SAMBA: SIMPLE HYBRID STATE SPACE MODELS FOR EFFICIENT UNLIMITED CONTEXT LANGUAGE MODELING

Anonymous authors

Paper under double-blind review

ABSTRACT

Efficiently modeling sequences with infinite context length has long been a challenging problem. Previous approaches have either suffered from quadratic computational complexity or limited extrapolation ability in length generalization. In this work, we present SAMBA, a simple hybrid architecture that layer-wise combines Mamba, a selective State Space Model (SSM), with Sliding Window Attention (SWA). SAMBA selectively compresses a given sequence into recurrent hidden states while still maintaining the ability to precisely recall recent memories with the attention mechanism. We scale SAMBA up to 3.8B parameters with 3.2T training tokens and demonstrate that it significantly outperforms state-of-the-art models across a variety of benchmarks. Pretrained on sequences of 4K length, SAMBA shows improved perplexity in context lengths of up to 1M in zero-shot. When finetuned on 4K-length sequences, SAMBA efficiently extrapolates to a 256K context length with perfect memory recall on the Passkey Retrieval task, and exhibits superior retrieval extrapolation on the challenging Phonebook task compared to full-attention models. As a linear-time sequence model, SAMBA achieves a $3.73 \times$ higher throughput compared to Transformers with grouped-query attention for user prompts of 128K length, and a $3.64 \times$ speedup when generating 64K tokens with unlimited streaming.

032

006

008 009 010

011

013

014

015

016

017

018

019

021

024

025

026

027

1 INTRODUCTION

033 Attention-based models (Vaswani et al., 2017; Bahdanau et al., 2014) have dominated the neural 034 architectures of Large Language Models (LLMs) (Radford et al., 2019; Brown et al., 2020; OpenAI, 2023; Bubeck et al., 2023) due to their ability to capture complex long-term dependencies and the 035 efficient parallelization for large-scale training (Dao et al., 2022a). Recently, State Space Models (SSMs) (Gu et al., 2021; Smith et al., 2023; Gu et al., 2022; Gu & Dao, 2023) have emerged as a 037 promising alternative, offering linear computation complexity and the potential for better extrapolation to longer sequences than seen during training. Specifically, Mamba (Gu & Dao, 2023), a variant of SSMs equipped with selective state spaces, has demonstrated notable promise through strong 040 empirical performance and efficient hardware-aware implementation. Recent work also shows that 041 transformers have poorer modeling capacities than input-dependent SSMs in state tracking problems 042 (Merrill et al., 2024). However, SSMs struggle with memory recall due to their recurrent nature 043 (Arora et al., 2023), and experimental results on information retrieval-related tasks (Fu et al., 2023; 044 Wen et al., 2024; Arora et al., 2024), have further shown that SSMs are not as competitive as their attention-based counterparts.

Previous works (Zuo et al., 2022; Fu et al., 2023; Ma et al., 2023; Ren et al., 2023) have explored various approaches to hybridize SSMs with the attention mechanism, but none have demonstrated significantly better language modeling performance compared to state-of-the-art Transformer ar-chitectures. Existing length extrapolation techniques (Han et al., 2023; Xiao et al., 2023; Jin et al., 2024) designed for attention mechanisms are constrained by quadratic computational complexity or insufficient context extrapolation performance, particularly when evaluated under perplexity metrics. In this paper, we introduce SAMBA, a simple neural architecture that harmonizes the strengths of both the SSM and the attention-based models, while achieving a potentially infinite length extrapolation with linear time complexity. SAMBA combines SSMs with attention through layer-wise interleaving

054 Mamba (Gu & Dao, 2023), SwiGLU (Shazeer, 2020), and Sliding Window Attention (SWA) (Beltagy 055 et al., 2020). Mamba layers capture the time-dependent semantics and provide a backbone for efficient 056 decoding, while SWA fills in the gap modeling complex, non-recurrent dependencies. A detailed 057 discussion of related work is included in Appendix A.

We scale SAMBA with 421M, 1.3B, 1.7B and up to 3.8B parameters with 3.2T tokens. In particular, 059 the largest 3.8B post-trained model achieves a 47.9 score for MMLU-Pro (Hendrycks et al., 2021), 060 70.1 for HumanEval (Chen et al., 2021), and 86.4 for GSM8K (Cobbe et al., 2021), substantially 061 outperforming strong open source language models up to 8B parameters, as detailed in Table 8. 062 Despite being pre-trained in the 4K sequence length, SAMBA can be extrapolated to 1M length in zero 063 shot with improved perplexity on Proof-Pile (Zhangir Azerbayev & Piotrowski, 2022), achieving a 064 $256 \times$ extrapolation ratio, while still maintaining the linear decoding time complexity with unlimited token streaming, as shown in Figure 2. We show that when instruction-tuned in a 4K context length 065 with only 500 steps, SAMBA can be extrapolated to a 256K context length with perfect memory recall 066 in Passkey Retrieval (Mohtashami & Jaggi, 2023). In contrast, the fine-tuned SWA-based model 067 simply cannot recall memories beyond 4K length. We further demonstrate that the instruction-tuned 068 SAMBA 3.8B model can achieve significantly better performance than the SWA-based models on 069 downstream long-context summarization tasks, while still keeping its impressive performance on 070 the short-context benchmarks. In a more challenging multiple key-value retrieval task, Phonebook 071 (Jelassi et al., 2024), we demonstrate that instruction fine-tuning enables SAMBA to bridge the retrieval 072 performance gap with full-attention models, while exhibiting significantly better extrapolation ability 073 when retrieving phone numbers beyond the training context length. Finally, we perform extensive 074 analyzes and ablation studies across model sizes up to 1.7B parameters to validate the architectural 075 design of SAMBA. We also offer potential explanations for the effectiveness of our simple hybrid approach through the lens of attention/selection entropy. To the best of our knowledge, Samba 076 is the first hybrid model showing that linear complexity models can be substantially better than 077 state-of-the-art Transformer models on short-context tasks at large scale, while still being able to extrapolate to extremely long sequences under the perplexity metric. 079

080 081

082 083

084

085

086

087

088

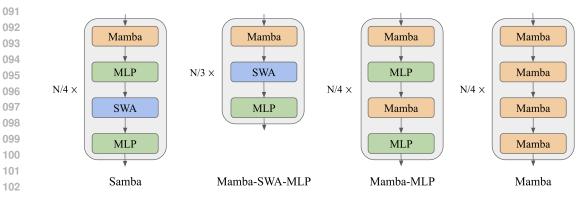
089

090 091

095

2 METHODOLOGY

We explore different hybridization strategies consisting of the layers of Mamba, Sliding Window Attention (SWA), and Multi-Layer Perceptron (Shazeer, 2020; Dauphin et al., 2016). We conceptualize the functionality of Mamba as the capture of recurrent sequence structures, SWA as the precise retrieval of memory, and MLP as the recall of factual knowledge. We also explore other linear recurrent layers including Multi-Scale Retention (Sun et al., 2023) and GLA (Yang et al., 2023) as potential substitutions for Mamba in Section 3.2. Our goal of hybridization is to harmonize between these distinct functioning blocks and find an efficient architecture for language modeling with unlimited length extrapolation ability.



103 Figure 1: From left to right: Samba, Mamba-SWA-MLP, Mamba-MLP, and Mamba. The illustrations 104 depict the layer-wise integration of Mamba with various configurations of Multi-Layer Perceptrons 105 (MLPs) and Sliding Window Attention (SWA). We assume the total number of intermediate layers to 106 be N, and omit the embedding layers and output projections for simplicity. Pre-Norm (Xiong et al., 2020; Zhang & Sennrich, 2019) and skip connections (He et al., 2016) are applied for each of the 107 intermediate layers.

108 2.1 ARCHITECTURE

As illustrated in Figure 1, we explore three kinds of layerwise hybridization strategies on the 1.7B
scale: Samba, Mamba-SWA-MLP, and Mamba-MLP. We also explore other hybridization approaches
with full self-attention on smaller scales in Section 4. The number of layers N is set to 48 for Samba,
Mamba-MLP, and Mamba, while Mamba-SWA-MLP has 54 layers, so each model has approximately
1.7B parameters. We only modify the layer-level arrangement for each of the models and keep every
other configuration the same to have apple-to-apple comparisons. More details on the configuration
of each layer are explained in the following subsections.

117 118

124

125

126

127 128 129

134

135

2.1.1 MAMBA LAYER

Mamba (Gu & Dao, 2023) is a recently proposed SSM-based model with selective state spaces. It enables input-dependent gating to both the recurrent states and the input representation for a soft selection of the input sequence elements. Given an input sequence representation $\mathbf{X} \in \mathbb{R}^{n \times d_m}$, where *n* is the length of the sequence and d_m is the hidden size, Mamba first expands the inputs to a higher dimension d_e , *i.e.*,

$$\mathbf{H} = \mathbf{X} \mathbf{W}_{\text{in}} \in \mathbb{R}^{n \times d_e}$$

where $\mathbf{W}_{in} \in \mathbb{R}^{d_m \times d_e}$ is a learnable projection matrix. Then a Short Convolution (SC) (Poli et al., 2023) operator is applied to smooth the input signal,

$$\mathbf{U} = \mathrm{SC}(\mathbf{H}) = \mathrm{SiLU}(\mathrm{DepthwiseConv}(\mathbf{H}, \mathbf{W}_{\mathrm{conv}})) \in \mathbb{R}^{n \times d_e}$$
(1)

where $\mathbf{W}_{conv} \in \mathbb{R}^{k \times d_e}$ and the kernel size k is set to 4 for hardware-aware efficiency. The Depthwise Convolution (He et al., 2019) is applied over the sequence dimension followed by a SiLU (Elfwing et al., 2017) activation function. The selective gate is then calculated through a low-rank projection followed by Softplus (Zheng et al., 2015),

$$\Delta = \text{Softplus}(\mathbf{U}\mathbf{W}_{r}\mathbf{W}_{q} + \mathbf{b}) \in \mathbb{R}^{n \times d_{e}}$$
(2)

where $\mathbf{W}_{r} \in \mathbb{R}^{d_{e} \times d_{r}}$, $\mathbf{W}_{q} \in \mathbb{R}^{d_{r} \times d_{e}}$ and d_{r} is the low-rank dimension. $\mathbf{b} \in \mathbb{R}^{d_{e}}$ is carefully initialized so that $\Delta \in [\Delta_{\min}, \Delta_{\max}]$ after the initialization stage. We set $[\Delta_{\min}, \Delta_{\max}] = [0.001, 0.1]$, and find that these values are not sensitive to language modeling performance under the perplexity metric. The input dependence is also introduced for the parameters **B** and **C** of SSM,

$$\mathbf{B} = \mathbf{U}\mathbf{W}_{\mathrm{b}} \ \in \mathbb{R}^{n imes d_s}$$
 $\mathbf{C} = \mathbf{U}\mathbf{W}_{\mathrm{c}} \ \in \mathbb{R}^{n imes d_s}$

140

where d_s is the state dimension. For each time step $1 \le t \le n$, the recurrent inference of the Selective SSM (S6) is performed in an expanded state space $\mathbf{Z}_t \in \mathbb{R}^{d_e \times d_s}$, *i.e.*,

$$\mathbf{Z}_t = \exp(-\Delta_t \odot \exp(\mathbf{A})) \odot \mathbf{Z}_{t-1} + \Delta_t \odot (\mathbf{B}_t \otimes \mathbf{U}_t) \in \mathbb{R}^{d_e \times d_s}$$

147 148 149

146

 $\mathbf{Y}_t = \mathbf{Z}_t \mathbf{C}_t + \mathbf{D} \odot \mathbf{U}_t \ \in \mathbb{R}^{d_e}$

where $\mathbf{Z}_0 = \mathbf{0}$, \odot means the point-wise product, \otimes means the outer product and exp means the point-wise natural exponential function. $\mathbf{D} \in \mathbb{R}^{d_e}$ is a learnable vector initialized as $D_i = 1$ and $\mathbf{A} \in \mathbb{R}^{d_e \times d_s}$ is a learnable matrix initialized as $A_{ij} = \log(j), 1 \le j \le d_s$, following the S4D-Real (Gu et al., 2022) initialization. In practice, Mamba implements a hardware-aware parallel scan algorithm for efficient parallelizable training. The final output is obtained through a gating mechanism similar to Gated Linear Unit (Shazeer, 2020; Dauphin et al., 2016),

156 157

$$\mathbf{O} = \mathbf{Y} \odot \operatorname{SiLU}(\mathbf{X}\mathbf{W}_{g})\mathbf{W}_{\operatorname{out}} \in \mathbb{R}^{n \times d_{m}}$$

where $\mathbf{W}_g \in \mathbb{R}^{d_m \times d_e}$ and $\mathbf{W}_{out} \in \mathbb{R}^{d_e \times d_m}$ are learnable parameters. In this work, we set $d_e = 2d_m$, $d_r = d_m/16$, and $d_s = 16$. The Mamba layer in SAMBA is expected to capture the time-dependent semantics of the input sequence through its recurrent structure. The input selection mechanism in the Mamba layer enables the model to focus on relevant inputs, thereby allowing the model to memorize important information in the long term.

162 2.1.2 SLIDING WINDOW ATTENTION (SWA) LAYER

164 We include Sliding Window Attention (Beltagy et al., 2020) layers to address the limitations of Mamba layers in capturing non-recurrent dependencies in sequences. Our SWA layer operates 165 on a window size w = 2048 that slides over the input sequence, ensuring that the computational 166 complexity remains linear with respect to the sequence length. RoPE (Su et al., 2021) is applied 167 within the sliding window, with a base frequency of 10,000. By directly accessing the contents in 168 the context window through attention, the SWA layer can retrieve high-definition signals from the middle to short-term history that cannot be clearly captured by the recurrent states of Mamba. We 170 use FlashAttention 2 (Dao, 2023) for the efficient implementation of self-attention throughout this 171 work. We also choose the 2048 sliding window size for efficiency consideration; FlashAttention 2 172 has the same training speed as Mamba's selective parallel scan at the sequence length of 2048 based 173 on the measurements in (Gu & Dao, 2023).

174 175

2.1.3 MULTI-LAYER PERCEPTRON (MLP) LAYER

The MLP layers in SAMBA serve as the architecture's primary mechanism for nonlinear transformation and recall of factual knowledge (Dai et al., 2022). We use SwiGLU (Shazeer, 2020) for all the models trained in this paper and denote its intermediate hidden size as d_p . As shown in Figure 1, Samba applies separate MLPs for different types of information captured by Mamba and the SWA layers.

180 181 182

206

3 EXPERIMENTS AND RESULTS

183 We pre-train four SAMBA models with different parameter sizes, 421M, 1.3B, 1.7B and 3.8B, to investigate its performance across different scales. The details of the hyperparameters for the training 185 and architecture designs are shown in Table 12 of Appendix G. We also train other hybrid architectures as mentioned in Section 2.1, including the baseline Mamba (Gu & Dao, 2023), Llama-3 (MetaAI, 187 2024; Dubey et al., 2024), and Mistral (Jiang et al., 2023) architecture on a scale of around 1.7B, with 188 detailed hyperparameters in Table 11 of Appendix G. We do comprehensive downstream evaluations 189 on a wide range of benchmarks, focusing on four main capabilities of the models: commonsense 190 reasoning (ARC (Clark et al., 2018), PIQA (Bisk et al., 2020), WinoGrande (Sakaguchi et al., 191 2021), SIQA (Sap et al., 2019), language understanding (HellaSwag (Zellers et al., 2019), BoolQ 192 (Clark et al., 2019), OpenbookQA (Mihaylov et al., 2018), SQuAD (Rajpurkar et al., 2016), MMLU 193 (Hendrycks et al., 2021), MMLU-Pro (Wang et al., 2024), GPQA(Rein et al., 2023)), truthfulness (TruthfulQA (Lin et al., 2022)) and math and coding (GSM8K (Cobbe et al., 2021), MBPP (Austin 194 et al., 2021), HumanEval (Chen et al., 2021)). 195

Table 1: Downstream performance comparison between Samba-3.8B-IT (preview) and Phi-3-mini-4K
on both long-context and short-context tasks. We report 5-shot accuracy (averaged by category) for
MMLU, 8-shot CoT (Wei et al., 2022) for GSM8K, 0-shot pass@1 for HumanEval, ROUGE-L for
both GovReport and SQuALITY. † Results from the Phi-3 technical report (Abdin et al., 2024).

Model	MMLU	GSM8K	HumanEval	GovReport	SQuALITY
Phi-3-mini-4K-instruct †	68.8	82.5	58.5	14.4	21.6
Samba-3.8B-IT (preview)	71.9	87.6	62.8	18.9	21.2

3.1 LANGUAGE MODELING ON TEXTBOOK QUALITY DATA

207 We first present results from our largest 3.8B SAMBA model, trained on the same data set used by 208 Phi3 (Abdin et al., 2024) with 3.2T tokens. We follow the same multiphase pretraining strategy as 209 Phi3-mini, and apply both the original Phi-3-mini post-training recipe and the Phi3-mini-June-2024 210 recipe to produce our instruction-tuned SAMBA 3.8B models, i.e., Samba-3.8B-IT (preview) and 211 Samba-3.8B (June) respectively. We report comprehensive benchmark results of the Samba 3.8B 212 base model and Samba-3.8B (June) in Appendix B. As shown in Table 1, we evaluate the downstream 213 performance of Samba-3.8B-IT (preview) on both long-context summarization tasks (GovReport (Huang et al., 2021), SQuALITY (Wang et al., 2022)) and major short-context benchmarks (MMLU, 214 GSM8K, HumanEval). We can see that Samba has substantially better performance than Phi-3-mini-215 4k-instruct on both the short-context (MMLU, GSM8K, HumanEval) and long-context (GovReport) tasks, while still having the 2048 window size of its SWA layer and maintaining the linear complexity
 for efficient processing of long documents. Details of data statistics and evaluation setup for long
 context tasks are included in Appendix F.

Table 2: Downstream evaluation of the architectures trained on 230B tokens of the Phi2 dataset.
We report the unnormalized accuracy for multiple choice tasks. GSM8K is evaluated with 5-shot
examples while other tasks are in zero-shot. Best results are in bold, second best underlined.

