

# TYPE-CONSTRAINED CODE GENERATION WITH LLMs

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## ABSTRACT

Large language models (LLMs) have achieved notable success in code generation. However, they still frequently produce uncompileable output because their next-token inference procedure does not model formal aspects of code. Although constrained decoding is a promising approach to alleviate this issue, it has only been applied to handle either domain-specific languages or syntactic language features. This leaves typing errors, which are beyond the domain of syntax and generally hard to adequately constrain. To address this challenge, we introduce a type-constrained decoding approach that leverages type systems to guide code generation. We develop novel prefix automata for this purpose and introduce a sound approach to enforce well-typedness based on type inference and a search over inhabitable types. We formalize our approach on a simply-typed language and extend it to TypeScript to demonstrate practicality. Our evaluation on HumanEval shows that our approach reduces compilation errors by more than half and increases functional correctness in code synthesis, translation, and repair tasks across LLMs of various sizes and model families, including SOTA open-weight models with more than 30B parameters.

## 1 INTRODUCTION

Large language models (LLMs) are remarkably successful in diverse fields (OpenAI, 2023; Brown et al., 2020; Grattafiori et al., 2024) and increasingly used in everyday coding tasks (GitHub, [n. d.]; Vella, 2024). Despite these achievements, LLM-generated code often contains compilation errors, logic flaws, or security vulnerabilities (Pan et al., 2024a; Dou et al., 2024; Pearce et al., 2022). These issues arise because LLM-based code generation does not provide any formal guarantees.

A promising solution is *constrained decoding*, which addresses this limitation by enforcing formal language rules during LLMs’ next-token generation process, rejecting invalid tokens. Prior work has shown that constraining to syntactic rules improves program correctness (Beurer-Kellner et al., 2024; Ugare et al., 2024; Poesia et al., 2022). However, their improvements are limited, as correct syntax accounts for only a small part of program correctness. Type systems detect and reject bugs at compile time (Mitchell, 1990; Matsakis and Klock, 2014) and are enforced in many popular programming languages (Bierman et al., 2014; Donovan and Kernighan, 2015; Arnold and Gosling, 1996). We suggest leveraging type systems to constrain LLMs based code generation.

The advantages of leveraging type systems are illustrated in Fig. 1. It presents five completion candidates for a partial program: (1)-(4) are rejected by the type system. Based on syntax, completions that contain line termination (;) or invalid characters (e.g., \$) could be rejected (1). However, other cases, such as (2)-(4), do not break syntactic rules but cause type errors. Candidate (2) accesses an undeclared identifier. Candidate (3) will fail at execution, as num is a number and can not be called. Candidate (4) passes a value of unexpected format to parseInt, which expects the first argument to be a string. In this example, (4) is generated by CodeLlama 34B (Rozière et al., 2023). Syntax-only constraining accepts this invalid completion, leading to a failing output. However, based on constraints derived from the type system, all but the valid completion (5) are rejected.

Implementing type-constrained decoding is challenging because type systems cannot be captured by context-free grammars (Mitchell, 1990), prohibiting the application of prior constrained decoding

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|                                                 | <completion>    | Vanilla | Syntax | Types  | Description           |
|-------------------------------------------------|-----------------|---------|--------|--------|-----------------------|
| <b>function</b> is_int(text: string): boolean { | (1) ;           | accept  | reject | reject | Syntactically invalid |
| <b>const</b> num = Number(text);                | (2) ber         | accept  | accept | reject | Undeclared identifier |
| <b>return</b> !isNaN(num) &&                    | (3) ( )         | accept  | accept | reject | Disallowed operator   |
| parseInt(num <completion>                       | (4) , 10)       | accept  | accept | reject | Invalid argument type |
| }                                               | (5) .toString() | accept  | accept | accept | Well-formed option    |

Figure 1: The left part is a partial TypeScript program derived from instance #113 of the MBPP benchmark (Austin et al., 2021), awaiting completion. On the right is a table listing five completion options: (1)-(4) are invalid and (5) is well-formed. Our type-constrained decoding is the only approach capable of correctly rejecting invalid completion candidates and accepting the valid one.

methods for program syntax (Ugare et al., 2024; Beurer-Kellner et al., 2024). Specifically, when generating expressions, we must address a key question: Can the partial expression be completed to match the required type? Essentially, this involves solving generalized type inhabitation (Urzyczyn, 1997; Gvero et al., 2013), a challenging problem that is PSPACE-complete even for simply typed lambda calculus, in the novel context of LLM-based code generation.

In this work, we introduce *type-constrained* decoding to enforce the formal rules of type systems on LLM-based code generation. In order to reason about the completability of partial code, we develop *prefix-automata*, which ensure that every visitable automaton state has a path to an accepting state. We then present a sound algorithm that determines types expressible through completions using type-search and an incrementally updated abstract syntax tree, including type annotations. To demonstrate its practical effectiveness, we instantiate our approach on a non-trivial subset of TypeScript, currently one of the most actively used languages (Madnight, 2024; GitHub, 2022). We perform an evaluation on TypeScript-translated HumanEval (Cassano et al., 2023) on synthesis, translation, and repair. Our experimental results show that type-constrained decoding significantly enhances code generation for LLMs of various sizes (2B-34B parameters) and families. For synthesis and translation, it reduces compilation errors by more than half and increases functional correctness relatively by 3.5% to 4.5%. Additionally, it enhances relative functional correctness of repaired code by around 34% on average. Our code implementation is publicly available.<sup>1</sup>

**LLM-based Code Generation** LLM-based code generation is incremental, depicted in Alg. 1 (without blue highlights). User prompt  $x$  specifies a task. The output program  $s$  is initialized to an empty string or program prefix in  $x$  (L. 1). In each iteration (L. 3), based on concatenation  $x \circ s$  of prompt  $x$  and partial program  $s$ , the LLM predicts a probability distribution  $p$  over a fixed, finite *vocabulary* of *tokens*, comprised of unicode characters, including common singleton characters (Sennrich et al., 2016). Next, based on distribution  $p$ , token  $t$  is sampled (L. 5) and appended to  $s$  (L. 10). This process repeats until special token *EOS* is sampled (L. 9).

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**Algorithm 1** Vanilla and constrained decoding

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**Input:** LLM, prompt  $x$ , completion engine  $CE_L$

