
Design-Bench: Benchmarks for Data-Driven Offline Model-Based Optimization

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Abstract

1 Black-box model-based optimization (MBO) problems, where the goal is to find
2 a design input that maximizes an unknown objective function, are ubiquitous
3 in a wide range of domains, such as the design of proteins, DNA sequences,
4 aircraft, and robots. Solving model-based optimization problems typically requires
5 actively querying the unknown objective function on design proposals, which
6 means physically building the candidate molecule, aircraft, or robot, testing it,
7 and storing the result. This process can be expensive and time consuming, and
8 one might instead prefer to optimize for the best design using only the data one
9 already has. This setting—called offline MBO—poses substantial and different
10 algorithmic challenges than more commonly studied online techniques. A number
11 of recent works have demonstrated success with offline MBO for high-dimensional
12 optimization problems using high-capacity deep neural networks. However, the
13 lack of standardized benchmarks in this emerging field is making progress difficult
14 to track. To address this, we present Design-Bench, a benchmark for offline MBO
15 with a unified evaluation protocol and reference implementations of recent methods.
16 Our benchmark includes a suite of diverse and realistic tasks derived from real-
17 world optimization problems in biology, materials science, and robotics that present
18 distinct challenges for offline MBO. Our benchmark and reference implementations
19 are publicly available at: github.com/brandontrabucco/design-bench

20 1 Introduction

21 Automatically synthesizing designs that maximize a desired objective function is one of the most
22 important challenges in scientific and engineering disciplines. From protein design in molecular
23 biology [33] to superconducting material discovery in physics [16], researchers have made significant
24 progress in applying machine learning to optimization problems over structured design spaces.
25 Commonly, the exact form of the objective function is unknown, and the objective value for a novel
26 design can only be found by either running computer simulations or real world experiments. This
27 process of optimizing an unknown function by only observing samples from this function is known as
28 black-box optimization, and is typically solved in an **online** iterative manner, where in each iteration
29 the solver proposes new designs and queries the objective function for feedback in order to inform
30 better design proposals at the next iteration [42]. In many domains however, the objective function is
31 prohibitively expensive to evaluate because it requires manually conducting experiments in the real
32 world. In this setting, one cannot query the true objective function, and cannot receive feedback on
33 design proposals. Instead, a collection of past records of designs and corresponding objective values
34 might be available, and the optimization method must instead leverage existing data to synthesize the
35 most optimal designs. This is the setting of **offline model-based optimization** (offline MBO).

36 Although online black-box optimization has been studied extensively, offline MBO has received
37 comparatively less attention, and only a small number of recent works study offline MBO in the setting
38 with high-dimensional design spaces [7, 22, 10, 11, 38]. This is partly because online techniques

39 cannot be directly applied in settings where offline MBO is used, especially in high-dimensional
 40 settings. Online techniques, such as Bayesian optimization [35], often require iterative feedback
 41 via queries to the objective function. Such online optimizers exhibit optimistic behavior: they rely
 42 on active queries at completely unseen designs irrespective of whether such a design is good or
 43 not. When access to these queries is removed, certain considerations change: optimism is no longer
 44 desirable and distribution shift becomes a major challenge [22].

45 Even with only a few existing offline MBO methods, it is hard to compare and track progress, as
 46 methods are typically proposed and evaluated on different tasks with distinct evaluation protocols. To
 47 the best of our knowledge, there is no commonly adopted benchmark for offline MBO. To address,
 48 we introduce a suite of tasks for offline MBO with a standardized evaluation protocol. We include
 49 a diverse set of tasks that span a wide range of application domains—from synthetic biology to
 50 robotics—that aims at representing the core challenges in real-world offline MBO. While the tasks are
 51 not intended to directly enable solving the corresponding real-world problems, which would require
 52 a lot of machinery in real hardware setup (e.g., a real robot or access to a wetlab for molecule design),
 53 they are intended to provide algorithm designers with a representative sampling of challenges that
 54 reflect the difficulties with real-world MBO. That is to say, the tasks are not intended to be *real*,
 55 but are intended to be *realistically challenging*. Further, the diversity of the tasks measures how
 56 they generalize across multiple domains and verifies they are not specialized to a single task. Our
 57 benchmark incorporates a variety of challenging factors, such as high dimensionality and sensitive
 58 discontinuous objective functions, which help identify the strengths and weaknesses of MBO methods.
 59 Along with this benchmark suite, we present reference implementations of a number of existing
 60 offline MBO and baseline optimization methods. We systematically evaluate them on all of the
 61 proposed benchmark tasks and report results. We hope that our work can provide insight into the
 62 progress of offline MBO methods and serve as a meaningful metric to galvanize research in this area.

63 2 Offline Model-Based Optimization Problem Statement

64 In online model-based optimization, the goal is to optimize a (possibly stochastic) black-box objective
 65 function $f(\mathbf{x})$ with respect to its input. The objective can be written as $\arg \max_{\mathbf{x}} f(\mathbf{x})$. Methods
 66 for online MBO typically optimize the objective iteratively, proposing design \mathbf{x}_k at the k th iteration
 67 and query the objective function to obtain $f(\mathbf{x}_k)$. Unlike its online counterpart, access to the true
 68 objective f is not available in offline MBO. Instead, the algorithm \mathfrak{A} is provided access to a static
 69 dataset $\mathcal{D} = \{(\mathbf{x}_i, y_i)\}$ of designs \mathbf{x}_i and a corresponding measurement of the objective value y_i . The
 70 algorithm consumes this dataset and produces an optimized candidate design \mathbf{x}^* which is evaluated
 71 against the true objective function. Abstractly, the objective for offline MBO is:

$$\arg \max_{\mathfrak{A}} f(\mathbf{x}^*) \text{ where } \mathbf{x}^* = \mathfrak{A}(\mathcal{D}). \quad (1)$$

72 In practice, producing a single optimal design entirely from offline data is very difficult, so offline
 73 MBO methods are more commonly evaluated [22] in terms of “ P percentile of top K ” performance,
 74 where the algorithm produces K candidates and the P percentile objective value determines final
 75 performance. Next we discuss two important aspects pertaining to offline MBO, namely, why offline
 76 MBO algorithms can improve beyond the best design observed in the offline dataset despite no active
 77 queries, and the associated challenges with devising offline MBO algorithms.

