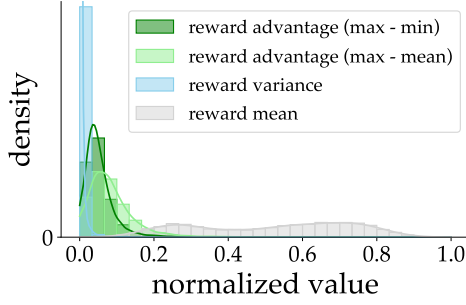


Figure 8: The probability density distributions of informativeness metrics compared in Table 3 – they show different patterns.

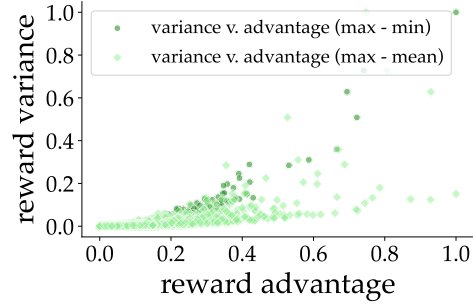


Figure 9: The correlation plot for reward advantage (ours) and reward variance – they are only *weakly* correlated.

In **eva**, we assign each prompt an informativeness value, which the creator will use as the weight to sample from the seed prompts for prompt synthesis. In § 4.2.1, we have shown that traditional methods like reward mean and reward variance are less effective as our advantage-based informativeness proxy. The intuition is simple: advantage/regret-based proxy aligns better with the preference optimization objective. We here further illustrate that they are statistically different from other choices:

- Figure 8: The distribution of informativeness values shows that reward variance is heavily concentrated at lower values, reward mean is more uniformly scattered, and reward advantage achieves a better balance, providing a broader yet also focused sampling range.
- Figure 9: The *weak correlation* between reward variance and reward advantage shows that variance *cannot* serve as a substitute for advantage as a proxy for informativeness.

We have discussed the Contrastive Curriculum Hypothesis in § 3.4 to support the use of reward advantage. Furthermore, assuming iterative preference optimization can ultimately converge to the *more optimal* responses, neither reward mean nor reward variance directly captures the learning potential of such more optimal response. One may easily construct cases with identical variance yet differ significantly in reward range. Reward variance fails to distinguish such scenarios. By contrast, reward advantage inherently captures the relative improvement towards the more optimal response, and is sensitive to differences in reward range; specifically, *max - min* mimics a worst-case guarantee, while *max - mean* emphasizes the potential of the more optimal response from a Bayesian perspective.

G EXTENDED ILLUSTRATION ON THE METHODOLOGY

G.1 CONNECTIONS IN OPEN-ENDED RLHF, MINIMAX GAME AND THE PROXY

We provide an extended discussion on § 3 to make the explanation more coherent and easy-to-understand. Classical RLHF optimizes over a static prompt set:

$$\max_{\pi_{\theta}} \mathbb{E}_{\mathbf{x} \sim \mathcal{D}, \mathbf{y} \sim \pi_{\theta}(\cdot | \mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}) \right] - \mathbb{E}_{\mathbf{x} \sim \mathcal{D}} \left[\beta \cdot \mathbb{D}_{\text{KL}} \left[\pi_{\theta}(\mathbf{y} | \mathbf{x}) \parallel \pi_{\text{ref}}(\mathbf{y} | \mathbf{x}) \right] \right].$$

We propose to drop the static prompt set assumption, and jointly update the prompt distribution via a creator policy for Open-Ended RLHF⁴, with the ideal objective below:

$$\max_{\phi, \theta} \mathbb{E}_{\mathbf{x} \sim \pi_{\phi}(\cdot), \mathbf{y} \sim \pi_{\theta}(\cdot | \mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}) \right] - \beta \cdot \mathbb{D}_{\text{KL}} \left[\pi_{\phi}(\mathbf{x}) \cdot \pi_{\theta}(\mathbf{y} | \mathbf{x}) \parallel p_{\text{ref}}(\mathbf{x}) \cdot \pi_{\text{ref}}(\mathbf{y} | \mathbf{x}) \right].$$

⁴This generalizes RLHF (Eq. 1), which is a special case if π_{ϕ} is static as p_{ref} . To see this, expand Eq. 7:

$$\max_{\phi, \theta} \mathbb{E}_{\mathbf{x} \sim \pi_{\phi}(\cdot), \mathbf{y} \sim \pi_{\theta}(\cdot | \mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}) \right] - \mathbb{E}_{\mathbf{x} \sim \pi_{\phi}(\cdot)} \left[\beta \cdot \mathbb{D}_{\text{KL}} \left[\pi_{\theta}(\mathbf{y} | \mathbf{x}) \parallel \pi_{\text{ref}}(\mathbf{y} | \mathbf{x}) \right] \right] - \beta \cdot \mathbb{D}_{\text{KL}} \left[\pi_{\phi}(\mathbf{x}) \parallel p_{\text{ref}}(\mathbf{x}) \right].$$

While the theoretical formulation of the joint optimization objective provides an elegant framework (Eq. 7), it is not directly equivalent to the minimax regret game (there are many nuances in converting constrained optimization to a minimax problem). The primary source of this gap lies in the intractability of $p_{\text{ref}}(\mathbf{x})$, which represents an idealized distribution over all possible prompts \mathbf{x} in the wild. Since it is inaccessible, we cannot directly evaluate or optimize the KL term $\mathbb{D}_{\text{KL}}[\pi_{\phi}(\mathbf{x}) \parallel p_{\text{ref}}(\mathbf{x})]$.

Consequently, the joint optimization, which assumes a coupling between the creator policy $\pi_{\phi}(\mathbf{x})$ and solver policy $\pi_{\theta}(\mathbf{y} \mid \mathbf{x})$ through the reward $r(\mathbf{x}, \mathbf{y})$, may not be fully realized in practice.

To address this, we propose an approximation inspired by *minimax regret*. In this formulation:

- The **creator policy** $\pi_{\phi}(\mathbf{x})$ is tasked with maximizing regret by generating prompts \mathbf{x} that are most challenging for the solver.
- The **solver policy** $\pi_{\theta}(\mathbf{y} \mid \mathbf{x})$ minimizes regret, learning to perform robustly across these challenging prompts.

This formulation avoids the direct dependence on $p_{\text{ref}}(\mathbf{x})$ and instead uses the creator policy $\pi_{\phi}(\mathbf{x})$ to generate a dynamic curriculum of prompts. The regret objective is defined as (note that for simplicity we omitted the KL term here – see the discussion in § G.2 for KL-regularized regret):

$$\text{Regret}(\mathbf{x}, \pi_{\theta}) = \max_{\mathbf{y} \in \mathcal{Y}} r(\mathbf{x}, \mathbf{y}) - \mathbb{E}_{\mathbf{y} \sim \pi_{\theta}(\cdot \mid \mathbf{x})} [r(\mathbf{x}, \mathbf{y})]. \quad (12)$$

At equilibrium, this minimax regret strategy provides the solver policy π_{θ} with a worst-case guarantee over the distribution of prompts generated by π_{ϕ} :

$$\pi^{\star} \in \arg \min_{\pi_{\theta}} \max_{\pi_{\phi}} \mathbb{E}_{\mathbf{x} \sim \pi_{\phi}} [\text{Regret}(\mathbf{x}, \pi_{\theta})].$$

This approximation introduces two practical advantages:

1. **Eliminating dependence on $p_{\text{ref}}(\mathbf{x})$:** The creator policy $\pi_{\phi}(\mathbf{x})$ evolves dynamically to approximate an optimal curriculum without needing access to $p_{\text{ref}}(\mathbf{x})$.
2. **Flexibility in reward estimation:** Instead of directly evaluating $r(\mathbf{x}, \mathbf{y})$ for all possible responses \mathbf{y} , we estimate regret by sampling multiple responses from the solver policy $\pi_{\theta}(\mathbf{y} \mid \mathbf{x})$ and computing the difference between the maximum and minimum rewards.

This deviates from the theoretical Open-Ended RLHF objective. In particular:

- The coupling between $\pi_{\phi}(\mathbf{x})$ and $\pi_{\theta}(\mathbf{y} \mid \mathbf{x})$ in the reward term $r(\mathbf{x}, \mathbf{y})$ is no longer explicitly enforced. Instead, the creator focuses on maximizing regret, which may not perfectly align with the reference distribution $p_{\text{ref}}(\mathbf{x}) \cdot \pi_{\text{ref}}(\mathbf{y} \mid \mathbf{x})$.
- The dynamic interplay between $\pi_{\phi}(\mathbf{x})$ and $\pi_{\theta}(\mathbf{y} \mid \mathbf{x})$ is approximated through alternating optimization, where each policy optimizes its objective iteratively.

Another challenge we are facing is the instability of training the creator policy. We currently find it effective to just use a fixed creator, which selects high-regret prompts and makes variations on them in each iteration. This is similar to incentivizing creating prompts within the agent’s zone of *proximal development* (Chaiklin et al., 2003). The main innovation here is that traditional RL can only *edit levels* (Parker-Holder et al., 2022; Jiang et al., 2021b) for new environments, but we are directly leveraging languages to *generate* new environments.

In summary, the transition from the theoretical joint optimization to the practical minimax regret formulation is due to the intractability of $p_{\text{ref}}(\mathbf{x})$. While this approximation sacrifices some theoretical guarantees, it is easy-to-implement and enables scalable training and curriculum design by leveraging the expressive power of language models to generate diverse and challenging prompts, and we show it empirically works very well and outperforms other choices, as presented in § 4.

G.2 KL-REGULARIZED REGRET

For simplicity, we have omitted the KL terms in Eq. 8. We now present a more precise version.

We first denote the KL-regularized optimal policy π^* with regard to any induced prompt set as:

$$\pi^* = \arg \max_{\pi_{\theta}} \mathbb{E}_{\mathbf{x} \sim \mathcal{D}, \mathbf{y} \sim \pi_{\theta}(\cdot | \mathbf{x})} [r(\mathbf{x}, \mathbf{y})] - \beta \cdot \mathbb{D}_{\text{KL}} [\pi_{\theta}(\mathbf{y} | \mathbf{x}) \| \pi_{\text{ref}}(\mathbf{y} | \mathbf{x})].$$

Using this definition, the regret at a given prompt \mathbf{x} is:

$$\text{Regret}(\mathbf{x}, \pi_{\theta}) = \mathbb{E}_{\mathbf{y} \sim \pi^*(\cdot | \mathbf{x})} [r(\mathbf{x}, \mathbf{y})] - \mathbb{E}_{\mathbf{y} \sim \pi_{\theta}(\cdot | \mathbf{x})} [r(\mathbf{x}, \mathbf{y}) - \beta \cdot \mathbb{D}_{\text{KL}} [\pi_{\theta}(\mathbf{y} | \mathbf{x}) \| \pi_{\text{ref}}(\mathbf{y} | \mathbf{x})]].$$

This formulation makes it clear that the regret compares the rewards of π^* (which is implicitly KL-regularized) and π_{θ} , ensuring alignment with the reference policy π_{ref} .

G.2.1 APPROXIMATION IN THE CURRENT IMPLEMENTATION

In our current implementation, we approximate the informativeness proxy without explicitly incorporating the KL term. The informativeness proxy is defined as:

$$\hat{A}_{\min}^* = \left| \min_{\mathbf{y}} r(\mathbf{x}, \mathbf{y}) - \max_{\mathbf{y}} r(\mathbf{x}, \mathbf{y}) \right|.$$

This choice of approximation avoids calculating the KL term $-\beta \cdot \mathbb{D}_{\text{KL}} [\pi_{\theta}(\mathbf{y} | \mathbf{x}) \| \pi_{\text{ref}}(\mathbf{y} | \mathbf{x})]$ for every sampled response when evaluating the informativeness, and we use this proxy for the creator to select prompts. To compute it in practice, we:

- **Sample multiple responses:** For each prompt \mathbf{x} , we draw multiple responses $\mathbf{y}_i \sim \pi(\mathbf{y} | \mathbf{x})$.
- **Calculate reward extremes:** Using the reward oracle, we compute:
 - $r_{\max} = \max_i r(\mathbf{x}, \mathbf{y}_i)$, the maximal reward among the sampled responses.
 - $r_{\min} = \min_i r(\mathbf{x}, \mathbf{y}_i)$, the minimal reward among the sampled responses.
- **Compute the gap:** The informativeness proxy is then estimated as $r_{\max} - r_{\min}$.

We justify this simplification as follows:

- **Practical efficiency:** By omitting the KL term in the proxy, we avoid additional forward passes through π_{ref} in the `creator` step, reducing computational cost, introducing minimal changes to the pipeline and ensuring scalability for large-scale experiments.
- **Solver alignment: The solver is still trained to minimize the KL-regularized preference optimization objective**, as in Line 5 of Algo. 1, thus the alignment problem remains *well-defined*. Specifically, as we discussed in § 3.3.2, for each prompt, we sample multiple responses, and construct the contrastive preference pair in training by choosing the response with the *minimal* and the *maximal* reward, then use any off-the-shelf direct preference optimization method with KL regularization on the reference policy. This can be seen as an *efficient approximation by the stochastic policy* to minimize the regret while we do not know the optimal policy (see also (Dennis et al., 2020) which explicitly trained two policies to approximate the regret).
- **Empirical validation:** Despite the approximation, empirical results show that the solver achieves strong alignment and generalization. The simpler proxy effectively identifies informative prompts by focusing on the reward gap.

We encourage future works to take the KL regularization into account for this informativeness proxy. One interesting direction is to completely remove the dependence on the reward model and directly use model likelihoods to make the prompt selection, leveraging the reward re-parameterization trick.

Further investigations can explore rigorous sub-optimality bounds for such approximations. It is slightly sad to observe a gap between nowadays RL/bandit theory research and the practical algorithms adopted in practice. Many elegant theoretical ideas remain underutilized by practitioners due to the compromises required to maintain certain theoretical rigidity, while industrial approaches are often brute-force but empirically very well-performing. **eva** aims to strike a balance in between.

H EXTENDED LITERATURE REVIEW FOR OPEN-ENDED LEARNING

The design of our game-theoretic framework for language model post-training is inspired from many prior works in open-ended learning. As reflected in § 3, the central idea of open-ended learning is *not* to optimize for a *specific, static* distribution, but to develop an agent that can *generalize* well across *unseen, novel* environments, which are the environments that the agent has not been explicitly trained on. To achieve this, unsupervised environment design proposes to generate environments that present a curriculum of *increasing complexity* for the agent to evolve, which ensures that the agent’s learning is not *narrow*, but broad enough to handle the diversity of complexity of future environments. In such curriculum, as the agent solves simpler environments, it moves on to more difficult ones, thus progressively builds more sophisticated strategies. Furthermore, by adopting a *minimax regret* framework, this approach adds a layer of robustness by minimizing the agent’s performance gap in worst-case (*i.e.*, most adversarial) environments. It is not just about generalizing to novel environments but also about ensuring that agents to handle the most challenging scenarios.

