
Imprecise Label Learning: A Unified Framework for Learning with Various Imprecise Label Configurations

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Abstract

Learning with reduced labeling standards, such as noisy label, partial label, and supplementary unlabeled data, which we generically refer to as *imprecise* label, is a commonplace challenge in machine learning tasks. Previous methods tend to propose specific designs for every emerging imprecise label configuration, which is usually unsustainable when multiple configurations of imprecision co-exist. In this paper, we introduce imprecise label learning (ILL), a framework for the unification of learning with various imprecise label configurations. ILL leverages expectation-maximization (EM) for modeling the imprecise label information, treating the precise labels as latent variables. Instead of approximating the correct labels for training, it considers the entire distribution of all possible labeling entailed by the imprecise information. We demonstrate that ILL can seamlessly adapt to partial label learning, semi-supervised learning, noisy label learning, and, more importantly, a mixture of these settings, with closed-form learning objectives derived from the unified EM modeling. Notably, ILL surpasses the existing specified techniques for handling imprecise labels, marking the first practical and unified framework with robust and effective performance across various challenging settings. We hope our work will inspire further research on this topic, unleashing the full potential of ILL in wider scenarios where precise labels are expensive and complicated to obtain. Code is available at: <https://github.com/Hhhhhhao/General-Framework-Weak-Supervision>.

1 Introduction

One of the critical challenges in machine learning is the collection of annotated data for model training [1–6]. Ideally, every data instance would be fully annotated with precise labels. However, collecting such data can be expensive, time-consuming, and error-prone. Often, the labels can be intrinsically difficult to ascertain precisely. Factors such as a lack of annotator expertise and privacy concerns can also negatively affect the quality and completeness of the annotations.

In an attempt to circumvent this limitation, several methods have been proposed to permit model learning from the data annotated with reduced labeling standards, which are generally easier to obtain. We will refer to such labels as *imprecise*. Fig. 1 illustrates some typical mechanisms of label imprecision that are commonly addressed in the literature. Label imprecision requires a modification of the standard supervised training mechanism to build models for each specific case. For instance, *partial label learning* (PLL) [7–13] allows instances to have a set of candidate labels, instead of a single definitive one. *Semi-supervised Learning* (SSL) [14–23] seeks to enhance the generalization ability when only a small set of labeled data is available, supplemented by a larger unlabeled set.

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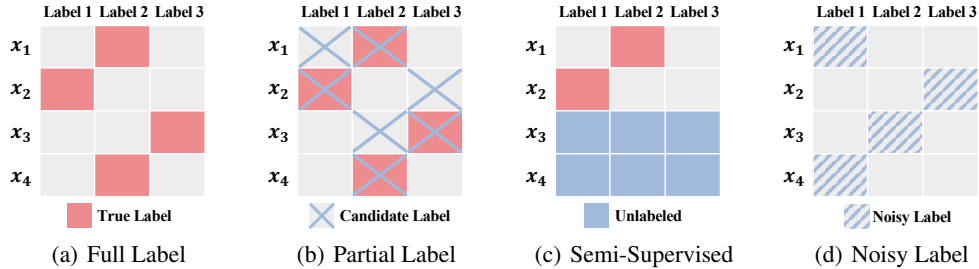


Figure 1: Illustration of the full label and imprecise label configurations. We use an example dataset of 4 training instances and 3 classes. (a) Full label, the annotation is a single true label; (b) Partial label, the annotation is a label candidate set containing true label; (c) Semi-supervised, only part of the dataset is labeled, and the others are unlabeled; (d) Noisy label, the annotation is mislabeled.

Noisy label learning (NLL) [24–37] deals with noisy scenarios where the labels are corrupted or incorrect. There is a greater variety of other forms of label imprecision, including crowd-sourcing [38, 39], programmable weak supervision [40, 41], and bag-level supervision [42–47], among others.

While prior arts have demonstrated success in handling individual configurations of label imprecision, their approaches often differ substantially. They are tailored to a *specific* form of imprecision, as depicted in Fig. 2. Such specificity not only imposes the necessity of devising a solution for emerging types of label imprecision scenarios, but also complicates the deployment in practical settings, where the annotations can be highly complex and may involve *multiple coexisting and interleaved* imprecision configurations. For instance, considering a scenario where both noisy labels and partial labels appear together, it might be challenging to adapt previous methods in NLL or PLL to this scenario since they either rely on the assumption of definite labels [39] or the existence of the correct label among label candidates [48], thus requiring additional algorithmic design. In fact, a few recent works have attempted to address the combinations of imprecise labels in this way, such as partial noisy label [49, 50] and semi-supervised partial label learning [51, 52]. However, simply utilizing a more sophisticated or ad-hoc design can hardly scale to other settings. In addition, most of these approaches attempt to infer the correct labels given the imprecise information (*e.g.* through consistency with adjacent data [14, 53, 54], iterative refinement [55, 56], average over given labels [57, 58], etc., to train the model, which inevitably accumulates error during training.

In this paper, we formulate the problem from a different perspective: rather than taking the imprecise label information provided as a potentially noisy or incomplete attempt at assigning labels to instances, we treat it generically as the information that imposes a deterministic or statistical restriction of the actual applicable true labels. We then train the model over the distribution of all possible labeling entailed by the given imprecise information. More specifically, for a dataset with samples X and imprecise label information I , we treat the inaccessible full and precise labels Y as a latent variable. The model is then trained to maximize the likelihood of the provided information I . Since the likelihood computed over the joint probability $P(X, I, Y; \theta) = \sum_Y P(X, I, Y; \theta)$ must marginalize out Y , the actual information I provided could permit a potentially exponential number of labeling. To deal with the resulting challenge of maximizing the logarithm of an expectation, we use the common approach of *expectation-maximization* (EM) [59], where the E-step computes the expectation of $P(X, I, Y; \theta)$ given the posterior of current belief $P(Y|X, I; \theta^t)$ at time step t and the M-step maximizes the tight variational lower bound over $P(X, I; \theta)$. The overall framework is thus largely agnostic to the various nature of label imprecision, with the imprecise label only affecting the manner in which the posterior $P(Y|X, I; \theta^t)$ is computed. In fact, current approaches designed for various imprecise label scenarios can be treated as specific instances of our framework. Our approach can serve as a solution towards a *unified and generalized* view for learning with *various* imprecise labels.

While there exist earlier attempts on generalized or EM solutions for different (other) imprecise supervisions or fuzzy observations [60–64, 45, 65–67], they usually require additional assumptions and approximations on the imprecise information for learnability [48, 68], thus presenting limited scalability on practical settings [62]. On the contrary, the unified framework we propose subsumes all of these and naturally extends to the more practical “mixed” style of data, where different types of imprecise labels coexist. Moreover, for noisy labels, our framework inherently enables the learning of a *noise model*, as we will show in Section 3.2. Through comprehensive experiments, we demonstrate that the proposed imprecise label learning (ILL) framework not only outperforms previous methods

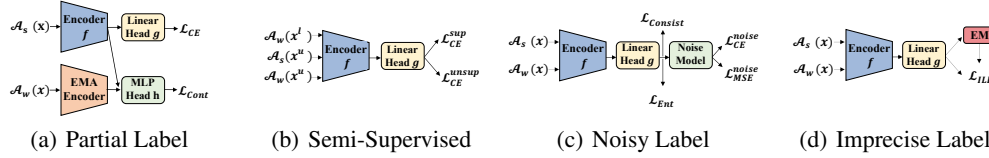


Figure 2: Baseline model pipelines for various imprecise label configurations. (a) PiCO [13] for partial label learning. (b) FixMatch [18] for semi-supervised learning. (c) SOP [69] for noisy label learning. (d) The proposed unified framework. It accommodates *any* imprecise label configurations and also mixed imprecise labels with an EM formulation.

for dealing with single imprecise labels of PLL, NLL, and SSL, but also presents robustness and effectiveness for mixed imprecise label learning (MILL) settings, leveraging the full potential to more challenging scenarios. Our contributions are summarized as follows:

- We propose an EM framework towards the unification of learning from *various* imprecise labels.
- We establish scalable and consistent state-of-the-art (SOTA) performance with the proposed method on partial label learning, semi-supervised learning, and noisy label learning, demonstrating our method’s robustness in more diverse, complex label noise scenarios.
- To the best of our knowledge, our work is the first to show the robustness and effectiveness of a single unified method for handling the mixture of various imprecise labels.

2 Preliminary

In this section, we illustrate the notations and baselines from different imprecise label settings that adopt various solutions. We will show later how our proposed method generalize and subsume these prior arts. Let \mathcal{X} denote the input space, and $\mathcal{Y} = [C] := \{1, \dots, C\}$ represent the label space with C distinct labels. A fully annotated training dataset of size N is represented as $\mathcal{D} = \{(\mathbf{x}_i, y_i)\}_{i \in [N]}$. Learning with imprecise labels involves approximating the mapping function $f \circ g : \mathcal{X} \rightarrow \mathcal{Y}$ from a training dataset where the true label y is not fully revealed from the annotation process. Here f is the backbone for feature extraction, g refers to the classifier built on top of the features, and the output from $f \circ g$ is the predicted probability $\mathbf{p}(y|\mathbf{x}; \theta)$, where θ is the learnable parameter for $f \circ g$. In this study, we primarily consider three imprecise label configurations (as illustrated in Fig. 1) and their corresponding representative learning paradigms (as shown in Fig. 2), namely partial label learning, semi-supervised learning, and noisy label learning.

Partial label learning (PLL). PLL aims to learn with a candidate label set $\mathbf{s} \subset \mathcal{Y}$, where the ground truth label $y \in \mathcal{Y}$ is concealed in \mathbf{s} . The training data for partial labels thus becomes $\mathcal{D}_{\text{PLL}} = \{(\mathbf{x}_i, \mathbf{s}_i)\}_{i \in [N]}$. PiCO [13] is a recent contrastive method that employs class prototypes to enhance label disambiguation (as shown in Fig. 2(a)). It optimizes the cross-entropy (CE)² loss between the prediction of the augmented training sample $\mathcal{A}_w(\mathbf{x})$ and the disambiguated labels $\hat{\mathbf{s}}$. PiCO learns a set of class prototypes from the features associated with the same pseudo-targets. A contrastive loss, based on MOCO [70], is employed to better learn the feature space, drawing the projected and normalized features \mathbf{z}_w and \mathbf{z}_s of the two augmented versions of data $\mathcal{A}_w(\mathbf{x})$ and $\mathcal{A}_s(\mathbf{x})$ ³ closer. The objective of PiCO is formulated as:

$$\mathcal{L}_{\text{PiCO}} = \mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathcal{A}_w(\mathbf{x}); \theta), \hat{\mathbf{s}}) + \mathcal{L}_{\text{Cont}}(\mathbf{z}_w, \mathbf{z}_s, \mathcal{M}). \quad (1)$$

Semi-supervised learning (SSL). For SSL, we can define the labeled dataset as $\mathcal{D}_{\text{SSL}}^L = \{(\mathbf{x}_i^l, y_i^l)\}_{i \in [N^L]}$, and the unlabeled dataset as $\mathcal{D}^U = \{\mathbf{x}_j^u\}_{j \in [N^L+1, N^L+N^U]}$, with $N^L \ll N^U$. A general confidence-thresholding based self-training [53, 18] pipeline for SSL is shown in Fig. 2(b). Consider FixMatch [18] as an example; there are usually two loss components: the supervised CE loss on labeled data and the unsupervised CE loss on unlabeled data. For the unsupervised objective, the pseudo-labels \hat{y}^u from the network itself are used to train on the unlabeled data. A “strong-weak” augmentation [53] is commonly adopted. To ensure the quality of the pseudo-labels,

²For simplicity, we use \mathcal{L}_{CE} for labels of the formats of class indices, one-hot vectors, and class probabilities.

