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# CrysMMNet: Multimodal Representation for Crystal Property Prediction

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## Abstract

Machine Learning models have emerged as a powerful tool for fast and accurate prediction of different crystalline properties. Existing state-of-the-art models rely on a single modality of crystal data i.e crystal graph structure, where they construct multi-graph by establishing edges between nearby atoms in 3D space and apply GNN to learn materials representation. Thereby, they encode local chemical semantics around the atoms successfully but fail to capture important global periodic structural information like space group number, crystal symmetry, rotational information etc, which influence different crystal properties. In this work, we leverage textual descriptions of materials to model global structural information into graph structure and learn a more robust and enriched representation of crystalline materials. To this effect, we first curate a textual dataset for crystalline material databases containing descriptions of each material. Further, we propose CrysMMNet, a simple multi-modal framework, which fuses both structural and textual representation together to generate a joint multimodal representation of crystalline materials. We conduct extensive experiments on two benchmark datasets across ten different properties to show that CrysMMNet outperforms existing state-of-the-art baseline methods with a good margin. We also observe that fusing the textual representation with crystal graph structure provides consistent improvement for all the SOTA GNN models compared to their own vanilla versions. We have shared the textual dataset, that we have curated for both the benchmark material databases, with the community for future use.

## 1 INTRODUCTION

In the recent past, we have witnessed a surge of interest in developing machine learning models Seko et al. [2015], Pilia et al. [2015], Lee et al. [2016], De Jong et al. [2016], Seko et al. [2017], Isayev et al. [2017], Ward et al. [2017], Lu et al. [2018], Im et al. [2019] for fast and accurate property prediction of crystalline materials. Crystalline materials are typically modeled by a minimal unit cell containing all the constituent atoms in different coordinates, repeated infinite times in 3D space on a regular lattice, which makes material structures periodic in nature. A key challenge in learning crystal representation is how to capture accurately global periodic structural information along with local chemical semantics. Recent state-of-the-art models Xie and Grossman [2018], Chen et al. [2019], Louis et al. [2020], Park and Wolverton [2020], Schmidt et al. [2021], Choudhary and DeCost [2021], Hsu et al. [2021], Das et al. [2022], Yan et al. [2022] construct multi-edge graphs for a 3D material structure where they create edges between nearby atoms within a pre-specified distance threshold in 3D space and apply GNN model to learn representations of crystal structures that are optimized for downstream property prediction tasks. Although existing variants of GNN models predict different crystal properties with high precision, they rely on a single modality of crystal data i.e crystal graph structure which limits the expressive power of these models. The architectural innovations of these approaches are primarily based on incorporating specific domain knowledge of the local bonding environment, such as explicitly encoding bond angle Choudhary and DeCost [2021], dihedral angle Hsu et al. [2021], etc. but they fail to incorporate crucial global periodic structural information like lattice constraint, space group number, crystal symmetry, rotational information, component 3D orientation, heterostructure information, etc, which will enrich its representation and subsequently aid the property prediction accuracy.

In this work, we propose to learn a more robust and enriched representation by using multi-modal data i.e graph structure and textual description of materials. One of the major advan-

tages of using the textual description of materials is it provides a diverse set of periodic structural information which is useful to estimate different crystal properties but difficult to incorporate explicitly into a graph structure. Leveraging textual modalities beyond graph structures of materials remains unexplored by the research community and to the best of our knowledge, there is no existing dataset containing textual descriptions of the materials. Hence, we first curate the textual dataset of two popular materials databases (Graph-based), Material Project (MP) and JARVIS, containing textual descriptions of each material of those databases. We used a popular tool robocrystallographer Ganose and Jain [2019] to generate descriptions for global crystal structures, which looks at the structural symmetry, local environment, and extended connectivity to generate a description that includes space group number, crystal symmetry, rotational information, component orientations, heterostructure information, etc.

Further, we propose, CrysMMNet (**Crystal Multi-Modal Network**), a simple multi-modal framework for crystalline materials, which has two components: Graph Encoder and Text Encoder. Given a material, Graph Encoder uses its graph structure and applies GNN based approach to encode the local neighborhood structural information around a node (atom), and subsequently learn graph (crystal) representation. On the contrary, Text Encoder is a transformer-based model, which encodes the global structural knowledge from the textual description of the material and generates a textual representation. Finally, both graph structural and textual representation are fused together to generate a more enriched multimodal representation of materials, which captures both global and local structural knowledge and subsequently improves property prediction accuracy.

To show the merit of our proposed algorithm, we performed comprehensive experiments on two popular benchmark datasets, Materials Project and JARVIS-DFT, across ten diverse sets of properties and compare the results with popular state-of-the-art models. We observe that for all the properties CrysMMNet can achieve the lowest error in comparison with other baseline models. In addition, our results demonstrate that multi-modal representation learning helps to achieve even better improvements when the dataset is sparse. We also perform some ablation studies to investigate the expressiveness of textual representation and robustness of multimodal representation on different GNN architectural choices. Result shows, textual representations alone are not expressive enough to learn the structure-property relationship of the materials. Moreover, fusing both graph structural and textual representation together leads to substantial performance improvements for all the state-of-the-art GNN models compared to their vanilla versions. We also investigate the influence of local compositional information and global material structural knowledge encoded through textual representation and found for all crystal properties both local and global knowledge improves the downstream

property prediction accuracy. We have shared the textual dataset, that we have curated for both the benchmark material databases with the community for future use.<sup>1</sup>