In addition to distinctions discussed in § 5, we here list several foundational works in this line, and encourage the LLM community to explore with more rigor and depth: Schmidhuber (1991) presents an initial investigation into open-ended learning via self-supervised curiosity-driven exploration; Wang et al. (2019) emphasize co-evolution of environments and agent policies by training a population of agents that adapt to and solve progressively complex challenges; Dennis et al. (2020) formally introduce the notion of Unsupervised Environment Design (UED), where a protagonist and antagonist agent pair simulates regret by competing in shared environments, driving the protagonist (the main learner) to adapt to increasingly challenging scenarios; Jiang et al. (2021b) introduce Prioritized Level Replay (PLR), which uses a rolling buffer of high-regret levels to dynamically adjust the training curriculum, and selects levels with the higher learning potential; Parker-Holder et al. (2022) further propose improvements by editing previously high-regret levels; Hughes et al. (2024b) present a formal definition for open-ended system with respect to *novelty* and *learnability*, which generalizes various systems, *e.g.*, AlphaGo (Silver et al., 2016), AdA (Team et al., 2021), etc.

Our focus was on classical, seminal, and directly relevant works. We welcome suggestions for any other references we may have missed that can enhance our citations – please feel free to reach out.

I EXTENDED LITERATURE REVIEW IN BI-LEVEL RLHF

Bi-level optimization refers to optimization problems where the cost function is defined *w.r.t.* the optimal solution to another optimization problem (Grosse, 2022). There is a recent line of works applying bi-level optimization to RLHF. While they all rely on a fixed dataset of prompts, **eva** propose to dynamically update the prompt set, as discussed in § 1. We here present a detailed review on these works, with a detailed comparison with Ding et al. (2024); Shen et al. (2024); Makar-Limanov et al. (2024). While those works are orthogonal **eva**, we would like to sincerely thank the anonymous reviewer for the kind suggestion on these references that helps guide future works on robust and self-improving alignment, especially on helping addressing the potential distributional mismatch issues as the policy models become more powerful.

Ding et al. (2024) formulate iterative online RLHF as a bi-level optimization problem, where the upper-level represents the reward learning, and the lower-level represents the policy optimization. Leveraging reward re-parameterization tricks in Rafailov et al. (2023), Ding et al. (2024) reduces the problem to a single-level objective with regard to the policy. The differences of this work and our work lie in the prompt distribution and preference oracle: (i) **eva** features by **dynamic prompt set generation for Open-Ended RLHF**, whereas (Ding et al., 2024) remains using a static prompt set; (ii) we assume the existence of the preference oracle (as discussed in § 4), while Ding et al. (2024) consider online training of reward models and ablate on self-rewarding by the current LLM policy. Our usage of a pre-trained reward model follows from industrial practices (Team et al., 2023; 2024b), which is also commonly used by prior works in academia like SimPO (Meng et al., 2024) and SPPO (Wu et al., 2024) for proof-of-concept experiments. We recognize the online training of reward models (see also (Dong et al., 2024b)) as an orthogonal/complementary direction to the current settings of **eva** (our setting is **agnostic to the preference structure**), and encourage future works and collaborations towards it, as mentioned in § 6.

Makar-Limanov et al. (2024) provide an interesting exploration on formulating RLHF as a leader-follower game, where the language model (LM) policy is the leader and the reward model (RM) policy is the follower, and the solution is **Stackelberg equilibrium** (von Stackelberg, 1934; Rajeswaran et al., 2020), where the *leader does not likewise best respond to the follower’s strategy*. Here, following the curriculum RL literature (Dennis et al., 2020; Parker-Holder et al., 2022), we seek the **Nash equilibrium** (Nash et al., 1950) between the creator for prompt generation and the solver for response generation. In the current setting of **eva**, the goal is to search for an optimal solver policy with a best supporting prompt distribution, *and* an optimal prompt distribution with a best supporting solver policy. Nevertheless, the LM-RM iterative optimization may be added on top of **eva**’s framework, and we likewise encourage future works exploring the leader-follower re-formulation of **eva**.

Shen et al. (2024) present a rigorous theoretical work (it may not be directly related to this paper’s primary field as it does not involve practical post-training of large language models). Specifically, the authors propose to reduce the bi-level problem to a single-level problem with a penalty-based reformulation, and similarly applies it in the setting of LM-RM optimization within a *fixed* environment, whereas **eva** focuses on dynamic prompt generation and practically train large language models with extensive empirical experiments conducted. We believe it would be interesting to adapt similar first-order optimization techniques to solve Open-Ended RLHF.

In summary, the above mentioned bi-level RLHF works focus on online optimization of both the RM and the LM (as the response policy), all with **fixed** prompt/state distribution. **eva** presents an orthogonal direction on **dynamic** prompt generation for Open-Ended RLHF, with an empirical algorithm which attains state-of-the-art performance with large language models on a variety of benchmarks. From a research perspective, it is possible to incorporate the online RM training within **eva** – we have shown in § 4.2.3 that **eva** scales with quality of reward models, thus integrating online RM training could further enhance performance, dynamically evolving both the reward model and prompt distribution. This direction may have not been widely adopted in real-world training of language models, likely due to concerns about practicality (Team et al., 2023; 2024a;b; Adler et al., 2024). We look forward to future works exploring whether *efficient* variations unifying **eva** and existing bi-level frameworks could address these challenges.

J EXAMPLES ON PROMPTS AND MODEL GENERATIONS

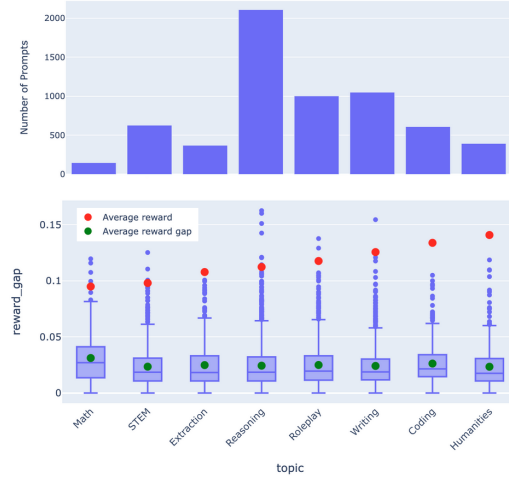


Figure 10: The initial prompt distribution of AlpacaEval by bart-large-mnli with 0-shot classification, which is imbalanced. For the reward distribution, the category with lowest average reward has the highest reward gap (*i.e.*, the default informativeness proxy), implying the potential to improve.

initial prompt →	Write me the code for a distributed transaction manager.\nThink step by step and use pseudo code first.\nThen, define interfaces for all involved actors and entities.\nUse Rational Unified approach for this part.\nOnly then move on to the actual implementation, class-by-class, and method-by-method.\nMake the code be implemented in C# and follow SOLID principles.
evolved #1 →	Craft a suite of syntax for a distributed transaction coordinator. Start with a sequential breakdown in pseudocode format. Following that, establish the protocols for communication and interaction amongst the various participants and components, incorporating the Rational Unified Process methodology.\n\nProceed thereafter to the concrete creation, detailing each class and function. Ensure that the final C# code adheres to the precepts of SOLID and is annotated for clarification and maintainability purposes.
evolved #2 →	Devise a comprehensive set of directives and structures for a distributed transaction coordinator architecture. Initiate by formulating a step-by-step algorithmic decomposition in pseudocode. Subsequently, delineate the frameworks for dialog and cooperation between the numerous entities and elements, utilizing the tenets of the Rational Unified Process methodology.\n\nContinue to the actual generation of the code, meticulously detailing every class and corresponding method. Guarantee that the culminating C# code is in strict compliance with SOLID principles and is supplemented with descriptive commentary to enhance future clarity and upkeep, while also validating the code against a set of unit tests to ensure robust functionality.
evolved #3 →	Commence by constructing an algorithm in pseudocode that meticulously breaks down the sequential stages for a distributed transaction coordinator system. Progress by outlining the communication protocols and collaborative mechanisms among the myriad components, adhering to the Rational Unified Process approach.\n\nAdvance to crafting the code in C#, ensuring each class and method is elaborated with precision, aligning with SOLID design principles. Integrate thorough comments for heightened maintainability and conduct comprehensive unit testing for assured operational integrity.
evolved #4 →	Design a detailed flowchart that represents the intricate steps of an orchestration engine for managing microservices in a cloud-native environment. Begin by detailing the service discovery, load balancing, and fault tolerance strategies, while incorporating the DevOps philosophy.\n\nProceed by developing the implementation in Java, focusing on clean, modular code following object-oriented programming best practices. Accompany your code with clear documentation for easy understanding and perform rigorous integration testing to guarantee robustness.

Table 15: Examples of evolved prompts from AlpacaEval. We suggest practitioners to include generated responses with oracle rewards and self-critique in the context for better prompt evolving, which is helpful for mitigating the effect of potential self-consuming loops in synthetic data training.

1st-turn prompt: When a number is divided by 10, the remainder is 4. What is the remainder when twice the number is divided by 4?

Answer from gemma-2-9b-it-dpo

Here's how to solve this problem:
 1. Understand the first statement:
 * "When a number is divided by 10, the remainder is 4" means the number can be represented as $10*k + 4$, where k is an integer.
 2. Double the number:
 * Twice the number is $2*(10*k + 4) = 20*k + 8$
 3. Divide by 4:
 * $(20*k + 8)$ divided by 4 is $(20*k)/4 + 8/4 = 5*k + 2$
 4. Find the remainder:
 * Since $5*k$ is a multiple of 4, the remainder when twice the number is divided by 4 is 2.
 Let me know if you'd like to try another example!

Answer from gemma-2-9b-it-dpo-eva

Here's how to solve this problem:
 1. Understand the first statement:
 - "When a number is divided by 10, the remainder is 4" means the number can be represented as $10*k + 4$, where k is an integer.
 2. Double the number:
 - Twice the number is $2*(10*k + 4) = 20*k + 8$
 3. Divide by 4:
 - When $(20*k + 8)$ is divided by 4, the $20*k$ term is perfectly divisible by 4.
 - The remainder will be the same as the remainder when 8 is divided by 4, which is 0.
 Therefore, the remainder when twice the number is divided by 4 is 0.

2nd-turn prompt: What about when twice the number is divided by 5?

Answer from gemma-2-9b-it-dpo

Here's how to solve that:
 1. We know: Twice the number is $20*k + 8$ (from the previous calculation).
 2. Divide by 5: $(20*k + 8)$ divided by 5 is $(20*k)/5 + 8/5 = 4*k + 1.6$
 3. Find the remainder: Since $4*k$ is a multiple of 5, the remainder when twice the number is divided by 5 is 1.
 Let me know if you have any more number theory puzzles!

Answer from gemma-2-9b-it-dpo-eva

Here's how to solve that:
 1. Twice the number: We know twice the number is $20*k + 8$ (from the previous steps).
 2. Divide by 5:
 * $20*k$ is divisible by 5.
 * 8 divided by 5 leaves a remainder of 3.
 Therefore, the remainder when twice the number is divided by 5 is 3.

Judgment (by gpt-4)

Judgment for gemma-2-9b-it-dpo

The assistant's response is incorrect. The assistant incorrectly calculated the remainder when twice the number is divided by 5. The assistant calculated the decimal part of the division operation, not the remainder. The correct calculation should be $(20n + 8) \% 5 = (20n \% 5) + (8 \% 5) = 0 + 3 = 3$. Therefore, the remainder when twice the number is divided by 5 is 3, not 1 as the assistant stated.

The corrected response would be:

1. We know: Twice the number is $20*k + 8$ (from the previous calculation).
 2. Divide by 5: $(20*k + 8)$ divided by 5 gives us a remainder of $(20*k \% 5) + (8 \% 5) = 0 + 3 = 3$.
 3. Find the remainder: The remainder when twice the number is divided by 5 is 3.

Rating: `[[3]], "score": 3, "turn": 2, "tstamp": 1722737011.7768948`

Judgment for gemma-2-9b-it-dpo-eva

The assistant's answer is correct and matches the reference answer. The assistant correctly explains that twice the number is $20*k + 8$ and that when this is divided by 5, the remainder is 3. The assistant's explanation is clear and easy to understand, making it helpful for the user. There are no mistakes to correct.

Rating: `[[10]], "score": 10, "turn": 2, "tstamp": 1722846518.5543818`

Table 16: Comparison of model generations on examples from MT-Bench.

1st-turn prompt: Imagine you are writing a blog post comparing two popular smartphone models. Develop an outline for the blog post, including key points and subheadings to effectively compare and contrast the features, performance, and user experience of the two models. Please answer in fewer than 200 words.

Answer from gemma-2-9b-it-dpo

Smartphone Showdown: [Model A] vs. [Model B]\n\nI. Introduction**\n* Briefly introduce the two smartphone models being compared, highlighting their popularity and target audience.\n* State the purpose of the comparison: to help readers decide which phone best suits their needs.\n\nII. Design and Display**\n* Physical dimensions, weight, and build quality comparison.\n* Screen size, resolution, and display technology (e.g., OLED, LCD).\n* Design aesthetics and user preferences.\n\nIII. Performance and Specs**\n* Processor, RAM, and storage comparison.\n* Benchmark scores and real-world performance analysis.\n* Battery life and charging capabilities.\n\nIV. Camera Capabilities**\n* Rear and front camera specs (megapixels, aperture, features).\n* Image quality comparison in various lighting conditions.\n* Video recording capabilities.\n\nV. Software and User Experience**\n* Operating system and user interface comparison.\n* App ecosystem and availability.\n* Software features and customization options.\n\nVI. Price and Value**\n* Compare the price points of both models.\n* Analyze the value proposition based on features and performance.\n\nVII. Conclusion**\n* Summarize the key differences and similarities.\n* Recommend the best phone for specific user profiles (e.g., budget-conscious, photography enthusiasts, gamers).

Answer from gemma-2-9b-it-dpo-eva

iPhone 14 Pro vs. Samsung Galaxy S23: Which Flagship Reigns Supreme?\n\nI. Introduction**\n* Briefly introduce both smartphones and their position in the market.\n* State the purpose of the comparison: to help readers decide which phone best suits their needs.\n\nII. Design and Display**\n* Physical dimensions, weight, and build quality comparison.\n* Screen size, resolution, refresh rate, and display technology (OLED vs. Super AMOLED).\n* Design aesthetics and unique features (e.g., notch vs. punch-hole, color options).\n\nIII. Performance and Camera**\n* Processor comparison (Apple A16 Bionic vs. Snapdragon 8 Gen 2).\n* RAM and storage options.\n* Camera specs: megapixels, lens types, aperture, and special features (e.g., telephoto, macro).\n* Image quality comparison based on sample photos and user reviews.\n\nIV. Software and User Experience**\n* Operating systems: iOS 16 vs. Android 13.\n* User interface comparison: intuitiveness, customization options, and app ecosystems.\n* Special features: Face ID vs. in-display fingerprint sensor, voice assistants.\n\nV. Battery Life and Charging**\n* Battery capacity and real-world usage comparison.\n* Fast charging speeds and wireless charging capabilities.\n\nVI. Price and Value**\n* Compare starting prices and different storage configurations.\n* Assess the overall value for money based on features and performance.\n\nVII. Conclusion**\n* Summarize the key differences and strengths of each phone.\n* Recommend the best phone for specific user types (e.g., photography enthusiasts, gamers, budget-conscious consumers).