³We use \mathcal{A}_w to indicate the weaker data augmentation and \mathcal{A}_s to indicate the stronger data augmentation.

only the pseudo-labels whose confidence scores \hat{p}^u are greater than a threshold τ are selected to participate in training:

$$\mathcal{L}_{\text{Fix}} = \mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathcal{A}_w(\mathbf{x}^l); \theta), y^l) + \mathbb{1}(\hat{p}^u \geq \tau) \mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathcal{A}_s(\mathbf{x}^u); \theta), \hat{y}^u). \quad (2)$$

Noisy label learning (NLL). NLL aims at learning with a dataset of corrupted labels, $\mathcal{D}_{\text{NLL}} = \{(\mathbf{x}_i, \hat{y}_i)\}_{i \in [N]}$. We illustrate the NLL pipeline (in Fig. 2(c)) with the recent sparse over-parameterization (SOP) model [69], where a sparse *noise model* consisting of parameters $\mathbf{u}_i, \mathbf{v}_i \in [-1, 1]^C$ for each sample is adopted. The noise model transforms the network prediction from the true label distribution into the noisy label distribution. A CE loss and a mean-squared-error (MSE) loss optimize parameter $\{\mathbf{u}_i\}$ and $\{\mathbf{v}_i\}$ respectively:

$$\mathcal{L}_{\text{SOP}} = \mathcal{L}_{\text{CE}}(\phi(\mathbf{p}(y|\mathcal{A}_w(\mathbf{x}); \theta) + \mathbf{m}), \hat{y}) + \mathcal{L}_{\text{MSE}}(\mathbf{p}(y|\mathcal{A}_w(\mathbf{x}); \theta) + \mathbf{m}, \hat{y}), \quad (3)$$

where ϕ denotes the L_∞ normalization and $\mathbf{m}_i = \mathbf{u}_i \odot \mathbf{u}_i \odot \hat{\mathbf{y}}_i^{\text{oh}} - \mathbf{v}_i \odot \mathbf{v}_i \odot (1 - \hat{\mathbf{y}}_i^{\text{oh}})$, with $\hat{\mathbf{y}}_i^{\text{oh}}$ referring to the one-hot version of y_i . Consistency regularization with strong-weak augmentation and entropy class-balance regularization are additionally utilized for better performance in SOP [69].

3 Imprecise Label Learning

Although current techniques demonstrate potential in addressing particular forms of imprecise labels, they frequently fall short in adaptability and transferability to more complicated and more realistic scenarios where multiple imprecise label types coexist and interleave. This section first defines the proposed expectation-maximization (EM) formulation for learning with various imprecise labels. Then, we demonstrate that our unified framework seamlessly extends to partial label learning, semi-supervised label learning, noisy label learning, and the more challenging setting of mixed imprecise label learning. Connections and generalization to previous pipelines can also be drawn clearly under the proposed EM framework.

3.1 A Unified Framework for Learning with Imprecise Labels

Exploiting information from imprecise labels. The challenge of learning with imprecise labels lies in learning effectively with inaccurate or incomplete annotation information. Per the analysis above, prior works catering to specific individual imprecise labels either explicitly or implicitly attempt to infer the precise labels from the imprecise label information. For example, partial label learning concentrates on the disambiguation of the ground truth label from the label candidates [13, 71, 50] or averaging equally over the label candidates [72]. In semi-supervised learning, after the model initially learns from the labeled data, the pseudo-labels are treated as correct labels and utilized to conduct self-training on the unlabeled data [73, 18]. Similarly, for noisy label learning, an integral part that helps mitigate overfitting to random noise is the implementation of an accurate noise model capable of identifying and rectifying the incorrect labels [33, 69], thereby ensuring the reliability of the learning process. However, inferring the correct labels from the imprecise labels or utilizing the imprecise labels directly can be very challenging and usually leads to errors accumulated during training [73, 74], which is also known as the confirmation bias. In this work, we take a different approach: we consider all possible labeling along with their likelihood that the imprecise labels fulfill to train the model, rather than using a single rectified label from the imprecise information. Such an approach also eliminates the requirements for designing different methods for various imprecise labels and provides a unified formulation instead, where closed-form solutions can be derived.

A unified framework for learning with imprecise labels (ILL). Let $\{\mathbf{x}_i\}_{i \in [N]}$ represent the features as realizations from X and $\{y_i\}_{i \in [N]}$ represent their precise labels as realizations from Y for the training data. Ideally, Y would be fully specified for X . In the imprecise label scenario, however, Y is not provided; instead we obtain imprecise label information I . We view I not as *labels*, but more abstractly as a variable representing the *information* about the labels. From this perspective, the actual labels Y would have a distribution $P(Y|I)$, and I can present in various forms. When the information I provided is the precise true label of the data, $P(Y|I)$ would be a delta distribution, taking a value 1 at the true label, and 0 elsewhere. If I represents partial labels, then $P(Y|I)$ would have non-zero value over the candidate labels, and be 0 elsewhere. When I represents a set of noisy labels, $P(Y|I)$ would represent the distribution of the true labels, given the noisy labels. When I does not contain any information, i.e., unlabeled data, Y can take any value.

By the maximum likelihood estimation (MLE) principle, we must estimate the model to maximize the likelihood of the data/information we have been provided, namely X and I . Let $P(X, I; \theta)$ represent a parametric form for the joint distribution of X and I ⁴. Explicitly considering the labels Y , we have $P(X, I; \theta) = \sum_Y P(X, Y, I; \theta)$. The maximum likelihood principle requires us to find:

$$\theta^* = \arg \max_{\theta} \log P(X, I; \theta) = \arg \max_{\theta} \log \sum_Y P(X, Y, I; \theta), \quad (4)$$

with θ^* denotes the optimal value of θ . Eq. (4) features the log of an expectation and cannot generally be solved in closed-form, and requires iterative hill-climbing solutions. Of these, arguably the most popular is the expectation-maximization (EM) algorithm [59], which iteratively maximizes a tight variational lower bound on the log-likelihood. In our case, applying it becomes:

$$\begin{aligned} \theta^{t+1} &= \arg \max_{\theta} \mathbb{E}_{Y|X, I; \theta^t} [\log P(X, Y, I; \theta)] \\ &= \arg \max_{\theta} \mathbb{E}_{Y|X, I; \theta^t} [\log P(Y|X; \theta) + \log P(I|X, Y; \theta)], \end{aligned} \quad (5)$$

where θ^t is the t^{th} estimate of the optimal θ . Note that $P(X; \theta)$ is omitted from Eq. (5) since $P(X)$ does not rely on θ . The detailed derivation of the variational lower bound is shown in Appendix C.1. There are several implications from Eq. (5). (i) The expectation over the posterior $P(Y|X, I; \theta^t)$ equates to considering *all* labeling entailed by the imprecise label information I , rather than any single (possibly corrected) choice of label. For independent instances setting mostly studied in this paper, we can derive closed-form training objectives from this formulation as shown in Section 3.2. (ii) The property of the second term $\log P(I|X, Y; \theta)$ is dependent on the nature of imprecise label I . If I is derivable from true labels Y , such as the actual labels or the label candidates, it can be reduced to $P(I|Y)$, *i.e.*, the probability of I is no longer dependent on X or θ and thus can be ignored from Eq. (5). If I represents the noisy labels, $P(I|X, Y; \theta)$ instead includes a potentially learnable noise model. (iii) It is a general framework towards the unification of any label configuration, including full labels, partial labels, low-resource labels, noisy labels, etc. In this work, we specialize the proposed EM framework to PLL, SSL, NLL, and the mixture of them in the following.

3.2 Instantiating the Unified EM Formulation

We illustrate how to seamlessly expand the formulation from Eq. (5) to partial label learning, semi-supervised learning, noisy label learning, and mixture settings, with derived closed-form loss function⁵ for each setting here. The actual imprecise labels only affect the manner in which the posterior $P(Y|X, I; \theta^t)$ is computed for each setting. We show that all learning objectives derived from Eq. (5) naturally include a consistency term with the posterior as the soft target. We also demonstrate that the proposed unified EM framework closely connects with the prior arts, which reveals the potential reason behind the success of these techniques. Note that while we only demonstrate the application of the proposed framework to four settings here, it can also be flexibly extended to other settings. More details of derivation below are shown in Appendix C.

Partial label learning (PLL). The imprecise label I for partial labels is defined as the label candidate sets S containing the true labels. These partial labels indicate that the posterior $P(Y|X, S; \theta^t)$ can only assign its masses on the candidate labels. Since S can be derived from true labels Y , $P(S|X, Y; \theta)$ reduces to $P(S|Y)$, and thus can be ignored. We also demonstrate with instance dependent partial labels that maintains $P(S|X, Y; \theta)$ in Appendix D.2.2. Defining the label candidates as $\{\mathbf{s}_i\}_{i \in [N]}$ and substituting it in Eq. (5), we have the loss function of PLL derived using ILL framework:

$$\mathcal{L}_{\text{ILL}}^{\text{PLL}} = - \sum_{Y \in [C]} P(Y|X, S; \theta^t) \log P(Y|X; \theta) \equiv \mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathcal{A}_s(\mathbf{x}); \theta), \mathbf{p}(y|\mathcal{A}_w(\mathbf{x}), \mathbf{s}; \theta^t)), \quad (6)$$

where $\mathbf{p}(y|\mathcal{A}_w(\mathbf{x}), \mathbf{s}; \theta^t)$ is the normalized probability that $\sum_{k \in C} p_k = 1$, and $p_k = 0, \forall k \in \mathbf{s}$. Eq. (6) corresponds exactly to consistency regularization [53], with the normalized predicted probability as the soft pseudo-targets. We use \mathcal{A}_s and \mathcal{A}_w to denote the strong and weak augmentation

⁴The actual parameters θ may apply only to some component such as $P(Y|X; \theta)$ of the overall distribution; we will nonetheless tag the entire distribution $P(X, I; \theta)$ with θ to indicate that it is dependent on θ overall.

⁵To formulate the loss function, we convert the problem to minimization of the negative log-likelihood.

as stated earlier. This realization on PLL shares similar insights as [12] which exploits a gradually induced loss weight for PLL on multiple augmentations of the data. However, our framework is much simpler and more concise as shown in Appendix D.2.2, which does not require additional techniques.