78 Would offline MBO even produce designs better than the best observed design in the dataset?

79 A natural question to ask is whether it is even reasonable to expect offline MBO algorithms to improve over the performance of the best design seen in the dataset. As we will show in our benchmark results, many of the tasks that we propose do already admit solutions from existing algorithms that exceed the performance of the best sample in the dataset. To provide some intuition for how this can be possible, consider a simple example of offline MBO problems, where the objective function $f(\mathbf{x})$ can be represented as a sum of functions of independent partitions of the design variables,

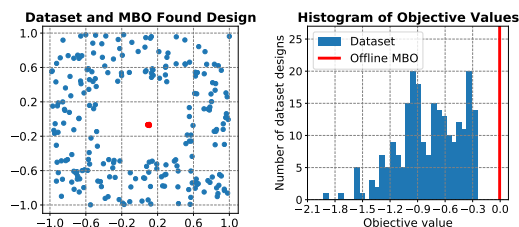


Figure 1: Offline MBO finds designs better than the best in the observed dataset by exploiting compositional structure of the objective function. **Left:** datapoints in a toy quadratic function MBO task over 2D space with optimum at $(0.0, 0.0)$ in blue, MBO found design in red. **Right:** Objective value for optimal design is much higher than that observed in the dataset.

Dataset Name	Size	Cardinality	Categories	Type	Oracle
TF Bind 8	65792	8	4	Discrete	Exact
GFP	56086	237	20	Discrete	Transformer
UTR	280000	50	4	Discrete	Transformer
ChEMBL	40516	425	591	Discrete	CNN
Superconductor	21263	86	N/A	Continuous	Random Forest
Hopper Controller	3200	5126	N/A	Continuous	Exact
Ant Morphology	25009	60	N/A	Continuous	Exact
D’Kitty Morphology	25009	56	N/A	Continuous	Exact

Table 1: **Overview of the tasks in our benchmark suite.** Design-Bench includes a variety of tasks from different domains with both discrete and continuous design spaces and 3 high-dimensional tasks with > 200 design dimensions, making it suitable for benchmarking offline MBO methods.

93 i.e., $f(\mathbf{x}) = f_1(\mathbf{x}[1]) + f_2(\mathbf{x}[2]) + \dots + f_N(\mathbf{x}[N])$, where $\mathbf{x}[1], \dots, \mathbf{x}[N]$ denotes disjoint subsets
94 of design variables \mathbf{x} . The dataset of the offline MBO problem contains optimal design variable for
95 each partition, but not the combination. If an offline MBO algorithm can identify the compositional
96 structure of independent partitions, it would be able to combine the optimal design variable for each
97 partition together to form the overall optimal design and therefore improving the performance over
98 the best design in the dataset. To better demonstrate this idea, we created a toy problem in two
99 dimensions, where the objective function is simply $f(x, y) = -x^2 - y^2$. We collect a dataset of best
100 uniformly sampled x and y from -1 to 1 , but discard the samples that have the combination of best
101 x and y . We then run a naïve gradient ascent algorithm, as we will describe later in this paper. In
102 Figure 1, we can clearly see that our offline MBO algorithm is able to learn to combine the best x
103 and y and produce designs significantly better than the best sample in the dataset. Such a condition
104 appears in a number of scenarios in practice e.g., in reinforcement learning (RL), where the Markov
105 structure provides a natural decomposition satisfying this composition criterion [12] and effective
106 offline RL algorithms are known to exploit this structure [12] or in protein design, where objective
107 such as fluorescence naturally decompose into functions of neighboring Amino acids [7].

108 **What makes offline MBO especially challenging?** The offline nature of the problem prevents
109 the algorithm \mathcal{A} from querying the ground truth objective f with its proposed design candidates,
110 and this makes the offline MBO problem much more difficult than the online design optimization
111 problem. One naïve approach to tackle this problem is to learn a model of the objective function
112 using the dataset, which we can denote $\hat{f}(\mathbf{x})$, and then convert this offline MBO problem into a
113 regular online MBO problem by treating the learned objective model as the true objective. However,
114 this generally does not work: optimizing the design \mathbf{x} with respect to a learned proxy $\hat{f}(\mathbf{x})$ will
115 produce *out-of-distribution* designs that “fool” $\hat{f}(\mathbf{x})$ into outputting a high value, analogously to
116 adversarial examples. Indeed, it is well known that optimizing naïvely with respect to model inputs
117 to obtain a desired output will usually simply “fool” the model [22]. A naïve strategy to address this
118 out-of-distribution issue is to constrain the design to stay close to the data, but this is also problematic,
119 since in order to produce a design that is better than the best training point, it is usually necessary
120 to deviate from the training data at least somewhat. In almost all practical MBO problems, such as
121 optimization over proteins or robot morphologies as we discuss in section 5, designs with the highest
122 objective values typically lie on the tail of the dataset distribution and we may not find them by
123 staying extremely close to the data distribution. This conflict between the need to remain close to the
124 data to avoid out-of-distribution inputs and the need to deviate from the data to produce better designs
125 is one of the core challenges of offline MBO. This challenge is often exacerbated in real-world
126 settings by the high dimensionality of the design space and the sparsity of the available data, as we
127 will show in our benchmark. A good offline MBO method needs to carefully balance these two sides,
128 producing optimized designs that are good, but not too far from the data distribution.

