DPPA: Merging Large Language Model using Dynamic Pruning and Partition Amplification

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Abstract

 Model merging aims to combine models with different capabilities into a single unified model, providing multiple capabilities with- out the necessity of retraining with the original training data. However, as distinctions between fine-tuned and base models grow, especially for large language models, current methods suffer significant performance drops, hindering true multi-domain capabilities. In this study, we propose a two-stage method, called Dynamic **Pruning and Partition Amplification (DPPA),** to address the challenge of merging models with significant distinctions. First, we intro- duce Dynamic Pruning (DP) to discover signif- icant parameters and remove redundant ones. Subsequently, we propose Dynamic Partition Amplification (DPA) to restore the capability in the domain. Experimental results demonstrate 019 that our approach performs outstandingly, im- proving model merging performance by almost **021** 20%.

022 1 Introduction

 Model merging, or model fusion, combines models with different capabilities into a unified model. Un- like multi-task learning, model merging requires no retraining on the original training data. On the one hand, model merging can combine models from different domains into a unified model, thereby offering multi-domain capabilities [\(Alonso et al.,](#page-8-0) [2024\)](#page-8-0). On the other hand, model merging can also fuse models trained on diverse data within the same domain, further enhancing overall domain perfor- mance [\(Fu et al.,](#page-8-1) [2024\)](#page-8-1). The challenge of model merging lies in resolving conflicts between the pa-rameters of different models.

036 The significance of the parameter varies depend- ing on the model. Minimal distinctions between fine-tuned models and their base models do not degrade the performance of merging model. The distinctions between fine-tuned models and their

base models become more significant when a large **041** amount of domain-specific data is used for tuning **042** in fields such as mathematics [\(Hendrycks et al.,](#page-8-2) **043** [2021\)](#page-8-2) and code [\(Rozière et al.,](#page-9-0) [2023\)](#page-9-0), or with **044** advancements in techniques like instruction tun- **045** ing [\(Mishra et al.,](#page-9-1) [2022\)](#page-9-1). These fine-tuned models **046** achieve enhanced domain-specific performance, al- **047** though increased parameter conflicts arise during **048** model merging. However, current merging meth- **049** [o](#page-10-2)ds [\(Yu et al.,](#page-10-0) [2023b;](#page-10-0) [Yang et al.,](#page-10-1) [2023a;](#page-10-1) [Yadav](#page-10-2) **050** [et al.,](#page-10-2) [2023b\)](#page-10-2) experience significant performance **051** drops with these fine-tuned models, rendering true **052** multi-domain capabilities unattainable. Further- **053** more, because significance determination is based **054** on the distinctions between these fine-tuned mod- **055** els and their base models, existing methods for **056** measuring parameter significance [\(Sun et al.,](#page-9-2) [2023;](#page-9-2) 057 [Frantar and Alistarh,](#page-8-3) [2023\)](#page-8-3) are not effective. **058**

In this study, we tackle the challenge of merging **059** models with significant distinctions by introduc- **060** ing a two-stage method known as Dynamic Prun- **061** ing and Partition Amplification (DPPA). First, we **062** introduce Dynamic Pruning (DP) to discover sig- **063** nificant parameters and remove redundant ones. **064** Subsequently, we propose Dynamic Partition Am- **065** plification (DPA), to further amplify the importance **066** of these significant parameters, thereby restoring **067** domain capabilities. Our approach is applied to the **068** delta parameter, which signifies the weight differ- **069** ence between the fine-tuned models and the base **070** model. **071**

Dynamic Pruning (DP) aims to discover signif- **072** icant parameters and remove redundant ones. A **073** simple but effective way to measure significance **074** is based on the magnitude of the delta parameter. **075** Based on their significance, we adjust the pruning **076** rate of different linear layers to retain the more cru- **077** cial parameters. As illustrated in Figure [1,](#page-1-0) there **078** are notable differences in significance between lay- **079** ers, and even within the same layer, different linear **080** layers exhibit varying levels of significance. For **081**

Figure 1: Within the left segment of figure, it can be found that Dynamically Pruning (DP) method modifies the pruning rate at both layer and linear layer levels, distinguishing it from magnitude pruning. On the figure's right segment, we can see the integration of DP and Dynamical Partition Amplification (DPA), paralleled with the drop and rescale operations inherent in the DARE system. This integration enhances complex model performance after the pruning process significantly.

2

082 example, the Q and K linear layers in layer *0* are **083** more significant than the other linear layers.

 Moreover, Dynamic Partition Amplification (DPA) makes these significant parameters more im- portant to restore the capability in the domain. We discover that the necessary factor changes depend- ing on the varying significance of the parameters. So we divide parameters based on their significance levels to get parameter partition. Each partition is then assigned various factors to enhance its domain capabilities. To evaluate the effectiveness of these factors, we use a validation dataset from the cor- responding domain. As shown in Figure [1,](#page-1-0) The factors for the two partitions are *1.3* and *1.1*.