**Output:** Program  $s$  such that  $s \in L$

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1: initialize  $s$ 
2: while true do
3:    $p \leftarrow \text{LLM}(x \circ s)$ 
4:   while true do
5:      $t \sim p$ 
6:     if  $CE_L(s \circ t)$  then break
7:     elif  $s \in L$  and  $t = \text{EOS}$  then break
8:     else  $p[t] \leftarrow 0$ ; normalize  $p$ 
9:   if  $t = \text{EOS}$  then break
10:   $s \leftarrow s \circ t$ 
11: return  $s$ 

```

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**Constrained Decoding** *Constrained decoding* analyzes intermediate model outputs to enforce validity of next tokens. It leverages a *completion engine*  $CE_L$ , specific to language  $L$ . The engine checks whether partial program  $s$  can be completed to a well-formed program in  $L$ , meaning whether there exists a (possibly empty) string  $s'$  such that  $s \circ s' \in L$ . Equivalently,  $CE_L(s)$  determines whether  $s$  belongs to the *prefix language*  $L^p$  of  $L$ , i.e., whether  $s \in L^p$ .

**Definition 1.** For a given language  $L$ , its *prefix language* is  $L^p = \{s \mid \exists s' : s \circ s' \in L\}$ .

As illustrated with blue highlights in Alg. 1, constrained decoding differs from vanilla LLM-based code generation by adding an additional sample-and-check loop in the token sampling process L. 4. A sampled token  $t$  is appended only if  $s \circ t$  can be completed to a well-formed program (L. 6) or  $t$  is *EOS* and  $s$  is already well-formed (L. 7). Otherwise, the probability of  $t$  is set to zero at L. 8, and the sample-and-check loop repeats. A token  $t$  satisfying L. 6 or L. 7 always exists, as  $s$  is in

<sup>1</sup>GitHub repository: <https://github.com/eth-sri/type-constrained-code-generation>

|                                 |                  |                           |                      |                                                 |                        |
|---------------------------------|------------------|---------------------------|----------------------|-------------------------------------------------|------------------------|
| $l ::=$                         | Literal          | $e ::= e_0 \mid e_1$      | Expression           | $x ::= \backslash w +$                          | Identifier             |
| $\backslash d +$                | Numeric Literal  | $e_0 ::=$                 | Base Expression      | $s ::=$                                         | Statement              |
| $\backslash w *$                | String Literal   | $l$                       | Literal              | $\text{let } x : T ;$                           | Variable Declaration   |
| $\text{true} \mid \text{false}$ | Boolean Literal  | $x$                       | Identifier           | $e ;$                                           | Expression Statement   |
| $T ::=$                         | Type             | $(\bar{p}) \Rightarrow e$ | Function Expression  | $\text{return } e ;$                            | Return Statement       |
| $\text{number}$                 | Numeric Type     | $(e)$                     | Grouped Expression   | $\{\bar{s}\}$                                   | Statement Block        |
| $\text{string}$                 | String Type      | $e_1 ::=$                 | Extension Expression | $\text{function } x(\bar{p}) : T \{ \bar{s} \}$ | Function Definition    |
| $\text{boolean}$                | Boolean Type     | $e \odot e$               | Binary Operator      | $\text{if } (e) \text{ } s \text{ else } s$     | If-Then-Else Statement |
| $(\bar{p}) \Rightarrow T$       | Function Type    | $e(\bar{e})$              | Function Call        | $M ::= \bar{s}$                                 | Program                |
| $p ::= x : T$                   | Typed Identifier | $e.n$                     | Member Access        |                                                 |                        |

Figure 2: The syntax of  $L_B$ . Expressions are categorized into base and extension expressions. The later extends a given expression with suffix operators to form more complicated expressions.

$L^P$  and LLMs’ vocabulary contains all common characters. Therefore, the iterations of the sample-and-check loop is bounded by the size of the vocabulary. In practice, only one or a few iterations are typically needed.

Constrained decoding not only provides token-level guarantees but also ensures the final program’s validity based on  $L$ . This whole-program guarantee can be proved inductively. At L. 1, we start with a valid prefix in  $L^P$ , i.e., either an empty string or a valid prefix provided in the user prompt. The check at L. 6 ensures that all intermediate model outputs remain prefixes in  $L^P$ . Additionally, L. 7 and L. 9 ensure that L. 11 is reached only if  $s \in L$ . In practice, the only other possible outcome is that the generation does not terminate within a predefined time or token limit.

## 2 TYPE CONSTRAINED DECODING

### 2.1 A SIMPLY TYPED LANGUAGE

We define a simply typed, Turing-complete language,  $L_B$ . The syntax of expressions, types, and statements match standard definitions and are a subset of TypeScript (Bierman et al., 2014). It includes expressions, typed declaration statements, type-annotated functions, and flow control. Its complete syntax is shown in Fig. 2 in Extended Backus Naur Form. In the spirit of Bierman et al. (2014), we use a bar to denote Kleene-Plus over repeated elements, i.e.,  $X^+ = \bar{X}$ .

The type system of  $L_B$  matches the type system of TypeScript and other conventional programming languages. Specifically, expressions are typed based on a type environment  $\Gamma$ , a map from identifiers to types. We write  $\Gamma \vdash e : T$  if expression  $e$  has type  $T$  in type environment  $\Gamma$ . The type environment is propagated through consecutive statements, block-scoped and updated by declarations.

A word is valid in  $L_B$  if it (i) is syntactically valid, (ii) adheres to derived types for expressions, and (iii) ensures a value of the indicated return type is returned on every execution path. Detailed syntax and type inference rules are presented in App. D.

### 2.2 PREFIX AUTOMATON DEFINITION

Prefix automata are standard automata that ensure a special *prefix property*<sup>2</sup>. This property enables using the prefix automaton as a completion engine  $CE_L$  to facilitate constrained decoding.

We consider an automaton  $A := \langle \Sigma, Q, \delta, I, F \rangle$ , a tuple of : (i)  $\Sigma$  an alphabet of input symbols; (ii)  $Q$  a set of states; (iii)  $\delta : Q \times \Sigma \mapsto \mathcal{P}(Q)$  a computable transition function mapping to finite sets; (iv)  $I \subseteq Q$  a finite set of initial states; and (v)  $F \subseteq Q$  a decidable set of accepting states. We denote a symbol in  $\Sigma$  as  $c$ , a string of symbols in  $\Sigma^*$  as  $s$ , and an operator for concatenating symbols and strings as  $\circ$ . The transition function  $\delta$  maps a state to all possible subsequent states. When  $\delta$  is applied on a set  $\mathbf{q} \subseteq Q$ , we take the union, i.e.,  $\delta(\mathbf{q}, c) = \bigcup_{q \in \mathbf{q}} \delta(q, c)$ . The transition function defines a directed graph  $G$  over  $Q$ , where every state is a node and there is an edge annotated with  $c$  from  $q$  to  $q'$  iff  $q' \in \delta(q, c)$ . The language parsed by  $A$  comprises all strings  $s$  such that traversing  $G$  from some state in  $I$  along the edges annotated  $c \in s$ , it is possible to reach some state in  $F$ . Formally, we define recursive traversal function  $\gamma$  for states  $\mathbf{q}$  as  $\gamma(\mathbf{q}, \varepsilon) := \mathbf{q}$  and  $\gamma(\mathbf{q}, s \circ c) := \gamma(\delta(\mathbf{q}, s), c)$ . The language accepted by  $A$  is defined as  $L(A) := \{s \mid \gamma(I, s) \cap F \neq \emptyset\}$ . The traversal function has two intuitive properties concerning reachability that can be shown inductively:

<sup>2</sup>Note that the prefix property defined in our work differs from the one discussed in classical texts, e.g., (Hopcroft and Ullman, 1979)

- (P1) A path along the graph can be split arbitrarily, i.e.  $\gamma(\mathbf{q}, s \circ s') = \gamma(\gamma(\mathbf{q}, s), s')$ .  
(P2) If  $s \circ s'$  reaches some state,  $s$  reaches some state, i.e.,  $\gamma(\mathbf{q}, s \circ s') \neq \emptyset \implies \gamma(\mathbf{q}, s) \neq \emptyset$ .

$A$  is a *prefix automaton* if there is a path from every reachable state to some accepting state:

**Definition 2.** For an automaton  $A$ , the prefix property holds iff  $\forall q \in Q : q \in \gamma(I, s) \implies \exists s' : \gamma(q, s') \cap F \neq \emptyset$ . The automaton is a prefix automaton if it satisfies the prefix property.

Intuitively, for such  $A$ , reaching any state through  $s$  implies that  $s$  is prefix to some  $s' \in L(A)$ . The *reachable language* of  $A$ , all inputs that result in any state, is  $L_r(A) := \{s \mid \gamma(I, s) \neq \emptyset\}$ . We see that  $L_r(A)$  is equivalent to  $L(A)^p$ , the prefix language of  $L(A)$  as defined in Def. 1.

**Lemma 1.** If  $A$  is a prefix automaton, then  $L(A)^p = L_r(A)$ .

*Proof.*  $s \in L(A)^p$  implies that there exists  $s'$  such that  $s \circ s' \in L(A)$ , by the definition of prefix languages. This means  $\gamma(I, s \circ s') \neq \emptyset$ . Then, using (P2), we further derive  $\gamma(I, s) \neq \emptyset$ , i.e.,  $s \in L_r(A)$ . Therefore,  $L(A)^p \subseteq L_r(A)$  holds. The other direction also holds. We first see that  $s \in L_r(A) \implies \gamma(I, s) \neq \emptyset$ . Then applying Def. 2 and (P1), we find  $\exists s' : \gamma(I, s \circ s') \cap F \neq \emptyset$ , implying  $s \circ s' \in L(A)$  and thus  $s \in L(A)^p$ .  $\square$

**From Prefix Automata to Completion Engines** With Lem. 1, given a prefix automaton  $A$ , we define a completion engine for  $L(A)$ :  $CE_{L(A)}(s) := \gamma(I, s) \neq \emptyset$ . To use  $A$  to constrain generation to  $L$ , we need to establish a relationship between  $L(A)$  and  $L$ . If  $L(A) \subseteq L$ , we are guaranteed that LLM generations constrained by  $CE_{L(A)}$  lie in  $L$ . Conversely, if  $L(A) \supseteq L$ , we are guaranteed that every  $s \in L$  can be expressed under constrained decoding, but not that all generations are valid. For example, if  $A$  permits syntactically correct programs, it guarantees all well-typed programs can be generated, but permits ill-typed programs. To enforce well-typedness, we thus require  $L(A) \subseteq L$ .

**Building a Prefix Automaton for  $L_B$**  We choose  $\Sigma$  to be the set of Unicode characters, making our completion engine agnostic to LLM vocabularies. When our completion engine is called during constrained decoding at L. 6 of Alg. 1, it processes the sampled token by characters.

Before proceeding, we briefly introduce several base prefix automata below, with their precise definitions detailed in App. E.1. These automata are later combined, with parts of the transition function being overwritten, to construct more complex automata.

- Union  $A_X \cup A_Y$  parses the language  $\{s \mid s \in L(A_X) \cup L(A_Y)\}$ . It is a prefix automaton if both  $A_X$  and  $A_Y$  are prefix automata.
- Concatenation  $A_{XY} = A_X \circ A_Y$  parses the language  $\{s \circ s' \mid s \in L(A_X), s' \in L(A_Y)\}$ . It is a prefix automaton if  $A_X$  and  $A_Y$  are both prefix automata, and  $L(A_Y) \neq \emptyset$ .
- Kleene-Star  $A_{\overline{X}}$  parses the language  $\{\overline{s} \mid s \in L(A_X)\}$ , a prefix automaton if  $A_X$  is a prefix automaton.
- Terminal  $A_S$  parses the language  $\{S\}$ , where  $S$  is a fixed, non-empty string.
- Empty  $A_\emptyset$  parses the empty language  $\emptyset$  and is always a prefix automaton.

### 2.3 PREFIX AUTOMATA FOR IDENTIFIERS, LITERALS, AND TYPES

**Literals** The prefix automaton for literals  $A_l := A_{\text{NUM}} \cup A_{\text{STR}} \cup A_{\text{BOOL}}$  accepts number, string, and boolean literals as defined in Fig. 2. The automata  $A_{\text{NUM}}$ ,  $A_{\text{STR}}$ , and  $A_{\text{BOOL}}$  are defined by the deterministic finite automaton representation of their regular expressions. To ensure the prefix property, we prune states from which accepting states can not be reached.

**Identifiers** During parsing, we maintain the current type environment  $\Gamma$ . We define the identifier automaton  $A_x$  as the union of the terminal automata for identifiers defined in  $\Gamma$ ,  $A_x := \bigcup_{y \in \Gamma} A_y$ .

**Types** The type automaton  $A_T$  accepts type annotations. It is defined as  $A_T := A_{\text{TYPE-LIT}} \cup A_{\text{TYPE-FUN}}$ , including type literal automaton  $A_{\text{TYPE-LIT}} := A_{\text{string}} \cup A_{\text{number}} \cup A_{\text{boolean}}$  and function type automaton  $A_{\text{TYPE-FUN}} := A_{(\overline{p}) \Rightarrow T}$ . The latter is a concatenation of multiple prefix automata, with the parameter and return types recursing on  $A_T$ . This recursive definition is valid, since it ensures a finite set of initial states, defines a decidable accepting set, and preserves the prefix property.

## 2.4 PREFIX AUTOMATON FOR EXPRESSIONS

**Unrestricted Expressions** We differentiate two kinds as shown in Fig. 2: *Base expressions*; identifiers, literals, grouped expressions, and anonymous functions, and *extension expressions*; operator applications (binary operator, member access, or function call) that extend a given expression.

The expression automaton  $A_e$  is the union of base expression automata  $A_x$ ,  $A_l$ ,  $A_{(e)}$ , and  $A_{(\bar{p}) \Rightarrow e}$ , with potential extensions  $A_{\odot e}$ ,  $A_{.n}$ , and  $A_{(\bar{e})}$ . The base and extension automata are constructed by concatenating the respective terminal automata and recursively  $A_e$ . Additionally, we restrict the type of the recursive  $A_e$  if required by the type system. We provide additional detail on the implementation in App. E.2. Since an expression can end after base and extensions, accepting states of both base and extending automata are accepting states of  $A_e$ . To implement extensions in the transition function  $\delta_e$ , we start from the base expression automata and adjust  $\delta_e$  with outgoing edges from accepting states to the initial states of the extending automata, formally:

$$\forall X, Y : \delta_e(q_Y^X, c) := \begin{cases} \delta_Y(q_Y^X, c) \cup \delta_e(I_{(\bar{e})}^X, c) \cup \delta_e(I_{\odot e}^X, c) \cup \delta_e(I_{.n}^X, c) & \text{if } q_Y^X \in F_Y \\ \delta_Y(q_Y^X, c) & \text{otherwise,} \end{cases}$$

where the labels  $X$  and  $Y$  for a state  $q_Y^X$  represent that a string  $X$  has been parsed, and currently the active automaton is  $A_Y$ , one of  $A_x$ ,  $A_l$ ,  $A_{\odot e}$ , etc. The superscripts are leveraged to determine the validity of extensions and transition to type-restricted expressions based on  $L_B$ 's typing rules. In general, we set  $I_Y^X := \emptyset$  when  $Y$  is an invalid extension to  $X$ . Our definition of  $A_e$  is valid, as  $\delta_e$  is computable,  $I_e$  is finite and  $F_e$  is decidable.

**Type-Constrained Expressions** To implement  $A_e \downarrow T$ , we must determine whether a partial expression  $s$  can be completed to inhabit type  $T$ . Completing  $s$  may express different types, and repeated extensions can alter the result type, but do not guarantee that the desired type can be expressed. However, extensions can be applied indefinitely, prohibiting an exhaustive enumeration.

We therefore develop a two-tiered algorithm. It first identifies *derivable types*  $\text{DERIVABLE}(q_s)$  of  $s$ , inhabitable without extensions, based on its current state  $q_s$ . Second, a *type reachability search*  $\text{REACHABLE}(\text{DERIVABLE}(q_e), T)$  determines if  $T$  can be inhabited by extending from the derivable types of  $s$ . We prune automaton transitions when this type search returns a negative result.

Table 1: Definition of  $\text{DERIVABLE}(x)$  for partial expressions in Fig. 2.  $s \leq s'$  means  $s$  is a prefix of  $s'$ .  $\text{pmatch}(s, T)$  returns whether prefix  $s$  partially matches regular expression of literals of type  $T$ .

| $s$                       | $\text{DERIVABLE}(q_s)$                                                                  |
|---------------------------|------------------------------------------------------------------------------------------|
| $l$                       | $\{T \mid \text{pmatch}(l, T), T \in \{\text{number}, \text{string}, \text{boolean}\}\}$ |
