Is ChatGPT Transforming Academics' Writing Style?

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Abstract

Based on one million arXiv papers submitted from May 2018 to January 2024, we assess the textual density of ChatGPT's writing style in their abstracts by means of a statistical analysis of word frequency changes. Our model is calibrated and validated on a mixture of real abstracts and ChatGPT-modified abstracts (simulated data) after a careful noise analysis. We find that ChatGPT is having an increasing impact on arXiv abstracts, especially in the field of computer science, where the fraction of ChatGPT style abstracts is estimated to be approximately 35%, if we take the output of one of the simplest prompts, "revise the following sentences", as a baseline. We conclude with an analysis of both positive and negative aspects of the penetration of ChatGPT into academics' writing style.

1. Introduction

Since its official release on November 30, 2022, ChatGPT has impacted many aspects of our lives, and academic writing has not been immune. While ChatGPT does increase productivity and may help scientific discovery (Noy & Zhang, 2023; AI4Science & Quantum, 2023), we must be wary of its potential risks and the possibility of negative impacts. A large number of papers have already explored the advantages and disadvantages of large language models (LLMs) (Kasneci et al., 2023). We focus on the impact of LLMs, especially ChatGPT, on academic writing, which should also be a non-negligible part of AI security.

While there is already a corpus of current research on using ChatGPT in academia (Casal & Kessler, 2023; Lingard et al., 2023; Fergus et al., 2023; Lund et al., 2023), to our knowledge only a handful of works have attempted to quantify its impact on the whole academic community. As this article was being finalized, two preprints appeared that addressed related questions: one focuses on AI conferences peer reviews (Liang et al., 2024a) and, even more recently, analyzes scientific papers(Liang et al., 2024b).

ChatGPT is of course able to generate abstracts directly given a suitable prompt (Luo et al., 2023), and studies have shown that identifying such abstracts is not easy even if they remain unedited by humans (Gao et al., 2023; Cheng et al., 2023) – watermarking being a possible strategy to enable such identification (Kirchenbauer et al., 2023). Determining whether a given few sentences were generated by ChatGPT is difficult, but determining that millions of sentences were influenced by ChatGPT is statistically feasible, as we demonstrate here.

In fact, that the abstract of a paper shows what we call the "ChatGPT style" does not necessarily mean that the authors directly utilized ChatGPT to generate or modify it. It is also possible that the authors used ChatGPT in another context and that, as a result, their writing habits were influenced by the ChatGPT style – not a remote possibility. It is worth considering in this context that reading and writing in English is more difficult for non-native English academics (Amano et al., 2023). Before ChatGPT was released, the pros and cons of other tools were discussed, such as Google Translate (Mundt & Groves, 2016) and Grammarly (Fitria, 2021).

We have seen similar AI-induced seismic shifts in the past: after AlphaGo (Silver et al., 2017) shocked the world, professional Go players have begun training with AI, and the sport of Go has been profoundly changed as a result (Kang et al., 2022). AlphaFold brings new opportunities for life science research (Varadi & Velankar, 2023) and ChatGPT has also been used for data extraction in materials science. (Polak & Morgan, 2023). A similar story may be happening with academic writing, especially for researchers whose first language is not English (Hwang et al., 2023).

2. Data

arXiv dataset: The metadata of arXiv papers are provided by Kaggle (arXiv.org submitters, 2024). Because the abstracts in this dataset are updated when authors submit changes, we used the first version in 2024 (version 161) as well as the last version before the ChatGPT era (version

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105). Our observations and analysis are based on one million arXiv articles submitted from May 2018 to January 2024.

English word frequency: Google Ngram dataset is chosen for comparison and reference (Michel et al., 2011). Specifically, we used the freely available mirrors on Kaggle (http: //kaggle.com/datasets/wheelercode/ english-word-frequency-list) covering word frequencies from the 1800s to 2019 as established from Google Books.

3. Observations and analysis

3.1. Changes in word frequency

We approach the problem by analyzing how the frequency of words changes after ChatGPT has been deployed, as presented in Figure 1. How could the frequencies of words like "**significant**" grow **significantly** together in 2023?



Figure 1. Examples of words with rapidly growing frequency.

Another striking example is the frequency change of the words "are" and "is", as depicted in Figure 2. The counts in 10,000 abstracts of these two words were quite stable before 2023. However, the frequency of these two terms has dropped by more than 10% in 2023.

These examples, anecdotal as they are, may represent the tip of the iceberg of a wider and growing phenomenon: the rapid increase in the usage of ChatGPT.

We wanted to be more specific about the impact of ChatGPT on articles from different disciplines, so we examined arXiv abstracts from different categories separately. The one million arXiv articles were divided into 20 periods later, which is not the same as the this part. The identifier numbers of the first and last arXiv articles corresponding to each period



Figure 2. The words "are" and "is" are decreasing in frequency.

are given in the appendix.

3.2. ChatGPT simulations

Previous studies have shown that ChatGPT has its own linguistic style (AlAfnan & MohdZuki, 2023), and that likely includes the frequency of some words. Although there is no direct way to investigate ChatGPT's word preference, we can ask ChatGPT to polish or rewrite real, pre-2023 abstracts, and use the resulting simulation data to calculate the estimated frequency change rate \hat{r}_{ij} of word *i* in category *j*:

$$\hat{r}_{ij} = \frac{\tilde{q}_{ij}^d - q_{ij}^d}{q_{ij}^d} = \frac{\tilde{q}_{ij}^d}{q_{ij}^d} - 1$$
(1)

where q_{ij}^d represents the word frequency of real abstracts in the dataset and \tilde{q}_{ij}^d means the frequency after ChatGPT processing. We have no way of knowing the real usage scenarios of ChatGPT, so some simple prompts were used, for example,

"Revise the following sentences:"

GPT-3.5 was utilized in our simulations for 10,000 abstracts in period 14 (April 2022 to July 2022), although it may have different word preferences than the more recent GPT-4. Many words have different frequencies before and after ChatGPT processing, such as the words "is", "are", and "significant" that we mentioned earlier. For simplicity, the results of the 4 categories with the highest number of articles are shown in Table 1 and the rest parts in this paper namely *cs* (computer science), *math* (mathematics), *astro* (astrophysics), and *cond-mat* (condensed matter).

