

Understanding Fairness Surrogate Functions in Algorithmic Fairness

Anonymous authors

Paper under double-blind review

Abstract

It has been observed that machine learning algorithms exhibit biased predictions against certain population groups. To mitigate such bias while achieving comparable accuracy, a promising approach is to introduce surrogate functions of the concerned fairness definition and solve a constrained optimization problem. However, it is intriguing in previous work that such fairness surrogate functions may yield unfair results and high instability. In this work, in order to deeply understand them, taking a widely used fairness definition—demographic parity as an example, we show that there is a *surrogate-fairness gap* between the fairness definition and the fairness surrogate function. Also, the theoretical analysis and experimental results about the “gap” motivate us that the fairness and stability will be affected by the points far from the decision boundary, which is the *large margin points issue* investigated in this paper. To address it, we propose the general sigmoid surrogate to simultaneously reduce both the surrogate-fairness gap and the variance, and offer a rigorous fairness and stability upper bound. Interestingly, the theory also provides insights into two important issues that deal with the *large margin points* as well as obtaining a more *balanced dataset* are beneficial to fairness and stability. Furthermore, we elaborate a novel and general algorithm called Balanced Surrogate, which iteratively reduces the “gap” to mitigate unfairness. Finally, we provide empirical evidence showing that our methods consistently improve fairness and stability while maintaining accuracy comparable to the baselines in three real-world datasets.

1 Introduction

Recently, increasing attention has been paid to the fairness issue in supervised machine learning. That is, although the classifiers seek a higher accuracy, some groups with certain sensitive features (e.g., sex, race, age) may be unfairly treated, which raises ethical problems (Julia Angwin & Kirchner, 2016; Mehrabi et al., 2021; Caton & Haas, 2020). One can be litigated for committing adverse impacts if his/her decision-making process disproportionately treats groups with sensitive attributes (Barocas & Selbst, 2016).

To quantitatively measure the extent of fairness violation, a usual way is adopting the fairness definition, *demographic parity* (DP), which requires the decision makers to accept a roughly equal proportion of each group (Barocas et al., 2019). Existing methods follow the fairness-aware manner of solving a constrained optimization problem, where the learning objective is integrated with the standard loss and a fairness constraint. To incorporate DP into the constraint, fairness surrogate functions are used to replace the indicator function, which is intractable for gradient-based algorithms (Lohaus et al., 2020; Bendekgey & Sudderth, 2021) (refer to Figure 1(a) for some examples). To date, various surrogate functions have been proposed to incorporate fairness definitions into constraints (Wu et al., 2019; Goh et al., 2016; Padh et al., 2021; Zafar et al., 2017a;b;c; Bendekgey & Sudderth, 2021). They are widely applied in various machine learning domains, such as differential privacy (Ding et al., 2020), meta-learning (Zhao et al., 2020), and semi-supervised learning (Zhang et al., 2020). Unfortunately, these surrogate functions encounter two risks. One risk is that if these fairness constraints are used, even when the constraints are perfectly satisfied, there is *no guarantee* whether DP is satisfied (Lohaus et al., 2020). And the fairness surrogate functions may lead to even unfair solutions (Radovanović et al., 2022). Moreover, another risk arises from the high variance issue observed in

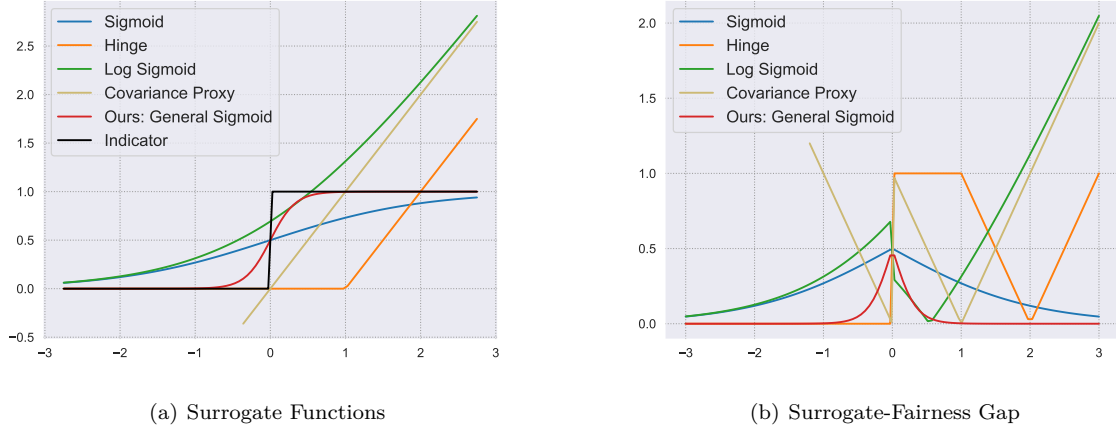


Figure 1: (a) Some examples of fairness surrogate functions. The closer the surrogate functions are to the indicator function, the better they represent DP. More details are introduced in Section 3.2. (b) The surrogate-fairness gap of different surrogate functions. It measures the difference between surrogate functions and the indicator function. There is a much smaller gap for our general sigmoid surrogate.

existing fairness-aware algorithms with surrogate functions (Friedler et al., 2019), rendering them unstable for deployment under fairness requirements (Ganesh et al., 2023).

In this paper, we evaluate these multifarious surrogate functions in algorithmic fairness with both rigorous theorems and extensive experiments. Firstly, we stress the importance of the “**surrogate-fairness gap**”, which is *the disparity between the fairness surrogate function and the fairness definition*. It is the decisive factor of whether the fairness surrogate function can lead to fair outcomes and should be minimized. Additionally, we delve into the **variance** of the substitute for DP, highlighting the adverse impact of unbounded surrogates on stability. Drawing upon the inherent property of the surrogate-fairness gap and instability, we conduct an in-depth examination of the **large margin points issue** within the context of unbounded surrogate functions. To reduce the “gap” and instability, we propose two solutions to improve the existing surrogate functions: a theoretically motivated fairness surrogate function named *general sigmoid* with upper bounds of DP and variance, and a novel algorithm called the *balanced surrogate* to iteratively reduce the gap during training.