| $x$                       | $\{T \mid x \leq n, (n : T) \in \Gamma\}$                                                |
| $(\bar{p}) \Rightarrow e$ | $\{(\bar{p}) \Rightarrow T \mid \text{REACHABLE}(\text{DERIVABLE}(q_e), T)\}$            |
| $(e$                      | $\{T \mid \text{REACHABLE}(\text{DERIVABLE}(q_e), T)\}$                                  |
| $e \odot$                 | $\{T \mid \exists S' : \Gamma \vdash e : S \wedge S \odot S' : T\}$                      |
| $e($                      | $\{R \mid \Gamma \vdash e : (\bar{p}) \Rightarrow R\}$                                   |
| $e.a$                     | $\{S \mid a \leq n, \Gamma \vdash e : T, \text{LOOKUP}(T, n) = S\}$                      |

**Derivable Types** For  $\text{DERIVABLE}$ , we enumerate all types inhabitable by the currently parsed expression  $s$  without extension. For a final state  $q$  of expression  $e$ , we define  $\text{DERIVABLE}(q) := T$ , where  $\Gamma \vdash e : T$ . We implement the unique derivability rules of expressions, detailed in Tab. 1. Note that for grouped expressions and function literals, we need to enumerate reachable types by recursively contained expressions. To avoid explicitly enumerating all reachable types, we integrate the derivability and reachability algorithms, discussed in more detail in App. E.4.

**Lemma 2.** For state  $q \in r(I_e, s)$  of partial expression  $s$ ,  $\text{DERIVABLE}(q)$  returns all  $T$  s.t. exists some suffix  $s'$  with  $\Gamma \vdash s \circ s' : T$  and  $s'$  does not involve an extension.

**Type Reachability** To determine which types are inhabitable by extending a base expression  $e$  of type  $T$ , we analyze sequences of extensions with compatible signatures. This process is conceptualized as a search over a graph where types as nodes and extension steps are edges. For binary operator  $\odot$  with signature  $T \odot X : S$ , an edge is created from type  $T$  to type  $S$ . As an example, the operator for numerical addition  $+$  has the signature  $\text{number} + \text{number} : \text{number}$ , thereby forming an edge from  $\text{number}$  to itself. Furthermore, for every member  $n$  of type  $T$ , we create an edge from  $T$  to  $\text{LOOKUP}(T, n)$ . Finally, we connect  $T$  and  $R$  for each function with type  $T = (\bar{p}) \Rightarrow R$ . Note that these steps are *abstract*, i.e., they focus on the expression types, disregarding textual representation.

The type reachability algorithm, Alg. 2, implements a depth-first search over this type graph. It starts from current type  $T$ , succeeding upon finding goal type  $G$  (L. 2), marking any visited types to prevent cycles (L. 3). It then iterates over valid extensions (L. 4) and computes the result type  $S$  of the extension (L. 5). At L. 7, we proceed to recursively search  $G$  can be reached from  $S$ . If all recursive calls are unsuccessful, the goal type  $G$  can not be reached (L. 8).

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**Algorithm 2** Type reachability search

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**Input:** Current type  $T$  of expression  $e$ , goal type  $G$   
**Output:** Whether  $G$  can be reached by extending  $e$ .  
1: **function** REACHABLE( $T, G$ )  
2:   **if**  $T = G$  **then return** true  
3:   **if**  $T$  is marked **then return** false **else** mark  $T$   
4:   **for each** valid extension step  $\diamond$  from  $T$  **do**  
5:      $S \leftarrow$  the resulting type of applying  $\diamond$  on  $T$   
6:     **if** PRUNESearch( $T, G, S$ ) **continue**  
7:     **if** REACHABLE( $S, G$ ) **return** true  
8:   **return** false

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Some programming languages define self-referential default members, e.g., `clone` in Java or `valueOf` in TypeScript, nullary functions returning the type of the callee,  $() \Rightarrow T$  for  $T$ . When these members are accessed in functions, higher-order functions can be derived indefinitely. We therefore need to restrict the type search to a finite set of types to ensure termination. At L. 6 of Alg. 2, we use heuristic PRUNESearch to restrict the search. We develop simple heuristic based on Gvero et al. (2013) to prune exploration of types with higher complexity than goal or source type, if they do not contain yet unexplored primitive types. We detail this heuristic in App. E.3. While ensuring termination, the heuristic leads to incompleteness and the potential rejection of well-typed expressions. However, in practical usage, only highly complex (thus less used) types are avoided.

**Lemma 3.** *The type search in Alg. 2 is sound, i.e., for any expression  $e$  with  $\Gamma \vdash e : T$ , if REACHABLE( $T, G$ ) holds, then there exists a sequence of extensions  $y$  such that  $\Gamma \vdash e \circ y : G$ .*

Note that any pruning heuristic at L. 6 of Alg. 2 preserves soundness, which is sufficient to preserve the prefix property of  $A_e \downarrow T$ . We conclude from Lems. 2 and 3 that  $A_e \downarrow T$  and  $A_e$  are prefix automata that parse a subset of well-typed expressions in  $L_B$ .

**Corollary 1.** *If REACHABLE(DERIVABLE( $q$ ),  $G$ ) holds for any  $q \in \gamma(I_e, s)$  of a partial expression  $s$ , then there exists a suffix  $s'$  such that  $\Gamma \vdash s \circ s' : G$ .*

**Lemma 4.** *The language parsed by  $A_e \downarrow T$  is thus a subset of the expressions of  $L_B$  of type  $T$ , i.e.,  $L(A_e \downarrow T) \subseteq \{s \mid \Gamma \vdash s : T\}$ . Since  $A_e$  recursively involves  $A_e \downarrow T$ , the language parsed by  $A_e$  is also a subset of well-typed expressions of  $L_B$ , i.e.,  $L(A_e) \subseteq \{s \mid \exists T : \Gamma \vdash s : T\}$ .*

## 2.5 PREFIX AUTOMATA FOR STATEMENTS

The statement automaton is defined recursively as  $A_s := A_{\text{DECL}} \cup A_{\text{EXPR}} \cup A_{\text{RET}} \cup A_{\text{BLOCK}} \cup A_{\text{FUN}} \cup A_{\text{ITE}}$ . The declaration automaton  $A_{\text{DECL}} := A_{\text{let } x : T}$  captures undefined variable names  $x$  by accepting all strings, except for existing identifiers. It is a prefix automaton as an accepting state can be reached by appending characters.  $A_{\text{RET}}$  is  $A_{\emptyset}$  when outside a function and otherwise restricts the parsed expression to the return type of the surrounding function. The remaining automata are mainly concatenations of previous automata and  $A_s$ , with small variations detailed in App. E.5.

**Guaranteeing Return Types** When parsing function bodies, the transition function of  $A_{\text{FUN}}$  maintains information about the declared return type and encountered return statements (if any).  $A_{\text{FUN}}$  only accepts when all return values match the declared return type, and all execution paths in the function body return, as in Fig. 8. Otherwise, another statement generation is forced. The prefix automaton property is preserved as we can always express a correct return statement using literals.

The described rules are implemented without violating the prefix property by deriving restrictions from already parsed input and ensuring completion is possible. We conclude that  $A_s$  is a prefix automaton. Moreover,  $A_s$  accepts all valid statements of  $L_B$ , excluding expressions rejected by  $A_e$ .

**Lemma 5.** *With  $A_{L_B} := A_{\bar{s}}$  it holds that  $A_{L_B}$  is a prefix automaton and  $L(A_{L_B}) \subseteq L_B$*

## 3 EXPERIMENTAL EVALUATION

We outline our evaluation setup, with further details and hyperparameters discussed in App. G.

**Tasks and Benchmarks** We evaluate on three relevant tasks of code generation: (i) *Synthesis*: Given a natural language task, generate a solution from scratch. (ii) *Translation*: Given a Python

Table 2: Number of instances with compiler errors in unconstrained generation (Vanilla), idealized syntax-only constraining (Syntax), and our proposed type constraining (Types). On average, type constraining reduces compiler errors by 75.3% in synthesis, compared to only 9.0% through Syntax.

| Model         | Synthesis |                       |                              | Translation |                        |                              | Repair  |                       |                               |
|---------------|-----------|-----------------------|------------------------------|-------------|------------------------|------------------------------|---------|-----------------------|-------------------------------|
|               | Vanilla   | Syntax                | Types                        | Vanilla     | Syntax                 | Types                        | Vanilla | Syntax                | Types                         |
| Gemma 2 2B    | 103       | 92 $\downarrow$ 10.7% | <b>44</b> $\downarrow$ 57.3% | 177         | 149 $\downarrow$ 15.8% | <b>80</b> $\downarrow$ 54.8% | 194     | 181 $\downarrow$ 6.7% | <b>103</b> $\downarrow$ 46.9% |
| Gemma 2 9B    | 45        | 41 $\downarrow$ 8.9%  | <b>13</b> $\downarrow$ 71.1% | 75          | 63 $\downarrow$ 16.0%  | <b>16</b> $\downarrow$ 78.7% | 113     | 108 $\downarrow$ 4.4% | <b>52</b> $\downarrow$ 54.0%  |
| Gemma 2 27B   | 15        | 13 $\downarrow$ 13.3% | <b>2</b> $\downarrow$ 86.7%  | 20          | 20 $\downarrow$ 0.0%   | <b>3</b> $\downarrow$ 85.0%  | 45      | 40 $\downarrow$ 11.1% | <b>22</b> $\downarrow$ 51.1%  |
| DS Coder 33B  | 26        | 25 $\downarrow$ 3.8%  | <b>5</b> $\downarrow$ 80.8%  | 18          | 17 $\downarrow$ 5.6%   | <b>7</b> $\downarrow$ 61.1%  | 36      | 36 $\downarrow$ 0.0%  | <b>15</b> $\downarrow$ 58.3%  |
| CodeLlama 34B | 86        | 71 $\downarrow$ 17.4% | <b>28</b> $\downarrow$ 67.4% | 158         | 124 $\downarrow$ 21.5% | <b>59</b> $\downarrow$ 62.7% | 153     | 142 $\downarrow$ 7.2% | <b>48</b> $\downarrow$ 68.6%  |
| Qwen2.5 32B   | 17        | 17 $\downarrow$ 0.0%  | <b>2</b> $\downarrow$ 88.2%  | 24          | 21 $\downarrow$ 12.5%  | <b>5</b> $\downarrow$ 79.2%  | 36      | 34 $\downarrow$ 5.6%  | <b>13</b> $\downarrow$ 63.9%  |

function, generate an equivalent TypeScript function. (iii) *Repair*: Given a natural language task, a non-compilable solution and compiler error, restore functionality of the flawed solution.

The tasks are sourced from the TypeScript translated HumanEval (Chen et al., 2021) subset of MultiPL-E (Cassano et al., 2023), containing 159 instances. To obtain more comprehensive results, we evaluate 4 times with different seeds and aggregate the outcomes. For Repair, we collect non-compiling programs from unconstrained synthesis for all models, resulting in 292 instances.

**Models and Methods** We use 6 different open-weight LLMs, covering 3 LLMs of varying parameter sizes from the same model family and 4 models of a similar size from different model families: the Gemma 2 model family with 2B/9B/27B parameters (Team et al., 2024), DeepSeek Coder 33B (Guo et al., 2024), CodeLlama 34B (Rozière et al., 2023), and Qwen2.5 32B (Yang et al., 2024). We always choose the instruction-tuned variants to ensure adherence to the natural language task.

Unconstrained LLM sampling is reported as *Vanilla*. We measure the upper bound improvement of syntactic constraining (*Syntax*) where all Syntax errors in Vanilla instances are considered resolved. We separately sample using type-constrained decoding (*Types*) based on §2. We emulate type constraining with the entire TypeScript feature set. Concretely, if a sample compiles correctly without any constraining, we report it as-is. Otherwise, we report the result of the constrained sample.

**Metrics** We compute two main metrics to assess the effectiveness of the compared methods. First, we determine *compiler errors*, any case in which the TypeScript compiler (Microsoft, 2024) reports an issue. To measure *functional correctness*, we leverage the pass@1 metric (Chen et al., 2021), measuring the percentage of generations that pass provided unit tests given only one trial.

### 3.1 RESULTS ON COMPILATION AND FUNCTIONAL CORRECTNESS

**Reduction of Compilation Errors** In Tab. 5, we present the number of compilation errors. For synthesis and translation, Syntax could resolve 9.0% and 11.9% of the non-compiling instances. In contrast, Types reduces compilation errors by 75.3% and 70.2%. We observe that all models and tasks benefit similarly from our constraining, with a minimum error reduction of 54.8%.

For Repair, we find that many models struggle to correctly localize and resolve compilation errors, with Gemma 2 2B for example repairing only 33.5% of the non-compiling instances in Vanilla. This is substantially increased to 56.4% in Types. On average, using type-constrained sampling, 57.1% more compilation errors are resolved than using vanilla LLM decoding.

**Improving Functional Correctness** Programs that do not compile are always considered functionally incorrect. With our type constraining, non-compilable generations can be turned into well-formed ones. In Tab. 6, we experimentally show that type constraining universally improves functional correctness. Employing type constraining improves LLMs’ pass@1 rate, achieving an increase by 3.5%, 4.5% in synthesis and translation respectively, and 34.1% in repair tasks.

**Overhead of Type Constraining** For an application of our method in practice, the effective runtime increase due to constrained decoding is highly relevant. To assess it, we measure the runtime per synthesis instance. We report the median runtime per instance for Types and its relative increase

Table 3: pass@1 of unconstrained generation (Vanilla) and type constraining (Types). The benefit of our type-constraining transfers from reduced compilation errors to improved functional correctness.

| Model         | Synthesis |             | Translation |             | Repair  |             |
|---------------|-----------|-------------|-------------|-------------|---------|-------------|
|               | Vanilla   | Types       | Vanilla     | Types       | Vanilla | Types       |
| Gemma 2 2B    | 29.1      | <b>30.2</b> | 50.2        | <b>53.9</b> | 11.6    | <b>20.9</b> |
| Gemma 2 9B    | 56.6      | <b>58.3</b> | 73.7        | <b>78.3</b> | 24.0    | <b>34.9</b> |
| Gemma 2 27B   | 69.5      | <b>71.2</b> | 86.6        | <b>87.7</b> | 38.4    | <b>41.1</b> |
| DS Coder 33B  | 68.9      | <b>71.1</b> | 88.7        | <b>90.1</b> | 47.6    | <b>50.7</b> |
| CodeLlama 34B | 41.0      | <b>43.4</b> | 58.6        | <b>63.5</b> | 17.5    | <b>27.4</b> |
| Qwen2.5 32B   | 79.6      | <b>81.8</b> | 92.1        | <b>93.9</b> | 65.4    | <b>71.2</b> |

Table 4: Median time per synthesis instance in seconds spent by Types and its relative increase to Vanilla.

| Model         | Overhead              |
|---------------|-----------------------|
| Gemma 2 2B    | 6.7 $\uparrow$ 38.3%  |
| Gemma 2 9B    | 8.3 $\uparrow$ 29.2%  |
| Gemma 2 27B   | 11.7 $\uparrow$ 19.9% |
| DS Coder 33B  | 11.5 $\uparrow$ 36.2% |
| CodeLlama 34B | 7.6 $\uparrow$ 40.8%  |
| Qwen2.5 32B   | 7.3 $\uparrow$ 39.6%  |

to Vanilla in Tab. 7. On average over the evaluated models, we observe a relative increase of 34.0%. We note our implementation is not optimized or systems-oriented such as Dong et al. (2024).