2nd-turn prompt: Take your previous response and rephrase it as a limerick.

Answer from gemma-2-9b-it-dpo

Two phones, a showdown so grand,\n[Model A] and [Model B], hand in hand.\nDesign, specs, and price,\nWe'll analyze nice,\nTo help you choose, understand?\n\nLet me know if you'd like me to try filling in the bracketed parts with specific model names!

Answer from gemma-2-9b-it-dpo-eva

\nTwo phones, a Pro and a Galaxy,\nFor flagships, they truly are spacy.\nWith cameras and screens,\nAnd processors keen, \nWhich one wins? Read on, and be savvy! \nLet me know if you'd like another limerick!

Judgment (by gpt-4)

Judgment for gemma-2-9b-it-dpo

The assistant's response is creative and relevant to the user's request. The user asked the assistant to rephrase the previous response, which was a detailed outline for a blog post, into a limerick. The assistant successfully did so, maintaining the essence of the original response in a limerick format. The assistant also offered to further customize the limerick by filling in the bracketed parts with specific model names, showing a willingness to provide additional detail if needed. However, the limerick does not fully capture the depth and detail of the original response, which is understandable given the constraints of the limerick format.

Rating: [[8]], "score": 8, "turn": 2, "tstamp": 1722737024.0327556

Judgment for gemma-2-9b-it-dpo-eva

The assistant's response is creative and relevant to the user's request. The assistant successfully rephrased the previous response, which was a detailed outline for a blog post comparing two smartphone models, into a limerick. The limerick is playful and engaging, and it maintains the essence of the original response, which is to compare the two phones and help the reader make an informed decision. The assistant also offers to create another limerick if the user wants, showing a willingness to continue the interaction.

Rating: [[9]], "score": 9, "turn": 2, "tstamp": 1722846542.9437995

Table 17: (Continued) comparison of model generations on examples from MT-Bench.

1st-turn prompt: Each problem consists of three statements. Based on the first two statements, the third statement may be true, false, or uncertain.\n1. Oranges cost more than apples.\n2. Oranges cost less than bananas.\n3. Bananas cost more than apples and bananas cost more than orange.\nIf the first two statements are true, then the third statement is?	
Answer from gemma-2-9b-it-dpo Here's how to break down the logic:\n\n* **Statement 1:** Oranges > Apples (Oranges cost more than apples)\n* **Statement 2:** Oranges < Bananas (Oranges cost less than bananas)\n\nThis means the price order is: Bananas > Oranges > Apples\n\n* **Statement 3:** Bananas > Apples AND Bananas > Oranges\n\nStatement 3 is **partially true**.\n\n* The part "Bananas > Apples" is true based on our price order.\n* The part "Bananas > Oranges" is also true based on our price order.\n\nLet me know if you'd like to try another one!	Answer from gemma-2-9b-it-dpo-eva Here's how to break down the logic:\n\n* **Statement 1:** Oranges > Apples (Oranges cost more than apples)\n* **Statement 2:** Oranges < Bananas (Oranges cost less than bananas)\n\nThese statements tell us that bananas are the most expensive, then oranges, and apples are the least expensive.\n\n* **Statement 3:** Bananas > Apples AND Bananas > Oranges\n\nSince bananas are indeed more expensive than both apples and oranges, statement 3 is **true**.\n\nLet me know if you'd like to try another one!
2nd-turn prompt: If the third statement is true. Is the first statement true, false, or uncertain? Please explain.	
Answer from gemma-2-9b-it-dpo If the third statement is true, the first statement is **false**.\n\nHere's why:\n\n* **Statement 3:** States that bananas cost more than both apples AND oranges.\n\nThis means the price order is: Bananas > Oranges > Apples.\n\n* **Statement 1:** States that oranges cost more than apples.\n\nIf bananas are the most expensive, and oranges are second, then oranges cannot be more expensive than apples.\n\nLet me know if you have any other logic puzzles!	Answer from gemma-2-9b-it-dpo-eva If the third statement is true, then the first statement is **uncertain**.\n\nHere's why:\n\n* **Statement 3:** Bananas > Apples AND Bananas > Oranges\n\nThis tells us bananas are the most expensive, but it doesn't explicitly state the relative prices of apples and oranges.\n\n* **Statement 1:** Oranges > Apples\n\nThis statement claims oranges are more expensive than apples.\n\nStatement 3 doesn't contradict statement 1, but it also doesn't confirm it. It's possible that oranges *are* more expensive than apples, but statement 3 alone doesn't give us enough information to be sure.
Judgment (by gpt-4)	
Judgment for gemma-2-9b-it-dpo The assistant's response is incorrect. The assistant states that if the third statement is true, the first statement is false. However, the third statement only establishes that bananas cost more than both apples and oranges. It does not provide information about the relative costs of apples and oranges. Therefore, the first statement could be true (if oranges cost more than apples), false (if oranges cost less than apples), or uncertain (if oranges and apples cost the same). The assistant's explanation is flawed because it incorrectly assumes that the order of costs must be Bananas > Oranges > Apples, when in fact the order could also be Bananas > Apples = Oranges or Bananas > Apples > Oranges. \n\nCorrected Assistant's Answer: If the third statement is true, then bananas cost more than apples and bananas cost more than oranges. This means that oranges could still cost more than apples, making the first statement true. However, it's also possible that oranges and apples have the same cost, which would make the first statement false. Therefore, based on the third statement alone, the first statement is uncertain.	Judgment for gemma-2-9b-it-dpo-eva The assistant's response is correct and helpful. The assistant explains that the first statement is uncertain if the third statement is true, which aligns with the reference answer. The assistant provides a clear explanation of why this is the case, stating that the third statement doesn't contradict the first statement, but it also doesn't confirm it. Therefore, the assistant's response is accurate and informative. \n\nThe assistant's response: "If the third statement is true, then the first statement is **uncertain**. Here's why: Statement 3: Bananas > Apples AND Bananas > Oranges. This tells us bananas are the most expensive, but it doesn't explicitly state the relative prices of apples and oranges. Statement 1: Oranges > Apples. This statement claims oranges are more expensive than apples. Statement 3 doesn't contradict statement 1, but it also doesn't confirm it. It's possible that oranges *are* more expensive than apples, but statement 3 alone doesn't give us enough information to be sure.
Rating: [[2]], "score": 2, "turn": 2, "tstamp": 1722737017.2808955	Rating: [[10]], "score": 10, "turn": 2, "tstamp": 1722846527.2339694

Table 18: (Continued) comparison of model generations on examples from MT-Bench.

1st-turn prompt: Implement a function to find the median of two sorted arrays of different sizes with O(1) space complexity and O(n) time complexity.	
<p>Answer from gemma-2-9b-it-dpo</p> <pre>python\def find_median_sorted_arrays(nums1, nums2):\n """\n Finds the median of two sorted arrays of different sizes.\n Args:\n nums1: The first sorted array.\n nums2: The second sorted array.\n Returns:\n The median of the two sorted arrays.\n """\n m, n = len(nums1), len(nums2)\n if m > n:\n nums1, nums2, m, n = nums2, nums1, n, m # Ensure m <= n\n imin, imax, half_len = 0, m, (m + n + 1) // 2\n while imin <= imax:\n i = (imin + imax) // 2\n j = half_len - i\n if i < m and nums2[j - 1] > nums1[i]:\n imin = i + 1 # i is too small, increase it\n elif i > 0 and nums1[i - 1] > nums2[j]:\n imax = i - 1 # i is too big, decrease it\n else:\n # i is perfect\n if i == 0:\n max_left = nums2[j - 1]\n elif j == 0:\n max_left = nums1[i - 1]\n else:\n max_left = max(nums1[i - 1], nums2[j - 1])\n if (m + n) % 2 == 1:\n return max_left\n if i == m:\n min_right = nums2[j]\n elif j == n:\n min_right = nums1[i]\n else:\n min_right = min(nums1[i], nums2[j])\n return (max_left + min_right) / 2.0\n\n# Example usage\nnums1 = [1, 3]\nnums2 = [2]\nmedian = find_median_sorted_arrays(nums1, nums2)\nprint(f"The median of {nums1} and {nums2} is: {median}")\n\n# Explanation:\n# Handle Unequal Lengths:\n# - If 'nums1' is longer than 'nums2', swap them to ensure 'nums1' is always the shorter array. This simplifies the logic.\n# - Binary Search:\n# - The core idea is to use binary search on the shorter array ('nums1').\n# - 'imin' and 'imax' define the search range for the partition point 'i' in 'nums1'. 'half_len' calculates the desired total number of elements on the left side of the partition (to find the median).\n# - Partitioning:\n# - In each iteration, 'i' divides 'nums1' into two parts: 'nums1[0:i]' and 'nums1[i:m]'. 'j' is calculated to divide 'nums2' so that the total number of elements on the left side is 'half_len'. # - Adjusting the Partition:\n# - We compare elements at the boundaries of the partitions to see if 'i' is in the correct position:\n# - If 'nums2[j - 1] > nums1[i]', 'i' is too small, so we move 'imin' to 'i + 1'. # - If 'nums1[i - 1] > nums2[j]', 'i' is too large, so we move 'imax' to 'i - 1'. # - Finding the Median:\n# - Once 'i' is in the correct position, we find:\n# - 'max_left': The maximum element in the left partitions of both arrays.\n# - 'min_right': The minimum element in the right partitions of both arrays. # - If the total length is odd, 'max_left' is the median. # - If the total length is even, the median is the average of 'max_left' and 'min_right'. # Time Complexity: O(log(min(m, n))) because we perform binary search on the shorter array.\n# Space Complexity: O(1) as we only use a constant amount of extra space for variables.</pre>	<p>Answer from gemma-2-9b-it-dpo-eva</p> <pre>python\def find_median_sorted_arrays(nums1, nums2):\n """\n Finds the median of two sorted arrays of different sizes.\n Args:\n nums1: The first sorted array.\n nums2: The second sorted array.\n Returns:\n The median of the two sorted arrays.\n """\n m, n = len(nums1), len(nums2)\n if m > n:\n nums1, nums2, m, n = nums2, nums1, n, m # Ensure m <= n\n imin, imax, half_len = 0, m, (m + n + 1) // 2\n while imin <= imax:\n i = (imin + imax) // 2\n j = half_len - i\n if i < m and nums2[j - 1] > nums1[i]:\n imin = i + 1 # i is too small, increase it\n elif i > 0 and nums1[i - 1] > nums2[j]:\n imax = i - 1 # i is too big, decrease it\n else:\n # i is perfect\n if i == 0:\n max_left = nums2[j - 1]\n elif j == 0:\n max_left = nums1[i - 1]\n else:\n max_left = max(nums1[i - 1], nums2[j - 1])\n if (m + n) % 2 == 1:\n return max_left\n if i == m:\n min_right = nums2[j]\n elif j == n:\n min_right = nums1[i]\n else:\n min_right = min(nums1[i], nums2[j])\n return (max_left + min_right) / 2.0\n\n# Example usage\nnums1 = [1, 3]\nnums2 = [2]\nmedian = find_median_sorted_arrays(nums1, nums2)\nprint(f"The median of {nums1} and {nums2} is: {median}")\n\n# Explanation:\n# Handle Unequal Lengths:\n# - If 'nums1' is longer than 'nums2', swap them to ensure 'nums1' is always the shorter array. This simplifies the logic.\n# - Binary Search:\n# - The core idea is to use binary search on the shorter array ('nums1').\n# - 'imin' and 'imax' define the search range for the partition point 'i' in 'nums1'. 'half_len' calculates the desired total number of elements on the left side of the partition (to find the median).\n# - Partitioning:\n# - In each iteration, 'i' divides 'nums1', and 'j' divides 'nums2' such that the total number of elements on the left side is 'half_len'. # - Adjusting the Search Range:\n# - If 'nums2[j - 1] > nums1[i]', it means 'i' is too small, so we need to move the partition point in 'nums1' to the right ('imin = i + 1'). # - If 'nums1[i - 1] > nums2[j]', 'i' is too large, so we move it to the left ('imax = i - 1'). # - Finding the Median:\n# - When the correct partition is found ('i' is in the right position), we find:\n# - 'max_left': The maximum element on the left side of the partition.\n# - 'min_right': The minimum element on the right side of the partition. # - If the total number of elements is odd, 'max_left' is the median. # - If even, the median is the average of 'max_left' and 'min_right'. # Time Complexity: O(log(min(m, n))) because we are performing binary search on the shorter array.\n# Space Complexity: O(1) as we are only using a constant amount of extra space for variables.</pre>
Judgment (by gpt-4)	
<p>Judgment for gemma-2-9b-it-dpo</p> <p>The assistant's answer is correct and provides a detailed explanation of the code. The assistant correctly states that the time complexity is $O(\log(\min(m, n)))$ and the space complexity is $O(1)$, which aligns with the reference answer. The assistant also provides an example usage of the function, which is helpful for understanding how to use it. The assistant's code is a different implementation than the reference answer, but it achieves the same result and meets the same complexity requirements. However, the assistant's answer does not address the user's original question about achieving $O(n)$ time complexity. The assistant should have clarified that it's not possible to find the median of two sorted arrays of different sizes with $O(1)$ space complexity and $O(n)$ time complexity, as stated in the reference answer.</p> <p>Rating: [[8]], "score": 8, "turn": 1, "timestamp": 1722737514.2011044</p>	<p>Judgment for gemma-2-9b-it-dpo-eva</p> <p>The assistant's answer is correct and provides a detailed explanation of the code. The assistant correctly states that the time complexity is $O(\log(\min(m, n)))$ and the space complexity is $O(1)$, which aligns with the reference answer. The assistant also provides a step-by-step explanation of the code, which is very helpful for understanding the logic behind the solution. The assistant's code is also correct and will correctly find the median of two sorted arrays of different sizes. Therefore, there are no corrections needed for the assistant's response.</p> <p>Rating: [[10]], "score": 10, "turn": 1, "timestamp": 1722846533.772981</p>

Table 19: (Continued) comparison of model generations on examples from MT-Bench.