Our analysis focuses on a popular surrogate, covariance proxy (Zafar et al., 2017c), in the case of a common fairness definition, DP. In particular, we first derive the violation of DP for the covariance proxy in Section 4.1. The violation of DP depends on two factors: the surrogate function itself and the surrogate-fairness gap. The “gap” (shown in Figure 1(b)) directly determines whether a surrogate function is an appropriate substitute for DP. Secondly, we explore the variance of the covariance proxy in Section 4.2, emphasizing the detrimental impact of unbounded surrogates on stability. Furthermore, driven by the “gap” and variance, we recognize that large margin points—those data points lying significantly distant from the decision boundary—pose challenges in constraining the fairness and stability for unbounded surrogate functions. This observation is validated through a case study on three real-world datasets in Section 4.3. With theoretical motivations, we introduce the general sigmoid surrogate in Section 5.1 to address large margin points and simultaneously bound the “gap” and variance. We theoretically demonstrate that there is a reliable fairness and stability guarantee for it. Interestingly, the theorems also shed light on the importance of a balanced dataset for both fairness and stability. Furthermore, in Section 5.2, we propose balanced surrogates, a novel and general algorithm that iteratively reduces the “gap” to improve fairness. It is a plug-and-play learning paradigm for the naive fairness-aware training framework using fairness surrogate functions. In the experiments in Section 6 using three real-world datasets, our methods consistently enhance fair predictions and stability, while maintaining accuracy comparable to the baselines. In general, our main contributions are three-fold:

- We demonstrate the importance of *surrogate-fairness gap* for fairness surrogate functions and provide an analysis of the *variance*. We urge researchers to pay attention to the impact of *large margin points issue* on fairness and stability for unbounded surrogate functions.
- We propose *General Sigmoid Surrogate* and demonstrate that it achieves fairness and stability guarantees. The theoretical results further provide insights to the community that *large margin points issue* needs to be solved and a *balanced dataset* is beneficial to obtain a fairer and more stable classifier.
- We present *Balanced Surrogate*, a novel and general method that iteratively reduces the “gap” to improve the fairness of any fairness surrogate functions.

2 Related Work

Fairness-aware Algorithms. To mitigate bias, there are various kinds of classical fair algorithms, most of which fall into three categories: pre-processing, in-processing, and post-processing. The pre-processing method is to learn a fair representation that tries to remove information correlated to the sensitive feature while preserving other information for training, e.g., (Calders et al., 2009; Kamiran & Calders, 2011; Zemel et al., 2013; Feldman et al., 2015; Calmon et al., 2017). The downstream tasks then use the fair representation instead of the original biased dataset. The post-processing method is to modify the prediction results to satisfy the fairness definition, e.g., (Kamiran et al., 2012; Fish et al., 2016; Hardt et al., 2016). The in-processing method is to remove unfairness during training. Some intuitive and easy-to-use ideas involve applying fairness constraints (Goh et al., 2016; Zafar et al., 2017a;b;c; Bechavod & Ligett, 2017; Wu et al., 2019; Bendekgey & Sudderth, 2021; Padh et al., 2021) and adding a regularization term to penalize unfairness (Kamishima et al., 2012; Berk et al., 2017; Agarwal et al., 2018; Lohaus et al., 2020; Shui et al., 2022). Our paper focuses on in-processing methods, with a particular emphasis on fairness surrogate functions, which are widely used in fairness constraints and fairness regularization methods mentioned above.

Fairness Surrogate Functions. Although many existing popular surrogates work well in practice, for example, linear (Donini et al., 2018; Agarwal et al., 2018; Bechavod & Ligett, 2017), ramp (Goh et al., 2016; Zafar et al., 2017b), convex-concave (Zafar et al., 2017a), sigmoid and log-sigmoid (Bendekgey & Sudderth, 2021). They suffer from the same issue: there is not a fairness guarantee for them (Lohaus et al., 2020). And using fairness constraints or regularization can unexpectedly yield unfair solutions (Radovanović et al., 2022). Refer to Appendix C for a meticulous overview of existing works, most of which present counterexamples for analysis. The high variance issue has been observed in existing fairness-aware algorithms (Ganesh et al., 2023), including the instability of the covariance proxy (Friedler et al., 2019). In this paper, in addition to empirically showing counter-examples, we both theoretically and empirically underscore the significance of the surrogate-fairness gap and variance, which are fundamental factors contributing to the two aforementioned problems, respectively. Our general sigmoid surrogate is shown to deal with the large margin points to simultaneously reduce both the surrogate-fairness gap and the variance. There is also fairness and stability upper bound for it, which is crucial in this field (Gallegos et al., 2023; Mehrabi et al., 2021; Caton & Haas, 2020). Additionally, in order to reduce the gap, we also devise a balanced surrogate approach to further improve the fairness and stability of surrogate functions.

3 Preliminaries

3.1 Fairness-aware Classification

Note the general purpose of fairness-aware classification is to find a classifier with minimal accuracy loss while satisfying certain fairness constraints. For simplicity, we set up the problem as the binary classification task with only a binary-sensitive feature: with the training set $\mathcal{S} = \{(\mathbf{x}_i, y_i)\}_{i=1}^N$ consisting of feature vectors $\mathbf{x}_i \in \mathbb{R}^d$ and the corresponding class labels $y \in \{0, 1\}$, one needs to predict the labels of a test set. Let $d_\theta(\mathbf{x})$ denotes the signed distance between the feature vector \mathbf{x} and the decision boundary parameterized by θ . Given a point \mathbf{x}_i in the test set, a classifier will predict it as positive if $d_\theta(\mathbf{x}_i) > 0$ and zero if $d_\theta(\mathbf{x}_i) \leq 0$. Among the features of \mathbf{x} , there is one binary sensitive attribute $z \in \{-1, +1\}$ (e.g., sex, race, age).

As introduced in Section 1, a widely used fairness definition is called the *demographic parity* (DP) (Mehrabi et al., 2021; Caton & Haas, 2020). It states that each protected class should receive the positive outcome at equal rates, i.e.,

$$P(d_\theta(\mathbf{x}) > 0 | z = +1) = P(d_\theta(\mathbf{x}) > 0 | z = -1).$$

And further, the *difference of demographic parity* (DDP) metric (Lohaus et al., 2020) can be used to measure the degree to which demographic parity is violated:

$$DDP = P(d_\theta(\mathbf{x}) > 0 | z = +1) - P(d_\theta(\mathbf{x}) > 0 | z = -1).$$

Then, with this metric, whether a classifier satisfies demographic parity can be determined by the condition $|DDP| \leq \epsilon$, where $\epsilon \geq 0$ is a given threshold.