## 2 BACKGROUND AND RELATED WORK

### 2.1 CRYSTAL REPRESENTATION

The structure of a crystalline material can be modeled by a minimum unit cell, repeated infinite times in three-dimensional (3D) euclidean space on a regular lattice, which makes the crystalline structure periodic in nature. As mentioned in Xie et al. [2021], Yan et al. [2022], for a given crystal we can describe its unit cell by two matrices: Feature Matrix ( $\mathbf{X}$ ) and Coordinate Matrix ( $\mathbf{C}$ ). Feature Matrix  $\mathbf{X} = [\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_n]^T \in R^{n \times d}$  denotes atomic feature set of the material, where  $\mathbf{x}_i \in R^d$  corresponds to the d-dimensional feature vector of i-th atom. On the other hand, Coordinate Matrix  $\mathbf{C} = [\mathbf{c}_1, \mathbf{c}_2, \dots, \mathbf{c}_n]^T \in R^{n \times 3}$  denotes atomic coordinate positions, where  $\mathbf{c}_i \in R^3$  corresponds to cartesian coordinates of i-th atom in the unit cell. Further, there is an additional lattice matrix  $\mathbf{L} = [\mathbf{l}_1, \mathbf{l}_2, \mathbf{l}_3]^T \in R^{3 \times 3}$ , which describes how a unit cell repeats itself in the 3D space towards  $\mathbf{l}_1, \mathbf{l}_2$  and  $\mathbf{l}_3$  direction to form the periodic 3D structure of the material. Formally, a given crystal can be defined as  $\mathbf{M} = (\mathbf{X}, \mathbf{C}, \mathbf{L})$  and we can represent its infinite periodic structure as

$$\hat{\mathbf{C}} = \{\hat{\mathbf{c}}_i | \hat{\mathbf{c}}_i = \mathbf{c}_i + \sum_{j=1}^3 k_j \mathbf{l}_j\}; \hat{\mathbf{X}} = \{\hat{\mathbf{x}}_i | \hat{\mathbf{x}}_i = \mathbf{x}_i\} \quad (1)$$

where  $k_1, k_2, k_3, i \in Z, 1 \leq i \leq n$ .

### 2.2 CRYSTAL PROPERTY PREDICTION USING GNNS

Graph neural networks have emerged as highly promising models in various domains of computer science, showcasing significant potential in many real-world applications including social networks Hamilton et al. [2017], Chen et al. [2018], Dai et al. [2018], recommender systems Berg et al. [2017], Ying et al. [2018], hyper-networks Yadati et al. [2019], Bandyopadhyay et al. [2020], chemical and biological networks Duvenaud et al. [2015], Gilmer et al. [2017] etc. Recently, graph neural network (GNN) based approaches have been very effective to encode structural information of the crystal materials into enriched embedding space so that it can predict different crystal properties with high accuracy. CGCNN Xie and Grossman [2018] is the first proposed model, which represents 3D crystal structure as an undirected weighted multi-edge graph  $\mathcal{G} = (\mathcal{V}, \mathcal{E}, \mathcal{X}, \mathcal{F})$  where  $\mathcal{V}$  denotes the set of nodes (atoms) in the unit cell

<sup>1</sup>Source code and dataset of CrysMMNet is made available at <https://github.com/kdmsit/crysmmnet>

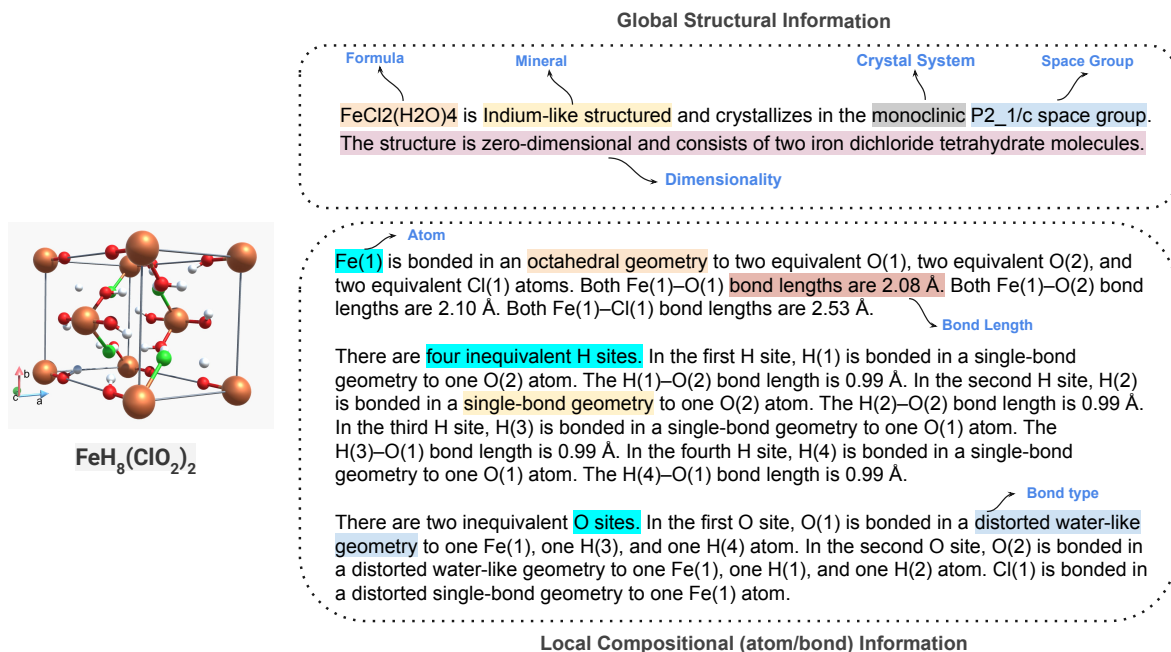


Figure 1: Textual description of  $\text{FeH}_8(\text{ClO}_2)_2$  material from JARVIS dataset generated by Robocrystallographer. The generated text contains both local chemical compositional information related to atom/bonds (like site coordination, geometry, polyhedral connectivity, and tilt angles) and global structural knowledge (like mineral type, space group information, symmetry, and dimensionality).