This corroborates the hypothesis, formulated earlier, that

word	category	before	after	change
is	cs	2.01	1.73	-14%
is	math	1.78	1.61	-9%
is	astro	2.13	1.90	-11%
is	cond-mat	2.00	1.68	-16%
are	cs	1.00	0.83	-17%
are	math	0.74	0.71	-5%
are	astro	1.39	1.25	-1%
are	cond-mat	0.92	0.80	-13%
significant	cs	0.09	0.18	99%
significant	math	0.01	0.03	308%
significant	astro	0.17	0.26	53%
significant	cond-mat	0.07	0.18	171%

Table 1. Word frequency (per abstract) before and after ChatGPT processing in simulation data of period 14.

the drop in the frequency of these two words observed in real abstracts in 2023 may have been caused by ChatGPT.

In the meantime, we also defined the word frequency change in all abstracts from year t - 1 to year t, $R_{ij,t}$:

$$R_{ij,t} = \frac{F_{ij,t} - F_{ij,t-1}}{F_{ij,t-1}},$$
(2)

where $F_{ij,t}$ represent frequency of word *i* per arXiv abstract in category *j* in year *t*.

Only words with a frequency larger than 0.1 times per abstract before ChatGPT processing are plotted in Figure 3 and Figure 4. The correlation coefficient between the word frequency change in arXiv abstracts and our estimated ChatGPT-induced word frequency change is very small in all four categories of abstracts, as shown in Figure 3.

However, Figure 4 presents a totally different pattern, where \hat{r}_{ij} and $R_{ij,2023}$ are strongly correlated, especially in computer science abstracts. Although many words seem insensitive to ChatGPT, we can still see a positive correlation for some words in this figure, even among the other categories.

Taken together, our consideration point to ChatGPT as one of the important reasons, possibly even the main reason, for the recent word frequency change in abstracts. Our next step is to start by modeling ChatGPT impact, as well as estimating the impact based on real data and simulations.

4. Models and methods

4.1. ChatGPT impact

As is well known, different prompts will lead to different outputs, which means different word frequency changes. Therefore, we use the more neutral term "ChatGPT impact" instead of "proportion" in our estimation part.

We start with a simple model, ignoring noise and variability



Figure 3. Comparison of the predicted frequency change rate due to ChatGPT \hat{r}_{ij} (x-axis) and the actual word frequency change for all abstracts from 2021 to 2022 $R_{ij,2022}$ (y-axis). CC indicates the correlation coefficient.



Figure 4. Comparison of the predicted frequency change rate due to ChatGPT \hat{r}_{ij} (x-axis) and the actual word frequency change for all abstracts from 2022 to 2023 $R_{ij,2023}$ (y-axis). The correlation coefficients (CC) are now significantly positive.

for this subsection. Suppose that the frequency of word i for abstracts in subject category j changes from f_{ij}^* to \tilde{f}_{ij}^* after being processed by ChatGPT. The corresponding word change rate is defined as

$$\bar{r}_{ij} = \frac{\tilde{f}_{ij}^* - f_{ij}^*}{f_{ij}^*} = \frac{\tilde{f}_{ij}^*}{f_{ij}^*} - 1.$$
(3)

Suppose that $\bar{f}_{ij}(t)$ is the word frequency for word *i* in

category j at time period t, this can be written as:

$$f_{ij}(t) = (1 - \eta_j(t))f_{ij}^*(t) + \eta_j(t)f_{ij}^*(t)(\bar{r}_{ij} + 1) = f_{ij}^*(t) + \eta_j(t)f_{ij}^*(t)\bar{r}_{ij}$$
(4)

where $\eta_j(t)$ denotes the proportion of abstracts in category j affected by ChatGPT, and $f_{ij}^*(t)$ represents the original evolution in word frequency without ChatGPT.

4.2. Noise model

We now consider the noise terms, which might be modelled in many different ways. For example, we denote the word frequency for word *i* in category *j* by f_{ij}^d , which represents the word frequency observed in the data:

$$f_{ij}^{d} = f_{ij}^{*} + \delta_{ij}(f_{ij}^{*}) \tag{5}$$

where $\delta_{ij}(\cdot)$ represents noise and word usage variability which are not directly related to the internal parameters of ChatGPT.

Thus, we can define

$$f_{ij}^{\delta,\eta}(t) = \eta_j(t) f_{ij}^*(t) + \delta_{ij}(\eta_j(t) f_{ij}^*(t))$$

$$f_{ij}^{\delta,1-\eta}(t) = (1 - \eta_j(t)) f_{ij}^*(t)$$

$$+ \delta_{ij}((1 - \eta_j(t)) f_{ij}^*(t)).$$
(6)

In this case, the equation corresponding to Eq. (4) is

$$f_{ij}^{d}(t) = f_{ij}^{\delta, 1-\eta}(t) + C_{ij}(f_{ij}^{\delta, \eta}(t))$$
(7)

where the function $C_{ij}(\cdot)$ means the frequency after Chat-GPT process.