129 3 Related Work

130 Prior work has extensively focused on online or active MBO which requires active querying on
131 the ground truth function, including algorithms using Bayesian optimization and their scalable
132 variants [23, 35, 36, 32, 26], direct search [21], genetic or evolutionary algorithms [41, 25, 45],
133 cross-entropy method [28], simulated annealing [39], etc. While efficient in solving the optimization
134 problem if the ground truth function can be easily evaluated, these methods are not well suited for
135 real-world problems where the ground truth function is expensive to evaluate and therefore prohibitive
136 for active querying. On the other hand, offline MBO that only utilizes an already existing database
137 of designs and objective values, for example, those obtained via previous experiments, presents an

138 attractive algorithmic paradigm towards approaching such scenarios. Since offline MBO prohibits
139 any ability to query the groundtruth objective actively, offline MBO presents different challenges
140 from the typically studied online MBO problem as we discuss in Section 5. We believe that these
141 challenges push the need for a new set of benchmarks to properly evaluate offline MBO methods.

142 The most important components for a good offline MBO benchmark are datasets that capture
143 the challenges of real-world problems. Fortunately, researchers working on a wide variety of
144 scientific fields have already collected many datasets of designs which we can use for training offline
145 MBO algorithms. Sarkisyan et al. [30] analyze the fluorescence of GFP proteins under blue and
146 ultraviolet light, and Brookes et al. [7] use this dataset for optimization to find the protein with the
147 highest fluorescence value. ChEMBL [13] provides a dataset for drug discovery, where molecule
148 activities are measured against a target assay. Hamidieh [16] analyze the critical temperatures for
149 superconductors and provide a dataset to search for room-temperature superconductors with potential
150 in the construction of quantum computers. Some of these datasets have already been employed in the
151 study of offline MBO methods [22, 7, 10]. However, these studies all use different sets of tasks and
152 their evaluation protocols are highly domain-specific, making it difficult to compare across methods.
153 In our benchmark, we incorporate modified variants of some of these datasets along with our own
154 tasks and provide a standardized evaluation protocol. We hope that these tasks can represent realistic
155 MBO problems across a wide range of domains and that the standardized evaluation protocol can
156 facilitate development of new and more powerful offline MBO algorithms.

157 Recently, several methods have been proposed for specifically addressing the offline MBO problem.
158 These methods [22, 7, 10] typically learn models of the objective function and optionally, a generative
159 model [20, 14, 24] of the design manifold and use them for optimization. We discuss these methods
160 in detail in Section 6 and benchmark their performance in Section 7.

161 4 Design-Bench Benchmark Tasks

162 In this section, we describe the set of tasks included in our benchmark. An overview of the tasks is
163 provided in Table 1. Each task in our benchmark suite comes with a dataset $\mathcal{D} = \{(\mathbf{x}_i, y_i)\}$, along
164 with a ground-truth oracle objective function f that can be used for evaluation. An offline MBO
165 algorithm should not query the ground-truth oracle function during training, even for hyperparameter
166 tuning. We first discuss the nature of oracles used in Design-Bench.

167 **Expert model as oracle function.** While in some of the tasks in our benchmark, such as tasks
168 pertaining to robotics (Hopper Controller, D’Kitty Morphology, and Ant Morphology), the oracle
169 functions are evaluated by running computer simulations to obtain the true objective values, in
170 the other tasks, the true objective values can only be obtained by conducting expensive physical
171 experiments. While the eventual aim of offline MBO is to make it possible to optimize designs in
172 precisely such settings, requiring real physical experiments for evaluation makes the design and
173 benchmarking of new algorithms difficult and time consuming. Therefore, to facilitate benchmarking,
174 we follow the evaluation methodology in prior work [7, 10] and use models built by domain experts as
175 our ground-truth oracle functions. Note, however, that the training data provided for offline MBO is
176 still real data – the domain expert model is used *only* to evaluate the result for benchmarking purposes.
177 In many cases, these expert models are *also* learned, but with representations that are hand-designed,
178 with built-in domain-specific inductive biases. The ground-truth oracle models are also trained on
179 much more data than is made available for solving the offline MBO problem, which increases the
180 likelihood that this expert model can provide an accurate evaluation of solutions found by offline
181 MBO, even if they lie outside the training distribution. While this approach to evaluation diminishes
182 the realism of our benchmark since these proxy “true functions” may not always be accurate, we
183 believe that this trade off is worthwhile to make benchmarking practical. The main purpose of our
184 benchmark is to facilitate the evaluation and development of offline MBO algorithms, and we believe
185 that it is important to include tasks in domains where the true objective values can only be obtained
186 via physical experiments, which make up a large portion of the real-world MBO problems. We
187 provide further analysis of the fidelity of our expert model oracles in Appendix F.

188 We now provide a detailed description of the tasks in our benchmark. A description of the data
189 collection strategy and the data pre-processing strategy can be found in Appendix A.

190 **GFP: protein fluorescence maximization.** The goal of this task is to design a derivative protein
191 from the *Aequorea victoria* green fluorescent protein (GFP) that has maximum fluorescence, using
192 a real-world dataset mapping proteins to fluorescence collected by Sarkisyan et al. [30]. While we

193 cannot precisely evaluate any novel protein, we employ an expert Transformer regression model [27]
194 as the oracle function, following the convention in prior work [7, 10]. Our Transformer is trained
195 on the complete GFP dataset containing 56,086 proteins and corresponding fluorescence values.
196 The model achieves a final Spearman’s rank-correlation coefficient with a held-out validation set of
197 0.8497. The design space is discrete, consisting of sequences of 237 categorical variables that take
198 one of 20 options, which corresponds to a sequence of amino acids.