Benchmark	Llama-3 1.6B	Mistral 1.6B	Mamba 1.8B	Mamba-SWA-MLP 1.6B	Mamba-MLP 1.9B	Samba 1.7B
ARC-Easy	76.85	77.02	77.99	76.68	78.91	79.25
ARC-Challenge	43.26	44.20	45.22	46.16	47.35	48.21
PIQA	76.66	75.79	77.31	76.50	78.84	77.10
WinoGrande	70.01	70.72	73.40	73.72	72.38	72.93
SIQA	51.23	52.00	53.12	55.12	54.30	53.68
HellaSwag	46.98	47.19	49.80	49.71	50.14	49.74
BoolQ	68.20	70.70	74.83	74.74	73.70	75.57
OpenbookQA	34.00	32.80	36.60	33.80	35.40	37.20
SQuAD	74.88	72.82	67.66	<u>76.73</u>	63.86	77.64
MMLU	43.84	43.54	45.28	<u>47.39</u>	43.68	48.01
TruthfulQA (MC1)	25.70	25.09	26.81	26.20	26.44	27.78
TruthfulQA (MC2)	40.35	38.80	40.66	40.80	40.04	41.62
GSM8K	32.68	32.45	32.07	44.05	27.52	38.97
MBPP	46.30	47.08	47.86	47.08	47.08	48.25
HumanEval	36.59	36.59	35.98	<u>37.80</u>	31.10	39.02
Average	51.17	51.12	52.31	<u>53.77</u>	51.38	54.33

To examine the different hybridization strategies mentioned in Section 2.1, we train 6 models with around 1.7B parameters on the Phi2 (Li et al., 2023) dataset with 230B tokens and evaluate them in the full suite of 15 downstream benchmarks to have a holistic assessment of hybrid and purebred architectures. As shown in Table 2, SAMBA demonstrates superior performance on a diverse set of tasks, including commonsense reasoning (ARC-Challenge), language understanding (MMLU, SQuAD), TruthfulQA and code generation (HumanEval, MBPP). It outperforms both the pure attention-based and SSM-based models in most tasks and achieves the best average performance. By comparing the performance of Mamba-MLP and Mamba in Table 2, we can observe that replacing Mamba blocks with MLPs does not harm common sense reasoning ability, but its performance in language understanding and complex reasoning ability, such as coding and mathematical reasoning, degenerates significantly. We can also see that pure Mamba models fall short on retrieval intensive tasks such as SQuAD due to their lack of precise memory retrieval ability. The best results are achieved through the combination of the attention and Mamba modules, as shown with our Samba architecture. We can also notice that Mamba-SWA-MLP has significantly better performance on GSM8K, potentially resulting from a closer collaboration between the Mamba and the SWA layers. The distinct downstream performances of different hybridization strategies pose interesting future work for developing task-adaptive dynamic architectures.

3.2 EXPLORATION ON HYBRIDIZING ATTENTION AND LINEAR RECURRENCE

Since SSMs belong to a broader realm of linear recurrent models (Orvieto et al., 2023; Qin et al., 2023; Yang et al., 2023; Katsch, 2023; Qin et al., 2024), there exist multiple alternatives other
than Mamba when combing attention-based layers with recurrent neural networks. We also add
architecture ablation studies to justify the design choices of Samba. Specifically, in addition to
Llama-2, Mamba, Samba and Mamba-SWA-MLP, we investigate the comparative analysis of the
following architectures:

- Llama-2-SWA is a pure attention-based architecture that replaces all full attention layers in Llama-2 with sliding window attention.

270Table 3: Perplexity on the validation set of SlimPajama for different attention and linear recurrent271model architectures trained at 4,096 context length. We use window size 2,048 for Sliding Window272Attention (SWA). The perplexity results have a fluctuation around $\pm 0.3\%$.

274	Architecture	Size	Layers	Training Speed $(\times 10^5 \text{ tokens/s})$	Validat 4096	tion Cont 8192	ext Length 16384
275 276		0.414	CDU	(×10 tokelis/s)	4090	0192	10384
277	20B training tokens o	$n 8 \times AI0$	00 GPUs				
278	Llama-2	438M	24	4.85	11.14	47.23	249.03
	Llama-2-SWA	438M	24	4.96	11.12	10.66	10.57
279	Mamba	432M	60	2.46	10.70	10.30	10.24
280	Sliding GLA	438M	24	4.94	10.43	10.00	9.92
281	Sliding RetNet	446M	24	4.32	10.38	9.96	9.87 12.25
82	Mega-S6 Mamba-SWA-MLP	422M 400M	24 24	3.26 4.21	12.63 10.07	12.25 9.67	12.25 9.59
283	MLP-SWA-MLP	400M 417M	24 24	4.21 5.08	10.07	9.07 10.50	10.41
284	SAMBA-NoPE	421M	24	4.48	10.95	28.97	314.78
285	SAMBA	421M	24	4.46	10.06	9.65	9.57
86							
287	100B training tokens	$On 04 \times r$					
88	Llama-2	1.3B	40	25.9	7.60	44.32	249.64
	Llama-2-SWA	1.3B	40	26.2	7.60	7.37	7.21
289	Mamba	1.3B	48	17.8	7.47	7.26	7.15
90	Sliding GLA	1.2B	36	25.9	7.58	7.35	7.19
91	Sliding RetNet	1.4B	36	23.0	7.56	7.35	7.56
92	Mega-S6	1.3B	36	17.9	9.01	8.81	8.68
93	Mamba-SWA-MLP	1.3B	36	23.5	7.37	7.16	7.00
94	MLP-SWA-MLP	1.3B	36	26.6	7.81	7.58	7.42
	SAMBA-NOPE	1.3B	36	25.2	7.33	20.40	326.17
95	SAMBA	1.3B	36	25.2	7.32	7.11	6.96
u 6							
.50					4 4		
	Sliding RetNet rep						
97	(Sun et al., 2023) I	ayers. R	etNet is a	linear attention mo			
296 297 298 299		ayers. R	etNet is a	linear attention mo			
97 98 99	(Sun et al., 2023) I	ayers. R the recu	etNet is a larrent hidd	linear attention mo en states.	del with	fixed and	d input-indepen
97 98 99 00	(Sun et al., 2023) I.decay applying toSliding GLA repla	ayers. R the recu aces Mar	etNet is a l irrent hidd mba layers	linear attention mo en states. in the Samba arch	del with	fixed and with Gat	d input-indepen ed Linear Atter
97 98 99 600 601	(Sun et al., 2023) I decay applying to • Sliding GLA repla (GLA) (Yang et a	ayers. R the recu aces Mar al., 2023	etNet is a l irrent hidd mba layers	linear attention mo en states. in the Samba arch	del with	fixed and with Gat	d input-indepen ed Linear Atter
297 298 299 800 801 802	 (Sun et al., 2023) I. decay applying to Sliding GLA replation (GLA) (Yang et a input-dependent g 	ayers. R the recu aces Mar al., 2023 ating.	etNet is a l irrent hidd mba layers 3). GLA i	linear attention mo en states. in the Samba arch is a more express	del with nitecture ive vari	fixed and with Gat ant of lin	d input-indepen ed Linear Atter near attention
297 298 299 300 301 302 303	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces 	ayers. R the recu aces Mar al., 2023 ating. all MD-	etNet is a l irrent hidd mba layers B). GLA i EMA mod	linear attention mo en states. in the Samba arch is a more express lules in the Mega (del with nitecture ive vari Ma et al	with Gat ant of lin ., 2023) a	d input-indepen ed Linear Atter near attention rchitecture with
297 298 299 300 301 302 303 304	 (Sun et al., 2023) I. decay applying to Sliding GLA replation (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 complexity (Substance) 	ayers. R the recu aces Man al., 2023 ating. all MD- nbinatio	etNet is a l urrent hidd mba layers 3). GLA i EMA mod ns from M	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg	del with nitecture ive vari Ma et al ga to the	i fixed and with Gat ant of lin ., 2023) a modern l	d input-indepen ed Linear Atter near attention urchitecture with Mamba architec
97 98 99 00 01 02 03 04	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 con Rotary position en 	ayers. R the recu aces Mar al., 2023 ating. all MD- nbinatio nbedding	etNet is a l irrent hidd mba layers B). GLA i EMA mod ns from M g, RMSNo	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a	del with nitecture ive vari Ma et al ga to the ttention	i fixed and with Gat ant of lin ., 2023) a modern l are also	d input-indepen ed Linear Atter near attention urchitecture with Mamba architec adopted. We se
97 98 99 00 01 02 03 04 05	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 cor Rotary position en intermediate dimendiate d	ayers. R the recu aces Man al., 2023 ating. all MD- mbinatio nbedding nsion of	etNet is a l irrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega-	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg rm and Softmax a S6 layer to be d_m	del with itecture ive vari Ma et al ga to the ttention so that i	i fixed and with Gat ant of lin ., 2023) a modern l are also a it has a ro	d input-indepen ed Linear Atter near attention urchitecture with Mamba architec adopted. We se bughly $5d_m^2$ nur
97 98 99 00 01 02 03 04 05 06	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 cor Rotary position en intermediate dimen of parameters. T 	ayers. R the recu aces Matal., 2023 ating. all MD- nbinatio nbedding nsion of his repr	etNet is a l mrent hidd mba layers B). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg rm and Softmax a S6 layer to be d_m	del with itecture ive vari Ma et al ga to the ttention so that i	i fixed and with Gat ant of lin ., 2023) a modern l are also a it has a ro	d input-indepen ed Linear Atter near attention urchitecture with Mamba architec adopted. We se bughly $5d_m^2$ nur
97 98 99 00 01 02 03 04 05 06 07	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 cor Rotary position en intermediate dimendiate d	ayers. R the recu aces Matal., 2023 ating. all MD- nbinatio nbedding nsion of his repr	etNet is a l mrent hidd mba layers B). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg rm and Softmax a S6 layer to be d_m	del with itecture ive vari Ma et al ga to the ttention so that i	i fixed and with Gat ant of lin ., 2023) a modern l are also a it has a ro	d input-indepen ed Linear Atter near attention urchitecture with Mamba architec adopted. We se bughly $5d_m^2$ nur
97 98 99 00 01 02 03 04 05 06 07 08	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 con Rotary position en intermediate dimen of parameters. TI SSM-Attention hy 	ayers. R the recu aces Mar al., 2023 ating. all MD- nbinatio nbedding nsion of his repr	etNet is a larrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion.	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a S6 layer to be d_m lassical baseline to	del with nitecture ive vari Ma et al ga to the ttention so that i that con	with Gat ant of lin ., 2023) a modern l are also a it has a re ducts see	d input-independent red Linear Atternear attention architecture with Mamba architectadopted. We se bughly $5d_m^2$ nur quential intra-l
97 98 99 00 01 02 03 04 05 06 07 08 09	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 corr Rotary position en intermediate dimentof parameters. The SSM-Attention hy MLP-SWA-MLP 	ayers. R the recu aces Mar al., 2023 ating. all MD- nbinatio nbedding nsion of his repr vbridizat replace	etNet is a l arrent hidd mba layers B). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a \cdot S6 layer to be d_m lassical baseline to nba layers in the	del with nitecture ive vari Ma et al ga to the ttention so that i that con	with Gat ant of lin ., 2023) a modern l are also a it has a re ducts see	d input-independent red Linear Atternear attention architecture with Mamba architectadopted. We se bughly $5d_m^2$ nur quential intra-l
97 98 99 00 01 02 03 04 05 06 07 08 09 10	 (Sun et al., 2023) I. decay applying to Sliding GLA replation (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 correst Rotary position en intermediate dimention of parameters. The SSM-Attention hy MLP-SWA-MLP SwiGLU layers were stated of the stated st	ayers. R the recu aces Man al., 2023 ating. all MD- nbinatio nbedding nsion of his repr bridizat replace ith $6d_m^2$	etNet is a l arrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a S6 layer to be d_m lassical baseline to nba layers in the f parameters.	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba	ifixed and with Gat ant of lin ., 2023) a modern l are also it has a ro ducts sec -SWA-M	d input-independent ed Linear Atternear attention urchitecture with Mamba architectadopted. We sepughly $5d_m^2$ nur quential intra-l
97 98 99 00 01 02 03 04 05 06 07 08 09 10	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 corr Rotary position en intermediate dimen of parameters. The SSM-Attention hy MLP-SWA-MLP SwiGLU layers w Samba-NoPE rem 	ayers. R the recu aces Mar al., 2023 ating. all MD- nbinatio nbeddin nsion of his repr bridizat replace ith $6d_m^2$ noves the	etNet is a larrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a cS6 layer to be d_m lassical baseline to nba layers in the f parameters. lative position eml	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba	ifixed and with Gat ant of lin ., 2023) a modern l are also it has a ro ducts sec -SWA-M	d input-independent ed Linear Atternear attention urchitecture with Mamba architectadopted. We sepughly $5d_m^2$ nur quential intra-l
97 98 99 00 01 02 03 04 05 06 07 08 09 10 11	 (Sun et al., 2023) I. decay applying to Sliding GLA replation (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 correst Rotary position en intermediate dimention of parameters. The SSM-Attention hy MLP-SWA-MLP SwiGLU layers were stated of the stated st	ayers. R the recu aces Mar al., 2023 ating. all MD- nbinatio nbeddin nsion of his repr bridizat replace ith $6d_m^2$ noves the	etNet is a larrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a cS6 layer to be d_m lassical baseline to nba layers in the f parameters. lative position eml	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba	ifixed and with Gat ant of lin ., 2023) a modern l are also it has a ro ducts sec -SWA-M	d input-independent ed Linear Atternear attention urchitecture with Mamba architectadopted. We sepughly $5d_m^2$ nur quential intra-l
97 98 99 00 01 02 03 04 05 06 07 08 09 10 11	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 corr Rotary position en intermediate dimen of parameters. TI SSM-Attention hy MLP-SWA-MLP SwiGLU layers w. Samba-NoPE ren any position embe 	ayers. R the recu aces Mar al., 2023 ating. all MD- nbinatio nbedding nsion of his repr 'bridizat replace ith $6d_m^2$ noves the edding in	etNet is a larrent hidd mba layers 3). GLA is EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re n the archit	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a S6 layer to be d_m lassical baseline to nba layers in the f parameters. lative position eml recture.	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba bedding	fixed and with Gat ant of lin ., 2023) a modern l are also a it has a re ducts see -SWA-M in Samba	d input-indepen red Linear Atter near attention urchitecture with Mamba architect adopted. We se bughly $5d_m^2$ nur quential intra-l ILP architectur a and does not l
97 98 99 00 01 02 03 04 05 06 07 08 09 10 11 12 13	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 corr Rotary position en intermediate dimen of parameters. TI SSM-Attention hy MLP-SWA-MLP SwiGLU layers w. Samba-NoPE ren any position embe 	ayers. R the recu aces Mar al., 2023 ating. all MD- nbinatio nbedding nsion of his repr bridizat replace ith $6d_m^2$ hoves the edding in	etNet is a larrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re n the archit e SlimPaja	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a S6 layer to be d_m lassical baseline to nba layers in the f parameters. lative position eml recture.	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba bedding al., 2023	i fixed and with Gat ant of lin ., 2023) a modern l are also a it has a ro ducts sed -SWA-M in Samba	d input-independent red Linear Atternear attention urchitecture with Mamba architect adopted. We see bughly $5d_m^2$ nur quential intra-l ILP architectur a and does not h
97 98 99 00 01 02 03 04 05 06 07 08 09 10 11 12 13 14	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 corr Rotary position en intermediate dimen of parameters. TI SSM-Attention hy MLP-SWA-MLP SwiGLU layers w. Samba-NoPE ren any position embe We pre-train all models on 438M and 1.3B settings, and 	ayers. R the recu aces Mar al., 2023 ating. all MD- mbinatio nbedding nsion of his repr bridizat replace ith $6d_m^2$ noves the edding in the sam	etNet is a l arrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re n the archit e SlimPaja iate these n	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a S6 layer to be d_m lassical baseline to nba layers in the f parameters. lative position eml recture.	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba bedding al., 2023 ting per	ifixed and with Gat ant of lin ., 2023) a modern l are also a it has a ro ducts sed -SWA-M in Samba 8) dataset plexity o	d input-independent red Linear Atternear attention architecture with Mamba architect adopted. We see bughly $5d_m^2$ nur- quential intra-l ILP architectur a and does not have cunder both arconthe the the the the the the the the the
97 98 99 00 01 02 03 04 05 06 07 08 09 10 11 12 13 14 15	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 corr Rotary position en intermediate dimen of parameters. TI SSM-Attention hy MLP-SWA-MLP SwiGLU layers w Samba-NoPE rem any position embe We pre-train all models on 438M and 1.3B settings, at with context length at 4096, 	ayers. R the recu aces Mar al., 2023 ating. all MD- mbinatio nbedding nsion of his repr bridizat replace ith $6d_m^2$ noves the edding in the sam nd evalu 8192, at	etNet is a l arrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of a the archit e SlimPaja late these i nd 16384 t	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a S6 layer to be d_m lassical baseline to nba layers in the f parameters. lative position eml recture. ama (Soboleva et a nodels by calcula okens to investigat	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba bedding al., 2023 ting per e their z	ifixed and with Gat ant of lin ., 2023) a modern l are also a it has a ro ducts sed -SWA-M in Samba 8) dataset plexity o ero-shot l	d input-indepen ed Linear Atter near attention urchitecture with Mamba architect adopted. We se bughly $5d_m^2$ nur quential intra-l ILP architectur a and does not l under both arcontectur n the validation
97 98 99 00 01 02 03 04 05 06 07 08 09 10 11 12 13 14 15 16	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 corr Rotary position en intermediate dimen of parameters. TI SSM-Attention hy MLP-SWA-MLP SwiGLU layers w Samba-NoPE rem any position embe We pre-train all models on 438M and 1.3B settings, ar with context length at 4096, ability. Peak training through the set of the set of	ayers. R the recu aces Mar al., 2023 ating. all MD- mbinatio nbedding nsion of his repr bridizat replace ith $6d_m^2$ noves the edding in the sam nd evalu 8192, at bughput	etNet is a l mrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re the archit e SlimPaja late these f nd 16384 t is also m	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a \cdot S6 layer to be d_m lassical baseline to nba layers in the f parameters. lative position eml fecture. ama (Soboleva et a models by calcula okens to investigat easured as an eff	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba bedding al., 2023 ting per e their z iciency	ifixed and with Gat ant of lin ., 2023) a modern l are also a it has a ro ducts see -SWA-M in Samba B) dataset plexity o ero-shot l metric.	d input-indepen ed Linear Atter near attention urchitecture with Mamba architec adopted. We se oughly $5d_m^2$ nur quential intra-1 ILP architectur a and does not l under both arco n the validation length extrapola The details of
97 98 99 00 01 02 03 04 05 06 07 08 09 10 11 12 13 14 15 16 17	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 corr Rotary position en intermediate dimen of parameters. TI SSM-Attention hy MLP-SWA-MLP SwiGLU layers w Samba-NoPE ren any position embe We pre-train all models on 438M and 1.3B settings, ar with context length at 4096, ability. Peak training through the settings of the set settings of the settings of the settings	ayers. R the recu aces Mar al., 2023 ating. all MD- mbinatio nbedding nsion of his repr bridizat replace ith $6d_m^2$ noves the edding in the sam nd evalu 8192, at pughput	etNet is a l mrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re the archit e SlimPaja ate these i nd 16384 t is also m led in App	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a \cdot S6 layer to be d_m lassical baseline to nba layers in the f parameters. lative position eml fecture. ama (Soboleva et a models by calcula okens to investigat easured as an eff pendix G. As show	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba bedding al., 2023 ting per e their z iciency wn in Ta	ifixed and with Gat ant of lin ., 2023) a modern l are also a it has a ro ducts see -SWA-M in Samba B) dataset plexity o ero-shot l metric. able 3, S	d input-indepen ed Linear Atter near attention urchitecture with Mamba architec adopted. We se oughly $5d_m^2$ nur quential intra-1 ILP architectur a and does not l under both arco n the validation length extrapola The details of AMBA consiste
97 98 99 00 01 02 03 04 05 06 07 08 09 10 11 12 13 14 15 16 17 18	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 corr Rotary position en intermediate dimen of parameters. The SSM-Attention hy MLP-SWA-MLP SwiGLU layers w Samba-NoPE rem any position embe We pre-train all models on 438M and 1.3B settings, ar with context length at 4096, ability. Peak training through the pre-train all other models are outperforms all other models on the settings of the settings ar outperforms all other models on the settings of the settings ar outperforms all other models on the settings are outperformed and the settings are outperformed and the settings are settings are outperformed and the settings are settings are settings and the settings are settings are settings and the settings are settings and the set times are settings are s	ayers. R the recu aces Mar al., 2023 ating. all MD- nbinatio nbedding nsion of his repr bridizat replace ith $6d_m^2$ noves the adding in the sam nd evalu 8192, ar bughput re incluce	etNet is a l mrent hidd mba layers B). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re n the archit e SlimPaja ate these n nd 16384 t is also m led in App fferent co	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg rm and Softmax a $S6$ layer to be d_m lassical baseline to nba layers in the f parameters. lative position emb recture. ama (Soboleva et a models by calcula okens to investigat easured as an eff pendix G. As show ntext lengths and	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba bedding al., 2023 ting per e their z iciency wn in Ta model s	ifixed and with Gat ant of lin ., 2023) a modern l are also a ducts see -SWA-M in Samba B) dataset plexity o ero-shot l metric. able 3, S sizes. Th	d input-independent ed Linear Atternear attention urchitecture with Mamba architecture with Mamba architecture adopted. We see bughly $5d_m^2$ nur quential intra-l ILP architecture a and does not l cunder both arcon length extrapola The details of AMBA consisted e training spee
97 98 99 00 01 02 03 04 05 06 07 08 09 10 11 12 13 14 15 16 17 18	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 corr Rotary position en intermediate dimen of parameters. TI SSM-Attention hy MLP-SWA-MLP SwiGLU layers w Samba-NoPE ren any position embe We pre-train all models on 438M and 1.3B settings, ar with context length at 4096, ability. Peak training through the settings of the set settings of the settings of the settings	ayers. R the recu aces Mar al., 2023 ating. all MD- nbinatio nbedding nsion of his repr bridizat replace ith $6d_m^2$ noves the adding in the sam nd evalu 8192, ar bughput re incluce	etNet is a l mrent hidd mba layers B). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re n the archit e SlimPaja ate these n nd 16384 t is also m led in App fferent co	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg rm and Softmax a $S6$ layer to be d_m lassical baseline to nba layers in the f parameters. lative position emb recture. ama (Soboleva et a models by calcula okens to investigat easured as an eff pendix G. As show ntext lengths and	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba bedding al., 2023 ting per e their z iciency wn in Ta model s	ifixed and with Gat ant of lin ., 2023) a modern l are also a ducts see -SWA-M in Samba B) dataset plexity o ero-shot l metric. able 3, S sizes. Th	d input-independent ed Linear Atternear attention urchitecture with Mamba architecture with Mamba architecture adopted. We see bughly $5d_m^2$ nur quential intra-l ILP architecture a and does not l cunder both arcon length extrapola The details of AMBA consisted e training spee
97 98 99 00 01 02 03 04 05 06 07 08 09 10 11 12 13 14 15 16 17 18	 (Sun et al., 2023) I. decay applying to Sliding GLA repla (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 corr Rotary position en intermediate dimen of parameters. The SSM-Attention hy MLP-SWA-MLP SwiGLU layers w Samba-NoPE rem any position embe We pre-train all models on 438M and 1.3B settings, ar with context length at 4096, ability. Peak training through the pre-train all other models are outperforms all other models on the settings of the settings ar outperforms all other models on the settings of the settings ar outperforms all other models on the settings are outperformed and the settings are outperformed and the settings are settings are outperformed and the settings are settings are settings and the settings are settings are settings and the settings are settings and the set times are settings are s	ayers. R the recu aces Man al., 2023 ating. all MD- nbinatio nbedding nsion of his repr bridizat replace ith $6d_m^2$ noves the adding in the sam nd evalu 8192, a pughput e include els in di npared to	etNet is a l arrent hidd mba layers B). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re n the archit e SlimPaja tate these r nd 16384 t is also m led in App fferent co o pure Tran	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg rm and Softmax a S6 layer to be d_m lassical baseline to nba layers in the f parameters. lative position emb recture. ama (Soboleva et a models by calcula okens to investigat easured as an eff pendix G. As show ntext lengths and nsformer-based mo	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba bedding al., 2023 ting per e their z iciency wn in Ta model s odels on	ifixed and with Gat ant of lin ., 2023) a modern l are also a it has a ro ducts see -SWA-M in Samba B) dataset plexity o ero-shot l metric. able 3, S sizes. Th the 1.3E	d input-independent ed Linear Atternear attention urchitecture with Mamba architect adopted. We see bughly $5d_m^2$ nur quential intra-l ILP architectur a and does not l under both architectur and
97 98 99 00 01 02 03 04 05 06 07 08 09 10 11 12 13 14 15 16 17 18 19 20	 (Sun et al., 2023) I. decay applying to Sliding GLA replation (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 correst Rotary position en intermediate dimention of parameters. The SSM-Attention hy MLP-SWA-MLP SwiGLU layers www. Samba-NoPE remains any position embetwith context length at 4096, ability. Peak training three hyperparameter settings aroutperforms all other mode SAMBA is competitive correst significantly worse training the set of set of the set of the	ayers. R the recu aces Man al., 2023 ating. all MD- nbinatio nbedding nsion of his repr bridizat replace ith $6d_m^2$ noves the adding in the sam nd evalue 8192, an oughput e include els in di npared to through	etNet is a l arrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re a the archit e SlimPaja tate these n nd 16384 t is also m led in App fferent co o pure Tran put becaus	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg rm and Softmax a S6 layer to be d_m lassical baseline to nba layers in the f parameters. lative position emb recture. ama (Soboleva et a models by calcula okens to investigat easured as an eff pendix G. As show ntext lengths and nsformer-based mose Mamba layers h	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba bedding al., 2023 ting per e their z iciency wn in Ta model s odels on ave slow	ifixed and with Gat ant of lin ., 2023) a modern l are also a it has a re ducts see -SWA-M in Samba B) dataset plexity o ero-shot l metric. able 3, S sizes. Th the 1.3E wer traini	d input-independent ed Linear Atternear attention urchitecture with Mamba architect adopted. We see bughly $5d_m^2$ nur quential intra-l ILP architectur a and does not l under both architectur and consiste e training speed b scale. Mamba
97 98 99 99 90 90 90 90 90 90 90 90 90 90 90	 (Sun et al., 2023) I. decay applying to Sliding GLA replation (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 correst Rotary position en intermediate dimention of parameters. The SSM-Attention hy MLP-SWA-MLP SwiGLU layers were samba-NoPE remains any position ember with context length at 4096, ability. Peak training three hyperparameter settings are outperforms all other models consignificantly worse training layers, and the purebred M 	ayers. R the recu aces Man al., 2023 ating. all MD- nbinatio nbedding nsion of his repr bridizat replace ith $6d_m^2$ noves the edding in the sam nd evalue 8192, as oughput re incluce els in di npared to through	etNet is a l arrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re n the archit e SlimPaja iate these n nd 16384 t is also m led in App fferent co o pure Tran put becaus nodels nee	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg rm and Softmax a S6 layer to be d_m lassical baseline to nba layers in the f parameters. lative position emb eccture. ama (Soboleva et a models by calcula okens to investigat easured as an eff pendix G. As show ntext lengths and nsformer-based mose Mamba layers h	del with nitecture ive vari Ma et al ga to the ttention so that i that con Mamba bedding al., 2023 ting per e their z ficiency wn in Ta model s odels on ave slow	ifixed and with Gat ant of lin ., 2023) a modern I are also a it has a ro ducts see -SWA-M in Samba B) dataset plexity o ero-shot I metric. able 3, S sizes. Th the 1.3E wer traini an other I	d input-independent ed Linear Atternear attention urchitecture with Mamba architectadopted. We see bughly $5d_m^2$ nur quential intra-l ILP architectur a and does not l under both architectur and architectur and does not l under both architectur and architectur and does not l under both architectur and both architectur and architectur and does not l under both architectur and architectur and does not l under both architectur and architectu
97 98 99 99 90 90 90 90 90 90 90 90 90 90 90	 (Sun et al., 2023) I. decay applying to Sliding GLA replation (GLA) (Yang et a input-dependent g Mega-S6 replaces ShortConv+S6 correst Rotary position en intermediate dimention of parameters. The SSM-Attention hy MLP-SWA-MLP SwiGLU layers www. Samba-NoPE remains any position embetwith context length at 4096, ability. Peak training three hyperparameter settings aroutperforms all other mode SAMBA is competitive correst significantly worse training the set of set of the set of the	ayers. R the recu aces Man al., 2023 ating. all MD- mbinatio nbedding nsion of his repr bridizat replace ith $6d_m^2$ noves the adding in the sam nd evalu 8192, as oughput re incluce els in di npared to through famba n	etNet is a l arrent hidd mba layers 3). GLA i EMA mod ns from M g, RMSNo the Mega- esents a c ion. es all Mar number of e rotary re n the archit e SlimPaja iate these n nd 16384 t is also m led in App fferent co o pure Tran put becaus nodels nee g Mamba-	linear attention mo en states. in the Samba arch is a more express lules in the Mega (amba to adapt Meg orm and Softmax a S6 layer to be d_m lassical baseline to nba layers in the f parameters. lative position emb eccture. ama (Soboleva et a models by calcula okens to investigat easured as an eff pendix G. As show ntext lengths and nsformer-based mo se Mamba layers in the d to have more la SWA-MLP with	del with hitecture ive vari Ma et al ga to the ttention so that i that con Mamba bedding al., 2023 ting per e their z icinency wn in Ta model s odels on ave slow uyers tha Samba,	ifixed and with Gat ant of lin ., 2023) a modern 1 are also it has a ro ducts see -SWA-M in Samba B) dataset plexity o ero-shot 1 metric. able 3, S sizes. Th a the 1.3E wer traini an other 1 we can s	d input-independent ed Linear Atternear attention urchitecture with Mamba architectadopted. We see bughly $5d_m^2$ nur quential intra-l ILP architectur a and does not l under both arc n the validation length extrapola The details of AMBA consistent e training speed scale. Mamba ng speed than Manodels at the size that Samba

