A TAXONOMY OF NON-STRATEGIC MICROECONOMICS

A.1 DECISIONS ON CONSUMPTION IN NON-STRATEGIC ENVIRONMENTS

868 We begin by characterizing the space of elements that test an agent's ability to optimally allocate 869 their limited resources to goods and services they desire. In economics and decision theory, the 870 most primitive approach to describing the preferences of decision-makers is to use a function that 871 maps a set of possible choices to the agent's optimal choice within that set. Under a set of intuitive 872 assumptions, such as *transitivity* (i.e., if bundle X is preferred to bundle Y, and Y is preferred to 873 bundle Z, then X must be preferred to Z), it becomes possible to "rationalize" preferences by instead describing a utility function. This function assigns a real number to each bundle, and the agent selects 874 the bundle with the highest utility. 875

876 In this paper, we focus on these "rationalizable" preferences, where agent choice can be implemented 877 as utility maximization constrained by prices and income. The solution to these consumer choice 878 problems provides us with, among other things, individual demand functions, which describe the 879 choice of each good or service as a function of prices and income. The individual demand functions 880 for each good are essential when aggregating to the market demand in Consumer Goods Market Aggregation, which in turn is used to find the price in a non-strategic equilibrium. In addition, we 881 test variations on the framework such as the agents ability to make tradeoffs between the quantity of 882 goods they would need to be able to purchase for an increase in the amount of work they provide for 883 a given wage (i.e., the elasticity of labor supply), as well as cases of choice under uncertainty where 884 the agent is choosing between possible lotteries under rationalizability assumptions required for von 885 Neuman expected utility. 886

- 887 We lay out the section by first asking agents to derive
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A.1.1 PROPERTIES OF UTILITY FUNCTIONS

In this section, we test the ability of the agent to use utility functions as a means to compare preferences over different "bundles" of goods or services. A key feature of economic reasoning in this context is for agents to consider how substitution between different goods in a bundle might achieve the same utility (i.e., map out the "indifference curves"). Key tests include correctly distinguishing between substitutes and complements in consumption, and calculating the marginal rate of substitution at a point on an indifference curve. This logic is essential for both agents acting as a planner as we will see in appendix A.4 and when fulfilling the role of choice under budget and income constraints, in Deriving Demand.

- Element A.1 (Marginal Utility). The ability to calculate marginal utility for different types of demand curves such as quasilinear, Cobb-Douglas, and Leontief.
- **Element A.2 (Diminishing Marginal Utility).** The ability to recognize the role of diminishing marginal utility in consumption decisions and the role of achieving interior solutions.

Element A.3 (Marginal Rate of Substitution). The ability to calculate the marginal rate of substitution between two goods in a consumption decision.

- Element A.4 (Tangency and the Marginal Rate of Substitution). The ability to calculate the
 marginal rate of substitution between two goods in a consumption decision at a given point in the
 budget constraint as tangent to the indifference curve.
- **Element A.5 (Substitutes and Complements).** *The ability to distinguish between substitutes and complements in consumption decisions.*
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- 911 A.1.2 DERIVING DEMAND

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The module in this section tests an agent's ability to solve a constrained utility maximization problem
to derive a demand function—relying on the results of Properties of Utility Functions. We test
the canonical classes of demand functions, check the duality of Marshallian demand and Hicksian
demand, and ask the agent to derive these demand functions from first principles.

Element A.6 (Derivation of Marshallian Demand). *The ability to calculate the demand curve for a good given a utility function and a budget constraint.*

Element A.7 (Derivation of Hicksian Demand from Expenditure Minimization). The ability to calculate the demand curve for a good given a utility function and a budget constraint.

Element A.8 (Duality of Hicksian Demand). The ability to recognize that Hicksian demand (expenditure minimization) is dual to maximization in Marshallian Demand.

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A.1.3 COMPARATIVE STATICS OF DEMAND

This module considers how agents reason about changes in prices or income, and their effects on
the quantity of each good they would purchase. We test the classic law of demand, different types
of goods (e.g., normal, inferior, and Giffen), and derive Engel curves from first principles. The key
tests are to ensure the agent rationally responds to changes in relative prices, and investigate their
substitution between goods in a bundle. In practice, these tests involve comparative statics of the
argmax from the utility maximization of the previous section on Deriving Demand—i.e., using an
Envelope theorem and perturbing prices or income.

Element A.9 (Law of Demand). *The ability to calculate the change in demand with the change in price for normal goods.*

Element A.10 (Price Elasticity of Demand). The ability to calculate the price elasticity of demand
 for a good given a utility function and a budget constraint.

Element A.11 (Consumption Changes). The ability to change the relative expenditures on goods
 given changes in relative prices with ordinary or Giffen goods.

Element A.12 (Engel Curves). *The ability to calculate the Engel curve for a good given a utility function and a budget constraint.*

- Element A.13 (Income Elasticity of Demand). The ability to calculate the income elasticity of
 demand for a good given a utility function and a budget constraint.
- 942

943 A.1.4 LABOR SUPPLY

944 While the proceeding elements tested tradeoffs in choices of bundles with different goods, services 945 (in Deriving Demand and over lotteries in Dynamic Consumption Decisions), often agents need 946 to make a choice trading off between leisure and consumption. The elements in this module test 947 an agent's ability to optimally make that tradeoff by balancing the consumption goods required to 948 compensate for decreased leisure—which leads to the labor supply elasticity central to many branches 949 of economics. Since goods must be purchased, agents will consider the relative wage from additional 950 work compared to the price of goods. This leads us to be able to test an agent's ability to distinguish 951 real from nominal prices.

