ProRefine: Inference-Time Prompt Refinement with Textual Feedback

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Abstract

Agentic workflows, where multiple AI agents collaborate to accomplish complex tasks like reasoning or planning, play a substantial role in many cutting-edge commercial applications, and continue to fascinate researchers across fields for their potential to accomplish expensive, complex tasks that, until recently, only humans have been trusted to do. These workflows depend critically on the prompts used to provide the roles models play in such workflows. Poorly designed prompts that fail even slightly to guide individual agents can lead to sub-optimal performance that may snowball within a system of agents, limiting their reliability and scalability. To address this important problem of inference-time prompt optimization, we introduce ProRefine, an innovative inference-time optimization method that uses an agentic loop of LLMs to generate and apply textual feedback. ProRefine dynamically refines prompts for multi-step reasoning tasks without additional training or ground truth labels. Evaluated on five benchmark mathematical reasoning datasets, ProRefine significantly surpasses zero-shot Chain-of-Thought baselines by 3 to 37 percentage points. This approach not only boosts accuracy but also allows smaller models to approach the performance of their larger counterparts. This highlights its potential for building more cost-effective and powerful hybrid AI systems, thereby democratizing access to high-performing AI.

1 Introduction

The advancement of Large Language Models (LLMs) is intrinsically linked to their alignment with human values and preferences [10]. While Reinforcement Learning from Human Feedback (RLHF) has been the cornerstone of this effort [5], recent research has pivoted towards using LLMs themselves as scalable proxies for human judgment, serving as evaluators, critics, and sources of feedback [47, 23, 27]. This has given rise to sophisticated agentic frameworks that can detect errors, critique outputs, and iteratively refine them, particularly for tasks demanding factual correctness [1, 17]. Methods like TextGrad have even demonstrated how textual feedback can "differentiate" through complex systems to optimize performance [43].

Our work focuses on optimizing the *prompt*, a key element in chain-of-thought (CoT) [40] based LLM reasoning. Although prior work has explored prompt optimization [7, 8, 29, 41], they all often focus on either *offline fine-tuning*, which requires extensive training data, or universal application of *largest, most capable models to every task*. This presents a practical dilemma in many real-world scenarios. Continuously fine-tuning is not always feasible, and relying exclusively on state-of-the-art models is often computationally prohibitive. A different approach is needed for scenarios that require *dynamic, on-the-fly repair* for specific and difficult queries where a standard prompt fails. This is

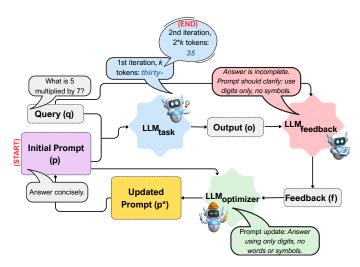


Figure 1: Overview of ProRefine system, illustrating the iterative process of prompt optimization using feedback from LLMs. In each iteration, LLM_{task} extends its output by an additional k tokens, enabling step-by-step feedback to progressively refine the prompt with $LLM_{optimizer}$.

particularly true in *resource-aware deployments*, where a smaller model may suffice for most tasks but requires enhancement for a small subset of critical queries. *The goal, therefore, shifts from finding a single, universally optimal prompt to performing targeted, inference-time intervention.*

To address this need, we introduce **ProRefine** (Inference-time **Pro**mpt **Refine**ment with Textual Feedback), which builds upon CoT by adaptively improving prompts using feedback ($LLM_{feedback}$) and an optimizer ($LLM_{optimizer}$) to refine prompts for the task-performing LLM (LLM_{task}). This workflow (Figure 1), motivated by the teacher-student framework [35] where a teacher agent guides a student agent to perform a task by providing feedback at intermediate steps, but implemented via LLM interactions without pre-training, represents a novel approach to adaptive agentic reasoning. We explore policy optimization for aligning compound AI systems, drawing inspiration from TextGrad and policy gradient algorithms, such as PPO.

This hybrid-model paradigm makes a method like ProRefine a practical solution. It is designed for resource-constrained environments where deploying the largest models for every query isn't feasible, but temporary access to a capable feedback LLM (perhaps via a separate API call) is possible for critical tasks. In such cases, the refinement process is triggered as an on-demand "expert intervention." ProRefine is task-agnostic and requires no additional training or ground-truth labels. It is an inference-time optimization method that relies on the availability of test-time compute and the ability of LLMs to provide and act upon feedback for optimization.

The ability to break complex tasks into smaller steps and dynamically improve prompts offers a crucial advantage in multi-step agentic workflows where errors can compound. As illustrated in Figure 4 in the Appendix, This method is also suitable for black-box LLMs where only API access is available. ProRefine could prove to be crucial in situations demanding greater interpretability, where feedback steps (outputs of $LLM_{feedback}$) offer insights into the reasoning correction process and applications requiring dynamic adaptation without retraining/fine-tuning cycles. To demonstrate its effectiveness, we evaluate ProRefine across five benchmark mathematical reasoning datasets, showing it offers a robust alternative to solely scaling up the base model for all queries.

Key Contributions:

- We propose a novel method ProRefine for prompt optimization at inference-time using textual feedback.
- We evaluated ProRefine on five datasets: object counting, word sorting, grade-school math problem solving, math word problems, and algebraic word problems, and compared our method against CoT and TextGrad.
- We evaluate the importance of using a verifier at inference time.

2 ProRefine

Algorithm 1: ProRefine

ProRefine is an inference-time prompt optimization algorithm that optimizes prompts by using textual feedback. ProRefine involves interactions between three LLMs:

 LLM_{task} : Executes the task based on the current prompt, generating the initial and subsequent outputs.

 $LLM_{feedback}$: A model that critiques the LLM_{task} 's output, providing detailed feedback on improvements. This model should be capable of providing insightful and accurate critiques [2, 27].

 $LLM_{optimizer}$: Interprets the feedback and refines the prompt, aiming for coherent and task-focused improvements. This LLM is crucial for ensuring the prompt evolves effectively.

ProRefine (Algorithm 1) works as follows¹:

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Input: Query: q, Initial prompt: p, tokens_per_step: k, max_steps: n, LLMs: LLM_{task}, LLM_{feedback}, LLM_{optimizer}

Output: Optimized prompt: p^*
p^* = p
for i = 1 to n do
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f_i = LLM_{feedback}(q,o_i) // Get textual feedback p* = LLM_{optimizer}(p^*,f_i) // Optimize the prompt if EOS\_token\ in\ o_i then \ \ \ \  break
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 $o_i = LLM_{task}(p^*,q)$ // Generate i*k tokens

return p^* // Return final optimized prompt

Initialization: Start with an initial prompt p for the task, a query q, and parameters defining the generation and optimization process (k tokens per step, n maximum steps).