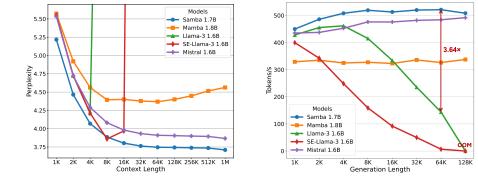
This also indicates that Mamba-SWA-MLP will have slower decoding speed than Samba due to larger total cache size resulting from more SSMs and Attention layers. We can further observe that replacing Mamba with MLP speeds up the training but harms perplexity significantly, indicating the importance of Mamba layers in the Samba architecture. Interestingly, even though we use SWA in Samba architecture, Samba-NoPE still has exploded perplexities beyond its training length without RoPE. We can also find that while RetNet can extrapolate well under the 438M scale, it has an increasing perplexity on 16K length at the 1.4B scale, which may indicate that its input-independent decay may need specific tuning at different scales to work well.

Table 4: Downstream evaluation of models pre-trained with 100B tokens from SlimPajama. We measure the character-normalized accuracy for HellaSwag following Gu & Dao (2023). All tasks are evaluated in zero-shot.

Architecture	Size	ARC-Easy acc ↑	HellaSwag acc_norm ↑	Wino. acc ↑	$\begin{array}{c} \mathbf{PIQA} \\ \mathbf{acc} \uparrow \end{array}$	LAMBADA acc ↑	Avg.
LLaMA-2	1.3B	55.09	52.32	53.35	71.11	48.52	56.08
LLaMA-2-SWA	1.3B	56.65	52.59	54.93	71.60	47.56	56.67
Sliding GLA	1.2B	56.94	52.52	56.75	71.38	48.17	57.15
Sliding RetNet	1.4B	57.66	52.64	56.75	71.33	48.34	57.34
Mega-S6	1.3B	50.63	41.91	52.96	68.17	37.88	50.31
Mamba	1.3B	58.08	54.93	53.99	71.98	45.97	56.99
Mamba-SWA-MLP	1.3B	59.64	54.50	55.25	72.42	49.12	58.19
MLP-SWA-MLP	1.3B	55.18	50.32	52.80	70.67	48.11	55.42
Samba-NoPE	1.3B	58.38	54.62	56.51	72.03	51.08	58.52
Samba	1.3B	58.21	<u>54.73</u>	55.72	<u>72.36</u>	51.68	58.54

In Table 4, we evaluate all our 1.3B scale models on five typical commonsense reasoning tasks (ARC-Easy, HellaSwag, WinoGrande, PIQA and the OpenAI variant ¹ of LAMBADA (Paperno et al., 2016)) to understand the effect of architecture designs on downstream performances. We can see that Samba has the best average accuracy, outperforming the LLaMA 2 architectures by a large margin. Similar to our perplexity evaluation, Samba and Samba-NoPE have similar average accuracies, whereas Mamba-SWA-MLP falls slightly behind. We observe that different architectures excel at different tasks. Mamba-SWA-MLP performs best on ARC-Easy, while Samba and Samba-NoPE achieve superior results on LAMBADA. Hybrid models based on Mamba generally outperform hybrid linear attention models and pure softmax-attention models on HellaSwag.

3.3 EFFICIENT LENGTH EXTRAPOLATION



(a) Perplexity on the test set of Proof-Pile

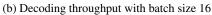


Figure 2: SAMBA shows improved prediction up to 1M tokens in the Proof-Pile test set while
achieving a 3.64× faster decoding throughput than the Llama-3 architecture on 64K generation
length. We also include an SE-Llama-3 1.6B baseline which applies the SelfExtend (Jin et al., 2024)
approach for zero-shot length extrapolation. All models are trained with 4K sequence length.

We use the test split of the Proof-Pile (Zhangir Azerbayev & Piotrowski, 2022) dataset to evaluate the length extrapolation ability of our models at a scale of around 1.7B parameters. We follow Position

¹https://huggingface.co/datasets/EleutherAI/lambada_openai

378 Interpolation (Chen et al., 2023a) for data pre-processing. The sliding window approach (Press 379 et al., 2021) is used for the perplexity evaluation with a window size of 4096. Besides having the 380 decoding throughput in Figure 2 for the generation efficiency metric, we also measure the prompt 381 processing speed in Figure 6 of Appendix B for the models SAMBA 1.7B, Mistral 1.6B, Mamba 382 1.8B, Llama-3 1.6B and its Self-Extended (Jin et al., 2024) version SE-Llama-3 1.6B with the prompt length sweeping from 1K to 128K. We set the group size to 4 and the neighborhood window to 1024 for Self-Extension. We fix the total processing tokens per measurement to be 128K and varying the 384 batch size accordingly. The throughput is measured on a single A100 GPU with the precision of 385 bfloat16. We repeat the measurements 10 times and report the averaged results. We can see that 386 Samba achieves $3.73 \times$ higher throughput in prompt processing compared to Llama-3 1.6B at the 387 128K prompt length, and the processing time remains linear with respect to the sequence length. 388 We can also observe that the existing zero-shot length extrapolation technique introduces significant 389 inference latency overhead on the full-attention counterpart, while it still cannot extrapolate infinitely 390 with perplexity performance comparable to that of Samba. In Figure 2, we can also see that Mamba 391 has a slowly and stably increasing perplexity up to 1M sequence length, which indicates that linear 392 recurrent models can still not extrapolate infinitely if the context length is extremely large. 393

3.4 LONG-CONTEXT UNDERSTANDING

394

395 396

397

398

399

400

401

402

403

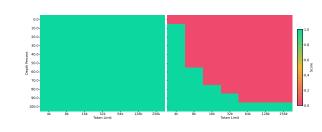
404

405

406

407

408



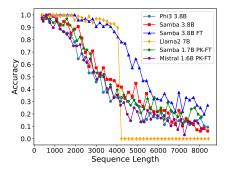


Figure 3: Passkey Retrieval performance up to 256K context length for SAMBA 1.7B (Left) vs. Mistral 1.6B (right) instruction tuned on 4K sequence length with 500 steps.