We assume that the noise for word *i* due to ChatGPT processing can be represented as $\epsilon_{ij}(\cdot)$ and $\epsilon_{ij}^{s}(\cdot)$, then Eq. (1) and Eq. (3) are related by

$$\frac{\tilde{f}_{ij}^* - \epsilon_{ij}(f_{ij}^*) - f_{ij}^*}{f_{ij}^*} = \frac{\tilde{q}_{ij}^d - \epsilon_{ij}^s(q_{ij}^d) - q_{ij}^d}{q_{ij}^d} \,. \tag{8}$$

Therefore,

$$C_{ij}(f_{ij}^{\delta,\eta}(t)) = f_{ij}^{\delta,\eta}(t)(\hat{r}_{ij} + 1 + \epsilon_{ij}^{\eta}(q, f, t))$$
(9)

where

$$\epsilon_{ij}^{\eta}(q,f,t) = \frac{\epsilon_{ij}(f_{ij}^{\epsilon,\eta}(t))}{f_{ij}^{\delta,\eta}(t)} - \frac{\epsilon_{ij}^s(q_{ij}^d)}{q_{ij}^d}.$$
 (10)

Then, Eq. (7) – representing the difference in word frequency before and after ChatGPT processing – can be rewritten as

$$f_{ij}^d(t) - f_{ij}^*(t) = \eta_j(t)x_{ij}(t) + g_{ij}(t) + \xi_{ij}(t)$$
(11)

where

$$x_{ij}(t) = f_{ij}^*(t)\hat{r}_{ij}$$
 (12)

$$g_{ij}(t) = \eta_j(t) f_{ij}^*(t) \epsilon_{ij}^\eta(q, f, t)$$
(13)
$$f_{ij}(t) = (\hat{r}_{ij}(t) - (\hat{r}_{ij}(t) - (f, t)) \delta_{ij}(r_{ij}(t) -$$

$$\xi_{ij}(t) = (\hat{r}_{ij} + 1 + \epsilon_{ij}'(q, f, t))\delta_{ij}(\eta_j(t)f_{ij}^*(t)) + \delta_{ij}'((1 - \eta_j(t))f_{ij}^*(t)).$$
(14)

where $\delta'_{ij}(\cdot)$ follows the same distribution as $\delta_{ij}(\cdot)$. It should be noted that $g_{ij}(t)$ includes only ChatGPT-related noise $\epsilon_{ij}(\cdot)$ and $\epsilon^s_{ij}(\cdot)$, however $\xi_{ij}(t)$ contains $\delta_{ij}(\cdot)$ and $\delta'_{ij}(\cdot)$ that are unrelated to ChatGPT.

4.3. Impact estimation and bias analysis

In many data analysis applications, more data point (in our case, using a larger number of words) means better estimates. But in our case, the effect of noise is different for each data point (word), and choosing wisely which words to include can improve our estimates.

For simplicity, we define

$$h_{ij}(t) = f_{ij}^d(t) - f_{ij}^*(t).$$
(15)

For abstracts in category j, we use the words in the subset I_j (whose determination is discussed below), of numerosity n_j . In order to estimate $\eta_j(t)$, we can use the quadratic loss function

$$L_{j,t}(\eta_j) = \frac{1}{n_j} \sum_{i \in I_j} (h_{ij}(t) - \eta_j(t) x_{ij}(t))^2$$

= $\frac{1}{n_j} \sum_{i \in I_j} (g_{ij}(t) + \xi_{ij}(t))^2.$ (16)

If we ignored the dependency of $g_{ij}(t)$ and $\xi_{ij}(t)$ on $\eta_j(t)$, the estimate of ChatGPT impact would simply be given by Ordinary Least Squares (OLS) as

$$\hat{\eta}_j(t) = \frac{\sum_{i \in I_j} h_{ij}(t) x_{ij}(t)}{\sum_{i \in I_j} x_{ij}^2(t)} \,. \tag{17}$$

However, since $g_{ij}(t)$ also depends on $\eta_j(t)$ and ξ_{ij} contains $\eta_j(t)$ as described in Eq. (13) and Eq. (14), we need to make additional assumptions to progress further.

Case 1: if the effect of $\eta_j(t)$ on $\xi_{ij}(t)$ can be ignored compared to other terms, e.g., the following simple scenario,

$$\operatorname{Var}[\delta_{ij}(\eta_j(t)f_{ij}^*(t))] \ll \eta_j(t)f_{ij}^*(t)\operatorname{Var}[\epsilon_{ij}^{\eta}(q, f, t)]$$
(18)

One can also derive the approximation below:

$$f_{ij}^{\delta,\eta}(t) \approx \eta_j(t) f_{ij}^*(t) + \delta_{ij}(*)$$
(19)

where $\delta_{ij}(*)$ is a random variable with zero mean and variance much smaller than $\eta_j(t)f_{ij}^*(t)$, and its derivative with respect to $\eta_j(t)$ is negligible compared to $f_{ij}^*(t)$.

Therefore, the loss function under this assumption is:

$$L_{j,t,g}(\eta_j) = \frac{1}{n_j} \sum_{i \in I_j} (h_{ij}(t) - \eta_j(t) x_{ij}(t) - g_{ij}(t))^2$$

$$= \frac{1}{n_j} \sum_{i \in I_j} \xi_{ij}^2(t) .$$
(20)

If we require a minimum by setting $\frac{\partial L_{j,t,g}(\eta_j)}{\partial \eta_j} = 0$, we obtain a new estimate $\hat{\eta}_j^g(t)$. After the assumptions and calculations listed in the appendix, the bias part is expressed as

$$\hat{\eta}_j(t) - \hat{\eta}_j^g(t) = \frac{\sum_{i \in I_j} \mathbb{E} \left[g_{ij}(t) \frac{\partial g_{ij}(t)}{\partial \eta_j(t)} \right]}{\sum_{i \in I_j} (f_{ij}^*(t) \hat{r}_{ij})^2} \,. \tag{21}$$

Some insights can be gained from the results above. For example, considering that the value of $\eta_j(t)$ affects the bias as well, which is not simply linear, we are led to consider adaptive or iterative criteria for word choice, which will in general depend on the true (and unknown) value of $\eta_j(t)$.