096 The base model adopted in this work is LLaMA- 2 [\(Touvron et al.,](#page-9-3) [2023\)](#page-9-3) and Mistral [\(Jiang et al.,](#page-8-4) [2023\)](#page-8-4). We focus on two distinct domains: Mathe- matics and Finance. The results of the experiment show that our method only keeps 20% of param- eters while yielding performance comparable to other methods that maintain up to 90% of parame- ters. Furthermore, our method shows outstanding performance, leading to a significant improvement of almost 20% in model merging performance. Our method even significantly outperforms others when fine-tuned models similar to the original, like Abel-mistral. In the detail analysis section, we examine

the impact of ignoring parameter size and the num- **109** ber of parameters on performance, compare DPA **110** with other pruning methods, and demonstrate results for different initialization methods. Through 112 parametric analysis, we explain DPPA's effective- **113** ness and investigate how increasing the number of **114** domains affects model performance. We will share **115** our code on GitHub. **116**

2 Background **¹¹⁷**

The challenge of model merging is resolving con- **118** flicts between the parameters of different models. 119 Model merging first goes through the pruning stage, **120** then the merging stage. For the pruning stage, the **121** current method [\(Yu et al.,](#page-10-0) [2023b\)](#page-10-0) aims to reduce **122** the number of conflicting parameters before param- **123** eters clash. For the merging stage, the predominant **124** methods [\(Yang et al.,](#page-10-1) [2023a;](#page-10-1) [Yadav et al.,](#page-10-3) [2023a;](#page-10-3) **125** [Jin et al.,](#page-9-4) [2023\)](#page-9-4) focus on resolving conflicts when **126** parameters clash. In contrast to previous studies, **127** our method focuses more on the pruning stage. **128**

We review the definition of model merging and 129 the delta parameter. It should be noted that our **130** approach is used for the delta parameter, which **131** represents the weight difference between the fine- **132** tuned models and their base model. **133**

134 2.1 Model Merging Problem

 Model merging combines multiple models derived from the same base model. It cannot handle the merging of multiple base models. Specifically, for 138 models $M^1 \sim M^k$, each associated with different **domains** $D^1 \sim D^k$, where each domain comprises **a** set of tasks $D^i = \{T_1^i \sim T_n^i\}$. Here, k represents the number of domains, i represents a specific do- main, and n represents the number of tasks within that domain.

144 **By merging** $M^1 \sim M^k$ **, we obtain the integrated** 145 model M^m , which possesses the ability to handle 146 **tasks from** $D^1 \sim D^k$ simultaneously.

147 2.2 Delta Parameter

 Analyzing the delta parameter enables a deeper understanding of the changes brought by the fine- tuning process. For each model, we find its com-151 mon base model M^B and the base weight W^B . **For model** M^i **, we have the corresponding weight** $Wⁱ$. We define the delta parameter as the tran- sition of the parameter space distribution from the base model to the fine-tuned model, which is $\Delta^i = W^i - W^B.$

¹⁵⁷ 3 Dynamic Pruning and Partition **¹⁵⁸** Amplification (DPPA)

 First, we introduce Dynamic Pruning (DP) to dis- cover significant parameters and remove redundant ones. Next, we propose Dynamic Partition Am- plification (DPA), which makes these significant parameters more important. Finally, we integrate the delta parameters from various fine-tuned mod- els into the base model, resulting in a single model with multiple capabilities.

167 3.1 Dynamic Pruning

 First, we use a single linear layer as an example to explain the overall notation system, as shown in Table [1.](#page-2-0) Next, we define the concept of parameter significance. Finally, we present the method for ad-justing the pruning rate based on this significance.

For a fine-tuned model, we first get the delta **173** parameters Δ of the model, mentioned at Sec. [2.2.](#page-2-1) **174** We do not take into account parameters such as **175** layer norm, focusing solely on linear layers, such as **176** Q, K, V, O in Attention, and up/down sampling in **177** MLP. We separate the linear layer delta parameters **178** δ_l from Δ and denote them as S_l by **179**

$$
S_l = \{ \delta_l | \delta_l \subseteq \Delta, \delta_l \text{ represents a linear layer} \}.
$$
\n(1)

(1) **180**

. (4) **210**

Parameter Significance We believe that not all 181 parameters in the delta parameters are significant. **182** For a group of parameters δ_l from one linear layer, 183 the significant parameters δ_l' are N times larger 184 than the average of absolute values of parameters **185** δ_l by 186

$$
\delta_l' = \{ \theta' | \theta' \in \delta_l, |\theta'| > N \cdot \frac{\sum_{\theta \in \delta_l} |\theta|}{\|\delta_l\|} \}.
$$
 (2)

The parameter significance $sig(\cdot)$ is of the sum of 188 the absolute values of these significant parameters **189** to the sum of the absolute values of all parameters, **190** as follows: **191**

$$
sig(\delta_l) = \frac{\sum_{\theta' \in \delta'_l} |\theta'|}{\sum_{\theta \in \delta_l} |\theta|}.
$$
 (3)

As demonstrated above, parameter significance pri- **193** marily focuses on the values of the parameters. **194**

Adjusting Pruning Rate Once the significance **195** of the parameters has been determined, we can **196** adjust the pruning rate based on the significance of **197** various linear layers. **198**