Figure 4: Phonebook evaluation accuracy of different base models.

409 Beyond its efficiency in processing long context, Samba can also extrapolate its memory recall 410 ability to 256K context length through supervised fine-tuning, and still keeps its linear computation 411 complexity. We fine-tune Samba 1.7B on Passkey Retrieval with a 4K training sequence length 412 for only 500 steps. As presented in Figure 3, SAMBA 1.7B demonstrates a remarkable ability to recall information from significantly longer contexts compared to Mistral 1.6B, a model based solely 413 on Sliding Window Attention (SWA). This capability is particularly evident in the heatmap, where 414 SAMBA maintains the perfect retrieval performance across a wider range of pass-key positions in a 415 long document of up to 256K length. We also draw the training loss curve and the overall passkey 416 retrieval accuracy across the fine-tuning procedure in Figure 7 and Figure 8 of Appendix C. We find 417 that despite the fact that both architectures can reach near-zero training loss in less than 250 steps, 418 Samba can achieve near-perfect retrieval early at 150 training steps, while the Mistral architecture 419 struggles at around 30% accuracy throughout the training process. This shows that Samba can have 420 better long-range retrieval ability than SWA due to the input selection mechanism introduced by the 421 Mamba layers. In Figure 8, we can also notice that the pre-trained base Samba model has a retrieval 422 accuracy (at step 0) similar to that of Mistral, highlighting the need for future work to improve Samba's zero-shot retrieval capabilities. 423

424 The encouraging results on Passkey Retrieval drives us to further explore the limits of our finetuning 425 approach. We perform instruction tuning to the Samba-3.8B base model on Phonebook (Jelassi et al., 426 2024) with only 100 steps on 4K sequence length and evaluate the resulting Samba-3.8B-FT model 427 for a sequence length up to 8K. The evaluation setting requires the models to retrieve a random 428 phone number from a phone book containing 20 (length 400) to 480 (length 8400) name-number pairs, resulting in a pressure test of memorization to Samba which has a constant memory state size. 429 Surprisingly, as shown in Figure 4, we can see that the Samba-3.8B-FT model can close most of its 430 gap with a full-attention model (Llama2 7B) that has twice the parameter size within the 4K training 431 length, and achieves much better extrapolation accuracy compared to all other models including

432 the Phi3 base model which also uses 2K sliding window attention. Since both Passkey Retrieval 433 and Phonebook require models to remember numbers in a long context document, it is interesting 434 to investigate if a model instruction-tuned on one task can transfer its ability to the other task in 435 zero-shot. We directly evaluate the Passkey Retrieval finetuned Samba 1.7B and Mistral 1.6B models 436 (named Samba 1.7B PK-FT and Mistral 1.6B PK-FT respectively) on the Phonebook task. As shown in Figure 4, Samba 1.7B has slightly better retrieval accuracy than Mistral 1.6B, but both models 437 cannot generalize their number recall ability beyond its sliding window size. We leave it for future 438 work to further explore the transferability of long-context capabilities in linear complexity models. 439

4 ANALYSIS

440 441

442

448

457

458

459

443 In this section, we analyze the experimental results of SAMBA by answering the following research 444 questions. The perplexity results on SlimPajama have a fluctuation around $\pm 0.3\%$. Training speed is 445 measured on $8 \times H100$ GPUs by default. All the models in this section are trained on SlimPajama with 20B tokens and 4K sequence length, unless otherwise specified. We also have additional analyses on 446 the effectiveness of short convolution in Appendix D. 447

Why not hybridize with full attention? Some previous works (Fu et al., 2023; Lieber et al., 2024) 449 suggest a hybrid architecture of Mamba with full attention. However, as shown in Table 5, the 450 extrapolation perplexity is exploding at a context length of 16K even if a single full attention layer 451 is placed at the beginning of the model. Although hybridization with full attention in the second 452 and middle sixth blocks (the fourth row in the table), following Dao et al. (2022b), can bridge the 453 perplexity gap between full-attention hybrids and Samba, they still cannot extrapolate beyond the 454 training sequence lengths. Samba also has much better training throughput compared to Mamba-MLP 455 alternatives because self-attention with the FlashAttention 2 implementation is more training efficient 456 than Mamba when the sequence length is 4096.

Table 5: Perplexity on SlimPajama of Mamba-MLP architectures with full attention layers replacing Mamba layers at different block indices. We define a block as two consecutive layers with a Mamba/Attention layer followed by an MLP. All the models have 12 blocks in total.

Architecture	Size	Block Index	Training Speed	Validation Context Length			
Architecture	of Full Attention		$(\times 10^5 \text{ tokens/s})$	4096	8192	16384	
	449M	11	7.78	10.29	10.53	13.66	
Manda MID	449M	5	7.78	10.10	10.05	12.83	
Mamba-MLP	449M	0	7.78	10.89	10.55	10.63	
	443M	1, 5	7.93	10.06	10.34	13.57	
SAMBA 421M SWA at o		SWA at odd indices	8.59	10.06	9.65	9.57	

471

473

475

How many parameters should be allocated to Attention? Given that Mamba can already capture low-rank information in the sequences through recurrent compression, the attention layers in Samba theoretically will only need to focus on information retrieval where a small number of attention 472 heads should suffice. In Table 6, we explore the techniques of query head grouping (Ainslie et al., 2023; Shazeer, 2019), for both the Llama and Samba models. Surprisingly, both the Llama-2-SWA 474 architecture and the Samba architecture show improved validation perplexity when there is only one key-value head. We conjecture that this is because small language models can be more easily 476 optimized with fewer KV heads to pay attention to the contexts. We can also see that Samba has a 477 $2 \times$ smaller optimal number of query heads than the SWA model, which confirms our hypothesis that 478 Samba can support a smaller number of attention heads.

479

480 **Potential explanations on why hybrid is better?** We examine the entropy of the attention distribu-481 tions for both the Samba 1.7B and the Mistral 1.6B models. As shown in Figure 5a, the Samba model 482 has a larger variance of the attention entropy distributed over the layer indices, with an interesting pattern that the upper and lower layers have entropy higher than the middle layers. This may indicate 483 that the attention layers are more specialized in the Samba architecture, with the middle layers 484 focusing on precise retrieval with low-entropy attention, and the top and bottom layers focusing on 485 integrating the global information through high-entropy attention. We can also see in Figure 5b that,

Table 6: Perplexity on SlimPajama of Llama-2-SWA and Samba models at the 430M scales trained with different number of Query and Key-Value heads. "KV Size" means the size of Key-Value vectors per token and attention layer. Since grouped query attention will reduce the parameters for attention from $4d_m^2$ to roughly $2d_m^2$, we increase the intermediate size of MLP from $8/3d_m$ to $3d_m = 4608$ to have roughly the same number of total parameters as the original models.

Query	Key-Value	Head	KV	Model	Training Speed	Valida	ext Length				
Head	Head	Dim.	Size	Size	$(\times 10^5 \text{ tokens/s})$	4096	8192	16384			
Llama-2-SWA Architecture											
12	2	128	512	419M	10.01	11.11	10.64	10.56			
6	1	256	512	419M	9.98	11.09	10.62	10.54			
12	1	128	256	414M	10.25	10.89	10.44	10.35			
12	4	128	1024	428M	9.85	11.11	10.64	10.56			
Samba Architecture											
12	2	128	512	426M	8.55	10.09	9.68	9.60			
6	1	256	512	426M	8.46	9.99	9.59	9.51			
12	1	128	256	424M	8.62	10.07	9.66	9.58			
12	4	128	1024	431M	8.57	10.02	9.62	9.55			

compared to the Mamba-MLP model, Samba has a higher entropy of input selection probabilities in the middle layers. This indicates that, given the memory recalling ability of the attention layers, the Mamba layers can focus more on modeling the recurrent structure rather than performing retrieval with precise input selections. This kind of specialization can be beneficial for the downstream model performance, which may explain the impressive results from the Samba architecture. Details on how entropy is calculated are included in Appendix E.

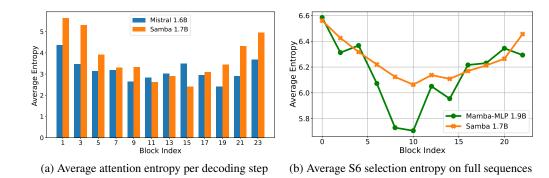


Figure 5: The average entropy of the attention mechanism and the Mamba's S6 input selection mechanism at each block of layers on 100 random samples from the GSM8K dataset.

CONCLUSION

In this paper, we introduce SAMBA, a simple yet powerful hybrid neural architecture designed for efficient language modeling with unlimited context length. We show that SAMBA substantially outperforms state-of-the-art pure attention-based and SSM-based models across a wide range of benchmarks including common-sense reasoning, language understanding, mathematics and coding. Furthermore, SAMBA exhibits remarkable efficiency in processing long contexts, achieving substantial speedups in prompt processing and decoding throughput compared to the state-of-the-art Transformer architecture. The architecture's ability to extrapolate memory recall to very long contexts (up to 256K) through minimal fine-tuning underscores its practical applicability for real-world tasks requiring extensive context understanding. This efficient long-term memorization ability is further demonstrated to be useful by our evaluations in downstream long-context summarization tasks. Our analyses also provide insight into the optimal training configurations for hybrid models and underscore the benefits of combining attention mechanisms with SSMs. We find that allocating fewer parameters to the attention mechanism while leveraging Mamba's strengths for capturing recurrent structures leads to more efficient and effective language modeling. Our results suggest that SAMBA is a strong neural architecture for language modeling with unlimited context length.

540 REFERENCES 541

567

Marah Abdin, Sam Ade Jacobs, Ammar Ahmad Awan, Jyoti Aneja, Ahmed Awadallah, Hany Awadalla, Nguyen 542 Bach, Amit Bahree, Arash Bakhtiari, Harkirat Behl, Alon Benhaim, Misha Bilenko, Johan Bjorck, Sébastien 543 Bubeck, Martin Cai, Caio César Teodoro Mendes, Weizhu Chen, Vishrav Chaudhary, Parul Chopra, Allie Del 544 Giorno, Gustavo de Rosa, Matthew Dixon, Ronen Eldan, Dan Iter, Abhishek Goswami, Suriya Gunasekar, Emman Haider, Junheng Hao, Russell J. Hewett, Jamie Huynh, Mojan Javaheripi, Xin Jin, Piero Kauffmann, Nikos Karampatziakis, Dongwoo Kim, Mahoud Khademi, Lev Kurilenko, James R. Lee, Yin Tat Lee, 546 Yuanzhi Li, Chen Liang, Weishung Liu, Eric Lin, Zeqi Lin, Piyush Madan, Arindam Mitra, Hardik Modi, 547 Anh Nguyen, Brandon Norick, Barun Patra, Daniel Perez-Becker, Thomas Portet, Reid Pryzant, Heyang Qin, 548 Marko Radmilac, Corby Rosset, Sambudha Roy, Olli Saarikivi, Amin Saied, Adil Salim, Michael Santacroce, 549 Shital Shah, Ning Shang, Hiteshi Sharma, Xia Song, Olatunji Ruwase, Xin Wang, Rachel Ward, Guanhua 550 Wang, Philipp Witte, Michael Wyatt, Can Xu, Jiahang Xu, Sonali Yadav, Fan Yang, Ziyi Yang, Donghan Yu, Chengruidong Zhang, Cyril Zhang, Jianwen Zhang, Li Lyna Zhang, Yi Zhang, Yunan Zhang, and Xiren 551 Zhou. Phi-3 technical report: A highly capable language model locally on your phone. arXiv preprint arXiv: 552 2404.14219, 2024. URL https://arxiv.org/abs/2404.14219v1. 553

- 554 J. Ainslie, J. Lee-Thorp, Michiel de Jong, Yury Zemlyanskiy, Federico Lebr'on, and Sumit K. Sanghai. Gqa: Training generalized multi-query transformer models from multi-head checkpoints. Conference on Empirical 555 Methods in Natural Language Processing, 2023. doi: 10.48550/arXiv.2305.13245. URL https://arxiv. 556 org/abs/2305.13245v3. 557
- 558 Ekin Akyürek, Bailin Wang, Yoon Kim, and Jacob Andreas. In-context language learning: Architectures and algorithms. arXiv preprint arXiv: 2401.12973, 2024. URL https://arxiv.org/abs/2401.12973v2. 559
- 560 Simran Arora, Sabri Eyuboglu, Aman Timalsina, Isys Johnson, Michael Poli, James Zou, Atri Rudra, and 561 Christopher Ré. Zoology: Measuring and improving recall in efficient language models. arXiv preprint arXiv: 2312.04927, 2023. URL https://arxiv.org/abs/2312.04927v1. 562
- 563 Simran Arora, Sabri Eyuboglu, Michael Zhang, Aman Timalsina, Silas Alberti, Dylan Zinsley, James Zou, Atri 564 Rudra, and Christopher Ré. Simple linear attention language models balance the recall-throughput tradeoff. 565 arXiv preprint arXiv:2402.18668, 2024.
- 566 Jacob Austin, Augustus Odena, Maxwell Nye, Maarten Bosma, Henryk Michalewski, David Dohan, Ellen Jiang, Carrie Cai, Michael Terry, Quoc Le, and Charles Sutton. Program synthesis with large language models. arXiv preprint arXiv: 2108.07732, 2021. URL https://arxiv.org/abs/2108.07732v1.
- 569 Dzmitry Bahdanau, Kyunghyun Cho, and Yoshua Bengio. Neural machine translation by jointly learning to 570 align and translate. International Conference On Learning Representations, 2014. URL https://arxiv. 571 org/abs/1409.0473v7. 572
- Iz Beltagy, Matthew E. Peters, and Arman Cohan. Longformer: The long-document transformer. arXiv preprint 573 arXiv: Arxiv-2004.05150, 2020. URL https://arxiv.org/abs/2004.05150v2. 574
- 575 Yonatan Bisk, Rowan Zellers, Ronan Le Bras, Jianfeng Gao, and Yejin Choi. PIQA: reasoning about physical commonsense in natural language. In The Thirty-Fourth AAAI Conference on Artificial Intelligence, AAAI 576 2020, The Thirty-Second Innovative Applications of Artificial Intelligence Conference, IAAI 2020, The 577 Tenth AAAI Symposium on Educational Advances in Artificial Intelligence, EAAI 2020, New York, NY, 578 USA, February 7-12, 2020, pp. 7432–7439. AAAI Press, 2020. doi: 10.1609/AAAI.V34I05.6239. URL https://doi.org/10.1609/aaai.v34i05.6239. 580
- Aleksandar Botev, Soham De, Samuel L Smith, Anushan Fernando, George-Cristian Muraru, Ruba Haroun, 581 Leonard Berrada, Razvan Pascanu, Pier Giuseppe Sessa, Robert Dadashi, Léonard Hussenot, Johan Ferret, 582 Sertan Girgin, Olivier Bachem, Alek Andreev, Kathleen Kenealy, Thomas Mesnard, Cassidy Hardin, Surya 583 Bhupatiraju, Shreya Pathak, Laurent Sifre, Morgane Rivière, Mihir Sanjay Kale, Juliette Love, Pouya Tafti, 584 Armand Joulin, Noah Fiedel, Evan Senter, Yutian Chen, Srivatsan Srinivasan, Guillaume Desjardins, David Budden, Arnaud Doucet, Sharad Vikram, Adam Paszke, Trevor Gale, Sebastian Borgeaud, Charlie Chen, 585 Andy Brock, Antonia Paterson, Jenny Brennan, Meg Risdal, Raj Gundluru, Nesh Devanathan, Paul Mooney, 586 Nilay Chauhan, Phil Culliton, Luiz GUStavo Martins, Elisa Bandy, David Huntsperger, Glenn Cameron, Arthur Zucker, Tris Warkentin, Ludovic Peran, Minh Giang, Zoubin Ghahramani, Clément Farabet, Koray 588 Kavukcuoglu, Demis Hassabis, Raia Hadsell, Yee Whye Teh, and Nando de Frietas. Recurrentgemma: 589 Moving past transformers for efficient open language models. arXiv preprint arXiv: 2404.07839, 2024. URL https://arxiv.org/abs/2404.07839v1. 590
- 591 Tom Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared D Kaplan, Prafulla Dhariwal, Arvind 592 Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, et al. Language models are few-shot learners. Advances in neural information processing systems, 33:1877–1901, 2020. URL https://arxiv.org/abs/ 2005.14165v4.

633

634 635

636

637

594	Sébastien Bubeck, Varun Chandrasekaran, Ronen Eldan, Johannes Gehrke, Eric Horvitz, Ece Kamar, Peter Lee,
595	Yin Tat Lee, Yuanzhi Li, Scott Lundberg, Harsha Nori, Hamid Palangi, Marco Tulio Ribeiro, and Yi Zhang.
596	Sparks of artificial general intelligence: Early experiments with gpt-4. arXiv preprint arXiv: 2303.12712,
597	2023. URL https://arxiv.org/abs/2303.12712v5.