**MBPP, Case Study and Discussion in Appendix** We provide results on MBPP (Austin et al., 2021) in App. A, a case study of our constraints in App. B and a discussion of our work in App. C.

## 4 RELATED WORK

**Code Language Models** Recently, LLMs have gained traction for diverse coding tasks (Jiang et al., 2024). LLMs are typically trained on trillion token datasets and have billions of parameters, both factors contributing to improved performance in code-related benchmarks (Rozière et al., 2023; Team et al., 2024; Guo et al., 2024). Meanwhile, even SOTA LLMs are well known to frequently make mistakes (Rawte et al., 2023; Huang et al., 2023), including code errors, as we showed.

**Improving Language Model Accuracy** Apart from constrained decoding, three primary approaches have been proposed to enhance the accuracy of language models on code tasks: fine-tuning, retrieval augmentation (RAG), and compiler or execution feedback. Fine-tuning adapts the model weights based on specifically collected training data (Tsai et al., 2024; Weyssow et al., 2023). RAG provides additional context based on databases or related code snippets (Bassamzadeh and Methani, 2024; Poesia et al., 2022). Feedback is only available after completed generation and requires re-sampling (Jana et al., 2024; Deligiannis et al., 2025; Wei et al., 2023). Constrained decoding is orthogonal to these, and, as indicated by Poesia et al. (2022) and our experimental results, combining constrained decoding with RAG or compiler feedback additionally improves model performance.

**Constrained Decoding** Prior work on constrained decoding failed to achieve strong results due to its limitation to syntactic language features. Constraining to context-free languages has been explored extensively (Beurer-Kellner et al., 2024; Poesia et al., 2022; Beurer-Kellner et al., 2023; Willard and Louf, 2023). Simple context-sensitive syntactic features, such as the space indentation in Python have been implemented (Melcer et al., 2024; Ugare et al., 2024). However, the rarity of syntax errors significantly reduces the potential of leveraging syntax for code correctness.

**Type Systems for Code Synthesis** Prior work that leveraged type systems for code synthesis was confined to specialized settings and unable to constrain general, complex program generation. Poesia et al. (2022) used column names to guide SQL query synthesis. Gvero et al. (2013) employed a search on the type graph for function call completion. Agrawal et al. (2023) leverage language-server-generated type annotations for object member accesses. Type constraints have also been used to direct code synthesis in specialized search procedures (Wei et al., 2023; Fiala et al., 2023; Perelman et al., 2012). However, these methods are not compatible with LLM-based code generation.

## 5 CONCLUSION

In this work, we explored how type systems in programming languages can be used to guide language models during decoding. We design and implement prefix automata to perform type constraining and implement it for TypeScript. We evaluate its impact on code synthesis, translation, and repair and observe significant reduction of compilation and functional errors.

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Table 5: Number of MBPP instances with compiler errors in unconstrained generation (Vanilla), idealized syntax-only constraining (Syntax), and our proposed type constraining (Types). Types constraining reduces compiler errors by 52.1% in synthesis, compared to only 4.9% through Syntax.

| Model         | Synthesis |                       |                              | Translation |                        |                              | Repair  |                       |                               |
|---------------|-----------|-----------------------|------------------------------|-------------|------------------------|------------------------------|---------|-----------------------|-------------------------------|
|               | Vanilla   | Syntax                | Types                        | Vanilla     | Syntax                 | Types                        | Vanilla | Syntax                | Types                         |
| Gemma 2 2B    | 67        | 64 $\downarrow$ 4.5%  | <b>27</b> $\downarrow$ 59.7% | 126         | 111 $\downarrow$ 11.9% | <b>79</b> $\downarrow$ 37.3% | 194     | 184 $\downarrow$ 5.2% | <b>108</b> $\downarrow$ 44.3% |
| Gemma 2 9B    | 30        | 29 $\downarrow$ 3.3%  | <b>10</b> $\downarrow$ 66.7% | 67          | 61 $\downarrow$ 9.0%   | <b>33</b> $\downarrow$ 50.7% | 129     | 124 $\downarrow$ 3.9% | <b>63</b> $\downarrow$ 51.2%  |
| Gemma 2 27B   | 20        | 19 $\downarrow$ 5.0%  | <b>7</b> $\downarrow$ 65.0%  | 37          | 36 $\downarrow$ 2.7%   | <b>22</b> $\downarrow$ 40.5% | 71      | 69 $\downarrow$ 2.8%  | <b>32</b> $\downarrow$ 54.9%  |
| DS Coder 33B  | 32        | 32 $\downarrow$ 0.0%  | <b>19</b> $\downarrow$ 40.6% | 29          | 27 $\downarrow$ 6.9%   | <b>13</b> $\downarrow$ 55.2% | 90      | 90 $\downarrow$ 0.0%  | <b>43</b> $\downarrow$ 52.2%  |
| CodeLlama 34B | 80        | 71 $\downarrow$ 11.2% | <b>41</b> $\downarrow$ 48.8% | 126         | 114 $\downarrow$ 9.5%  | <b>54</b> $\downarrow$ 57.1% | 157     | 148 $\downarrow$ 5.7% | <b>76</b> $\downarrow$ 51.6%  |
| Qwen2.5 32B   | 19        | 18 $\downarrow$ 5.3%  | <b>13</b> $\downarrow$ 31.6% | 22          | 22 $\downarrow$ 0.0%   | <b>16</b> $\downarrow$ 27.3% | 55      | 52 $\downarrow$ 5.5%  | <b>29</b> $\downarrow$ 47.3%  |

Table 6: MBPP pass@1 of unconstrained generation (Vanilla) and type constraining (Types). We observe a similar transfer of improvements as in HumanEval.

| Model         | Synthesis |             | Translation |             | Repair  |             |
|---------------|-----------|-------------|-------------|-------------|---------|-------------|
|               | Vanilla   | Types       | Vanilla     | Types       | Vanilla | Types       |
| Gemma 2 2B    | 40.4      | <b>42.4</b> | 52.3        | <b>56.0</b> | 12.1    | <b>22.6</b> |
| Gemma 2 9B    | 65.4      | <b>67.4</b> | 71.4        | <b>75.8</b> | 24.2    | <b>31.9</b> |
| Gemma 2 27B   | 70.6      | <b>72.1</b> | 83.1        | <b>84.4</b> | 39.1    | <b>45.2</b> |
| DS Coder 33B  | 65.4      | <b>67.2</b> | 85.9        | <b>89.1</b> | 35.1    | <b>43.1</b> |
| CodeLlama 34B | 42.2      | <b>45.6</b> | 55.7        | <b>63.3</b> | 15.7    | <b>26.6</b> |
| Qwen2.5 32B   | 76.3      | <b>76.6</b> | 89.6        | <b>90.4</b> | 48.0    | <b>54.0</b> |

Table 7: Median time per synthesis instance in seconds spent by Types and its relative increase to Vanilla on MBPP.

| Model         | Overhead              |
|---------------|-----------------------|
| Gemma 2 2B    | 6.3 $\uparrow$ 35.4%  |
| Gemma 2 9B    | 9.5 $\uparrow$ 46.8%  |
| Gemma 2 27B   | 11.7 $\uparrow$ 32.8% |
| DS Coder 33B  | 9.4 $\uparrow$ 59.5%  |
| CodeLlama 34B | 7.0 $\uparrow$ 37.6%  |
| Qwen2.5 32B   | 4.9 $\uparrow$ 54.8%  |

## A EXPERIMENTAL EVALUATION ON MBPP

We outline our experiment on MBPP (Austin et al., 2021), mirroring the main experiment on HumanEval, with the same tasks, methods, models and metrics as in §3.

**Dataset** The instances are based on TypeScript-translated MBPP tasks (Austin et al., 2021), contained in the MultiPL-E dataset (Cassano et al., 2023), with 384 instances each. Contrasting our main experiments, in MBPP, we generate each sample once. For Repair, we collect all non-compiling programs from the unconstrained synthesis task for all models, resulting in 248 instances.

### A.1 RESULTS ON COMPILATION AND FUNCTIONAL CORRECTNESS

**Reduction of Compilation Errors** In Tab. 5, we present the number of compilation errors. For synthesis and translation, Syntax could improve 4.9% and 6.7% of the non-compiling instances respectively. In contrast, Types reduces compilation errors by 52.1% and 44.7%. We observe that models across all sizes and families benefit similarly from our constraining, with a minimum error reduction of 27.3%.

For Repair, we again find that many models struggle to correctly localize and resolve compilation errors, with Gemma 2 2B for example repairing only 31.6% of the non-compiling instances in Vanilla. This is substantially increased to 58.5% in Types. On average, using type-constrained sampling, 50.3% more compilation errors are resolved than using vanilla LLM decoding.

**Improving Functional Correctness** Programs that do not compile are always considered functionally incorrect. With our type constraining, non-compilable generations can be turned into well-formed ones. In Tab. 6, we experimentally show that type constraining universally improves functional correctness. Employing type constraining improves LLMs’ pass@1 rate, achieving an increase by 3.6%, 5.5% in synthesis and translation respectively, and 39.8% in repair tasks.

**Overhead of Type Constraining** For an application of our method in practice, the effective runtime increase due to constrained decoding is highly relevant. To assess it, we measure the runtime per synthesis instance. We report the median runtime per instance for Types and its relative increase

to Vanilla in Tab. 7. On average over the evaluated models, we observe a relative increase of 44.5%. We note our implementation is not optimized or systems-oriented such as Dong et al. (2024).

### Number of Sample-and-Check Loop Iterations

To provide an in-depth analysis of the overhead of our type constraining method, we measure the number of iterations spent by the sample-and-check loop to find an admissible token. The results are provided in Fig. 3. We observe that the number of loop iterations follows a long-tail distribution. For 99.5% of cases, only one loop iteration is needed. This number is similar for stronger models, with Gemma 2 9B and 27B requiring one iteration in 99.2% and 99.7% of cases, respectively. This means that, in most instances, LLMs can generate a valid token on the first attempt, which is then verified by the completion engine. In cases where more than one iteration is needed, the completion engine intervenes to guide the selection of valid tokens. These interventions help resolve errors in many instances in our benchmarks, providing significant benefit, as discussed in App. A.1.

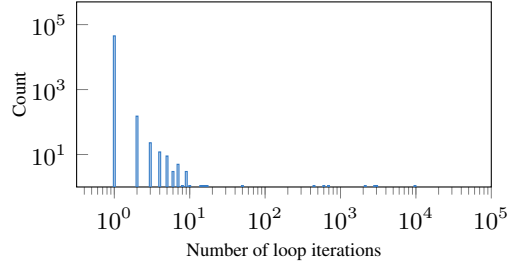


Figure 3: Histogram on the number of iterations consumed by the sample-and-check loop at L. 4 of Alg. 1 to find a valid token, measured with Gemma 2 2B for MBPP synthesis.

Prior work (Ugare et al., 2024; Beurer-Kellner et al., 2024; Poesia et al., 2022) implemented constrained decoding differently than Alg. 1. Instead of running the sample-and-check loop, they execute the completion engine for all tokens in the LLM’s vocabulary, mask out all invalid tokens, and sample once from the remaining valid tokens based on their normalized likelihoods. This implementation is less efficient than ours, especially when calling the completion engine is costly. Based on the long-tail distribution depicted in Fig. 3, our implementation requires only a single invocation to the completion engine for most cases, whereas their implementation calls it for every token in the LLM’s vocabulary for all cases. In our experiments, their implementation results in timeouts for all benchmark instances, with a timeout of 5 minutes per instance. This justifies our choice of using the sample-and-check loop.

## B CASE STUDY

For a qualitative evaluation, we manually inspect instances where unconstrained decoding fails and our type constraining approach successfully corrects errors. We find that our technique effectively amends various types of compilation errors. We showcase three such examples in Fig. 4 (shortened for brevity), with full outputs provided in App. H.

**Wrong Parameter Count** In Fig. 4a, the task is to find all words in a string that contain a number of consonants. When Gemma 2 2B attempts to solve this problem, translating from the Python version to TypeScript, it calls `split` without arguments. This is allowed in Python, but not in TypeScript, where a single `string` argument is required. Type constraining correctly detects this and guides the generation to sample a space character as parameter.

**Missing Return Statement** In Fig. 4b, to complete function `largest_divisor`, the model must compute a straightforward divisor loop. DeepSeek Coder 33B Instruct (Guo et al., 2024) implements a correct loop, but does not guarantee returning a value in every execution path. When the return statement in the loop is never executed, e.g., for negative inputs, the function thus returns `undefined`, violating the type rules. Our method detects this issue and forces the generation of another statement in the function body, resulting in a correct fallback return statement.

**Incorrect Type Inference** This example is shown in Fig. 4c. The task is to insert a delimiter between every element in an array. Gemma 2 9B solves this using the `reduce` function. This generic function accepts two arguments; the first argument is a callback function that is called consecutively for every element in the array and accumulates a result, the second argument is an initial value for the callback function. The type of the accumulator of the callback function is derived implicitly from the type of the second argument. In the given example, the second argument is an empty array,

|     | Vanilla                                                                                                                                                      | Types                                                                                                                                                                 |
|-----|--------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| (a) | <pre>// find all words with consonants function select_words(s: string): string[] {   for (const word of s. <b>split()</b>)</pre>                            | <pre>// find all words with consonants function select_words(s: string): string[] {   for (const word of s. <b>split(' ')</b>)</pre>                                  |
| (b) | <pre>function largest_divisor(n: number): number {   for(let i = n - 1; i &gt; 0; i--) {     if(n % i === 0) return i;   }   <b>// No return</b> }</pre>     | <pre>function largest_divisor(n: number): number {   for(let i = n - 1; i &gt; 0; i--) {     if(n % i === 0) return i;   }   <b>return 1;</b> }</pre>                 |
| (c) | <pre>// insert a delimiter between every element return nums.reduce(   (<b>acc</b>, curr, index) =&gt; {     acc.push(curr);     return acc;   }, []);</pre> | <pre>// insert a delimiter between every element return nums.reduce(   (<b>acc: number[]</b>, num, index) =&gt; {     acc.push(curr);     return acc;   }, []);</pre> |

Figure 4: Three examples illustrating for the effect of type-constrained sampling. Left are unconstrained generations with problematic tokens highlighted in **red**, and right are type-constrained results with corrected tokens highlighted in **green**, adapted for clarity. In (a), Gemma 2 2B attempts to call `split`, missing required arguments. In (b), DeepSeek Coder 33B attempts to complete a function without a guaranteed return. The issue is resolved by forcing generation of another statement after the main loop. In (c), Gemma 2 9B calls `reduce` with an anonymous function without type annotation. This leads to an incorrect type inference for the first parameter. The issue is solved by guiding the model to add type annotation.

which should collect the new outputs. However, TypeScript infers a special type `never[]` for the empty array, disallowing pushing the number array elements into the array. As a result, the program fails to compile. This inference is a well-known problem and a limitation of the TypeScript compiler that often confuses even expert developers (Various, 2024; nop33, 2024). Our method resolves the issue by enforcing adequate type annotation on the first argument of the callback function.

## C DISCUSSION

Our general type constraining approach, backed by strong experimental results, opens exciting avenues for future research, which we discuss below.

**Remaining Compiler Errors** We observe that, even though constrained decoding guarantees a valid result upon termination, a considerable amount of compilation errors remain due to non-termination within the given token or time limit. We find this to be caused by generation loops, entered when generation is forced to comply with a constraint and the LLM is unable to recover. An example is depicted in Fig. 5, where CodeLlama 34B tries to access the invalid member `sort` on an expression of type `number`. Future work may add additional constraints to force stopping such unconstructive loops and steer the model more strictly, e.g., by limiting the complexity of generated expressions.

**Implementation Effort** Developing a completion engine for a target programming language currently requires manual efforts. However, we expect that the involved effort to adopt our method to other languages will be reduced significantly, as many features transfer from our implementation for  $L_B$  and TypeScript. Moreover, we believe that, due to the huge impact of LLMs on code generation, the effort will pay off. Future programming language developers may consider generally writing their compilers as an incremental completion engine, which additionally enables automatic adoption for constrained code generation, besides conventional grammar parsing and type checking.

**Broader Application to More Complex Tasks and Stronger LLMs** Stronger LLMs, such as the latest OpenAI models (Jaech et al., 2024), may make fewer typing errors on the HumanEval and MBPP datasets. Our evaluation results in Tab. 5 also demonstrate that compilation errors decrease with increasing model size for the Gemma family. However, recent findings showed that currently, even the strongest LLMs struggle with generating compilable code for more complex coding tasks, stricter typing rules, and low-resource languages (e.g., newly invented DSLs). Gu-