We translate significance to dynamic pruning **199** rates $rat(\cdot)$ by using a modified normalization 200 method. We consider the variations in the num- **201** ber of parameters among linear layers. Our goal is **202** to ensure that the product of the adjusted pruning **203** rates and the number of parameters in each linear **204** layer averages out to zero, thereby maintaining the **205** predetermined overall pruning rate. As a result, we **206** weighted the mean significance by multiplying it 207 with the number of parameters in each linear layer, 208 as follows: **209**

$$
rat(\delta_l, S_l) = sig(\delta_l) - \sum_{\delta \in S_l} sig(\delta) \cdot \frac{\|\delta\|}{\|\Delta\|}. \quad (4)
$$

We examine the fluctuations in adjustment rates, **211** where excessively high adjustments have led to 212 pruning rates exceeding 100%. We define the max- **213** imum value of pruning rate fluctuation as λ . As a 214

Figure 2: We use green and orange lines to show amplification rate trajectories. The blue star marks the optimal rate at 90% pruning, and the red star marks it at 80%. Contour lines illustrate performance in the mathematical domain.

 result, We first find the maximum absolute value **b** of the dynamical pruning rates, $rat(\cdot)$, across all **linear layers.** The scaling factor, $fac(\cdot)$, is then 218 calculated by dividing λ by this maximum value, as illustrated below:

$$
fac(S_l) = \frac{\lambda}{\arg\max_{\delta \in S_l} abs(rat(\delta, S_l))}.
$$
 (5)

 Following the principle that higher parameter significance corresponds to lower pruning rates, We modify the pruning rate by applying a scaling factor, resulting in the final adjusted rate for a linear $layer, \alpha_l,$ as follows:

$$
\alpha_l = \alpha - fac(S_l) \cdot rat(\delta_l, S_l), \qquad (6)
$$

227 where α represents predetermined overall pruning **228** rate.

229 3.2 Dynamic Partition Amplification

 First, we apply Dynamic Pruning at various prun- ing rates to partition the parameters. To restore performance, we amplify and combine these par- titions. By acknowledging parameter interactions during enhancement, we propose two initialization methods and assess their effectiveness across var- ious scenarios. Finally, we provide detailed infor- mation on the data used and the validation metrics employed during the enhancement process.

239 Partition of Parameters The number of retained **240** parameters varies with different pruning rates. Compared to lower pruning rates, the higher prun- **241** ing rates retained the fewer but more crucial param- **242** eters. At lower pruning rates, more parameters are **243** retained. For example, as shown in Fig. [1,](#page-1-0) higher **244** pruning rates retain only the purple parameters, **245** while lower rates retain both the purple and green 246 parameters. Therefore, the parameter partition for **247** the lower rate includes the green parameters. We **248** set the partition size to β , implying that when the **249** low pruning rate is x , the high pruning rate be- 250 comes $x + \beta$. 251

Partition Amplification Partitions with higher **252** pruning rates are considered more important. The **253** importance of the partitions is ranked based on their **254** pruning rates. After initialization, we first amplify **255** the most important partition. By multiplying the **256** partition parameters by a dynamic factor, an ex- **257** panded partition is obtained. This dynamic factor **258** starts at 1 and increases by a hyperparameter, de- **259** noted as γ, until optimal performance is achieved. **260** Once the primary parameter partition factor is de- **261** termined, adjust the secondary parameter partitions **262** accordingly, and continue this process as needed. **263**

Initialization methods There are interacted **264** among partition parameters, and our approach only **265** changes one partition at each stage. Thus, whether **266** considering the impact of other partitions when **267** amplifying partition is crucial. We propose two **268** initialization methods: one ignoring parameter in- **269** teractions and the other considering them. Use the **270** first method if performance differences between **271** partitions are within 5%, otherwise use the second **272** method. Method 1 adjust parameters within the **273** 90% pruning rate partition, setting the remainder **274** to zero. The resulting curve from this method is **275** illustrated by the green line in Fig. [2.](#page-3-0) Method 2 use **276** the partition that matches the target pruning rate **277** while adjusting the 90% partition. The resulting 278 curve from this method is illustrated by the orange **279** line in Fig. [2.](#page-3-0) **280**

Validation Metrics For adjusted models men- **281** tioned above, we verify their capabilities using in- **282** domain datasets. No additional training is required; **283** we simply infer the model's performance on the **284** validation dataset. **285**

To normalize performance differences across **286** tasks, we introduced the Task-Ratio metric. For **287** a task T_i , the Task-Ratio is the performance ratio 288 of the adjusted model M_{adj} to the dense model 289

290 M_{den} , defined as:

$$
\text{Task-Ratio}_j = \frac{Per(M_{adj}, T_j)}{Per(M_{den}, T_j)},\tag{7}
$$

292 where $Per(M, T)$ represents the performance of **293** model M on task T. According to the formula, the **294** Task-Ratio of the dense model is 100%.