1st-turn prompt: You are given two sorted lists of size m and n. Implement a function to find the kth smallest element in the union of the two lists with linear complexity.	
<p>Answer from gemma-2-9b-it-dpo</p> <pre> '''python def find_kth_smallest(list1, list2, k): """ Finds the kth smallest element in the union of two sorted lists. Args: list1: The first sorted list. list2: The second sorted list. k: The desired kth smallest element. Returns: The kth smallest element in the union of the two lists. """ m, n = len(list1), len(list2) i, j = 0, 0 min_heap = [] # Build a min-heap # with the first elements of both lists for x in range(min(m, n)): heapq.heappush(min_heap, (list1[x], x, 0)) heapq.heappush(min_heap, (list2[x], x, 1)) # Extract k smallest elements from the heap for _ in range(k - 1): _, _, _ = heapq.heappop(min_heap) # The top element of the heap is the kth smallest return heapq.heappop(min_heap)[0] # Example usage: nlist1 = [2, 5, 8, 12] nlist2 = [1, 3, 7, 9, 10] nk = 5 kth_smallest = find_kth_smallest(list1, list2, k) print(f"The {k}th smallest element is: {kth_smallest}") # Explanation: # Initialization: # - 'm' and 'n' store the lengths # of the input lists. # - 'i' and 'j' are pointers # to track the current position in each list. # - 'min_heap' is a min-heap used to efficiently store # and retrieve the smallest elements encountered so # far. # Building the Min-Heap: # - The code # iterates through the first 'min(m, n)' elements of # both lists. # - For each element, a tuple '(value, # list_index, position_in_list)' is pushed onto the # 'min_heap'. This tuple helps us keep track of # the element's value, the list it belongs to, and # its original position. # Extracting k-1 # Smallest Elements: # - The 'for' loop runs 'k - # 1' times, effectively extracting the 'k-1' smallest # elements from the 'min_heap'. # Finding the kth # Smallest: # - After the loop, the top element of # the 'min_heap' contains the 'k'th smallest element. # - 'heapq.heappop(min_heap)' removes and returns this # element. # Time Complexity: # Building the # min-heap: O(m + n) # Extracting k-1 elements: O(k * # log(k)) # Overall: O(m + n + k * log(k)), which # is approximately O(m + n) since 'k' is usually much # smaller than 'm + n'. Let me know if you have any other questions! </pre>	<p>Answer from gemma-2-9b-it-dpo-eva</p> <pre> '''python def find_kth_smallest(list1, list2, k): """ Finds the kth smallest element in the union of two sorted lists. Args: list1: The first sorted list. list2: The second sorted list. k: The desired rank of the smallest element. Returns: The kth smallest element in the union of the lists. """ i = 0 # Index for list1 j = 0 # Index for list2 merged = [] # Store the merged elements while i < len(list1) and j < len(list2): if list1[i] <= list2[j]: merged.append(list1[i]) i += 1 else: merged.append(list2[j]) j += 1 # Add any remaining elements from list1 while i < len(list1): merged.append(list1[i]) i += 1 # Add any remaining elements from list2 while j < len(list2): merged.append(list2[j]) j += 1 return merged[k - 1] # Return the kth # element (index k-1) # Example usage: nlist1 = [2, 5, 8, 12] nlist2 = [1, 3, 7, 9, 10] nk = 5 kth_smallest = find_kth_smallest(list1, list2, k) print(f"The {k}th smallest element is: {kth_smallest}") # Explanation: # Initialization: # - 'i' and 'j' are index pointers # for 'list1' and 'list2' respectively, starting at # 0. # - 'merged' is an empty list to store the merged # sorted elements. # Building the Merged List: # - The 'while' # loop continues as long as both 'i' and 'j' are within # the bounds of their respective lists. # In each # iteration, it compares the elements at 'list1[i]' # and 'list2[j]'. # The smaller element is appended # to 'merged', and the corresponding index ('i' or # 'j') is incremented. # Adding Remaining # Elements: # - After one list is exhausted, the # remaining elements from the other list are directly # appended to 'merged'. # Returning the kth # Element: # - Finally, 'merged[k - 1]' is returned, # which represents the kth smallest element in the union # (remember that list indices start from 0). # Linear # Complexity: # The algorithm iterates through each # element in both lists at most once during the merging # process. # The time complexity is therefore O(m + n), # which is linear in the total number of elements (m + # n), making it efficient for large lists. </pre>
Judgment (by gpt-4)	
<p>Judgment for gemma-2-9b-it-dpo</p> <p>The assistant's answer is incorrect. The user asked for a solution with linear complexity, but the assistant provided a solution with a time complexity of $O(m + n + k \cdot \log(k))$, which is not linear. The assistant's solution uses a min-heap, which is not necessary and adds unnecessary complexity to the solution.</p> <p>Rating: [[2]], "score": 2, "turn": 1, "timestamp": 1722737030.6411152</p>	<p>Judgment for gemma-2-9b-it-dpo-eva</p> <p>The assistant's answer is correct and helpful. It provides a Python function that implements the two-pointer approach to find the kth smallest element in the union of two sorted lists. The assistant's function merges the two lists into a new list and then returns the kth element from the merged list. The assistant also provides a detailed explanation of how the function works and confirms that the time complexity is linear, which is what the user asked for. However, the assistant's function uses extra space to store the merged list, which is not necessary and not as efficient as the reference.</p> <p>Rating: [[8]], "score": 8, "turn": 1, "timestamp": 1722846543.867601</p>

Table 20: (Continued) comparison of model generations on examples from MT-Bench.

2nd-turn prompt: Does there exist an algorithm with better time complexity? If so, implement it.	
<p>Answer from gemma-2-9b-it-dpo</p> <p>You are absolutely right! There's a more efficient algorithm with a time complexity of $O(m + n)$ without using a heap. Here's the implementation:</p> <pre>def find_kth_smallest_optimized(list1, list2, k): """Finds the kth smallest element in the union of two sorted lists with O(m + n) time complexity. Args: list1: The first sorted list. list2: The second sorted list. k: The desired kth smallest element. Returns: The kth smallest element in the union of the two lists. """ m, n = len(list1), len(list2) i, j = 0, 0 result = [] # Merge the lists while keeping track of the kth smallest while len(result) < k: if i < m and j < n: if list1[i] <= list2[j]: result.append(list1[i]) i += 1 else: result.append(list2[j]) j += 1 elif i < m: result.append(list1[i]) i += 1 else: result.append(list2[j]) j += 1 return result[k - 1] # Example usage: list1 = [2, 5, 8, 12] list2 = [1, 3, 7, 9, 10] k = 5 kth_smallest = find_kth_smallest_optimized(list1, list2, k) print(f"The {k}th smallest element is: {kth_smallest}") # Explanation: # Initialization: # - 'm' and 'n' store the lengths of the lists. # - 'i' and 'j' are pointers for 'list1' and 'list2', respectively. # - 'result' is a list to store the merged and sorted elements. # Merging and Tracking: # - The 'while' loop continues until 'k' elements are in the 'result' list. # - In each iteration, it compares the current elements from 'list1' and 'list2'. # - The smaller element is appended to 'result', and the corresponding pointer ('i' or 'j') is incremented. # - If one list is exhausted, the remaining elements from the other list are appended to 'result'. # Returning the kth Smallest: # - Finally, 'result[k - 1]' contains the 'k'th smallest element. # Time Complexity: # - The algorithm iterates through both lists once, resulting in a time complexity of $O(m + n)$. # Let me know if you have any more questions! </pre>	<p>Answer from gemma-2-9b-it-dpo-eva</p> <p>You are right to ask! While the previous algorithm has linear time complexity, we can achieve an even better solution with $O(\log(\min(m, n)))$ time complexity using a slightly more sophisticated approach. The key idea is to leverage the sorted nature of the lists and use a binary search strategy. Here's the implementation:</p> <pre>def find_kth_smallest_optimized(list1, list2, k): """Finds the kth smallest element in the union of two sorted lists with O(log(min(m, n))) time complexity. Args: list1: The first sorted list. list2: The second sorted list. k: The desired rank of the smallest element. Returns: The kth smallest element in the union of the lists. """ m, n = len(list1), len(list2) if m > n: list1, list2, m, n = list2, list1, n, m # Ensure list1 is the shorter one left, right = 0, m while left < right: partitionX = (left + right) // 2 partitionY = k - partitionX maxLeftX = list1[partitionX - 1] if partitionX > 0 else float('-inf') minRightX = list1[partitionX] if partitionX < m else float('inf') maxLeftY = list2[partitionY - 1] if partitionY > 0 else float('-inf') minRightY = list2[partitionY] if partitionY < n else float('inf') if maxLeftX <= minRightY and maxLeftY <= minRightX: if partitionX == 0: return list2[partitionY - 1] elif partitionY == 0: return list1[partitionX - 1] else: return max(list1[partitionX - 1], list2[partitionY - 1]) elif maxLeftX > minRightY: right = partitionX - 1 # Too many elements on the right side of list1 else: left = partitionX + 1 # Too many elements on the right side of list2 return list1[n] # Explanation: # Shorten Lists: # If 'list1' is longer than 'list2', swap them to ensure 'list1' is always the shorter one. This simplifies the logic. # Binary Search: # - 'left' and 'right' pointers define the search space within 'list1'. # - 'partitionX' is the middle point in 'list1', and 'partitionY' is calculated to divide the remaining elements in 'list2' such that 'partitionX + partitionY = k'. # - 'maxLeftX', 'minRightX', 'maxLeftY', and 'minRightY' represent the largest element to the left and smallest element to the right of the partitions in both lists. # Comparison and Adjustment: # - If the 'maxLeftX' is less than or equal to 'minRightY' and 'maxLeftY' is less than or equal to 'minRightX', it means the kth smallest element lies within the current partitions. We return the larger of 'maxLeftX' and 'maxLeftY'. # - If 'maxLeftX' is greater than 'minRightY', it indicates that we need to search in the left subarray of 'list1' (i.e., decrease 'right'). # - Otherwise, we search in the right subarray of 'list1' (i.e., increase 'left'). # Termination: # The binary search continues until 'left' crosses 'right', indicating the correct partition has been found. # Time Complexity: # The binary search divides the search space in half at each step. Therefore, the time complexity is $O(\log(\min(m, n)))$, which is significantly faster than linear time for large lists where one list is much smaller than the other. </pre>
Judgment (by gpt-4)	
<p>Judgment for gemma-2-9b-it-dpo</p> <p>The assistant's first response to the user's question is incorrect. The user asked for a function to find the kth smallest element in the union of two sorted lists with linear complexity. The assistant provided a function that uses a min-heap, which has a time complexity of $O(m + n + k \cdot \log(k))$. This is not linear complexity, as the user requested. The assistant's second response to the user's question is also incorrect. The user asked if there exists an algorithm with better time complexity than linear. The assistant provided a function that has a time complexity of $O(m + n)$, which is linear, not better than linear. The assistant should have provided a function that uses a binary search approach, which has a time complexity of $O(\log(m) + \log(n))$, as the reference answer correctly does.</p> <p>Rating: $[[2]]$, "score": 2, "turn": 2, "timestamp": 1722737031.5033472</p>	<p>Judgment for gemma-2-9b-it-dpo-eva</p> <p>The assistant's response is correct and helpful. The assistant provided a Python function that uses a binary search approach to find the kth smallest element in the union of two sorted lists. The assistant also provided a detailed explanation of how the function works, including the time complexity of the function. The assistant's answer matches the reference answer in terms of the algorithm used and the explanation provided. The assistant also correctly identified that the binary search approach has a better time complexity than the linear approach. However, the assistant's code has a minor issue. The assistant's code does not handle the case when 'k' is greater than the sum of the lengths of the two lists. In such a case, the code will raise an 'IndexError'. This can be fixed by adding a check at the beginning of the function to return 'None' if 'k' is greater than the sum of the lengths of the two lists.</p> <p>Rating: $[[9]]$, "score": 9, "turn": 2, "timestamp": 1722846556.6828268</p>

Table 21: (Continued) comparison of model generations on examples from MT-Bench.

REBUTTAL TO REVIEWER AC2P

Summary. We sincerely thank the reviewer for the appreciation of the **eva** method and the constructive feedback. In the following, we have:

- added experiments on implementing **different evolving methods** and discussed relevant strengths and weaknesses in § D.1;
- added **visualization on the learning curriculum** in § E;
- provided detailed discussion on **scaling up eva** with million-level data on larger-scale seed sets and/or inference-time scaling for synthesizing prompts.

Q1 (Choice of the Evolving Method): Could you explain more about the particular choice of evolution algorithm used in your implementation of eva and different potential strengths and weaknesses related to this choice?

TL;DR: We use EvolInstruct (Xu et al., 2023a) as it is among the most easy-to-implement methods. We added new experiments w/ other methods, including SelfInstruct (Wang et al., 2022), EvolQuality and EvolComplexity (Liu et al., 2023b), and show that **eva** remains to be effective in § D.1.

Answer: As an addition to Table 1, we have experimented with three different `evolve()` methods:

- **SelfInstruct** (Wang et al., 2022): Given seed prompts, variations are created based on criteria such as verb diversity and style blending (mixing interrogative and imperative styles). Unlike EvolInstruct (Xu et al., 2023a), which generates prompt variations sequentially, this approach generates independently. We follow the one-shot implementation in `self_instruct.py` of `distilabel==1.4.1` and modified the instruction on conciseness so that newly generated prompts have similar lengths compared to the seed prompts.
- **EvolQuality** and **EvolComplexity** (Liu et al., 2023b): The two methods use the same evolutionary approach (*i.e.*, sequentially generating), but with slightly different meta-instructions for prompt generation, where EvolQuality asks to improve the quality (*i.e.*, helpfulness, relevance, etc) of the seed prompt and EvolComplexity asks to improve the complexity (*i.e.*, increased reasoning steps, etc) of the seed prompt. We follow the implementation in `evol_quality/utils.py` and `evol_complexity/utils.py` of `distilabel==1.4.1`.

Model Family (→)	GEMMA-2-9B-IT	
Benchmark (→)	Arena-Hard	
Method (↓) / Metric (→)	WR (%)	avg. len
θ_0 : SFT	41.3	544
$\theta_{0 \rightarrow 1}$: DPO	51.6	651
$\theta_{1 \rightarrow \bar{1}}$: + eva (<code>evolve()</code> = EvolInstruct)	60.1	733
$\theta_{1 \rightarrow \bar{1}}$: + eva (<code>evolve()</code> = EvolQuality)	58.7	721
$\theta_{1 \rightarrow \bar{1}}$: + eva (<code>evolve()</code> = EvolComplexity)	60.6	749
$\theta_{1 \rightarrow \bar{1}}$: + eva (<code>evolve()</code> = SelfInstruct)	57.2	725

Table 22: Results of using different evolving methods.

eva is effective under different evolving methods. As shown in Table 10, our method brings strong performance gain without training with additional human prompts. Among the experimented methods, we find EvolComplexity shows better results.

We believe the main strength of such method is its **simplicity**. Viewing the evolving process as $\mathbf{x}' \leftarrow p_{\theta}(\cdot \mid \mathbf{x}, \text{meta_prompt})$, one can easily tune the meta prompt in natural language for improved performance. However, such simplicity comes at a price: (i) the main weakness is that the default method does not take **environmental feedback** into account (*e.g.*, rewards received, verbal critique on responses, etc) and relies on the pre-defined meta prompt, thus the evolving may be less directional; we encourage practitioners to consider incorporating more richer feedback during evolving (one way

to formulate this is by generative optimization (Yuksekgonul et al., 2024; Cheng et al., 2024; Nie et al., 2024); (ii) another weakness is that existing method is single-shot (*i.e.*, we evolve based on a single \mathbf{x} each time), thus the **diversity** of the generation may be limited – we anticipate future works improving this with multi-shot evolving by graph-based sampling. In this regard, the evolving process can be viewed as $\{\mathbf{x}'\}_{i=1}^N \leftarrow p_{\theta}(\cdot | \{\mathbf{x}\}_{i=1}^M, \text{meta-prompt}, \text{env-feedback})$.

Q2 & Q3 (Empirical Evidence on Learning Progress and Curriculum): Do you see empirical evidence of your intuition about learning progress discussed in section 3.4? It seems like some of these claims are directly testable. Could you visualize the curriculum learned in your experiments with *eva*? It would be very nice to get an intuition for why performance improves and what the heuristic prioritizes over time.