598 Mark Chen, Jerry Tworek, Heewoo Jun, Qiming Yuan, Henrique Ponde de Oliveira Pinto, Jared Kaplan, 599 Harri Edwards, Yuri Burda, Nicholas Joseph, Greg Brockman, Alex Ray, Raul Puri, Gretchen Krueger, 600 Michael Petrov, Heidy Khlaaf, Girish Sastry, Pamela Mishkin, Brooke Chan, Scott Gray, Nick Ryder, 601 Mikhail Pavlov, Alethea Power, Lukasz Kaiser, Mohammad Bavarian, Clemens Winter, Philippe Tillet, Felipe Petroski Such, Dave Cummings, Matthias Plappert, Fotios Chantzis, Elizabeth Barnes, Ariel Herbert-602 Voss, William Hebgen Guss, Alex Nichol, Alex Paino, Nikolas Tezak, Jie Tang, Igor Babuschkin, Suchir 603 Balaji, Shantanu Jain, William Saunders, Christopher Hesse, Andrew N. Carr, Jan Leike, Josh Achiam, 604 Vedant Misra, Evan Morikawa, Alec Radford, Matthew Knight, Miles Brundage, Mira Murati, Katie Mayer, 605 Peter Welinder, Bob McGrew, Dario Amodei, Sam McCandlish, Ilya Sutskever, and Wojciech Zaremba. 606 Evaluating large language models trained on code. arXiv preprint arXiv: 2107.03374, 2021. URL https: //arxiv.org/abs/2107.03374v2. 607

- Shouyuan Chen, Sherman Wong, Liangjian Chen, and Yuandong Tian. Extending context window of large language models via positional interpolation. *arXiv preprint arXiv: 2306.15595*, 2023a. URL https://arxiv.org/abs/2306.15595v2.
- Yukang Chen, Shengju Qian, Haotian Tang, Xin Lai, Zhijian Liu, Song Han, and Jiaya Jia. Longlora: Efficient fine-tuning of long-context large language models. *International Conference on Learning Representations*, 2023b. doi: 10.48550/arXiv.2309.12307. URL https://arxiv.org/abs/2309.12307v1.
- Rewon Child, Scott Gray, Alec Radford, and Ilya Sutskever. Generating long sequences with sparse transformers.
 PREPRINT, 2019. URL https://arxiv.org/abs/1904.10509v1.
- Christopher Clark, Kenton Lee, Ming-Wei Chang, Tom Kwiatkowski, Michael Collins, and Kristina Toutanova. Boolq: Exploring the surprising difficulty of natural yes/no questions. In Jill Burstein, Christy Doran, and Thamar Solorio (eds.), *Proceedings of the 2019 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, NAACL-HLT 2019, Minneapolis, MN, USA, June 2-7, 2019, Volume 1 (Long and Short Papers)*, pp. 2924–2936. Association for Computational Linguistics, 2019. doi: 10.18653/V1/N19-1300. URL https://doi.org/10.18653/v1/n19-1300.
- Peter Clark, Isaac Cowhey, Oren Etzioni, Tushar Khot, Ashish Sabharwal, Carissa Schoenick, and Oyvind
 Tafjord. Think you have solved question answering? try arc, the ai2 reasoning challenge. arXiv preprint
 arXiv: 1803.05457, 2018. URL https://arxiv.org/abs/1803.05457v1.
- Karl Cobbe, Vineet Kosaraju, Mohammad Bavarian, Mark Chen, Heewoo Jun, Lukasz Kaiser, Matthias Plappert, Jerry Tworek, Jacob Hilton, Reiichiro Nakano, Christopher Hesse, and John Schulman. Training verifiers to solve math word problems. *arXiv preprint arXiv: 2110.14168*, 2021. URL https://arxiv.org/abs/2110.14168y2.
- Damai Dai, Li Dong, Yaru Hao, Zhifang Sui, Baobao Chang, and Furu Wei. Knowledge neurons in pretrained transformers. *ACL*, 2022. URL https://arxiv.org/abs/2104.08696v2.
 - Tri Dao. Flashattention-2: Faster attention with better parallelism and work partitioning. *arXiv preprint arXiv:* 2307.08691, 2023. URL https://arxiv.org/abs/2307.08691v1.
 - Tri Dao, Daniel Y. Fu, Stefano Ermon, Atri Rudra, and Christopher Ré. FlashAttention: Fast and memoryefficient exact attention with IO-awareness. In *Advances in Neural Information Processing Systems*, 2022a.
- Tri Dao, Daniel Y. Fu, Khaled Kamal Saab, A. Thomas, A. Rudra, and Christopher Ré. Hungry hungry hippos: Towards language modeling with state space models. *International Conference On Learning Representations*, 2022b. doi: 10.48550/arXiv.2212.14052. URL https://arxiv.org/abs/2212.14052v3.
- Y. Dauphin, Angela Fan, Michael Auli, and David Grangier. Language modeling with gated convolutional networks. *International Conference On Machine Learning*, 2016. URL https://arxiv.org/abs/1612.
 08083v3.

Soham De, Samuel L. Smith, Anushan Fernando, Aleksandar Botev, George Cristian-Muraru, Albert Gu, Ruba Haroun, Leonard Berrada, Yutian Chen, Srivatsan Srinivasan, Guillaume Desjardins, Arnaud Doucet, David Budden, Yee Whye Teh, Razvan Pascanu, Nando De Freitas, and Caglar Gulcehre. Griffin: Mixing gated linear recurrences with local attention for efficient language models. *arXiv preprint arXiv: 2402.19427*, 2024. URL https://arxiv.org/abs/2402.19427v1.

649

650

Yiran Ding, L. Zhang, Chengruidong Zhang, Yuanyuan Xu, Ning Shang, Jiahang Xu, Fan Yang, and Mao Yang. Longrope: Extending llm context window beyond 2 million tokens. *International Conference on Machine Learning*, 2024. doi: 10.48550/arXiv.2402.13753.

Abhimanyu Dubey, Abhinav Jauhri, Abhinav Pandey, Abhishek Kadian, Ahmad Al-Dahle, Aiesha Letman, 652 Akhil Mathur, Alan Schelten, Amy Yang, Angela Fan, Anirudh Goyal, Anthony Hartshorn, Aobo Yang, Archi 653 Mitra, Archie Sravankumar, Artem Korenev, Arthur Hinsvark, Arun Rao, Aston Zhang, Aurelien Rodriguez, 654 Austen Gregerson, Ava Spataru, Baptiste Roziere, Bethany Biron, Binh Tang, Bobbie Chern, Charlotte Caucheteux, Chaya Nayak, Chloe Bi, Chris Marra, Chris McConnell, Christian Keller, Christophe Touret, 656 Chunyang Wu, Corinne Wong, Cristian Canton Ferrer, Cyrus Nikolaidis, Damien Allonsius, Daniel Song, Danielle Pintz, Danny Livshits, David Esiobu, Dhruv Choudhary, Dhruv Mahajan, Diego Garcia-Olano, Diego 657 Perino, Dieuwke Hupkes, Egor Lakomkin, Ehab AlBadawy, Elina Lobanova, Emily Dinan, Eric Michael 658 Smith, Filip Radenovic, Frank Zhang, Gabriel Synnaeve, Gabrielle Lee, Georgia Lewis Anderson, Graeme 659 Nail, Gregoire Mialon, Guan Pang, Guillem Cucurell, Hailey Nguyen, Hannah Korevaar, Hu Xu, Hugo 660 Touvron, Iliyan Zarov, Imanol Arrieta Ibarra, Isabel Kloumann, Ishan Misra, Ivan Evtimov, Jade Copet, Jaewon Lee, Jan Geffert, Jana Vranes, Jason Park, Jay Mahadeokar, Jeet Shah, Jelmer van der Linde, Jennifer 661 Billock, Jenny Hong, Jenya Lee, Jeremy Fu, Jianfeng Chi, Jianyu Huang, Jiawen Liu, Jie Wang, Jiecao 662 Yu, Joanna Bitton, Joe Spisak, Jongsoo Park, Joseph Rocca, Joshua Johnstun, Joshua Saxe, Junteng Jia, 663 Kalyan Vasuden Alwala, Kartikeya Upasani, Kate Plawiak, Ke Li, Kenneth Heafield, Kevin Stone, Khalid 664 El-Arini, Krithika Iyer, Kshitiz Malik, Kuenley Chiu, Kunal Bhalla, Lauren Rantala-Yeary, Laurens van der 665 Maaten, Lawrence Chen, Liang Tan, Liz Jenkins, Louis Martin, Lovish Madaan, Lubo Malo, Lukas Blecher, Lukas Landzaat, Luke de Oliveira, Madeline Muzzi, Mahesh Pasupuleti, Mannat Singh, Manohar Paluri, 666 Marcin Kardas, Mathew Oldham, Mathieu Rita, Maya Pavlova, Melanie Kambadur, Mike Lewis, Min Si, 667 Mitesh Kumar Singh, Mona Hassan, Naman Goyal, Narjes Torabi, Nikolay Bashlykov, Nikolay Bogoychev, Niladri Chatterji, Olivier Duchenne, Onur Çelebi, Patrick Alrassy, Pengchuan Zhang, Pengwei Li, Petar 669 Vasic, Peter Weng, Prajjwal Bhargava, Pratik Dubal, Praveen Krishnan, Punit Singh Koura, Puxin Xu, Qing 670 He, Qingxiao Dong, Ragavan Srinivasan, Raj Ganapathy, Ramon Calderer, Ricardo Silveira Cabral, Robert 671 Stojnic, Roberta Raileanu, Rohit Girdhar, Rohit Patel, Romain Sauvestre, Ronnie Polidoro, Roshan Sumbaly, Ross Taylor, Ruan Silva, Rui Hou, Rui Wang, Saghar Hosseini, Sahana Chennabasappa, Sanjay Singh, Sean Bell, Seohyun Sonia Kim, Sergey Edunov, Shaoliang Nie, Sharan Narang, Sharath Raparthy, Sheng 673 Shen, Shengye Wan, Shruti Bhosale, Shun Zhang, Simon Vandenhende, Soumya Batra, Spencer Whitman, 674 Sten Sootla, Stephane Collot, Suchin Gururangan, Sydney Borodinsky, Tamar Herman, Tara Fowler, Tarek 675 Sheasha, Thomas Georgiou, Thomas Scialom, Tobias Speckbacher, Todor Mihaylov, Tong Xiao, Ujjwal 676 Karn, Vedanuj Goswami, Vibhor Gupta, Vignesh Ramanathan, Viktor Kerkez, Vincent Gonguet, Virginie Do, Vish Vogeti, Vladan Petrovic, Weiwei Chu, Wenhan Xiong, Wenyin Fu, Whitney Meers, Xavier Martinet, 677 Xiaodong Wang, Xiaoqing Ellen Tan, Xinfeng Xie, Xuchao Jia, Xuewei Wang, Yaelle Goldschlag, Yashesh 678 Gaur, Yasmine Babaei, Yi Wen, Yiwen Song, Yuchen Zhang, Yue Li, Yuning Mao, Zacharie Delpierre 679 Coudert, Zheng Yan, Zhengxing Chen, Zoe Papakipos, Aaditya Singh, Aaron Grattafiori, Abha Jain, Adam 680 Kelsey, Adam Shajnfeld, Adithya Gangidi, Adolfo Victoria, Ahuva Goldstand, Ajay Menon, Ajay Sharma, Alex Boesenberg, Alex Vaughan, Alexei Baevski, Allie Feinstein, Amanda Kallet, Amit Sangani, Anam 681 Yunus, Andrei Lupu, Andres Alvarado, Andrew Caples, Andrew Gu, Andrew Ho, Andrew Poulton, Andrew 682 Ryan, Ankit Ramchandani, Annie Franco, Aparajita Saraf, Arkabandhu Chowdhury, Ashley Gabriel, Ashwin Bharambe, Assaf Eisenman, Azadeh Yazdan, Beau James, Ben Maurer, Benjamin Leonhardi, Bernie Huang, Beth Loyd, Beto De Paola, Bhargavi Paranjape, Bing Liu, Bo Wu, Boyu Ni, Braden Hancock, Bram Wasti, 685 Brandon Spence, Brani Stojkovic, Brian Gamido, Britt Montalvo, Carl Parker, Carly Burton, Catalina Mejia, Changhan Wang, Changkyu Kim, Chao Zhou, Chester Hu, Ching-Hsiang Chu, Chris Cai, Chris Tindal, Christoph Feichtenhofer, Damon Civin, Dana Beaty, Daniel Kreymer, Daniel Li, Danny Wyatt, David Adkins, David Xu, Davide Testuggine, Delia David, Devi Parikh, Diana Liskovich, Didem Foss, Dingkang Wang, 688 Duc Le, Dustin Holland, Edward Dowling, Eissa Jamil, Elaine Montgomery, Eleonora Presani, Emily Hahn, Emily Wood, Erik Brinkman, Esteban Arcaute, Evan Dunbar, Evan Smothers, Fei Sun, Felix Kreuk, Feng 690 Tian, Firat Ozgenel, Francesco Caggioni, Francisco Guzmán, Frank Kanayet, Frank Seide, Gabriela Medina Florez, Gabriella Schwarz, Gada Badeer, Georgia Swee, Gil Halpern, Govind Thattai, Grant Herman, Grigory 691 Sizov, Guangyi, Zhang, Guna Lakshminarayanan, Hamid Shojanazeri, Han Zou, Hannah Wang, Hanwen 692 Zha, Haroun Habeeb, Harrison Rudolph, Helen Suk, Henry Aspegren, Hunter Goldman, Igor Molybog, Igor 693 Tufanov, Irina-Elena Veliche, Itai Gat, Jake Weissman, James Geboski, James Kohli, Japhet Asher, Jean-694 Baptiste Gaya, Jeff Marcus, Jeff Tang, Jennifer Chan, Jenny Zhen, Jeremy Reizenstein, Jeremy Teboul, Jessica 695 Zhong, Jian Jin, Jingyi Yang, Joe Cummings, Jon Carvill, Jon Shepard, Jonathan McPhie, Jonathan Torres, Josh Ginsburg, Junjie Wang, Kai Wu, Kam Hou U, Karan Saxena, Karthik Prasad, Kartikay Khandelwal, 696 Katayoun Zand, Kathy Matosich, Kaushik Veeraraghavan, Kelly Michelena, Keqian Li, Kun Huang, Kunal 697 Chawla, Kushal Lakhotia, Kyle Huang, Lailin Chen, Lakshya Garg, Lavender A, Leandro Silva, Lee Bell, 698 Lei Zhang, Liangpeng Guo, Licheng Yu, Liron Moshkovich, Luca Wehrstedt, Madian Khabsa, Manav 699 Avalani, Manish Bhatt, Maria Tsimpoukelli, Martynas Mankus, Matan Hasson, Matthew Lennie, Matthias 700 Reso, Maxim Groshev, Maxim Naumov, Maya Lathi, Meghan Keneally, Michael L. Seltzer, Michal Valko, 701 Michelle Restrepo, Mihir Patel, Mik Vyatskov, Mikayel Samvelyan, Mike Clark, Mike Macey, Mike Wang, Miquel Jubert Hermoso, Mo Metanat, Mohammad Rastegari, Munish Bansal, Nandhini Santhanam, Natascha

702	Parks, Natasha White, Navyata Bawa, Nayan Singhal, Nick Egebo, Nicolas Usunier, Nikolay Pavlovich
703	Laptev, Ning Dong, Ning Zhang, Norman Cheng, Oleg Chernoguz, Olivia Hart, Omkar Salpekar, Ozlem
704	Kalinli, Parkin Kent, Parth Parekh, Paul Saab, Pavan Balaji, Pedro Rittner, Philip Bontrager, Pierre Roux,
705	Piotr Dollar, Polina Zvyagina, Prashant Ratanchandani, Pritish Yuvraj, Qian Liang, Rachad Alao, Rachel
706	Rodriguez, Rafi Ayub, Raghotham Murthy, Raghu Nayani, Rahul Mitra, Raymond Li, Rebekkah Hogan,
707	Robin Battey, Rocky Wang, Rohan Maheswari, Russ Howes, Ruty Rinott, Sai Jayesh Bondu, Samyak Datta, Sara Chugh, Sara Hunt, Sargun Dhillon, Sasha Sidorov, Satadru Pan, Saurabh Verma, Seiji Yamamoto,
708	Sharadh Ramaswamy, Shaun Lindsay, Shaun Lindsay, Sheng Feng, Shenghao Lin, Shengxin Cindy Zha,
709	Shiva Shankar, Shuqiang Zhang, Shuqiang Zhang, Sinong Wang, Sneha Agarwal, Soji Sajuyigbe, Soumith
710	Chintala, Stephanie Max, Stephen Chen, Steve Kehoe, Steve Satterfield, Sudarshan Govindaprasad, Sumit
711	Gupta, Sungmin Cho, Sunny Virk, Suraj Subramanian, Sy Choudhury, Sydney Goldman, Tal Remez, Tamar
712	Glaser, Tamara Best, Thilo Kohler, Thomas Robinson, Tianhe Li, Tianjun Zhang, Tim Matthews, Timothy Chou, Tzook Shaked, Varun Vontimitta, Victoria Ajayi, Victoria Montanez, Vijai Mohan, Vinay Satish Kumar,
713	Vishal Mangla, Vlad Ionescu, Vlad Poenaru, Vlad Tiberiu Mihailescu, Vladimir Ivanov, Wei Li, Wenchen
714	Wang, Wenwen Jiang, Wes Bouaziz, Will Constable, Xiaocheng Tang, Xiaofang Wang, Xiaojian Wu, Xiaolan
715	Wang, Xide Xia, Xilun Wu, Xinbo Gao, Yanjun Chen, Ye Hu, Ye Jia, Ye Qi, Yenda Li, Yilin Zhang, Ying
716	Zhang, Yossi Adi, Youngjin Nam, Yu, Wang, Yuchen Hao, Yundi Qian, Yuzi He, Zach Rait, Zachary DeVito,
717	Zef Rosnbrick, Zhaoduo Wen, Zhenyu Yang, and Zhiwei Zhao. The llama 3 herd of models. <i>arXiv preprint arXiv:</i> 2407.21783, 2024. URL https://arxiv.org/abs/2407.21783v1.
718	u_{XIV} . 2407.21763, 2024. OKL https://arxiv.org/ab3/2407.21763v1.
719 720	Stefan Elfwing, E. Uchibe, and K. Doya. Sigmoid-weighted linear units for neural network function approximation in reinforcement learning. <i>Neural Networks</i> , 2017. doi: 10.1016/j.neunet.2017.12.012.
721	
722	Mahan Fathi, Jonathan Pilault, Orhan Firat, Christopher Pal, Pierre-Luc Bacon, and Ross Goroshin. Block-state
723	transformers. <i>NEURIPS</i> , 2023. URL https://arxiv.org/abs/2306.09539v4.
724	Daniel Y Fu, Tri Dao, Khaled Kamal Saab, Armin W Thomas, Atri Rudra, and Christopher Re. Hungry hungry
725	hippos: Towards language modeling with state space models. In The Eleventh International Conference on
726	<i>Learning Representations</i> , 2023. URL https://openreview.net/forum?id=COZDy0WYGg.
727	Allert Consul Tri Day Manhar Lincontinue and aller with a lattice state and a Vice state
728	Albert Gu and Tri Dao. Mamba: Linear-time sequence modeling with selective state spaces. <i>arXiv preprint arXiv:2312.00752</i> , 2023.
729	univ.2312.00752, 2025.
730	Albert Gu, Karan Goel, and Christopher R'e. Efficiently modeling long sequences with structured state spaces.
731	International Conference On Learning Representations, 2021.
732	Albert Cr. Andrit Cruste Kenne Cash and Christenber Dé On the annuaterization and initialization of discourse
733	Albert Gu, Ankit Gupta, Karan Goel, and Christopher Ré. On the parameterization and initialization of diagonal state space models. <i>ARXIV.ORG</i> , 2022. doi: 10.48550/arXiv.2206.11893.
734	sale space models. (man //o/to, 2022, doi: 10.10550/di/in/2200.11095.
735	Chi Han, Qifan Wang, Wenhan Xiong, Yu Chen, Heng Ji, and Sinong Wang. Lm-infinite: Simple on-the-fly
736	length generalization for large language models. arXiv preprint arXiv: 2308.16137, 2023. URL https:
737	//arxiv.org/abs/2308.16137v3.
738	Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. CVPR,
739	2016. URL https://arxiv.org/abs/1512.03385v1.
740	
741	Yihui He, Jianing Qian, Jianren Wang, Cindy X. Le, Congrui Hetang, Qi Lyu, Wenping Wang, and Tianwei Yue.
742	Depth-wise decomposition for accelerating separable convolutions in efficient convolutional neural networks. <i>arXiv preprint arXiv: 1910.09455</i> , 2019. URL https://arxiv.org/abs/1910.09455v3.
743	<i>urxiv preprint urxiv. 1910.09433</i> , 2019. OKL https://arxiv.org/abs/1910.09455v5.
744	Dan Hendrycks, Collin Burns, Steven Basart, Andy Zou, Mantas Mazeika, Dawn Song, and Jacob Stein-
745	hardt. Measuring massive multitask language understanding. In 9th International Conference on Learn-
746	ing Representations, ICLR 2021, Virtual Event, Austria, May 3-7, 2021. OpenReview.net, 2021. URL
747	https://openreview.net/forum?id=d7KBjmI3GmQ.
748	Ari Holtzman, Jan Buys, Li Du, Maxwell Forbes, and Yejin Choi. The curious case of neural text degeneration. In-
749	ternational Conference on Learning Representations, 2019. URL https://arxiv.org/abs/1904.09751v2.
750	
751	Luyang Huang, Shuyang Cao, Nikolaus Parulian, Heng Ji, and Lu Wang. Efficient attentions for long document
752	summarization. Proceedings of the 2021 Conference of the North American Chapter of the Association for
753	Computational Linguistics: Human Language Technologies, pp. 1419–1436, 2021.
754	Samy Jelassi, David Brandfonbrener, Sham M. Kakade, and Eran Malach. Repeat after me: Transformers
755	are better than state space models at copying. <i>arXiv preprint arXiv: 2402.01032</i> , 2024. URL https: //arxiv.org/abs/2402.01032v1.