```

1 function sort_third(l: number[], r: number[]): number[] {
2   for (let i = 0; i < l.length; i++) {
3     r.push(l[i].toString()).slice(0, 3).concat(l[i].toString().slice(3).split(''))
4     .reverse().join('')).split('').reverse().join('').toString() + l[i] ...

```

Figure 5: Compilations errors remain when the model does not terminate after a corrected token. In this example for synthesis on the HumanEval task #33, CodeLlama 34B is steered away from accessing non-existing member `.sort` and instead accesses `.toString`.

sanidas ([n. d.]) evaluated various state-of-the-art LLMs on difficult code synthesis tasks in Rust, reporting compilation error rates of 18% for OpenAI o1-mini (Jaech et al., 2024), 39% for DeepSeek R1 (DeepSeek-AI et al., 2025) and 27% for Anthropic’s Claude 3.5 Sonnet (Anthropic, [n. d.]). For OCaml and Haskell, which are sparsely represented in LLMs’ training data, the error rate is even higher at 40% – 60% for all models, matching a trend of worse performance on low-resource languages (Joel et al., 2024; Giagnorio et al., 2025). Pan et al. (2024b) compiled a large dataset of code translation and found 44.3% of GPT-4-generated code to contain compilation errors. Similarly, Shetty et al. (2024) report around 25% compilation errors for C-to-Rust translation using OpenAI o1 models. Our type constraining approach is broadly applicable to all these scenarios. Future work can consider extending our approach to address these challenges.

Constrained decoding in general requires access to the next-token probability distributions produced by LLMs. Currently, commercially available black-box LLM APIs only return sampled tokens and do not offer complete next-token distributions. A possible solution is to integrate our method into the backend of model providers, as was recently implemented for guaranteeing adherence to JSON Schemas (Anthropic, 2025; OpenAI, 2025).

## D A SIMPLY TYPED LANGUAGE

We define a simply typed, Turing-complete language,  $L_B$ . Its grammar and type system are generic, resembling the principles found in popular statically typed languages, such as TypeScript, Java, and Go. However, there may be a slight bias towards TypeScript, as our implementation is based on it.

**Syntax** The syntax of  $L_B$  is shown in Fig. 2. The language includes expressions, type-annotated variable and function definitions, and control flows. Overall, it is based on a core subset of TypeScript (Bierman et al., 2014) but can be adapted for other statically typed languages. Similar to Bierman et al. (2014), we represent Kleene-Star repetitions using an overline, e.g.,  $\bar{s}$  represents a sequence of statements  $s$ , and adhere to the TypeScript documentation to annotate parameter types in function signatures with argument names (Developers, [n. d.]). We make a distinction between base and extension expressions. The latter applies operators to previous expressions, leading to more complex expressions. This differentiation is useful later in §2.4 for constructing the prefix automaton for parsing expressions.

**Expression Typing Rules** The typing rules for  $L_B$ ’s expressions are detailed in Fig. 6. These rules form a subset of safeFTS, a type-safe portion of TypeScript described by Bierman et al. (2014), allowing us to leverage their soundness results. The type rules for  $L_B$  use the standard concept of a *type environment*, denoted as  $\Gamma$ , which is a collection of pairs  $(x : T)$  of identifiers  $x$  and types  $T$ . We write  $\Gamma \vdash e : T$  if the expression  $e$  has type  $T$  in the type environment  $\Gamma$ . An expression  $e$  is considered valid if its type can be derived by applying the given typing rules.

Literals are evaluated to their respective types (LIT – {NUM, STR, BOOL}). Identifiers  $x$  are evaluated based on the corresponding type in the type environment (IDENT). Anonymous functions are typed according to their annotated parameter types, with the return type determined by the returned expression (ANON). Grouping preserves the type of the inner expression (GROUP).

Binary operators have predefined signatures  $S_1 \odot S_2 : T$ , such as  $\text{number} + \text{number} : \text{number}$  for addition and  $T = T : T$  for assignments. These signatures must be satisfied in well-typed expressions (OP). Function calls require parameters to match the function signature (CALL). The type of member accesses  $e.n$  is determined using an auxiliary function  $\text{LOOKUP}(S, n)$ , which fetches the type of

member  $n$  for type  $S$ . An instantiation of LOOKUP for TypeScript is provided by [Bierman et al. \(2014\)](#).

**Statements and Type Environments** The typing rules for statements are presented in Fig. 7. Type environments are modified by statements, in particular variable declarations and function definitions. We use the notation  $\Gamma_1 \vdash s \mapsto \Gamma_2$  to indicate that after executing statement  $s$  in type environment  $\Gamma_1$ , the new environment is  $\Gamma_2$ .

Variable declarations introduce the identifier with declared type into the type environment, provided the identifier is not already defined (DECL). The type environment defines the context to evaluate expressions (EXPR) and return statements (RET). Return statements are only well-typed inside function bodies. The statements inside statement blocks and if-then-else statements must maintain valid type environments, though they do not have an external effect (BLOCK, ITE). This also applies to function definitions; however, the defined function is finally added to the external type environment (FUN). Lastly, empty statements do not alter the type environment (NOP), while statement sequences propagate the type environment along the execution (SEQ).

**Return Types** The rules for checking return types are presented in Fig. 8. Firstly, return statements must contain expressions matching the function’s declared return type. Secondly, such an expression must be returned on every execution path. We use the notation  $\Gamma \vdash \bar{s} : R$  to indicate the sequence of statements  $\bar{s}$  ensures a return value of type  $R$ .

For variable declarations and expression statements, the return type of the subsequent statements is considered (R-DECL, R-EXPR). The return type of a return statement directly corresponds to the type of the returned expression (R-RET). For statement blocks, the return type is decided by either the block itself or the subsequent statements (R-BLOCK-SELF, R-BLOCK-NEXT). In function definitions, the return type is determined by the type of the subsequent statements, similar to expression statements. It is additionally required that the function body returns a type matching the declared return type (R-FUN). For if-then-else statements, both branches must return the same type (R-ITE-SELF), or the return type is determined by the following statements (R-ITE-NEXT).

**Language Definition** In summary, a program  $s$  is in language  $L_B$  if both (i)  $s$  conforms to the grammar in Fig. 2 and (ii)  $s$  is well-typed according to the typing rules in Figs. 6–8.

## E DETAILED PREFIX AUTOMATON DEFINITIONS

In this section, we provide more detailed definitions and analysis of the various automata for  $L_B$ .

### E.1 BASE AUTOMATA

We now provide detailed definitions for the base prefix automata introduced at the end of §2.2: union, concatenation, Kleene-Star, and terminal.

**Union** For the union  $A_X \cup A_Y$ , we define the resulting sets of initial states and accepting states as  $I := I_X \cup I_Y$  and  $F := F_X \cup F_Y$ , respectively. The transition function is defined as follows:

$$\delta(q, c) := \begin{cases} \delta_X(q, c) & \text{if } q \in Q_X \\ \delta_Y(q, c) & \text{if } q \in Q_Y \end{cases}$$

To show that the language parsed by this automaton is indeed the union  $L(A_X \cup A_Y) = L(A_X) \cup L(A_Y)$ , we employ a short helper lemma, which can be shown inductively.

**Lemma 6.** *The set of the reachable states from a set of states  $\mathbf{q}$  is equal to the union of reachable states from each state in  $\mathbf{q}$ , i.e.  $\gamma(\mathbf{q}, s) = \bigcup_{q \in \mathbf{q}} \gamma(q, s)$ .*

Since the states are distinct and we merely combine the transition functions of both automata, using the lemma, we can quickly see that the language parsed is indeed the union. Moreover, if both  $A_X$  and  $A_Y$  are prefix automata, this also holds for  $A_X \cup A_Y$ .

$$\begin{array}{c}
\text{[LIT-NUM]} \frac{}{\Gamma \vdash \backslash \mathbf{d+} : \text{number}} \quad \text{[LIT-STR]} \frac{}{\Gamma \vdash \backslash \mathbf{w*} : \text{string}} \quad \text{[LIT-BOOL]} \frac{}{\Gamma \vdash \text{true}, \text{false} : \text{boolean}} \\
\text{[IDENT]} \frac{(x : T) \in \Gamma}{\Gamma \vdash x : T} \quad \text{[ANON]} \frac{\Gamma \cup \bar{p} \vdash e : T}{\Gamma \vdash (\bar{p}) \Rightarrow e : (\bar{p}) \Rightarrow T} \quad \text{[CALL]} \frac{\Gamma \vdash f : (\bar{x} : \bar{S}) \Rightarrow T \quad \Gamma \vdash \bar{e} : \bar{S}}{\Gamma \vdash f(\bar{e}) : T} \\
\text{[GROUP]} \frac{\Gamma \vdash e : T}{\Gamma \vdash (e) : T} \quad \text{[OP]} \frac{\Gamma \vdash e_1 : S_1 \quad \Gamma \vdash e_2 : S_2 \quad S_1 \odot S_2 : T}{\Gamma \vdash e_1 \odot e_2 : T} \quad \text{[MEM]} \frac{\Gamma \vdash e : S \quad \text{LOOKUP}(S, n) = T}{\Gamma \vdash e.n : T}
\end{array}$$

Figure 6: Typing rules for  $L_B$ 's expressions.

$$\begin{array}{c}
\text{[DECL]} \frac{x \notin \Gamma}{\Gamma \vdash \text{let } x : T; \succ \rightarrow \Gamma \cup (x : T)} \quad \text{[EXPR]} \frac{\Gamma \vdash e : T}{\Gamma \vdash e; \succ \rightarrow \Gamma} \quad \text{[RET]} \frac{\text{inside function body} \quad \Gamma \vdash e : T}{\Gamma \vdash \text{return } e; \succ \rightarrow \Gamma} \\
\text{[BLOCK]} \frac{\Gamma \vdash \bar{s}_B \succ \rightarrow \Gamma_B}{\Gamma \vdash \{\bar{s}_B\} \succ \rightarrow \Gamma} \quad \text{[FUN]} \frac{x \notin \Gamma \quad \Gamma \cup (x : (\bar{p}) \Rightarrow T) \cup (\bar{p}) \vdash \bar{s}_x \succ \rightarrow \Gamma_x}{\Gamma_1 \vdash \text{function } x(\bar{p}) : T \{\bar{s}_x\} \succ \rightarrow \Gamma \cup (x : (\bar{p}) \Rightarrow T)} \\
\text{[ITE]} \frac{\Gamma \vdash s_{if} \succ \rightarrow \Gamma_{if} \quad \Gamma \vdash s_{else} \succ \rightarrow \Gamma_{else}}{\Gamma \vdash \text{if } (e) \text{ } s_{if} \text{ else } s_{else} \succ \rightarrow \Gamma} \quad \text{[NOP]} \frac{}{\Gamma \vdash \bullet \succ \rightarrow \Gamma} \quad \text{[SEQ]} \frac{\Gamma_1 \vdash \bar{s} \succ \rightarrow \Gamma_2 \quad \Gamma_2 \vdash s \succ \rightarrow \Gamma_3}{\Gamma_1 \vdash \bar{s} s \succ \rightarrow \Gamma_3}
\end{array}$$

Figure 7: Type environment extension rules for sequences of statements in  $L_B$ .

$$\begin{array}{c}
\text{[R-DECL]} \frac{\Gamma \vdash \bar{s} : R}{\Gamma \vdash \text{let } x : T; \bar{s} : R} \quad \text{[R-EXPR]} \frac{\Gamma \vdash \bar{s} : R}{\Gamma \vdash e; \bar{s} : R} \quad \text{[R-RET]} \frac{\Gamma \vdash e : R}{\Gamma \vdash \text{return } e; \bar{s} : R} \\
\text{[R-BLOCK-SELF]} \frac{\Gamma \vdash \bar{s}_B : R \quad \Gamma \vdash \bar{s}}{\Gamma \vdash \{\bar{s}_B\} \bar{s} : R} \quad \text{[R-BLOCK-NEXT]} \frac{\Gamma \vdash \bar{s}_B \quad \Gamma \vdash \bar{s} : R}{\Gamma \vdash \{\bar{s}_B\} \bar{s} : R} \\
\text{[R-FUN]} \frac{\Gamma \cup (x : (\bar{p} \Rightarrow R)) \vdash \bar{s} : R' \quad \Gamma \cup (x : (\bar{p}) \Rightarrow R) \cup (\bar{p}) \vdash \bar{s}_x : R}{\Gamma \vdash \text{function } x(\bar{p}) : R \{\bar{s}_x\} \bar{s} : R'} \\
\text{[R-ITE-SELF]} \frac{\Gamma \vdash s_{if} : R \quad \Gamma \vdash s_{else} : R}{\Gamma \vdash \text{if } (e) \text{ } s_{if} \text{ else } s_{else} \bar{s} : R} \quad \text{[R-ITE-NEXT]} \frac{\Gamma \vdash \bar{s} : R}{\Gamma \vdash \text{if } (e) \text{ } s_{if} \text{ else } s_{else} \bar{s} : R}
\end{array}$$

Figure 8:  $L_B$ 's typing rules for function returns.

**Concatenation** For the concatenation automaton  $A_{XY} = A_X \circ A_Y$ , we define  $I := I_X$ ,  $F := F_Y$ , and the transition function as follows:

$$\delta_{XY}(q, c) := \begin{cases} \delta_X(q, c) & \text{if } q \in Q_X \setminus F_X \\ \delta_X(q, c) \cup \delta_Y(I_Y, c) & \text{if } q \in F_X \\ \delta_Y(q, c) & \text{if } q \in Q_Y \end{cases}$$

Informally, concatenation preserves the parsing behaviour of both  $A_X$  and  $A_Y$  in their respective states. When  $A_{XY}$  reaches an accepting state of  $A_X$  and receives another input character, it either remains in  $A_X$  or transitions to  $A_Y$ , as defined in the second case of  $\delta_{XY}$ . Essentially, this maintains outgoing edges from accepting states in  $A_X$  while adding edges from these accepting states to initial states of  $A_Y$ .

It follows from a similar argument that  $L(A_{XY}) = L(A_X) \circ L(A_Y)$ , where  $L(A_X) \circ L(A_Y)$  is defined as  $\{s_X \circ s_Y \mid s_X \in L(A_X), s_Y \in L(A_Y)\}$ . We first show  $L(A_{XY}) \subseteq L(A_X) \circ L(A_Y)$ . Due to (P1), we can always split any  $s \in L(A_{XY})$  into  $s_X$  that extends from  $I_X$  to  $F_X$  and  $s_Y$  that extends from  $I_Y$  to  $F_Y$ . Then  $s_X \in L(A_X)$  and  $s_Y \in L(A_Y)$ . For  $L(A_X) \circ L(A_Y) \subseteq L(A_X \circ A_Y)$ , we pick any  $s_X \circ s_Y$  from  $L(A_X) \circ L(A_Y)$  and parse it using  $A_{XY}$ . We observe that it will first traverse from  $I_X$  to  $F_X$  consuming  $s_X$ , and then transition through  $I_Y$  to  $F_Y$  by consuming  $s_Y$ .

Moreover  $A_{XY}$  is a prefix automaton, if  $A_X$  and  $A_Y$  are prefix automata and  $L(A_Y) \neq \emptyset$ . Since  $A_X$  is a prefix automaton, we can reach  $F_X$  from any state in  $Q_X$ . From  $F_X$  we additionally reach  $I_Y \subseteq Q_Y$ . Since  $A_Y$  is a prefix automaton, we can reach  $F_Y$  for any state in  $Q_Y$ . This construction is a prefix automaton only if  $I_Y \neq \emptyset$ , which, due to the prefix property, is equivalent to  $L(A_Y) \neq \emptyset$ .

**Kleene-Star** We define the Kleene-Star automaton  $A_{\overline{X}}$  that parses indefinite repetitions of words accepted by  $X$ . First, we consider all initial states as final states, i.e., we ensure  $I_X \subseteq F_{\overline{X}}$ . Then we add transitions to the transition function  $\delta_X$  from the final states  $F_X$  back to the initial states  $I_X$ .

$$\delta_{\overline{X}}(q_X, c) := \begin{cases} \delta_X(q_X, c) & \text{if } q \notin F_X \\ \delta_X(q_X, c) \cup \delta(I_X, c) & \text{if } q_X \in F_X \end{cases}$$

We can quickly see that  $L(A_{\overline{X}}) = \{\overline{s} \mid s \in L(A_X)\}$ , with the same argument as the concatenation automaton. Additionally, because the initial states are accepting, the empty word (zero repetitions) is in  $L(A_{\overline{X}})$ . We similarly see that this is prefix automaton if  $A_X$  is a prefix automaton. Note that here  $L(A_X) \neq \emptyset$  is not required. This is because if  $L(A_X) \neq \emptyset$ , then  $A_{\overline{X}} = A_X = A_{\emptyset}$ , which is still a prefix automaton.