Answer: We thank the reviewer for the constructive suggestions on empirically validating the intuition. We have revised the manuscript with additional visualization on potential curriculum learned in § E. In general, we observe the creator prioritizes learning in math and coding, which brings gradual improvement on benchmark performance on relevant categories over iterations. We have attached the bar plot and radar figure here for the reviewer’s reference:

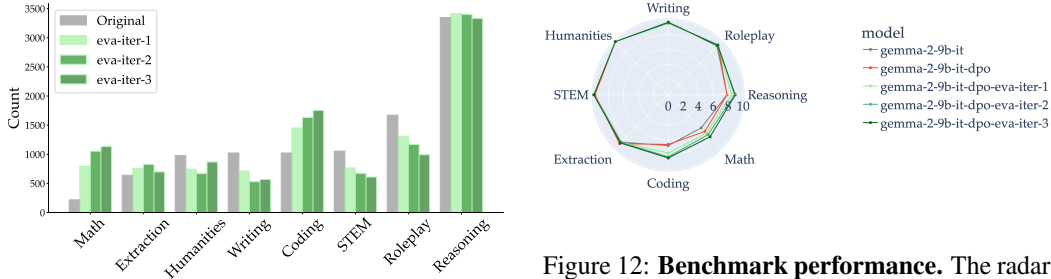


Figure 11: **Training distributions.** The prompt distribution of Table 11 for evolved prompts by zero-shot classification. *eva* creates a curriculum that prioritizes math / coding prompts.

Figure 12: **Benchmark performance.** The radar figure for ratings on MT-Bench (Zheng et al., 2023), where each category contains ten problems. *eva* prioritizes and gradually improves on coding, math and reasoning over iterations, implicitly reflecting a learned curriculum.

Q4 (Scaling): When discussing future directions, the authors write further scaling up w/ million-level data. Can you clarify what this means? Seems like some important context is missing?

TL;DR: We consider (i) applying *eva* when the seed set contain million-level or more prompts; or (ii) using *eva* to robustly generate million-level or more data for self-training.

Answer: (i) The current paper uses the UltraFeedback (Cui et al., 2023) as the seed prompt set, which is a ten-thousands level dataset; in training practically useful large language models (Brown et al., 2020; Team et al., 2024a; Singh et al., 2023), the seed prompt sets are usually much more larger than such a level. We believe it is an interesting direction to explore the data scaling properties of *eva* on larger seed prompt sets, in combination with our on-policy variants. (ii) On the other hand, when the seed prompt set contains only limited data (this issue is particularly concerning in hard reasoning tasks like math (Yang et al., 2024)), can we still follow the data generating curriculum and synthesize million-level prompts/problems to help training, and how to robustly verify the generated prompts/problems? There is a recent trend in inference-time scaling (Snell et al., 2024), however these works only consider scaling in the \mathcal{Y} space, not the \mathcal{X} or the joint $(\mathcal{X}, \mathcal{Y})$ space. We believe this is also a new direction worth investigating.

We thank the reviewer once again for spending time on our submission and providing constructive feedback that helps improve the *eva* method. Please let us know if there is any other concerns or questions, and we are more than grateful to have the opportunity to learn from and discuss with you.

REBUTTAL TO REVIEWER ZXTK

Summary. We sincerely thank the reviewer for all the constructive feedback helping improving the **eva** method. In response, we have provided:

- experiments on more iterations in § D.2.
- extended discussions on the regret objective and the proxy in § G.
- evidence on distinction of advantage-based metrics and variance-based ones in § F.

We believe the additional discussions and rebuttals provided have sufficiently addressed the weaknesses and questions raised by the reviewer. Please let us know if there is any additional revision needed and we would be grateful to incorporate.

W1 (Running for More Iterations): The number of iterations in the main results is 2, with only one EVA step in each experiment, which is a little different from what the demonstration in Figure 3 shows. If the **eva** step is performed multiple times, would the results be better or worse? What is performance like when you access all data in UltraFeedback?

TL;DR: We added experimental result on running more iterations with more data, and **eva** remains to be effective. We have added § D.2 in the manuscript to incorporate the reviewer’s suggestion.

Rebuttal: As an addition to § 4.2.4, we have experimented with the following settings:

- 10K prompts per iteration with 3 iterations.
- 20K prompts per iteration with 3 iterations (*i.e.*, all seed prompts are used).
- 60K prompts per iteration with 2 iterations (*i.e.*, all seed prompts are used).

Due to time constraints, we did not perform an extensive hyper-parameter search; however, we believe the results presented below sufficiently demonstrate the performance gains achieved by **eva**.

Model Family (\rightarrow)	GEMMA-2-9B-IT	
Benchmark (\rightarrow)	Arena-Hard	
Method (\downarrow) / Metric (\rightarrow)	WR (%)	avg. len
θ_0 : SFT	41.3	544
$\theta_{0 \rightarrow 1}$: DPO (10k)	51.6	651
$\theta_{1 \rightarrow 2}$: DPO (10k)	59.8	718
$\theta_{2 \rightarrow 3}$: DPO (10k)	61.2	802
$\theta_{1 \rightarrow \tilde{1}}$: + eva (10k)	60.1	733
$\theta_{\tilde{1} \rightarrow 2}$: + eva (10k)	62.0	787
$\theta_{\tilde{2} \rightarrow 3}$: + eva (10k)	62.2	774

Table 23: Results of using 10k prompts per iteration.

Model Family (\rightarrow)	GEMMA-2-9B-IT	
Benchmark (\rightarrow)	Arena-Hard	
Method (\downarrow) / Metric (\rightarrow)	WR (%)	avg. len
θ_0 : SFT	41.3	544
$\theta_{0 \rightarrow 1}$: DPO (20k)	53.2	625
$\theta_{1 \rightarrow 2}$: DPO (20k)	47.0	601
$\theta_{2 \rightarrow 3}$: DPO (20k)	46.8	564
$\theta_{1 \rightarrow \tilde{1}}$: + eva (20k)	59.5	826
$\theta_{\tilde{1} \rightarrow 2}$: + eva (20k)	60.0	817
$\theta_{\tilde{2} \rightarrow 3}$: + eva (20k)	61.4	791

Table 24: Results of using 20k prompts per iteration.

Model Family (\rightarrow)	GEMMA-2-9B-IT	
Benchmark (\rightarrow)	Arena-Hard	
Method (\downarrow) / Metric (\rightarrow)	WR (%)	avg. len
θ_0 : SFT	41.3	544
$\theta_{0 \rightarrow 1}$: DPO (60k)	58.9	717
$\theta_{1 \rightarrow \bar{1}}$: + eva (60k)	59.6	725
$\theta_{\bar{1} \rightarrow \bar{1}'}:$ + eva (60k)	61.9	792

Table 25: Results of using 60k prompts per iteration.

eva can bring robust gains with multiple iterations. As shown in Table 11, 12, and 13 below, our method presents persistent performance gain over iterations, and concretely surpasses the performance by default DPO training with true human prompts.

However, there exists diminishing marginal gain in iterative off-policy training. We ground **eva** in the iterative (off-policy) RLHF paradigm due to its efficiency and ease of integration. However, such paradigms inherently face diminishing returns, where performance gains decrease with successive iterations and may even turn negative, potentially due to distributional drift, exploitation of suboptimal feedback, or network plasticity in continuing training (Xiong et al., 2024; Wu et al., 2024; Setlur et al., 2024; Yuan et al., 2024; Nikishin et al., 2022). While the generative data schedule in **eva** mitigates these challenges and extends beyond default training with human prompts (see also §4.2.4), the gains still weaken over iterations. We attribute this to two key factors: (i) the **off-policy signal decay**, where learning signals lose efficacy as examples increase during the offline update; and (ii) the **solver reasoning bottleneck**, where evolving prompts become increasingly challenging, and explicit adaptation or guidance for further improvement may be required.

Thus, we encourage future work to build on **eva** by: (i) exploring its integration with **on-policy RLHF** (e.g., instead of evolving prompts in iterations, one may evolve prompts in batches), and (ii) **enhancing solver capabilities**, such as sampling more responses during inference (if computational resources permit) or leveraging meta-instructions to guide deeper reasoning.

Bonus experiments on adding rewriter in the solver step. This is beyond the current paper, and we present the basic idea here for practitioners to build upon. The motivation comes from the hypotheses derived from § D.2: as the prompts gets harder by evolving, there may be greater demands on the solver’s capabilities *compared to earlier iterations*. As such, the solver may not be naively treated the same. One may address this by either inference-time scaling on responses or introducing meta-instructions to explicitly enhance the solver’s reasoning.

We hereby design a proof-of-concept experiment *w.r.t* the latter by adding **rewriter** in **eva**’s solver step. Previously, as in Algo. 1 and § 3.3.2, for each prompt \mathbf{x} , we generate multiple responses, and choose the best as \mathbf{y}_+ and the worst as \mathbf{y}_- for preference optimization. Now, we add one more rewriting step that attempts to enhance \mathbf{y}_+ to be \mathbf{y}'_+ , by applying a rewriting instruction (Liu et al., 2023b) that asks the solver to alter \mathbf{y}_+ with improved helpfulness, relevance, reasoning depths, creativity and details while keeping the similar length. We then train with $(\mathbf{x}, \mathbf{y}'_+, \mathbf{y}_-)$ for preference optimization. Table 14 shows that adding the rewriter yields concrete performance gains over the default training method, while keeping the training budget and slightly increasing inference cost.

Model Family (\rightarrow)	GEMMA-2-9B-IT	
Benchmark (\rightarrow)	Arena-Hard	
Method (\downarrow) / Metric (\rightarrow)	WR (%)	avg. len
θ_0 : SFT	41.3	544
$\theta_{0 \rightarrow 1}$: DPO	51.6	651
$\theta_{1 \rightarrow \bar{1}}$: + eva	60.1	733
$\theta_{1 \rightarrow \bar{1}}$: + eva with rewriter	61.9	741

Table 26: Results of adding **rewriter** in the **solver** step.

W2 (Connection in Minimax Regret and The Algorithm): The connection between the minimax regret objective and the algorithm is a somehow vague. The regret concerns the performance gap with the optimal policy. It's not reflected by the informativeness proxy.

TL;DR: The informativeness proxy is an approximation to the regret leveraging the stochastic policy of the language model. We have added § G to address the reviewer's concern.

Rebuttal: On a high-level, we first use the alternating optimization by minimax game to replace the joint optimization in Eq. 7; secondly, we use regret as the objective for the game, where the creator seeks to maximize and the solver seeks to minimize. Specifically, for the creator, the regret is approximated by the informativeness proxy through sampling from the stochastic policy and measuring the gap between the maximal and the minimal reward received. Please see § G for detailed explanation. (Note: without access to the optimal policy, we *need* approximate the regret in practice; classical works have trained two players (Dennis et al., 2020), while our approach is more simple and efficient, avoids training instability and empirically brings strong performance gain).

Q1 (Advantage v.s. Variance): The informativeness proxy seems to be similar to the variance of the rewards because they all concern the diversity of the generated responses. However, in lines 393-395, the results shows using variance leads to poor performance. How to interpret this?

TL;DR: To explain, (i) variance does not directly capture the **learning potential** in preference optimization, while advantage-based informativeness proxy is better aligned to the learning objective; (iii) we empirically show that variance and advantage are only weakly correlated thus will likely result in different sampling. We have added § F to incorporate the reviewer's suggestion.

Rebuttal:

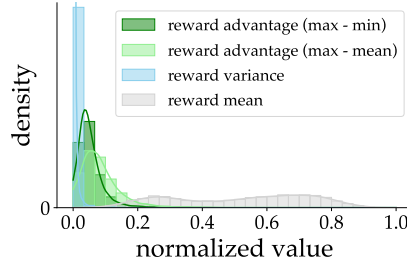


Figure 13: The probability density distributions of informativeness metrics in Table 3 – they show different patterns.

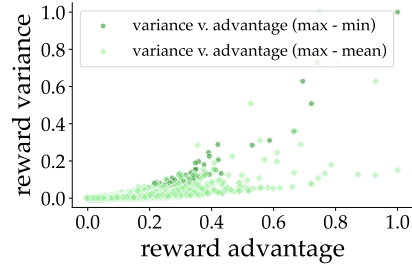


Figure 14: The correlation plot for reward advantage (ours) and reward variance – they are only *weakly* correlated.

In **eva**, we assign each prompt an informativeness value, which the creator will use as the weight to sample from the seed prompts for prompt synthesis. In § 4.2.1, we have shown that traditional methods like reward mean and reward variance are less effective as our advantage-based informativeness proxy. The intuition is simple: advantage/regret-based proxy aligns better with the preference optimization objective. We here further illustrate that they are statistically different from other choices:

- Figure 8: The distribution of informativeness values shows that reward variance is heavily concentrated at lower values, reward mean is more uniformly scattered, and reward advantage achieves a better balance, providing a broader yet also focused sampling range.
- Figure 9: The *weak correlation* between reward variance and reward advantage shows that variance *cannot* serve as a substitute for advantage as a proxy for informativeness.

We have discussed the Contrastive Curriculum Hypothesis in § 3.4 to support the use of reward advantage. Furthermore, assuming iterative preference optimization can ultimately converge to the *more optimal* responses, neither reward mean nor reward variance directly captures the learning potential of such more optimal response. One may easily construct cases with identical variance yet differ much in reward range. Reward variance fails to distinguish such scenarios. By contrast, reward advantage inherently captures the relative improvement towards the more optimal response, and is sensitive to differences in reward range; specifically, *max - min* mimics a worst-case guarantee, while *max - mean* emphasizes the potential of the more optimal response from a Bayesian perspective.

REBUTTAL TO REVIEWER 19KX

Summary. We thank the reviewer for the thoughtful and detailed feedback. In response, we have:

- provided a point-by-point rebuttal addressing each suggested weakness and question.
- revised the manuscript with methodological justifications in § G and new experiments in § E and § D for additional empirical evidence.

We sincerely appreciate the reviewer’s thoughtful suggestions, and note that their perspective may align with a more theory-first approach, akin to the references listed ([1], [2], and [3]), which we highly value and find inspiring. The current **eva** framework, however, takes a complementary **method-first** approach, prioritizing methodological simplicity and empirical performance over rigid theoretical justifications. This design choice is intentional: we aim to offer a **new, simple, easy-to-implement training paradigm** that can be easily adopted, extended, and elaborated upon by the broader community, both in academia and industry.

To achieve this, we have intentionally included many approximations to make the framework practical and easy to use; we consider the main concerns of the reviewer may also come from such approximations made – in a way that this paper is not perfect in theory. We wish to clarify that our primary goal is to prioritize the method itself, similar to prior works like CoT and ReST. The theoretical bits we provide serve to establish a high-level principle that inspires both practical and theoretical exploration, rather than being the central contribution of this work.

We also recognize the broader context in which this discussion takes place. It is slightly unfortunate that a gap exists between modern RL/bandit theory research and the practical algorithms adopted in real-world settings. Many elegant theoretical ideas remain underutilized due to the compromises required to maintain theoretical rigor, while industrial approaches often succeed with brute-force methods that prioritize empirical performance over elegance. With **eva**, we aim to strike a balance between them, offering a conceptual framework that is theoretically inspired and practically impactful.