of material and  $\mathcal{E} = \{(u, v, k_{uv})\}$  denotes a multi-set of node pairs and  $k_{uv}$  denotes number of edges between a node pair  $(u, v)$ .  $\mathcal{X} = \{(x_u | u \in \mathcal{V})\}$  denotes the node feature set, which includes different chemical properties like electronegativity, valance electron, covalent radius, etc. Finally,  $\mathcal{F}_i = \{(s^k)_{(u,v)} | (u, v) \in \mathcal{E}, k \in \{1..k_{uv}\}\}$  denotes the multi-set of edge weights where  $s^k$  corresponds to the  $k^{\text{th}}$  bond length between a node pair  $(u, v)$ , which signifies the inter-atomic bond distance between two atoms. Further, CGCNN develops a graph convolution neural network to update node features based on their local chemical and structural environment.

Following CGCNN, there are a lot of subsequent studies Chen et al. [2019], Louis et al. [2020], Park and Wolverton [2020], Schmidt et al. [2021], where authors proposed different variants of GNN architectures for effective crystal representation learning. Through multiple layers of graph convolutions, these models can implicitly encode many-body interactions. Further, ALIGNN Choudhary and DeCost [2021] explicitly captures many-body interactions by incorporating bond angles and local geometric distortions into the GNN encoding module to enhance property prediction accuracy and became SOTA for a large range of properties. Recently, transformer-based architecture Matformer Yan et al. [2022] is proposed to learn the periodic graph representation of the material, which is invariant to periodicity and can capture repeating patterns explicitly. Matformer marginally improves the performance compared to ALIGNN, however, is much

faster than it. Moreover, scarcity of labeled data makes these models difficult to train for all the properties, and recently, some key studies Jha et al. [2019], Das et al. [2022, 2023] have shown promising results to mitigate this issue using transfer learning, pre-training, and knowledge distillation respectively.

### 3 METHODOLOGY

In this section, we first discuss the insights on the textual dataset that we have curated for two popular crystalline databases and explain the local compositional and global periodic information we are able to encode using textual representation, which is difficult to incorporate explicitly into a graph structure. Then we give a detailed overview of our proposed multi-modal framework CrysMMNet that generates joint embedding for materials, which facilitates accurate property prediction.

#### 3.1 TEXTUAL DATASET

Leveraging textual modalities beyond the conventional graph structure of the materials to capture both local atomic and global periodic knowledge remains largely unexplored by the research community. To the best of our knowledge, there is no existing dataset containing textual descriptions of the materials. Hence, we first curate the textual dataset

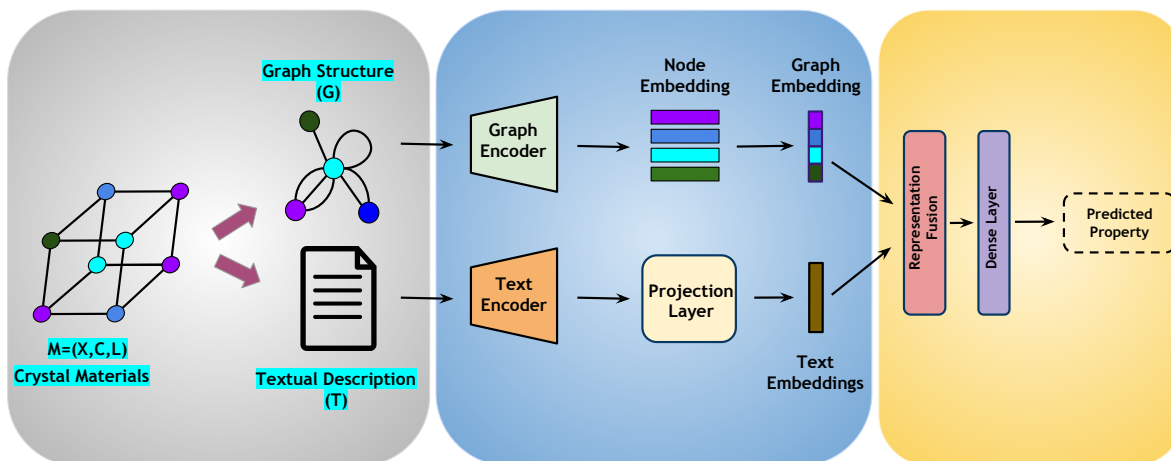


Figure 2: Overview of our adopted methodology CrysMMNet. Given Crystal Material ( $M$ ), we use two modalities - Graph Structure ( $\mathcal{G}$ ) and Textual Description ( $\mathcal{T}$ ). Graph structure ( $\mathcal{G}$ ) is passed through a graph encoder to generate graph embedding ( $\mathcal{Z}_G$ ). Textual Description ( $\mathcal{T}$ ) is fed through a text encoder followed by a projection layer to generate text embedding ( $\mathcal{Z}_T$ ). Finally, both the representations are fused together and predict the crystal properties based on joint modeling of the input modalities.

for two popular material databases JARVIS and Material Project (MP), containing textual descriptions for each material of those databases. Conventionally, in these databases, the periodic structure of the materials is represented in Crystallographic Information File (CIF File). We use Robocrytallographer Ganose and Jain [2019], which is a free utility, to generate a textual description of the material from the CIF file. Robocrytallographer decomposes crystal structures into local compositional (site coordination, geometry, polyhedral connectivity, and tilt angles) and global structural (mineral type, space group information, symmetry, dimensionality) components (Figure 1) and output this information in three formats: JSON for machine use, human-readable text, and machine learning format. In this work, we use human-readable text for collecting textual datasets, which are easily interpretable and resembles a human description of the crystal structure.