Case 2: Gaussian distribution for $\delta_{ij}(f_{ij})$, e.g., $\delta_{ij}(f_{ij}) \sim \mathcal{N}(0, f_{ij}\sigma_{ij}^2)$, which is justified empirically in the appendix, Figure 14 and Figure 16. As a result,

$$\xi_{ij}(t) = (\hat{r}_{ij} + \epsilon_{ij}^{\eta}(q, f, t))\delta_{ij}(\eta_j(t)f_{ij}^*(t)) + \delta_{ij}'(f_{ij}^*(t))$$
(22)

which gives us similar conclusions with more details in the appendix.

Finding criteria for selecting the words that are included in the frequency change analysis greatly reduces the computational complexity compared to trying different word combinations.

4.4. Calibration and test

We construct N different sets of abstract data for calibration, D_n , with its correspond mixed ratio of ChatGPT-processed abstracts, η_n , as

$$(D_n, \eta_n), n \in \{1, 2, \dots, N\}$$
 (23)

and similarly for test data $T_{n'}$ and $\eta'_{n'}$,

$$(T'_n, \eta'_n), n' \in \{1, 2, \dots, N'\}.$$
 (24)

And for one pair of (D_n, η_n) and a specific word choice requirement q_k (for example, $q_{ij}^d > 0.1$ and $\frac{\hat{r}_{ij}+1}{\hat{r}_{ij}^2} < \frac{0.1+1}{0.1^2}$), the efficiency can be defined as

$$e(D_n, \eta_n, q_k) = |\eta_n - \hat{\eta}_n(D_n, q_k)|$$
(25)

where $\hat{\eta}_n(D_n, q_k)$ is the estimate of η_n using Eq. (17) and the words set I_i can be derived from q_k , denoted $I_i(q_k)$

For a given set of q_k (examples can be found in the appendix), we are looking for the best one minimizing $e(D_n, \eta_n, q_k)$, denoted $q(D_n, \eta_n)$, which is the calibration part. For the test data $T_{n'}$, the estimate of $\eta_{n'}$ is calculated from Eq. (17) with different I_j , based on different $q(D_n, \eta_n)$ obtained in the calibration procedure.

Because of the goal of the calibration, word choice may well actually introduce a new bias to neutralize the original bias, so that the estimate is not necessarily higher in the test results than the ground truth.

5. Results

5.1. Calibration and test results

To calibrate the choice of set I_j , we use different mixing ratios, in proportion to the value of $\eta_j(t)$. In addition, we only consider the 10,000 words with the highest frequency in the Google Ngram dataset.

We used the first 10 periods to estimate $f_{ij}^*(t)$ (as they weren't influenced by ChatGPT), 20,000 abstracts in period 13 to estimate r_{ij} , 10,000 abstracts in period 12 for calibration, and 10,000 abstracts in period 14 for testing.

We take $\{\eta_n\} = \{0, 0.05, 1, \dots, 0.45, 0.5\}$ and m = 1, which means $N = \#\{(D_n, \eta_n)\} = 11$. Then the 11 I_j (with possible repetitions), obtained from mixed data with 11 corresponding η_n of period 12, were used for η'_n estimation in the test data (period 14). Other parameters can be found in the appendix.

The results using the same prompt for generating calibration and test data are shown in Figure 5, with injected mixed ratio (i.e., ChatGPT impact) η'_n from 0 to 0.5. It is clear that when the calibration and test sets are mixed in the same ratio, word combinations that achieve better estimates on the calibration set generally work better on the test set, as well.

Because one may use a wide variety of prompts in practical applications, we also evaluated the robustness of our approach by adopting a different prompt for generating the test data than the one we used for calibration, shown in the appendix.

5.2. Estimation from real data

The estimates of ChatGPT impact on the real data are shown in Figure 6 and Figure 19 (in the appendix). Based on our calibration results, we chose 11 words set I_j for different injected values of η_n . According to the results of the first estimation about $\eta_j(t)$, we found the three values of η_n that were closest to the mean of the first estimation and used



Figure 5. Test results for simulated admixtures of abstracts in period 14. The error bars represent the standard deviation of the estimation results, and the red star is the estimated value of η'_n from test data based on optimal I_j with the same mixed ratio η_n as in the calibration data. The orange dashed lines correspond to perfect estimation.

their optimal word set I_j in the calibration procedure for a second estimation, leading to the triangle points shown in the figures.

Our estimate indicates that the density of ChatGPT style texts of the most recent time period in this category is around 35%, when we use the results of one simple prompt, "revise the following sentences", as a baseline. By contrast, we detected a much smaller uptick in ChatGPT impact in *math*, while *astro* and *cond-mat* both reach values between 10% and 20%, approximately.

It is important to note that our ChatGPT impact here is a relative value that corresponds to the change in word frequency from the use of simple prompts. More precise prompts, both in reality and in simulation, could potentially lead to an impact value greater than 1.

6. Conclusions

Is ChatGPT transforming academics' writing style? An important question before these discussions is the evaluation of the actual penetration of the usage of ChatGPT in academic writing – without a quantitative estimate, the debate is founded on anecdotal evidence.

We have demonstrated here that we can monitor the impact of ChaGPT on academic writing by using simple and transparent statistical methods (e.g., word frequencies) rather than black-box GPT detectors. Our proposed strategy will



Figure 6. Estimates of $\eta_j(t)$ (i.e., ChatGPT impact) from real data. Word frequencies were normalized on the number of abstracts in each period before the estimation was performed. The error bars represent the standard deviation of the estimation results, using 11 different word sets I_j obtained in the calibration procedure with 11 different η_n . The points of the triangle represent the average of the 3 estimates, corresponding to the 3 word selection requirements qbased on the 3 η_n closest to the mean of the previous 11 estimates.

help us to develop better safeguards for tomorrow's AI systems.