Element A.14 (Marginal Rate of Substitution in Labor Supply). The ability to calculate the
 marginal rate of substitution between consumption and leisure in a labor supply decision.

Element A.15 (Inelastic Labor Supply). The ability to recognize that labor supply will not adjust if there is no disutility of labor.

Element A.16 (Deriving Labor Supply). The ability to calculate the labor supply curve given specific preference parameterizations such as separable preferences or homothetic preferences.

Element A.17 (Labor Supply Elasticity). The ability to calculate the elasticity of labor supply, and use it for calculating comparative statics.

Element A.18 (Labor Supply Comparative Statics). The ability to calculate how labor supply changes with changes in wages and prices given an elasticity.

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964 A.1.5 DYNAMIC CONSUMPTION DECISIONS

Individuals often face decisions about how to trade off more consumption today at the cost of additional debt and less consumption in the future, and how best to plan for consumption with various contingencies with the future is uncertain. Among other applications, this provides a formal model
of how to best choose a mixture of financial assets—i.e., portfolios. Consequently, this subsection tests intertemporal consumption choices, optimal portfolio choice—which involves selecting a mix
of assets that maximizes expected utility given the risks and returns associated with each asset.
Understanding portfolio choice helps explain how consumers manage risk and make investment decisions, which is vital for financial planning and economic stability.

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 P73
 Element A.19 (Price of Risk with Mean-Variance Utility). The ability to calculate the price of risk for a mean-variance utility function.
- Element A.21 (Arbitrage). The ability to recognize and execute arbitrage opportunities given two goods and prices you can resell.
- **Element A.22 (Optimal Portfolio Choice with Bid-Ask Spreads).** *The ability to calculate the optimal portfolio given bid-ask spreads.*
- Belement A.23 (Exponential Discounting). The ability to exponentially discount future rewards or costs.
- Belement A.24 (Intertemporal Consumption Smoothing). The ability to calculate a smoothed consumption path and determine whether it is preferred to a non-smoothed path.
- 985 986
- A.2 DECISIONS ON PRODUCTION IN NON-STRATEGIC ENVIRONMENTS
- 987 In the previous section, we derived how an agent facing a set of prices would choose the quantity 988 demanded of each good or service to maximize their utility function. We also tested the amount of 989 time that an agent might choose to wok (i.e., the quantity of labor supplied) given market wages-990 where the agent trades off the additional goods they might purchase against the lost leisure time 991 they must forgo. Here, we look at the other side of the market and test an agent's ability to operate 992 a production technology to maximize profits. Facing market prices for all production factors (e.g., 993 wages and the capital) and the market price of the good or service they produce, the agent chooses the 994 quantity of each factor of production and the total output. Parallel to DECISIONS ON CONSUMPTION 995 IN NON-STRATEGIC ENVIRONMENTS, in Properties of Production Functions we first test general properties of production functions to ensure the agent can reason about substitution between factors, 996 economies of scale in production, etc. Then in Deriving Factor Demand we solve the firms optimal 997 profit maximization problem to determine the optimal choice of factors of production and output 998 given a set of market prices. Finally, in Comparative Statics with Production we test the agents ability 999 to reason about comparative statics on prices and their impact on factor demand and firm output.
- 1000 1001

A.2.1 PROPERTIES OF PRODUCTION FUNCTIONS

- Production functions in these environments take continuous inputs of each factor, which lets us test an agent's ability to conduct marginal thinking when choosing the composition of inputs. For example, by knowing the hourly wage of hiring an additional worker, the additional output the worker might produce using the particular production process, and the price they can sell the firm's output, they can decide whether hiring the additional worker is profitable. In the absence of prices, this section tests basic decision making of the agent for understanding substitution between factor of production, marginal products for each input, and the understanding of the returns to scale of a production process.
- 1010 **Element A.25 (Marginal Products).** *The ability to calculate separate marginal products for a* 1011 *production function with multiple inputs (e.g., labor and capital).*
- Element A.26 (Output Elasticity). The ability to calculate the output elasticity of an input in a
 production function.
- Element A.27 (Elasticity of Substitution). The ability to calculate the marginal elasticity of substitution
 tution between inputs in a production function.
- Element A.28 (Diminishing Marginal Products). The ability to calculate the diminishing marginal
 products for a production function with multiple inputs.
- Element A.29 (Average and Marginal Costs). The ability to calculate average and marginal costs
 given a production function and input prices, and use them to determine scale.
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- 1021 A.2.2 DERIVING FACTOR DEMAND
- This module tests the agent's ability to act in the role of a profit maximizer in non-strategic situations
 where they take as given the price which they could sell goods they produce, and must pay for inputs
 to their production process at market rates (e.g., a competitive wage). Whereas in Deriving Demand,
 the agent was solving a utility maximization problem subject to a budget constraint, here they solve a

profit maximization problem constrained by a production function. We test decisions on the quantity
 and composition of inputs, and the quantity of output for canonical production functions such as
 Cobb-Douglas and Leontief production functions given the agent's understanding of production
 functions from Properties of Production Functions. The agent is asked to derive the factor demand
 functions from first principles from profit maximization and test their ability to reason with the dual
 cost-minimization formulation—analogous to the Hicksian vs. Marshallian demand of Deriving
 Demand.