 We propose Domain-Ratio metrics to evaluate performance across abundant datasets in a domain. We use a multiplicative approach to account for all tasks and avoid obscuring low-performance ones. To make performance independent of task number n, we square the product. The formula for Domain-Accuracy is as follows:

302 Domain-Ratio =
$$
\sqrt[n]{\prod_{j=1}^{n} \text{Task-Ratio}_j}
$$
. (8)

303 3.3 Model Merging

 After applying Dynamic Pruning and Partition Am- plification, We obtained the pruned delta parame- ters of different models. In Section [5.3,](#page-7-0) we refer to multiple existing methodologies for merging stage. We employ Ties-Merging [\(Yadav et al.,](#page-10-2) [2023b\)](#page-10-2), to resolve parameter conflicts during the merging stage after the pruning stage. Thus, we get the final merging model:

$$
W^m = W^B + \text{Ties}(\Sigma_{i=1}^k \text{DPPA}(\Delta^i)) \tag{9}
$$

³¹³ 4 Experiments

314 4.1 Experimental Setup

 Pre-Trained Backbone and Fine-tune Models Considering the need to fine-tune the base model for different domains and its performance impact, we chose LLaMa 2 [\(Touvron et al.,](#page-9-3) [2023\)](#page-9-3) as the base model over other pre-trained models. For the mathematics and finance domains, we selected two high-performing models: Abel [\(Chern et al.,](#page-8-5) [2023\)](#page-8-5) and Finance-chat [\(Cheng et al.,](#page-8-6) [2023\)](#page-8-6). We chose Mistral despite its few fine-tuning models to test our method on different base models and minimal variations from the original. Abel-Mistral represents such small differences.

 Datasets and Metric For each domain, we selected two datasets. In mathematics, we chose GSM8k [\(Cobbe et al.,](#page-8-7) [2021\)](#page-8-7) and MATH [\(Hendrycks et al.,](#page-8-2) [2021\)](#page-8-2), evaluating models using zero-shot accuracy with Abel's testing script [\(Chern et al.,](#page-8-5) [2023\)](#page-8-5). In finance, we chose [F](#page-9-6)iQA_SA [\(Maia et al.,](#page-9-5) [2018\)](#page-9-5) and FPB [\(Malo](#page-9-6)

[et al.,](#page-9-6) [2014\)](#page-9-6), also using zero-shot accuracy. For **334** AdaptLLM [\(Cheng et al.,](#page-8-6) [2023\)](#page-8-6), without a testing **335** script, we deemed a multiple-choice question **336** correct if the predicted sentence included the **337** correct choice. The evaluation metric is detailed in **338** Sec. [3.2.](#page-3-1) **339**

Implementation Details In our study using the **340** vLLM framework, we set a batch size of 32 for **341** GSM8k and MATH, and a batch size of 1 for **342** FiQA_SA and FPB. We used greedy decoding with **343** a temperature of 0 and a maximum generation **344** length of 2048, conducted on an NVIDIA Tesla **345** A100 GPU. We set N to 5, λ to 0.08, and both β 346 and γ to 0.1. **347**

4.2 Baseline Method **348**

We establish two sample weight averaging meth- **349** ods, one merging-based, and five pruning-based **350** methods as baselines. they are described below: **351**

- Model Soups [\(Wortsman et al.,](#page-10-4) [2022\)](#page-10-4) aver- **352** ages all model parameters. **353**
- LM-Cocktail [\(Xiao et al.,](#page-10-5) [2023\)](#page-10-5) weights mod- **354** els from different domains to select the opti- **355** mal result. **356**
- Ties-Merging [\(Yadav et al.,](#page-10-2) [2023b\)](#page-10-2) resolves **357** parameter conflicts during merging stage. **358**
- Wanda [\(Sun et al.,](#page-9-2) [2023\)](#page-9-2) trims parameters **359** that minimally impact inference. **360**
- SparseGPT [\(Frantar and Alistarh,](#page-8-3) [2023\)](#page-8-3) ad- **361** justs pruned parameters for better perfor- **362** mance. 363
- Magnitude [\(Han et al.,](#page-8-8) [2015b\)](#page-8-8) keeps weights **364** with larger absolute values, removing smaller 365 ones. **366**
- OWL [\(Yin et al.,](#page-10-6) [2023\)](#page-10-6) recognizes parameter **367** significance varies across model layers. **368**
- DARE [\(Yu et al.,](#page-10-0) [2023b\)](#page-10-0) starts with random **369** pruning, then expands remaining parameters **370 based on pruning rate.** 371

4.3 Main Result of DPPA **372**

We present the Domain-Ratio and Task-Ratio re- **373** sults for all datasets. Table [2](#page-5-0) displays results for **374** three models with varying pruning rates. Our **375** method performs optimally at high pruning rates **376** on both Llama2 and Mistral, regardless of Domain- **377** Ratio or Task-Ratio. The experimental results show **378** our approach retains only 20% of parameters yet **379** performs comparably to methods retaining 90%, **380**