7. Discussion

The debate around the usage of generative models such as ChatGPT in academic writing is multi-faceted. However, the tools such as ChatGPT also have positive impacts: they help non-English native writers to improve the quality and flow of their text, as well as to translate into English from their mother tongue or vice versa. In this sense, generative AI is a great leveller, and as such it is a welcome addition to the academic's toolbox.

What we need to be wary of is its use in fully generative mode, without expert human supervision. We should be prepared to face the sensitive applications and dangerous capabilities of AI in academic writing.

As our results have shown, ChatGPT is having an increasing impact on academic publications. With the increasing influx of young researchers, especially non-native English speakers, tools based on large language models, represented by ChatGPT, are transforming academic writing, at least for some disciplines. Even if you refuse to use them, you are likely to be influenced indirectly.

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A. Bonus!

ChatGPT 3.5 ~

O You

Revise the following sentences: "Based on one million arXiv papers submitted from May 2018 to January 2024, we assess the textual density of ChatGPT's writing style in their abstracts by means of a statistical analysis of word frequency changes. Our model is calibrated and validated on a mixture of real abstracts and ChatGPTmodified abstracts (simulated data) after a careful noise analysis. We find that ChatGPT is having an increasing impact on arXiv abstracts, especially in the field of computer science, where the fraction of ChatGPT-revise abstracts is estimated to be approximately 35%, if we take the output of one of the simplest prompts, "revise the following sentences", as a baseline. We conclude with an analysis of both positive and negative aspects of the penetration of ChatGPT into academics' writing style."

🌀 ChatGPT

"Utilizing a dataset of one million arXiv papers spanning from May 2018 to January 2024, we conduct a comprehensive examination of ChatGPT's textual density within abstracts through statistical analysis of word frequency shifts. Our approach involves calibrating and validating our model on a combination of authentic abstracts and ChatGPT-altered abstracts (synthetic data), following meticulous noise analysis. Our findings indicate a growing influence of ChatGPT on arXiv abstracts, particularly pronounced in the realm of computer science, where an estimated 35% of abstracts are believed to have been revised by ChatGPT, using the output of a basic prompt such as 'revise the following sentences' as a benchmark. We conclude with a nuanced evaluation of the merits and drawbacks associated with ChatGPT's integration into the writing styles of academic professionals."

Figure 7. Revise the following sentences:

B. Period divisions

Table 2. First and last arXiv paper identifier of 20 periods.

period	first paper	last paper	
1	1805.08929	1810.00786	
2	1810.00787	1902.00889	
3	1902.00890	1905.13537	
4	1905.13538	1909.11935	
5	1909.11936	2001.06560	
6	2001.06561	2005.02178	
7	2005.02179	2008.04251	
8	2008.04252	2011.09225	
9	2011.09226	2103.01828	
10	2103.01829	2106.04209	
11	2106.04210	2109.09152	
12	2109.09153	2112.12197	
13	2112.12198	2204.01835	
14	2204.01836	2207.06075	
15	2207.06076	2210.10618	
16	2210.10619	2301.10909	
17	2301.10910	2304.13927	
18	2304.13928	2307.10978	
19	2307.10979	2310.09716	
20	2310.09717	2401.02417	

ChatGPT 3.5 ~

C You

Please rewrite the following paragraph from an academic paper: "Based on one million arXiv papers submitted from May 2018 to January 2024, we assess the textual density of ChatGPTs writing style in their abstracts by means of a statistical analysis of word frequency changes. Our model is calibrated and validated on a mixture of real abstracts and ChatGPT-modified abstracts (simulated data) after a careful noise analysis. We find that ChatGPT is having an increasing impact on arXiv abstracts, especially in the field of computer science, where the fraction of ChatGPT-revised abstracts is estimated to be approximately 35%, if we take the output of one of the simplest prompts, "revise the following sentences", as a baseline. We conclude with an analysis of both positive and negative aspects of the penetration of ChatGPT into academics' writing style."

ChatGPT

Utilizing a dataset comprising one million arXiv papers submitted between May 2018 and January 2024, we conduct an examination of ChatGPT's textual density as reflected in abstracts through a statistical scrutiny of shifts in word frequency. Our approach involves the calibration and validation of a model on a composite of authentic abstracts and ChatGPT-attered abstracts (generated data) following a meticulous analysis of noise. Our findings indicate a burgeoning influence of ChatGPT on arXiv abstracts, particularly noticeable within the domain of computer science, where approximately 35% of abstracts are estimated to have undergone ChatGPT-mediated revisions, using the output from a straightforward prompt such as "revise the following sentences" as a benchmark. We culminate our analysis with a nuanced examination of both the favorable and unfavorable ramifications stemming from ChatGPTs integration into the writing style of academic professionals.

Figure 8. Please rewrite the following paragraph from an academic paper:

C. arXiv categories

Formally, arXiv has 8 categories in total: physics, mathematics, computer science, quantitative biology, quantitative finance, statistics, electrical engineering and systems science, economics. The first 3 categories contribute the vast majority of arXiv articles, around 91% among the 1 million articles. Hence, we divided the physics papers into sub-categories: astrophysics, condensed matter, high energy physics, etc. The four categories (computer science, mathematics, astrophysics, condensed matter) we selected account for 70% of the total number of articles. To avoid repetition, we also only count the first category of the article for those that have multiple categories (cross-postings).

D. Other observations

We define the change factor in the frequency of word i, R_i , as follows:

$$R_{i} = \frac{\max_{t}(f_{i}(t)) - \min_{t}(f_{i}(t))}{\max_{t}(f_{i}(t))}$$
(26)

where $f_i(t)$ is the count of word *i* during the time period *t*. We divided the 1 million abstracts into 100 uneven timeperiods, each encompassing 10,000 abstracts.