**Local compositional** information describes local chemical environments around different atoms and inter-atomic bonds in a unit cell. It provides a detailed description of different sites of the materials, like atomic compositions of different sites, site coordination, inter-atomic connectivity through chemical bonds, bond type, and length. Further, the geometry of each site is mentioned and the presence of corner-sharing tetrahedra connectivity is specified. On the contrary, **global structural** information illustrates the global environment i.e. periodic structure and orientation of the material in 3D space. The most useful information it provides is regarding crystal symmetry, which includes the specific space group and crystal system the material belongs to. Space group is used to describe the symmetry of a unit

cell of the crystal material in 3D space. In materials science literature there are 230 unique space groups and each crystal (graph) has a unique space group number. Further based on the space group level information can classify a crystal graph into 7 broad groups of crystal systems like Triclinic, Monoclinic, Orthorhombic, Tetragonal, Trigonal, Hexagonal, and Cubic. Moreover, it contains the mineral type of the material and the dimensionality of the crystal structure. Minerals are naturally occurring, inorganic substances with a specific chemical composition and a crystalline structure. The most common types include silicates (which contain silicon and oxygen), carbonates (which contain carbon and oxygen), sulfates (which contain sulfur and oxygen), halides (which contain a halogen element), oxides (which contain oxygen and one or more other elements), and sulfides (which contain sulfur and one or more other elements). Examples of minerals in each category include quartz, calcite, gypsum, halite, hematite, and pyrite. The chemical composition and crystal structure of a mineral determine its properties, such as its hardness, color, and cleavage. Further, dimensionality of a material is a significant global feature that refers to the number of dimensions that a particular component of the material spans. The dimensionality of a bonded cluster of atoms can be determined by calculating the rank of the subspace spanned by the central atom and its periodically connected neighbors.

A comprehensive understanding of both local and global environments is necessary for robust prediction of material properties. For example, in the case of formation energy, the local chemical environment, such as atom composition, bond length, and bond angles, plays a crucial role in deter-

mining the electronic and geometric structure of the material, which directly affects its formation energy. A slight variation in the local environment can result in significant changes in the electron density and, subsequently, the energy required to form the materials. Similarly, the global chemical environment, like the space group, has a profound impact on the formation energy by controlling the arrangement of atoms within the material. Different space groups are associated with different crystal structures and packing arrangements, which can lead to different formation energies. Moreover, the study by Larsen *et. al* [2019] showed that the formation energies of layered materials can be related to their dimensionality, highlighting the importance of considering this feature in the investigation of materials.

### 3.2 MULTI-MODAL FRAMEWORK

Next, we propose a simple, yet effective multi-modal framework, CrysMMNet, for graph and textual embedding of materials, which realizes material dataset as  $D = \{(\mathcal{G}, \mathcal{T}), \mathcal{Y}\}$ , where  $\mathcal{G}, \mathcal{T}$  and  $\mathcal{Y}$  denote multi-graph structure, textual description and property value the material respectively. In our multi-modal architecture, the goal is to learn a function  $f_\theta(\mathcal{G}, \mathcal{T})$

$$f_\theta : (\mathcal{G}, \mathcal{T}) \rightarrow \mathcal{Y} \quad (2)$$

By design, CrysMMNet (as shown in Figure 2) is composed of three modules: graph encoder  $M_V(\mathcal{G}) \rightarrow \mathcal{Z}_G$ , text encoder  $M_L(\mathcal{T}) \rightarrow \mathcal{Z}_T$ , and joint embedding model  $E(\mathcal{Z}_G, \mathcal{Z}_T) \rightarrow \mathcal{Z}$ , where  $\mathcal{Z}_G, \mathcal{Z}_T$  and  $\mathcal{Z}$  are graph-level, textual and multimodal embedding respectively. Next, we explain each part of the CrysMMNet framework in detail.

#### 3.2.1 Graph Encoder:

CrysMMNet adopts a GNN architecture inspired by ALIGNN Choudhary and DeCost [2021] as Graph Encoder, to encode the chemical, structural, and bond angular information of a crystal graph  $\mathcal{G}$ . We derive additional line graph  $\mathcal{L}(\mathcal{G})$  from the crystal graph  $\mathcal{G}$  to describe the angles between the edges in  $\mathcal{G}$ , where nodes and edges in line graph  $\mathcal{L}(\mathcal{G})$  correspond to inter-atomic bonds and bond angles. We denote  $h_i^l, e_{i,j}^l$  and  $t_{i,j,k}^l$  as  $l$ -th layer representation for  $i$ -th atom,  $\{i, j\}$ -th bond, and  $\{i, j, k\}$ -th angle (triplet) respectively. Graph encoder alternates edge-gated graph convolution layers between  $\mathcal{L}(\mathcal{G})$  and  $\mathcal{G}$  to propagate bond angular information through inter-atomic bond representation to atom embedding and vice versa. Specifically, at the  $(l)$ -th layer, given the line graph  $\mathcal{L}(\mathcal{G})$ , we apply Gated Graph ConvNet (GatedGCN) Dwivedi et al. [2020] to update triplet representation and generate bond messages  $m$  as