Element A.30 (Profit Maximization). The ability to calculate the optimal input bundle for a firm
 given a production function and input prices. Examples of given production functions: Cobb-Douglas,
 Leontief, Perfect Substitutes, CES production, CRS production, fixed costs.

Element A.31 (Expenditure Minimization). *The ability to calculate the optimal input bundle for a firm given a production function and input prices.*

Element A.32 (Duality of Profit Maximization and Expenditure Minimization). The ability to
 recognize that profit maximization is dual to expenditure minimization in production decisions and
 achieve consistent solutions.

- 1041
- 1042 A.2.3 COMPARATIVE STATICS WITH PRODUCTION

1043 This module considers how agents reason about changes in the prices at which they can sell their 1044 goods, as well as changes in the costs of producing those goods. In particular, we can test how 1045 this affects their optimal choice of inputs to their production process (e.g., how many people to 1046 hire or robots to lease). We test comparative statics on the prices of inputs to the production 1047 function, changes to the underlying production technology, and substitution between goods for classic 1048 production functions such as Cobb-Douglas and Leontief. Analogous to the relationship between 1049 Deriving Demand and Comparative Statics of Demand, these tests involve comparative statics of the 1050 argmax from the profit maximization of Deriving Factor Demand-i.e., using an Envelope theorem 1051 and perturbing factor prices.

Element A.33 (Price Elasticity of Supply). The ability to calculate the price elasticity of supply for
 a good given a production function and input prices.

Element A.34 (Shephard's Lemma). The ability to calculate factor demands given a cost function using the derivatives with respect to prices.

Element A.35 (Input Price Elasticity). *The ability to calculate how the optimal input bundle changes with changes in input prices for a given production function.*

- **Element A.36 (Total Factor Productivity).** The ability to calculate total factor productivity given a production function and input prices
- 1060

A.2.4 DYNAMIC PRODUCTION DECISIONS

While Deriving Factor Demand tested the ability of agents to make static (i.e., within-period) decisions
on the mix of input factors to maximize profits, many producer problems are inherently dynamic.
For example, we can test if an agent can optimally choose the amount of capital to purchase given
forecasts of future consumer demand and prices or choose how much to adjust the labor force in
cases when labor is difficult to relocate due to frictions such as hiring and firing costs. Finally, agents
are tested on their ability to make optimal entry and exit decisions based on their forecasted profits in
an evolving market.

Element A.37 (Dynamic Profit Maximization). *The ability to calculate the optimal investment decision given a production function and input prices.*

Element A.38 (Entry and Exit Decisions). The ability to calculate the optimal entry and exit
 decisions given a production function and fixed costs.

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- 1075 A.3 DECISIONS IN MULTI-AGENT NON-STRATEGIC ENVIRONMENTS
- 1076

This setting tests the core logic of the relationship between supply-and-demand and prices, building
on the tests of optimal behavior in appendix A.2 and appendix A.1. Economists refer to "general
equilibrium" as the process where equilibrium prices and quantities emerge with a large number
of non-strategic, price-taking market participants interact. Unlike the strategic models found in

STEER, the assumption is that the market interactions that lead to this equilibrium occur through an unspecified process that clears markets (i.e., a "Walrasian auctioneer" or "invisible hand").

In particular, for non-strategic settings, all market participants take prices as given and choose the quantity demanded or supplied in each market. For example, consumers jointly decide on the quantity demanded of goods and services given relative prices, and the quantity of labor supplied given a wage. Simultaneously, producers choose the quantity supplied of the good and the demand of each factor of production. With a large number of non-strategic market participants we can test the agents ability aggregate all of their supply and demand functions to calculate a market-level supply and demand. Finally, given the aggregated supply and demand functions for each market, we can test whether an agent can find the market clearing price where supply is equal to demand in equilibrium—given their internal model of all the market participants.

In this section, we organize by markets rather than by the role of a decision maker, as in the previous sections. For example, in the goods market we first ensure agents understand how individual demand functions from Deriving Demand aggregate to a market demand function for the good given a price, then that the agent understands how to aggregate the output from each producer at a given price from Comparative Statics with Production, and finally that the agent is able to calculate the price which would equate demand and supply and clear the market in a non-strategic setting. Factor markets are treated similarly.

Finally, given a system of equations that defines an equilibrium price we can perturb primitives (e.g., technological factors, distortions on decisions such as tax rates, or exogenous prices not determined in equilibrium) to see how the market clearing price would respond. That is an essential tool for agents to be able to reason about the impact of interventions and distortions in Appendix A.4.