Figure 9 illustrates that most of the words with the largest change rate in the time period considered (generally, an increase) in the abstracts are related to hot research topics



Figure 9. The 12 words with the highest change rate R_i and satisfying $\max_t(f_i(t)) > 500$. The vertical red dashed line demarcates the first time period after ChatGPT's release.

of the last few years, such as "Covid-19", "LLMs", "AI".

We also define a change factor in the frequency of word i, R_i' , as follows:

$$R_{i}' = \frac{\max_{t}(f_{i}'(t)) - \min_{t}(f_{i}'(t))}{\max_{t}(f_{i}'(t))}$$
(27)

where $f_i'(t)$ is the count of word *i* in period *t*, normalized to the same value of $\sum_i f_i(t)$ for all periods *t*.

The total number of words in all abstracts of the first period is used as a base to normalize the frequency of words in the other periods, and the corresponding results are shown in Figure 10, Figure 11, and Figure 12.

E. Parameters

E.1. ChatGPT simulations

- model: gpt-3.5-turbo-1106
- temperature: 0.7
- seed: 1106
- top_p: 0.2

E.2. Calibration

- $\frac{1}{q_{ij}^a}$: 10, 20, 30, 40, 50, 60, 70, 80, 100, 150, 200, 500
- \hat{r}_{ij} : 0.1, 0.15, 0.2, 0,3, 0.4, 0.5, 0.6, 0.7, 0.8 (corresponding value of $\frac{\hat{r}_{ij}+1}{\hat{r}_{ij}^2}$)



Figure 10. The 12 words with the highest change rate R_i' and satisfying $\max_t(f_i'(t)) > 500$.



Figure 11. Examples of words with rapidly growing frequency.

For example, when we take $\frac{1}{q_{ij}^d} < 10$ and $\frac{\hat{r}_{ij}+1}{\hat{r}_{ij}^2} < \frac{0.1+1}{0.1^2}$ for abstracts in computer science, the words that satisfy the conditions are: 'the', 'is', 'for', 'by', 'be', 'this', 'are', 'i', 'at', 'which', 'an', 'have', 'but', 'we', 'all', 'they', 'one', 'has', 'their', 'other', 'there', 'more', 'new', 'any', 'these', 'time', 'than', 'some', 'only', 'two', 'into', 'them', 'our', 'under', 'first', 'most', 'then', 'over', 'work', 'where', 'many', 'through', 'well', 'how', 'even', 'while', 'however', 'high', 'given', 'present', 'large', 'research', 'different', 'set', 'study', 'important', 'several', 'e', 'further', 'including', 'often', 'provide', 'due', 'using', 'better', 'various', 'problem', 'show', 'problems', 'design', 'proposed', 'g',



Figure 12. The words "are" and "is" are decreasing in frequency.

'across', 'approach', 'existing', 'compared', 'task', 'learn', 'improve', 'achieve', 'novel', 'domain', 'demonstrate', 'introduce', 'propose', 'prediction'.

And when $\frac{1}{q_{ij}^d} < 50$ and $\frac{\hat{r}_{ij}+1}{\hat{r}_{ij}^2} < \frac{0.8+1}{0.8^2}$, the words are: 'i', 'would', 'so', 'some', 'what', 'out', 'work', 'very', 'because', 'much', 'good', 'way', 'great', 'here', 'since', 'might', 'last', 'end', 'means', 'having', 'thus', 'above', 'give', 'e', 'further', 'far', 'find', 'although', 'show', 'n', 'help', 'together', 'particular', 'whose', 'issue', 'according', 'addition', 'usually', 'art', 'especially', 'respect', 'works', 'shows', 'g', 'makes', 'hard', 'significant', 'run', 'address', 'particularly', 'idea', 'consider', 'includes', 'built', 'adopted', 'obtain', 'establish', 'useful', 'leading', 'performed', 'create', 'named', 'conducted', 'resulting', 'hence', 'findings', 'towards', 'prove', 'build', 'perform', 'moreover', 'describe', 'besides', 'demonstrated', 'via', 'presents', 'mainly', 'fail', 'namely', 'allowing', 'demonstrate', 'advances', 'suffer', 'overcome', 'introduce', 'accurately', 'identifying', 'enhance', 'crucial', 'etc', 'utilize', 'demonstrates', 'additionally', 'focuses', 'motivated', 'characterize'.

F. Noise analysis

F.1. Variance in real data

Abstracts in the *cs* category among the first 500,000 articles were divided into groups in chronological order, with the same number in each group. We counted the number of occurrences of each word within each group, and calculated the variance between the different groups. This was repeated as a function of the number of abstracts included in each group, and the results are shown in Figure 13.



Figure 13. Variance of the word counts between groups of abstracts as a function of the number of abstracts included in each group.

Then we also analyzed the variance-to-mean ratio (defined as the variance of the sum of a word's counts divided by the mean of the sum) and the coefficient of variation (defined as the standard deviation of the sum divided by the mean of the sum) for the 12 most frequent words, as shown in Figure 14 and Figure 15, and the variance-mean ratio of further words as in Figure 16.



Figure 14. Variance-to-mean ratio.

We observe that, at least for a subset of the words considered here, the variance-to-mean ratios are essentially on the same scale (although there are words that do not follow this



Figure 15. Coefficient of variation.



Figure 16. Variance-to-mean ratio for some further words.

pattern). Therefore, a simple Gaussian distribution

$$\delta_{ij}(f_{ij}) \sim \mathcal{N}(0, f_{ij}\sigma_{ij}^2) \,. \tag{28}$$

which corresponds to case 2, seems to be a reasonable approximation.