3.2 Surrogate Functions

We divide the training set into four classes according to the predicted labels and sensitive features:

$$\begin{aligned} \mathcal{N}_{1a} &= \{(\mathbf{x}_i, y_i) \in \mathcal{S} \mid d_\theta(\mathbf{x}_i) > 0, z_i = +1\}, & \mathcal{N}_{1b} &= \{(\mathbf{x}_i, y_i) \in \mathcal{S} \mid d_\theta(\mathbf{x}_i) > 0, z_i = -1\}, \\ \mathcal{N}_{0a} &= \{(\mathbf{x}_i, y_i) \in \mathcal{S} \mid d_\theta(\mathbf{x}_i) \leq 0, z_i = +1\}, & \mathcal{N}_{0b} &= \{(\mathbf{x}_i, y_i) \in \mathcal{S} \mid d_\theta(\mathbf{x}_i) \leq 0, z_i = -1\}, \end{aligned}$$

where $N_{1a}, N_{1b}, N_{0a}, N_{0b}$ are sizes of $\mathcal{N}_{1a}, \mathcal{N}_{1b}, \mathcal{N}_{0a}, \mathcal{N}_{0b}$, respectively. Then, to consider DDP as fairness constraints for optimization, the probability in it cannot be computed directly, so frequency is used to estimate them:

$$\begin{aligned} \widehat{DDP} &= \frac{N_{1a}}{N_{1a} + N_{0a}} - \frac{N_{1b}}{N_{1b} + N_{0b}} \\ &= \frac{\sum_{\mathcal{N}_{1a}, \mathcal{N}_{0a}} \mathbb{1}_{d_\theta(\mathbf{x}) > 0}}{N_{1a} + N_{0a}} - \frac{\sum_{\mathcal{N}_{1b}, \mathcal{N}_{0b}} \mathbb{1}_{d_\theta(\mathbf{x}) > 0}}{N_{1b} + N_{0b}}, \end{aligned} \quad (1)$$

where $\mathbb{1}_{[\cdot]} : \mathbb{R} \rightarrow \{0, 1\}$ is the indicator function that returns 1 if the condition is true and 0 otherwise.

In application, \widehat{DDP} usually serves as a substitute for DDP to judge the fairness of a classifier. However, due to $\mathbb{1}_{d_\theta(\mathbf{x}) > 0}$, it is intractable to directly incorporate \widehat{DDP} into constraints for gradient-based algorithms. So smooth **surrogate function** $\phi : \mathbb{R} \rightarrow \mathbb{R}$ is used to replace $\mathbb{1}_{d_\theta(\mathbf{x}) > 0}$ with $\phi(d_\theta(\mathbf{x}))$. There exists a widely recognized form of the surrogate function: *Covariance Proxy* (CP) (Zafar et al., 2017c). To date, according to Google Scholar¹, this article has garnered over 1,000 citations. Empirical study shows that CP can reflect the difference of demographic parity and can be incorporated as constraints for fairness-aware classification problem (Ding et al., 2020; Zhao et al., 2020; Zhang et al., 2020). CP finds application in a diverse range of scenarios (Mehrabi et al., 2021), and is also generalized to other fairness definitions, such as disparate mistreatment (Zafar et al., 2017a). The original CP is defined as $Cov(z, d_\theta(\mathbf{x})) = \mathbb{E}[(z - \bar{z})d_\theta(\mathbf{x})]$, where \bar{z} is the mean of z over the training set. The expectation can not be computed directly, so its empirical form $\frac{1}{N} \sum_{i=1}^N (z_i - \bar{z})d_\theta(\mathbf{x}_i)$ is proposed to estimate the expectation. Here we defined a general version of it:

$$\widehat{Cov}(\phi) = \frac{1}{N} \sum_{i=1}^N (z_i - \bar{z})\phi(d_\theta(\mathbf{x}_i)) \propto \left(\frac{\sum_{\mathcal{N}_{1a}, \mathcal{N}_{0a}} \phi(d_\theta(\mathbf{x}_i))}{N_{1a} + N_{0a}} - \frac{\sum_{\mathcal{N}_{1b}, \mathcal{N}_{0b}} \phi(d_\theta(\mathbf{x}_i))}{N_{1b} + N_{0b}} \right). \quad (2)$$

The proof can be found in Appendix A.1. If $\phi(x) = x$, the equation (2) recovers the original definition of CP in (Zafar et al., 2017c). It means that *the original CP is equivalent to the linear surrogate function* $\phi(x) = x$, which is also explained in previous work (Lohaus et al., 2020; Bendekgy & Sudderth, 2021).

4 Three Unsolved Problems

We underline three unsolved problems of CP: surrogate-fairness gap, instability and large margin points. Specifically, the large margin points will exacerbate the first two problems.

¹ <https://scholar.google.com/>

4.1 The Surrogate-fairness Gap

In this part, we connect \widehat{DDP} and \widehat{Cov} together, and build the surrogate-fairness gap between DP and CP.

Proposition 1. *Define the magnitude of the signed distance by $D_\theta(\mathbf{x})$, i.e., $D_\theta(\mathbf{x}) = |d_\theta(\mathbf{x})|$. Let $\phi(x) = x$ and $S_{1a} = \sum_{\mathcal{N}_{1a}} \phi(D_\theta(\mathbf{x}_i))$, $T_{1a} = \sum_{\mathcal{N}_{1a}} (\phi(D_\theta(\mathbf{x}_i)) - 1)$ and it is similar for $\mathcal{N}_{1b}, \mathcal{N}_{0a}, \mathcal{N}_{0b}$. It satisfies:*

$$\widehat{DDP} = \frac{N^2}{2(N_{1a} + N_{0a})(N_{1b} + N_{0b})} \widehat{Cov}(\phi) - \underbrace{\left(\frac{T_{1a} - S_{0a}}{N_{1a} + N_{0a}} - \frac{T_{1b} - S_{0b}}{N_{1b} + N_{0b}} \right)}_{\text{surrogate-fairness gap}}. \quad (3)$$