Semi-supervised learning (SSL) In SSL, the input X consists of the labeled data X^L and the unlabeled data X^U . The imprecise label for SSL is realized as the limited number of full labels Y^L for X^L . The labels Y^U for unlabeled X^U are unknown and become the latent variable. Interestingly, for the unlabeled data, there is no constraint on possible labels it can take. The posterior $P(Y^U|X^L, X^U, Y^L; \theta)$, which is the actual prediction from the network, can be directly utilized as soft targets for self-training. Since Y^L is conditionally independent with Y^U given X , the second term of Eq. (5): $P(Y^L|X^L, X^U, Y^U; \theta)$, is reduced to $P(Y^L|X^L; \theta)$, which corresponds to the supervised objective on labeled data. The loss function for SSL thus becomes:

$$\begin{aligned} \mathcal{L}_{\text{ILL}}^{\text{SSL}} &= - \sum_{Y \in [C]} P(Y^U|X^U, X^L, Y^L; \theta^t) \log P(Y^U|X^U, X^L; \theta) - \log P(Y^L|X^L; \theta) \\ &\equiv \mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathcal{A}_s(\mathbf{x}^u); \theta), \mathbf{p}(y|\mathcal{A}_w(\mathbf{x}^u); \theta^t)) + \mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathcal{A}_w(\mathbf{x}^l); \theta), y^l) \end{aligned} \quad (7)$$

The first term corresponds to the unsupervised consistency regularization usually employed in SSL, and the second term refers to the supervised CE loss only on labeled data. Eq. (7) has several advantages over the previous methods. It adopts the prediction as soft-targets of all possible labeling on unlabeled data, potentially circumventing the confirmation bias caused by pseudo-labeling and naturally utilizing all unlabeled data which resolves the quantity-quality trade-off commonly existing in SSL [18, 23]. It also indicates that previous pseudo-labeling with confidence threshold implicitly conducts the EM optimization, where the maximal probable prediction approximates the expectation, and the degree of the approximation is determined by the threshold τ , rationalizing the effectiveness of dynamic thresholding.

Noisy label learning (NLL). Things become more complicated here since the noisy labels \hat{Y} do not directly reveal the true information about Y , thus $P(\hat{Y}|Y, X; \theta)$ inherently involves a noise model that needs to be learned. We define a simplified instance-independent⁶ noise transition model $\mathcal{T}(\hat{Y}|Y; \omega)$ with parameters ω , and take a slightly different way to formulate the loss function for NLL from the ILL framework:

$$\begin{aligned} \mathcal{L}_{\text{ILL}}^{\text{NLL}} &= - \sum_{Y \in [C]} P(Y|X, \hat{Y}; \theta^t, \omega^t) \log P(Y|X, \hat{Y}; \theta, \omega) - \log P(\hat{Y}|X; \theta, \omega) \\ &\equiv \mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathcal{A}_s(\mathbf{x}), \hat{y}; \theta, \omega^t), \mathbf{p}(y|\mathcal{A}_w(\mathbf{x}), \hat{y}; \theta^t, \omega^t)) + \mathcal{L}_{\text{CE}}(\mathbf{p}(\hat{y}|\mathcal{A}_w(\mathbf{x}); \theta, \omega), \hat{y}), \end{aligned} \quad (8)$$

where the parameters ω and θ are learned end-to-end. The first term corresponds to the consistency regularization of prediction conditioned on noisy labels and the second term corresponds to the supervised loss on noisy predictions that are converted from the ground truth predictions. Both quantities are computed using the noise transition model given the noisy label \hat{y} :

$$\mathbf{p}(y|\mathbf{x}, \hat{y}; \theta, \omega^t) \propto \mathbf{p}(y|\mathbf{x}; \theta) \mathcal{T}(\hat{y}|y; \omega^t), \text{ and } \mathbf{p}(\hat{y}|\mathbf{x}; \theta, \omega) = \sum_{y \in [C]} \mathbf{p}(y|\mathbf{x}; \theta) \mathcal{T}(\hat{y}|y; \omega). \quad (9)$$

Mixture imprecise label learning (MILL). We additionally consider a more practical setting, mixture of imprecise label learning, with partial labels, noisy labels, and unlabeled data interleaved together. On the unlabeled data, the unsupervised objective is the same as the unsupervised consistency regularization of SSL as shown in Eq. (7). The labeled data here present partial and noisy labels \hat{s} . Thus the noisy supervised objective in Eq. (9) becomes the supervised consistency regularization as in Eq. (6) of partial label setting to train the noise transition model, and the noisy unsupervised objective becomes the consistency regularization of the prediction conditioned on noisy partial labels. Thus we have the loss function for MILL derived as:

$$\begin{aligned} \mathcal{L}_{\text{ILL}}^{\text{MILL}} &= \mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathcal{A}_s(\mathbf{x}^l), \hat{s}^l; \theta, \omega^t), \mathbf{p}(y|\mathcal{A}_w(\mathbf{x}^l), \hat{s}^l; \theta^t, \omega^t)) \\ &\quad + \mathcal{L}_{\text{CE}}(\mathbf{p}(\hat{y}|\mathcal{A}_w(\mathbf{x}^l); \theta, \omega), \hat{s}^l) \\ &\quad + \mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathcal{A}_s(\mathbf{x}^u); \theta), \mathbf{p}(y|\mathcal{A}_w(\mathbf{x}^u); \theta^t)) \end{aligned} \quad (10)$$

⁶A more complicated instance-dependent noise model $\mathcal{T}(\hat{Y}|Y, X; \omega)$ can also be formulated under our unified framework, but not considered in this work. Also, since we use \mathcal{T} both in forward fashion and backward fashion, it is unidentifiable in this work.

Table 1: Accuracy of different partial ratio q on CIFAR-10, CIFAR-100, and CUB-200 for **partial label learning**. The best and the second best results are indicated in **bold** and underline respectively.

Dataset	CIFAR-10			CIFAR-100			CUB-200
	0.1	0.3	0.5	0.01	0.05	0.1	0.05
Fully-Supervised	94.91±0.07			73.56±0.10			-
LWS [11]	90.30±0.60	88.99±1.43	86.16±0.85	65.78±0.02	59.56±0.33	53.53±0.08	39.74±0.47
PRODEN [55]	90.24±0.32	89.38±0.31	87.78±0.07	62.60±0.02	60.73±0.03	56.80±0.29	62.56±0.10
CC [9]	82.30±0.21	79.08±0.07	74.05±0.35	49.76±0.45	47.62±0.08	35.72±0.47	55.61±0.02
MSE [79]	79.97±0.45	75.65±0.28	67.09±0.66	49.17±0.05	46.02±1.82	43.81±0.49	22.07±2.36
EXP [79]	79.23±0.10	75.79±0.21	70.34±1.32	44.45±1.50	41.05±1.40	29.27±2.81	9.44±2.32
PiCO [13]	<u>94.39±0.18</u>	<u>94.18±0.12</u>	<u>93.58±0.06</u>	<u>73.09±0.34</u>	<u>72.74±0.30</u>	<u>69.91±0.24</u>	72.17±0.72
Ours	96.37±0.08	96.26±0.03	95.91±0.05	75.31±0.19	74.58±0.03	74.00±0.02	<u>70.77±0.29</u>

We can compute both quantity through the noise transition model:

$$\mathbf{p}(y|\mathbf{x}, \hat{\mathbf{s}}; \theta, \omega^t) \propto \mathbf{p}(y|\mathbf{x}; \theta) \prod_{\hat{y} \in \hat{\mathbf{s}}} \mathcal{T}(y|\hat{y}; \omega^t), \text{ and } \mathbf{p}(\hat{y}|\mathbf{x}; \theta, \omega) = \sum_{y \in [C]} \mathbf{p}(y|\mathbf{x}; \theta) \mathcal{T}(\hat{y}|y; \omega). \quad (11)$$

4 Experiments

In this section, we conduct extensive experiments to evaluate ILL. Albeit simple, the ILL framework achieves comparable state-of-the-art performance regarding previous methods on partial label learning, semi-supervised learning, and noisy label learning. Moreover, our experiments show that ILL could be easily extended to a more practical setting with a mixture of various imprecise label configurations. For all settings, we additionally adopt an entropy loss for balancing learned cluster sizes [75, 76], similarly as [69, 22]. Experiments are conducted with three runs using NVIDIA V100 GPUs.

4.1 Partial Label Learning

Setup. Following [13], we evaluate our method on partial label learning setting using CIFAR-10 [77], CIFAR-100 [77], and CUB-200 [78]. We generate partially labeled datasets by flipping negative labels to false positive labels with a probability q , denoted as a partial ratio. The $C - 1$ negative labels are then uniformly aggregated into the ground truth label to form a set of label candidates. We consider $q \in \{0.1, 0.3, 0.5\}$ for CIFAR-10, $q \in \{0.01, 0.05, 0.1\}$ for CIFAR-100, and $q = 0.05$ for CUB-200. We choose six baselines for PLL using ResNet-18 [1]: LWS [11], PRODEN [55], CC [9], MSE and EXP [79], and PiCO [13]. The detailed hyper-parameters, comparison with the more recent method R-CR [12] that utilizes a different training recipe and model [80], and comparison with instance-dependent partial labels [81] are shown in Appendix D.2.2.

Results. The results for PLL are shown in Table 1. Our method achieves the best performance compared to the baseline methods. Perhaps more surprisingly, on CIFAR-10 and CIFAR-100, our method even outperforms the fully-supervised reference, indicating the potential better generalization capability using the proposed framework, sharing similar insights as in Wu et al. [12]. While PiCO adopts a contrastive learning objective, our method still surpasses PiCO by an average of **2.13%** on CIFAR-10 and **2.72%** on CIFAR-100. Our approach can be further enhanced by incorporating contrastive learning objectives, potentially leading to more significant performance.

4.2 Semi-Supervised Learning

Setup. For experiments of SSL, we follow the training and evaluation protocols of USB [82] on image and text classification. To construct the labeled dataset for semi-supervised learning, we uniformly select l/C samples from each class and treat the remaining samples as the unlabeled dataset. We present the results on CIFAR-100 and STL-10 [77] for image classification, and IMDB [83] and Amazon Review [84] for text classification. We compare with the current methods with confidence thresholding, such as FixMatch [18], AdaMatch [85], FlexMatch [20], FreeMatch [22], and SoftMatch [23]. We also compare with methods with the contrastive loss, CoMatch [86] and SimMatch [87]. A full comparison of the USB datasets and hyper-parameters is shown in Appendix D.3.

Results. We present the results for SSL on Table 2. Although no individual SSL algorithm dominates the USB benchmark [82], our method still shows competitive performance. Notably, our method

Table 2: Error rate of different number of labels l on CIFAR-100, STL-10, IMDB, and Amazon Review datasets for **semi-supervised learning**.