F.2. Calculation details

Case 1: we know that

$$\begin{aligned} &\frac{\partial L_{j,t,g}(\eta_j)}{\partial \eta_j} \\ = &\frac{2}{n_j} \sum_{i \in I_j} \left(\eta_j(t) x_{ij}^2(t) - h_{ij}(t) x_{ij}(t) \right) \\ &- \frac{2}{n_j} \sum_{i \in I_j} \frac{\partial g_{ij}(t)}{\partial \eta_j(t)} \left(h_{ij}(t) - \eta_j(t) x_{ij}(t) - g_{ij}(t) \right) \\ &+ \frac{2}{n_j} \sum_{i \in I_j} x_{ij}(t) g_{ij}(t) \end{aligned}$$

and

$$(\hat{\eta}_{j}^{g}(t) - \hat{\eta}_{j}(t)) \sum_{i \in I_{j}} x_{ij}^{2}(t)$$

$$= \sum_{i \in I_{j}} \frac{\partial g_{ij}(t)}{\partial \eta_{j}(t)} (h_{ij}(t) - \eta_{j}(t)x_{ij}(t))$$

$$- \sum_{i \in I_{j}} x_{ij}(t)g_{ij}(t) - \sum_{i \in I_{j}} g_{ij}(t) \frac{\partial g_{ij}(t)}{\partial \eta_{j}(t)}.$$
(29)

But without knowing the distribution of $\epsilon_{ij}(\cdot)$ and $\epsilon^s_{ij}(\cdot)$, we have no way of estimating the value of this bias, so we assume that $\epsilon_{ij}(f_{ij}) \sim \mathcal{N}(0, f_{ij}\sigma^2_{ij,\epsilon})$ and $\epsilon^s_{ij}(f_{ij}) \sim \mathcal{N}(0, f_{ij}\sigma^2_{ij,\epsilon})$, e.g., $\epsilon_{ij}(1) \sim \mathcal{N}(0, \sigma^2_{ij,\epsilon})$, then we can obtain an expression for $\epsilon^{\eta}_{ij}(q, f, t)$:

$$\epsilon_{ij}^{\eta}(q,f,t) = \frac{\epsilon_{ij}(1)}{\sqrt{\eta_j(t)f_{ij}^*(t) + \delta_{ij}(*)}} - \frac{\epsilon_{ij}^s(1)}{\sqrt{q_{ij}^d}} \qquad (30)$$

$$g_{ij}(t) = \frac{\eta_j(t) f_{ij}^*(t) \epsilon_{ij}(1)}{\sqrt{\eta_j(t) f_{ij}^*(t) + \delta_{ij}(*)}}$$
(31)

$$-\frac{\eta_j(t)f_{ij}^*(t)\epsilon_{ij}^s(1)}{\sqrt{q_{ij}^d}}.$$
 (32)

Therefore, all terms on the right-hand side of Eq. (29) are zero-mean noise, except for the last one:

$$g_{ij}(t) \frac{\partial g_{ij}(t)}{\partial \eta_j(t)} = g_{ij}(t) \frac{f_{ij}^*(t)(\eta_j(t)f_{ij}^*(t) + 2\delta_{ij}(*))\epsilon_{ij}(1)}{2(\eta_j(t)f_{ij}^*(t) + \delta_{ij}(*))^{\frac{3}{2}}} \qquad (33)$$
$$- g_{ij}(t) \frac{f_{ij}^*\epsilon_{ij}^*(1)}{\sqrt{q_{ij}^d}}.$$

Removing the items with zero means, we get

We can get more insight from the previous results. As by definition $\eta_j(t) \ge 0$, the estimate $\hat{\eta}_j(t)$ given by Eq. (17) tends to be biased high in our model. The value of \hat{r}_{ij} plays a role in the minimization of bias, as it only appears in the denominator in Eq. (21). Similarly, if the value of \hat{r}_{ij} and f_{ij}^* will reduce the bias, as seen from Eq. (34) – therefore, we should consider including preferentially in our analysis words with larger values of q_{ij}^d , and \hat{r}_{ij} , f_{ij}^* and \hat{r}_{ij} .

Case 2: we have

$$\xi_{ij}(t) = (\hat{r}_{ij} + \epsilon^{\eta}_{ij}(q, f, t))\delta_{ij}(\eta_j(t)f^*_{ij}(t)) + \delta'_{ij}(f^*_{ij}(t)) = \sqrt{\eta_j(t)f^*_{ij}(t)}(\hat{r}_{ij} + \epsilon^{\eta}_{ij}(q, f, t))\delta_{ij}(1) + \sqrt{f^*_{ij}(t)}\delta'_{ij}(1).$$
(35)

Then we can define $g_{ij}^c(t)$ and $\xi_{ij}^c(t)$:

$$g_{ij}^{c}(t) = \eta_{j}(t)f_{ij}^{*}(t)\epsilon_{ij}^{\eta}(q, f, t) + \sqrt{\eta_{j}(t)f_{ij}^{*}(t)}(\hat{r}_{ij} + \epsilon_{ij}^{\eta}(q, f, t))\delta_{ij}(1)$$

$$\xi_{ij}^{c}(t) = \sqrt{f_{ij}^{*}(t)}\delta_{ij}'(1)$$
(36)
(37)

As $\xi_{ij}^c(t)$ doesn't depend on $\eta_j(t)$, the loss function under this assumption is:

$$L_{j,t,g}^{c}(\eta_{j}) = \frac{1}{n_{j}} \sum_{i \in I_{j}} (h_{ij}(t) - \eta_{j}(t)x_{ij}(t) - g_{ij}^{c}(t))^{2}$$

$$= \frac{1}{n_{j}} \sum_{i \in I_{j}} (\xi_{ij}^{c}(t))^{2}.$$
(38)

And we will get a complex expression for the bias part like Eq. (29).