follows :

$$\begin{aligned} t_{i,j,k}^{l+1} &= t_{i,j,k}^l + \gamma \left( \text{BN} \left( A_{lg}^l e_{i,j}^l + B_{lg}^l e_{j,k}^l + C_{lg}^l t_{i,j,k}^l \right) \right) \\ \hat{t}_{i,j,k}^{l+1} &= \frac{\sigma(t_{i,j,k}^{l+1})}{\sum_{(j,m) \in N_{i,j}} \sigma(t_{i,j,m}^{l+1}) + \epsilon} \\ m_{i,j}^l &= e_{i,j}^l + \gamma \left( \text{BN} \left( W_{lg}^l e_{i,j}^l + \sum_{\substack{(j,k) \\ \in N_{i,j}}} \hat{t}_{i,j,k}^{l+1} \odot V_{lg}^l e_{j,k}^l \right) \right) \end{aligned} \quad (3)$$

Further, we apply another GatedGCN on the crystal graph  $\mathcal{G}$  and update bond and atom features as follows :

$$\begin{aligned} e_{i,j}^{l+1} &= e_{i,j}^l + \gamma \left( \text{BN} \left( A_g^l h_i^l + B_g^l h_j^l + C_g^l m_{i,j}^l \right) \right) \\ \hat{e}_{i,j}^{l+1} &= \frac{\sigma(e_{i,j}^{l+1})}{\sum_{k \in N_i} \sigma(e_{i,k}^{l+1}) + \epsilon} \\ h_i^{l+1} &= h_i^l + \gamma \left( \text{BN} \left( W_g^l h_i^l + \sum_{j \in N_i} \hat{e}_{i,j}^{l+1} \odot V_g^l h_j^l \right) \right) \end{aligned} \quad (4)$$

where  $\sigma$  is the sigmoid function,  $\epsilon$  is a small fixed constant for numerical stability,  $\odot$  is the Hadamard product, BN is batch normalization and  $\gamma$  is the activation function where we use Sigmoid Linear Unit (SiLU).  $A_{lg}^l, B_{lg}^l, C_{lg}^l, V_{lg}^l, W_{lg}^l$  are learnable parameters of GatedGCN applied on  $\mathcal{L}(\mathcal{G})$  and  $A_g^l, B_g^l, C_g^l, V_g^l, W_g^l$  are learnable parameters of GatedGCN applied on  $\mathcal{G}$ . We apply  $L$  such layers of aggregation and update in Graph Encoder and return the final set of node embeddings  $\mathcal{H} = \{h_1, \dots, h_{|\mathcal{V}|}\}$ , where  $h_i := h_i^L \in R^d$  represents the final embedding of node  $i$ . We subsequently use a symmetric aggregation function (AvgPool) to generate graph-level representation  $\mathcal{Z}_G \in R^{d'}$  (we set  $d'$  as 256) of the crystal material  $M$ .

$$\mathcal{Z}_G = \sum_{i=1}^{|\mathcal{V}|} h_i^L \quad (5)$$

#### 3.2.2 Text Encoder:

As a text encoder, we adopt a pre-trained MatSciBERT model, which is a domain-specific language model for materials science, followed by a projection layer. MatSciBERT is effectively a pre-trained SciBERT model on a scientific text corpus of 3.17B words, which is further trained on a huge text corpus of materials science containing around 285 M words, using domain adaptive pretraining objective proposed by Gururangan et al. [2020]. We feed textual description of material  $\mathcal{T}$  and extract embedding of [CLS] token  $\mathcal{Z}_{CLS} \in R^{768}$  as a representation of the whole text. Further, we pass  $\mathcal{Z}_{CLS}$  through a projection layer (two-layer

Property	Unit	CIFID	CGCNN	SchNet	MEGNET	GATGNN	ALIGNN	Matformer	CrysMMNet
Formation Energy	eV/atom	0.140	0.063	0.045	0.047	0.047	0.033	0.033*	<b>0.028</b>
Bandgap(OPT)	eV	0.301	0.200	0.192	0.145	0.170	0.142	0.137*	<b>0.128</b>
Bandgap(MBJ)	eV	0.532	0.413	0.433	0.344	0.513	0.310	0.302*	<b>0.278</b>
Total Energy	eV/atom	0.244	0.078	0.047	0.058	0.056	0.037	0.035*	<b>0.034</b>
Bulk Moduli(Kv)	GPa	14.12	14.47	14.33	15.11	14.32	10.40*	11.21	<b>9.625</b>
Shear Moduli(Gv)	GPa	11.98	11.75	10.67	13.09	12.48	9.481*	10.76	<b>8.471</b>

Table 1: Summary of the prediction performance (MAE) of CrysMMNet and different state-of-the-art models for different properties in JARVIS-DFT Dataset. The best performance is highlighted in bold and the second-best results are highlighted with \*.

neural network) to generate the textual embedding for the material  $\mathcal{Z}_{\mathcal{T}} \in R^d$

$$\mathcal{Z}_{\mathcal{T}} = W_2(g(W_1\mathcal{Z}_{CLS})) \quad (6)$$

We use standard non-linear function  $\text{ReLU}(\cdot)$  as  $g(\cdot)$ ,  $W_1 \in R^{768 \times 128}$  and  $W_2 \in R^{128 \times d}$  are parameter matrix that project  $\mathcal{Z}_{CLS}$  to embedding space  $R^d$ . In our experiment, we set  $d$  as 64.