Datasets	CIFAR-100		STL-10		IMDB		Amazon Review	
	200	400	40	100	20	100	250	1000
AdaMatch [85]	22.32±1.73	16.66±0.62	13.64±2.49	7.62±1.90	8.09±0.99	7.11±0.20	45.40±0.96	40.16±0.49
FixMatch [18]	29.60±0.90	19.56±0.52	16.15±1.89	8.11±0.68	7.72±0.33	7.33±0.13	47.61±0.83	43.05±0.54
FlexMatch [20]	26.76±1.12	18.24±0.36	14.40±3.11	8.17±0.78	7.82±0.77	7.41±0.38	45.73±1.60	42.25±0.33
CoMatch [86]	35.08±0.69	25.35±0.50	15.12±1.88	9.56±1.35	7.44±0.30	7.72±1.14	48.76±0.90	43.36±0.21
SimMatch [87]	23.78±1.08	17.06±0.78	11.77±3.20	7.55±1.86	7.93±0.55	7.08±0.33	45.91±0.95	42.21±0.30
FreeMatch [22]	21.40±0.30	15.65±0.26	12.73±3.22	8.52±0.53	8.94±0.21	7.95±0.45	46.41±0.60	42.64±0.06
SoftMatch [23]	22.67±1.32	16.84±0.66	13.55±3.16	7.84±1.72	7.76±0.58	7.97±0.72	45.29±0.95	42.21±0.20
Ours	<u>22.06±1.06</u>	<u>16.40±0.54</u>	11.09±0.71	8.10±1.02	7.32±0.12	7.64±0.67	43.96±0.32	42.32±0.02

Table 3: Accuracy of synthetic noise on CIFAR-10 and CIFAR-100 and instance noise on Clothing1M and WebVision for **noisy label learning**. We use noise ratio of $\{0.2, 0.5, 0.8\}$ for synthetic symmetric noise and 0.4 for asymmetric label noise. The instance noise ratio is unknown.

Dataset	CIFAR-10				CIFAR-100				Clothing1M	WebVision
	Sym.		Asym.		Sym.		Asym.		Ins.	Ins.
Noise Ratio η	0.2	0.5	0.8	0.4	0.2	0.5	0.8	0.4	-	-
CE	87.20	80.70	65.80	82.20	58.10	47.10	23.80	43.30	69.10	-
Mixup [90]	93.50	87.90	72.30	-	69.90	57.30	33.60	-	-	-
DivideMix [33]	96.10	94.60	93.20	93.40	77.10	74.60	60.20	72.10	74.26	77.32
ELR [32]	95.80	94.80	93.30	93.00	77.70	73.80	60.80	77.50	72.90	76.20
SOP [69]	96.30	95.50	94.00	93.80	78.80	75.90	63.30	78.00	73.50	76.60
Ours	96.78±0.11	96.60±0.15	94.31±0.07	94.75±0.81	77.49±0.28	<u>75.51±0.52</u>	66.46±0.72	75.82±1.89	<u>74.02±0.12</u>	79.37±0.09

performs best on STL-10 with 40 labels and Amazon Review with 250 labels, outperforming the previous best by **0.68%** and **1.33%**. In the other settings, the performance of our method is also very close to the best-performing methods. More remarkably, our method does not employ any thresholding, re-weighting, or contrastive techniques to achieve current results, demonstrating a significant potential to be further explored.

4.3 Noisy Label Learning

Setup. We conduct the experiments of NLL following SOP [69] on both synthetic symmetric/asymmetric noise on CIFAR-10 and CIFAR-100, and more realistic and larger-scale instance noise on Clothing1M [88], and WebVision [89]. To introduce the synthetic symmetric noise to CIFAR-10 and CIFAR-100, we uniformly flip labels for a probability η into other classes. For asymmetric noise, we only randomly flip the labels for particular pairs of classes. The introduced noise is then treated as ground truth labels to train the model. We mainly select three previous best methods as baselines: DivideMix [33]; ELR [32]; and SOP [69]. We also include the normal cross-entropy (CE) training and mixup [90] as baselines. More comparisons of other methods [91, 28] and on CIFAR-10N [92] with training details and more baselines [93, 28] are shown in Appendix D.4.

Results. We present the noisy label learning results in Table 3. The proposed method is comparable to the previous best methods. On synthetic noise of CIFAR-10, our method demonstrates the best performance on both symmetric noise and asymmetric noise. On CIFAR-100, our method generally produces similar results comparable to SOP. One may notice that our method shows inferior performance on asymmetric noise of CIFAR-100; we argue this is mainly due to the oversimplification of the noise transition model. Our method also achieves the best results on WebVision, outperforming the previous best by **2.05%**. On Clothing1M, our results are also very close to DivideMix, which trains for 80 epochs compared to 10 epochs in ours.

4.4 Mixed Imprecise Label Learning

Setup. We evaluate on CIFAR-10 and CIFAR-100 in a more challenging and realistic setting, the mixture of various imprecise label configurations, with unlabeled, partially labeled, and noisy labeled data existing simultaneously. We first sample the labeled dataset and treat other samples as the unlabeled. On the labeled dataset, we generate partial labels and randomly corrupt the true label of the partial labels. We set $l \in \{1000, 5000, 50000\}$ for CIFAR-10, and $l \in \{5000, 10000, 50000\}$ for

Table 4: Accuracy comparison of **mixture of different imprecise labels**. We report results of full labels, partial ratio q of 0.1 (0.01) and 0.3 (0.05) for CIFAR-10 (CIFAR-100), and noise ratio η of 0.1, 0.2, and 0.3 for CIFAR-10 and CIFAR-100.

Method	q	CIFAR-10, $l=50000$			q	CIFAR-100, $l=50000$		
		$\eta=0.1$	$\eta=0.2$	$\eta=0.3$		$\eta=0.1$	$\eta=0.2$	$\eta=0.3$
PiCO+ [94]	0.1	93.64	93.13	92.18	0.01	71.42	70.22	66.14
IRNet [71]		93.44	92.57	92.38		71.17	70.10	68.77
DALI [50]		94.15	94.04	93.77		72.26	71.98	71.04
PiCO+ Mixup [50]		94.58	94.74	94.43		75.04	74.31	71.79
DALI Mixup [50]		95.83	95.86	95.75		76.52	76.55	76.09
Ours		96.47\pm0.11	96.09\pm0.20	95.83\pm0.05		77.53\pm0.24	76.96\pm0.02	76.43\pm0.27
PiCO+ [94]	0.3	92.32	92.22	89.95	0.05	69.40	66.67	62.24
IRNet [71]		92.81	92.18	91.35		70.73	69.33	68.09
DALI [50]		93.44	93.25	92.42		72.28	71.35	70.05
PiCO+ Mixup [50]		94.02	94.03	92.94		73.06	71.37	67.56
DALI Mixup [50]		95.52	95.41	94.67		76.87	75.23	74.49
Ours		96.2\pm0.02	95.87\pm0.14	95.22\pm0.06		77.07\pm0.16	76.34\pm0.08	75.13\pm0.63

Table 5: Robust test accuracy results of our method on **more mixture of imprecise label configurations**. l , q and η are the number of labels, partial, and noise ratio.

l	q	CIFAR10				l	q	CIFAR100			
		$\eta=0.0$	$\eta=0.1$	$\eta=0.2$	$\eta=0.3$			$\eta=0.0$	$\eta=0.1$	$\eta=0.2$	$\eta=0.3$
5,000	0.1	95.29 \pm 0.18	93.90 \pm 0.11	92.02 \pm 0.22	89.02 \pm 0.63	10,000	0.01	69.90 \pm 0.23	68.74 \pm 0.15	66.87 \pm 0.34	65.34 \pm 0.02
	0.3	95.13 \pm 0.16	92.95 \pm 0.37	90.14 \pm 0.61	87.31 \pm 0.27		0.05	69.85 \pm 0.20	68.08 \pm 0.28	66.78 \pm 0.43	64.83 \pm 0.17
	0.5	95.04 \pm 0.10	92.18 \pm 0.52	88.39 \pm 0.62	83.09 \pm 0.56		0.10	68.92 \pm 0.45	67.15 \pm 0.63	64.44 \pm 1.29	60.26 \pm 1.96
1,000	0.1	94.48 \pm 0.09	91.68 \pm 0.17	87.17 \pm 0.51	81.04 \pm 1.13	5,000	0.01	65.66 \pm 0.27	63.13 \pm 0.27	60.93 \pm 0.17	58.36 \pm 0.56
	0.3	94.35 \pm 0.05	89.94 \pm 1.90	82.06 \pm 1.52	69.20 \pm 2.16		0.05	65.06 \pm 0.04	62.28 \pm 0.47	58.92 \pm 0.34	53.24 \pm 1.69
	0.5	93.92 \pm 0.29	86.34 \pm 2.37	70.86 \pm 2.78	38.19 \pm 6.55		0.10	63.32 \pm 0.55	58.73 \pm 1.33	53.27 \pm 1.57	46.19 \pm 1.04

CIFAR-100. For partial labels, we set $q \in \{0.1, 0.3, 0.5\}$ for CIFAR-10, and $q \in \{0.01, 0.05, 0.1\}$ for CIFAR-100. For noisy labels, we set $\eta \in \{0, 0.1, 0.2, 0.3\}$ for both datasets. Since there is no prior work that can handle all settings all at once, we compare on partial noisy label learning with PiCO+ [94], IRNet [71], and DALI [50]. Although there are also prior efforts on partial semi-supervised learning [51, 52], they do not scale on simple dataset even on CIFAR-10. Thus, we did not include them in comparison. We conduct additional validation of our method on more complex settings for partial noisy labels with unlabeled data to demonstrate its robustness to various imprecise labels.

Results. We report the comparison with partial noisy label learning methods in Table 4. Compared to previous methods, the proposed method achieves the best performance. Despite the simplicity, our method outperforms PiCO+ and DALI with mixup, showing the effectiveness of dealing with mixed imprecise labels. We also report the results of our methods on more mixed imprecise label configurations in Table 5. Our method demonstrates significant robustness against various settings of the size of labeled data, partial ratio, and noise ratio. Note that this is the first work that naturally deals with all three imprecise label configurations simultaneously, with superior performance than previous methods handling specific types or combinations of label configurations. This indicates the enormous potential of our work in realistic applications for handling more practical and complicated data annotations common in real world applications.

5 Conclusion

We present the imprecise label learning (ILL) framework, a unified and consolidated solution for learning from all types of imprecise labels. ILL effectively employs an expectation-maximization (EM) algorithm for maximum likelihood estimation (MLE) of the distribution over the latent ground truth labels Y , imprecise label information I , and data X . It naturally extends and encompasses previous formulations for various imprecise label settings, achieving promising results. Notably, in scenarios where mixed configurations of imprecise labels coexist, our method exhibits substantial robustness against diverse forms of label imprecision. The potential **broader impact** of the ILL framework is substantial. It stands poised to transform domains where obtaining precise labels poses a challenge, offering a simple, unified, and effective approach to such contexts. Beyond the three imprecise label configurations we have demonstrated in this study, the ILL framework shows promise for an extension to more intricate scenarios such as multi-instance learning [42] and multi-label crowd-sourcing learning [38]. However, it is also crucial to acknowledge the **limitations** of the ILL

framework. Although its effectiveness has been substantiated on relatively smaller-scale datasets, additional empirical validation is necessary to assess its scalability to larger datasets. Furthermore, our study only considers balanced datasets; thus, the performance of the ILL framework when dealing with imbalanced data and open-set data still remains an open area for future exploration. We hope that our study will constitute a significant stride towards a comprehensive solution for imprecise label learning and catalyze further research in this crucial field.