Generation and Feedback Loop:

- Generation: Use LLM_{task} to generate an output based on the current prompt p^* and query q. This step is limited to i*k tokens to control the granularity of the feedback. In each iteration, LLM_{task} produces k more tokens, attempting to refine prior output while progressively continuing its response to the query.
- **Feedback:** $LLM_{feedback}$ evaluates the generated output o_i against the query q to provide textual feedback f_i . This feedback encapsulates how the output could be improved, focusing on aspects such as accuracy, relevance, or coherence.
- Optimization: $LLM_{optimizer}$ uses the feedback f_i to refine the prompt p^* . This step involves modifying the prompt to better align with the task requirements or to correct identified deficiencies in previous generations.

Termination: The process iterates until either the maximum number of steps n is reached or an end-of-sequence (EOS) token is detected in the output, indicating the completion of the task.

The granularity and duration of the optimization process are governed by two parameters: k, the number of tokens per step, and n, the maximum number of steps. These parameters can be adjusted according to the task's complexity and the desired output quality. For example, rather than generating feedback every k tokens, we might instead choose to provide feedback after each sentence or paragraph, particularly in tasks such as machine translation or text summarization, where larger semantic units may be more meaningful.

¹The code is available at https://github.com/deepakpandita57/ProRefine_public

Unifying Verifier and Feedback: At inference time, verifiers play a crucial role in judging model outputs [6, 14, 31]. For simplicity in this study, we do not train a bespoke verifier; rather, we employ the Llama3.1-70B-instruct model to function as both the feedback mechanism ($LLM_{feedback}$) and the verifier. We manage these roles through separate API calls, each with a role-defining prompt. A smaller model, specifically fine-tuned for these tasks, could also be used. The verifier's function is to evaluate the initial output generated by LLM_{task} for each query. If the verifier assesses the output to be incorrect, the refinement process is triggered; otherwise, the output is used as is. This also saves computation on answers that are already correct.

To quantify the verifier's impact, we analyze three distinct scenarios: ProRefine (verifier), our standard approach which employs $LLM_{feedback}$ to guide refinement; ProRefine (no verifier), wherein the refinement process operates without verifier input; and ProRefine (optimal verifier), guided by a perfect verifier (simulated using ground-truth labels). This optimal condition reveals the upper bound of the refinement loop's potential. Consequently, the performance difference between ProRefine (verifier) and ProRefine (optimal verifier) underscores the significance of verifier accuracy. It is important to note that ProRefine's methodology does not inherently rely on labels or optimal verification, despite their use in this specific evaluation.

3 Experiments and Evaluation

Dataset	Method	Llama-3.2 1B-it	Llama-3.2 3B-it	Llama-3.1 8B-it
Object Counting	CoT	0.48 [0.382, 0.578]	0.65 [0.556, 0.744]	0.73 [0.643, 0.817]
	TextGrad	0.62 [0.524, 0.716]	0.73 [0.643, 0.817]	0.86 [0.792, 0.928]
	ProRefine (no verifier)	0.51 [0.412, 0.608]	0.75 [0.665, 0.835]	0.77 [0.687, 0.853]
	ProRefine (verifier)	0.6 [0.503, 0.696]	0.72 [0.632, 0.808]	0.89 * [0.839, 0.959]
	ProRefine (optimal verifier)	0.67 [0.577, 0.763]	0.85 [0.780, 0.920]	0.94* [0.893, 0.987]
Word Sorting	CoT	0.11 [0.048, 0.172]	0.10 [0.041, 0.159]	0.50 [0.401, 0.598]
	TextGrad	0.33 * [0.237, 0.423]	0.61 * [0.514, 0.706]	0.69* [0.599, 0.781]
	ProRefine (no verifier)	0.22 [0.138, 0.302]	0.47* [0.372, 0.568]	0.68 [0.595, 0.779]
	ProRefine (verifier)	0.19 [0.113, 0.267]	0.32* [0.228, 0.412]	0.71 * [0.621, 0.799]
	†ProRefine (optimal verifier)	0.29* [0.192, 0.368]	0.53* [0.432, 0.628]	0.86** [0.792, 0.928]
GSM8K	CoT	0.450 [0.423, 0.476]	0.809 [0.787, 0.829]	0.819 [0.797, 0.839]
	TextGrad	0.463 [0.436, 0.489]	0.801 [0.779, 0.822]	0.864* [0.845, 0.882]
	ProRefine (no verifier)	0.636** [0.610, 0.662]	0.797 [0.774, 0.818]	0.843 [0.823, 0.863
	ProRefine (verifier)	0.654 ** [0.627, 0.678]	0.866 ** [0.847, 0.883]	0.885 * [0.868, 0.902]
	[†] ProRefine (optimal verifier)	0.725** [0.701, 0.749]	0.904** [0.888, 0.920]	0.936** [0.922, 0.949]
SVAMP	CoT	0.689 [0.66, 0.718]	0.869 [0.848, 0.890]	0.854 [0.832 , 0.876]
	TextGrad	0.684 [0.655, 0.713]	0.861 [0.840, 0.882]	0.84 [0.817, 0.863]
	ProRefine (no verifier)	0.774** [0.748, 0.800]	0.878 [0.858, 0.898]	0.877 [0.857, 0.897]
	ProRefine (verifier)	0.808 ** [0.784, 0.832]	0.896 [0.877, 0.915]	0.893 * [0.874, 0.912]
	*ProRefine (optimal verifier)	0.861** [0.840, 0.882]	0.925** [0.909, 0.941]	0.938** [0.923, 0.953]
AQUARAT	CoT	0.259 [0.202, 0.31]	0.563 [0.498, 0.620]	0.586 [0.522, 0.643]
	TextGrad	0.311 [0.250, 0.364]	0.524 [0.462 , 0.585]	0.559 [0.494, 0.616]
	ProRefine (no verifier)	0.205 [0.151, 0.250]	0.343 [0.284, 0.401]	0.398 [0.337 , 0.458]
	ProRefine (verifier)	0.268 [0.209, 0.318]	0.551 [0.486 , 0.608]	0.606 [0.542, 0.663]
	†ProRefine (optimal verifier)	0.354 [0.292, 0.409]	0.598 [0.538, 0.659]	0.657 [0.595, 0.712]

Table 1: Test Accuracy with 95% confidence intervals across five benchmark datasets and models. * and ** denote statistically significant improvements over one or two baseline methods, respectively. Results in bold indicate the highest accuracy for a dataset-method combination. † demonstrates the upper bound potential of the optimization loop and the impact of verifier quality. *Llama3.1-70B-instruct* is employed for feedback generation, prompt optimization, and evaluation.