We hope we have sufficiently addressed the reviewer’s concerns, and we warmly encourage the reviewer to consider the **strong performance gains** with the **simple design** of **eva**, and to evaluate the merit of a work (*cf.*, (Castro, 2021)) *w.r.t.* the practicality and how the community can easily build on top of it (*cf.*, (Hamming, 1986)).

We sincerely thank the reviewer once again for dedicating their valuable time to carefully reviewing our manuscript and for providing constructive feedback to improve **eva**. We warmly welcome any future collaborative discussions and are more than happy to address any follow-up questions and to learn from the reviewer’s insights.

W1 (Proxy Tractability): How is Eq. 10 tractable and being solved? Any heuristic of sampling and approximating should result in sub-optimality which is not clear where its accounted.

W2 (Regret and KL): The optimization is over π in Eq. 9 for solving the minimax regret. However, its not absolutely clear how the KL divergence plays a role here and how it is ensured that the response and prompt distributions are close to reference. Without that, the alignment problem is ill-defined. Please provide concrete justifications in theory and empirical results.

TL;DR: We have added § G to address related concerns. Specifically, (i) we have revised the manuscript *w.r.t.* KL-regularized regret and discussed our approximation made in § G.2; (ii) we sample multiple times from the stochastic policy to tractably estimate the informativeness proxy, which we explained in detail at § G.2.1; (iii) the **solver maintains the KL regularization** during training, thus the alignment problem at each iteration remains correctly defined; (iv) the creator does not have a tractable reference distribution, and we use a fixed creator and apply meta instructions and buffer sampling to adapt/constrain the prompt generations (as described in § 3.3, § A and § D.1), which is easy-to-implement and empirically effective.

Rebuttal: We thank the reviewer for catching the omission of the KL term in the original writeup on regret. Please see our revised definition and detailed discussion on the approximation that we made in § G, and empirical results in § 4.1 on alignment gains over different algorithms and benchmarks, § E on generated prompt distributions and alignment gains across different categories.

W3 (Understanding the Iterative Algorithm): As described in Algorithm 1, informativeness is evaluated and a prompt subset is created based on current policy estimate and then the policy is updated based on the prompt subset. However, this causes an inter-dependence between the two which leads to nested structure, which is not clearly explained. Specifically, while computing the informativeness score for the prompts, it depends on $\theta^*(x_{t-1})$, i.e., optimal parameter for the previous distribution. Provide clear explanation on the same.

TL;DR: We intend to use an iterative best-response framework to approximate equilibrium in expectation, balancing computational efficiency and practicality. We also added discussions in § I on Stackelberg v.s. Nash equilibrium which may be potentially related to this.

Rebuttal: The iterative updates in **eva**, as described in Algo. 1, are based on a best-response-to-best-response framework. Specifically, the creator updates the prompt distribution based on the solver’s current policy, and the solver then optimizes its policy for the updated prompts, and the process repeats. This sequential structure approximates a Nash equilibrium in expectation over iterations, inspired by works such as Freund and Schapire (1999); Wu et al. (2024), which establish convergence to optimal policies on average through iterative optimization.

We intentionally avoid simultaneous joint optimization as it would significantly increase computational and memory overhead, making it less practical for integration into current RLHF pipelines. The current approach is simple and effective, and leads to concrete empirical performance gain as shown in § E. While this paper emphasizes **practical usability** over formal theoretical guarantees, we look forward to future works on extensions for Open-Ended RLHF (such as adding convergence rates and equilibrium guarantees, deriving first-order solutions, etc). We would greatly appreciate any further suggestions or insights the reviewer may have to improve this direction.

W4 (Understanding Reward Models): While iterating, every new prompt distribution will require generating new response, how is the evaluation coming from which reward model? Is the ground reward available, if not please explain how the preference is obtained and how does it affect suboptimality? Also: **Q3 (RM Availability):** What’s the reward model availability? Is the true reward model available?

TL;DR: We assume a preference oracle provided by an **external, pre-trained reward model**, which is practically used in many real-world LLM training scenarios (Team et al., 2023).

Rebuttal: As discussed in the beginning of the experimental setting in § 4, we assume the availability of a pre-trained, fixed reward model. This approach is practically adopted in industry (Team et al., 2023; 2024a;b) and is also commonly used in academia works (Xu et al., 2023b; Meng et al., 2024; Wu et al., 2024). The reason is more on efficiency concerns. For example, in GEMMA-2 training, the reward model is *an order of magnitude larger* than the policy (Team et al., 2024b); it would thus be impractical or the gain may only be marginal if we update the reward model on-the-fly (as done in many prior works on bi-level RLHF – thanks again for the reviewer’s nice references).

Nevertheless, it is possible to incorporate the online RM training within **eva** – we have shown in § 4.2.3 that **eva** scales with quality of reward models, thus integrating online RM training may further enhance performance and address the potential distribution mismatch problem. We believe this is an interesting direction to pursue, and have listed it in § 6 on adding more players including rewarders in the self-play loop.

W5 (Improvement of Sub-Optimality): Overall, which expression/Theorem guides us in understanding the improvement of prior suboptimality is not clear? Can you please point out/highlight how the current method improves upon the prior suboptimality due to static prompt distribution?

TL;DR: The improvement of sub-optimality is guided by the minimax regret objective (Remark 1) through its iterative implementation. While this work does not explicitly derive suboptimality bounds, our approach has demonstrated **strong empirical gains** over the training by static distributions, as shown in § 4, § E, and § D.2.

Rebuttal: In general, the improvement of prior suboptimality due to static prompt distributions is guided by the minimax game outlined in Remark 1. This expression forms the basic foundation for

our iterative algorithm, where the creator updates prompts to maximize informativeness (proxy for regret), and the solver minimizes regret (implicitly through direct preference optimization). This iterative process ensures the solver and creator adapt to each other, implicitly forming a curriculum and addressing sub-optimality inherent in static prompts. We have also added § H with additional literature on open-ended learning to help illustrate the intuition behind.

While we do not explicitly derive suboptimality bounds (as would be typical in formal RL/bandit theory), the empirical results in § 4, § E, and § D.2 demonstrate that the dynamic prompt distribution improves solver performance and alignment metrics, thereby effectively mitigating suboptimality.

We thank the reviewer’s suggestions on formalizing sub-optimality analysis further and would love to consider this an exciting direction for future work.

W6 (Prompt Distribution): It is extremely crucial to show the prompt distribution and demonstrate its perplexity to ensure its not generating some meaningless or irrelevant prompts, since its not very evident on the KL divergence in the prompt space and its relation with the informative measure. Please provide detailed explanation to clarify that.

TL;DR: We have (i) added experimental results in § E and § J to verify that **eva** evolves meaningful and relevant prompts; (ii) added explanation in § G on the KL regularization and in this rebuttal.

Rebuttal: (This rebuttal also addresses Reviewer ac2p’s concerns on curriculum.)

We have revised the manuscript with additional visualization on potential curriculum learned in § E. In general, we observe the creator prioritizes learning in math and coding for the generated prompt distribution, which brings gradual improvement on benchmark performance on relevant categories over iterations. In other words, **eva** effectively shifts focus towards harder yet learnable categories. We have attached the bar plot and radar figure here for the reviewer’s reference:

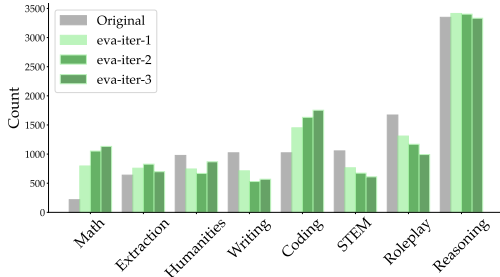


Figure 15: **Training distributions.** The prompt distribution of Table 11 for evolved prompts by zero-shot classification. **eva** creates a curriculum that prioritizes math / coding prompts.

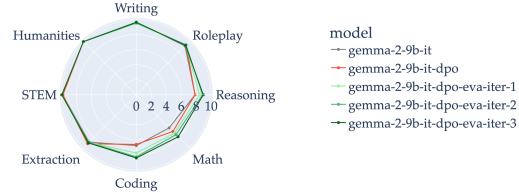


Figure 16: **Benchmark performance.** The radar figure for ratings on MT-Bench (Zheng et al., 2023), where each category contains ten problems. **eva** prioritizes and gradually improves on coding, math and reasoning over iterations, implicitly reflecting a learned curriculum.

We have added Table 15 providing qualitative examples for evolved prompts. Also, as noted in § G, the solver maintains KL regularization during optimization, ensuring that the response distribution remain close to the reference policy; in the this work, we do not explicitly add KL regularization in the prompt distribution since we do not directly conduct parameter update for the creator (which we empirically find to bring training instability); rather, we use **meta instructions** and **buffer sampling** to constrain the prompt generations (as described in § 3.3, § A and § D.1), which is empirically very effective, and introduces only minimal changes to existing pipeline thus can be easily applied. As noted in § 6, we look forward future works on making the creator policy differentiable.

Regarding the relation with the informativeness measure, our current proxy is an efficient proxy among many possibilities. We have provided detailed discussions in § G.2.1 to help interpret it. There could be other proxies – one interesting direction is to completely remove the dependence on the reward model and directly use model likelihoods to make the prompt selection.

Q1 and Q2 (KL in the Solver Loop): Since equation 7, can't be directly solved, and is solved in an asymmetric fashion, then in the solver loop the KL should be over the response distribution and not joint right? How is the KL divergence w.r.t reference policy for the algorithm? Please provide detailed ablation.

Answer: (i) Yes, in the solver loop, the KL regularization is applied over the response distribution, not the joint distribution, as shown in Line 5 of Algo. 1. (ii) The KL divergence w.r.t. reference policy is determined by the plug-in solver (e.g., DPO, SimPO, ...), which is orthogonal to our framework. We have added detailed explanation in § G to illustrate the whole process.

Q3 (RM Availability): What's the reward model availability? Is the true reward model available?

Answer: Yes, we assume the availability of a pre-trained, off-the-shelf reward model. This approach is practically adopted in industry (Team et al., 2023; 2024a;b) and is also commonly used in academia works (Xu et al., 2023b; Meng et al., 2024; Wu et al., 2024). See also our detailed rebuttal for W4.

Q4 (Added Paper Review): There is a recent line of works on Stacklberg and Bilevel RLHF which deals with the entanglement in a leader-follower setting. Although not specific to updating prompt dist, but can be trivially applied. Provide a detailed comparison with the literature around that [1,2,3].

TL;DR: We thank the reviewer for this nice suggestion. Please see below for a detailed review on the relevant literature, highlighting the unique contribution of **eva**. We have added § I in the manuscript.

Rebuttal: Bi-level optimization refers to optimization problems where the cost function is defined w.r.t. the optimal solution to another optimization problem (Grosse, 2022). There is a recent line of works applying bi-level optimization to RLHF. While they all rely on a fixed dataset of prompts, **eva** propose to dynamically update the prompt set, as discussed in § 1. We here present a detailed review on these works, with a detailed comparison with Ding et al. (2024); Shen et al. (2024); Makar-Limanov et al. (2024). While those works are orthogonal **eva**, we would like to sincerely thank the anonymous reviewer for the kind suggestion on these references that helps guide future works on robust and self-improving alignment, especially on helping addressing the potential distributional mismatch issues as the policy models become more powerful.

Ding et al. (2024) formulate iterative online RLHF as a bi-level optimization problem, where the upper-level represents the reward learning, and the lower-level represents the policy optimization. Leveraging reward re-parameterization tricks in Rafailov et al. (2023), Ding et al. (2024) reduces the problem to a single-level objective with regard to the policy. The differences of this work and our work lie in the prompt distribution and preference oracle: (i) **eva** features by **dynamic prompt set generation for Open-Ended RLHF**, whereas (Ding et al., 2024) remains using a static prompt set; (ii) we assume the existence of the preference oracle (as discussed in § 4), while Ding et al. (2024) consider online training of reward models and ablate on self-rewarding by the current LLM policy. Our usage of a pre-trained reward model follows from industrial practices (Team et al., 2023; 2024b), which is also commonly used by prior works in academia like SimPO (Meng et al., 2024) and SPPO (Wu et al., 2024) for proof-of-concept experiments. We recognize the online training of reward models (see also (Dong et al., 2024b)) as an orthogonal/complementary direction to the current settings of **eva** (our setting is **agnostic to the preference structure**), and encourage future works and collaborations towards it, as mentioned in § 6.

Makar-Limanov et al. (2024) provide an interesting exploration on formulating RLHF as a leader-follower game, where the language model (LM) policy is the leader and the reward model (RM) policy is the follower, and the solution is **Stackelberg equilibrium** (von Stackelberg, 1934; Rajeswaran et al., 2020), where the *leader does not likewise best respond to the follower's strategy*. Here, following the curriculum RL literature (Dennis et al., 2020; Parker-Holder et al., 2022), we seek the **Nash equilibrium** (Nash et al., 1950) between the creator for prompt generation and the solver for response generation. In the current setting of **eva**, the goal is to search for an optimal solver policy with a best supporting prompt distribution, *and* an optimal prompt distribution with a best supporting solver policy. Nevertheless, the LM-RM iterative optimization may be added on top of **eva**'s framework, and we likewise encourage future works exploring the leader-follower re-formulation of **eva**.

Shen et al. (2024) present a rigorous theoretical work (it may not be directly related to this paper’s primary field as it does not involve practical post-training of large language models). Specifically, the authors propose to reduce the bi-level problem to a single-level problem with a penalty-based reformulation, and similarly applies it in the setting of LM-RM optimization within a *fixed* environment, whereas **eva** focuses on dynamic prompt generation and practically train large language models with extensive empirical experiments conducted. We believe it would be interesting to adapt similar first-order optimization techniques to solve Open-Ended RLHF.

In summary, the above mentioned bi-level RLHF works focus on online optimization of both the RM and the LM (as the response policy), all with **fixed** prompt/state distribution. **eva** presents an orthogonal direction on **dynamic** prompt generation for Open-Ended RLHF, with an empirical algorithm which attains state-of-the-art performance with large language models on a variety of benchmarks. From a research perspective, it is possible to incorporate the online RM training within **eva** – we have shown in § 4.2.3 that **eva** scales with quality of reward models, thus integrating online RM training may further enhance performance, dynamically evolving both the reward model and prompt distribution. This direction may have not been widely adopted in real-world training of language models, likely due to concerns about practicality (Team et al., 2023; 2024a;b; Adler et al., 2024). We look forward to future works exploring whether *efficient* variations unifying **eva** and existing bi-level frameworks could address these challenges.

Q5 (Intuition on Open-Ended RLHF): Can you provide intuitions behind equation 7, on the KL divergence between the joint policy for both prompt and response? Is it even tractable to estimate or approximate this KL?

Answer: To avoid repetition, please see our detailed rebuttal for **W1**. We have also added § G to ensure this concern is sufficiently addressed.