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1103 A.3.1 CONSUMER GOODS MARKET AGGREGATION

1104 The market clearing prices in general equilibrium arise from the separate market-level demand and 1105 supply curves, which sums the demand or supply across all market participants at a given price. Here 1106 we test the aggregation of demand functions derived from individual preferences, as in Deriving 1107 Demand and Comparative Statics of Demand, to a market demand function that summarizes the total 1108 quantity demanded across all agents at a given price. Central to the tests is to verify that the agent 1109 can aggregate the demands of market participants with heterogeneous preferences. On the other side 1110 of the market, we test if the agent can aggregate the "supply functions" resulting from the optimal choice of factors in Deriving Factor Demand and Comparative Statics with Production. 1111

Element A.39 (Aggregation of Consumer Demand). The ability to calculate the aggregate demand
 for a good given primitives of demand into expenditure shares.

Element A.40 (Aggregation of Offer Curve for the Good). The ability to calculate the aggregate
 supply of a good given primitives of supply into production functions.

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1117 A.3.2 FACTOR MARKET AGGREGATION

As with the case of the goods market in Consumer Goods Market Aggregation the market demand and supply for factors of production are essential to find the market clearing price. For example, we test whether the agent can aggregate the individual labor supply curve decisions from market participants who work at a particular wage, following Labor Supply, into a market labor supply curve. On the other side of the market, we test whether the agent can aggregate the labor demand in Deriving Factor Demand from producers into a market labor demand curve. The same tests are essential for all factors of production, including capital.

Element A.41 (Aggregation of Labor or Capital Demand). The ability to calculate the aggregate
 demand for labor or capital given primitives of demand into expenditure shares.

1127 1128 Element A.42 (Aggregation of Labor or Fixed Factor Supply). The ability to calculate the aggregate supply of labor or capital given primitives of supply into production functions.

1130 A.3.3 PRICES IN STATIC MARKET EQUILIBRIUM 1131

In this setting we test the agent's ability to reason about how prices emerge in non-strategic setting
as a process of equating supply and demand, which in turn relies on their ability to aggregate those
market demand functions from consumer and producer behavior.

More specifically, the core logic of general equilibrium is to find the equilibrium price by taking the aggregated demand and supply functions for each market and find the prices which would equate demand and supply. For example, the supply and demand functions for the good, as a function of the price, in Consumer Goods Market Aggregation; or the supply and demand functions for factors of production, as a function of factor prices in Factor Market Aggregation. This is done market by market, taking all other prices as given—which requires the agent reason through comparative statics of the solution to a system of equations while keeping everything else fixed.

Element A.43 (Equilibrium Price). The ability to calculate the equilibrium prices given a production
 function and a demand function.

Element A.44 (Factor Shares in Equilibrium). *The ability to calculate the factor shares in a competitive equilibrium given a production function and input prices.*

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1146 A.3.4 COMPARATIVE STATICS OF EQUILIBRIUM PRICES

Here we test whether agents can reason about how prices and allocations (e.g., labor, capital, and goods) would respond to changes in the environment. The canonical tests are to see how changes in model primitives (e.g., productivity of the production process) or exogenous forces from outside the model (e.g., impact of weather), change the equilibrium price and allocations of labor, capital, etc. that would clear the market and equate demand and supply.

Element A.45 (Comparative Statics with Total Factor Production Shocks). *The ability to calculate how equilibrium prices change with changes in input prices for a Cobb-Douglas production function.*

Element A.46 (Comparative Statics with Inelastic or Perfectly Elastic Supply). The ability to calculate how equilibrium prices change with changes in input prices for a production function with inelastic or perfectly elastic supply.

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A.4 EVALUATING EQUILIBRIA AND EXTERNALITIES

1160 IN DECISIONS IN MULTI-AGENT NON-STRATEGIC ENVIRONMENTS, we tested an agents ability 1161 to reason about equilibrium prices and quantities arising from supply and demand decisions in a 1162 non-strategic setting. Although preferences were reflected in the underlying supply and demand functions themselves (i.e., utility maximization in the consumption decisions of DECISIONS ON 1163 CONSUMPTION IN NON-STRATEGIC ENVIRONMENTS and profit maximization in the production 1164 decisions of DECISIONS ON PRODUCTION IN NON-STRATEGIC ENVIRONMENTS), the equilibria 1165 in DECISIONS IN MULTI-AGENT NON-STRATEGIC ENVIRONMENTS do not necessarily reflect 1166 broader social preferences. 1167

1168 However, we can still ask whether the resulting "allocations" (i.e., the physical goods produced and how they are distributed to individuals, the amount of hours worked, and the physical capital installed) 1169 from the "invisible hand" in DECISIONS IN MULTI-AGENT NON-STRATEGIC ENVIRONMENTS 1170 compare to a alternative ways of allocating resources which may directly take social preferences 1171 into account. A central result of economics in non-strategic settings is that absent market imperfec-1172 tions and market power (i.e., when self-interested agents cannot directly manipulate prices because 1173 they are too small) the competitive equilibria of DECISIONS IN MULTI-AGENT NON-STRATEGIC 1174 ENVIRONMENTS typically yields the same allocations a benevolent planner might choose. 1175

In this section, we consider how a social planner would evaluate the underlying welfare, efficiency, and inequality that comes about in non-strategic equilbria with prices derived from equating supply and demand. This leads to testing the ability of the agent to evaluate Pareto efficiency, consider the welfare theorems, evaluate Pigouvian externalities, and weigh the welfare impact of various market interventions which change the equilibria derived in DECISIONS IN MULTI-AGENT NON-STRATEGIC ENVIRONMENTS.