### 3.2.3 Joint Embedding Model:

The graph encoder encodes local structural and chemical semantics around atoms in a unit cell of the material, whereas the text encoder captures global periodic knowledge from the textual description. Further, in the joint embedding model, we fuse both the representations ( $\mathcal{Z}_{\mathcal{G}}, \mathcal{Z}_{\mathcal{T}}$ ) together into a single multi-modal representation  $\mathcal{Z} := (\mathcal{Z}_{\mathcal{G}} \oplus \mathcal{Z}_{\mathcal{T}}) \in R^{(d'+d)}$ , which can now capture both local and global structural semantics of the material. We tried different ways to fuse both the embeddings like sum, average, concatenation ( $\oplus$ ) and found concatenation performs best.

Further, we pass this multi-modal representation  $\mathcal{Z}$  through a multi-layer perceptron which predicts the value of the properties. We train CrysMMNet end to end to optimize the following mean square error(MSE) loss :

$$\mathcal{L}_{MSE} = \|\hat{\mathcal{Y}} - \mathcal{Y}\|^2 \quad (7)$$

where  $\hat{\mathcal{Y}}$  and  $\mathcal{Y}$  are predicted and true property values respectively. Note, while training CrysMMNet we freeze the weights of MatSciBERT and don't tune it further. Fine-tuning MatSciBERT with CrysMMNet training for a specific property will add more computational overhead as it will increase the number of parameters significantly. This provides scope for further investigation and we keep it as future work.

## 4 EXPERIMENTAL RESULTS

In this section, we begin by describing the experimental setup which includes the benchmark datasets used for eval-

uation, alternate baseline approaches, and implementation details. Then we evaluate the performance of CrysMMNet in comparison with different SOTA property predictors on the downstream property prediction tasks using two popular material benchmark datasets. Next, we present the empirical evaluation results of our proposed framework in limited training data settings. Further, we conduct some ablation studies to demonstrate the expressiveness and robustness of textual representation and the importance of global and local knowledge encoded in textual embedding. Finally, we perform a qualitative analysis of the attention layer of MatSciBert to visualize attention in different tokens in the material description.

### 4.1 EXPERIMENTAL SETUP

To evaluate the effectiveness of CrysMMNet, we conduct experiments on two benchmark material datasets, Materials Project Jain et al. [2013] (MP 2018.6.1) and JARVIS-DFT Choudhary et al. [2020] (2021.8.1), which comprises some important physical properties obtained with high-throughput DFT calculations. MP 2018.6.1 consists of 69,239 materials whereas JARVIS-DFT consists of 55,722 materials. We curated textual datasets for both datasets using robocrytalographer with a textual description of each material as described in subsection 3.1. We choose seven state of the art algorithms for crystal property prediction CIFID Choudhary et al. [2018], CGCNN Xie and Grossman [2018], SchNet Schütt et al. [2017], MEGNET Chen et al. [2019], GATGNN Louis et al. [2020], ALIGNN Choudhary and DeCost [2021] and Matformer Yan et al. [2022]. To avoid any deterioration of the performance of the baseline algorithms due to insufficient hyperparameter tuning, we report the property prediction results from the respective papers of the baseline models.

We use four convolution layers of the graph encoder module and pre-trained MatSciBERT followed by a two-layer neural network (projection layer) as the text encoder module in CrysMMNet. We train it for 1000 epochs using AdamW Loshchilov and Hutter [2017] optimizer with normalized weight decay of  $10^{-5}$  and keep the batch size as 64. We schedule the learning rate according to the one-cycle policy

Property	Unit	CGCNN	SchNet	MEGNET	GATGNN	ALIGNN	Matformer	CrysMMNet
Formation Energy	eV/atom	0.031	0.033	0.030	0.033	0.022	0.021*	<b>0.020</b>
Bandgap	eV	0.292	0.345	0.307	0.280	0.218	0.211*	<b>0.197</b>
Bulk Moduli(Kv)	log(GPa)	0.047	0.066	0.060	0.045	0.051	0.043*	<b>0.038</b>
Shear Moduli(Gv)	log(GPa)	0.077	0.099	0.099	0.075	0.078	0.073*	<b>0.062</b>

Table 2: Summary of the prediction performance (MAE) of CrysMMNet and different state-of-the-art models for different properties in The Materials Project dataset. The best performance is highlighted in bold and the second-best results are highlighted with \*.

Property	Train-set Size	CGCNN	ALIGNN	CrysMMNet
Bandgap(MBJ)	3634	0.522	0.483	<b>0.456</b>
Bulk Moduli	3936	14.98	14.13	<b>13.04</b>
Shear Moduli	3936	13.07	12.61	<b>11.57</b>

Table 3: : MAE values of CGCNN, ALIGNN and CrysMMNet for three different properties in the JARVIS-DFT dataset with 20% training instances. The best performance is highlighted in bold.

Smith [2018] with a maximum learning rate of 0.001. We keep embedding dimensions of the graph and text encoder as 64 and 256 respectively. We perform the experiments in shared servers having Intel E5-2620v4 processors which contain 16 cores/thread and four GTX 1080Ti 11GB GPUs each.