Remarks. We sincerely thank Reviewer i9kx for the precious time and efforts on the **eva** method. We value all those opinions, and have made careful efforts to address them. Regarding the rejection, we warmly encourage the reviewer to consider the points that we have summarized at the beginning of this rebuttal, on the **strong performance gain** brought by the **simple design** of **eva**, also on judging the merit of a work (*cf.*, (Castro, 2021)) *w.r.t.* the practicality and how the community can easily build on top of it (*cf.*, (Hamming, 1986)). We look forward to any future discussions and suggestions on theoretical future works, and we would like to again express our gratitude to the reviewer once again for the time spent for reviewing.

REFERENCES

- Zaheer Abbas, Rosie Zhao, Joseph Modayil, Adam White, and Marlos C Machado. [Loss of plasticity in continual deep reinforcement learning](#). In *Conference on Lifelong Learning Agents*, pages 620–636. PMLR, 2023.
- Bo Adler, Niket Agarwal, Ashwath Aithal, Dong H Anh, Pallab Bhattacharya, Annika Brundyn, Jared Casper, Bryan Catanzaro, Sharon Clay, Jonathan Cohen, et al. [Nemotron-4 340B Technical Report](#). *arXiv preprint arXiv:2406.11704*, 2024.
- Arash Ahmadian, Chris Cremer, Matthias Gallé, Marzieh Fadaee, Julia Kreutzer, Ahmet Üstün, and Sara Hooker. [Back to basics: Revisiting reinforce style optimization for learning from human feedback in llms](#). *arXiv preprint arXiv:2402.14740*, 2024.
- Jordan T Ash and Ryan P Adams. [On the difficulty of warm-starting neural network training](#). *arXiv preprint arXiv:1910.08475*, 2019.
- Alfredo Banos. [On pseudo-games](#). *The Annals of Mathematical Statistics*, 39(6):1932–1945, 1968.
- Yoshua Bengio, Jérôme Louradour, Ronan Collobert, and Jason Weston. [Curriculum learning](#). In *Proceedings of the 26th annual international conference on machine learning*, pages 41–48, 2009.
- Michael Beukman, Samuel Coward, Michael Matthews, Mattie Fellows, Minqi Jiang, Michael Dennis, and Jakob Foerster. [Refining Minimax Regret for Unsupervised Environment Design](#). *arXiv preprint arXiv:2402.12284*, 2024.
- Tom Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared D Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, Sandhini Agarwal, Ariel Herbert-Voss, Gretchen Krueger, Tom Henighan, Rewon Child, Aditya Ramesh, Daniel Ziegler, Jeffrey Wu, Clemens Winter, Chris Hesse, Mark Chen, Eric Sigler, Mateusz Litwin, Scott Gray, Benjamin Chess, Jack Clark, Christopher Berner, Sam McCandlish, Alec Radford, Ilya Sutskever, and Dario Amodei. [Language models are few-shot learners](#). In H. Larochelle, M. Ranzato, R. Hadsell, M.F. Balcan, and H. Lin, editors, *Advances in Neural Information Processing Systems*, volume 33, pages 1877–1901. Curran Associates, Inc., 2020. URL https://proceedings.neurips.cc/paper_files/paper/2020/file/1457c0d6bfc4967418bfb8ac142f64a-Paper.pdf.
- Seth Chaiklin et al. [The zone of proximal development in Vygotsky’s analysis of learning and instruction](#). *Vygotsky’s educational theory in cultural context*, 1(2):39–64, 2003.
- Ching-An Cheng, Allen Nie, and Adith Swaminathan. [Trace is the Next AutoDiff: Generative Optimization with Rich Feedback, Execution Traces, and LLMs](#). *arXiv preprint arXiv:2406.16218*, 2024.
- Eugene Choi, Arash Ahmadian, Matthieu Geist, Olivier Pietquin, and Mohammad Gheshlaghi Azar. [Self-Improving Robust Preference Optimization](#). *arXiv preprint arXiv:2406.01660*, 2024.
- Paul F Christiano, Jan Leike, Tom Brown, Miljan Martic, Shane Legg, and Dario Amodei. [Deep reinforcement learning from human preferences](#). *Advances in neural information processing systems*, 30, 2017.
- Ganqu Cui, Lifan Yuan, Ning Ding, Guanming Yao, Wei Zhu, Yuan Ni, Guotong Xie, Zhiyuan Liu, and Maosong Sun. [Ultrafeedback: Boosting language models with high-quality feedback](#). *arXiv preprint arXiv:2310.01377*, 2023.
- Nirjhar Das, Souradip Chakraborty, Aldo Pacchiano, and Sayak Ray Chowdhury. [Provably sample efficient rlhf via active preference optimization](#). *arXiv preprint arXiv:2402.10500*, 2024.
- Peter Dayan and Geoffrey E Hinton. [Using expectation-maximization for reinforcement learning](#). *Neural Computation*, 9(2):271–278, 1997.
- Michael Dennis, Natasha Jaques, Eugene Vinitzky, Alexandre Bayen, Stuart Russell, Andrew Critch, and Sergey Levine. [Emergent complexity and zero-shot transfer via unsupervised environment design](#). *Advances in neural information processing systems*, 33:13049–13061, 2020.

- Mucong Ding, Souradip Chakraborty, Vibhu Agrawal, Zora Che, Alec Koppel, Mengdi Wang, Amrit Bedi, and Furong Huang. [Sail: Self-improving efficient online alignment of large language models](#). *arXiv preprint arXiv:2406.15567*, 2024.
- Shibhansh Dohare, J Fernando Hernandez-Garcia, Parash Rahman, A Rupam Mahmood, and Richard S Sutton. [Maintaining plasticity in deep continual learning](#). *arXiv preprint arXiv:2306.13812*, 2023.
- Hanze Dong, Wei Xiong, Deepanshu Goyal, Yihan Zhang, Winnie Chow, Rui Pan, Shizhe Diao, Jipeng Zhang, Kashun Shum, and Tong Zhang. [Raft: Reward ranked finetuning for generative foundation model alignment](#). *arXiv preprint arXiv:2304.06767*, 2023.
- Hanze Dong, Wei Xiong, Bo Pang, Haoxiang Wang, Han Zhao, Yingbo Zhou, Nan Jiang, Doyen Sahoo, Caiming Xiong, and Tong Zhang. [RLHF Workflow: From Reward Modeling to Online RLHF](#), 2024a.
- Hanze Dong, Wei Xiong, Bo Pang, Haoxiang Wang, Han Zhao, Yingbo Zhou, Nan Jiang, Doyen Sahoo, Caiming Xiong, and Tong Zhang. [Rlhf workflow: From reward modeling to online rlhf](#). *arXiv preprint arXiv:2405.07863*, 2024b.
- Abhimanyu Dubey, Abhinav Jauhri, Abhinav Pandey, Abhishek Kadian, Ahmad Al-Dahle, Aiesha Letman, Akhil Mathur, Alan Schelten, Amy Yang, Angela Fan, et al. [The llama 3 herd of models](#). *arXiv preprint arXiv:2407.21783*, 2024.
- Yann Dubois, Balázs Galambosi, Percy Liang, and Tatsunori B Hashimoto. [Length-controlled alpacaeval: A simple way to debias automatic evaluators](#). *arXiv preprint arXiv:2404.04475*, 2024.
- Ky Fan. [Minimax theorems](#). *Proceedings of the National Academy of Sciences*, 39(1):42–47, 1953.
- Yoav Freund and Robert E. Schapire. [\(Adaptive Game Playing Using Multiplicative Weights\)](#). *Games and Economic Behavior*, 29:79–103, 1999.
- Matthias Gerstgrasser, Rylan Schaeffer, Apratim Dey, Rafael Rafailov, Henry Sleight, John Hughes, Tomasz Korbak, Rajashree Agrawal, Dhruv Pai, Andrey Gromov, et al. [Is model collapse inevitable? breaking the curse of recursion by accumulating real and synthetic data](#). *arXiv preprint arXiv:2404.01413*, 2024.
- Ian Goodfellow, Jean Pouget-Abadie, Mehdi Mirza, Bing Xu, David Warde-Farley, Sherjil Ozair, Aaron Courville, and Yoshua Bengio. [Generative adversarial nets](#). *Advances in neural information processing systems*, 27, 2014.
- Roger Grosse. [Bilevel Optimization and Generalization](#), 2022.
- Caglar Gulcehre, Tom Le Paine, Srivatsan Srinivasan, Ksenia Konyushkova, Lotte Weerts, Abhishek Sharma, Aditya Siddhant, Alex Ahern, Miaosen Wang, Chenjie Gu, et al. [Reinforced self-training \(rest\) for language modeling](#). *arXiv preprint arXiv:2308.08998*, 2023.
- Qingyan Guo, Rui Wang, Junliang Guo, Bei Li, Kaitao Song, Xu Tan, Guoqing Liu, Jiang Bian, and Yujiu Yang. [Connecting large language models with evolutionary algorithms yields powerful prompt optimizers](#). *arXiv preprint arXiv:2309.08532*, 2023.
- Shangmin Guo, Biao Zhang, Tianlin Liu, Tianqi Liu, Misha Khalman, Felipe Llinares, Alexandre Rame, Thomas Mesnard, Yao Zhao, Bilal Piot, et al. [Direct language model alignment from online ai feedback](#). *arXiv preprint arXiv:2402.04792*, 2024.
- Joey Hejna, Rafael Rafailov, Harshit Sikchi, Chelsea Finn, Scott Niekum, W Bradley Knox, and Dorsa Sadigh. [Contrastive preference learning: Learning from human feedback without rl](#). *arXiv preprint arXiv:2310.13639*, 2023.
- Jiwoo Hong, Noah Lee, and James Thorne. [Orpo: Monolithic preference optimization without reference model](#). *arXiv preprint arXiv:2403.07691*, 2(4):5, 2024.
- Jiaxin Huang, Shixiang Shane Gu, Le Hou, Yuexin Wu, Xuezhi Wang, Hongkun Yu, and Jiawei Han. [Large language models can self-improve](#). *arXiv preprint arXiv:2210.11610*, 2022.

- Edward Hughes, Michael Dennis, Jack Parker-Holder, Feryal Behbahani, Aditi Mavalankar, Yuge Shi, Tom Schaul, and Tim Rocktaschel. [Open-Endedness is Essential for Artificial Superhuman Intelligence](#). *arXiv preprint arXiv:2406.04268*, 2024a.
- Edward Hughes, Michael Dennis, Jack Parker-Holder, Feryal Behbahani, Aditi Mavalankar, Yuge Shi, Tom Schaul, and Tim Rocktaschel. [Open-Endedness is Essential for Artificial Superhuman Intelligence](#). *arXiv preprint arXiv:2406.04268*, 2024b.
- Angela H Jiang, Daniel L-K Wong, Giulio Zhou, David G Andersen, Jeffrey Dean, Gregory R Ganger, Gauri Joshi, Michael Kaminsky, Michael Kozuch, Zachary C Lipton, et al. [Accelerating deep learning by focusing on the biggest losers](#). *arXiv preprint arXiv:1910.00762*, 2019.
- Dongfu Jiang, Xiang Ren, and Bill Yuchen Lin. [Llm-blender: Ensembling large language models with pairwise ranking and generative fusion](#). *arXiv preprint arXiv:2306.02561*, 2023.
- Minqi Jiang, Michael Dennis, Jack Parker-Holder, Jakob Foerster, Edward Grefenstette, and Tim Rocktäschel. [Replay-guided adversarial environment design](#). *Advances in Neural Information Processing Systems*, 34:1884–1897, 2021a.
- Minqi Jiang, Edward Grefenstette, and Tim Rocktäschel. [Prioritized level replay](#). In *International Conference on Machine Learning*, pages 4940–4950. PMLR, 2021b.
- Kenji Kawaguchi and Haihao Lu. [Ordered sgd: A new stochastic optimization framework for empirical risk minimization](#). In *International Conference on Artificial Intelligence and Statistics*, pages 669–679. PMLR, 2020.
- John Maynard Keynes. [A treatise on probability](#). Courier Corporation, 1921.
- Haoran Li, Qingxiu Dong, Zhengyang Tang, Chaojun Wang, Xingxing Zhang, Haoyang Huang, Shao-han Huang, Xiaolong Huang, Zeqiang Huang, Dongdong Zhang, et al. [Synthetic data \(almost\) from scratch: Generalized instruction tuning for language models](#). *arXiv preprint arXiv:2402.13064*, 2024a.
- Tianle Li, Wei-Lin Chiang, Evan Frick, Lisa Dunlap, Tianhao Wu, Banghua Zhu, Joseph E Gonzalez, and Ion Stoica. [From Crowdsourced Data to High-Quality Benchmarks: Arena-Hard and BenchBuilder Pipeline](#). *arXiv preprint arXiv:2406.11939*, 2024b.
- Chris Yuhao Liu and Liang Zeng. [Skywork Reward Model Series](#). <https://huggingface.co/Skywork>, September 2024. URL <https://huggingface.co/Skywork>.
- Tianqi Liu, Yao Zhao, Rishabh Joshi, Misha Khalman, Mohammad Saleh, Peter J Liu, and Jialu Liu. Statistical rejection sampling improves preference optimization. *arXiv preprint arXiv:2309.06657*, 2023a.
- Wei Liu, Weihao Zeng, Keqing He, Yong Jiang, and Junxian He. [What makes good data for alignment? a comprehensive study of automatic data selection in instruction tuning](#). *arXiv preprint arXiv:2312.15685*, 2023b.
- Lin Long, Rui Wang, Ruixuan Xiao, Junbo Zhao, Xiao Ding, Gang Chen, and Haobo Wang. [On llms-driven synthetic data generation, curation, and evaluation: A survey](#). *arXiv preprint arXiv:2406.15126*, 2024.
- Haipeng Luo, Qingfeng Sun, Can Xu, Pu Zhao, Jianguang Lou, Chongyang Tao, Xiubo Geng, Qingwei Lin, Shifeng Chen, and Dongmei Zhang. [Wizardmath: Empowering mathematical reasoning for large language models via reinforced evol-instruct](#). *arXiv preprint arXiv:2308.09583*, 2023.
- Jacob Makar-Limanov, Arjun Prakash, Denizalp Goktas, Amy Greenwald, and Nora Ayanian. [STA-RLHF: Stackelberg Aligned Reinforcement Learning with Human Feedback](#). In *Coordination and Cooperation for Multi-Agent Reinforcement Learning Methods Workshop*, 2024. URL <https://openreview.net/forum?id=Jcn8pxwRa9>.
- Yu Meng, Mengzhou Xia, and Danqi Chen. [SimPO: Simple Preference Optimization with a Reference-Free Reward](#). *arXiv preprint arXiv:2405.14734*, 2024.