**Terminals** The terminal automaton  $A_S$  parses exactly the terminal  $S$ . They accept the usual alphabet  $\Sigma$  and feature the states  $Q := \{q_s \mid s \text{ is a suffix of } S\}$ ,  $F := \{q_\varepsilon\}$ ,  $I := \{q_S\}$ . The transition function  $\delta$  is defined as follows:

$$\delta(q_s, c) := \begin{cases} \{q_{s'c}\} & \text{if } c \circ s' = s \\ \emptyset & \text{otherwise} \end{cases}$$

Clearly  $A_S$  is a prefix automaton. We can show inductively that for any  $s$ :  $\gamma(q_s, s') = \{q_\varepsilon\} \iff s = s'$ , and thus  $L(A_S) = \{S\}$ . With a simple modification, we introduce  $A_s^W$ , where  $W$  denotes whitespace characters. The transition function is defined as  $\delta(q_s^W, c) := \{A_s^W\}$  if  $c \in W$ ; otherwise,  $\delta(A_{\text{cos}}^W, t) := \{A_s^W\}$ . This allows arbitrary whitespaces before parsing  $s$ . This is how we implement syntactic indifference to whitespace between terminals.

**Notational Details** In the following, we will implicitly assume that  $\delta(q, c) = \emptyset$  if not explicitly defined otherwise, making notation more concise. For any state, we access the following information through dot notation or the special notation on the state, which we assume is passed to subsequent states through the transition function (unless otherwise stated). This information is alternatively passed through to entire automata in composite automata, e.g., in  $A_{XY}$  from  $A_X$  to  $A_Y$ .

- $q \downarrow T$ : Type  $T$  to which state  $q$  is constrained (introduced in more detail later).
- $q \in F_X$ : Whether state  $q$  is an accepting state of the automaton  $A_X$ .
- $q.\Gamma$ : The type environment based on state  $q$  currently being parsed.

- $q.\text{LHS}$ : The left-hand side expression of an extending expression represented by state  $q$ , i.e., when extending  $X$  with  $Y$  and currently parsing  $q_Y$ , then  $q_Y.\text{LHS} = X$ .
- $q.\text{TYP}$ : The described type of the last coherent expression that this state belongs to. This is only defined for accepting states. Generally, we ensure that when some expression  $e$  was parsed, the corresponding state  $q_e$  has attribute  $q_e.\text{TYP}$  such that  $q_e.\Gamma \vdash e : q_e.\text{TYP}$ .

When accessing the properties of  $A$ , we access the property of the current state of the automaton  $q \in Q$ , e.g.,  $A.\text{LHS} = q.\text{LHS}$ . For parsed automata, the current state is the final, accepting state.

## E.2 EXPRESSIONS

Expressions are parsed using recursive automata as introduced in §2.4. In this part of the appendix, we describe in more detail how information is passed between states, using the additional properties of states introduced in App. E.1.

In the case of expressions, the  $\text{TYP}$  attribute expresses the type of the expression parsed so far. In expression states  $q$ , we leverage the  $\text{LHS}$  to accurately determine  $q.\text{TYP}$ .

$$\begin{aligned}
q_{\text{STR}}.\text{TYP} &:= \text{string} \\
q_{\text{NUM}}.\text{TYP} &:= \text{number} \\
q_{\text{BOOL}}.\text{TYP} &:= \text{boolean} \\
q_x.\text{TYP} &:= T \text{ where } q_x.\Gamma \vdash x : T \\
q_{(\bar{p}) \Rightarrow e}.\text{TYP} &:= (A_{\bar{p}}.\text{TYP}) \Rightarrow A_e.\text{TYP} \\
q_{(e)}.\text{TYP} &:= A_e.\text{TYP} \\
q_{\odot e}.\text{TYP} &:= R, \text{ for } q_{\odot e}.\text{LHS}.\text{TYP} = S, A_e.\text{TYP} = T \text{ and } S \odot T : R \\
q_{(\bar{e})}.\text{TYP} &:= T, \text{ for } q_{(\bar{e})}.\text{LHS}.\text{TYP} = (\bar{p}) \Rightarrow T \\
q_n.\text{TYP} &:= T, \text{ for } \text{LOOKUP}(q_n.\text{LHS}.\text{TYP}, n) = T
\end{aligned}$$

**Unrestricted Expressions** The left-hand side of the currently parsed expression is used in the definition of automata for three extending expressions; arithmetic operators, function call, and member access. The arithmetic operator automaton constrains its states to those with valid operators, i.e.:

$$A_{\odot e} := \bigcup_{\exists R: A_{\odot e}.\text{LHS}.\text{TYP} \odot T = R} A_{\odot}(\odot A_e \downarrow T)$$

For function call, the automaton is only valid if the left-hand side is a function, and accepts only the valid signature.

$$A_{(\bar{e})} := \begin{cases} A_{\downarrow} \circ (A_{\bar{e}} \downarrow A_{\bar{p}}.\text{TYP}) \circ A_{\downarrow} & \text{if } A_{(\bar{e})}.\text{LHS}.\text{TYP} = (\bar{p}) \Rightarrow T \\ A_{\emptyset} & \text{otherwise} \end{cases}$$

Finally, the member access automaton is a union of the automata that parses the attributes of the left-hand side expression. Or formally,

$$A_{,n} := \bigcup_{\exists T: \text{LOOKUP}(A_{,n}.\text{LHS}.\text{TYP}, m) = T} A_{,m}.$$

**Type-Restricted Expressions** The type restricted versions of the automata are all covered by the definition presented in §2.4. Note that the  $\text{DERIVABLE}$  function presented in Tab. 1 implicitly leverages access to  $q_s.\text{LHS} = e$  when accessing the expression  $e$  in the extension expressions.

## E.3 PRUNING THE TYPE SEARCH

In this section, we present our heuristic for pruning the type search recursion from §2.4, i.e., our implementation of  $\text{PRUNESearch}$  at L. 6 of Alg. 2. The heuristic is based on the complexity and novelty of candidate types to explore.

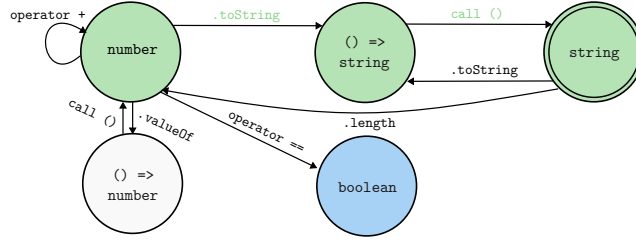


Figure 9: An example search through the graph for type reachability, starting from  $T = \text{number}$  with the goal string, e.g., after parsing `let x : string; x = 1`. States and edges along the final path are marked in green and explored nodes in blue. The  $() \Rightarrow \text{number}$  node is not explored, as complex types are avoided by our heuristic. The node  $() \Rightarrow \text{string}$  is explored as it enables reaching new type string.

Based on the assumptions about the LOOKUP function and operators in §2.1, we observe a restriction in the reachable types by extensions: From any given type, we reach itself, result types of arithmetic operators via OP, return types through CALL, and member types through MEMBER. A higher-order type  $() \Rightarrow T$  does not allow access to types not reachable from  $T$ . Consequently, we avoid exploring such higher-order types unless the target type is of higher order, or the higher-order type offers novel, yet unexplored types. For instance, in Fig. 9, the type  $() \Rightarrow \text{number}$  is not explored, because it is more complex than both the initial and goal types, number and string, and does not contain any unexplored type.

To formalize this understanding, we introduce the concepts about the *depth* and *root types* of a given type, denoted as DEPTH and ROOT, respectively. DEPTH measures the complexity of a type, specifically the order of a function, while ROOT returns all types of minimal depth (e.g., string, number, and boolean) that constitute a higher-order type. They are defined as follows:

$$\text{DEPTH}(T) := \begin{cases} \text{DEPTH}(S) + 1 & \text{if } T = (\bar{p}) \Rightarrow S, \\ 0 & \text{otherwise.} \end{cases} \quad \text{ROOT}(T) := \begin{cases} \text{ROOT}(S) & \text{if } T = (\bar{p}) \Rightarrow S, \\ \{T\} & \text{otherwise.} \end{cases}$$

We leverage DEPTH and ROOT to implement  $\text{PRUNESearch}(T, G, S)$  for a current type  $T$ , a goal type  $G$ , and a type  $S$  after an extension is applied on  $T$ . In general, if  $G$  is not directly accessible from  $T$ , it will also not be accessible from expressions with the same root types but greater depth, such as  $() \Rightarrow T$ . When  $G$  is of higher order, exploring up to the depth of  $G$  can be required, such as when  $G = () \Rightarrow ( () \Rightarrow \text{number} )$ . Based on these two ideas, we stop exploring  $S$  when  $\text{DEPTH}(S) > \max(\text{DEPTH}(G), \text{DEPTH}(T))$ .

Further, if a higher-depth function returns an unexplored type, we need to explore it. Sticking to the example in Fig. 9, type number has the member `toString` of type  $() \Rightarrow \text{string}$ . The type string can only be reached by exploring the member access at depth 1. On the contrary, we do not explore a higher-depth function if it does not introduce novel types other than explored. To achieve this, we adapt Alg. 2 to additionally define a set of root types  $R$ , which is initialized to an empty set and is updated by  $R = R \cup \text{ROOT}(T)$ . We do not explore  $S$  if  $\text{ROOT}(S) \subseteq R$ .

Taking the conjunction of the aforementioned two aspects, our pruning heuristic is implemented as  $\text{PRUNESearch}(T, G, S) := \text{DEPTH}(S) > \max(\text{DEPTH}(T), \text{DEPTH}(S)) \wedge \text{ROOT}(S) \subseteq R$ . The restrictions based on depth and root types are based on the results of the rigorously analyzed search over succinct types by Gvero et al. (2013). This provides a robust heuristic for exploring as many relevant inhabitable types as possible. However, due to the additional complexity introduced by the lookup function, we can not guarantee completeness and instead refer to the strong empirical results in our evaluation in §3 as evidence of the search’s high coverage.

#### E.4 IMPLEMENTATION OF DERIVABLE

Recall that in Tab. 1, DERIVABLE for function expressions are defined as:  $\text{DERIVABLE}(q_{(\bar{p}) \Rightarrow e}) = \{(\bar{p}) \Rightarrow T \mid \text{REACHABLE}(\text{DERIVABLE}(q_e), T)\}$ . This involves constructing a type reachability graph and collecting all  $T$  types reachable from  $\text{DERIVABLE}(q_e)$ . However, this process is in-

tractable because  $T$  can be of arbitrarily high-order, as such there are infinitely many  $T$  to explore. A similar issue exists for grouped expressions, as their `DERIVABLE` function is also defined to enumerate reachable types. We introduce two optimization heuristics to address this problem.

We first observe that `DERIVABLE` is always called within the context of an invocation of `REACHABLE` with target type  $G$ , e.g., `REACHABLE(DERIVABLE( $q(\bar{p}) \Rightarrow e$ ),  $G$ )` for function expressions. To compute `DERIVABLE( $q(\bar{p}) \Rightarrow e$ )`, we enumerate all types present on the type graph represented by `REACHABLE(DERIVABLE( $q_e$ ),  $G$ )`, which is finite with due to application of the pruning heuristics in App. E.3. In other words, we bound the maximum complexity of considered types  $T$  using the pruning heuristic for reachability of target type  $G$ . This leads to a sound but potentially incomplete version of `DERIVABLE`. However, since the final goal is to reach  $G$ , this heuristic provides a practically useful set of all relevant derivable types.

Second, we observe that the resulting two-tiered call `REACHABLE(DERIVABLE( $q(\bar{p}) \Rightarrow e$ ),  $G$ )` can be integrated into a single call to further reduce the amount of explored types. Concretely, when discovering some type  $M$  in `REACHABLE(DERIVABLE( $q_e$ ),  $G$ )`, as per the previous heuristic, we allow transitioning directly to `REACHABLE( $(\bar{p}) \Rightarrow M$ ,  $G$ )` to allow a depth-prioritizing exploration of the search graph. This allows us to efficiently discover a path to  $G$  if it exists.

## E.5 STATEMENTS

We define the remaining automata to capture the complete language from §2.1. To correctly handle function return types, we pass on related information when entering function bodies:

- $q.R$ : The expected return type of the current state  $q$ .
- $q.RETURNED$ : Whether the currently parsed program block has returned in all branches.
- $q.MUSTRETURN$ : Whether the currently parsed program block must return (i.e., If-Then-Else branches do not need to contain return statements even if a return type is expected of the surrounding code block).

The single statement automaton is another recursive definition, since some statements, e.g., If-Then-Else, can themselves contain statements. The statement automaton is defined recursively as  $A_s := A_{DECL} \cup A_{EXPR} \cup A_{RET} \cup A_{BLOCK} \cup A_{FUN} \cup A_{ITE}$ . The expression statement automaton and block automaton are simply defined as  $A_{EXPR} := A_e$ ; and  $A_{BLOCK} := A_{\{\bar{s}\}}$ . The declaration automaton  $A_{DECL} := A_{\text{let } x:T}$ ; captures variable names  $x$  using an automaton for non-existing identifiers, which works the same way as  $A_x$  except that it rejects terminals that match an existing variable. This automaton is a prefix automaton as well, since indefinite additional characters can be added to the variable name and there are only finitely many defined variables. The If-Then-Else automaton is defined using standard concatenation:  $A_{ITE} := A_{\text{if}(e) s \text{ else } s}$ . The statements automaton  $A_{\bar{s}}$ , based on the Kleene-Star automaton definition and the single statement automaton. Return statements are only non-empty when the expected return type is set, i.e. when parsing inside a function:

$$A_{RET} := \begin{cases} A_{\text{return}} \circ A_e \downarrow T & \text{if } A_{RET}.R = T \\ A_{\emptyset} & \text{otherwise} \end{cases}$$

For functions, the automaton is based on the standard concatenation  $A_{FUN} = A_{\text{function } x(\bar{p}) : T \{\bar{s}\}}$ . However, the transition function updates the states of the statement automata inside the function:

- $q.R = T$ , i.e., the return type of these statements is set to the return type of the function. This value is propagated recursively to all sub-automata.
- $q.MUSTRETURN = \text{true}$ , for the outermost statement block automaton. It is set to false for deeper nested statement blocks and as soon as a parsed statement  $X$  has  $q_X.RETURNED$  set to true - i.e. one of the main body statements returned in every branch.
- $q.RETURNED = \text{false}$ , per default in every statement, except a) in return automata, b) inside a multi-statement automaton where the previous statement has  $RETURNED = \text{true}$  and c) in ITE-automata where both branching statements have  $RETURNED = \text{true}$ .

As long as a state  $q$  in a multi-statement automaton has  $X.RETURNED = \text{false}$  and  $q.MUSTRETURN = \text{true}$ , it can not accept but instead forces the generation of another statement.

Since we can always express the requested type through literals and can always simply generate a return statement to fulfill this requirement, the prefix automaton property is not violated.

**Tracking Type Environments** Generally, we follow the typing rules in Fig. 7. Identifiers are passed on through all state transitions, matching the rule SEQ, where the type environment of consecutive statements needs to be compatible. However, in the cases of BLOCK, ITE and FUN, we discard the local type environment after parsing, matching the respective typing rules. In FUN additionally, the function signature and parameters are added into the type environment of the function body automaton.

## F EXTENSION TO TYPESCRIPT

We extend our completion engine described in §2 to handle a core subset of modern TypeScript. In this section, we selectively discuss the implementation of interesting language features. We provide a complete list of supported features in Tab. 8 of App. G.