There is a surrogate-fairness gap between \widehat{DDP} and \widehat{Cov} . So there is no guarantee whether DP is already satisfied even when the empirical \widehat{Cov} is minimized to zero. The first term related to \widehat{Cov} is controllable: Considering the constraints in (Zafar et al., 2017c) that $|\widehat{Cov}| \leq \epsilon$ where $\epsilon \geq 0$ is a small constant specified in advance. The coefficient in front of \widehat{Cov} is also invariable because $N, N_{1a} + N_{0a}, N_{1b} + N_{0b}$ are constants. But it is totally different for the ‘‘gap’’. It comes from the difference between the surrogate and the indicator function. For the ideal case $d_\theta(\mathbf{x}) = \mathbb{1}_{d_\theta(\mathbf{x}) > 0}$ which is equivalent to $\phi(x) = \mathbb{1}_{x > 0}$,

4.2 Instability

The variance of $\widehat{Cov}(\phi)$ is $Var(\widehat{Cov}(\phi)) = \mathbb{E}(\widehat{Cov}(\phi))^2 - [\mathbb{E}(\widehat{Cov}(\phi))]^2$. If we choose bounded surrogate $\phi(x) \in [0, 1]$, then $\widehat{Cov}(\phi) \in [-1, 1]$, which means that $Var(\widehat{Cov}(\phi)) \in [0, 1]$ (Refer to the mathematical derivation in Appendix A.1). However, if we choose unbounded surrogate function (such as $\phi(x) = x$ for the original CP), the resulting values of ϕ are not constrained within the range $[0, 1]$. Consequently, there is no longer a stability guarantee for $\widehat{Cov}(\phi)$. In contrast, there is stability guarantee for \widehat{DDP} due to the fact that $Var(\widehat{DDP}) \in [0, 1]$.

To summarize the aforementioned two unsolved problems, incorporating \widehat{Cov} into fairness regularization and constraints to indirectly minimize \widehat{DDP} may encounter difficulties for two reasons. Firstly, due to the existence of the surrogate-fairness gap, minimizing \widehat{Cov} is not equivalent to minimizing \widehat{DDP} . Secondly, if unbounded surrogate functions are employed, the uncontrollable variance of \widehat{Cov} makes it even more challenging to be an appropriate estimator of \widehat{DDP} .

4.3 The Large Margin Points

We emphasize the third trouble here: the large margin points. In this paper, the points with too large $D_\theta(\mathbf{x})$ are called *large margin points* and others are normal points. Unfortunately, we regret to assert that these large margin points may simultaneously worsen the first two issues mentioned above. To illustrate, we take CP as an example. For three famous real-world data sets, Adult (Kohavi, 1996), COMPAS (Julia Angwin & Kirchner, 2016) and Bank Marketing (S. Moro & Rita, 2014), we provide the boxplot of $d_\theta(\mathbf{x})$ in the test set in Figure 2. The experimental details are in Appendix D.1. There are three main observations in Figure 2: (i) Most of the points are near the decision boundary. (ii) Over 5% points are large margin points for Adult and COMPAS. (iii) Almost all the large margin points are predicted as positive class.

Firstly, for the surrogate-fairness gap problem, the gap in (3) may be amplified in the presence of such large margin points with positive prediction labels because they make T_{1a} and T_{1b} larger. For example, in Figure 2, most of the large margin points are predicted positive, so S_{0a} and S_{0b} are bounded (for instance, In Figure 2(b), we have $|S_{0a}| \leq 2N_{0a}$). However, the distance between large margin points and the decision boundary is uncertain, so there is not a tight bound for T_{1a} and T_{1b} , which may lead to a large surrogate-fairness gap. Finally, when the gap becomes large, constraining the fairness surrogate function is inconsistent with the specific fairness definition, which may lead to unfair result.

Secondly, regarding the instability issue, while the majority of points are close to the decision boundary, a small number of large margin points contribute to the increased variance of $d_\theta(\mathbf{x})$, thereby influencing

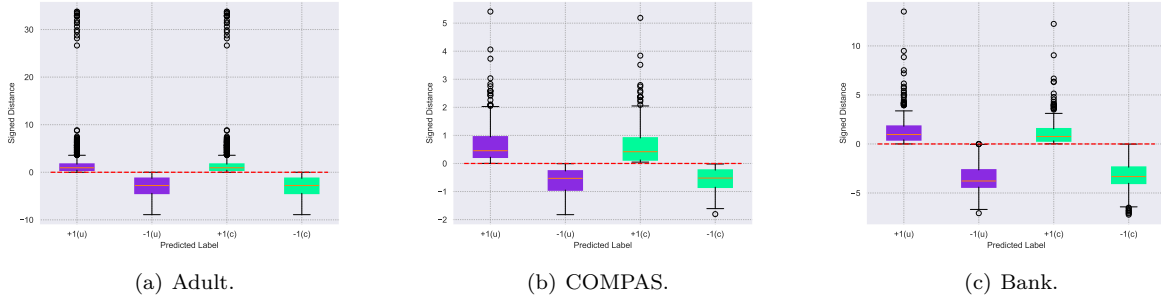


Figure 2: The boxplot for the unconstrained logistic classifier (u) and logistic classifier with fairness constraints using linear surrogate (c) in three datasets. +1 and -1 represent the predicted label. The red dashed line means $d_\theta(\mathbf{x}) = 0$. The orange line in the box is the median. The circles outside the box are large margin points. The rates of large margin points are 7.61%, 5.12% and 0.82% respectively.

both $\widehat{Cov}(\phi)$ and $Var(\widehat{Cov}(\phi))$. The presence of large margin points, along with the use of an unbounded surrogate function, surpasses the constraint on $Var(\widehat{Cov}(\phi))$ and may result in unstable fairness guidance for the classifier. These analytical insights above will be further validated through our experiments.

5 Our Approach

We devise the general sigmoid surrogate function with fairness and stability guarantees in Section 5.1. The theory suggests that addressing the large margin points issue and obtaining a more balanced dataset contribute to a fairer classifier. Then we present our balanced surrogates in Section 5.2, which is a novel iterative approach to reduce the “gap” and thus improving fairness.