3.1 Data

We evaluate ProRefine on five reasoning tasks, each of which involves multi-step reasoning, making them suitable for evaluating prompt optimization in agentic workflows. We utilize object counting and word sorting from the BIG-Bench Hard benchmark [33], grade-school math problem-solving from GSM8K [6], math word problems from SVAMP [22], and algebraic word problems from AQUARAT [15]. See Appendix B for details about data splits.

3.2 Experimental Setup

We experiment with three models - Llama3.2-1B-instruct, Llama3.2-3B-instruct, and Llama3.1-8B-instruct [19] for LLM_{task} . The prompts are optimized using ProRefine, with Llama3.1-70B-instruct used for feedback generation, prompt optimization, and evaluation. We select the values of hyperparameters k=10 and n=25 to control the granularity of feedback and duration of

optimization. Hyperparameters k and n were fixed based on general preliminary exploration and not tuned per task using benchmark training/validation data.

We compare ProRefine against the zero-shot Chain-of-Thought (CoT) baseline and TextGrad [43], and report test accuracy with 95% confidence interval. It is essential to remember that TextGrad is a supervised fine-tuning method that utilizes both the training and validation sets.

3.3 Results

Our results (Table 1) demonstrate that ProRefine significantly improves LLM_{task} performance over the zero-shot CoT baseline in all but one experiment, and it outperforms TextGrad in 11 out of 15 cases overall. For Llama3.2-1B-instruct model, ProRefine can significantly outperform CoT and TextGrad on 2 out of 5 datasets. For Llama3.2-3B-instruct model, ProRefine can outperform CoT and TextGrad on 3 out of 5 datasets with one significant result. For Llama3.1-8B-instruct model, ProRefine can outperform CoT and TextGrad on all 5 datasets with 4 significant results.

Object Counting: ProRefine improves performance by 3-16 percentage points over CoT, with significant gains observed for *Llama3.1-8B-instruct*. It outperforms TextGrad on 2 out of 3 models, yielding a 2-3 percentage point advantage. However, a performance drop of 2 points is observed for *Llama3.2-1B-instruct*.

Word Sorting: Performance gains over CoT range from 8-37 percentage points, with significant improvements for *Llama3.2-3B-instruct* and *Llama3.1-8B-instruct*. ProRefine surpasses TextGrad on 1 of 3 models with a 2-point gain, but performance drops of 11-14 points are observed for *Llama3.2-1B-instruct* and *Llama3.2-3B-instruct*.

GSM8K: ProRefine achieves 2.4-20.4 percentage points improvement over CoT, with significant improvement observed for all the models; however, a slight performance drop (1.2) is observed for Llama3.2-3B-instruct. It outperforms TextGrad on all models, achieving a 2.1-19.1 percentage point gain with significant results observed for Llama3.2-1B-instruct and Llama3.2-3B-instruct models. Minor performance drop of 0.4-2.1 is observed for Llama3.2-3B-instruct and Llama3.1-8B-instruct.

SVAMP: Performance improves by 0.9 - 11.9 percentage points over CoT, with significant gains for *Llama3.2-1B-instruct* and *Llama3.1-8B-instruct*. ProRefine outperforms TextGrad across all models, with 1.7 - 12.4 percentage point gains and significant results for *Llama3.2-1B-instruct*.

AQUARAT: Gains over CoT range from 0.9-2 percentage points, but declines of 5.4-22 points are also observed. ProRefine exceeds TextGrad on 2 of 3 models, with 2.7-4.7 percentage point gains, although performance drops of 10.6-18.1 points are also recorded.

Our results demonstrate that using ProRefine with an optimal verifier significantly improves performance for all tasks, achieving the best results in 13 out of 15 cases, highlighting the critical role of verifier quality. Notably, the number of significant improvements increases with larger model sizes. We also observe that ProRefine enables smaller models, such as *Llama3.2-3B-instruct* and *Llama3.1-8B-instruct*, to approach the zero-shot performance of larger models like *Llama3.1-8B-instruct* and *Llama3.1-70B-instruct*, respectively.

4 Conclusion

We introduced ProRefine, a novel, practical, and *inference-time* prompt optimization method for agentic workflows. ProRefine leverages LLM-generated textual feedback to dynamically refine prompts, leading to significant performance improvements on multi-step reasoning tasks without requiring additional training or ground-truth labels. Our results demonstrate its ability to bridge the performance gap between smaller and larger LLMs, making it a key enabler for more efficient and cost-effective hybrid-model deployments. The *inference-time* nature of ProRefine makes it readily deployable for on-demand reasoning correction, contributing to more adaptable and accessible AI systems. Future work will explore applying this framework to new domains, developing more sophisticated feedback and optimizer agents, and exploring adaptive policies for hyperparameter tuning to further optimize the cost-performance trade-off.