756 757	Albert Q. Jiang, Alexandre Sablayrolles, Arthur Mensch, Chris Bamford, Devendra Singh Chaplot, Diego de las Casas, Florian Bressand, Gianna Lengyel, Guillaume Lample, Lucile Saulnier, Lélio Renard Lavaud, Marie-
758 759	Anne Lachaux, Pierre Stock, Teven Le Scao, Thibaut Lavril, Thomas Wang, Timothée Lacroix, and William El Sayed. Mistral 7b. <i>arXiv preprint arXiv: 2310.06825</i> , 2023. URL https://arxiv.org/abs/2310.06825v1.
760	
761	Hongye Jin, Xiaotian Han, Jingfeng Yang, Zhimeng Jiang, Zirui Liu, Chia-Yuan Chang, Huiyuan Chen, and Xia
762	Hu. Llm maybe longlm: Self-extend llm context window without tuning. <i>arXiv preprint arXiv: 2401.01325</i> , 2024. URL https://arxiv.org/abs/2401.01325v1.
763	Tobias Katsch. Gateloop: Fully data-controlled linear recurrence for sequence modeling. arXiv preprint arXiv:
764 765	2311.01927, 2023. URL https://arxiv.org/abs/2311.01927v1.
766	Nikita Kitaev, Łukasz Kaiser, and Anselm Levskaya. Reformer: The efficient transformer. arXiv preprint
767	arXiv:2001.04451, 2020.
768	Yuanzhi Li, Sébastien Bubeck, Ronen Eldan, Allie Del Giorno, Suriya Gunasekar, and Yin Tat Lee. Textbooks
769 770	are all you need ii: phi-1.5 technical report. <i>arXiv preprint arXiv: 2309.05463</i> , 2023. URL https: //arxiv.org/abs/2309.05463v1.
771	
772	Opher Lieber, Barak Lenz, Hofit Bata, Gal Cohen, Jhonathan Osin, Itay Dalmedigos, Erez Safahi, Shaked
773	Meirom, Yonatan Belinkov, Shai Shalev-Shwartz, Omri Abend, Raz Alon, Tomer Asida, Amir Bergman, Roman Glozman, Michael Gokhman, Avashalom Manevich, Nir Ratner, Noam Rozen, Erez Shwartz, Mor
774	Zusman, and Yoav Shoham. Jamba: A hybrid transformer-mamba language model. <i>arXiv preprint arXiv</i> :
775	2403.19887, 2024. URL https://arxiv.org/abs/2403.19887v1.
776	Stephanie Lin, Jacob Hilton, and Owain Evans. TruthfulQA: Measuring how models mimic human falsehoods.
777	In Smaranda Muresan, Preslav Nakov, and Aline Villavicencio (eds.), Proceedings of the 60th Annual
778	Meeting of the Association for Computational Linguistics (Volume 1: Long Papers), pp. 3214–3252, Dublin,
779	Ireland, may 2022. Association for Computational Linguistics. doi: 10.18653/v1/2022.acl-long.229. URL
780	https://aclanthology.org/2022.acl-long.229.
781	Ilya Loshchilov and Frank Hutter. Decoupled weight decay regularization. In International Conference on
782	Learning Representations, 2018.
783	Xuezhe Ma, Chunting Zhou, Xiang Kong, Junxian He, Liangke Gui, Graham Neubig, Jonathan May, and Luke
784 785	Zettlemoyer. Mega: Moving average equipped gated attention. In <i>The Eleventh International Conference on Learning Representations</i> , 2023. URL https://openreview.net/forum?id=qNLe3iq2E1.
786	
787	Xuezhe Ma, Xiaomeng Yang, Wenhan Xiong, Beidi Chen, Lili Yu, Hao Zhang, Jonathan May, Luke Zettlemoyer,
788 789	Omer Levy, and Chunting Zhou. Megalodon: Efficient llm pretraining and inference with unlimited context length. <i>arXiv preprint arXiv: 2404.08801</i> , 2024. URL https://arxiv.org/abs/2404.08801v1.
790	Eric Martin and Chris Cundy. Parallelizing linear recurrent neural nets over sequence length. In 6th International
791	Conference on Learning Representations, ICLR 2018, Vancouver, BC, Canada, April 30 - May 3, 2018, Conference Track Proceedings. OpenReview.net, 2018. URL https://openreview.net/forum?id=HyUNwulC
792	
793 794	Harsh Mehta, Ankit Gupta, Ashok Cutkosky, and Behnam Neyshabur. Long range language modeling via gated state spaces. In <i>The Eleventh International Conference on Learning Representations, ICLR 2023, Kigali,</i>
795	<i>Rwanda, May 1-5, 2023.</i> OpenReview.net, 2023. URL https://openreview.net/forum?id=5MkYIYCbva.
796	William Mamill Jackson Datty and Ashiah Sakhamyal The Illusion of state in state and a state of the state
797	William Merrill, Jackson Petty, and Ashish Sabharwal. The illusion of state in state-space models. <i>arXiv preprint arXiv: 2404.08819</i> , 2024. URL https://arxiv.org/abs/2404.08819v1.
798	<i>arxiv: 2101.00017, 202</i> 7. OKE https://arxiv.org/ab3/2404.00013v1.
799	MetaAI. Introducing meta llama 3: The most capable openly available llm to date, 2024. URL: https:
800	<pre>//ai.meta.com/blog/meta-llama-3/.</pre>
801	Todor Mihaylov, Peter Clark, Tushar Khot, and Ashish Sabharwal. Can a suit of armor conduct electricity?
802	a new dataset for open book question answering. <i>Conference on Empirical Methods in Natural Language</i>
803	Processing, 2018. doi: 10.18653/v1/D18-1260. URL https://arxiv.org/abs/1809.02789v1.
804	Amigraiyan Maktachami and Martin Jaggi. Landmark attention: Dandam access infinite contact low the
805	Amirkeivan Mohtashami and Martin Jaggi. Landmark attention: Random-access infinite context length for transformers. <i>arXiv preprint arXiv: 2305.16300</i> , 2023. URL https://arxiv.org/abs/2305.16300v2.
806	
807	Tsendsuren Munkhdalai, Manaal Faruqui, and Siddharth Gopal. Leave no context behind: Efficient infinite
808	context transformers with infini-attention. <i>arXiv preprint arXiv: 2404.07143</i> , 2024. URL https://arxiv.
809	org/abs/2404.07143v1.

OpenAI. Gpt-4 technical report. *PREPRINT*, 2023. URL https://arxiv.org/abs/2303.08774v4.

813

830

842

848

849

850

851

852

853

854

010	Antonio Orvieto, Samuel L. Smith, Albert Gu, Anushan Fernando, Caglar Gulcehre, Razvan Pascanu, and
811	Soham De. Resurrecting recurrent neural networks for long sequences. International Conference on Machine
812	Learning, 2023. doi: 10.48550/arXiv.2303.06349. URL https://arxiv.org/abs/2303.06349v1.

- Denis Paperno, Germán Kruszewski, Angeliki Lazaridou, Q. N. Pham, R. Bernardi, Sandro Pezzelle, Marco Baroni, Gemma Boleda, and R. Fernández. The lambada dataset: Word prediction requiring a broad discourse context. *Annual Meeting of the Association for Computational Linguistics*, 2016. doi: 10.18653/v1/P16-1144.
- Jongho Park, Jaeseung Park, Zheyang Xiong, Nayoung Lee, Jaewoong Cho, Samet Oymak, Kangwook Lee, and Dimitris Papailiopoulos. Can mamba learn how to learn? a comparative study on in-context learning tasks. arXiv preprint arXiv: 2402.04248, 2024. URL https://arxiv.org/abs/2402.04248v1.
- Michael Poli, Stefano Massaroli, Eric Q. Nguyen, Daniel Y. Fu, Tri Dao, S. Baccus, Y. Bengio, Stefano
 Ermon, and Christopher Ré. Hyena hierarchy: Towards larger convolutional language models. *International Conference On Machine Learning*, 2023. doi: 10.48550/arXiv.2302.10866. URL https://arxiv.org/abs/2302.10866v3.
- Ofir Press, Noah A. Smith, and M. Lewis. Train short, test long: Attention with linear biases enables input length extrapolation. *International Conference On Learning Representations*, 2021. URL https://arxiv.org/abs/2108.12409v2.
- Zhen Qin, Songlin Yang, and Yiran Zhong. Hierarchically gated recurrent neural network for sequence modeling. *Neural Information Processing Systems*, 2023. doi: 10.48550/arXiv.2311.04823. URL https://arxiv.org/abs/2311.04823v1.
- Zhen Qin, Songlin Yang, Weixuan Sun, Xuyang Shen, Dong Li, Weigao Sun, and Yiran Zhong. Hgrn2: Gated linear rnns with state expansion. *arXiv preprint arXiv: 2404.07904*, 2024. URL https://arxiv.org/abs/2404.07904v1.
- Alec Radford, Jeff Wu, Rewon Child, David Luan, Dario Amodei, and Ilya Sutskever. Language models are unsupervised multitask learners. arXiv preprint, 2019. URL https://api.semanticscholar.org/ CorpusID:160025533.
- Pranav Rajpurkar, Jian Zhang, Konstantin Lopyrev, and Percy Liang. Squad: 100,000+ questions for machine
 comprehension of text. *EMNLP*, 2016. URL https://arxiv.org/abs/1606.05250v3.
- Bavid Rein, Betty Li Hou, Asa Cooper Stickland, Jackson Petty, Richard Yuanzhe Pang, Julien Dirani, Julian Michael, and Samuel R. Bowman. Gpqa: A graduate-level google-proof qa benchmark. *arXiv preprint arXiv:* 2311.12022, 2023. URL https://arxiv.org/abs/2311.12022v1.
- Liliang Ren, Yang Liu, Shuohang Wang, Yichong Xu, Chenguang Zhu, and ChengXiang Zhai. Sparse modular activation for efficient sequence modeling. *NEURIPS*, 2023. URL https://arxiv.org/abs/2306.11197v1.
- Aurko Roy, M. Saffar, Ashish Vaswani, and David Grangier. Efficient content-based sparse attention with routing transformers. *International Conference On Topology, Algebra And Categories In Logic*, 2020. doi: 10.1162/tacl_a_00353.
 - Keisuke Sakaguchi, Ronan Le Bras, Chandra Bhagavatula, and Yejin Choi. Winogrande: An adversarial winograd schema challenge at scale. *Communications of the ACM*, 64(9):99–106, 2021. URL https://arxiv.org/abs/1907.10641v2.
 - Maarten Sap, Hannah Rashkin, Derek Chen, Ronan LeBras, and Yejin Choi. Socialiqa: Commonsense reasoning about social interactions. arXiv preprint arXiv: 1904.09728, 2019. URL https://arxiv.org/abs/1904. 09728v3.
- Imanol Schlag, Kazuki Irie, and Jürgen Schmidhuber. Linear transformers are secretly fast weight programmers. In Marina Meila and Tong Zhang (eds.), *Proceedings of the 38th International Conference on Machine Learning, ICML 2021, 18-24 July 2021, Virtual Event*, volume 139 of *Proceedings of Machine Learning Research*, pp. 9355–9366. PMLR, 2021. URL http://proceedings.mlr.press/v139/schlag21a.html.
- Jay Shah, Ganesh Bikshandi, Ying Zhang, Vijay Thakkar, Pradeep Ramani, and Tri Dao. Flashattention-3: Fast and accurate attention with asynchrony and low-precision. *arXiv preprint arXiv: 2407.08608*, 2024. URL https://arxiv.org/abs/2407.08608v2.
- Uri Shaham, Maor Ivgi, Avia Efrat, Jonathan Berant, and Omer Levy. Zeroscrolls: A zero-shot benchmark for
 long text understanding. *Conference on Empirical Methods in Natural Language Processing*, 2023. doi: 10.48550/arXiv.2305.14196. URL https://arxiv.org/abs/2305.14196v2.