5.1 General Sigmoid Surrogates

We generalize sigmoid function as

$$G(x) = \sigma(wx), \quad (4)$$

where $\sigma(x)$ is the sigmoid function and $w > 0$ is the parameter. The general sigmoid surrogate is flexible because of the adjustable w . Moreover, of paramount importance, it achieves a much lower surrogate-fairness gap, making it more consistent with DP, which is shown in Figure 1(b). Additionally, it enjoys stability guarantees as its values fall within the range $[0, 1]$, ensuring that $Var(\widehat{Cov}(G)) \in [0, 1]$.

5.1.1 Fairness Guarantees

The following Theorem 1 provides the upper bound of $|\widehat{DDP}|$ when $G(D_\theta(\mathbf{x}))$ is close to 1 for all the points under the CP fairness constraint.

Theorem 1. *We assume that $G(D_\theta(\mathbf{x})) \in [1 - \gamma, 1]$, where $\gamma > 0$. $\forall \epsilon > 0$, if $|\widehat{Cov}(G)| \leq \epsilon$, then it holds:*

$$|\widehat{DDP}| \leq \frac{N^2}{4(N_{1a} + N_{0a})(N_{1b} + N_{0b})} \epsilon + \gamma.$$

The proof can be found in Appendix A.2. The first term is similar to that in (3). Now with the assumption $G(D_\theta(\mathbf{x})) \in [1 - \gamma, 1]$, the gap here can be limited to a small range of variation. If the general sigmoid surrogates limit $G(D_\theta(\mathbf{x}))$ to around 1 so that γ is small enough, then there are fairness guarantees for the classifier. In contrast, the gap for CP is influenced by the magnitude of $D_\theta(\mathbf{x})$ for every large margin point and thus hard to be bounded.

Remark. In Appendix B.3, we provide extensions of Theorem 1 to other five fairness definitions: three kinds of disparate mistreatment (Theorem 5-10 in Appendix B.3.1) and balance for positive (negative) class (Theorem 11-12 in Appendix B.3.2). In particular, CP is generalized to disparate mistreatment (Zafar et al., 2017a), and we theoretically devise the form of CP to better meet with disparate mistreatment, which is empirically validated in (Zafar et al., 2019).

However, in some cases, we do not need to guarantee that the assumption $G(D_\theta(\mathbf{x})) \in [1 - \gamma, 1]$ holds for all the points. So the theorem below relaxes the assumption by giving the upper bound of $|\widehat{DDP}|$ when most of the points satisfy the assumption in Theorem 1.

Theorem 2. We assume that k points satisfy $G(D_\theta(\mathbf{x})) \in [0, 1 - \gamma]$ and others satisfy $G(D_\theta(\mathbf{x})) \in [1 - \gamma, 1]$, where $\gamma > 0$. $\forall \epsilon > 0$, if $|\widehat{Cov}(G)| \leq \epsilon$, then it holds:

$$|\widehat{DDP}| \leq \frac{N^2}{4(N_{1a} + N_{0a})(N_{1b} + N_{0b})} \epsilon + \gamma + \underbrace{\frac{1}{2} \left(\frac{1}{N_{1a} + N_{0a}} + \frac{1}{N_{1b} + N_{0b}} \right)}_{\text{relaxation factor}} k.$$

The proof can be found in Appendix A.3. Comparing Theorem 1 with Theorem 2, the relaxation of the assumption produces an extra relaxation factor. According to Theorem 1, if w is large, then γ can be small enough, thus leading to a classifier with fairness guarantee. But an arbitrarily too large w makes training more challenging because of the diminished gradient magnitude for general sigmoid surrogate. Theorem 2 tells us that we need not to assume that all points satisfy $G(D_\theta(\mathbf{x})) \in [1 - \gamma, 1]$. Few points violating the assumption (a small k) can also be tolerated. So it supports the idea that we do not have to choose a large w because a relatively small w can also guarantee fairness.

5.1.2 Insights from the Theorems

Large Margin Points Issue. An obvious takeaway of Theorem 2 is that addressing the large margin points issue makes k lower and thus obtaining a tighter bound of $|\widehat{DDP}|$. While Bendekgey & Sudderth (2021) also explores the influence of outliers on the model under fairness constraints, their theoretical analysis in primarily centers on loss degeneracy under fairness constraints, whereas our paper aims to establish upper bounds concerning fairness.

Balanced Dataset. Another interesting take-away of Theorem 1-2 is that we need a *balanced dataset* to obtain a fairer classifier. The approximately same number between two sensitive groups contributes to a tighter $|\widehat{DDP}|$ upper bound. First of all, for Theorem 1, the coefficient of ϵ satisfies $\frac{N^2}{4(N_{1a} + N_{0a})(N_{1b} + N_{0b})} \geq 1$. The equality holds if and only if $N_{1a} + N_{0a} = N_{1b} + N_{0b}$, which means that the two sensitive groups share the equal size. Therefore, a more balanced dataset will obtain a tighter $|\widehat{DDP}|$ upper bound. Similarly, comparing to Theorem 1, we discover that those k points in Theorem 2 relaxed the original bound by a relaxation factor. The coefficient of the relaxation factor $\frac{1}{2} \left(\frac{N}{N_{1a} + N_{0a}} + \frac{N}{N_{1b} + N_{0b}} \right) \geq 2$, and the equality holds if and only if $N_{1a} + N_{0a} = N_{1b} + N_{0b}$. So, if we use a balanced dataset, then $N_{1a} + N_{0a}$ and $N_{1b} + N_{0b}$ are close to each other, thus making the fairness bounded tighter. The imbalance issue also applies to other surrogates and one can balance the dataset in advance to achieve better fairness performance.

Notably, certain theoretical investigations illuminate the positive impact of a *balanced dataset* on fostering fairness in machine learning. For example, the impossibility theorem (Bell et al., 2023) in fairness literature states that, in the context of binary classification, equalizing some specific set of multiple common performance metrics between protected classes is impossible, except in two special cases: a perfect predictor and equal *base rate* (Chouldechova, 2017; Kleinberg et al., 2017; Pleiss et al., 2017). Furthermore, the reduction of variation in group *base rates* has been demonstrated to yield a diminished lower bound for separation gap and independence gap (Liu et al., 2019). Moreover, minimizing the difference in *base rates* results in a decreased lower bound for joint error across both sensitive groups (Zhao & Gordon, 2022). In contrast, our Theorem 2 provides an elucidation from the perspective of *upper bound*. It implies that a more balanced dataset results in a tighter upper bound on the violation of DP.