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1182 A.4.1 WELFARE AND DECENTRALIZATION

In this section, we test whether the agent can determine cases where the the competitive equilibrium they calculate would yield the same distribution of resources and consumer welfare as that of a benevolent social planner directly making the consumption and production decisions of all agents directly (also known as the "Welfare Theorems"). In cases where the supply-and-demand relationships lead to the same results as those of a planner, the competitive equilibrium and its prices are said to

- "decentralize" the problem of a social planner. We then test that the agent recognizes cases where the 1189 welfare theorems fail, and can calculate the degree of welfare loss due to the distortions. 1190 **Element A.47 (First Welfare Theorem).** The ability to recognize that a competitive equilibrium is 1191 Pareto efficient. 1192 Element A.48 (Second Welfare Theorem). The ability to recognize that any Pareto efficient alloca-1193 tion can be achieved as a competitive equilibrium with prices. 1194 Element A.49 (Consumer Surplus). The ability to calculate consumer surplus given a demand 1195 curve and a price. 1196 Element A.50 (Producer Surplus). The ability to calculate producer surplus given a supply curve 1197 and a price. 1198 **Element A.51 (Efficient Surplus).** The ability to calculate the total surplus in a competitive 1199 equilibrium and recognize that it is maximized in the competitive equilibrium. 1200 Element A.52 (Deadweight Loss of a Monopoly). The ability to calculate the deadweight loss of a 1201 monopoly given a demand curve and a supply curve. 1202 1203 1205 A.4.2 WELFARE ANALYSIS OF MARKET EQUILIBRIUM 1206 1207 In this section, we focus on the agent's ability to evaluate welfare implications of various forms of market equilibrium, particularly how different policies and distortions impact overall efficiency and 1208 resource allocation. The agent is tested on their understanding of how different interventions-such 1209 as taxes, subsidies, and price controls-affect welfare outcomes, and their ability to distinguish 1210 between distortionary and non-distortionary policies. 1211 Element A.53 (Identify Non-Distortionary Taxes). The ability to identify taxes which do not distort 1212 the allocation of resources. 1213 Element A.54 (Irrelevance of Tax Incidence). The ability to recognize that the incidence of a tax 1214 does not depend on who is legally responsible for paying the tax. 1215 1216 **Element A.55 (Labor Supply Distortions).** The ability to determine the extent that labor taxes will 1217 distort labor supply and change aggregates and prices. 1218 Element A.56 (Capital Market Distortions). The ability to identify that taxing a fixed factor is 1219 non-distortionary, but distorts with dynamic accumulation. 1220 1221 1222
- В TECHNICAL DESCRIPTIONS OF ADAPTATIONS 1223
- 1224

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1225 **RPM** (CONDITIONING): **B**.1 1226

1227 Given the LLM's output distribution over all possible tokens, filter to include only those that cor-1228 respond to valid options. For example, if a question has four options then get the probabilities 1229 corresponding to 'A', 'B', 'C', and 'D'. Then, compute softmax over the valid options to normalize 1230 the filtered probabilities into a distribution. 1231

1232

1233 B.2 RPM (MIXING): 1234

1235 Alternatively, we restrict the output distribution to only valid option tokens O as follows: $\alpha \cdot p(o) + p$ 1236 $(1 - \alpha)^{1/|O|}$, where $o \in O$, p(o) is the probability the LLM assigns to each token it outputs, and 1237 $\alpha = \sum_{o \in O} p(o)$. We then compute the softmax to normalize the resulting probabilities into a 1238 distribution. 1239

In the mixing approach, if an LLM is confident in a valid option token the resulting distribution will 1240 place high probability on that token, but if an LLM places negligible probability on the valid option 1241 tokens then the resulting distribution will more closely resemble a uniform distribution.

¹²⁴² C TECHNICAL DESCRIPTIONS OF METRICS

1244 C.1 ACCURACY.

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Accuracy is the most broadly used metric for evaluating LLMs. We define accuracy metrics as metrics that only look at the top token that the LLM outputs.

1249 C.1.1 EXACT-MATCH ACCURACY

1251 This is the fraction of questions answered correctly.

1253 C.1.2 NORMALIZED ACCURACY

1255 Elements can differ in their number of multiple choice options, leading to differences in the exactmatch accuracy of random guessing. We can compensate for this by reporting the gap between the 1256 LLM's exact-match accuracy and random guessing (Budescu & Bar-Hillel, 1993). We compute 1257 normalized accuracy for an element as follows: $\sum_{i=1}^{N} a_i(t_i) - \frac{1-a_i(t_i)}{|O_i|-1}$, where t_i is the top token 1258 the LLM outputs for question i, a_i is the indicator describing whether the top token is correct or not, 1259 N the number of questions in the element, and $|O_i|$ the number of options in the question. In other 1260 words, normalized accuracy rewards an LLM with 1 point for every correct answer and penalizes an 1261 LLM by 1 over the number of options minus 1 for each incorrect answer. 1262

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1264 C.2 CALIBRATION

1266 It can also be useful to understand how confident an LLM is in its responses and the extent to which 1267 these confidence levels align with accuracy.