867

868

882

- Noam Shazeer. Fast transformer decoding: One write-head is all you need. *arXiv preprint arXiv: 1911.02150*, 2019. URL https://arxiv.org/abs/1911.02150v1.
 - Noam Shazeer. Glu variants improve transformer. *arXiv preprint arXiv: 2002.05202*, 2020. URL https: //arxiv.org/abs/2002.05202v1.
- Jimmy T.H. Smith, Andrew Warrington, and Scott Linderman. Simplified state space layers for sequence
 modeling. In *The Eleventh International Conference on Learning Representations*, 2023. URL https:
 //openreview.net/forum?id=Ai8Hw3AXqks.
- Daria Soboleva, Faisal Al-Khateeb, Robert Myers, Jacob R Steeves, Joel Hestness, and Nolan Dey. Slimpajama:
 A 627b token cleaned and deduplicated version of redpajama, 2023. URL: https://www.cerebras.net/blog/slimpajama-a-627b-token-cleaned-and-deduplicated-version-of-redpajama.
- Jianlin Su, Yu Lu, Shengfeng Pan, Ahmed Murtadha, Bo Wen, and Yunfeng Liu. Roformer: Enhanced
 transformer with rotary position embedding. *arXiv preprint arXiv: 2104.09864*, 2021.
- Yutao Sun, Li Dong, Shaohan Huang, Shuming Ma, Yuqing Xia, Jilong Xue, Jianyong Wang, and Furu Wei.
 Retentive network: A successor to transformer for large language models. *arXiv preprint arXiv:2307.08621*, 2023.
- Gemma Team. Gemma: Open models based on gemini research and technology. *arXiv preprint arXiv:* 2403.08295, 2024. URL https://arxiv.org/abs/2403.08295v1.
- Jamba Team, Barak Lenz, Alan Arazi, Amir Bergman, Avshalom Manevich, Barak Peleg, Ben Aviram, Chen 883 Almagor, Clara Fridman, Dan Padnos, Daniel Gissin, Daniel Jannai, Dor Muhlgay, Dor Zimberg, Edden M 884 Gerber, Elad Dolev, Eran Krakovsky, Erez Safahi, Erez Schwartz, Gal Cohen, Gal Shachaf, Haim Rozenblum, 885 Hofit Bata, Ido Blass, Inbal Magar, Itay Dalmedigos, Jhonathan Osin, Julie Fadlon, Maria Rozman, Matan 886 Danos, Michael Gokhman, Mor Zusman, Naama Gidron, Nir Ratner, Noam Gat, Noam Rozen, Oded Fried, Ohad Leshno, Omer Antverg, Omri Abend, Opher Lieber, Or Dagan, Orit Cohavi, Raz Alon, Ro'i Belson, 887 Roi Cohen, Rom Gilad, Roman Glozman, Shahar Lev, Shaked Meirom, Tal Delbari, Tal Ness, Tomer Asida, Tom Ben Gal, Tom Braude, Uriya Pumerantz, Yehoshua Cohen, Yonatan Belinkov, Yuval Globerson, 889 Yuval Peleg Levy, and Yoav Shoham. Jamba-1.5: Hybrid transformer-mamba models at scale. arXiv preprint 890 arXiv: 2408.12570, 2024. URL https://arxiv.org/abs/2408.12570v1.
- 891 Hugo Touvron, Louis Martin, Kevin Stone, Peter Albert, Amjad Almahairi, Yasmine Babaei, Nikolay Bashlykov, 892 Soumya Batra, Prajjwal Bhargava, Shruti Bhosale, Dan Bikel, Lukas Blecher, Cristian Canton Ferrer, Moya 893 Chen, Guillem Cucurull, David Esiobu, Jude Fernandes, Jeremy Fu, Wenyin Fu, Brian Fuller, Cynthia Gao, 894 Vedanuj Goswami, Naman Goyal, Anthony Hartshorn, Saghar Hosseini, Rui Hou, Hakan Inan, Marcin Kardas, Viktor Kerkez, Madian Khabsa, Isabel Kloumann, Artem Korenev, Punit Singh Koura, Marie-Anne Lachaux, 895 Thibaut Lavril, Jenya Lee, Diana Liskovich, Yinghai Lu, Yuning Mao, Xavier Martinet, Todor Mihaylov, Pushkar Mishra, Igor Molybog, Yixin Nie, Andrew Poulton, Jeremy Reizenstein, Rashi Rungta, Kalyan 897 Saladi, Alan Schelten, Ruan Silva, Eric Michael Smith, Ranjan Subramanian, Xiaoqing Ellen Tan, Binh Tang, 898 Ross Taylor, Adina Williams, Jian Xiang Kuan, Puxin Xu, Zheng Yan, Iliyan Zarov, Yuchen Zhang, Angela 899 Fan, Melanie Kambadur, Sharan Narang, Aurelien Rodriguez, Robert Stojnic, Sergey Edunov, and Thomas Scialom. Llama 2: Open foundation and fine-tuned chat models. arXiv preprint arXiv: 2307.09288, 2023. 900 URL https://arxiv.org/abs/2307.09288v2. 901
- Szymon Tworkowski, Konrad Staniszewski, Mikołaj Pacek, Yuhuai Wu, Henryk Michalewski, and Piotr Miłoś. Focused transformer: Contrastive training for context scaling. *NEURIPS*, 2023. URL https: //arxiv.org/abs/2307.03170v2.
- Dusan Varis and Ondřej Bojar. Sequence length is a domain: Length-based overfitting in transformer models. In
 Marie-Francine Moens, Xuanjing Huang, Lucia Specia, and Scott Wen-tau Yih (eds.), *Proceedings of the* 2021 Conference on Empirical Methods in Natural Language Processing, pp. 8246–8257, Online and Punta
 Cana, Dominican Republic, nov 2021. Association for Computational Linguistics. doi: 10.18653/v1/2021.
 emnlp-main.650. URL https://aclanthology.org/2021.emnlp-main.650.
- 910Ashish Vaswani, Noam M. Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N. Gomez, Lukasz Kaiser,
and Illia Polosukhin. Attention is all you need. *NIPS*, 2017.
- Alex Wang, Richard Yuanzhe Pang, Angelica Chen, Jason Phang, and Samuel R. Bowman. Squality: Building a long-document summarization dataset the hard way. *Conference on Empirical Methods in Natural Language Processing*, 2022. doi: 10.48550/arXiv.2205.11465. URL https://arxiv.org/abs/2205.11465v1.
- Yubo Wang, Xueguang Ma, Ge Zhang, Yuansheng Ni, Abhranil Chandra, Shiguang Guo, Weiming Ren, Aaran Arulraj, Xuan He, Ziyan Jiang, Tianle Li, Max Ku, Kai Wang, Alex Zhuang, Rongqi Fan, Xiang Yue, and Wenhu Chen. Mmlu-pro: A more robust and challenging multi-task language understanding benchmark. arXiv preprint arXiv: 2406.01574, 2024. URL https://arxiv.org/abs/2406.01574v4.

918 919 920	Jason Wei, Xuezhi Wang, Dale Schuurmans, Maarten Bosma, E. Chi, F. Xia, Quoc Le, and Denny Zhou. Chain-of-thought prompting elicits reasoning in large language models. <i>Neural Information Processing</i> <i>Systems</i> , 2022. URL https://arxiv.org/abs/2201.11903v6.
921 922	Kaiyue Wen, Xingyu Dang, and Kaifeng Lyu. Rnns are not transformers (yet): The key bottleneck on in-context retrieval. <i>arXiv preprint arXiv: 2402.18510</i> , 2024. URL https://arxiv.org/abs/2402.18510v1.
923 924 925	Yuhuai Wu, Markus N. Rabe, DeLesley S. Hutchins, and Christian Szegedy. Memorizing transformers. <i>International Conference On Learning Representations</i> , 2022. doi: 10.48550/arXiv.2203.08913. URL https://arxiv.org/abs/2203.08913v1.
926 927 928 929	Guangxuan Xiao, Yuandong Tian, Beidi Chen, Song Han, and Mike Lewis. Efficient streaming language models with attention sinks. arXiv preprint arXiv: 2309.17453, 2023. URL https://arxiv.org/abs/2309. 17453v1.
930 931 932	Guangxuan Xiao, Yuandong Tian, Beidi Chen, Song Han, and Mike Lewis. Efficient streaming language models with attention sinks. In <i>The Twelfth International Conference on Learning Representations, ICLR 2024, Vienna, Austria, May 7-11, 2024</i> . OpenReview.net, 2024. URL https://openreview.net/forum?id=NG7sS51zVF.
933 934 935 936 937	Ruibin Xiong, Yunchang Yang, Di He, Kai Zheng, Shuxin Zheng, Chen Xing, Huishuai Zhang, Yanyan Lan, Liwei Wang, and Tie-Yan Liu. On layer normalization in the transformer architecture. In <i>Proceedings of the 37th International Conference on Machine Learning, ICML 2020, 13-18 July 2020, Virtual Event</i> , volume 119 of <i>Proceedings of Machine Learning Research</i> , pp. 10524–10533. PMLR, 2020. URL http://proceedings.mlr.press/v119/xiong20b.html.
938 939 940 941	Wenhan Xiong, Jingyu Liu, Igor Molybog, Hejia Zhang, Prajjwal Bhargava, Rui Hou, Louis Martin, Rashi Rungta, Karthik Abinav Sankararaman, Barlas Oguz, Madian Khabsa, Han Fang, Yashar Mehdad, Sharan Narang, Kshitiz Malik, Angela Fan, Shruti Bhosale, Sergey Edunov, Mike Lewis, Sinong Wang, and Hao Ma. Effective long-context scaling of foundation models. arXiv preprint arXiv: 2309.16039, 2023.
942 943	Songlin Yang and Yu Zhang. Fla: A triton-based library for hardware-efficient implementations of linear attention mechanism, January 2024. URL https://github.com/sustcsonglin/flash-linear-attention.
944 945	Songlin Yang, Bailin Wang, Yikang Shen, Rameswar Panda, and Yoon Kim. Gated linear attention transformers with hardware-efficient training. <i>arXiv preprint arXiv:2312.06635</i> , 2023.
946 947 948 949	Manzil Zaheer, Guru Guruganesh, Kumar Avinava Dubey, Joshua Ainslie, Chris Alberti, Santiago Ontanon, Philip Pham, Anirudh Ravula, Qifan Wang, Li Yang, et al. Big bird: Transformers for longer sequences. <i>Advances in neural information processing systems</i> , 33:17283–17297, 2020. URL https://arxiv.org/abs/2007.14062v2.
950 951 952 953	Rowan Zellers, Ari Holtzman, Yonatan Bisk, Ali Farhadi, and Yejin Choi. Hellaswag: Can a machine really finish your sentence? <i>Annual Meeting of the Association for Computational Linguistics</i> , 2019. doi: 10.18653/v1/P19-1472. URL https://arxiv.org/abs/1905.07830v1.
954 955	Biao Zhang and Rico Sennrich. Root mean square layer normalization. <i>Neural Information Processing Systems</i> , 2019. doi: 10.5167/UZH-177483. URL https://arxiv.org/abs/1910.07467v1.
956 957	Edward Ayers Zhangir Azerbayev and Bartosz Piotrowski. Proof-pile, 2022. URL: https://github.com/ zhangir-azerbayev/proof-pile.
958 959 960 961	Hao Zheng, Zhanlei Yang, Wenju Liu, Jizhong Liang, and Yanpeng Li. Improving deep neural networks using softplus units. <i>2015 International Joint Conference on Neural Networks (IJCNN)</i> , pp. 1–4, 2015. doi: 10.1109/IJCNN.2015.7280459. URL https://ieeexplore.ieee.org/document/7280459.
962 963 964 965	Simiao Zuo, Xiaodong Liu, Jian Jiao, Denis Charles, Eren Manavoglu, Tuo Zhao, and Jianfeng Gao. Efficient long sequence modeling via state space augmented transformer. arXiv preprint arXiv: 2212.08136, 2022. URL https://arxiv.org/abs/2212.08136v1.
966 967	A RELATED WORKS
968 969 970	Hybrid Recurrent Models Many recent works (Park et al., 2024; Jelassi et al., 2024; Akyürek et al., 2024) point out the lack of retrieval ability of linear SSMs, and propose hybridization of SSMs with the Attention mechanism. However, the history of SSM/RNN-Attention hybridization

972 sequences. The revitalization of the fact that linear recurrent models are sequentially parallelizable 973 (Martin & Cundy, 2018; Gu et al., 2021) has catalyzed a contemporary renaissance in hybrid recurrent 974 architectures. SPADE (Zuo et al., 2022), GSS (Mehta et al., 2023), MEGA (Ma et al., 2023), Block 975 State transformers (Fathi et al., 2023) and Megalodon (Ma et al., 2024) combine SSMs with chunked 976 attention, while H3 (Dao et al., 2022b), Mambaformer (Park et al., 2024) and Jamba (Lieber et al., 2024; Team et al., 2024) propose to hybridize with quadratic self-attention. Our works focus 977 particularly on the wall-time efficiency and the length extrapolatability of the hybrid SSM-Attention 978 models, and propose to interleave SSMs with Sliding Window Attention (SWA), which has both 979 linear computation complexity and the translation-invariant property over the sequence length. Infini-980 Attention (Munkhdalai et al., 2024) is a recently proposed method that implements an intra-layer 981 hybridization (Wu et al., 2022) between SWA and Linear Attention with the delta rule (Schlag et al., 982 2021). While the preliminary results look promising, its performance in the setting of large-scale 983 pre-training from scratch remains questionable. The most similar work to ours is Griffin (De et al., 984 2024), which interleaves the Real-Gated Linear Recurrent Unit (RG-LRU) with Sliding Window 985 Attention (SWA). However, Samba hybridizes SWA with Mamba instead of RG-LRU and shows 986 that this simple hybrid architecture can provide substantially better performance over state-of-the-art 987 Transformer architectures across scales, while Griffin and its follow-up work RecurrentGemma (Botev et al., 2024) only show comparable or worse results than Transformers. The original Mamba 988 paper (Gu & Dao, 2023) also explores hybridizing pure Mamba models with full attention or MLP 989 layers, but it does not consider the wall-time efficiency of these hybridization and only achieves 990 marginally better performance than the pure Mamba model. In contrast, we are the first to show that 991 interleaving Mamba with both SWA and MLP can substantially outperform modern Transformers 992 (and Mamba) at a scale up to 3.8B parameters, while achieving comparable training speed and better 993 length extrapolation ability under perplexity metrics. 994

- 995 **Efficient Sparse Attention** Previous works have proposed sparsifying self-attention (Vaswani et al., 996 2017) with a static attention pattern (Child et al., 2019; Zaheer et al., 2020; Beltagy et al., 2020) 997 or a dynamic learnable pattern (Roy et al., 2020; Kitaev et al., 2020; Ren et al., 2023) to model 998 long sequences with subquadratic complexity over the sequence length. However, due to the lack of 999 hardware-aware efficient implementation, its actual wall-time training efficiency is often worse than 1000 the dense attention optimized with FlashAttention (Dao et al., 2022a; Dao, 2023; Shah et al., 2024). 1001 In this work, we choose Sliding Window Attention, a simple static sparse attention pattern, because it can easily leverage the highly optimized FlashAttention kernels to enjoy an actual training speed-up 1002 over its dense self-attention counterpart. 1003
 - 1004

Length Extrapolation Many previous works have focused on extending the context length of 1005 pretrained Transformers to improve their performance on long-context tasks. Methods such as LM-1006 Infinite (Han et al., 2023), StreamingLLM (Xiao et al., 2024) and LongLoRA (Chen et al., 2023b) 1007 achieve linear complexity for length extrapolation, but they only stabilize the perplexity beyond the 1008 training sequence length. However, we show that if we pre-train Transformers with Sliding Window 1009 Attention from scratch, it can naturally have improved perplexity beyond the training sequence length. 1010 Other approaches, including LLaMA-2-Long (Xiong et al., 2023), LongLLaMA (Tworkowski et al., 1011 2023), PI (Chen et al., 2023a), LongRoPE (Ding et al., 2024) and Self-Extend (Jin et al., 2024), 1012 attempt to extend the full attention through modifying position embedding or continual training 1013 strategies, but they typically retain quadratic complexity in the attention mechanism with additional computation or memory I/O overhead, therefore they do not scale well to long sequences. Although 1014 these methods achieve an improved perplexity on a certain time longer sequence length than the 1015 training sequence length, their perplexity still explodes if the sequence is extremely long. Our method 1016 achieves both linear complexity and superior extrapolation performance compared to zero-shot length 1017 extrapolation methods, such as Self-Extend, under the perplexity metric. However, we acknowledge 1018 that, in terms of zero-shot retrieval performance, our method still lags behind these approaches. 1019 This underscores a trade-off between perplexity performance and retrieval performance in length 1020 extrapolation, which we plan to explore and address in future work. 1021

1022

B ADDITIONAL EVALUATION RESULTS

1023 1024

1025 In Table 7, we conduct comprehensive evaluations on a diverse subset of the benchmarks to assess SAMBA base model's performance across all the domains mentioned in Section 3 to ensure Table 7: Downstream performance comparison of the SAMBA 3.8B base model with other pretrained base language models without instruction tuning. ARC-C and HellaSwag are measured with character-normalized accuracy. MMLU and GSM8K are measured in 5-shot, while others are in zero-shot. We report the MC2 score for TruthfulQA, maj@1 for GSM8K, and pass@1 for HumanEval. * Measured by ours. The fair comparison should only be considered between TFM++ and Samba.

Model	Size	Tokens	MMLU	Hella- Swag	ARC- C	Wino- Gran.	Truth. QA	GSM 8K	Hum. Eval	Avg.
Llama 2	6.7B	2T	45.3	77.2	45.9	69.2	38.8	14.6	12.8	43.4
	13B	2T	54.8	80.7	49.4	72.8	37.4	28.7	18.3	48.9
Mistral	7.2B	-	60.1	81.3	55.5	75.3	42.2	35.4	30.5	53.6
Mamba	2.8B	600B	26.2	71.0	41.7	65.9	34.4*	3.6*	7.3*	35.7
Gemma	2.5B	3T	42.3	71.4	42.1	65.4	33.1	17.7	22.0	42.0
	8.5B	6T	64.3	81.2	53.2	72.3	44.8	46.4	32.3	56.4
R-Gemma	2.7B	2T	38.4	71.0	42.3	67.8	35.1	13.4	21.3	41.3
Llama 3	8.0B	15T+	66.6	79.2*	53.2*	72.6*	43.9	45.8	28.7^{*}	55.8
TFM++	3.8B	3.2T	67.2	76.6	53.8	72.6	47.3	51.5	51.8	60.1
Samba	3.8B	3.2T	71.2	77.4	55.7	77.1	43.4	69.6	54.9	64.2
	Llama 2 Mistral Mamba Gemma R-Gemma Llama 3 TFM++	Llama 2 6.7B 13B Mistral 7.2B Mamba 2.8B Gemma 2.5B 8.5B R-Gemma 2.7B Llama 3 8.0B TFM++ 3.8B	Llama 2 6.7B 2T 13B 2T Mistral 7.2B - Mamba 2.8B 600B Gemma 2.5B 3T 8.5B 6T R-Gemma 2.7B 2T Llama 3 8.0B 15T+ TFM++ 3.8B 3.2T	Llama 2 6.7B 2T 45.3 13B 2T 54.8 Mistral 7.2B - 60.1 Mamba 2.8B 600B 26.2 Gemma 2.5B 3T 42.3 8.5B 6T 64.3 R-Gemma 2.7B 2T 38.4 Llama 3 8.0B 15T+ 66.6 TFM++ 3.8B 3.2T 67.2	Model Size Tokens MMLU Swag Llama 2 6.7B 2T 45.3 77.2 13B 2T 54.8 80.7 Mistral 7.2B - 60.1 81.3 Mamba 2.8B 600B 26.2 71.0 Gemma 2.5B 3T 42.3 71.4 8.5B 6T 64.3 81.2 R-Gemma 2.7B 2T 38.4 71.0 Llama 3 8.0B 15T+ 66.6 79.2* TFM++ 3.8B 3.2T 67.2 76.6	Model Size Iokens MMLU Swag C Llama 2 6.7B 2T 45.3 77.2 45.9 13B 2T 54.8 80.7 49.4 Mistral 7.2B - 60.1 81.3 55.5 Mamba 2.8B 600B 26.2 71.0 41.7 Gemma 2.5B 3T 42.3 71.4 42.1 8.5B 6T 64.3 81.2 53.2 R-Gemma 2.7B 2T 38.4 71.0 42.3 Llama 3 8.0B 15T+ 66.6 79.2* 53.2* TFM++ 3.8B 3.2T 67.2 76.6 53.8	Model Size Tokens MMLU Swag C Gran. Llama 2 6.7B 2T 45.3 77.2 45.9 69.2 13B 2T 54.8 80.7 49.4 72.8 Mistral 7.2B - 60.1 81.3 55.5 75.3 Mamba 2.8B 600B 26.2 71.0 41.7 65.9 Gemma 2.5B 3T 42.3 71.4 42.1 65.4 8.5B 6T 64.3 81.2 53.2 72.3 R-Gemma 2.7B 2T 38.4 71.0 42.3 67.8 Llama 3 8.0B 15T+ 66.6 79.2* 53.2* 72.6* TFM++ 3.8B 3.2T 67.2 76.6 53.8 72.6*	Model Size Iokens MMLU Swag C Gran. QA Llama 2 6.7B 2T 45.3 77.2 45.9 69.2 38.8 13B 2T 54.8 80.7 49.4 72.8 37.4 Mistral 7.2B - 60.1 81.3 55.5 75.3 42.2 Mamba 2.8B 600B 26.2 71.0 41.7 65.9 34.4* Gemma 2.5B 3T 42.3 71.4 42.1 65.4 33.1 8.5B 6T 64.3 81.2 53.2 72.3 44.8 R-Gemma 2.7B 2T 38.4 71.0 42.3 67.8 35.1 Llama 3 8.0B 15T+ 66.6 79.2* 53.2* 72.6* 43.9 TFM++ 3.8B 3.2T 67.2 76.6 53.8 72.6 47.3	Model Size Iokens MMLU Swag C Gran. QA 8K Llama 2 6.7B 2T 45.3 77.2 45.9 69.2 38.8 14.6 13B 2T 54.8 80.7 49.4 72.8 37.4 28.7 Mistral 7.2B - 60.1 81.3 55.5 75.3 42.2 35.4 Mamba 2.8B 600B 26.2 71.0 41.7 65.9 34.4* 3.6* Gemma 2.5B 3T 42.3 71.4 42.1 65.4 33.1 17.7 8.5B 6T 64.3 81.2 53.2 72.3 44.8 46.4 R-Gemma 2.7B 2T 38.4 71.0 42.3 67.8 35.1 13.4 Llama 3 8.0B 15T+ 66.6 79.2* 53.2* 72.6* 43.9 45.8 TFM++ 3.8B 3.2T 67.2 76.6 53	Model Size Iokens MMLU Swag C Gran. QA 8K Eval Llama 2 6.7B 2T 45.3 77.2 45.9 69.2 38.8 14.6 12.8 13B 2T 54.8 80.7 49.4 72.8 37.4 28.7 18.3 Mistral 7.2B - 60.1 81.3 55.5 75.3 42.2 35.4 30.5 Mamba 2.8B 600B 26.2 71.0 41.7 65.9 34.4* 3.6* 7.3* Gemma 2.5B 3T 42.3 71.4 42.1 65.4 33.1 17.7 22.0 8.5B 6T 64.3 81.2 53.2 72.3 44.8 46.4 32.3 R-Gemma 2.7B 2T 38.4 71.0 42.3 67.8 35.1 13.4 21.3 Llama 3 8.0B 15T+ 66.6 79.2* 53.2* 72.6*