Remark. In Appendix A.5, we compute an upper bound of $\text{Var}(\widehat{DDP})$ and the Theorem 4 highlights the advantage of a balanced dataset in reducing variance.

5.2 Balanced Surrogates

The naive fairness-aware training framework can be formulated as

$$\min L(\theta, \mathbf{x}, y) + \lambda \cdot \widehat{DDP}, \quad (5)$$

where $L(\theta, \mathbf{x}, y)$ is the loss function for accuracy, $\widehat{DDP} = \frac{\sum_{\mathcal{N}_{1a}, \mathcal{N}_{0a}} \phi(d_\theta(\mathbf{x}))}{N_{1a} + N_{0a}} - \frac{\sum_{\mathcal{N}_{1b}, \mathcal{N}_{0b}} \phi(d_\theta(\mathbf{x}))}{N_{1b} + N_{0b}}$ is the fairness regularization, and $\lambda > 0$ is the coefficient. Recall that whether \widehat{DDP} is an appropriate estimation of DP depends on ϕ . Thus, the existence of surrogate-fairness gap motivates us that it is still necessary to reduce “gap” to improve fairness.

Our balanced surrogates approach mitigates unfairness by treating different sensitive groups differently using a parameter being updated during training. The key idea of the updating procedure is *making the magnitude of “gap” as small as possible*. It is a general plug-and-play learning paradigm for training framework using fairness surrogate functions like (5), which is validated in the experiments.

Specifically, we consider different surrogates for two sensitive groups, i.e.,

$$\phi(d_\theta(\mathbf{x}_i)) = \begin{cases} \phi_1(d_\theta(\mathbf{x}_i)), & z_i = +1. \\ \phi_2(d_\theta(\mathbf{x}_i)), & z_i = -1. \end{cases} \quad (6)$$

With (6), we rewrite \widehat{DDP} as:

$$\widehat{DDP} = \frac{\sum_{\mathcal{N}_{1a}, \mathcal{N}_{0a}} \phi_1(d_\theta(\mathbf{x}))}{N_{1a} + N_{0a}} - \frac{\sum_{\mathcal{N}_{1b}, \mathcal{N}_{0b}} \phi_2(d_\theta(\mathbf{x}))}{N_{1b} + N_{0b}}, \quad (7)$$

For simplicity, we assume

$$\phi_2(x) = \lambda \phi_1(x), \quad (8)$$

where $\lambda \geq 0$ is the *balance factor* to be updated to reduce the gap. Our objective is

$$\widehat{DDP} - \widehat{DDP} = 0, \quad (9)$$

which is equivalent to a Surrogate-fairness Gap of zero. Plug equations (1), (7) and (8) into the equation (9), we then solve for λ :

$$\lambda = \frac{(N_{1b} + N_{0b}) \sum_{\mathcal{N}_{1a}, \mathcal{N}_{0a}} \phi_1(d_\theta(\mathbf{x})) - (N_{1a}N_{0b} - N_{0a}N_{1b})}{(N_{1a} + N_{0a}) \sum_{\mathcal{N}_{1b}, \mathcal{N}_{0b}} \phi_1(d_\theta(\mathbf{x}))} \quad (10)$$

In this way, we can first specify ϕ_1 in (6), initiate λ as λ_0 , and train an unconstrained classifier with the produced θ_0 as the start point of the iteration. Then we iteratively solve (5) and compute (10) until convergence. In order to avoid oscillation and accelerate the convergence, we use exponential smoothing for λ :

$$\lambda_t = \begin{cases} \lambda_0, & t = 0. \\ \alpha \lambda'_t + (1 - \alpha) \lambda_{t-1}, & t = 1, 2, \dots, N. \end{cases} \quad (11)$$

Where λ'_t comes from (10) after t iterations, λ_t is the result of λ'_t after exponential smoothing and $0 \leq \alpha \leq 1$ is the smoothing factor. Notice that $\lambda \leq 0$ is meaningless, so when this happens, we abandon this algorithm and set λ_t to 1, which recovers (5). When the difference of λ_t between two successive iterations is less than a termination threshold η , the algorithm is over. If we choose the smoothing factor α and the termination threshold η properly, then the loop will terminate after a few runs. The algorithmic representation of the balanced surrogates can be found in Appendix D.

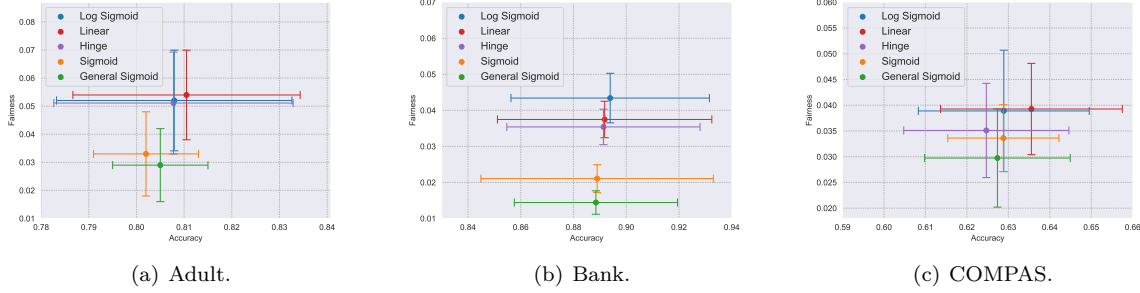


Figure 3: Results of different surrogate functions.

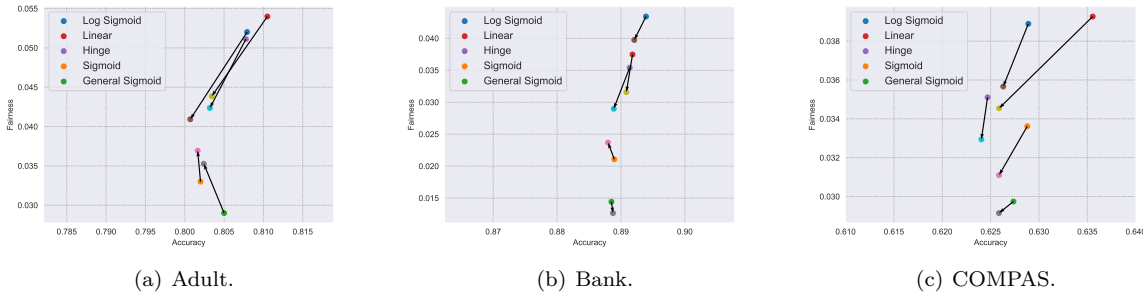


Figure 4: Results of applying balanced surrogate to different surrogate functions. The arrow starts with the result of a surrogate and ends with the result of the same surrogate function using balanced surrogate method.