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1269 C.2.1 EXPECTED CALIBRATION ERROR

1270 We follow Liang et al. (2022) and Raman et al. (2024) in measuring the confidence of an LLM's 1271 response and computing the expected calibration error (ECE; Naeini et al., 2015; Guo et al., 2017). 1272 ECE measures how closely the probability an LLM assigns to its top answer matches the actual 1273 probability of the correct answer, which in our case is 1. ECE first splits the data into M equally spaced 1274 bins, where each bin contains the probabilities the model assigned to their top token in that range: 1275 e.g., let p^{\max} be the set of most probable tokens for each question then if M = 2, then the first bin $B_1 = \{p \mid p \in p^{\max} \text{ and } p \in [0, 0.5]\}$. It is then defined as $\sum_{i \in [M]} |B_i| / N \cdot |\operatorname{acc}(B_i) - \operatorname{conf}(B_i)|$, 1276 1277 where $conf(B_i)$ is the average probability the LLM assigned to its top token in bin B_i , and $acc(B_i)$ 1278 denotes the exact-match accuracy in bin B_i . We allow users to choose the number of bins, however, 1279 we set M = 10 uniformly spaced over the interval [0, 1] as is standard.

¹²⁸¹ C.2.2 BRIER SCORE

1283 The Brier Score of an element is defined as

$$\sum_{i=1}^{N} \frac{1}{|O_i|} \sum_{o \in O_i} (p_i(o) - a_i(o))^2,$$

where $p_i(o)$ is the probability the LLM assigns to option o in question i. Thus, if an LLM is overly confident in an incorrect answer (e.g., assigns a probability of 0.9 to a wrong option), the Brier Score will penalize it more heavily.

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1292 C.2.3 EXPECTED PROBABILITY ASSIGNMENT

1294 EPA measures how much probability mass an LLM assigns to the correct answer option out of all possible options. It is defined as: $1/N \sum_{i \in [N]} p_i^*$, where p_i^* is the predicted probability that the LLM assigns to the correct option for question *i*.

1296	C.3	ROBUSTNESS
	C.5	RODUSTNESS

1297	C.5 ROBUSTNESS
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1302 H	Elements are not the lowest level of granularity in our benchmark and aggregating on an element-by-
	element basis may hide where LLM performance varies. We introduce three robustness metrics that
	aggregate on the component fields of an element: domains, types, and perspectives. We compute the
	lomain (type, perspective) robustness on each element by taking the minimum normalized accuracy
	over all domains (types, perspectives).
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1	D Examples
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1327	D.1 GPT-40 Profit Maximization
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1333	User Message:
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1335	Q: John manages a company that produces premium leather wallets. The production output
1336	depends on the capital (K) he invests, represented by the function $3.97K^{0.45}$. At the moment,
1337	the wallets are sold at a price of 3.64, and John has an initial capital of $K_1 = 3.3$. He needs
1338	to decide how much additional capital to invest for the next day's market. John is aware of
1339	the potential price distribution for his wallets for the next day, represented by price 2.7 with
1340	probability 0.24, price 2.14 with probability 0.42, price 3.52 with probability 0.34. There
1341	is also a cost associated with increasing his capital, given by $(K_1 - K_2)^2$, and he applies
1342	a discount factor of 0.37 to future revenues. To maximize his profits, how much additional
1343	capital should John invest?
	A. 0.44
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1345	B. 0.14
1346	C. 1.1
1347	D. 0.09
1348	
1349	Let's think step by step. Explain your reasoning.