## 4.2 DOWNSTREAM TASK EVALUATION

### 4.2.1 JARVIS-DFT Dataset

To evaluate CrysMMNet, we first conduct experiments on the JARVIS-DFT dataset, which is a widely used large-scale material benchmark containing 55,722 crystals. Following previous state-of-the-art works, we choose six crystal properties including formation energy, bandgap (OPT), bandgap (MBJ), total energy, bulk moduli, and shear moduli for the downstream property prediction task. We use 80%, 10%, and 10% train, validation, and test split for all the properties as used by ALIGNN. We report mean absolute error (MAE) of the predicted and actual value of a particular property for test data in table 1 to compare the performance of CrysMMNet and different participating methods. We observe that CrysMMNet outperforms every baseline model across all the properties with a significant margin. In specific, we observe 13.84%, 2.85%, 6.56%, 7.33%, 7.40%, and 10.65% improvements compared to the competing second-best baseline model for formation energy, total energy, bandgap (OPT), bandgap (MBJ), bulk moduli, and shear moduli respectively, which shows the effectiveness of multimodal representation capturing both local chemical semantics and global periodic structural knowledge towards crystal property prediction.

### 4.2.2 Materials Project (MP) Dataset

We further use another benchmark material dataset, Materials Project-2018.6.1, comprises 69,239 materials. Here we evaluate CrysMMNet with all state-of-the-art models using four crystal properties namely formation energy, bandgap, bulk moduli, and shear moduli. For formation energy and bandgap, we use 60000, 5000, and 4239 crystals as train, validation, and test split as used by ALIGNN, whereas use 4664, 393, and 393 crystals as train, validation, and test split for bulk and shear moduli as used by GATGNN. We report the mean absolute error (MAE) of the predicted and actual property value for test data in table 2 to compare the performance of CrysMMNet with different participating methods. Note, to maintain consistency with the results reported by baseline works, we report (GPa) values of bulk and shear moduli in table 1, whereas log(GPa) values in table 2. We observe that CrysMMNet outperforms every baseline model across all the properties with a significant margin. In specific, we observe 4.76%, 6.63%, 6.9%, and 15.06% improvements compared to the competing second-best baseline model for formation energy, bandgap, bulk moduli, and shear moduli respectively. Overall, the superior performances show the effectiveness of multi-modal representation in CrysMMNet.

### 4.2.3 Results on Limited Training Data

CrysMMNet performs well in limited data settings as well. With 4664 training samples only CrysMMNet achieves 6.9% and 15.06% improvements for bulk moduli and shear moduli respectively in the Materials Project dataset. Further, in JARVIS-DFT Dataset, we conduct an additional set of experiments for three different properties including bandgap (MBJ), bulk moduli, and shear moduli, where we have limited labeled data. More specifically, we take 20-10-10% training-validation-test data split and evaluate the performance of CGCNN, ALIGNN, and CrysMMNet in the table 3. We observe, CrysMMNet achieves improvement for all three properties compared to CGCNN and ALIGNN. Overall, these superior performances indicate the robustness of our model and its adaptive ability to tasks of various data scales.



Property	CrysTextNet	CGCNN	ALIGNN
Formation Energy	0.447	0.063	0.033
Total Energy	0.352	0.078	0.037
Bandgap(OPT)	0.595	0.201	0.142
Bandgap(MBJ)	0.849	0.411	0.311
Bulk Moduli(Kv)	21.98	14.47	10.42
Shear Moduli(Gv)	14.76	11.75	9.483

Table 4: Summary of experiments for the ablation study on the effectiveness of Textual Representation.

### 4.3 ABLATION STUDY

In this subsection, We demonstrate the robustness of multimodal representation on different GNN architecture choices and the influence of textual modality on CrysMMNet performance, by designing the following set of ablation studies:

1. Is only textual information sufficient to infer better property prediction accuracy?
2. How robust is the multimodal representation on different GNN architecture choices for graph encoder?
3. What are the influences of global structural and local compositional knowledge from the textual datasets on property prediction performance?

In the following subsections, we will thoroughly discuss these.

#### 4.3.1 Expressiveness of Textual Representation

First, we are interested to understand whether textual representations are alone expressive enough, to encode atomic chemical and periodic structural semantics from the curated textual data and predict different properties precisely. We conduct an ablation experiment, where we consider only the text embeddings  $\mathcal{Z}_{\mathcal{T}}$  of CrysMMNet (output of projection layer) and pass it alone through a multi-layer perceptron to predict the property value. We denote this model as CrysTextNet and compare it with state-of-the-art graph-based models on different properties of the JARVIS-DFT dataset. We report the MAE for test data in table 4. We observe, for all the properties, test MAE is higher for the CrysTextNet model compared to state-of-the-art graph-based models like CGCNN and ALIGNN. In specific, for mechanical properties like bulk modulus and shear modulus, CrysTextNet works better (closer test MAE with competing GNN baselines) than properties like formation energy, band-gap, and total energy. This is because properties, such as formation energy, band gap, and total energy rely on microscopic chemical information which textual representation fails to encode. Instead, graph encodings include node features  $\mathbf{x}_u$  ( $u \in \mathcal{V}$ ) that are high-dimensional vectors with meaningful chemi-

cal quantities like electronegativity, group number, covalent radius, number of valence electrons, first ionization energy, etc. Furthermore, through message passing and aggregation in the graph convolution layer, GNN models capture many-body interactions among atoms in the material. On the other side, mechanical properties like bulk modulus and shear modulus are more dependent on structural information like lattice structure and symmetry of the material, which textual representations are able to capture.