- Sören Mindermann, Jan M Brauner, Muhammed T Razzak, Mrinank Sharma, Andreas Kirsch, Winnie Xu, Benedikt Höltingen, Aidan N Gomez, Adrien Morisot, Sebastian Farquhar, et al. [Prioritized training on points that are learnable, worth learning, and not yet learnt](#). In *International Conference on Machine Learning*, pages 15630–15649. PMLR, 2022.
- William Muldrew, Peter Hayes, Mingtian Zhang, and David Barber. [Active Preference Learning for Large Language Models](#). *arXiv preprint arXiv:2402.08114*, 2024.
- Rémi Munos, Michal Valko, Daniele Calandriello, Mohammad Gheshlaghi Azar, Mark Rowland, Zhaohan Daniel Guo, Yunhao Tang, Matthieu Geist, Thomas Mesnard, Andrea Michi, et al. [Nash learning from human feedback](#). *arXiv preprint arXiv:2312.00886*, 2023.
- John F Nash et al. [Non-cooperative games](#). *Princeton University*, 1950.
- Allen Nie, Ching-An Cheng, Andrey Kolobov, and Adith Swaminathan. [The Importance of Directional Feedback for LLM-based Optimizers](#). *arXiv preprint arXiv:2405.16434*, 2024.
- Evgenii Nikishin, Max Schwarzer, Pierluca D’Oro, Pierre-Luc Bacon, and Aaron Courville. The primacy bias in deep reinforcement learning. In *International conference on machine learning*, pages 16828–16847. PMLR, 2022.
- Long Ouyang, Jeffrey Wu, Xu Jiang, Diogo Almeida, Carroll Wainwright, Pamela Mishkin, Chong Zhang, Sandhini Agarwal, Katarina Slama, Alex Ray, et al. [Training language models to follow instructions with human feedback](#). *Advances in neural information processing systems*, 35:27730–27744, 2022.
- Richard Yuanzhe Pang, Weizhe Yuan, Kyunghyun Cho, He He, Sainbayar Sukhbaatar, and Jason Weston. [Iterative reasoning preference optimization](#). *arXiv preprint arXiv:2404.19733*, 2024.
- Jack Parker-Holder, Minqi Jiang, Michael Dennis, Mikayel Samvelyan, Jakob Foerster, Edward Grefenstette, and Tim Rocktäschel. [Evolving curricula with regret-based environment design](#). In *International Conference on Machine Learning*, pages 17473–17498. PMLR, 2022.
- Gabriel Poesia, David Broman, Nick Haber, and Noah D Goodman. [Learning Formal Mathematics From Intrinsic Motivation](#). *arXiv preprint arXiv:2407.00695*, 2024.
- Rafael Rafailov, Archit Sharma, Eric Mitchell, Stefano Ermon, Christopher D Manning, and Chelsea Finn. [Direct preference optimization: Your language model is secretly a reward model](#). *arXiv preprint arXiv:2305.18290*, 2023.
- Aravind Rajeswaran, Igor Mordatch, and Vikash Kumar. [A game theoretic framework for model based reinforcement learning](#). In *International conference on machine learning*, pages 7953–7963. PMLR, 2020.
- Corby Rosset, Ching-An Cheng, Arindam Mitra, Michael Santacrose, Ahmed Awadallah, and Tengyang Xie. [Direct Nash Optimization: Teaching Language Models to Self-Improve with General Preferences](#). *arXiv preprint arXiv:2404.03715*, 2024.
- Daniel J Russo, Benjamin Van Roy, Abbas Kazerouni, Ian Osband, Zheng Wen, et al. [A tutorial on thompson sampling](#). *Foundations and Trends® in Machine Learning*, 11(1):1–96, 2018.
- Arthur L Samuel. [Some studies in machine learning using the game of checkers](#). *IBM Journal of research and development*, 3(3):210–229, 1959.
- Mikayel Samvelyan, Akbir Khan, Michael Dennis, Minqi Jiang, Jack Parker-Holder, Jakob Foerster, Roberta Raileanu, and Tim Rocktäschel. [MAESTRO: Open-ended environment design for multi-agent reinforcement learning](#). *arXiv preprint arXiv:2303.03376*, 2023.
- Leonard J Savage. [The theory of statistical decision](#). *Journal of the American Statistical association*, 46(253):55–67, 1951.
- Jürgen Schmidhuber. [A possibility for implementing curiosity and boredom in model-building neural controllers](#). In *Proc. of the international conference on simulation of adaptive behavior: From animals to animats*, 1991.

- Hans-Paul Schwefel. *Evolutionsstrategien für die numerische Optimierung*. Springer, 1977.
- Amrith Setlur, Saurabh Garg, Xinyang Geng, Naman Garg, Virginia Smith, and Aviral Kumar. [RL on Incorrect Synthetic Data Scales the Efficiency of LLM Math Reasoning by Eight-Fold](#). *arXiv preprint arXiv:2406.14532*, 2024.
- Han Shen, Zhuoran Yang, and Tianyi Chen. [Principled penalty-based methods for bilevel reinforcement learning and rlhf](#). *arXiv preprint arXiv:2402.06886*, 2024.
- David Silver, Aja Huang, Chris J Maddison, Arthur Guez, Laurent Sifre, George Van Den Driessche, Julian Schrittwieser, Ioannis Antonoglou, Veda Panneershelvam, Marc Lanctot, et al. [Mastering the game of Go with deep neural networks and tree search](#). *nature*, 529(7587):484–489, 2016.
- David Silver, Satinder Singh, Doina Precup, and Richard S Sutton. [Reward is enough](#). *Artificial Intelligence*, 299:103535, 2021.
- Avi Singh, John D Co-Reyes, Rishabh Agarwal, Ankesh Anand, Piyush Patil, Peter J Liu, James Harrison, Jaehoon Lee, Kelvin Xu, Aaron Parisi, et al. [Beyond human data: Scaling self-training for problem-solving with language models](#). *arXiv preprint arXiv:2312.06585*, 2023.
- Charlie Snell, Jaehoon Lee, Kelvin Xu, and Aviral Kumar. [Scaling llm test-time compute optimally can be more effective than scaling model parameters](#). *arXiv preprint arXiv:2408.03314*, 2024.
- Sainbayar Sukhbaatar, Zeming Lin, Ilya Kostrikov, Gabriel Synnaeve, Arthur Szlam, and Rob Fergus. [Intrinsic motivation and automatic curricula via asymmetric self-play](#). *arXiv preprint arXiv:1703.05407*, 2017.
- Zhiqing Sun, Yikang Shen, Qinzhong Zhou, Hongxin Zhang, Zhenfang Chen, David Cox, Yiming Yang, and Chuang Gan. [Principle-driven self-alignment of language models from scratch with minimal human supervision](#). *Advances in Neural Information Processing Systems*, 36, 2024.
- Richard S Sutton, Joseph Modayil, Michael Delp, Thomas Degris, Patrick M Pilarski, Adam White, and Doina Precup. [Horde: A scalable real-time architecture for learning knowledge from unsupervised sensorimotor interaction](#). In *The 10th International Conference on Autonomous Agents and Multiagent Systems-Volume 2*, pages 761–768, 2011.
- Fahim Tajwar, Anikait Singh, Archit Sharma, Rafael Rafailov, Jeff Schneider, Tengyang Xie, Stefano Ermon, Chelsea Finn, and Aviral Kumar. [Preference fine-tuning of llms should leverage suboptimal, on-policy data](#). *arXiv preprint arXiv:2404.14367*, 2024.
- Yunhao Tang, Zhaohan Daniel Guo, Zeyu Zheng, Daniele Calandriello, Rémi Munos, Mark Rowland, Pierre Harvey Richemond, Michal Valko, Bernardo Ávila Pires, and Bilal Piot. [Generalized preference optimization: A unified approach to offline alignment](#). *arXiv preprint arXiv:2402.05749*, 2024.
- Gemini Team, Rohan Anil, Sebastian Borgeaud, Yonghui Wu, Jean-Baptiste Alayrac, Jiahui Yu, Radu Soricut, Johan Schalkwyk, Andrew M Dai, Anja Hauth, et al. [Gemini: a family of highly capable multimodal models](#). *arXiv preprint arXiv:2312.11805*, 2023.
- Gemini Team, M Reid, N Savinov, D Teplyashin, Lepikhin Dmitry, T Lillicrap, JB Alayrac, R Soricut, A Lazaridou, O Firat, et al. [Gemini 1.5: Unlocking multimodal understanding across millions of tokens of context](#). *arXiv preprint arXiv:2403.05530*, 2024a.
- Gemma Team, Morgane Riviere, Shreya Pathak, Pier Giuseppe Sessa, Cassidy Hardin, Surya Bhupatiraju, Léonard Hussenot, Thomas Mesnard, Bobak Shahriari, Alexandre Ramé, et al. [Gemma 2: Improving open language models at a practical size](#). *arXiv preprint arXiv:2408.00118*, 2024b.
- Open Ended Learning Team, Adam Stooke, Anuj Mahajan, Catarina Barros, Charlie Deck, Jakob Bauer, Jakub Sygnowski, Maja Trebacz, Max Jaderberg, Michael Mathieu, et al. [Open-ended learning leads to generally capable agents](#). *arXiv preprint arXiv:2107.12808*, 2021.

- Josh Tobin, Rachel Fong, Alex Ray, Jonas Schneider, Wojciech Zaremba, and Pieter Abbeel. [Domain randomization for transferring deep neural networks from simulation to the real world](#). In *2017 IEEE/RSJ international conference on intelligent robots and systems (IROS)*, pages 23–30. IEEE, 2017.
- Hoang Tran, Chris Glaze, and Braden Hancock. [Iterative DPO Alignment](#). Technical report, Snorkel AI, 2023.
- Pablo Villalobos, Jaime Sevilla, Lennart Heim, Tamay Besiroglu, Marius Hobbhahn, and Anson Ho. [Will we run out of data? Limits of LLM scaling based on human-generated data](#). *arXiv preprint arXiv:2211.04325*, 2024.
- Heinrich von Stackelberg. [Marktform und Gleichgewicht](#). Die Handelsblatt-Bibliothek "Klassiker der Nationalökonomie". J. Springer, 1934. URL <https://books.google.com/books?id=wihBAAAAIAAJ>.
- Haoxiang Wang, Wei Xiong, Tengyang Xie, Han Zhao, and Tong Zhang. [Interpretable Preferences via Multi-Objective Reward Modeling and Mixture-of-Experts](#). *arXiv preprint arXiv:2406.12845*, 2024.
- Rui Wang, Joel Lehman, Jeff Clune, and Kenneth O Stanley. [Paired open-ended trailblazer \(poet\): Endlessly generating increasingly complex and diverse learning environments and their solutions](#). *arXiv preprint arXiv:1901.01753*, 2019.
- Yizhong Wang, Yeganeh Kordi, Swaroop Mishra, Alisa Liu, Noah A Smith, Daniel Khashabi, and Hannaneh Hajishirzi. [Self-instruct: Aligning language models with self-generated instructions](#). *arXiv preprint arXiv:2212.10560*, 2022.
- Huasen Wu and Xin Liu. [Double thompson sampling for dueling bandits](#). *Advances in neural information processing systems*, 29, 2016.
- Yue Wu, Zhiqing Sun, Huizhuo Yuan, Kaixuan Ji, Yiming Yang, and Quanquan Gu. [Self-play preference optimization for language model alignment](#). *arXiv preprint arXiv:2405.00675*, 2024.
- Wei Xiong, Hanze Dong, Chenlu Ye, Ziqi Wang, Han Zhong, Heng Ji, Nan Jiang, and Tong Zhang. [Iterative preference learning from human feedback: Bridging theory and practice for rlhf under kl-constraint](#). In *Forty-first International Conference on Machine Learning*, 2024.
- Can Xu, Qingfeng Sun, Kai Zheng, Xiubo Geng, Pu Zhao, Jiazhan Feng, Chongyang Tao, and Daxin Jiang. [Wizardlm: Empowering large language models to follow complex instructions](#). *arXiv preprint arXiv:2304.12244*, 2023a.
- Jing Xu, Andrew Lee, Sainbayar Sukhbaatar, and Jason Weston. [Some things are more cringe than others: Preference optimization with the pairwise cringe loss](#). *arXiv preprint arXiv:2312.16682*, 2023b.
- Zhangchen Xu, Fengqing Jiang, Luyao Niu, Yuntian Deng, Radha Poovendran, Yejin Choi, and Bill Yuchen Lin. [Magpie: Alignment Data Synthesis from Scratch by Prompting Aligned LLMs with Nothing](#). *arXiv preprint arXiv:2406.08464*, 2024.
- Fuzhao Xue, Yao Fu, Wangchunshu Zhou, Zangwei Zheng, and Yang You. [To repeat or not to repeat: Insights from scaling llm under token-crisis](#). *Advances in Neural Information Processing Systems*, 36, 2024.
- Kaiyu Yang, Aidan Swope, Alex Gu, Rahul Chalamala, Peiyang Song, Shixing Yu, Saad Godil, Ryan J Prenger, and Animashree Anandkumar. [Leandojo: Theorem proving with retrieval-augmented language models](#). *Advances in Neural Information Processing Systems*, 36, 2024.
- Weizhe Yuan, Richard Yuanzhe Pang, Kyunghyun Cho, Sainbayar Sukhbaatar, Jing Xu, and Jason Weston. [Self-rewarding language models](#). *arXiv preprint arXiv:2401.10020*, 2024.
- Zheng Yuan, Hongyi Yuan, Chengpeng Li, Guanting Dong, Keming Lu, Chuanqi Tan, Chang Zhou, and Jingren Zhou. [Scaling relationship on learning mathematical reasoning with large language models](#). *arXiv preprint arXiv:2308.01825*, 2023.

2322 Mert Yuksekgonul, Federico Bianchi, Joseph Boen, Sheng Liu, Zhi Huang, Carlos Guestrin, and
2323 James Zou. [TextGrad: Automatic” Differentiation” via Text](#). *arXiv preprint arXiv:2406.07496*,
2324 2024.

2325 Eric Zelikman, Yuhuai Wu, Jesse Mu, and Noah Goodman. [Star: Bootstrapping reasoning with](#)
2326 [reasoning](#). *Advances in Neural Information Processing Systems*, 35:15476–15488, 2022.

2327

2328 Yao Zhao, Rishabh Joshi, Tianqi Liu, Misha Khalman, Mohammad Saleh, and Peter J Liu. [Slic-hf:](#)
2329 [Sequence likelihood calibration with human feedback](#). *arXiv preprint arXiv:2305.10425*, 2023.

2330

2331 Lianmin Zheng, Wei-Lin Chiang, Ying Sheng, Siyuan Zhuang, Zhanghao Wu, Yonghao Zhuang,
2332 Zi Lin, Zhuohan Li, Dacheng Li, Eric Xing, et al. [Judging llm-as-a-judge with mt-bench and](#)
2333 [chatbot arena](#). *Advances in Neural Information Processing Systems*, 36:46595–46623, 2023.

2334 Rui Zheng, Hongyi Guo, Zhihan Liu, Xiaoying Zhang, Yuanshun Yao, Xiaojun Xu, Zhaoran Wang,
2335 Zhiheng Xi, Tao Gui, Qi Zhang, et al. [Toward Optimal LLM Alignments Using Two-Player Games](#).
2336 *arXiv preprint arXiv:2406.10977*, 2024.

2337

2338

2339

2340

2341

2342

2343

2344

2345

2346

2347

2348

2349

2350

2351

2352

2353

2354

2355

2356

2357

2358

2359

2360

2361

2362

2363

2364

2365

2366

2367

2368

2369

2370

2371

2372

2373

2374

2375