References

- [1] Afra Feyza Akyurek, Ekin Akyurek, Ashwin Kalyan, Peter Clark, Derry Tanti Wijaya, and Niket Tandon. RL4F: Generating natural language feedback with reinforcement learning for repairing model outputs. In Anna Rogers, Jordan Boyd-Graber, and Naoaki Okazaki, editors, *Proceedings of the 61st Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*, pages 7716–7733, Toronto, Canada, July 2023. Association for Computational Linguistics. doi: 10.18653/v1/2023.acl-long.427. URL https://aclanthology.org/2023.acl-long.427/.
- [2] Yuntao Bai, Saurav Kadavath, Sandipan Kundu, Amanda Askell, Jackson Kernion, Andy Jones, Anna Chen, Anna Goldie, Azalia Mirhoseini, Cameron McKinnon, et al. Constitutional ai: Harmlessness from ai feedback. *arXiv preprint arXiv:2212.08073*, 2022.
- [3] Anna Bavaresco, Raffaella Bernardi, Leonardo Bertolazzi, Desmond Elliott, Raquel Fernández, Albert Gatt, Esam Ghaleb, Mario Giulianelli, Michael Hanna, Alexander Koller, André F. T. Martins, Philipp Mondorf, Vera Neplenbroek, Sandro Pezzelle, Barbara Plank, David Schlangen, Alessandro Suglia, Aditya K Surikuchi, Ece Takmaz, and Alberto Testoni. Llms instead of human judges? a large scale empirical study across 20 nlp evaluation tasks, 2024. URL https://arxiv.org/abs/2406.18403.
- [4] Cheng-Han Chiang and Hung-yi Lee. Can large language models be an alternative to human evaluations? In Anna Rogers, Jordan Boyd-Graber, and Naoaki Okazaki, editors, *Proceedings of the 61st Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*, pages 15607–15631, Toronto, Canada, July 2023. Association for Computational Linguistics. doi: 10.18653/v1/2023.acl-long.870. URL https://aclanthology.org/2023.acl-long.870/.
- [5] Paul F Christiano, Jan Leike, Tom Brown, Miljan Martic, Shane Legg, and Dario Amodei. Deep reinforcement learning from human preferences. In I. Guyon, U. Von Luxburg, S. Bengio, H. Wallach, R. Fergus, S. Vishwanathan, and R. Garnett, editors, *Advances in Neural Information Processing Systems*, volume 30. Curran Associates, Inc., 2017. URL https://proceedings.neurips.cc/paper_files/paper/2017/file/d5e2c0adad503c91f91df240d0cd4e49-Paper.pdf.
- [6] Karl Cobbe, Vineet Kosaraju, Mohammad Bavarian, Mark Chen, Heewoo Jun, Lukasz Kaiser, Matthias Plappert, Jerry Tworek, Jacob Hilton, Reiichiro Nakano, et al. Training verifiers to solve math word problems. *arXiv preprint arXiv:2110.14168*, 2021.
- [7] Mingkai Deng, Jianyu Wang, Cheng-Ping Hsieh, Yihan Wang, Han Guo, Tianmin Shu, Meng Song, Eric Xing, and Zhiting Hu. RLPrompt: Optimizing discrete text prompts with reinforcement learning. In Yoav Goldberg, Zornitsa Kozareva, and Yue Zhang, editors, *Proceedings of the 2022 Conference on Empirical Methods in Natural Language Processing*, pages 3369–3391, Abu Dhabi, United Arab Emirates, December 2022. Association for Computational Linguistics. doi: 10.18653/v1/2022.emnlp-main.222. URL https://aclanthology.org/2022.emnlp-main.222/.
- [8] Yihong Dong, Kangcheng Luo, Xue Jiang, Zhi Jin, and Ge Li. PACE: Improving prompt with actor-critic editing for large language model. In Lun-Wei Ku, Andre Martins, and Vivek Srikumar, editors, *Findings of the Association for Computational Linguistics: ACL 2024*, pages 7304–7323, Bangkok, Thailand, August 2024. Association for Computational Linguistics. doi: 10.18653/v1/2024.findings-acl.436. URL https://aclanthology.org/2024.findings-acl.436/.
- [9] Yilun Du, Shuang Li, Antonio Torralba, Joshua B. Tenenbaum, and Igor Mordatch. Improving factuality and reasoning in language models through multiagent debate. In *Forty-first International Conference on Machine Learning*, 2024. URL https://openreview.net/forum?id=zj7YuTE4t8.
- [10] Yicheng Feng, Yuxuan Wang, Jiazheng Liu, Sipeng Zheng, and Zongqing Lu. LLaMA-rider: Spurring large language models to explore the open world. In Kevin Duh, Helena Gomez, and Steven Bethard, editors, Findings of the Association for Computational Linguistics: NAACL

- 2024, pages 4705-4724, Mexico City, Mexico, June 2024. Association for Computational Linguistics. doi: 10.18653/v1/2024.findings-naacl.292. URL https://aclanthology.org/2024.findings-naacl.292/.
- [11] Qianyue Hao, Sibo Li, Jian Yuan, and Yong Li. Rl of thoughts: Navigating llm reasoning with inference-time reinforcement learning, 2025. URL https://arxiv.org/abs/2505.14140.
- [12] Omar Khattab, Arnav Singhvi, Paridhi Maheshwari, Zhiyuan Zhang, Keshav Santhanam, Sri Vardhamanan A, Saiful Haq, Ashutosh Sharma, Thomas T. Joshi, Hanna Moazam, Heather Miller, Matei Zaharia, and Christopher Potts. DSPy: Compiling declarative language model calls into state-of-the-art pipelines. In *The Twelfth International Conference on Learning Representations*, 2024. URL https://openreview.net/forum?id=sY5N0zY50d.
- [13] Zhen Li, Xiaohan Xu, Tao Shen, Can Xu, Jia-Chen Gu, Yuxuan Lai, Chongyang Tao, and Shuai Ma. Leveraging large language models for NLG evaluation: Advances and challenges. In Yaser Al-Onaizan, Mohit Bansal, and Yun-Nung Chen, editors, *Proceedings of the 2024 Conference on Empirical Methods in Natural Language Processing*, pages 16028–16045, Miami, Florida, USA, November 2024. Association for Computational Linguistics. doi: 10.18653/v1/2024. emnlp-main.896. URL https://aclanthology.org/2024.emnlp-main.896/.
- [14] Hunter Lightman, Vineet Kosaraju, Yuri Burda, Harrison Edwards, Bowen Baker, Teddy Lee, Jan Leike, John Schulman, Ilya Sutskever, and Karl Cobbe. Let's Verify Step by Step. In *The Twelfth International Conference on Learning Representations*, October 2024. URL https://openreview.net/forum?id=v8L0pN6E0i.
- [15] Wang Ling, Dani Yogatama, Chris Dyer, and Phil Blunsom. Program induction by rationale generation: Learning to solve and explain algebraic word problems. In Regina Barzilay and Min-Yen Kan, editors, *Proceedings of the 55th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*, pages 158–167, Vancouver, Canada, July 2017. Association for Computational Linguistics. doi: 10.18653/v1/P17-1015. URL https://aclanthology.org/P17-1015/.
- [16] Yang Liu, Dan Iter, Yichong Xu, Shuohang Wang, Ruochen Xu, and Chenguang Zhu. Geval: NLG evaluation using gpt-4 with better human alignment. In Houda Bouamor, Juan Pino, and Kalika Bali, editors, *Proceedings of the 2023 Conference on Empirical Methods in Natural Language Processing*, pages 2511–2522, Singapore, December 2023. Association for Computational Linguistics. doi: 10.18653/v1/2023.emnlp-main.153. URL https://aclanthology.org/2023.emnlp-main.153/.
- [17] Aman Madaan, Niket Tandon, Prakhar Gupta, Skyler Hallinan, Luyu Gao, Sarah Wiegreffe, Uri Alon, Nouha Dziri, Shrimai Prabhumoye, Yiming Yang, Shashank Gupta, Bodhisattwa Prasad Majumder, Katherine Hermann, Sean Welleck, Amir Yazdanbakhsh, and Peter Clark. Self-refine: Iterative refinement with self-feedback. In A. Oh, T. Naumann, A. Globerson, K. Saenko, M. Hardt, and S. Levine, editors, *Advances in Neural Information Processing Systems*, volume 36, pages 46534–46594. Curran Associates, Inc., 2023. URL https://proceedings.neurips.cc/paper_files/paper/2023/file/91edff07232fb1b55a505a9e9f6c0ff3-Paper-Conference.pdf.
- [18] Maitrey Mehta, Valentina Pyatkin, and Vivek Srikumar. Promptly predicting structures: The return of inference. In *Proceedings of the 2024 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies (Volume 1: Long Papers)*, pages 112–130, 2024.
- [19] Meta. llama-models/models/llama3_2/MODEL_card.md at main · meta-llama/llama-models, 2024. URL https://github.com/meta-llama/llama-models/blob/main/models/llama3_2/MODEL_CARD.md.
- [20] Niklas Muennighoff, Zitong Yang, Weijia Shi, Xiang Lisa Li, Li Fei-Fei, Hannaneh Hajishirzi, Luke Zettlemoyer, Percy Liang, Emmanuel Candès, and Tatsunori Hashimoto. s1: Simple test-time scaling. *arXiv preprint arXiv:2501.19393*, 2025.