199 **TF Bind 8 and UTR: DNA sequence optimization.** The goal of TF Bind 8 is to find the length-8
200 DNA sequence with maximum binding affinity with a particular transcription factor (SIX6_REF_R1
201 by default). The ground truth binding affinities for all 65,792 designs are available [5]. The goal of
202 the UTR task is to find a human length-50 5’UTR DNA sequence that maximizes the expression level
203 of its corresponding gene. Following Sample et al. [29], we train a Transformer oracle to predict
204 ribosome load from length-50 DNA sequences. The Transformer is trained on the entire UTR dataset
205 used in Sample et al. [29], consisting of 280,000 DNA sequences and measured ribosome loads. The
206 oracle achieves a final Spearman’s rank-correlation with a held-out validation set of 0.8617. The
207 design space consists of sequences of one of four categorical variables, one for each nucleotide.

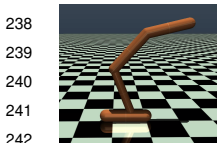
208 **ChEMBL: molecule design via SMILES [40] strings.** This task is taken from the domain of drug
209 discovery with the goal to design the SMILES [40] string of a molecule that exhibits high activity
210 with a target assay. We adapt the ChEMBL [13] dataset and choose the standard type GI50 and
211 ASSAY_ChEMBL_ID ChEMBL1964047, resulting in a dataset of 40,516 pairs of SMILES strings
212 and GI50 values. The true GI50 value can only be determined by physical experiments, so we train a
213 convnet oracle to predict GI50 values from SMILES on all 40,516 examples, which achieves a final
214 Spearman’s rank-correlation on a held-out validation set of 0.3208. The design space is a sequence of
215 425 categorical variables that take any of 591 options, representing tokenized SMILES strings.

216 **Superconductor: critical temperature maximization.** The Superconductor task is taken from the
217 domain of materials science, where the goal is to design the chemical formula for a superconducting
218 material that has a high critical temperature. We adapt a real-world dataset proposed by Hamidieh
219 [16]. The dataset contains 21263 superconductors annotated with critical temperatures. Prior work
220 has employed this dataset for the study of offline MBO methods [10], and we follow their convention
221 using a random forest regression model, detailed in [16], for our oracle. The model achieves a final
222 Spearman’s rank-correlation coefficient with a held-out validation set of 0.9210. The design space
223 for Superconductor is a vector with 86 real-valued components representing the mixture of elements
224 by number of atoms in the chemical formula of each superconductor.

225 **Ant and D’Kitty Morphology: robot morphology optimization.** The goal
226 is to optimize the morphological structure of two simulated robots: Ant from
227 OpenAI Gym [6] and D’Kitty from ROBEL [1]. For Ant Morphology, the
228 we need to optimize the morphology of a quadruped robot, to run as fast as
229 possible, with a pre-trained neural network controller. For D’Kitty Morphology,
230 the goal is to optimize the morphology of D’Kitty robot (shown on the right),
231 such that a pre-trained neural network controller can navigate the robot to a



232 fixed location. Thus the goal is to find morphologies optimal for the pre-trained controller. The
233 pre-trained neural network controller is a morphology conditioned action predictor trained to work
234 well on a large range of morphologies. The morphology parameters of both robots include size,
235 orientation, and location of the limbs, giving us 60 continuous values in total for Ant and 56 for
236 D’Kitty. To evaluate a given design, we run robotic simulation in MuJoCo [37] for 100 time steps,
237 averaging 16 independent trials giving us reliable but cheap to compute estimates.



238 **Hopper Controller: robot neural network controller optimization.** The goal in
239 this task is to optimize the weights of a neural network policy so as to maximize the
240 expected discounted return on the Hopper-v2 locomotion task in OpenAI Gym [6].
241 While this might appear similar to reinforcement learning (RL), our formulation is
242 distinct: unlike RL, we don’t have access to any form of trajectory data in the dataset.
243 Instead, our dataset only comprises of neural network controller weights and the corresponding return
244 values, which invalidates the applicability of conventional RL methods. We evaluate the true objective
245 value of any design by running 1000 steps of simulation in the MuJoCo simulator conventionally
246 used with this environment. The design space of this task is high-dimensional with 5126 continuous
247 variables corresponding to the flattened weights of a neural network controller. The dataset is collected
248 by training a PPO [31] and recording the agent’s weights every 10,000 samples.

249 **5 Task Properties, Challenges, and Considerations**

250 The primary goal of our proposed benchmark is to provide a general test bench for developing,
 251 evaluating, and comparing algorithms for offline MBO. While in principle any online active black-
 252 box optimization problem can be formulated into an offline MBO problem by collecting a dataset
 253 of designs and corresponding objective measurements, it is important to pick a subset of tasks
 254 that represent the challenges of real-world problems in order to convincingly evaluate algorithms
 255 and obtain insights about algorithm behavior. Therefore, several factors must be considered when
 256 choosing the tasks, which we discuss next.

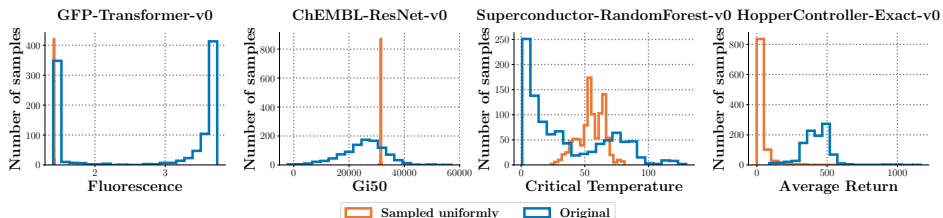


Figure 2: **Histogram (frequency distribution) of objective values in the dataset compared to a uniform re-sampling of the dataset** from the design space. In every case, re-sampling skews the distribution of values to the left, suggesting that there exists a thin manifold of valid designs in the high-dimensional design space, and most of the volume in this space is occupied by low-scoring designs. The distribution of objective values in the dataset are often heavy-tailed, for instance, in the case of ChEMBL and Superconductor.