6 Experiments

6.1 Experimental Setup

Dataset. We use three real-world datasets: Adult (Kohavi, 1996), Bank Marketing (S. Moro & Rita, 2014) and COMPAS (Julia Angwin & Kirchner, 2016), which are commonly used in fair machine learning (Mehrabi et al., 2021).

- **Adult.** The Adult dataset contains 48842 instances and 14 attributes. The goal is predicting whether the income for a person is more than \$50,000 a year. We consider sex as the sensitive feature with values male and female.
- **Bank.** The Bank Marketing dataset contains 41188 instances and 20 input features. The goal is predicting whether the client will subscribe a term deposit. We follow (Zafar et al., 2017c) and consider age as the binary sensitive attribute, which is discretized into the case whether the client’s age is between 25 and 60 years.
- **COMPAS.** The COMPAS dataset was compiled to investigate racial bias in recidivism prediction. The goal is predicting whether a criminal defendant will be a recidivist in two years. We use only the subset of the data with sensitive attribute Caucasian or African-American.

Baseline. In addition to an unconstrained logistic regression classifier (denoted as ‘Unconstrained’), we compare our general sigmoid surrogate (denoted as ‘General Sigmoid’) with other four surrogate functions below, which have also appeared in Figure 1.

- Linear surrogate (CP) $\phi(x) = x$ (Zafar et al., 2017c) (denoted as ‘Linear’).
- Sigmoid surrogate $\phi(x) = \sigma(x)$ (Bendekgey & Sudderth, 2021) (denoted as ‘Sigmoid’).
- Log-sigmoid surrogate $\phi(x) = -\log \sigma(-x)$ (Bendekgey & Sudderth, 2021) (denoted as ‘Log-Sigmoid’).
- Hinge-like surrogate $\phi(x) = \max(x + 1, 0)$ (denoted as ‘Hinge’).

6.2 Learning Fair Classifiers

We conduct two main experiments. One is the comparison among general sigmoid surrogate and other surrogate functions on classification tasks. The other is validating the effect of balanced surrogates method by applying it to different surrogate functions. Following (Bendekgey & Sudderth, 2021), a linear classifier is used as the base classifier. The dataset is randomly divided into training set (70%), validation set (5%) and test set (25%). The parameter setting is described in Appendix D.2. We report two metrics on the test set: $|\widehat{DDP}|$ (lower is better) and accuracy (higher is better), and standard deviation is shown for the metrics.

6.3 Main Results

The results are in Figures 3-4. Refer to Appendix D.4 for specific numerical results of all three datasets.

General Sigmoid Surrogate. In Figure 3, on the one hand, we observe that the general sigmoid surrogate achieves better fairness than unbounded surrogate functions (Log sigmoid, Linear and Hinge), which indicates that the general sigmoid surrogate does effectively shorten the surrogate-fairness gap and therefore improve fairness. On the other hand, comparing to the sigmoid surrogate function, our proposed surrogate not only further reduces the gap, but it is also more flexible due to the parameter w . Moreover, it is intriguing to note that the variance of fairness and accuracy of general sigmoid surrogate is also comparatively smaller than other surrogate functions, demonstrating its superiority in terms of stability. It offers a simple solution to the long-standing high variance issue observed in existing fairness-aware algorithms (Friedler et al., 2019; Ganesh et al., 2023). We provide some theoretical analysis on variance to Appendix A.5. Exploring automated methods to search for a suitable parameter w for improved fairness performance while reducing variance presents an intriguing avenue for future research.

Balanced Surrogates Method. In Figure 4, we observe that balanced surrogates method succeeds in improving fairness of unbounded surrogate functions but sometimes slightly compromising fairness of bounded surrogate functions. For the reason of this phenomenon, fairness-aware algorithms aim to reduce $|\widehat{DDP}|$. Firstly, fairness regularization aims at lowering $|\widehat{DDP}|$. Secondly, the key idea of balanced surrogates is to reduce the magnitude of “gap” $|\widehat{DDP} - \widehat{DDP}|$ thus indirectly lower $|\widehat{DDP}|$ (because $|\widehat{DDP}| \leq |\widehat{DDP}| + |\widehat{DDP} - \widehat{DDP}|$). However, an infinitesimal $|\widehat{DDP}|$ is not always better. In Appendix A.4, we show in Theorem 3 that there is still a discrepancy between \widehat{DDP} and DDP , indicating that a small enough $|\widehat{DDP}|$ is not equivalent to a small $|DDP|$. When the “gap” is large (such as the unbounded surrogate functions), balanced surrogates method can effectively reduce “gap” and achieves a fairer result. But when the “gap” is limited (such as sigmoid and general sigmoid), an infinitesimal magnitude of “gap” may sometimes undermine fairness instead. Interestingly, similar to the stability enhancement observed in general sigmoid surrogate, the numerical results in Appendix D.4 also show that our balanced surrogates method attains smaller variance compared to other surrogate functions. Incorporating mechanisms such as the balanced surrogate method into existing fairness-aware algorithms to enhance both fairness and stability is also a promising direction.