- [21] Rithesh Murthy, Ming Zhu, Liangwei Yang, Jielin Qiu, Juntao Tan, Shelby Heinecke, Caiming Xiong, Silvio Savarese, and Huan Wang. Promptomatix: An automatic prompt optimization framework for large language models, 2025. URL https://arxiv.org/abs/2507.14241.
- [22] Arkil Patel, Satwik Bhattamishra, and Navin Goyal. Are NLP models really able to solve simple math word problems? In Kristina Toutanova, Anna Rumshisky, Luke Zettlemoyer, Dilek Hakkani-Tur, Iz Beltagy, Steven Bethard, Ryan Cotterell, Tanmoy Chakraborty, and Yichao Zhou, editors, *Proceedings of the 2021 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies*, pages 2080–2094, Online, June 2021. Association for Computational Linguistics. doi: 10.18653/v1/2021. naacl-main.168. URL https://aclanthology.org/2021.naacl-main.168/.
- [23] Reid Pryzant, Dan Iter, Jerry Li, Yin Lee, Chenguang Zhu, and Michael Zeng. Automatic prompt optimization with "gradient descent" and beam search. In Houda Bouamor, Juan Pino, and Kalika Bali, editors, *Proceedings of the 2023 Conference on Empirical Methods in Natural Language Processing*, pages 7957–7968, Singapore, December 2023. Association for Computational Linguistics. doi: 10.18653/v1/2023.emnlp-main.494. URL https://aclanthology.org/2023.emnlp-main.494/.
- [24] Yuxiao Qu, Tianjun Zhang, Naman Garg, and Aviral Kumar. Recursive introspection: Teaching language model agents how to self-improve. In *The Thirty-eighth Annual Conference on Neural Information Processing Systems*, 2024. URL https://openreview.net/forum?id=DRC9pZwBwR.
- [25] Gollam Rabby, Farhana Keya, and Sören Auer. Mc-nest: Enhancing mathematical reasoning in large language models leveraging a monte carlo self-refine tree, 2025. URL https://arxiv. org/abs/2411.15645.
- [26] Leonardo Ranaldi and Andrè Freitas. Self-refine instruction-tuning for aligning reasoning in language models. *arXiv preprint arXiv:2405.00402*, 2024.
- [27] William Saunders, Catherine Yeh, Jeff Wu, Steven Bills, Long Ouyang, Jonathan Ward, and Jan Leike. Self-critiquing models for assisting human evaluators, June 2022. URL http://arxiv.org/abs/2206.05802. arXiv:2206.05802 [cs].
- [28] Timo Schick, Jane A. Yu, Zhengbao Jiang, Fabio Petroni, Patrick Lewis, Gautier Izacard, Qingfei You, Christoforos Nalmpantis, Edouard Grave, and Sebastian Riedel. PEER: A collaborative language model. In *The Eleventh International Conference on Learning Representations*, 2023. URL https://openreview.net/forum?id=KbYevcLjnc.
- [29] Taylor Shin, Yasaman Razeghi, Robert L. Logan IV, Eric Wallace, and Sameer Singh. Auto-Prompt: Eliciting Knowledge from Language Models with Automatically Generated Prompts. In Bonnie Webber, Trevor Cohn, Yulan He, and Yang Liu, editors, *Proceedings of the 2020 Conference on Empirical Methods in Natural Language Processing (EMNLP)*, pages 4222–4235, Online, November 2020. Association for Computational Linguistics. doi: 10.18653/v1/2020. emnlp-main.346. URL https://aclanthology.org/2020.emnlp-main.346/.
- [30] Charlie Snell, Jaehoon Lee, Kelvin Xu, and Aviral Kumar. Scaling Ilm test-time compute optimally can be more effective than scaling model parameters, 2024. URL https://arxiv.org/abs/2408.03314.
- [31] Charlie Snell, Jaehoon Lee, Kelvin Xu, and Aviral Kumar. Scaling LLM Test-Time Compute Optimally can be More Effective than Scaling Model Parameters, August 2024. URL http://arxiv.org/abs/2408.03314. arXiv:2408.03314 [cs].
- [32] Kefan Song, Amir Moeini, Peng Wang, Lei Gong, Rohan Chandra, Yanjun Qi, and Shangtong Zhang. Reward is enough: Llms are in-context reinforcement learners, 2025. URL https://arxiv.org/abs/2506.06303.
- [33] Aarohi Srivastava, Abhinav Rastogi, Abhishek Rao, Abu Awal Md Shoeb, Abubakar Abid, Adam Fisch, Adam R Brown, Adam Santoro, Aditya Gupta, Adrià Garriga-Alonso, et al. Beyond the imitation game: Quantifying and extrapolating the capabilities of language models. *Transactions on Machine Learning Research*, 2023.