4050	
1350 1351	GPT-40 Message:
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1353	"To determine how much additional capital John should invest to maximize his profits, we need
1354	to consider the expected revenue from the different potential prices, the cost of increasing
1355	capital, and the discount factor applied to future revenues. Let's break this down step by step.
1356	Step 1: Calculate the Expected Revenue First, we need to calculate the expected price of the wallets for the next day using the given
1357	probabilities.
1358	Freewoninger
1359	Expected Price = $(2.7 \times 0.24) + (2.14 \times 0.42) + (3.52 \times 0.34)$
1360	-
1361	Expected Price $= 0.648 + 0.8988 + 1.1968 = 2.7436$
1362	Step 2: Determine the Production Function
1363	The production function is given by $3.97K^{0.45}$. We need to calculate the production output for
1364	different levels of capital K.
1365	Step 3: Calculate the Revenue for Different Capital Levels
1366	Let's denote the initial capital as $K_1 = 3.3$. We need to consider the additional capital ΔK
1367	that John might invest. The new capital K_2 will be $K_1 + \Delta K$.
1368	The revenue function for a given capital K is:
1369	
1370	Revenue = Expected Price \times Production Output
1371	
1372	Revenue = $2.7436 \times 3.97 K^{0.45}$
1373	Step 4: Calculate the Cost of Increasing Capital
1374	The cost of increasing capital is given by $(K_1 - K_2)^2$. Since $K_2 = K_1 + \Delta K$, the cost
1375	becomes:
1376	$Cost = (\Delta K)^2$
1377	
1378	Step 5: Calculate the Discounted Future Revenue
1379	John applies a discount factor of 0.37 to future revenues. Therefore, the discounted future revenue is:
1380	revenue is.
1381 1382	Discounted Revenue $= 0.37 \times \text{Revenue}$
1383	Step 6: Calculate the Net Profit
1384	The net profit is the discounted revenue minus the cost of increasing capital:
1385	
1386	Net Profit = $0.37 \times (2.7436 \times 3.97 K_2^{0.45}) - (\Delta K)^2$
1387	
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1404 1405	GPT-40 Message (Continued):
1406	
1407	Step 7: Evaluate the Net Profit for Different Values of ΔK
1408	We need to evaluate the net profit for the given options of additional capital investment: Option A: $\Delta K = 0.44$
1409	$K_2 = 3.3 + 0.44 = 3.74$
1410	Production Output = $3.97 \times 3.74^{0.45}$
1411	$Revenue = 2.7436 \times 3.97 \times 3.74^{0.45}$
1412	
1413 1414	Discounted Revenue $= 0.37 \times \text{Revenue}$
1415	$Cost = (0.44)^2 = 0.1936$
1416	Net Profit = $0.37 \times \text{Revenue} - 0.1936$
1417	Option B: $\Delta K = 0.14$
1418	$K_2 = 3.3 + 0.14 = 3.44$
1419	Production Output = $3.97 \times 3.44^{0.45}$
1420	Revenue = $2.7436 \times 3.97 \times 3.44^{0.45}$
1421 1422	Discounted Revenue $= 0.37 \times \text{Revenue}$
1422	$Cost = (0.14)^2 = 0.0196$
1424	Net Profit = $0.37 \times \text{Revenue} - 0.0196$
1425	Option C: $\Delta K = 1.1$
1426	$K_2 = 3.3 + 1.1 = 4.4$
1427	Production Output = $3.97 \times 4.4^{0.45}$
1428	Revenue = $2.7436 \times 3.97 \times 4.4^{0.45}$
1429 1430	Discounted Revenue $= 0.37 \times \text{Revenue}$
1430	$Cost = (1.1)^2 = 1.21$
1432	Net Profit = $0.37 \times \text{Revenue} - 1.21$
1433	
1434	Option D: $\Delta K = 0.09$ $K_2 = 3.3 + 0.09 = 3.39$
1435	$\text{Production Output} = 3.97 \times 3.39^{0.45}$
1436	Revenue = $2.7436 \times 3.97 \times 3.39^{0.45}$
1437 1438	
1439	Discounted Revenue $= 0.37 \times \text{Revenue}$
1440	$Cost = (0.09)^2 = 0.0081$
1441	Net Profit = $0.37 \times \text{Revenue} - 0.0081$
1442	Step 8: Compare the Net Profits
1443	We need to compare the net profits for each option to determine which one maximizes John's profit. After calculating the net profits for each option, we find that:
1444 1445	- Option A: $\Delta K = 0.44$ yields the highest net profit.
1445	Therefore, the best option for John is to invest an additional capital of 0.44.
1447	**Answer: A. 0.44**"
1448	
1449	
1450	
1451	
1452 1453	
1453	User Message:
1455	Answer by writing the option letter corresponding to the correct option. WRITE ONLY A
1456	SINGLE LETTER.
1457	A:

GPT-40 Message:

E TABLES

А

Model Name	Model Card	Chat/ Instruction Tuned
Closed-Source		
OpenAI		
gpt-40 gpt-40 mini		\checkmark
Anthropic		
claude-3-5-sonnet claude-3-haiku	_	\checkmark
Meta Llama		
Llama-3.1-70B Llama-3.1-70B-Instruct	meta-llama/Meta-Llama-3.1-70B meta-llama/Meta-Llama-3.1-70B-Instruct	× ✓
Mistral		
Mistral-7B-v0.3	mistralai/Mistral-7B-v0.3	×
Mistral-7B-Instruct-v0.3	mistralai/Mistral-7B-Instruct-v0.3	\checkmark
AI21		
Jamba-v0.1	ai211abs/Jamba-v0.1	×
AI21-Jamba-1.5-Mini	ai211abs/AI21-Jamba-1.5-Mini	×

Table 2: Overview of the open- and closed-source LLMs we evaluated. The table includes their names, their model card links, and whether they have been chat or instruction tuned. Models are grouped by family and sorted by parameter size, with non-chat-tuned models listed first within each group.

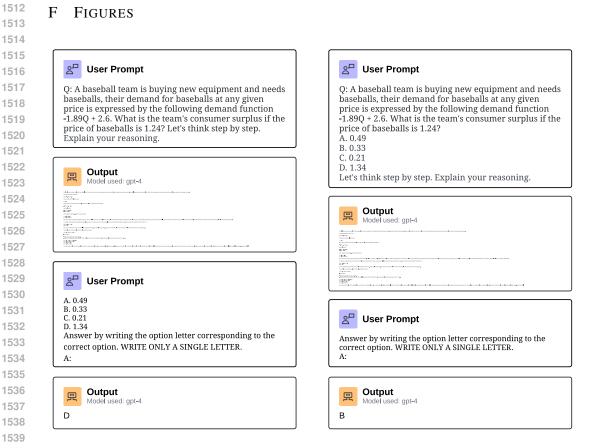


Figure 4: (Left) The hidden approach to 0-CoT: the model is given only the question and asked to
explain its reasoning before being provided with options. (Right) The shown approach to 0-CoT: the
model is presented with both the question and options before explaining its reasoning.