Sparse Ratio		Domain-Ratio					Task-Ratio		
	Magnitude	OWL	DARE	DPPA	Task	Magnitude	OWL	DARE	DPPA
Abel-Llama									
10%	96.46	96.69	96.64	98.86	GSM8k	100.14	99.63	98.23	98.49
					Math	92.92	93.84	95.07	99.23
80%	80.12	77.11	87.41	97.08	GSM8k	83.78	82.77	89.49	95.56
					Math	76.61	71.84	85.38	98.61
90%	53.41	54.09	73.44	86.85	GSM8k	57.42	57.29	83.28	87.71
					Math	49.69	51.07	64.76	86.00
Finance-Llama									
10%	90.81	89.12	91.04	97.05	FiQA SA	88.81	86.95	91.92	95.14
					FPB	92.84	91.35	90.16	99.01
80%	71.04	74.92	84.01	96.65	FiQA SA	75.77	81.36	83.22	94.41
					FPB	66.61	69.00	84.79	98.95
90%	54.71	56.74	82.90	92.11	FiQA SA	53.41	57.76	83.85	88.82
					FPB	56.03	55.73	81.96	95.52
Abel-Mistral									
10%	99.63	99.67	99.75	99.70	GSM8k	99.82	99.82	99.85	99.82
					Math	99.45	99.52	99.66	99.59
80%	93.46	92.52	95.32	99.98	GSM8k	92.50	92.31	94.72	97.38
					Math	94.43	92.73	95.92	102.64
90%	81.24	79.92	86.88	94.99	GSM8k	84.90	83.49	88.66	93.15
					Math	77.73	76.51	85.13	96.87

Table 2: Domain-Ratio and Task-Ratio of different methods at various pruning rates. Additional results under remainder pruning rates and the specific performance values for different tasks are presented in Appendix [A.](#page-10-7)

Methods	Math	Fin	Average
Model Soups	15.99	79.46	47.73
LM-Cocktail	76.96	78.80	77.88
Ties-Merging	96.23	22.12	59.18
w/ Wanda	8.30	20.65	14.48
w/SparseGPT	21.74	18.60	20.17
w/DARE 90%	21.10	64.88	42.99
w/DPPA 90%	89.25	79.40	84.33
w/DARE 80%	58.43	77.16	67.79
w/DPPA 80%	92.75	95.45	94.10

Table 3: Domain-Ratio of the merged Llama model that combines domains mathematics and finance. The specific performance values are presented in Appendix [A.](#page-10-7)

Domains	Magnitude	OWL	DР
Math	53.41	54.09	54.97
Fin	54.71	56.74	62.06

Table 4: Domain-Ratio of DP at a pruning rate of 90%.

381 guaranteeing over 96% of the domain's perfor-**382** mance.

383 Due to space constraints, detailed values, remain-**384** der pruning rates, and DPA parameter partition fac-**385** tors are included in Appendix [A.](#page-10-7)

386 4.4 Main Result of Merge Methods

387 We validate our pruning method for model merging **388** by integrating models. Table [3](#page-5-1) displays results of

Model	Min	10%	90%	Max
Abel-Llama	-0.01733	-0.00114	0.00114	0.02014
Fin-Llama	-0.02612	-0.00160	0.00160	0.02011
Abel-Mistral	-0.00127	-0.00010	0.00010	0.00139

Table 5: The offset of different models from the base model at different position proportions.

two domains at 80% and 90% pruning rates and **389** other baselines. Sample weight averaging methods **390** like Model Soups and LM-Cocktail suffer perfor- **391** mance degradation due to unresolved parameter **392** conflicts. Traditional pruning methods like Wanda **393** and SparseGPT measures the importance of full **394** parameter, unlike the delta parameter, impacting **395** the model after merging. Our method improves **396** performance by over 20% compared to DARE at **397** the same pruning rate, demonstrating its efficacy in **398** model merging. 399

4.5 Detail Analysis 400

We present the performance of DP in Table [4](#page-5-2) and 401 discuss cases where DP can replace DARE. Table [6](#page-6-0) 402 examines the results of disregarding the parameter **403** magnitude considering only the number of parame- **404** ters as the definition of parameter significance and **405** the effects of rounding off $fac(\cdot)$. We compare **406** performance of DPA using other pruning methods **407** in Table [7](#page-6-1) and demonstrate the performance of two **408**

Figure 3: After analyzing the pruned parameters of the financial model, it is evident that there is a higher parameter count in the initial and final 0, 31 layers, while the middle 17 layers have fewer parameters. Additionally, in the Q, K, V components, it is observed that 90% of the parameters are concentrated in certain dimensions. To facilitate observation, we have amplified the value by a factor of 1000.

Methods	Math	Fin
DР	54.97	62.06
change_sig	53.13	60.57
w/o fac	52.69	61.84

Table 6: Domain-Ratio of the variants of DP at a pruning rate of 90%.

 different initializations in Table [8.](#page-6-2) We analyzed why DPPA is effective, as shown in the Fig. [3.](#page-6-3) Fi- nally, we explore the performance impact of adding a domain in Table [9.](#page-7-1)

 The Effectiveness of DP As seen in Table [4,](#page-5-2) DP outperforms at high pruning rates by adjusting the significance of parameters within each layer, re- taining crucial ones. The DARE method struggles when parameter deviations exceed 0.03, with per- formance worsening as offsets increase (see Ta- ble [5\)](#page-5-3). More detailed results are in Appendix [B.](#page-11-0) When DARE's performance drops below 90% at a 90% pruning rate, our method offers a viable alternative.