257 **Diversity and realistically challenging.** First of all, the tasks need to be diverse and realistically
 258 challenging in order to prevent offline MBO algorithms from overfitting to a particular problem
 259 domain and to expect that methods performing well on this benchmark suite would also perform
 260 well on real-world offline MBO problems. Design-Bench consists of tasks that are diverse in many
 261 respects. It includes both tasks with *discrete* and with *continuous* design spaces. Continuous design
 262 spaces, equipped with metric space and ordering structures, could make the problem easier to solve
 263 than discrete design spaces. However, discrete design spaces are finite and therefore might enjoy
 264 better dataset coverage than some continuous tasks. A strong offline MBO algorithm needs to be
 265 able to handle both cases. Further, our tasks have varying dimensionality, ranging from 56 to 5126
 266 dimensions. While our tasks are not intended to directly solve real-world problems (e.g., we don't
 267 actually expect the best robot morphology in our benchmark to actually correspond to the best
 268 possible real robot morphology), they are intended to provide method designers with a representative
 269 sampling of challenges that reflect the kinds of difficulties they would face with real-world datasets,
 270 making them realistically challenging.

271 **High-dimensional design spaces.** In many real-world offline MBO problems, such as drug discov-
 272 ery [13], the design space is *high-dimensional* and the valid designs sparsely lie on a *thin manifold* in
 273 this high-dimensional space. This property poses a unique challenge for many MBO methods: to be
 274 effective on such problem domains, MBO methods need to capture the thin manifold of the design
 275 space to be able to produce valid designs. Prior work [22] has noted that this can be very hard in
 276 practice. In our benchmark, we include GFP, ChEMBL and HopperController tasks with up to 5000
 277 dimensional design spaces to capture this challenge. To intuitively understand this challenge, we
 278 performed a study on some tasks in Figure 2, where we sampled 3200 designs uniformly at random
 279 from the design space and plotted a histogram of the objective values against those in the dataset we
 280 provide, which only consists of valid designs. Observe the discrepancy in objective values, where
 281 randomly sampled designs generally attain objective values much lower than the dataset average.
 282 This indicates that valid designs only lie on a thin manifold in the design space and therefore we are
 283 very unlikely to hit a valid design by random sampling.

284 **Highly sensitive objective function.** Another important challenge that should be taken into con-
 285 sideration is the *high sensitivity* of objective functions, where closeness of two designs in design
 286 space need not correspond to closeness in their objective values, which may differ drastically. This
 287 challenge is naturally present in practical problems like protein synthesis [33], where the change
 288 of a single amino acid could significantly alter the property of the protein. The DKittyMorphology
 289 and AntMorphology tasks in our benchmark suite are also particularly challenging in this direction.
 290 To visualize the high sensitivity of the objective function, we plot a one dimensional slice of the
 291 objective function around a single sample in our dataset in Figure 3. Observe that with other variables
 292 kept the same, slightly altering one variable can significantly reduce the objective value, making it
 293 hard for offline MBO methods to produce the optimal design.

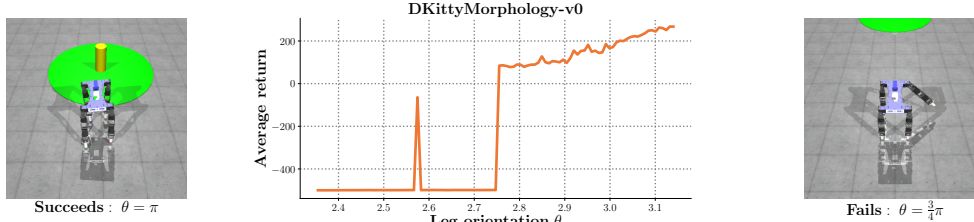


Figure 3: **Highly sensitive landscape of the ground truth objective function in DKittyMorphology.** A small change in a single dimension of the design space, for instance changing the orientation θ (x-axis) of the base of the robot’s front right leg, critically impacts the performance value (y-axis). The robot’s design is the original D’Kitty design and is held constant while varying θ uniformly from $\frac{3}{4}\pi$ to π .

294 **Heavy-tailed data distributions.** Finally, another challenging property for offline MBO methods is
 295 the shape of the data distribution. Learning algorithms are likely to exhibit poor learning behavior
 296 when the distribution of objective values in the dataset is heavy-tailed. This challenge is often present
 297 in black-box optimization [8] and can hurt the performance of MBO algorithms that use a generative
 298 model as well as those that use a learned model of the objective function. As shown in Figure 2 tasks
 299 in our benchmark exhibit this heavy-tailed structure.

300 6 Algorithm Implementations In Design-Bench

301 To provide a baseline for comparisons in future work, we benchmark a number of recently proposed
 302 offline MBO algorithms on each of our tasks. Since the dimensionality of our tasks ranges from 56 to
 303 5126, we chose prior methods that can handle *both* the case of offline training data (i.e., no active
 304 interaction) and high-dimensional inputs. Thus, we include MINs [22], CbAS [7], autofocusing
 305 CbAS [10] and REINFORCE/CMA-ES [43] in our comparisons, along with a baseline naïve “gradient
 306 ascent” method that approximates the true function $f(\mathbf{x})$ with a deep neural network and then performs
 307 gradient ascent on the output of this model. In this section, we briefly discuss these algorithms, before
 308 performing a comparative evaluation in the next section. Our implementation of these algorithms are
 309 open sourced and can be found at github.com/brandontrabucco/design-baselines.