**Constant Variable Declarations** In addition to variable declaration using `let`, TypeScript supports constant declarations using `const`. This defines immutable identifiers. We thus additionally track mutability of each identifier in the type environment and disallow applying the assignment operator to immutable identifiers.

**Arrays** We add support for array type annotation, parsing array expressions, and reading from and assigning to array fields. In array expressions, we enforce that all array elements have the same type. Moreover, array types introduce another dimension of type nesting. Therefore we adapt the type reachability pruning heuristic to handle this additional dimension to ensure termination.

**Loops** TypeScript supports various loop constructs, including `for`, `while`, `do-while`, and `for...of` loops. These are implemented mostly as variations of the statement block parser. The `for...of` loop uniquely constrains the right-hand side of the `...of` operator to an array of any type. To adapt the type search, we introduce a generic array type  $\bullet[]$ , which matches any array type. For example, both types `number[]` and `string[]` match  $\bullet[]$  in L. 2 of Alg. 2.

**Additional Operators and Types** We add several arithmetic and logic operators, such as modulo `%`, exact equality `===`, logical or `||`, and the ternary operator `?:`. To handle these operators, we add additional edges to the type search graph. Moreover, we add support for post- and prefix operators such as `--` and `++`, which are only valid extensions to mutable expressions.

**Operator Precedence** TypeScript defines an operator precedence, which determines the implicit grouping of expressions. For example `1 + 2.toString()` is parsed as `1 + (2.toString())`. We adapt our expression parsing algorithm in two places to handle operator precedences. First, in the expression automaton, we leverage the knowledge about previously parsed extensions to determine the implicit grouping and thus where the next operator is applied. For example, for state  $q^{1+2}$ , the member access extension `.n` is applied to `2`, as opposed to `1 + 2`. Second, we adapt the type search in Alg. 2. Concretely, we ensure that only extensions that can be validly applied based on operator precedence are iterated over. For this, we track the operator precedence of previously parsed extensions and extensions considered during the traversal of the type graph and omit operators in L. 5 that violate operator precedence.

**Global Identifiers and Imports** In TypeScript, many identifiers are defined globally and available in any execution. These global identifiers are incorporated by initializing the type environment of the program automaton accordingly. Identifiers such as `Math` introduce additional types, which we additionally implement. We also model the import of the `crypto` library using `require`.

**Polymorphic Built-In Members** The TypeScript LOOKUP implementation defines a few polymorphic members for built-in types. For example, for array `x` of type `T[]`, `x.map(f)` takes a callback function `f` and returns a new array `[f(x[0]), f(x[1]), ...]`. If `f` has type `(T) => P`, the returned

array has type  $P[]$ . Here  $P$  is a *type parameter*, which is instantiated by matching the type of the passed function to the type pattern.

We support such polymorphisms by adapting the type search. We track type patterns and enforce that type parameters are instantiated before the goal type is reached. We then continue the search from the instantiated version. In the `map` example, when searching completions of `x.map`, we first search for functions that instantiate the type parameter, and then continue the search from the instantiated type. When anonymous functions are generated as call parameters, we enforce that the function matches the searched type pattern.

**Mandatory Type Annotation** TypeScript is designed to be flexible, allowing many type annotations to be omitted when they can be automatically inferred. While this is generally beneficial, such as inferring types from initial values, it can lead to unexpected types when annotations are omitted, often confusing even experienced developers (nop33, 2024; Various, 2024). Moreover, in the context of LLM-based code generation, having more type annotations can provide valuable information for both the model and our type constraining algorithms. We have identified three situations where generated code often fails to compile without type annotations, prompting us to enforce them. First, we require annotations for all function parameters and return types. Second, all variable declarations must either have a type annotation or be initialized with a value. Third, we enforce type annotations for the first parameter of anonymous functions used as callbacks in the polymorphic built-in member `reduce`. These constraints trade-off practical correctness with theoretical language completeness.

## G DETAILS ABOUT EXPERIMENTAL EVALUATION

In this section, we detail how executable code is extracted from the model responses and a slight modification to the decoding algorithm used, that increases throughput heuristically.

**Implementation Details** Our implementation is written in Python and contains 11249 lines of code. To ensure robust implementation, we built a large set of around four hundred unit tests and frequently compared the behaviors of our implementation with the official TypeScript compiler (Microsoft, 2024).

We have two main external dependencies. To implement the regular-expression-based literal automata, we leverage the `regex` library,<sup>3</sup> as it allows checking if the current string can be completed to match a regular expression. To implement LLM inference, we leverage the `transformers` library.<sup>4</sup> We provide an exhaustive list of supported features and unsupported features of the TypeScript language in our final implementation in Tab. 8.

**Hyperparameters** We run the models on A100 NVidia GPUs with 80 GB of VRAM. We use CUDA 12.4 and the Hugging Face library. We set the sampling temperature to 1. We set seeds to 0 to 4 on the four HumanEval runs and 0 on the one MBPP run respectively. We limit the completions to 1000 tokens and time out after 300 seconds. We compute syntactic correctness using the Oxidation toolchain (oxc project, 2024) as the TypeScript Compiler does not clearly distinguish between syntactic and semantic errors.

**Excluded MBPP Instances** We discovered that a number of TypeScript translations contained invalidly generated nested tuples. After reporting them to the developers, they have been resolved in the latest version of MBPP and we include them in our evaluation. Still, we find that the TypeScript translation of a number of MBPP instances contains too broad type annotation, annotating elements as any or array of any. We therefore exclude the following 6 instances from the evaluation:

- mbpp\_405\_check\_tuplex
- mbpp\_563\_extract\_values
- mbpp\_580\_extract\_even
- mbpp\_612\_merge

<sup>3</sup><https://pypi.org/project/regex/>

<sup>4</sup><https://huggingface.co/docs/transformers>

Table 8: Supported and Missing TypeScript Features

| Supported TypeScript Features                                         | Examples                                |
|-----------------------------------------------------------------------|-----------------------------------------|
| Expressions, Statements, Function Declarations                        | ( $L_B$ as introduced in §2)            |
| Additional Literals: BigInt, Regex, Template Strings                  | 10n, /\d*/, `hello \${user}`            |
| Additional Types: void, null, undefined                               | void, undefined, null                   |
| Index Signature Types and Literals                                    | let x: {[y: number]: string} = 1: "hi"; |
| Anonymous Functions                                                   | function (): bool {return true}         |
| Lambda Functions with and without Function Bodies                     | x => {return y}, x => y                 |
| Ternary and Logic Operators                                           | ? :,   , &&                             |
| Arithmetic and Boolean Operations                                     | +, -, **, &, !                          |
| Assigning Pre-and Postfix Operators                                   | ++, --                                  |
| Arrays                                                                | [1, 2, 3]                               |
| Access and Assignment to Computed Members                             | x[10] = y[i];                           |
| Constructors and "new" Calls                                          | let x = new Number(1);                  |
| Calls with Optional and Rest Parameters                               | function foo(x?: number, y...: string)  |
| Sets and Maps                                                         | Map<string, number>()                   |
| Parameterized Constructor Calls                                       | new Set<string>()                       |
| Tuples                                                                | let x: [int, string] = [1, "hello"];    |
| Optional Chaining                                                     | x.get("hi")?.get("world")               |
| Spread Operator                                                       | [...xs]                                 |
| Type Assertions                                                       | "hello" as any                          |
| For Loops                                                             | for(int x = 0; i < 10; i++)             |
| For Of Loops                                                          | for(x of xs)                            |
| For Of Loops with Tuple Destructuring                                 | for([x, y] of xys)                      |
| Do-While and While Loops                                              | while (true) {...}                      |
| Typed and Untyped Variable Declarations                               | let x: number = 1; let y = 100;         |
| Comments, Multiline Comments                                          | // Comment                              |
| Returning without Expressions                                         | return;                                 |
| Try-Catch Statements with a Fixed Exception Type                      | try { ... } catch (e) { ... }           |
| Throw Statements                                                      | throw new Error("...")                  |
| Importing the crypto Library                                          | require("crypto")                       |
| Global Scope Objects                                                  | Math, parseInt                          |
| Automatic Semicolon Insertion                                         |                                         |
| Missing Features                                                      | Examples                                |
| General Library Imports                                               | require("example")                      |
| Use of Functions Before Declaration                                   |                                         |
| For In Loops                                                          | for(x in y)                             |
| Type Declaration                                                      |                                         |
| User-Defined Classes                                                  |                                         |
| Declaration and Parameterized Call of General Parameterized Functions |                                         |
| Destructuring Assignment                                              | [x, y] = z                              |
| Uninitialized, Unannotated Variable Declarations                      | let x;                                  |
| Return Type Inference                                                 |                                         |
| Literal Types                                                         |                                         |
| Enums                                                                 |                                         |
| Symbols                                                               |                                         |

- mbbp\_725\_extract\_quotation
- mbbp\_791\_remove\_nested

**Complete Prompts** We provide the complete prompts to the language models for the settings synthesis, translation, and repair. The prompts are templates, instantiated with the prompt from the Multipl-E dataset (Cassano et al., 2023). Since the models were instruction tuned, there are various formats for the chat template. We therefore provide the prompts on a high level. The system prompt has been prepended to the first user prompt where no system prompts were available. The model instruction is the comment preceding the problem in the original benchmark presentation. To match the chat interaction template, we remove the comment prefix `//` and insert it as a user prompt. Sample test cases are preserved when present. The model completion starts from a pre-filled assistant response. The prompts for synthesis and translation are presented in Figs. 11 and 12.

In the repair setting, we add the model output, annotated with line numbers, as assistant output and use a second turn to pass back compiler outputs as demonstrated in Fig. 13. Compiler errors contain line numbers for localization, which is why we annotate the output with line numbers.

We find that Qwen2.5 32B tends to always generate test cases, which lead to errors during compilation. We therefore append the sentence `Do not include test cases in the code.` to its prompt.

**Executable Code Generation and Extraction** When generating code, we employ two techniques to speed up generation and extract the generated code. First, we stop generation after encountering a closing code-fence (`` ```). This drastically reduces generation time, as the model usually continues to generate some explanation or additional code that is irrelevant to our evaluation. Then we try to extract the generated function and all relevant subsequent function definitions.

We found that unconstrained models frequently generate non-compiling code caused by generated unsolicited demonstrations and additional test cases. In order to remove them and decrease such irrelevant compilation errors for unconstrained generation, we try to detect and extract the relevant code snippet.

Concretely, we first extract the corresponding TypeScript code block (i.e., ````typescript...````), or do not cut off if the block is not closed. Inside the code block, we cut off after the closing curly brace of the last balanced pair of curly braces, if it is followed by a newline or semicolon. This determines the last statement block generated, and avoids cutting off, e.g., inside a template literal. Again, if no such case is found, we do not prune the output. We demonstrate the operation of this cutoff algorithm in Fig. 10.

## H CASE STUDY FULL OUTPUTS

In this section, we provide the full outputs of the examples shown in the case study in Figs. 14, 15a, 15b and 16. Details about the functionality for each instance are provided in the respective captions.