 The Variants of DP As shown in Table [6,](#page-6-0) change_sig disregards parameter magnitude, con- sidering only the number of parameters for sig-**nificance, while w/o fac ignores effects of** $fac(\cdot)$ **.** Removing the parameter importance causes a sig- nificant performance drop, while the tuning factor has a minor effect.

 The Generality of DPA Our experimental re- sults are in Table [7.](#page-6-1) We tested the DPA method on DARE and OWL. Since DARE already amplifies parameters significantly at high pruning rates (5x for 80% and 10x for 90%), we switched to dynamic reduction. Since Owl is similar to the DP method,

Methods	Math	Fin
DPPA	86.85	92.11
DARE	73.44	82.90
w/DPA	83.63	85.08
OWL	54.09	56.74
w/DPA	84.24	87.56

Table 7: Domain-Ratio of DARE and OWL using DPA at a pruning rate of 90%.

Domains	Method 1	Method 2
Math	88.45	97.08
Fin	96.65	94.89

Table 8: Domain-Ratio of two method in DPA at a pruning rate of 80%.

its performance with DPA surpasses DARE's. **436**

Initialization methods We show a performance 437 comparison of the two initialization methods at **438** 80% pruning rate in Table [8.](#page-6-2) For models with **439** small performance differences, use method 1; for 440 large differences, use method 2, which offers more **441** significant improvement. **442**

why DPPA is effective? To investigate, we ana- **443** lyzed the Delta parameters (see Fig [3\)](#page-6-3), exploring **444** the relationship between remaining parameters af- **445** ter DP at different pruning rates and linear layers. **446** The graph shows that, despite being an unstruc- **447** tured pruning method, DP exhibits aspects of struc- **448** tured pruning at high pruning rates. This dimension **449** partitioning aids in interpreting parameter space **450** distribution within specific domains. Using DPA, **451** we amplify parameters, strengthen domain-specific **452** weights in these dimensions, and restore certain **453** capabilities. **454**

Method & Pruning Rate	Math	Fin	Law
DARE 90%	7.89	51.48	53.86
DPPA 90%	89.95	85.24	122.08
DARE 80%	32.61	74.49	78.11
DPPA 80%	91.28	95.20	146.23

Table 9: Domain-Ratio of the model that combines domains mathematics, finance and law.

 Mergeing more Domain In Table [9,](#page-7-1) we present the merging results for adding law domains. Com- paring this with Table [3,](#page-5-1) it is evident that integrat- ing a fine-tuned model from an additional domain greatly degrades DARE's performance. Conversely, our method maintains comparable performance de- spite the extra domain, though performance de- creases at varying pruning rates. This result is ex- pected, as parameter conflicts during model merg- ing typically cause performance degradation. Rel- evant information about the added law domain is placed in Appendix [C.](#page-11-1)

⁴⁶⁷ 5 Related Work

468 5.1 Pruning Techniques

 Traditional pruning techniques aim to reduce model parameters [\(Zhu et al.,](#page-10-8) [2023\)](#page-10-8). Although extensively [s](#page-9-7)tudied [\(Hubara et al.,](#page-8-9) [2021;](#page-8-9) [Mozer and Smolen-](#page-9-7) [sky,](#page-9-7) [1988;](#page-9-7) [Han et al.,](#page-8-10) [2015a;](#page-8-10) [Lin et al.,](#page-9-8) [2019\)](#page-9-8), progress has been slow with large language mod- els due to the significant fine-tuning data required. LORA fine-tuning [\(Ma et al.,](#page-9-9) [2023\)](#page-9-9) was proposed to restore performance. Newer methods avoid fine- tuning: SparseGPT [\(Frantar and Alistarh,](#page-8-3) [2023\)](#page-8-3) uses the Hessian matrix for pruning and weight [u](#page-9-2)pdates to reduce reconstruction error, Wanda [\(Sun](#page-9-2) [et al.,](#page-9-2) [2023\)](#page-9-2) combines weight magnitudes and input activations, DSOT [\(Zhang et al.,](#page-10-9) [2023c\)](#page-10-9) adjusts pa- [r](#page-10-6)ameters to minimize discrepancies, and OWL [\(Yin](#page-10-6) [et al.,](#page-10-6) [2023\)](#page-10-6) introduces non-uniform layered spar-sity for higher pruning rates.

485 5.2 Special Domain Fine-Tuning

 This trend continues with large language models, leading to domain-specific models in fields like cod- ing [\(Rozière et al.,](#page-9-0) [2023;](#page-9-0) [Yu et al.,](#page-10-10) [2023c;](#page-10-10) [Luo et al.,](#page-9-10) [2023b\)](#page-9-10), mathematics [\(Luo et al.,](#page-9-11) [2023a;](#page-9-11) [Yue et al.,](#page-10-11) [2023;](#page-10-11) [Yu et al.,](#page-10-12) [2023a;](#page-10-12) [Gou et al.,](#page-8-11) [2023;](#page-8-11) [Yuan et al.,](#page-10-13) [2023\)](#page-10-13), medicine [\(Kweon et al.,](#page-9-12) [2023;](#page-9-12) [Chen et al.,](#page-8-12) [2023;](#page-8-12) [Toma et al.,](#page-9-13) [2023\)](#page-9-13), and finance [\(Zhang et al.,](#page-10-14) [2023a;](#page-10-14) [Yang et al.,](#page-10-15) [2023b;](#page-10-15) [Xie et al.,](#page-10-16) [2023\)](#page-10-16). How-ever, fine-tuning across multiple domains demands

significant computational resources, prompting in- **495** terest in model merging methods. **496**