Acknowledge

Masashi Sugiyama was supported by the Institute for AI and Beyond, UTokyo.

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Appendix

A Notation

We present the notation table for each symbol used in this paper in Table 6.

Table 6: Notation Table

Notation	Definition
\mathbf{x}	A training instance
y	A class index label
$\{\mathbf{x}_i\}_{i \in [N]}$	A set of data instances \mathbf{x} of size N
$\{y_i\}_{i \in [N]}$	A set of precise label indices y of size N
$[l]$	An imprecise label, which might contain multiple class indices
$\{[l]_i\}_{i \in [N]}$	A set of imprecise labels $[l]$ of size N
X	Random variable of training instance
\mathcal{X}	Input space where \mathbf{x} is drawn from
Y	Random variable of ground-truth labels
\mathcal{Y}	Label space where y is drawn from
I	Random variable of imprecise labels
f	Model backbone
g	Model classifier
h	Model multi-layer perceptron
$f \circ g$	Model mapping $\mathcal{X} \rightarrow \mathcal{Y}$
θ	Learnable parameters of $f \circ g$
$\mathbf{p}(y \mathbf{x}; \theta)$	Output probability from model $f \circ g$
$f \circ h$	Model mapping $\mathcal{X} \rightarrow \mathcal{Z}$, where Z is a projected feature space
\mathcal{D}	Dataset
\mathcal{L}	Loss function
\mathcal{A}_w	Weak data augmentation, usually is HorizontalFlip
\mathcal{A}_s	Strong data augmentation, usually is RandAugment [95]
\mathbf{z}_w	Projected features from $f \circ h$ on weakly-augmented data
\mathbf{z}_s	Projected features from $f \circ h$ on strongly-augmented data
\mathcal{M}	Memory queue in MoCo [70]
s	A partial label, with ground-truth label contained
$\{s_i\}_{i \in [N]}$	A set partial labels, with ground-truth label contained of size N
S	Random variable of partial label
\mathbf{x}^l	A labeled training example
y^l	A labeled class index
\mathbf{x}^u	A unlabeled training example
y^u	A unknown class index for unlabeled data
X^L	A set of labeled data instances
Y^L	A set of labels for labeled data instances
X^U	A set of unlabeled data instances
Y^U	A set of unknown labels for unlabeled data instances
\hat{p}^u	The maximum predicted probability on unlabeled data $\max(\mathbf{p}(y \mathbf{x}^u; \theta))$
\hat{y}^u	The pseudo-label from the predicted probability on unlabeled data $\arg \max(\mathbf{p}(y \mathbf{x}^u; \theta))$
τ	The threshold for confidence thresholding
\hat{y}	A corrupted/noisy label
\hat{y}^{oh}	An one-hot version of the corrupted/noisy label
\hat{Y}	Random variable of noisy labels
$\mathbf{u}, \mathbf{v}, \mathbf{m}$	Noise model related parameters in SOP [69]
$\mathcal{T}(\hat{y} y; \omega)$	The simplified noise transition model in ILL
ω	The parameters in the simplified noise model

B Related Work

Many previous methods have been proposed for dealing with the specific types and some combinations of imprecise label configurations. We revisit the relevant work in this section, especially the state-of-the-art popular baselines for learning with individual and mixture imprecise label configurations.

Partial label learning (PLL). The prior arts can be roughly divided into identification-based for label disambiguation [96–99] or average-based for utilizing all candidate labels [72, 7, 58]. The traditional average-based methods usually treat all candidate labels equally, which may involve the misleading false positive labels into training. To overcome these limitations, researchers have

explored identification-based methods, viewing the ground-truth label as a latent variable. They seek to maximize its estimated probability using either the maximum margin criterion [100, 101] or the maximum likelihood criterion [102]. Deep learning techniques have recently been incorporated into identification-based methods, yielding promising results across multiple datasets. For example, PRODEN [55] proposed a self-training strategy that disambiguates candidate labels using model outputs. CC [9] introduced classifier-consistent and risk-consistent algorithms, assuming uniform candidate label generation. LWS [11] relaxed this assumption and proposed a family of loss functions for label disambiguation. More recently, Wangt et al. [13] incorporated contrastive learning into PLL, enabling the model to learn discriminative representations and show promising results under various levels of ambiguity. RCR involves consistency regularization into PLL recently [12].

Semi-supervised learning (SSL). SSL is a paradigm for learning with a limited labeled dataset supplemented by a much larger unlabeled dataset. Consistency regularization and self-training, inspired by clusteriness and smoothness assumptions, have been proposed to encourage the network to generate similar predictions for inputs under varying perturbations [103, 15, 104]. Self-training [14, 73, 18] is a widely-used approach for leveraging unlabeled data. Pseudo Label [14, 73], a well-known self-training technique, iteratively creates pseudo labels that are then used within the same model. Recent studies focus largely on generating high-quality pseudo-labels. MixMatch [16], for instance, generates pseudo labels by averaging predictions from multiple augmentations. Other methods like ReMixMatch [17], UDA [53], and FixMatch [18] adopt confidence thresholds to generate pseudo labels for weakly augmented samples, which are then used to annotate strongly augmented samples. Methods such as Dash [105], FlexMatch [20], and FreeMatch [22] dynamically adjust these thresholds following a curriculum learning approach. SoftMatch [23] introduces a novel utilization of pseudo-labels through Gaussian re-weighting. SSL has also seen improvements through the incorporation of label propagation, contrastive loss, and meta learning [106, 107, 86, 87, 82].

Noisy label learning (NLL). Overfitting to the noisy labels could result in poor generalization performance, even if the training error is optimized towards zero [108, 109]. Several strategies to address the noisy labels have been proposed [110]. Designing loss functions that are robust to noise is a well-explored strategy for tackling the label noise problem [29, 31, 111, 112]. Additionally, methods that re-weight loss [113] have also been explored for learning with noisy labels. Another common strategy to handle label noise involves assuming that the noisy label originates from a probability distribution that depends on the actual label. Early works [26] incorporated these transition probabilities into a noise adaptation layer that is stacked over a classification network and trained in an end-to-end fashion. More recent work, such as Forward [91], prefers to estimate these transition probabilities using separate procedures. However, the success of this method is contingent upon the availability of clean validation data [114] or additional assumptions about the data [115]. Noise correction has shown promising results in noisy label learning recently [116–118, 69]. During the early learning phase, the model can accurately predict a subset of the mislabeled examples [32]. This observation suggests a potential strategy of correcting the corresponding labels. This could be accomplished by generating new labels equivalent to soft or hard pseudo-labels estimated by the model [119, 120]. Co-Teaching uses multiple differently trained networks for correcting noisy labels [28]. SELFIE [121] corrects a subset of labels by replacing them based on past model outputs. Another study in [122] uses a two-component mixture model for sample selection, and then corrects labels using a convex combination. Similarly, DivideMix [33] employs two networks for sample selection using a mixture model and Mixup [90].

Mixture imprecise label settings. Various previous works have explored dealing with distinct types of imprecise labels. However, they have yet to tackle a combination of partial labels, limited labels, and noisy labels, which is a highly realistic scenario. For instance, recent attention has been paid to the issue of partial noisy label learning. PiCO+ [94], an extended version of PiCO [13], is tailored specifically for partial noisy labels. IRNet [71] uses two modules: noisy sample detection and label correction, transforming the scenario of noisy PLL into a more traditional PLL. DALI [50] is another framework designed to reduce the negative impact of detection errors by creating a balance between the initial candidate set and model outputs, with theoretical assurances of its effectiveness. Additionally, some work has focused on semi-supervised partial label learning [51, 52]. No existing research can effectively address the challenge of handling a combination of partial, limited, and noisy labels simultaneously, which underscores the novelty and significance of our work.

Previous attempts towards unification of learning from imprecise labels. There are earlier attempts for the generalized solutions of different kinds of imprecise labels/observations. Denœux

[60] proposed an EM algorithm for the likelihood estimation of fuzzy data and verified the algorithm on linear regression and uni-variate normal mixture estimation. Van Rooyen et al. [63] developed an abstract framework that generically tackles label corruption via the Markov transition. Quost et al. [62] further extended the EM algorithm of fuzzy data on the finite mixture of Gaussians. Gong et al. [64] proposed a general framework with centroid estimation for imprecise supervision. A unified partial AUC optimization approach was also proposed earlier [67]. Zhang et al. [45] and Wei et al. [66] proposed generalized solutions for aggregate observations. A unified solution based on dynamic programming for count-based weak supervision was also proposed [123] While relating to these works on the surface, ILL does not require any assumption on the imprecise information and generalizes well to more practical settings with noisy labels. Some other works for individual settings also related EM framework, but usually involved the approximation on the EM [124, 25, 13].

C Methods

C.1 Derivation of Variational Lower Bound

Evidence lower bound (ELBO), or equivalently variational lower bound [59], is the core quantity in EM. From Eq. (5), to model $\log P(X, I; \theta)$, we have:

$$\begin{aligned}
\log P(X, I; \theta) &= \int Q(Y) \log P(X, I; \theta) dY \\
&= \int Q(Y) \log P(X, I; \theta) \frac{P(Y|X, I; \theta)}{P(Y|X, I; \theta)} dY \\
&= \int Q(Y) \log \frac{P(X, I, Y; \theta) Q(Y)}{P(Y|X, I; \theta) Q(Y)} dY \\
&= \int Q(Y) \log \frac{P(X, I, Y; \theta)}{Q(Y)} dY - \int Q(Y) \log \frac{P(Y|X, I; \theta)}{Q(Y)} dY
\end{aligned} \tag{12}$$

where the first term is the ELBO and the second term is the KL divergence $\mathcal{D}_{KL}(Q(Y)||P(Y|X, I; \theta))$. Replacing $Q(Y)$ with $P(Y|X, I; \theta^t)$ at each iteration will obtain Eq. (5).