```

1  ```typescript
2  function next_smallest_palindrome(num: number): number {
3      const numStr = num.toString();
4      const reversedNumStr = numStr.split('').reverse().join('');
5      let min = Math.min(Number(numStr), Number(reversedNumStr));
6
7      if (min === Number(numStr)) {
8          return Number(numStr);
9      } else {
10         return parseInt(min.toString() + 1);
11     }
12 }
13
14 const findNextSmallestPalindrome = next_smallest_palindrome(12321);
15 console.log(findNextSmallestPalindrome); // Output: 12322
16
17
18 **Explanation**
19
20 1. **Input:** The function takes a number as input (`num`) in the given criteria.
21 ...

```

Figure 10: The code generated by Gemma 2 2B for MBPP #0. The cutoff algorithm first extracts the fenced code, last line marked in **blue**. To avoid the usage of the `console` object from the browser extension of TypeScript in the generated examples, we further cut off after the last code block, marked in **red**.

```

System:
You are an expert in TypeScript programming. Solve the given problem by writing solution code in TypeScript.
When answering, insert the solution code in a ```typescript...``` block.
Do not include test cases in the code.

User:
Check if in given array of numbers, are any two numbers closer to each other than
given threshold.
>>> has_close_elements([1.0, 2.0, 3.0], 0.5)
false
>>> has_close_elements([1.0, 2.8, 3.0, 4.0, 5.0, 2.0], 0.3)
true function

Assistant:
```typescript
function has_close_elements(numbers: number[], threshold: number): boolean {

```

Figure 11: The full prompt for the synthesis setting. Text in green is based on the problem instance, in this case HumanEval #0. The red sentence is only added for Qwen2.5 32B due to its tendency to include non-compiling test cases.

```

System:
You are a helpful and expert programmer in Python and TypeScript. You will be given an input program in Python and your task is
to translate this program into TypeScript. You may assume that the input program is correct and that the translation should be
semantically equivalent.
When answering, insert the solution code in a ```typescript...``` block.
Do not include test cases in the code.

User:
The following is the source program in Python:
```python
from typing import List

def has_close_elements(numbers: List[float], threshold: float) -> bool:
    for idx, elem in enumerate(numbers):
        for idx2, elem2 in enumerate(numbers):
            if idx != idx2:
                distance = abs(elem - elem2)
                if distance < threshold:
                    return True

    return False
```

Please translate the source program to TypeScript.

Assistant:
```typescript
function has_close_elements(numbers: number[], threshold: number): boolean {

```

Figure 12: The full prompt for the translation setting. Text in green is based on the problem instance, blue is the original Python canonical solution, in this case HumanEval #0. The red sentence is only added for Qwen2.5 32B due to its tendency to include non-compiling test cases.

**System:**  
 You are an expert in TypeScript programming. Solve the given problem by writing solution code in TypeScript.  
 When answering, insert the solution code in a ````typescript...```` block.

**User:**  
 Given an array of positive integers x. return a sorted array of all elements that hasn't any even digit.  
 Note: Returned array should be sorted in increasing order.  
 For example:  
 »> unique\_digits([15, 33, 1422, 1])  
 [1, 15, 33]  
 »> unique\_digits([152, 323, 1422, 10])  
 []

**Assistant:**  

```

001: function unique_digits(x: number[]): number[] {
002:   const filteredArray: number[] = []; // initialize empty array
003:   for (let i = 0; i < x.length; i++) {
004:     let strx = "" + x[i];
005:     let filteredStr = strx
006:       .toString()
007:       .split("")
008:       .filter((digit) => parseInt(digit) % 2 !== 0);
009:     if (filteredStr.length > 0) {
010:       filteredArray.push(...filteredStr);
011:     }
012:   }
013:   return filteredArray.sort((a, b) => a - b);
014: }
  
```

**User:**  
 This output produced an error:  

```

../../../../tmp/tmpaewlckfv.ts(10,26): error TS2345: Argument of type 'string' is not assignable to parameter of type 'number'.
  
```

Write the program again, and make sure to fix the error this time.

**Assistant:**  

```

```typescript
function unique_digits(x: number[]): number[] {
  
```

Figure 13: The full prompt for the repair setting. Text in **green** is based on the problem instance, **red** is model output from the synthesis step, **blue** is compiler output. In this case HumanEval #104 and Gemma 2 2B on its own previous output. Generations from the synthesis step are annotated with line numbers to aid localizing the compiler error.

```

1 function select_words(s: string, n: number): string[] {
2   const result: string[] = [];
3   for (const word of s.split()) {
4     let nConsonants = 0;
5     for (let i = 0; i < word.length; i++) {
6       const char = word[i].toLowerCase();
7       if (!['a', 'e', 'i', 'o', 'u'].includes(char)) {
8         nConsonants++;
9       }
10    }
11    if (nConsonants === n) {
12      result.push(word);
13    }
14  }
15  return result;
16 }

```

(a) The code generated by the unconstrained Gemma 2 2B when translating a Python solution. The model tries to call the `split` member of a *string* object without parameters. This is legal in Python but not allowed in TypeScript.

```

1 function select_words(s: string, n: number): string[] {
2   const result: string[] = [];
3   for (const word of s.split(' ')) {
4     let nConsonants = 0;
5     for (let i = 0; i < word.length; i++) {
6       const letter = word[i].toLowerCase();
7       if (!['a', 'e', 'i', 'o', 'u'].includes(letter)) {
8         nConsonants++;
9       }
10    }
11    if (nConsonants === n) {
12      result.push(word);
13    }
14  }
15  return result;
16 }

```

(b) The code generated by Gemma 2 2B with type constraints. The constraint guides the model and help it generate the required argument to `split`, which determines the characters around which to split the string.

Figure 14: Comparison between the function generated by unconstrained Gemma 2 2B (Team et al., 2024) and the code generated with the guidance of type constraints on the problem `select_words` in HumanEval (Chen et al., 2021). This problem requires a function that selects words from a given list that contain a specified number of consonants.

```

1 function largest_divisor(n: number): number {
2   for(let i = n - 1; i > 0; i--) {
3     if(n % i === 0) {
4       return i;
5     }
6   }
7 }

```

(a) The code generated by the unconstrained Deepseek Coder 33B Instruct. The function loops over all numbers smaller than  $n$  to determine the largest divisor. Even though functionally correct for positive numbers, this function returns undefined when the return statement in the loop is never called (e.g., for negative inputs), violating the type system rules.

```

1 function largest_divisor(n: number): number {
2   for(let i = n - 1; i > 0; i--) {
3     if(n % i === 0) {
4       return i;
5     }
6   }
7   return 1; // Return 1 if no such divisor found
8 }

```

(b) The code generated by Deepseek Coder 33B Instruct with type constraints. The system ensures that every path returns a value matching the annotated type. This forces the LLM to generate another line after the loop, and the model correctly chooses to generate a fallback return statement.

Figure 15: Comparison between the function generated by the unconstrained DeepSeek Coder 33B Instruct (Guo et al., 2024) and the code generated with the guidance of type constraints on the problem `largest_divisor` in HumanEval (Chen et al., 2021). The problem asks to compute the largest divisor of a given number.

```

1 function intersperse(numbers: number[], delimiter: number): number[] {
2   return numbers.reduce((acc, curr, index) => {
3     acc.push(curr);
4     if (index < numbers.length - 1) {
5       acc.push(delimiter);
6     }
7     return acc;
8   }, []);
9 }

```

(a) The code generated by the unconstrained Gemma 2 9B. The code uses the `reduce` member of arrays in TypeScript. The `reduce` member is a generic function that accepts a callback as first argument. This callback has three parameters: An accumulator, a current value and an index. The types of the second and third parameter are fixed to the element type of the callee array and number. The first argument type of the callback function is automatically inferred from the type of the second argument to the `reduce` function, in this case an empty array. The type of this array is `never[]`, a special type denoting arrays without members. Since we can assign this type to the callee type `number[]`, the accumulator parameter obtains type `never[]`. However, calling `push` on this type results in a type violation as the pushed value of type `number` is not compatible with the inferred element type `never`. This issue is well known in TypeScript and even human developers frequently stumble upon this issue (Various, 2024; nop33, 2024)

```

1 function intersperse(numbers: number[], delimiter: number): number[] {
2   return numbers.reduce((acc: number[], num: number, index: number) => {
3     if (index > 0) {
4       acc.push(delimiter);
5     }
6     acc.push(num);
7     return acc;
8   }, []);
9 }

```

(b) The code generated by Gemma 2 9B (Team et al., 2024) with type constraints. We force the model to generate type annotations for the callback function in `reduce` and thus enable the model to generate the correct type annotation and avoid the issue in the unconstrained code.

Figure 16: Comparison between the function generated by the unconstrained Gemma 2 9B (Yang et al., 2024) and the code generated with the guidance of type constraints on the problem `intersperse` in HumanEval (Chen et al., 2021). The task in this problem is to insert a delimiter number between consecutive elements of an input list.