As in case 1, we set $\frac{\partial L^c_{j,t,g}(\eta_j)}{\partial \eta_j} = 0$ to obtain the new

estimate $\hat{\eta}_{i}^{g}(t)$ corrected for bias and noise,

$$(\hat{\eta}_{j}^{g}(t) - \hat{\eta}_{j}(t)) \sum_{i \in I_{j}} x_{ij}^{2}(t)$$

$$= \sum_{i \in I_{j}} \frac{\partial g_{ij}^{c}(t)}{\partial \eta_{j}(t)} (h_{ij}(t) - \eta_{j}(t)x_{ij}(t))$$

$$- \sum_{i \in I_{j}} x_{ij}(t)g_{ij}^{c}(t) - \sum_{i \in I_{j}} g_{ij}^{c}(t)\frac{\partial g_{ij}^{c}(t)}{\partial \eta_{j}(t)}$$
(39)

where

$$\frac{\partial g_{ij}^{c}(t)}{\partial \eta_{j}(t)} = f_{ij}^{*}(t)\epsilon_{ij}^{\eta}(q, f, t) + \eta_{j}(t)f_{ij}^{*}\frac{\partial \epsilon_{ij}^{\eta}(q, f, t)}{\partial \eta_{j}(t)} \\
+ \frac{\sqrt{f_{ij}^{*}(t)}}{2\sqrt{\eta_{j}(t)}}(\hat{r}_{ij} + \epsilon_{ij}^{\eta}(q, f, t))\delta_{ij}(1) \\
+ \sqrt{\eta_{j}(t)f_{ij}^{*}(t)}\frac{\partial \epsilon_{ij}^{\eta}(q, f, t)}{\partial \eta_{j}(t)}\delta_{ij}(1).$$
(40)

The bias part is also expressed as

$$\hat{\eta}_{j}(t) - \hat{\eta}_{j}^{g}(t) = \frac{\sum_{i \in I_{j}} \mathbf{E} \left[g_{ij}^{c}(t) \frac{\partial g_{ij}^{c}(t)}{\partial \eta_{j}(t)} \right]}{\sum_{i \in I_{j}} (f_{ij}^{*}(t)\hat{r}_{ij})^{2}} \,. \tag{41}$$

Also with the same assumptions for $\epsilon_{ij}(\cdot)$ and $\epsilon_{ij}^s(\cdot)$, $\epsilon_{ij}(f_{ij}) \sim \mathcal{N}(0, f_{ij}\sigma_{ij,\epsilon}^2)$ and $\epsilon_{ij}^s(f_{ij}) \sim \mathcal{N}(0, f_{ij}\sigma_{ij,\epsilon}^2)$. then we can obtain an expression for $\epsilon_{ij}^{\eta}(q, f, t)$,

$$\epsilon_{ij}^{\eta}(q, f, t) = \frac{\epsilon_{ij}(1)}{\sqrt{\eta_j(t)f_{ij}^*(t) + \sqrt{\eta_j(t)f_{ij}^*(t)}\delta_{ij}(1)}} - \frac{\epsilon_{ij}^s(1)}{\sqrt{q_{ij}^d}}$$
(42)

and its derivative,

$$\frac{\frac{\partial \epsilon_{ij}'(q, f, t)}{\partial \eta_j(t)}}{= \frac{-\left(2f_{ij}^*(t)\sqrt{\eta_j(t)} + \sqrt{f_{ij}^*(t)}\delta_{ij}(1)\right)\epsilon_{ij}(1)}{4\sqrt{\eta_j(t)}\left(\eta_j(t)f_{ij}^*(t) + \sqrt{\eta_j(t)}f_{ij}^*(t)\delta_{ij}(1)\right)^{\frac{3}{2}}}.$$
(43)

Combining the above equations, we can get similar conclusions as in case 1.

F.3. Approximations in real data

Unfortunately, we cannot know the true value of $f_{ij}^*(t)$ in the ChatGPT era, but we can replace it with the estimation $\hat{f}_{ij}^*(t)$ based on the word frequency before ChatGPT was introduced. As our objective is to identify the words that Chat-GPT "likes" (or "dislikes") to use compared to academic researchers on average, we assume that the frequencies of these words should remain stable without ChatGPT, i.e., we take the average of the pre-ChatGPT periods before T_0 as following:

$$f_{ij}^{*}(t) = \frac{1}{\#\{t \le T_0\}} \sum_{t \le T_0} f_{ij}^d(t), \text{ if } t > T_0.$$
 (44)

Considering that the noise in real data is likely highly complex, we did not estimate the variance of $\epsilon_{ij}(\cdot)$. Instead, we used ChatGPT to process additional abstracts (on top of those used to estimate r_{ij}), and used the resulting frequencies as calibration for the bias and noise.

G. Other results



Figure 17. Similar to Figure 5, but normalized to the total number of words, rather than the total number of abstracts.

The corresponding results in Figure 18 use the following prompt:

"Please rewrite the following paragraph from an academic paper:"

In this example, we add the word "please" and make it clear that this comes from an "academic paper", replacing "revise" with "rewrite".

Although the quantitative results of our tests were not as good as before, the errors were still small at lower mixed ratios, which also illustrates the robustness of our method. This is understandable because in data generated with different prompts, not all of our previous assumptions hold, and the estimate of \hat{r}_{ij} on r_{ij} in our model may be biased. We can also note that most of our estimates in Figure 18 are on the high side relative to the ground truth, most likely



Figure 18. Similar to Figure 17, but with a different prompt for test data than used in calibration data.

because we use a more precise prompt for the test data here, making the frequency change rate of the relevant words higher.



Figure 19. The same estimates as in Figure 6, but word frequencies were normalized by the number of words.