- [34] Jinwei Su, Yinghui Xia, Ronghua Shi, Jianhui Wang, Jianuo Huang, Yijin Wang, Tianyu Shi, Yang Jingsong, and Lewei He. Debflow: Automating agent creation via agent debate, 2025. URL https://arxiv.org/abs/2503.23781.
- [35] Lisa Torrey and Matthew Taylor. Teaching on a budget: Agents advising agents in reinforcement learning. In Proceedings of the 2013 international conference on Autonomous agents and multiagent systems, pages 1053–1060, 2013.
- [36] Pat Verga, Sebastian Hofstatter, Sophia Althammer, Yixuan Su, Aleksandra Piktus, Arkady Arkhangorodsky, Minjie Xu, Naomi White, and Patrick Lewis. Replacing judges with juries: Evaluating Ilm generations with a panel of diverse models. *arXiv preprint arXiv:2404.18796*, 2024.
- [37] Manya Wadhwa, Xinyu Zhao, Junyi Jessy Li, and Greg Durrett. Learning to refine with fine-grained natural language feedback. In Yaser Al-Onaizan, Mohit Bansal, and Yun-Nung Chen, editors, *Findings of the Association for Computational Linguistics: EMNLP 2024*, pages 12281–12308, Miami, Florida, USA, November 2024. Association for Computational Linguistics. doi: 10.18653/v1/2024.findings-emnlp.716. URL https://aclanthology.org/2024.findings-emnlp.716/.
- [38] Jiaan Wang, Yunlong Liang, Fandong Meng, Zengkui Sun, Haoxiang Shi, Zhixu Li, Jinan Xu, Jianfeng Qu, and Jie Zhou. Is ChatGPT a good NLG evaluator? a preliminary study. In Yue Dong, Wen Xiao, Lu Wang, Fei Liu, and Giuseppe Carenini, editors, *Proceedings of the 4th New Frontiers in Summarization Workshop*, pages 1–11, Singapore, December 2023. Association for Computational Linguistics. doi: 10.18653/v1/2023.newsum-1.1. URL https://aclanthology.org/2023.newsum-1.1/.
- [39] Yingxu Wang, Siwei Liu, Jinyuan Fang, and Zaiqiao Meng. Evoagentx: An automated framework for evolving agentic workflows, 2025. URL https://arxiv.org/abs/2507.03616.
- [40] Jason Wei, Xuezhi Wang, Dale Schuurmans, Maarten Bosma, brian ichter, Fei Xia, Ed Chi, Quoc V Le, and Denny Zhou. Chain-of-thought prompting elicits reasoning in large language models. In S. Koyejo, S. Mohamed, A. Agarwal, D. Belgrave, K. Cho, and A. Oh, editors, Advances in Neural Information Processing Systems, volume 35, pages 24824–24837. Curran Associates, Inc., 2022. URL https://proceedings.neurips.cc/paper_files/paper/2022/file/9d5609613524ecf4f15af0f7b31abca4-Paper-Conference.pdf.
- [41] Chengrun Yang, Xuezhi Wang, Yifeng Lu, Hanxiao Liu, Quoc V. Le, Denny Zhou, and Xinyun Chen. Large language models as optimizers, 2024. URL https://arxiv.org/abs/2309.03409.
- [42] Kevin Yang, Yuandong Tian, Nanyun Peng, and Dan Klein. Re3: Generating longer stories with recursive reprompting and revision. In Yoav Goldberg, Zornitsa Kozareva, and Yue Zhang, editors, *Proceedings of the 2022 Conference on Empirical Methods in Natural Language Processing*, pages 4393–4479, Abu Dhabi, United Arab Emirates, December 2022. Association for Computational Linguistics. doi: 10.18653/v1/2022.emnlp-main.296. URL https://aclanthology.org/2022.emnlp-main.296/.
- [43] Mert Yuksekgonul, Federico Bianchi, Joseph Boen, Sheng Liu, Zhi Huang, Carlos Guestrin, and James Zou. Textgrad: Automatic" differentiation" via text. arXiv preprint arXiv:2406.07496, 2024.
- [44] Yongcheng Zeng, Xinyu Cui, Xuanfa Jin, Guoqing Liu, Zexu Sun, Dong Li, Ning Yang, Jianye Hao, Haifeng Zhang, and Jun Wang. Evolving llms' self-refinement capability via iterative preference optimization, 2025. URL https://arxiv.org/abs/2502.05605.
- [45] Haoke Zhang, Xiaobo Liang, Cunxiang Wang, Juntao Li, and Min Zhang. Unlocking recursive thinking of llms: Alignment via refinement, 2025. URL https://arxiv.org/abs/2506.06009.
- [46] Jiayi Zhang, Jinyu Xiang, Zhaoyang Yu, Fengwei Teng, Xionghui Chen, Jiaqi Chen, Mingchen Zhuge, Xin Cheng, Sirui Hong, Jinlin Wang, Bingnan Zheng, Bang Liu, Yuyu Luo, and Chenglin Wu. Aflow: Automating agentic workflow generation, 2025. URL https://arxiv.org/abs/2410.10762.

- [47] Lianmin Zheng, Wei-Lin Chiang, Ying Sheng, Siyuan Zhuang, Zhanghao Wu, Yonghao Zhuang, Zi Lin, Zhuohan Li, Dacheng Li, Eric Xing, Hao Zhang, Joseph E Gonzalez, and Ion Stoica. Judging llm-as-a-judge with mt-bench and chatbot arena. In A. Oh, T. Naumann, A. Globerson, K. Saenko, M. Hardt, and S. Levine, editors, *Advances in Neural Information Processing Systems*, volume 36, pages 46595–46623. Curran Associates, Inc., 2023. URL https://proceedings.neurips.cc/paper_files/paper/2023/file/91f18a1287b398d378ef22505bf41832-Paper-Datasets_and_Benchmarks.pdf.
- [48] Han Zhou, Xingchen Wan, Ruoxi Sun, Hamid Palangi, Shariq Iqbal, Ivan Vulic, Anna Korhonen, and Sercan O. Arık. Multi-agent design: Optimizing agents with better prompts and topologies, 2025. URL https://arxiv.org/abs/2502.02533.
- [49] Yongchao Zhou, Andrei Ioan Muresanu, Ziwen Han, Keiran Paster, Silviu Pitis, Harris Chan, and Jimmy Ba. Large language models are human-level prompt engineers. *arXiv preprint arXiv:2211.01910*, 2022.
- [50] Mingchen Zhuge, Changsheng Zhao, Dylan Ashley, Wenyi Wang, Dmitrii Khizbullin, Yunyang Xiong, Zechun Liu, Ernie Chang, Raghuraman Krishnamoorthi, Yuandong Tian, Yangyang Shi, Vikas Chandra, and Jürgen Schmidhuber. Agent-as-a-judge: Evaluate agents with agents, 2024. URL https://arxiv.org/abs/2410.10934.

A Related Work

ProRefine draws inspiration from and contributes to several interconnected research areas. The performance of LLMs is heavily dependent on the quality of the prompts they receive. Early efforts in this domain centered on crafting prompts manually [40], a meticulous process of designing effective prompts to elicit desired responses. Recognizing the limitations and scalability challenges of manual methods, research has increasingly focused on automatic prompt optimization with a growing emphasis on agentic workflows that enable dynamic and adaptive reasoning.