1044 1045

1045

a thorough examination of the model's capabilities. We also report the performance of the Trans-1047 former++ (TFM++) model, which uses the same architecture, pre-training recipe as Phi3-mini, for 1048 a fair comparison. The details of the generation configurations are included in Appendix G. We 1049 compare with several strong baselines, including Llama 2 (Touvron et al., 2023), Mistral (Jiang et al., 1050 2023), Mamba (Gu & Dao, 2023), Gemma (Team, 2024), Recurrent-Gemma (R-Gemma) (Botev 1051 et al., 2024), Llama 3 (MetaAI, 2024) and TFM++. As shown in Table 7, SAMBA achieves the 1052 highest average score on all benchmarks, demonstrating its superior performance in handling various 1053 language comprehension tasks. Notably, SAMBA excels in the GSM8K benchmark, achieving an 1054 absolute 18.1% higher accuracy than TFM++ trained on the same dataset. This shows the surprising complementary effect of combining SSM with the attention mechanism. We conjecture that when 1055 combined with attention, Mamba, as an input-dependent SSM, can focus more on performing the 1056 arithmetic operation through its recurrent states than on doing the retrieval operation which can be 1057 easily learned by the sliding window attention. 1058

1059

1063

Table 8: Post-trained models quality on representative benchmarks under the chat mode. The fair
 comparison should only be considered between SAMBA and Phi3 as we control the training recipes
 and datasets to be the same. Best results are in bold, second best underlined.

Category	Benchmark	SAMBA (June) 3.8B	Phi3 (June) 3.8B	R-Gemma 9B	FalconMamba 7B	Jamba-1.5-Mini 12B/52B	Llama-3.2-In 3B	Llama-3.1-In 8B
	MMLU (5-shot)	69.0	67.2	60.5	62.1	69.7	61.8	68.1
MMLU	MMLU-Pro (0-shot, CoT)	47.9	<u>46.5</u>	17.8	14.5	42.5	39.2	44
.	ARC-C (10-shot)	87.8	<u>86.8</u>	52.0	62.0	85.7	76.1	83.1
Reasoning	GPQA (0-shot, CoT)	<u>29.5</u>	29.0	4.7	8.1	32.3	26.6	26.3
Math	GSM8K (8-shot, CoT)	86.4	<u>84.8</u>	42.6	52.5	75.8	75.6	77.4
Code	HumanEval (0-shot)	70.1	<u>66.5</u>	31.1	-	62.8	62.8	<u>66.5</u>
Code	MBPP (3-shot)	<u>71.7</u>	70.0	42.0	-	75.8	67.2	69.4
Av	erage	66.1	64.4	35.8	-	63.5	58.5	62.1

1077 1078

1079 As shown in Table 8, we can see that post-trained hybrid models can achieve superior performance compared to industry-standard Transformer-based LLMs such as Llama-3.1-Instruct 8B and Llama-

3.2-Instruct 3B, and SSM-based LLMs such as FalconMamba². Recent progress on hybrid LLMs, including Jamba 1.5 (Team et al., 2024) and our own work on SAMBA, shows significant improvement over earlier approaches like R-Gemma (Botev et al., 2024), which hybridizes attention with linear recurrent models but is trained on smaller data scales. SAMBA delivers comparable performance to Jamba-1.5-Mini while using around 3× fewer active parameters and 13× fewer total parameters, due to an advanced text-book data synthesis technique (Abdin et al., 2024). Additionally, SAMBA outperforms the Phi3 architecture, which is trained on the same data and optimization setting, further highlighting the superiority of our hybrid architecture over modern Transformer models.

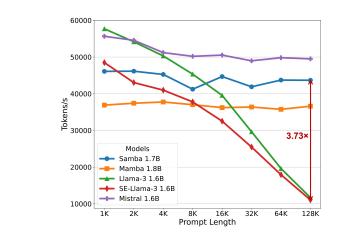


Figure 6: Prompt processing throughput of different models with around 1.7B parameters.

C ADDITIONAL EXPERIMENT DETAILS

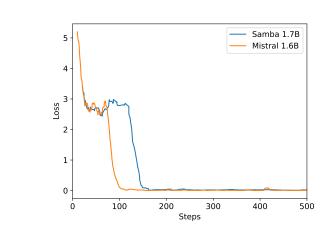


Figure 7: Training loss curves of Samba 1.7B and Mistral 1.6B models during 500 steps of instruction tuning on Passkey Retrieval with 4K sequence length. We plot the loss curves for both models using the simple moving average of window size 10.

1127 We perform instruction tuning for both Mistral 1.6B and Samba 1.7B on Passkey Retrieval using 1128 document length 4096, where we generated the data on the fly through randomly sampling a 5-digit 1129 integer passkey value and a location/depth between zero and the document length to insert the passkey. 1130 The model is then asked to generate the passkey given the full document. We train both models using 1131 batch size 2048, 250 warm-up steps with a peak learning rate of $1e^{-4}$, and 0.1 weight decay with 1132 AdamW (Loshchilov & Hutter, 2018) optimizer. In both cases, the loss converges quickly in 100-200

²https://huggingface.co/tiiuae/falcon-mamba-7b-instruct

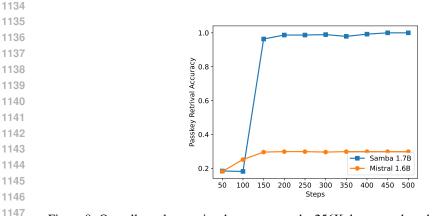


Figure 8: Overall passkey retrieval accuracy on the 256K document length of Samba 1.7B and Mistral 1.6B models during 500 steps of instruction tuning.

steps. During the evaluation, we measure the overall average accuracies of the passkey retrieval at the document length of [4k, 8k, 16k, 32k, 64k, 128k, 256k], for each length we evaluate at 11 different depths of the document (from 0, 0.1, 0.2, ... to 1.0). In addition, for each location of the passkey (depth) in the document, we evaluate the model with five different passkeys to measure accuracy. As seen in Figure 8, the average passkey retrieval accuracy for Samba 1.7B almost reaches 100% in around 150 steps, while the accuracy for Mistral 1.6B remains low, demonstrating the extrapolation ability of the Samba architecture.

1158

1167

1150

1159 D ADDITIONAL ANALYSES

How to train models with Sliding Window Attention (SWA)? Since SWA has linear complexity with respect to the sequence length, it seems alluring to trade off the batch size to have a longer training sequence length without substantially decreasing the training throughput. However, as shown in Table 9, when the sequence length is increased, the validation perplexity also increases in all context lengths due to smaller batch sizes (Varis & Bojar, 2021), and the optimal ratio of sequence length/window size observed is 2, resulting in a training length of 4096.

1168Table 9: Perplexity on SlimPajama of Llama-2-SWA 438M models trained on different context sizes1169and batch sizes. We fix the sliding window size as 2048 and the training tokens per step as 2M.

Batch Size	Comment of the	Training Speed	Validation Context Length			
Datch Size	Sequence Length	$(\times 10^5 \text{ tokens/s})$	2048	4096	8192	16384
1024	2048 (Full Attention)	10.4	11.59	38.12	156.18	357.32
512	4096	9.88	11.87	11.16	10.69	10.61
256	8192	9.66	11.98	11.26	10.79	10.69
128	16384	9.48	12.37	11.63	11.12	11.02
64	32768	9.29	12.94	12.46	11.96	11.86

¹¹⁷⁷ 1178

1179 Fair comparison between Mamba and other linear recurrent models? We can notice that the 1180 Short Convolution (SC) operator in Equation (1) is independent to the design of other parts of Mamba 1181 and can be applied to other linear recurrent models. As shown in Table 10, we explore the effect 1182 of SC on model performance through enhancing Llama-2-SWA, Sliding GLA, and Sliding RetNet 1183 with SC. Surprisingly, besides boosting the performance of RetNet, adding SC can also significantly 1184 improve the SWA's performance, while the effect on GLA is less prominent. We think this is because 1185 GLA already has the fine-grained decays at the channel level, so the depthwise convolution doesn't add much of the useful inductive bias for better modeling power. Notably, even with the SC enhancer, 1186 Sliding GLA and Sliding RetNet still fall short than the original Samba 421M's performance shown in 1187 Table 3. This further justifies our choice of using Mamba for hybridization. We also find that adding

Table 10: Perplexity on the SlimPajama validation set of different linear recurrent and sliding window attention models with Short Convolution (SC) modules added separately to query, key and value representations. For hybrid models, SC is applied only to linear attention layers. The training speed is measured on 8×A100 GPUs.

Architecture	Size	Training Speed $(\times 10^5 \text{ tokens/s})$	Validat 4096	tion Cont 8192	ext Lengtl 16384
Llama-2-SWA	438M	4.96	11.12	10.66	10.57
+ SC	438M	4.69	10.83	10.39	10.31
Sliding GLA	438M	4.94	10.43	10.00	9.92
+ SC	438M	4.44	10.39	9.96	9.87
Sliding RetNet	446M	4.32	10.38	9.96	9.87
+ SC	446M	3.80	10.25	9.82	9.74

SC to both the SWA and the linear attention layers in hybrid models produces negative results, and we leave it as a future work to understand the surprising effectiveness of SC in language modeling.

E DETAILS OF ENTROPY MEASUREMENT

Given a causal attention probability matrix $A \in \mathbb{R}^{h \times n \times n}$, $A_{ijk} = 0 \forall j < k$, with *h* number of heads and a sequence length of *n*, and the generation length 0 < l < n, we calculate the average attention entropy per decoding step as follows,

$$\mathcal{H}_{a} = -\frac{1}{l \cdot h} \sum_{i=1}^{h} \sum_{j=n-l+1}^{n} \sum_{k=1}^{n} A_{ijk} \log(A_{ijk}).$$

For the selective gate $\Delta \in \mathbb{R}^{n \times d_e}$ used by S6 in Equation (2) of the Mamba layers, we first normalize it to be in the simplex $[0, 1]^{n \times d_e}$, *i.e.*,

$$\Delta' = \frac{\Delta}{\sum_{i=1}^{n} \Delta_i} \in [0,1]^{n \times d_e}.$$

The average selection entropy of S6 throughout the entire sequence is then calculated as

$$\mathcal{H}_s = -\frac{1}{d_e} \sum_{j=1}^{d_e} \sum_{i=1}^n \Delta'_{ij} \log(\Delta'_{ij}).$$

F DETAILS OF DOWNSTREAM LONG-CONTEXT EVALUATION

We use the GovReport (Huang et al., 2021) and the SQUALITY (Wang et al., 2022) datasets from the ZeroSCROLLS (Shaham et al., 2023) benchmark to evaluate models' long-context summarization capability in the real world. After tokenizing with the *Phi3-mini-4k* tokenizer, the average document length for the GovReport dataset is 11,533 tokens, with a median of 10,332, a minimum of 1,493, and a maximum of 40,592 tokens. For the SQuALITY dataset, the average sequence length is 7,974 tokens, with a median of 8,145, a minimum of 5,457, and a maximum of 10,757 tokens. For evaluation, we use greedy decoding for both tasks. A maximum generation length of 450 tokens is applied for GovReport and 600 for SQuALITY.

1237 G IMPLEMENTATION DETAILS

For the GLA layer in the Sliding GLA architecture, we use the number of heads $d_m/384$, a key expansion ratio of 0.5, and a value expansion ratio of 1. For the RetNet layer we use a number of head that is half of the number of attention query heads, key expansion ratio of 1 and value expansion ratio of 2. The GLA and RetNet implementations are from the Flash Linear Attention (Yang & Zhang,

Architecture	Llama-3	Mistral	Mamba	Mamba-SWA-MLP	Mamba-MLP
Parameters	1.6B	1.6B	1.8B	1.6B	1.9B
Batch size	2048	2048	2048	2048	2048
Learning rate	0.0006	0.0006	0.0006	0.0006	0.0006
Weight decay	0.1	0.1	0.1	0.1	0.1
Gradient clipping	1.0	1.0	1.0	1.0	1.0
Sequence length	4096	4096	4096	4096	4096
Sliding window size, w	-	2048	-	2048	-
Number of layers, N	48	48	64	54	48
Model width, d_m	2048	2048	2048	2048	2048
MLP intermediate size, d_p	8196	8196	-	8196	8196
Number of query heads	32	32	-	32	32
Number of KV heads	4	4	-	4	4
Number of Attention Layers	24	24	0	18	0
Number of Mamba Layers	0	0	64	18	24
Vocabulary size	50304	50304	50304	50304	50304

Table 11: Detailed hyper-parameters of the baselines models trained on the Phi2 dataset with 230B tokens.

2024) repository³. We use the FlashAttention-based implementation for Self-Extend extrapolation⁴. The Mamba 432M model has a model width of 1024 and the Mamba 1.3B model has a model width of 2048. All models trained on SlimPajama have the same training configurations and the MLP intermediate size as Samba, unless otherwise specified. The training infrastructure on SlimPajama is based on a modified version of the TinyLlama codebase⁵.

Table 12: Detailed hyper-parameters of the SAMBA models trained at different scales. We only show the optimization settings for the first training phase of the 3.8B model.

270	Total Parameters	421M	1.3B	1.7B	3.8B
?71	Dataset	SlimPajama	SlimPajama	Phi-2	Phi-3
72	Batch size	512	512	2048	2048
73	Learning rate	0.0004	0.0004	0.0006	0.0006
74	Total training tokens	20B	100B	230B	3.2T
75	Weight decay	0.1	0.1	0.1	0.1
76	Gradient clipping	1.0	1.0	1.0	1.0
77	Sequence length	4096	4096	4096	4096
78	Sliding window size, w	2048	2048	2048	2048
79	Number of layers, N	24	36	48	64
-	Model width, d_m	1536	2304	2048	2816
30	MLP intermediate size, d_p	4096	6144	8196	9984
81	Number of query heads	12	18	32	11
82	Number of key-value heads	12	18	4	1
83	Vocabulary size	32000	32000	50304	32064

In the generation configurations for the downstream tasks, we use greedy decoding for GSM8K, and Nucleus Sampling (Holtzman et al., 2019) with a temperature of $\tau = 0.2$ and top-p = 0.95 for HumanEval. For MBPP and SQuAD, we set $\tau = 0.01$ and top-p = 0.95.

LIMITATIONS & BROADER IMPACT Η

Although Samba demonstrates promising memory retrieval performance through instruction tuning, its pre-trained base model has retrieval performance similar to that of the SWA-based model, as

³https://github.com/sustcsonglin/flash-linear-attention

⁴https://github.com/datamllab/LongLM/blob/master/self_extend_patch/Llama.py ⁵https://github.com/jzhang38/TinyLlama

1296 1297 1298 1299 1300 1301 1302 1303 1304 1305	shown in Figure 8. This opens up future direction on further improving the Samba's retrieval ability without compromising its efficiency and extrapolation ability. In addition, the hybridization strategy of Samba is not consistently better than other alternatives in all tasks. As shown in Table 2, Mamba-SWA-MLP shows improved performance on tasks such as WinoGrande, SIQA, and GSM8K. This gives us the potential to invest in a more sophisticated approach to perform input-dependent dynamic combinations of SWA-based and SSM-based models (Ren et al., 2023). With the improved short-context performance and the long-term memorization ability of linear complexity LLMs such as Samba, cost-effective applications can be developed for personalized learning and automated tutoring. Samba can also be used for emotional accompaniment. The efficiency of the Samba architecture can save inference energy costs for models deployed on the edges, resulting in greener and more sustainable AI applications.
1306	
1307	
1308	
1309	
1310	
1311	
1312	
1313	
1314	
1315	
1316	
1317	
1318	
1319	
1320	
1321	
1322	
1323	
1324	
1325	
1326	
1327	
1328	
1329	
1330	
1331	
1332	
1333	
1334	
1335	
1336	
1337	
1338	
1339	
1340	
1341	
1342	
1343	
1344	
1345	
1346	
1347	
1348	
1349	