310 **Gradient ascent (Grad).** This is a simple baseline that learns a model of the objective function,
 311 $\hat{f}(\mathbf{x})$, and optimizes \mathbf{x} against this learned model via gradient ascent. Formally, the optimal solution
 312 \mathbf{x}^* generated by this method can be computed as a fixed point of the following update: $\mathbf{x}_{t+1} \leftarrow$
 313 $\mathbf{x}_t + \alpha \nabla_{\mathbf{x}} \hat{f}(\mathbf{x})|_{\mathbf{x}=\mathbf{x}_t}$. In practice we perform $T = 200$ gradient steps, and report \mathbf{x}_T as the final
 314 solution. Such methods are susceptible to producing invalid solutions, since the learned model does
 315 not capture the manifold of valid-designs and hence cannot constrain the resulting \mathbf{x}_T to be on the
 316 manifold. We additionally evaluate a variant (**Grad. Min**) optimizing over the minimum prediction
 317 of $N = 5$ learned objective functions in an ensemble of learned objective functions and (**Grad.**
 318 **Mean**) that optimizes the mean ensemble prediction. We discuss additional tricks (e.g., normalization
 319 of inputs and outputs) that we found beneficial with this baseline in Appendix D.

320 **Covariance matrix adaptation (CMA-ES).** CMA-ES Hansen [17] is a simple optimization algo-
 321 rithm that maintains a belief distribution over the optimal design, and gradually refines this distribution
 322 by adapting the covariance matrix using feedback from a (learned) objective function, $\hat{f}(\mathbf{x})$. Formally,
 323 let $\mathbf{x}_t \sim \mathcal{N}(\mu_t, \Sigma_t)$ be the samples obtained from the distribution at an iteration t , then CMA-ES
 324 computes the value of learned $\hat{f}(\mathbf{x}_t)$ on samples \mathbf{x}_t , and fits Σ_{t+1} to the highest scoring fraction of
 325 these samples and repeats this multiple times. The learned $\hat{f}(\mathbf{x})$ is trained via supervised regression.

326 **REINFORCE [43].** We also evaluated a method that optimizes a learned objective function, $\hat{f}(\mathbf{x})$,
 327 using the REINFORCE-style policy-gradient estimator. REINFORCE is capable of handling non-
 328 smooth and highly stochastic objectives, making it an effective choice. This method parameterizes
 329 a distribution $\pi_{\theta}(\mathbf{x})$ over the design space and then updates the parameters θ of this distribution
 330 towards the design that maximizes $\hat{f}(\mathbf{x})$, using the gradient, $\mathbb{E}_{\mathbf{x} \sim \pi_{\theta}(\mathbf{x})}[\nabla_{\theta} \log \pi_{\theta}(\mathbf{x}) \cdot \hat{f}(\mathbf{x})]$. We train
 331 an ensemble of $\hat{f}(\mathbf{x})$ models and pick the subset of models that satisfy a validation loss threshold τ .
 332 This threshold is task-specific; for example, $\tau \leq 0.25$ is sufficient for Superconductor-v0.

333 **Conditioning by adaptive sampling (CbAS) [7].** CbAS learns a density model in the space of
 334 design inputs, $p_0(\mathbf{x})$ that approximates the data distribution and gradually adapts it towards the
 335 optimized solution \mathbf{x}^* . In a particular iteration t , CbAS alternates between (1) training a variational
 336 auto-encoder (VAE) [20] on a set of samples generated from the previous model $\mathcal{D}_t = \{\mathbf{x}_i\}_{i=1}^m$; $\mathbf{x}_i \sim$

337 $p_{t-1}(\cdot)$ using a weighted version of the standard ELBO objective biased towards *estimated* better
 338 designs and (2) generating new design samples from the autoencoder to serve as $\mathcal{D}_{t+1} = \{\mathbf{x}_i | \mathbf{x}_i \sim$
 339 $p_t(\cdot)\}$. In order to estimate the objective values for designs sampled from the learned density model
 340 $p_t(\mathbf{x})$, CbAS utilizes separately trained models of the objective function, $\hat{f}(\mathbf{x})$ trained via supervised
 341 regression. This training process, at a given iteration t , is:

$$p_{t+1}(\mathbf{x}) := \arg \min_p \frac{1}{m} \sum_{i=1}^m \frac{p_0(\mathbf{x}_i)}{p_t(\mathbf{x}_i)} P(\hat{f}(\mathbf{x}_i) \geq \tau) \log p_t(\mathbf{x}_i)$$

where $\{\mathbf{x}_i\}_{i=1}^m \sim p_t(\cdot)$. (2)

342 **Autofocused CbAS (Auto. CbAS) [10].** Since CbAS uses a learned model of the objective function
 343 $\hat{f}(\mathbf{x})$ to iteratively adapt the generative model $p(\mathbf{x})$ towards the optimized design, the function $\hat{f}(\mathbf{x})$
 344 will inevitably be required to make predictions on shifting design distributions $p_t(\mathbf{x})$. Hence, any
 345 inaccuracy in these values can adversely affect the optimization procedure. Autofocused CbAS aims
 346 to correct for this shift by re-training $\hat{f}(\mathbf{x})$ (now denoted $\hat{f}_t(\mathbf{x})$) under the design distribution given
 347 by the current model, $p_t(\mathbf{x})$ via importance sampling, which is then fed into CbAS.

$$\hat{f}_{t+1} := \arg \min_{\hat{f}} \frac{1}{|\mathcal{D}|} \sum_{i=1}^{|\mathcal{D}|} \frac{p_t(\mathbf{x}_i)}{p_0(\mathbf{x}_i)} \cdot \left(\hat{f}(\mathbf{x}_i) - y_i \right)^2,$$

348 **Model inversion networks (MINs) [22].** MINs learn an inverse map from the objective value to
 349 a design, $\hat{f}^{-1} : \mathcal{Y} \rightarrow \mathcal{X}$ by using objective-conditioned inverse maps, search for optimal y values
 350 during optimization and finally query the learned inverse map to produce the corresponding optimal
 351 design. MIN minimizes a divergence measure $\mathcal{L}_p(\mathcal{D}) := \mathbb{E}_{y \sim p_{\mathcal{D}}(y)} \left[D(p_{\mathcal{D}}(\mathbf{x}|y), \hat{f}^{-1}(\mathbf{x}|y)) \right]$ to train
 352 such an inverse map. During optimization, MINs obtain the optimal y -value that is used to query the
 353 inverse map, and obtains the optimized design by sampling from the inverse map.