Prompt Generation: Some pioneering automatic methods, such as AutoPrompt [29] and RLPrompt [7], employ gradient-based search and reinforcement learning techniques, respectively. AutoPrompt [29] uses gradient-based search to generate prompts for masked language models. It reformulates tasks as fill-in-the-blank problems, achieving performance comparable to supervised models in tasks like sentiment analysis. However, it requires training data and gradient access, limiting its applicability to black-box models. Other approaches leverage LLMs themselves for prompt generation [18, 23, 41, 42, 49]. Recent works like Promptomatix [21] and EvoAgentX [39] extend this direction by enabling automatic prompt refinement across multiple tasks, workflows, and tools. ProRefine distinguishes itself by operating simply at inference-time, requiring no training data, gradient access, or model retraining, while enabling prompt refinement in dynamically evolving settings.

Self-Refinement: There is a substantial and growing body of work exploring the capacity of LLMs to act as judges or evaluators [3, 4, 13, 16, 36, 38, 47, 50]. This capability has been leveraged to assess response quality or provide self-feedback. ProRefine adopts this principle, using LLM-generated textual feedback to improve its own prompting process. Unlike prior uses of LLM evaluation solely for ranking or filtering, ProRefine uses that feedback in a closed-loop for optimization during inference.

The idea of LLM iterative refinement is highly relevant. Self-Refine [17] is a prominent example, where an LLM generates both output and feedback, using the latter for refinement. ARIES [44] further enhances refinement via Elo-style agent debate. Other works explore self-critiquing [27] and reinforcement learning for critique generation (RL4F) [1], along with various feedback and refinement mechanisms [8, 12, 24, 26, 28, 37], and Monte Carlo-based refinement in math reasoning (MC-NEST) [25]. While ProRefine shares the self-refinement spirit, it focuses on prompt refinement, suitable for agentic workflows and black-box LLMs, while avoiding reinforcement learning and direct output modification.

Inference-Time Scaling: ProRefine belongs to the broader category of inference-time methods [20, 30], that improve LLMs without weight modification [9]. Inference-time methods aim to

improve the performance of models by utilizing test-time compute resources. TextGrad [43] performs gradient-free inference-time optimization using textual feedback. ProRefine applies a similar idea to intermediate prompt refinement for dynamic reasoning chains. TextGrad relies on supervised fine-tuning, whereas ProRefine operates without training data, offering ease of integration. Other inference-time strategies include RL-of-Thoughts [11] and Reward-Is-Enough [32], which apply RL-based signal propagation during inference. AvR (Alignment via Refinement) [45] proposes recursive CoT refinement using long-form reasoning. ProRefine, by contrast, performs step-level feedback on prompts rather than final outputs, and requires no external tools or supervision.

Agentic Workflows: ProRefine also fits into a broader trend toward agentic workflows. AFlow [46] automates agentic workflows through prompt-based search over prior structures, while EvoAgentX [39] evolves agent behaviors and topologies. Meanwhile, Mass [48] and DebFlow [34] optimize multi-agent configurations via interleaved search and debate. ProRefine focuses instead on optimizing individual agent prompts within fixed workflows, complementing these methods. Unlike tool-integrated or debate-based systems, ProRefine remains model-agnostic and easy to integrate into any prompt-based agent loop.

B Experiments and Evaluation

B.1 Data

We evaluate ProRefine on five reasoning tasks, each of which involves multi-step reasoning, making them suitable for evaluating prompt optimization in agentic workflows. We include the original dataset split sizes in (train/validation/test) format: object counting and word sorting from the BIG-Bench Hard benchmark [33] (50/100/100), grade-school math problem-solving from GSM8K [6] (200/300/1319), math word problems from SVAMP [22] (2516/622/1000), and algebraic word problems from AQUARAT [15] (97467/254/254). We use the same splits and evaluation as Yuksekgonul et al. [43] for object counting, word sorting, and GSM8K.

B.2 Experimental Setup

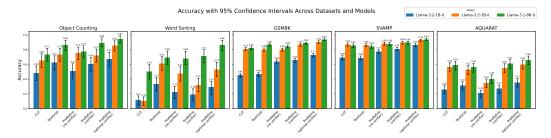


Figure 2: Test Accuracy [with 95% confidence interval] across different models and datasets. *Llama3.1-70B-instruct* is employed for feedback generation, prompt optimization, and evaluation.

We experiment with three models - Llama3.2-1B-instruct, Llama3.2-3B-instruct, and Llama3.1-8B-instruct [19] for LLM_{task} . The prompts are optimized using Algorithm 1, with Llama3.1-70B-instruct used for feedback generation, prompt optimization, and evaluation. We select the values of hyperparameters k=10 and n=25 to control the granularity of feedback and duration of optimization. Hyperparameters k and k were fixed based on general preliminary exploration and not tuned per task using benchmark training/validation data.

We compare the performance of our method against the zero-shot Chain-of-Thought (CoT) baseline and TextGrad [43], and report test accuracy with 95% confidence interval. We choose TextGrad as a baseline because Yuksekgonul et al. [43] reported performance at par or better than DSPy [12] for prompt optimization on object counting, word sorting, and GSM8k datasets. It is essential to remember that TextGrad is a supervised fine-tuning method that utilizes both the training and validation sets. For TextGrad, we use a comparative setup consisting of a task model to be fine-tuned and *Llama3.1-70B-instruct* model for feedback generation and backpropagation. The results are shown in Table 1 and Figure 2.

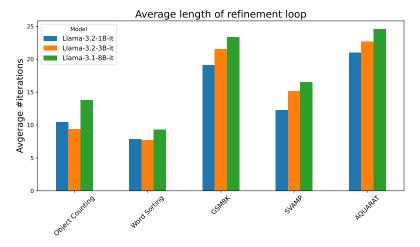


Figure 3: Average number of prompt refinement iterations.

C Discussion

This work investigates the following research questions.

RQ1 How effectively can textual feedback enhance the performance of LLMs during inference?

RQ2 To what extent does model size impact the ability of LLMs to utilize textual feedback?

RQ3 What is the impact of incorporating a verifier on accuracy at inference time?

Regarding RQ1, the results demonstrate that ProRefine is a broadly applicable method that utilizes textual feedback to improve LLM performance at inference time. The "performance gap bridging" effect is particularly noteworthy, suggesting that ProRefine may serve as an effective alternative to simply scaling up model size, potentially avoiding costly fine-tuning an advantage in resource-constrained settings.

The largest performance gains are observed on the word sorting task, indicating that tasks requiring more complex reasoning or manipulation of intermediate outputs benefit the most from ProRefine's iterative refinement. The mixed results when using a smaller model for $LLM_{feedback}$ illustrate the importance of "knowledge asymmetry," i.e., that the feedback model should be "sufficiently capable" of providing useful critiques.