Overall, though textual representations can capture many useful local and global information about the materials, unlike graph structural models, they are not alone expressive enough to capture atomic chemical features and the structural connectivity between different atoms in the materials. Message passing and neighborhood aggregation between atoms through the GNN model are still very fundamental in learning the structure-property relationship of the materials.

#### 4.3.2 Robustness of Textual Representation

Further, we investigate the robustness of textual representations on different crystal GNN encoders. We conduct an ablation study where we replace graph encode of CrysMMNet with popular crystal GNN variants, e.g, CGCNN, MEGNET, GATGNN and evaluate the performance. We set up the experiments with six properties of the JARVIS dataset and report the MAE values in table 5 for the baseline GNN models and different variants of CrysMMNet with different GNN architectural choices as graph encoder. We observe all these variants outperform corresponding vanilla GNN models with a good margin for all the properties, which shows textual representations are rich enough to encode global structural knowledge which aids the property prediction accuracy of any state-of-the-art GNN models.

#### 4.3.3 Importance of Local and Global Knowledge

Finally, we are curious to understand the importance of local (atom/bond) compositional information and global material structural knowledge encoded through textual representation in CrysMMNet. Specifically, we conduct an ablation study, where we train CrysMMNet in two additional setups along with the conventional (Global+Local) setup for CrysMMNet. (a) Only Global: In this scenario, we take only global knowledge about the periodic structure of the materials as textual data to train CrysMMNet. (b) Only Local: In this scenario, we take only local compositional information about atoms and inter-atomic bonds as textual data to train CrysMMNet. We use six properties of JARVIS-DFT dataset for the experiment and report MAE in Table 6. We observe performance gain across all the properties using both global and local information combined as textual knowledge, compared to only global or local knowledge separately.



Property	CGCNN	CrysMMNet (CGCNN)	MEGNET	CrysMMNet (MEGNET)	GATGNN	CrysMMNet (GATGNN)
Formation Energy	0.063	0.046	0.076	0.060	0.077	0.064
Bandgap(OPT)	0.200	0.163	0.184	0.165	0.169	0.157
Bandgap(MBJ)	0.413	0.339	0.369	0.339	0.343	0.331
Total Energy	0.078	0.059	0.058	0.057	0.056	0.053
Bulk Moduli(Kv)	14.47	12.98	15.11	13.29	14.32	13.73
Shear Moduli(Gv)	11.75	10.71	13.09	11.86	12.48	12.04

Table 5: Summary of the prediction performance (MAE) of different state-of-the-art GNN models with textual representation for six different properties in The JARVIS-DFT Dataset. Model M is the SOTA baseline model and CrysMMNet(M) is a variant where we replace graph encoder with M.

Property	Global+Local	Only Global	Only Local
Formation Energy	<b>0.028</b>	0.039	0.039
Total Energy	<b>0.034</b>	0.042	0.046
Bandgap(OPT)	<b>0.114</b>	0.191	0.147
Bandgap(MBJ)	<b>0.209</b>	0.216	0.218
Bulk Moduli(Kv)	<b>6.860</b>	6.910	6.870
Shear Moduli(Gv)	<b>6.440</b>	6.730	6.880

Table 6: Summary of experiments for the ablation study on the importance of Local and Global Material Knowledge.

#### 4.4 QUALITATIVE ANALYSIS OF ATTENTION LAYERS

Finally, to visualize and understand attentions in different tokens in the material description, we perform a qualitative analysis of the attention layer in MatSciBert. We utilized the standard BertViz tool [Vig \[2019\]<sup>2</sup>](https://github.com/jessevig/bertviz) to analyze and visualize the attention scores in the MatSciBert Model. We present a case study of the textual data of  $FeH_8(ClO_2)_2$  in **Figure 3 & 4 in Section A of Appendix**, where we have examined the attention score of the [CLS] token at the 5th layer of MatSciBert.

We observe MatSciBert allocates higher attention scores to tokens that defines global features of the crystal, such as ‘Formula’, ‘Mineral’, ‘Crystal System’, ‘Space Group Number’, and ‘Dimensionality’. Further, we investigate attention weights for local information corresponding to Fe, H, and O atoms. MatSciBert provides more attention score to tokens related to *bond types (octahedral geometry, equivalent bond, distorted water-like geometry, etc)* and *bond lengths (2.08 Å, 2.10 Å, and 2.53 Å bond length)*. It is evident from these observations that MatSciBert is attending the important tokens related to global and local material information, to generate more expressive multimodal representation.

<sup>2</sup><https://github.com/jessevig/bertviz>

## 5 CONCLUSIONS

In this work, we address the limitation of state-of-the-art GNN models for crystal property prediction to capture global periodic structural information and leverage textual modalities beside graph structures to resolve the issue. To this end, we curate textual datasets of two popular benchmark databases containing textual descriptions of each material containing both local compositional and global structural information of a material. Further, we propose a simple yet effective multi-modal framework, CrysMMNet, for crystalline materials, which fuse both graph structural and textual representation together to generate a more enriched and robust multimodal representation for materials, which subsequently improves property prediction accuracy. Extensive experiments show CrysMMNet outperforms all the popular state-of-the-art baselines across ten diverse sets of properties on two popular datasets. Further, we conduct ablation studies to demonstrate the expressiveness and robustness of textual representation on different crystal GNN encoders and show performance gain across all the properties using both global and local information combined as textual knowledge, compared to only global or local knowledge separately. Finally, we visualize attention weights between [CLS] token and other tokens in the material’s description to understand the important tokens. that the text encoder is attending to generate more expressive multimodal representation

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