354 **Bayesian optimization (BO-qEI).** We perform offline Bayesian optimization to maximize the value
 355 of a learned objective function, $\hat{f}(\mathbf{x})$, by fitting a Gaussian Process, proposing candidate solutions,
 356 and labeling these candidates using $\hat{f}(\mathbf{x})$. To improve efficiency, we choose the quasi-Expected-
 357 Improvement acquisition function [44], and the implementation from the BoTorch framework [4].

358 7 Benchmarking Prior Methods

359 In this section, we provide a comparison of prior algorithms discussed in Section 6 on our proposed
 360 tasks. For purposes of standardization, easy benchmarking, and future algorithm development,
 361 we present results for all Design-Bench tasks in Table 2. As discussed in Section 2, we provide
 362 each method with a dataset, and allow it to produce $K = 128$ optimized design candidates. These
 363 $K = 128$ candidates are then evaluated with the oracle function, and we report the 100th percentile
 364 performance among them averaged over 8 independent runs, following convention in prior offline
 365 MBO work [10, 7, 22]. We also provide unofimralized and 50th%ile results in Appendices C.3, C.2.

366 **Algorithm setup and hyperparameter tuning.** Since our goal is to generate high-performing
 367 solutions without *any* knowledge of the ground truth function, any form of hyperparameter tuning
 368 on the parameters of the learned model should crucially respect this evaluation boundary and tuning
 369 must be performed completely offline, agnostic of the objective function. We provide a recommended
 370 method for tuning each algorithm described in Section 6 in Appendix E, which also serves as a set of
 371 guidelines for tuning future methods with similar components.

372 To briefly summarize, **for CbAS**, hyperparameter tuning amounts to finding a stable configuration for
 373 a VAE, such that samples from the prior distribution map to on-manifold designs after reconstruction.
 374 We empirically found that a β -VAE was essential for stability of CbAS—and high values of $\beta > 1$
 375 are especially important for modelling high-dimensional spaces like that of HopperController. As a
 376 general task-agnostic principle for selecting β , we choose the smallest β such that the VAE’s latent
 377 space does not collapse during importance sampling. Collapsing latent-spaces seem to coincide with
 378 diverging importance sampling, and the VAE’s reconstructions collapsing to a single mode. **For**
 379 **MINs**, hyperparameter tuning amounts to fitting a good generative model. We observe that MINs
 380 is particularly sensitive to the scale of y_i when conditioning, which we resolve by normalizing the
 381 objective values. We implement MINs using WGAN-GP, and find that similar hyperparameters work
 382 well-across domains. **For Gradient Ascent**, while prior work has generally obtained extremely poor
 383 performance for naïve gradient ascent based optimization procedures on top of learned models of

the objective function, we find that by normalizing the designs \mathbf{x} and objective values y to have unit Gaussian statistics, and by multiplying the learning rate $\alpha \leftarrow \alpha\sqrt{d}$ where d is the dimension of the design space (discussed in Appendix D), a naïve gradient ascent based procedure performs reasonably well on most tasks without task-specific tuning. For discrete tasks, only the objective values are normalized, and optimization is performed over log-probabilities of designs. We then uniformly evaluate samples obtained by running 200 steps of gradient ascent starting from the top scoring 128 samples in each dataset. Tuning instructions for each baseline are available in Appendix E.

Results. The results for all tasks are provided in Table 2. There are several takeaways from these results. First, these results indicate that there is no clear winner between the three prior offline MBO methods (MINs, CbAS, and Autofocused CbAS), provided they are all trained offline with no access to ground truth evaluation for any form of hyperparameter tuning. Furthermore, perhaps somewhat surprisingly, a naïve gradient ascent baseline is competitive

	GFP	TF Bind 8	UTR	ChEMBL
Auto. CbAS	0.865 ± 0.000	0.910 ± 0.044	0.650 ± 0.006	0.470 ± 0.000
CbAS	0.865 ± 0.000	0.927 ± 0.051	0.650 ± 0.002	0.517 ± 0.055
BO-qEI	0.254 ± 0.352	0.798 ± 0.083	0.659 ± 0.000	0.333 ± 0.035
CMA-ES	0.054 ± 0.002	0.953 ± 0.022	0.666 ± 0.004	0.350 ± 0.017
Grad.	0.864 ± 0.001	0.977 ± 0.025	0.639 ± 0.009	0.360 ± 0.029
Grad. Min	0.864 ± 0.000	0.984 ± 0.012	0.647 ± 0.007	0.361 ± 0.004
Grad. Mean	0.864 ± 0.000	0.986 ± 0.012	0.647 ± 0.005	0.373 ± 0.013
MINs	0.865 ± 0.001	0.905 ± 0.052	0.649 ± 0.004	0.473 ± 0.057
REINFORCE	0.865 ± 0.000	0.948 ± 0.028	0.646 ± 0.005	0.459 ± 0.036
	Superconductor	Ant Morphology	DKitty Morphology	Hopper Controller
Auto. CbAS	0.421 ± 0.045	0.884 ± 0.046	0.906 ± 0.006	0.137 ± 0.005
CbAS	0.503 ± 0.069	0.879 ± 0.032	0.892 ± 0.008	0.141 ± 0.012
BO-qEI	0.402 ± 0.034	0.820 ± 0.000	0.896 ± 0.000	0.550 ± 0.118
CMA-ES	0.465 ± 0.024	1.219 ± 0.738	0.724 ± 0.001	0.604 ± 0.215
Grad.	0.518 ± 0.024	0.291 ± 0.023	0.874 ± 0.022	1.035 ± 0.482
Grad. Min	0.506 ± 0.009	0.478 ± 0.064	0.889 ± 0.011	1.391 ± 0.589
Grad. Mean	0.499 ± 0.017	0.444 ± 0.081	0.892 ± 0.011	1.586 ± 0.454
MINs	0.469 ± 0.023	0.916 ± 0.036	0.945 ± 0.012	0.424 ± 0.166
REINFORCE	0.481 ± 0.013	0.263 ± 0.032	0.562 ± 0.196	-0.020 ± 0.067