C.2 Instantiations to Partial Label Learning

The imprecise label I for partial labels is defined as the label candidate sets S with $\{\mathbf{s}_i\}_{i \in [N]}$ containing the true labels. Now we can derive Eq. (6) by replacing I with S in Eq. (5):

$$\begin{aligned}
&\mathbb{E}_{Y|X, I; \theta^t} [\log P(Y|X; \theta) + \log P(I|X, Y; \theta)] \\
&= \mathbb{E}_{Y|X, S; \theta^t} [\log P(Y|X; \theta) + \log P(I|X, Y; \theta)] \\
&= \sum_Y P(Y|X, S; \theta^t) [\log P(Y|X; \theta) + \log P(I|X, Y; \theta)] \\
&= \sum_Y P(Y|X, S; \theta^t) [\log P(Y|X; \theta)] + \log P(I|X, Y; \theta)
\end{aligned} \tag{13}$$

Note that $P(I|Y, X; \theta)$ can be moved out of the expectation because it is a fixed quantity to any Y . Now we replace Y, X , and S to y, \mathbf{x} , and \mathbf{s} for each instance, and converting the maximization problem to negative log-likelihood minimization problem to drive the loss function:

$$\mathcal{L}_{\text{ILL}}^{\text{PLL}} = -\frac{1}{N} \sum_i \mathbf{p}(y_i|\mathbf{x}_i, \mathbf{s}_i; \theta^t) \log \mathbf{p}(y_i|\mathbf{x}_i; \theta) - \frac{1}{N} \sum_i \log \mathbf{p}(\mathbf{s}_i|\mathbf{x}_i, y_i; \theta). \tag{14}$$

The first term is the Cross-Entropy loss we derived in Eq. (6). If S is not instance-dependent, then knowing Y also knows S , the second term thus can be ignored in Eq. (6). If S becomes instance-dependent, the second term can be maintained as a supervised term as in [12] to optimize θ .

C.3 Instantiations to Semi-Supervised Learning

In SSL, the input X consists of the labeled data X^{L} and the unlabeled data X^{U} . The imprecise label for SSL is realized as the limited number of full labels Y^{L} for X^{L} . The labels Y^{U} for unlabeled X^{U}

are unknown and become the latent variable. Thus we can write:

$$\begin{aligned}
& \mathbb{E}_{Y|X,I;\theta^t} [\log P(Y|X;\theta) + \log P(I|X,Y;\theta)] \\
&= \mathbb{E}_{Y^U|X^U,X^L,Y^L;\theta^t} [\log P(Y^U|X^U,X^L;\theta) + \log P(Y^L|X^L,X^U,Y^U;\theta)] \\
&= \sum_{Y^U} P(Y^U|X^U;\theta^t) [\log P(Y^U|X^U;\theta)] + \log P(Y^L|X^L;\theta).
\end{aligned} \tag{15}$$

The negative log-likelihood loss function for $\{\mathbf{x}_i^l, y_i^l\}_{i \in [N^L]}$ and $\{\mathbf{x}_i^u\}_{i \in [N^U]}$ thus becomes:

$$\mathcal{L}_{\text{ILL}}^{\text{SSL}} = \mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathbf{x}^u;\theta), \mathbf{p}(y|\mathbf{x}^u;\theta^t)) + \mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathbf{x}^L;\theta), y^L) \tag{16}$$

C.4 Instantiations to Noisy Label Learning

We denote the given noisy labels as \hat{Y} . For noisy label learning, our method naturally supports a noise transition model $\mathcal{T}(\hat{Y}|Y;\omega)$ with learnable parameter ω , as we will show in the following:

$$\begin{aligned}
& \mathbb{E}_{Y|X,I;\theta^t} [\log P(Y|X;\theta) + \log P(I|X,Y;\theta)] \\
&= \mathbb{E}_{Y|X,\hat{Y};\theta^t} [\log P(Y,\hat{Y}|X;\theta)] \\
&= \mathbb{E}_{Y|X,\hat{Y};\theta^t} [\log P(Y|\hat{Y},X;\theta) + \log P(\hat{Y}|X;\theta)] \\
&= \sum_Y P(Y|\hat{Y},X;\theta^t) \log P(Y|\hat{Y},X;\theta) + \log P(\hat{Y}|X;\theta).
\end{aligned} \tag{17}$$

The loss function is:

$$\mathcal{L}_{\text{ILL}}^{\text{NLL}} = \mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathbf{x},\hat{y};\theta,\omega^t), \mathbf{p}(y|\mathbf{x},\hat{y};\theta^t,\omega^t)) + \mathcal{L}_{\text{CE}}(\mathbf{p}(\hat{y}|\mathbf{x};\theta,\omega), \hat{y}) \tag{18}$$

Note that both term is computed from the noise transition matrix as mentioned in Eq. (9).

C.5 Instantiations to Mixed Imprecise Label Learning

In this setting, we have both labeled data and unlabeled data, where the labels for the labeled data are both partial and noisy. On the unlabeled data, the unsupervised objective is the same as the unsupervised consistency regularization of semi-supervised learning shown in Eq. (7). On the labeled data, it mainly follows the Eq. (9) of noisy label learning, with the noisy single label becoming the noisy partial labels $\hat{\mathbf{s}}$. For noisy partial labels, the noisy supervised objective in Eq. 8 becomes the supervised consistency regularization as in Eq. 6 of partial label setting to train the noise transition model, and the noisy unsupervised objective becomes the consistency regularization of the prediction conditioned on noisy partial labels:

$$\mathcal{L}_{\text{CE}}(\mathbf{p}(y|\mathcal{A}_s(\mathbf{x}),\hat{\mathbf{s}};\theta,\omega^t), \mathbf{p}(y|\mathcal{A}_w(\mathbf{x}),\hat{y};\theta^t,\omega^t)) + \mathcal{L}_{\text{CE}}(\mathbf{p}(\hat{y}|\mathcal{A}_w(\mathbf{x});\theta,\omega), \hat{\mathbf{s}}) \tag{19}$$

We can compute both quantity through the noise transition model:

$$\mathbf{p}(y|\mathbf{x},\hat{\mathbf{s}};\theta,\omega^t) \propto \mathbf{p}(y|\mathbf{x};\theta) \prod_{\hat{y} \in \hat{\mathbf{s}}} \mathcal{T}(y|\hat{y};\omega^t), \text{ and } \mathbf{p}(\hat{y}|\mathbf{x};\theta,\omega) = \sum_{y \in [C]} \mathbf{p}(y|\mathbf{x};\theta) \mathcal{T}(\hat{y}|y;\omega). \tag{20}$$

D Experiments

D.1 Additional Training Details

We adopt two additional training strategies for the ILL framework. The first is the ‘‘strong-weak’’ augmentation strategy [53]. Since there is a consistency regularization term in each imprecise label formulation of ILL, we use the soft pseudo-targets of the weakly-augmented data to train the strongly-augmented data. The second is the entropy loss [75] for class balancing, which is also adopted in SOP [69] and FreeMatch [22]. We set the loss weight for the entropy loss uniformly for all experiments as 0.1.

D.2 Partial Label Learning

D.2.1 Setup

Following previous work [125, 11, 13], we evaluate our method on partial label learning setting using CIFAR-10, CIFAR-100, and CUB-200 [78]. We generate partially labeled datasets by flipping negative labels to false positive labels with a probability q , which is also denoted as a partial ratio. Specifically, the $C - 1$ negative labels are uniformly aggregated into the ground truth label to form a set of label candidates. We consider $q \in \{0.1, 0.3, 0.5\}$ for CIFAR-10, $q \in \{0.01, 0.05, 0.1\}$ for CIFAR-100, and $q = 0.05$ for CUB-200. For CIFAR-10 and CIFAR-100, we use ResNet-18 [1] as backbone. We use SGD as an optimizer with a learning rate of 0.01, a momentum of 0.9, and a weight decay of $1e-3$. For CUB-200, we initialize the ResNet-18 [1] with ImageNet-1K [126] pre-trained weights. We train 800 epochs for CIFAR-10 and CIFAR-100 [77], and 300 epochs for CUB-200, with a cosine learning rate scheduler. For CIFAR-10 and CIFAR-100, we use an input image size of 32. For CUB-200, we use an input image size of 224. A batch size of 256 is used for all datasets. The choice of these parameters mainly follows PiCO [13]. We present the full hyper-parameters systematically in Table 7.

Table 7: Hyper-parameters for **partial label learning** used in experiments.

Hyper-parameter	CIFAR-10	CIFAR-100	CUB-200
Image Size	32	32	224
Model	ResNet-18	ResNet-18	ResNet-18 (ImageNet-1K Pretrained)
Batch Size	256	256	256
Learning Rate	0.01	0.01	0.01
Weight Decay	1e-3	1e-3	1e-5
LR Scheduler	Cosine	Cosine	Cosine
Training Epochs	800	800	300
Classes	10	100	200

D.2.2 Discussion

We additionally compare our method with R-CR [12], which uses a different architecture as the results in Table 1. R-CR uses Wide-ResNet34x10 as backbone, and adopts multiple strong data augmentations. It also adjusts the loss weight along training. For fair comparison, we use the same architecture without multiple augmentation and the curriculum adjust on loss. The results are shown in Table 8, where our method outperforms R-CR on CIFAR-10 and is comparable on CIFAR-100.

Table 8: Comparison with R-CR in partial label learning

Method	CIFAR-10		CIFAR-100	
	0.3	0.5	0.05	0.10
R-CR	97.28±0.02	97.05±0.05	82.77±0.10	82.24±0.07
Ours	97.55±0.07	97.17±0.11	82.46±0.08	82.22±0.05

We also provide the comparison of our method on instance-dependent partial label learning as proposed by Xu et al. [81, 125]. Due to the nature of instance-dependence, we maintain the term $P(S|Y, X; \theta)$ from Eq. (5) as a supervised term for optimization. We compare our method with VALEN [81], RCR [12], PiCO [13], and POP [125] on MNIST, Kuzushiji-MNIST, Fashion-MNIST, CIFAR-10, and CIFAR-100, with synthetic instance-dependent partial labels generated according to Xu et al. [125]. From the results in Table 9, we proposed method demonstrate the best performance across different datasets evaluated.

A recent work on PLL discussed and analyzed the robustness performance of different loss functions, especially the average-based methods [58]. We perform a similar analysis here for the derived loss function in ILL. Following the notation in [58], let \mathbf{s} denote the candidate label set, \mathbf{x} as the training instance, g as the probability score from the model, and f as the classifier $f(\mathbf{x}) = \arg \max_{i \in \mathcal{Y}} g_i(\mathbf{x})$, the average-based PLL can be formulated as:

$$\mathcal{L}_{avg-PLL}(f(\mathbf{x}), \mathbf{s}) = \frac{1}{|\mathbf{s}|} \sum_{i \in \mathbf{s}} \ell(f(\mathbf{x}), i) \quad (21)$$

Table 9: Comparison on instance-dependent partial label learning

	MNIST	Kuzushiji-MNIST	Fashion-MNIST	CIFAR-10	CIFAR-100
VALEN [81]	99.03	90.15	96.31	92.01	71.48
RCR [12]	98.81	90.62	96.64	86.11	71.07
PICO [13]	98.76	88.87	94.83	89.35	66.30
POP [125]	99.28	91.09	96.93	93.00	71.82
Ours	99.19	91.35	97.01	93.86	72.43

Lv et al. [58] compared different loss functions ℓ on both noise-free and noisy PLL settings, where they find both theoretically and empirically that average-based PLL with *bounded* loss are robust under mild assumptions. Empirical study in [58] suggests that both *Mean Absolute Error* and *Generalized Cross-Entropy* loss [29] that proposed for noisy label learning achieves the best performance and robustness for average-based PLL.