Regarding RQ2, the results indicate that ProRefine outperforms the baselines on 2 and 3 datasets when using the *Llama3.2-1B-instruct* and *Llama3.2-3B-instruct* models, respectively, and on all 5 datasets when using the *Llama3.1-8B-instruct* model. This suggests that performance improvements scale with model size. These findings imply that larger models are preferable to smaller ones, particularly in agentic workflows that may require test-time scaling and the effective use of textual feedback to solve complex tasks.

Regarding RQ3, the results highlight that employing a high-quality verifier is crucial for significantly improving task performance at inference time. We observe some cases where "no verifier" outperforms the "verifier" setting, which indicates the verifier incorrectly accepted a flawed initial answer, thereby preventing the refinement process from correcting the error. This reveals a trade-off: the verifier reduces computational cost on correct answers but risks prematurely halting on incorrect ones. The superior results of the "optimal verifier" highlight the critical role of verifier accuracy. Beyond enhancing performance, the verifier also reduces computational cost during inference by guiding the refinement process. Moreover, it opens up promising avenues for future work, where an optimizer could be designed to maximize rewards guided by the verifier's assessments. ProRefine can offer a degree of interpretability by exposing the outputs from $LLM_{feedback}$, allowing insights into the model's reasoning process. Figures 4 and 5 demonstrate cases where model feedback successfully

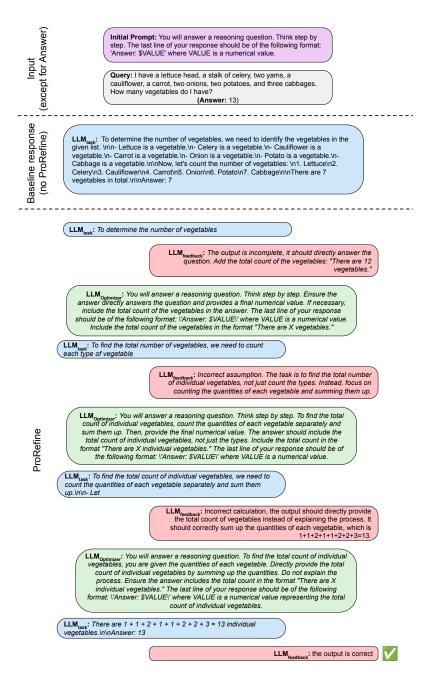


Figure 4: ProRefine example. Given an input query (which in this case has a correct answer: 13) and an initial prompt, the task model (LLM_{task}) gives an incorrect answer. ProRefine uses two additional models, $LLM_{feedback}$ and $LLM_{optimizer}$, to iteratively improve the prompt as the LLM_{task} generates its response. Refining the prompt during generation allows the feedback model to target local regions of the response, providing finer-grained feedback than waiting for the response to complete. We also provide an additional example illustrating our approach in Figure 5.

improves the output and where it fails, respectively. Although evaluated on reasoning and math tasks, ProRefine is general and applicable to other tasks.

A crucial consideration for ProRefine is the trade-off between its accuracy gains and the increased computational cost at inference time. Each refinement step requires additional calls to the $LLM_{feedback}$ and $LLM_{optimizer}$, making any single query more expensive to process than a standard single-pass generation. However, this per-query cost should be evaluated within ProRefine's intended hybrid-

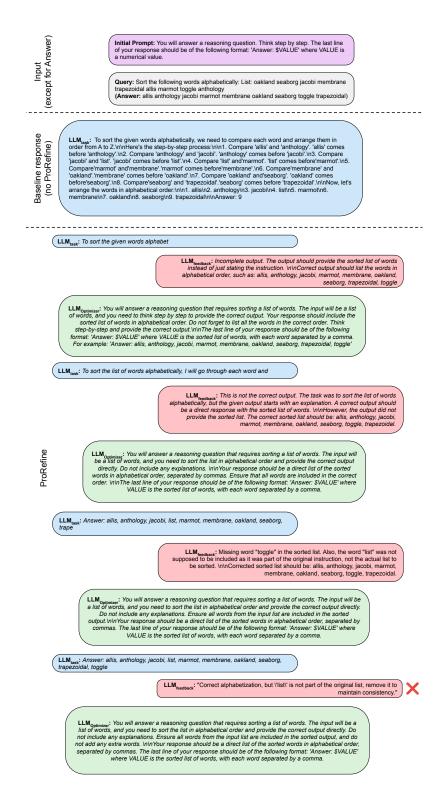


Figure 5: This figure is an instance when $LLM_{optimizer}$ is not aligned with the feedback from $LLM_{feedback}$ and misses important guiding steps. The framework is similar to Figure 4 when $LLM_{optimizer}$ conveys feedback effectively. We've observed a few failed instances following this pattern.

model deployment. The strategy is not to run refinement on every query, but to use it as an on-demand intervention precisely when a more efficient base model fails. Therefore, the overall system cost is not a simple sum of expensive refinement processes. Instead, it is a blend of low-cost successes from the base model and high-value, targeted corrections. Moreover, the cost is still considerably lower than full model retraining or fine-tuning. Our results support this approach's practicality: Figure 3 shows that the average number of refinement iterations is typically low, ensuring the per-incident cost of intervention is contained. This cost-accuracy balance can be further optimized by tuning hyperparameters like feedback granularity (k) and maximum iterations (n).

D Limitations and Future Work

This work has the following limitations that we acknowledge have potential for future explorations:

- Computational Cost and Practicality: While ProRefine is designed for cost-effective hybrid deployments, its iterative process inherently increases inference-time latency and computational cost compared to a single-pass query. The cost-benefit of this trade-off must be carefully evaluated for each specific application, as its viability depends on the base model's failure rate and the relative costs of the LLMs involved.
- **Generalizability:** Our evaluation is currently focused on mathematical and multi-step reasoning tasks. Further research is needed to assess performance across a broader range of reasoning tasks and domains. Our method is also sensitive to hyperparameters and requires manual tuning. Developing more robust, automated, or adaptive methods for setting parameters would enhance the method's usability.
- Dependence on High-Quality Feedback: The system's performance is dependent on the quality of the $LLM_{feedback}$. Future work could explore using a specialized "critic" model or fine-tuning feedback models to improve diagnostic accuracy. Furthermore, using LLMs for evaluation introduces potential biases and more comprehensive human evaluations and robust methods are need for mitigating evaluator bias.
- Stability of the Refinement Loop: The iterative nature of ProRefine lacks a formal convergence guarantee. In some cases, the refinement process can suffer from prompt degradation after many iterations or plateau before reaching an optimal solution. Investigating methods to ensure stable and monotonic improvement is a key area for future research.