5.3 Model Merge **497**

[M](#page-9-14)odel merging methods include alignment [\(Li](#page-9-14) **498** [et al.,](#page-9-14) [2016\)](#page-9-14), model ensemble [\(Pathak et al.,](#page-9-15) [2010\)](#page-9-15), **499** module connection [\(Freeman and Bruna,](#page-8-13) [2017\)](#page-8-13), **500** and weight averaging [\(Wang et al.,](#page-10-17) [2020\)](#page-10-17). Of these, 501 only weight averaging reduces model parameters. **502** Approaches within weight averaging include sub- **503** [s](#page-8-14)pace weight averaging [\(Li et al.,](#page-9-16) [2023\)](#page-9-16), SWA [\(Iz-](#page-8-14) 504 [mailov et al.,](#page-8-14) [2018\)](#page-8-14), and task arithmetic [\(Ilharco](#page-8-15) 505 [et al.,](#page-8-15) [2023\)](#page-8-15). Task arithmetic is notable as it in- **506** volves domain-specific offsets added or subtracted **507** from base model weights. Further developments **508** in task arithmetic focus on LORA [\(Zhang et al.,](#page-10-18) **509** [2023b;](#page-10-18) [Chitale et al.,](#page-8-16) [2023;](#page-8-16) [Chronopoulou et al.,](#page-8-17) **510** [2023\)](#page-8-17) and minimizing parameter conflicts via scal- **511** [i](#page-10-1)ng coefficients [\(Ortiz-Jiménez et al.,](#page-9-17) [2023;](#page-9-17) [Yang](#page-10-1) **512** [et al.,](#page-10-1) [2023a;](#page-10-1) [Yadav et al.,](#page-10-2) [2023b;](#page-10-2) [Stoica et al.,](#page-9-18) **513** [2023\)](#page-9-18), selective weight retention [\(Yadav et al.,](#page-10-3) **514** [2023a\)](#page-10-3), and vector space adjustments [\(Jin et al.,](#page-9-4) **515** [2023\)](#page-9-4). **516**

5.4 Federated Learning **517**

Federated learning allows multiple clients to collab- **518** oratively train models under a central aggregator, **519** preserving data privacy [\(Zhang et al.,](#page-10-19) [2021\)](#page-10-19). This **520** setup aligns well with model merging, as it com- **521** bines locally trained models without risking data **522** leakage. **523**

6 Conclusions **⁵²⁴**

In this study, we introduce a pruning method called **525** DP, which is an improved approach based on mag- **526** nitude pruning to enhance performance at higher **527** pruning rates. Subsequently, we propose DPA, **528** which focuses on dynamically amplifying parti- 529 tions of parameters based on their varying levels of **530** significance. Using DPPA, we address the chal- 531 lenge of model merging in complex fine-tuned **532** models. The experimental results show that our **533** approach only keep 20% of the specific domain pa- **534** rameters, while achieves comparable performance **535** to other methods that retain 90% of the specific **536** domain parameters. Furthermore, our method also **537** achieves a significant improvement of nearly 20% **538** in model merging. Through parametric analysis, **539** we explain DPPA's effectiveness and investigate **540** how increasing the number of domains affects **541** model performance. **542**

⁵⁴³ Limitations

544 Our method performs less effectively than DARE **545** on fine-tuned models with minimal differences **546** compared to the original model.

547 DAP requires a longer time to find the optimal **548** ratio.

549 While it mitigates parameter conflicts in model **550** merging, there remains the issue of performance **551** degradation.

⁵⁵² References

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A Main Result of Various Pruning **⁸⁷⁰ Methods on Specific Tasks** 871

We presented all pruning results of Llama-based **872** model in Table [13](#page-12-0) and Mistral-based model in Ta- **873** ble [11.](#page-11-2) The table displays the performance of two 874

Sparse ratio	Magnitude	OWL	DP	DARE
gsm8k				
0.1	0.806671721	0.806671721	0.804397271	0.806887854
0.2	0.806671721	0.805155421	0.803639121	0.805155421
0.3	0.805155421	0.808188021	0.808188021	0.806671721
0.4	0.806671721	0.807429871	0.808188021	0.803639121
0.5	0.794541319	0.80288097	0.79681577	0.805913571
0.6	0.785443518	0.782410917	0.784685368	0.809704321
0.7	0.761182714	0.762699014	0.760424564	0.780136467
0.8	0.747536012	0.746019712	0.746777862	0.765432321
0.9	0.686125853	0.674753601	0.683093252	0.716461463
MATH				
0.1	0.2930	0.2932	0.2930	0.2936
0.2	0.2916	0.2916	0.2910	0.2924
0.3	0.2938	0.2936	0.2926	0.2944
0.4	0.2982	0.2964	0.2968	0.2932
0.5	0.2948	0.2954	0.2946	0.2966
0.6	0.2900	0.2950	0.2934	0.2958
0.7	0.2866	0.2876	0.2902	0.2914
0.8	0.2782	0.2732	0.2746	0.2826
0.9	0.2290	0.2254	0.2250	0.2508

Table 10: The offset of different models from the base model at different position proportions.