Our solution for PLL can be viewed as an instantiation of the average-based PLL as in [58] with:

$$\ell(f(\mathbf{x}), i) = -\bar{g}_i(\mathbf{x}) \log g_i(\mathbf{x}) \quad (22)$$

where \bar{g} is normalized probability over \mathbf{s} with detached gradient. We can further show that the above loss function is bounded for $0 < \ell \leq \frac{1}{e}$ and thus bounded for summation of all classes, which demonstrates robustness, as we show in Table 4.

D.3 Semi-Supervised Learning

D.3.1 Setup

For experiments of SSL, we follow the training and evaluation protocols of USB [82] on image and text classification. To construct the labeled dataset for semi-supervised learning, we uniformly select l/C samples from each class and treat the remaining samples as the unlabeled dataset. For image classification tasks, ImageNet-1K [126] Vision Transformers [4] are used, including CIFAR-100 [77], EuroSAT [127], STL-10 [128], TissueMNIST [129, 130], Semi-Aves [131]. For text classification tasks, we adopt BERT [3] as backbone, including IMDB [83], Amazon Review [84], Yelp Review [132], AG News [133], Yahoo Answer [134]. The hyper-parameters strictly follow USB, and are shown in Table 10 and Table 11.

Table 10: Hyper-parameters of **semi-supervised learning** used in vision experiments of USB.

Hyper-parameter	CIFAR-100	STL-10	Euro-SAT	TissueMNIST	Semi-Aves
Image Size	32	96	32	32	224
Model	ViT-S-P4-32	ViT-B-P16-96	ViT-S-P4-32	ViT-T-P4-32	ViT-S-P16-224
Labeled Batch size			16		
Unlabeled Batch size			16		
Learning Rate	5e-4	1e-4	5e-5	5e-5	1e-3
Weight Decay			5e-4		
Layer Decay Rate	0.5	0.95	1.0	0.95	0.65
LR Scheduler			$\eta = \eta_0 \cos(\frac{7\pi k}{16K})$		
Training epochs			20		
Classes	100	10	10	10	200
Model EMA Momentum			0.0		
Prediction EMA Momentum			0.999		
Weak Augmentation		Random Crop, Random Horizontal Flip			
Strong Augmentation		RandAugment [95]			

D.3.2 Results

In the main paper, we only provide the comparison on CIFAR-100, STL-10, IMDB, and Amazon Review. Here we provide the full comparison in Table 12 and Table 13. From the full results, similar conclusion can be drawn as in the main paper. Our ILL framework demonstrates comparable performance as previous methods.

Table 11: Hyper-parameters of **semi-supervised learning** NLP experiments in USB.

Hyper-parameter	AG News	Yahoo! Answer	IMDB	Amazon-5	Yelp-5
Max Length			512		
Model			Bert-Base		
Labeled Batch size			4		
Unlabeled Batch size			4		
Learning Rate	5e-5	1e-4	5e-5	1e-5	5e-5
Weight Decay			1e-4		
Layer Decay Rate	0.65	0.65	0.75	0.75	0.75
LR Scheduler			$\eta = \eta_0 \cos(\frac{\pi k}{16K})$		
Training epochs			10		
Classes	4	10	2	5	5
Model EMA Momentum			0.0		
Prediction EMA Momentum			0.999		
Weak Augmentation			None		
Strong Augmentation			Back-Translation [53]		

Table 12: Error rate comparison of different number of labels on CIFAR-100, STL-10, EuroSAT, TissueMNIST, and SemiAves for **semi-supervised learning**. We use USB [82] image classification task results. The best results are indicated in bold. Our results are averaged over 3 independent runs.

Datasets	CIFAR-100		STL-10		EuroSat		TissueMNIST		SemiAves
	200	400	40	100	20	40	80	400	3959
Pseudo-Label [14]	33.99±0.95	25.32±0.29	19.14±1.33	10.77±0.60	25.46±1.36	15.70±2.12	56.92±4.54	50.86±1.79	40.35±0.30
Mean-Teacher [103]	35.47±0.40	26.03±0.30	18.67±1.69	24.19±10.15	26.83±1.46	15.85±1.66	62.06±3.43	55.12±2.53	38.55±0.21
VAT [104]	31.49±1.33	21.34±0.50	18.45±1.47	10.69±0.51	26.16±0.96	10.09±0.94	57.49±5.47	51.30±1.73	38.82±0.04
MixMatch [16]	38.22±0.71	26.72±0.72	58.77±1.98	36.74±1.24	24.85±4.85	17.28±2.67	55.53±1.51	49.64±2.28	37.25±0.08
ReMixMatch [17]	22.21±2.21	16.86±0.57	13.08±3.34	7.21±0.39	5.05±1.05	5.07±0.56	58.77±4.43	49.82±1.18	30.20±0.03
AdaMatch [85]	22.32±1.73	16.66±0.62	13.64±2.49	7.62±1.90	7.02±0.79	4.75±1.10	58.35±4.87	52.40±2.08	31.75±0.13
FixMatch [18]	29.60±0.90	19.56±0.52	16.15±1.89	8.11±0.68	13.44±3.53	5.91±2.02	55.37±4.50	51.24±1.56	31.90±0.06
FlexMatch [20]	26.76±1.12	18.24±0.36	14.40±3.11	8.17±0.78	5.17±0.57	5.58±0.81	58.36±3.80	51.89±3.21	32.48±0.15
Dash [105]	30.61±0.98	19.38±0.10	16.22±5.95	7.85±0.74	11.19±0.90	6.96±0.87	56.98±2.93	51.97±1.55	32.38±0.16
CoMatch [86]	35.08±0.69	25.35±0.50	15.12±1.88	9.56±1.35	5.75±0.43	4.81±1.05	59.04±4.90	52.92±0.04	38.65±0.18
SimMatch [87]	23.78±1.08	17.06±0.78	11.77±3.20	7.55±1.86	7.66±0.60	5.27±0.89	60.88±4.31	52.93±1.56	33.85±0.08
FreeMatch [22]	21.40±0.30	15.65±0.26	12.73±3.22	8.52±0.53	6.50±0.78	5.78±0.51	58.24±3.08	52.19±1.35	32.85±0.31
SoftMatch [23]	22.67±1.32	16.84±0.66	13.55±3.16	7.84±1.72	5.75±0.62	5.90±1.42	57.98±3.66	51.73±2.84	31.80±0.22
Ours	22.06±1.06	17.40±1.04	11.09±0.71	8.10±1.02	5.86±1.06	5.74±1.13	57.99±2.16	50.95±2.03	33.08±0.26

Table 13: Error rate comparison of different number of labels on IMDB, AG News, Amazon Review, Yahoo Answers, and Yelp Review for **semi-supervised learning**. We use USB [82] text classification task results. Best results are indicated in bold. Our results are averaged over 3 independent runs.

Datasets	IMDB		AG News		Amazon Review		Yahoo Answers		Yelp Review	
	20	100	40	200	250	1000	500	2000	250	1000
Pseudo-Label [14]	45.45±4.43	19.67±1.01	19.49±3.07	14.69±1.88	53.45±1.9	47.00±0.79	37.70±0.65	32.72±0.31	54.51±0.82	47.33±0.20
Mean-Teacher [103]	20.06±2.51	13.97±1.49	15.17±1.21	13.93±0.65	52.14±0.52	47.66±0.84	37.09±0.18	33.43±0.28	50.60±0.62	47.21±0.31
VAT [104]	25.93±2.58	11.61±1.79	14.70±1.19	11.71±0.84	49.83±0.46	46.54±0.31	34.87±0.41	31.50±0.35	52.97±1.41	45.30±0.32
MixMatch [16]	26.12±6.13	15.47±0.65	13.50±1.51	11.75±0.60	59.54±0.67	61.69±3.32	35.75±0.71	33.62±0.14	53.98±0.59	51.70±0.68
AdaMatch [85]	8.09±0.99	7.11±0.20	11.73±0.17	11.22±0.95	46.72±0.72	42.27±0.25	32.75±0.35	30.44±0.31	45.40±0.96	40.16±0.49
FixMatch [18]	7.72±0.33	7.33±0.13	30.17±1.87	11.71±1.95	47.61±0.83	43.05±0.54	33.03±0.49	30.51±0.53	46.52±0.94	40.65±0.46
FlexMatch [20]	7.82±0.77	7.41±0.38	16.38±3.94	12.08±0.73	45.73±1.60	42.25±0.33	35.61±1.08	31.13±0.18	43.35±0.69	40.51±0.34
Dash [105]	8.34±0.86	7.55±0.35	17.67±3.19	13.76±1.67	47.10±0.74	43.09±0.60	35.26±0.33	31.19±0.29	45.24±2.02	40.14±0.79
CoMatch [86]	7.44±0.30	7.72±1.14	11.95±0.76	10.75±0.35	48.76±0.90	43.36±0.21	33.48±0.51	30.25±0.35	45.40±1.12	40.27±0.51
SimMatch [87]	7.93±0.55	7.08±0.33	14.26±1.51	12.45±1.37	45.91±0.95	42.21±0.30	33.06±0.20	30.16±0.21	46.12±0.48	40.26±0.62
FreeMatch [22]	8.94±0.21	7.95±0.45	12.98±0.58	11.73±0.63	46.41±0.60	42.64±0.06	32.77±0.26	30.32±0.18	47.95±1.45	40.37±1.00
SoftMatch [23]	7.76±0.58	7.97±0.72	11.90±0.27	11.72±1.58	45.29±0.95	42.21±0.20	33.07±0.31	30.44±0.62	44.09±0.50	39.76±0.13
Ours	7.32±0.12	7.64±0.67	14.77±1.59	12.21±0.82	43.96±0.32	42.32±0.02	33.80±0.25	30.86±0.17	44.82±0.17	39.67±0.71

D.4 Noisy Label Learning

D.4.1 Setup

We conduct experiments of noisy label learning following SOP [69]. We evaluate the proposed method on both synthetic symmetric/asymmetric noise on CIFAR-10 and CIFAR-100, and more realistic and larger-scale instance noise on Clothing1M and WebVision. To introduce the synthetic symmetric noise to CIFAR-10 and CIFAR-100, we uniformly flip labels for a probability η into other classes. For asymmetric noise, we only randomly flip the labels for particular pairs of classes. For CIFAR-10 and CIFAR-100, we train PreAct-ResNet-18 with SGD using a learning rate of 0.02, a

weight decay of $1e-3$, and a momentum of 0.9. We train for 300 epochs with a cosine learning rate schedule and a batch size of 128. For WebVision, we use InceptionResNet-v2 as the backbone and set the batch size to 32. Other settings are similar to CIFAR-10. For Clothing1M, we use ImageNet-1K pre trained ResNet-50 as the backbone. We train it using SGD with an initial learning rate of $2e-3$ for a total of 10 epochs, where the learning rate is reduced by 10 after 5 epochs. In addition, we also conduct experiments on CIFAR-10N and CIFAR-100N. We present the detailed hyper-parameters in Table 14.