Table 2: **100th percentile** evaluations. Results are averaged over 8 trials, and \pm indicates the standard deviation of the reported objective value. For a description of the objective normalization methodology, please refer to Appendix C.1. *The MINs result for ChEMBL is missing because the MINs architecture does not fit into our computational budget. We will update our GitHub when the result is ready.

with several highly sophisticated MBO methods in 4 out of 8 tasks (Table 2), especially on high-dimensional tasks (e.g., HopperController). This result suggests that it might be difficult for generative models to capture high-dimensional task distributions with enough precision to be used for optimization, and in a number of tasks, these components might be unnecessary. However, on the other hand, as described in Appendix D and E.4, this simple baseline is also sensitive to certain design choices such as input normalization schemes and the number of optimization steps T . Therefore, while not a full-fledged offline MBO method, we believe that gradient ascent has potential to form a fundamental building block for future offline MBO methods. Finally, we remark that the performance of methods in Table 2 differ from the those reported by prior works. This difference stems from the standardization procedure employed in dataset generation (which we discuss in Appendix A), and the use of task-agnostic, uniform hyperparameter tuning.

8 Discussion and Conclusion

Offline MBO carries the promise to convert existing databases of designs into powerful optimizers, without the need for expensive real-world experiments for actively querying the ground truth objective function. However, due to the lack of standardized benchmarks and evaluation protocols, it has been difficult to accurately track the progress of offline MBO methods. To address this problem, we introduce Design-Bench, a benchmark suite of offline MBO tasks that covers a wide variety of domains, and both continuous and discrete, low and high dimensional design spaces. We provide a comprehensive evaluation of existing methods under identical assumptions. The comparatively high efficacy of even simple baselines such as naïve gradient ascent suggests the need for careful tuning and standardization of methods in this area. An interesting avenue for future work in offline MBO is to devise methods that can be used to perform model-selection and hyperparameter selection. One approach to address this problem is to devise methods for offline evaluation of produced solutions, which is also an interesting topic for future work. We hope that our benchmark will be adopted as the standard metric in evaluating offline MBO algorithms and provides insight in future algorithm development. Since our benchmark aims to standardize the evaluation of offline MBO, we note that while it may have both positive (e.g., enhancing human life quality via automation) and negative (e.g., loss of jobs) impact on society, all these impacts are more broadly applicable to offline MBO algorithms in general and not specifically to this work.

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588 **Checklist**

- 589 1. For all authors...
- 590 (a) Do the main claims made in the abstract and introduction accurately reflect the paper’s
591 contributions and scope? [Yes]
- 592 (b) Did you describe the limitations of your work? [Yes] See Section 8.
- 593 (c) Did you discuss any potential negative societal impacts of your work? [Yes] See
594 Section 8.
- 595 (d) Have you read the ethics review guidelines and ensured that your paper conforms to
596 them? [Yes]
- 597 2. If you are including theoretical results...
- 598 (a) Did you state the full set of assumptions of all theoretical results? [N/A]
- 599 (b) Did you include complete proofs of all theoretical results? [N/A]
- 600 3. If you ran experiments (e.g. for benchmarks)...
- 601 (a) Did you include the code, data, and instructions needed to reproduce the main ex-
602 perimental results (either in the supplemental material or as a URL)? [Yes] See
603 github.com/brandonrabucco/design-bench and github.com/brandonrabucco/design-baselines.
604
- 605 (b) Did you specify all the training details (e.g., data splits, hyperparameters, how they
606 were chosen)? [Yes] See Appendix E
- 607 (c) Did you report error bars (e.g., with respect to the random seed after running experi-
608 ments multiple times)? [Yes]
- 609 (d) Did you include the total amount of compute and the type of resources used (e.g., type
610 of GPUs, internal cluster, or cloud provider)? [Yes] See Appendix C.4.
- 611 4. If you are using existing assets (e.g., code, data, models) or curating/releasing new assets...
- 612 (a) If your work uses existing assets, did you cite the creators? [Yes]
- 613 (b) Did you mention the license of the assets? [Yes] The license is included in the [GitHub](#)
614 [repository](#) for our benchmark.
- 615 (c) Did you include any new assets either in the supplemental material or as a URL? [Yes]
616 All materials we use are open sourced in our [GitHub repository](#).
- 617 (d) Did you discuss whether and how consent was obtained from people whose data you’re
618 using/curating? [Yes] All the data we use are open source and we do not include any
619 data collected from human experiment.
- 620 (e) Did you discuss whether the data you are using/curating contains personally identifiable
621 information or offensive content? [N/A] All the data we use are collected from natural
622 science experiments without any human data.
- 623 5. If you used crowdsourcing or conducted research with human subjects...
- 624 (a) Did you include the full text of instructions given to participants and screenshots, if
625 applicable? [N/A]
- 626 (b) Did you describe any potential participant risks, with links to Institutional Review
627 Board (IRB) approvals, if applicable? [N/A]
- 628 (c) Did you include the estimated hourly wage paid to participants and the total amount
629 spent on participant compensation? [N/A]