Table 11: All pruning result for Abel-Mistral model in math domain.

875 llama2-based models in their respective domains, **876** including DP performance and DPA search results **877** in various domains.

 We show the factor of DPA and the correspond- ing results on each dataset. For Abel-Llama, the amplification factor is 1.3 for 80% and 1.1 for 90% of the partitions; for gsm8k is 0.5716, for Math is 0.1282. For Finance-Llama, the factor is 1.0 for 80% and 1.1 for 90% of the partitions; for FiQA_SA is 0.646808511, for FPB is 0.684536082. For Abel-Mistral, the factor is 1.0 for 80% and 1.7 for 90% of the partitions; for gsm8k is 0.7870, for Math is 0.3024.

888 And, we show the numerical results after the **889** Merging of each method as shown in the Table [12.](#page-12-1)

890 **B** The Offset of Models

891 We presented ten different percentage values in **892** Table [10.](#page-11-3)

⁸⁹³ C Law

 Our method achieves performance close to the dense model but may fall short for tasks requir- ing superior performance. Interestingly, in the law domain, pruned models significantly outperformed the dense model, achieving 120-140% of its per- **898** formance at pruning rates of 10-90%. We attribute **899** this to the low performance of the law domain fine- **900** tune model and the potential enhancement from **901** offsetting a local minimum through pruning. **902**

Methods	GSM8k	MATH	FiOA SA	FPB
Model Soups	0.121304018	0.0164	0.544680851	0.549484536
LM-Cocktail	0.473843821	0.0972	0.527659574	0.557731959
Ties-Merging	0.576952236	0.1248	0.208510638	0.111340206
w/Wanda	0.039423805	0.0136	0.132471678	0.169123487
w/SparseGPT	0.062816479	0.0528	0.12158879	0.134876196
w/DARE 90%	0.154662623	0.0224	0.455319149	0.43814433
w/DPPA 90%	0.557998484	0.111	0.591489362	0.505154639
$w/DARE$ 80%	0.392721759	0.0676	0.523404255	0.539175258
w/DPPA 80%	0.577710387	0.1158	0.663829787	0.650515464

Table 12: The specific performance values of the merged Llama model that combines domains mathematics and finance.

Sparse ratio	Magnitude	OWL	DP	DARE
gsm8k				
0.1	0.59893859	0.595905989	0.589082638	0.587566338
0.2	0.593631539	0.592873389	0.59893859	0.585291888
0.3	0.590598939	0.589082638	0.594389689	0.586808188
0.4	0.578468537	0.579984837	0.588324488	0.567096285
0.5	0.584533738	0.589840788	0.587566338	0.563305534
0.6	0.578468537	0.574677786	0.570128886	0.557240334
0.7	0.546626232	0.542835481	0.545109932	0.558756634
0.8	0.501137225	0.495072024	0.489006823	0.53525398
0.9	0.343442002	0.342683851	0.351781653	0.498104625
MATH				
0.1	0.1208	0.122	0.129	0.1236
0.2	0.1218	0.1212	0.1232	0.1298
0.3	0.125	0.1232	0.1238	0.1274
0.4	0.1262	0.1258	0.1276	0.1264
0.5	0.122	0.125	0.1248	0.1216
0.6	0.1254	0.124	0.1194	0.1184
0.7	0.1176	0.1148	0.1142	0.1134
0.8	0.0996	0.0934	0.095	0.111
0.9	0.0646	0.0664	0.0668	0.0842
FiQA_SA				
0.1	0.608510638	0.595744681	0.635744681	0.629787234
0.2	0.612765957	0.642553191	0.629787234	0.621276596
0.3	0.629787234	0.646808511	0.621276596	0.634042553
0.4	0.629787234	0.621276596	0.629787234	0.625531915
0.5	0.582978723	0.561702128	0.34893617	0.561702128
0.6	0.595744681	0.540425532	0.54893617	0.685106383
0.7	0.540425532	0.510638298	0.195744681	0.587234043
0.8	0.519148936	0.557446809	0.493617021	0.570212766
0.9	0.365957447	0.395744681	0.438297872	0.574468085
FPB				
0.1	0.642268041	0.631958763	0.62556701	0.62371134
0.2	0.620618557	0.616494845	0.611340206	0.634020619
0.3	0.597938144	0.608247423	0.628865979	0.627835052
0.4	0.610309278	0.609278351	0.601030928	0.644329897
0.5	0.590721649	0.57628866	0.605154639	0.611340206
0.6	0.597938144	0.579381443	0.579381443	0.615463918
0.7	0.534020619	0.550515464	0.537113402	0.607216495
0.8	0.460824742	0.477319588	0.471134021	0.586597938
0.9	0.387628866	0.38556701	0.416494845	0.567010309

Table 13: All pruning result for Llama-based model in two domain.