Table 14: Hyper-parameters for **noisy label learning** used in experiments.

Hyper-parameter	CIFAR-10 (CIFAR-10N)	CIFAR-100 (CIFAR-100N)	Clothing1M	WebVision
Image Size	32	32	224	299
Model	PreAct-ResNet-18 (ResNet-34)	PreAct-ResNet-18 (ResNet-34)	ResNet-50 (ImageNet-1K Pretrained)	Inception-ResNet-v2
Batch Size	128	128	64	32
Learning Rate	0.02	0.02	0.002	0.02
Weight Decay	$1e-3$	$1e-3$	$1e-3$	$5e-4$
LR Scheduler	Cosine	Cosine	MultiStep	MultiStep
Training Epochs	300	300	10	100
Classes	10	100	14	50
Noisy Matrix Scale	1.0	2.0	0.5	2.5

D.4.2 Results

In addition to the results regarding noisy label learning provided in the main paper, we also present comparison results on CIFAR-10N and CIFAR-100N [92] in Table 15. We include a full comparison on Clothing1M and WebVision, incorporating methods like Co-Teaching, Forward, and CORES, in Table 16. As shown in Table 15, the proposed ILL framework achieves performance comparable to the previous best method, SOP [69]. On CIFAR-10N, our method yields results very close to SOP in the Random and Aggregate case noise scenarios and surpasses SOP in the Worst case noise scenario. However, on CIFAR-100N, our method slightly underperforms previous methods, possibly due to the oversimplified noise model utilized in ILL. We believe that a more realistic noise transition model and further tuning of our method could lead to improved performance.

Table 15: Test accuracy comparison of instance independent label noise on CIFAR-10N and CIFAR-100N for **noisy label learning**. The best results are indicated in **bold**, and the second best results are indicated in underline. Our results are averaged over three independent runs with ResNet34 as the backbone.

Dataset	CIFAR-10N						CIFAR-100N	
	Clean	Random 1	Random 2	Random 3	Aggregate	Worst	Clean	Noisy
CE	92.92±0.11	85.02±0.65	86.46±1.79	85.16±0.61	87.77±0.38	77.69±1.55	76.70±0.74	55.50±0.66
Forward [91]	93.02±0.12	86.88±0.50	86.14±0.24	87.04±0.35	88.24±0.22	79.79±0.46	76.18±0.37	57.01±1.03
Co-teaching [28]	93.35±0.14	90.33±0.13	90.30±0.17	90.15±0.18	91.20±0.13	83.83±0.13	73.46±0.09	60.37±0.27
DivideMix [33]	-	<u>95.16±0.19</u>	<u>95.23±0.07</u>	<u>95.21±0.14</u>	95.01±0.71	92.56±0.42	-	71.13±0.48
ELR [32]	95.39±0.05	94.43±0.41	94.20±0.24	94.34±0.22	94.83±0.10	91.09±1.60	<u>78.57±0.12</u>	<u>66.72±0.07</u>
CORES [135]	94.16±0.11	94.45±0.14	94.88±0.31	94.74±0.03	95.25±0.09	91.66±0.09	73.87±0.16	55.72±0.42
SOP [69]	96.38±0.31	<u>95.28±0.13</u>	<u>95.31±0.10</u>	<u>95.39±0.11</u>	<u>95.61±0.13</u>	<u>93.24±0.21</u>	78.91±0.43	<u>67.81±0.23</u>
Ours	<u>96.21±0.29</u>	96.06±0.07	95.98±0.12	96.10±0.05	96.40±0.03	93.55±0.14	78.53±0.21	68.07±0.33

D.5 Mixed Imprecise Label Learning

D.5.1 Setup

To create a mixture of various imprecise label configurations, we select CIFAR-10 and CIFAR-100 as base datasets. We first uniformly sample l/C labeled samples from each class to form the labeled dataset and treat the remaining samples as the unlabeled dataset. Based on the labeled dataset, we generate partially labeled datasets by flipping negative labels to false positive labels with the partial ratio q . After obtaining the partial labels, we randomly select η percentage of samples from each class, and recreate the partial labels for them by flipping the ground truth label uniformly to another class. In this setting, unlabeled data, partially labeled data, and noisy labeled data exist simultaneously, which is very challenging and more closely resembles realistic situations. For CIFAR-10, we set $l \in \{1000, 5000, 50000\}$, and for CIFAR-100, we set $l \in \{5000, 10000, 50000\}$. Similarly in

Table 16: Test accuracy comparison of realistic noisy labels on Clothing1M and WebVision for **noisy label learning**. The best results are indicated in **bold** and the second best results are indicated in underline. Our results are averaged over 3 independent runs. For Clothing1M, we use ImageNet-1K pre trained ResNet50 as the backbone. For WebVision, InceptionResNetv2 is used as the backbone.

Dataset	Clothing1M	WebVision
CE	69.10	-
Forward [91]	69.80	61.10
MentorNet [93]	66.17	63.00
Co-Teaching [28]	69.20	63.60
DivideMix [33]	74.76	<u>77.32</u>
ELR [32]	72.90	76.20
CORES [135]	73.20	-
SOP [69]	73.50	76.60
Ours	<u>74.02±0.12</u>	79.37±0.09

the partial label setting, we set $q \in \{0.1, 0.3, 0.5\}$ for CIFAR-10, and $q \in \{0.01, 0.05, 0.1\}$ for CIFAR-100. For noisy labels, we set $\eta \in \{0.1, 0.2, 0.3\}$ for both datasets.

D.5.2 Results

We provide a more complete version of Table 4 in Table 17. On partial noisy labels of CIFAR-10 with partial ratio 0.5 and of CIFAR-100 with partial ratio 0.1, most baseline methods are more robust or even fail to perform. However, our ILL still shows very robust performance with minor performance degradation as increase of noise ratios.

D.6 Ablation on Strong-Augmentation and Entropy Loss

We provide the ablation study on the strong-augmentation and entropy loss components here, which are common techniques in each setting [18, 13, 69]. For example, in SSL, strong-weak augmentation is an important strategy for SSL algorithms widely used in existing works such as FixMatch [18] and FlexMatch [20]. Thus, it is important to adopt strong-weak augmentation to achieve better performance in SSL [22, 23, 82]. This is similar in PLL settings [13, 12]. PiCO [13, 12] also used strong augmentation). Strong-weak augmentation and entropy loss are also adopted in SOP [69] of NLL. However, we found these techniques are less important for our formulation of NLL. We provide an ablation study on the entropy loss of SSL, and both techniques for NLL and PLL here to demonstrate our discussions.

D.7 Runtime Analysis

We provide the runtime analysis on CIFAR-100 of our method on different settings, compared with the SOTA baselines. We compute the average runtime from all training iterations on CIFAR-100. The results are shown in Table 21. Our method in general present faster runtime without complex design such as contrastive loss.

Table 17: Test accuracy comparison of **mixture of different imprecise labels**. We report results of full labels, partial ratio q of $\{0.1, 0.3, 0.5\}$ for CIFAR-10 and $\{0.01, 0.05, 0.1\}$ for CIFAR-100, and noise ratio η of $\{0.1, 0.2, 0.3\}$ for CIFAR-10 and CIFAR-100.

Dataset	# Labels	Partial Ratio q	Noise Ratio η	0	0.1	0.2	0.3
CIFAR-10	50,000	0.1	PiCO+ [94]	95.99 \pm 0.03	93.64	93.13	92.18
			IRNet [71]	-	93.44	92.57	92.38
			DALI [50]	-	94.15	94.04	93.77
			PiCO+ w/ Mixup [50]	-	94.58	94.74	94.43
			DALI w/ Mixup [50]	-	95.83	95.86	95.75
			Ours	96.55\pm0.08	96.47\pm0.11	96.09\pm0.20	95.83\pm0.05
		0.3	PiCO+ [94]	95.73 \pm 0.10	92.32	92.22	89.95
			IRNet [71]	-	92.81	92.18	91.35
			Ours	96.52\pm0.12	96.2\pm0.02	95.87\pm0.14	95.22\pm0.06
0.5	PiCO+ [94]	95.33 \pm 0.06	91.07	89.68	84.08		
	IRNet [71]	-	91.51	90.76	86.19		
	DALI [50]	-	92.67	91.83	89.8		
	PiCO+ w/ Mixup [50]	-	93.56	92.65	88.21		
	DALI w/ Mixup [50]	-	95.19	93.89	92.26		
	Ours	96.28\pm0.13	95.82\pm0.07	95.28\pm0.08	94.35\pm0.08		
CIFAR-100	50,000	0.01	PiCO+ [94]	76.29 \pm 0.42	71.42	70.22	66.14
			IRNet [71]	-	71.17	70.10	68.77
			DALI [50]	-	72.26	71.98	71.04
			PiCO+ w/ Mixup [50]	-	75.04	74.31	71.79
			DALI w/ Mixup [50]	-	76.52	76.55	76.09
			Ours	78.08\pm0.26	77.53\pm0.24	76.96\pm0.02	76.43\pm0.27
	0.05	PiCO+ [94]	76.17 \pm 0.18	69.40	66.67	62.24	
		IRNet [71]	-	70.73	69.33	68.09	
		DALI [50]	-	72.28	71.35	70.05	
		PiCO+ w/ Mixup [50]	-	73.06	71.37	67.56	
		DALI w/ Mixup [50]	-	76.87	75.23	74.49	
		Ours	76.95\pm0.46	77.07\pm0.16	76.34\pm0.08	75.13\pm0.63	
	0.1	PiCO+ [94]	75.55 \pm 0.21	-	-	-	
		IRNet [71]	-	-	-	-	
		DALI [50]	-	-	-	-	
		PiCO+ w/ Mixup [50]	-	-	-	-	
		DALI w/ Mixup [50]	-	-	-	-	
		Ours	76.41\pm1.02	75.50\pm0.54	74.67\pm0.30	73.88\pm0.60	

Table 18: SSL ablation

	CIFAR100 $l=200$	STL10 $l=40$
Ours	22.06	11.09
Ours w/o ent.	22.41	11.23

Table 19: PLL ablation

	CIFAR10 $q = 0.5$	CIFAR100 $q = 0.1$
PiCO	93.58	69.91
Ours	95.91	74.00
PiCO w/o s. a.	91.78	66.43
Ours w/o s. a.	94.53	72.69
Ours w/o ent.	95.87	73.75

Table 20: NLL ablation

	CIFAR10 $\eta = 0.5$	CIFAR100 $\eta = 0.1$
SOP	94.00	63.30
Ours	94.31	66.46
SOP w/o s. a.	66.85	36.60
Ours w/o s. a.	93.56	65.89
SOP w/o ent.	93.04	62.85
Ours w/o ent.	94.16	66.12

Table 21: Runtime Analysis on CIFAR-100

Setting	Algorithm	CIFAR-100 Avg. Runtime (s/iter)
SSL	FreeMatch	0.2157
SSL	Ours	0.1146
PLL	PiCO	0.3249
PLL	Ours	0.2919
NLL	SOP	0.1176
NLL	Ours	0.1021

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