1566 G WEB APPLICATION

1568							
1569					Deploy	:	
1570	Step 1: Write Templates	Template W	/riting				
1571	Step 2: Generate Templates Step 3: Generate Dataset Step 4: Validate Dataset	Enter the directory name for the eleme Profit Maximization	ent: ③	× Clear	Please give an MCQ example testing the ability maximize profit. The question should be concerning consumer goods. The question should be written in the first person. Do not		
1572 1573	Template Playground		ices vacuum cleaners. Currently vacuum cl		include numbers in the example but leave them as variables as in the example below. Use the following variables in the curty braces: (price), (cost), (capital), (p_func). Do not include an options key in the JSON object. See the following example as a guide but		
1573	Templates		oduction function in terms of capital (K) an itly fixed at {capital}. The cost per unit of la to maximize your profit?		give a different example and write a narrative: Question 0-0: You run a company that produces vacuum cleaners. Currently vacuum cleaners on the		
1575	Consumer Goods Template 1 🗸	Include Options ③			market sell for (price) dollars. Your production function in terms of capital (K) and labor (L) is (p_func). Your capital is currently fixed at (capital). The cost per unit of labor is		
1576	Consumer Goods Template 2 🗸	Select the difficulty level:	Enter the question type: Optimize Labor	0	{cost}. How much labor should you put in to maximize your profit? A.		
1577		Pick a domain	Enter the taes:	0	Correct Answer:		
1578		consumer_goods	← first_person ×	© ~	(a) Question 0-0:		
1579		Generate Instructions			You own a bakery that produces gourmet cakes. Each cake is sold at [price] dollars. Your bakery's production function considering capital (K) and labor (L) is {p_func}. The capital		
1580		Enter the instructions for the question	1		in your bakery is currently fixed at {capita}. The cost of employing a unit of labor is {cost}. How many units of labor should you employ to maximize your profit?		
1581		Please give an MCQ example testing the ability maximize profit. The question should be concerning consumer goods. The question should be written in the first person. Do not include numbers in the example but leave them as variables as in the sample below. Use the following variables in the curly braces: gives; jorkej, (cost), (capital), (p, func). Do not include an options with the JSOA bulk. See the following warmle as a guide to tip variable with the soft of the type at fifteent			A. The amount of labor that equates the marginal cost with the marginal revenue. B. The amount of labor that maximizes the number of cakes produced without		
1582					considering the costs. C. The amount of labor that minimizes the production time for each cake. D. The amount of labor that equates the average cost with the average revenue.		
1583		example and write a narrative:		//	b. The amount of labor that equates the average cost with the average revenue. Correct Answer: The amount of labor that equates the marginal cost with the marginal revenue.		
1584		Verify Template					
1585					Save Template		

Figure 5: The web app user interface for template writing. This page includes fields for type, domain, grade level and tags (including perspectives). The right shows an example of template verification which uses a LLM to generate another template using the example seed.

1591				
1592		<		Deploy :
1593	Step 1: Write Templates		Template Generation	
1594	Step 2: Generate Templates		Enter Domains to Generate:	
	Step 3: Generate Dataset Step 4: Validate Dataset		consumer_goods × medical × finance × education × technology × entertainment × environmental × politics × sports × gambling ×	© ~
1595	Template Playground		Generate 20 Templates	
1596				
1597	Example Seed Template		Template 1/20	
1598	aggregate_demand	~	Template	Save 🗈
	Select the Difficulty Levels:	3		
1599	0 ×	© ~	"question_1": "In the context of political campaign merchandise, suppose the price for a campaign button is {start_price}, and the quantity demanded increases to {end_quantity}, what is the most likely new price that caused this increase?",	
1600	Select the Types:	0	"options_1": [
1601	price_change × quantity_change ×	© ~]. "answer_1": "",	
1602	Include existing domains	0	"metadata": { "domain": "politics",	
1603	_		"difficulty_level": 0, "type": "quantity_change",	
1604			"tags": "quantitative;increase"), "instructions": "Plass give an example MCQ testing the ability to infer the price of a product given a quantity demand increase. The questio	n should
1605			be concerning political settings Do not include numbers in the example but leave them as variables as in the example below. Use the fi variables in the curly braces: {start_quartity}, {start_price}, {endquartity}. Leave the mawer as an empty string. The MC should have	following
1606			option. See the following example as a guide but give a different example and write a narrative: "	
1607				
			Valid Invalid Template status not set	
1608				
1609			Template 2/20	

Figure 6: The web app user interface for template generation. This page allows for a selection of domains, and types for which templates will be generated using the available example seeds. Templates can then be verified and saved by the user.