6.4 Experimental Verification for the Theoretical Insights

Large Margin Points Issue. The boxplot with our general sigmoid surrogate is shown in Figure 6. Recall that with an unbounded surrogate function ϕ , the large margin points will influence the “gap”. Now they

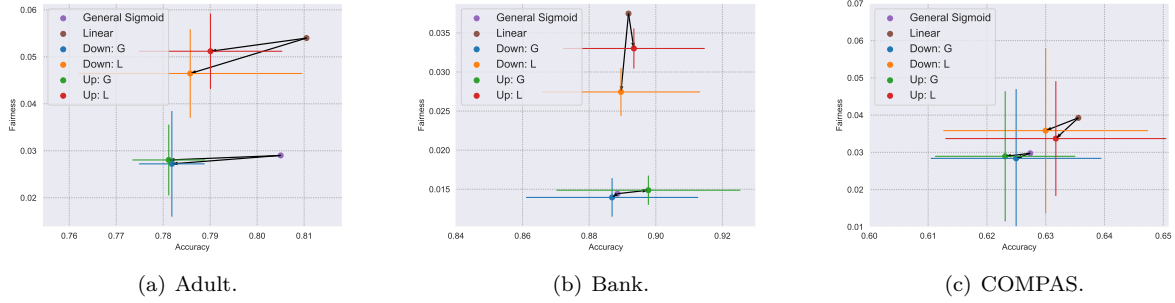


Figure 5: The result of balanced dataset. 'G' and 'L' indicates general sigmoid surrogate and linear surrogate, respectively. 'Up' and 'Down' correspond to upsampling and downsampling, respectively.

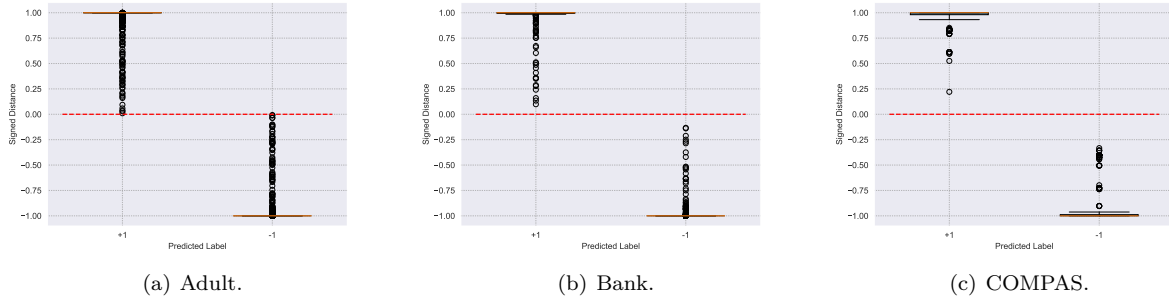


Figure 6: Boxplots for three datasets with general sigmoid surrogate. +1 and -1 represent the predicted label. The red dashed line means $d_{\theta}(\mathbf{x}) = 0$. The orange line in the box is the median. The median line and the edges of the boxplot almost overlap with the box itself.

have a minor impact on the “gap” mentioned before because they are bounded ($G(D_{\theta}(\mathbf{x})) \leq 1$). Furthermore, the two edges almost overlap, indicating that the variation of $D_{\theta}(\mathbf{x})$ is small, contributing to more stable results. Overall, the general sigmoid surrogate successfully deals with the large margin points, mitigating both the surrogate-fairness gap and instability simultaneously.

Balanced Dataset. From the perspective of sensitive attribute, the Adult dataset is an *imbalanced* dataset: there are 32650 male instances and 16192 female instances. The ratio of the two groups is approximately 2:1. The Bank Marketing and COMPAS datasets also suffer from the imbalance issue. The ratio of the two groups are 39210:1978 (about 20:1) and 3175:2103 (about 3:2), respectively. Such imbalanced datasets lead to a loose bound in Theorem 2. We randomly split the dataset into training set (70%) and test set (30%). According to the number of minority group, we conduct two experiments: Downsampling and Upsampling, which means randomly downsampling (upsampling) the majority (minority) group in the original training set and form the new training set to make two demographic groups more balanced. Refer to Appendix D.3 for the details of our sampling schemes. The test set is partitioned in advance so that it is still imbalanced. We choose an unbounded surrogate function: Linear, and our bounded surrogate: general sigmoid.

The results in Figure 5 show that downsampling the majority group and upsampling the minority group contribute to a balanced dataset and a fairer result. However, in our experiments here, downsampling will lead to reduction of the training set, and upsampling will lead to replication of the training set, which may cause underfitting and overfitting problems, respectively. So the accuracy sometimes decreases. In conclusion, before fairness-aware training, we suggest using fair data augmentation strategies to obtain a balanced dataset, such as Fair Mixup (Chuang & Mroueh, 2021), and algorithms designed to address data imbalance, such as SMOTE (Chawla et al., 2002).

7 Conclusion

In this paper, we research on surrogate functions in algorithmic fairness. We derive the surrogate-fairness gap between DP and CP. With boxplots, we find that unbounded surrogates are especially faced with the large margin points issue, which further amplify the “gap” and instability. To address these challenges, we propose general sigmoid surrogate with theoretically validated fairness and stability guarantees to deal with large margin points. The theoretical analysis further provides insights to the community that dealing with the large margin points issue as well as obtaining a more balanced dataset contribute to a fairer and more stable classifier. We further elaborate balanced surrogates method, which is an iterative algorithm to reduce the gap during training. It is also applicable to other fairness surrogate functions. Finally, our experiments using three real-world datasets not only validate the insights of our theorems, but also show that our methods get better fairness and stability performance.

References

- Alekh Agarwal, Alina Beygelzimer, Miroslav Dudik, John Langford, and Hanna Wallach. A reductions approach to fair classification. In *Proceedings of the 35th International Conference on Machine Learning*, 2018.
- Solon Barocas and Andrew D Selbst. Big data’s disparate impact. *California law review*, pp. 671–732, 2016.
- Solon Barocas, Moritz Hardt, and Arvind Narayanan. *Fairness and Machine Learning*. fairmlbook.org, 2019. <http://www.fairmlbook.org>.
- Yahav Bechavod and Katrina Ligett. Penalizing unfairness in binary classification. *arXiv preprint arXiv:1707.00044*, 2017.
- Andrew Bell, Lucius Bynum, Nazarii Drushchak, Tetiana Zakharchenko, Lucas Rosenblatt, and Julia Stoyanovich. The possibility of fairness: Revisiting the impossibility theorem in practice. In *Proceedings of the 2023 ACM Conference on Fairness, Accountability, and Transparency*, pp. 400–422, 2023.
- Harry Bendekgey and Erik B. Sudderth. Scalable and stable surrogates for flexible classifiers with fairness constraints. In *Advances in Neural Information Processing Systems*, 2021.
- Richard Berk, Hoda Heidari, Shahin Jabbari, Matthew Joseph, Michael Kearns, Jamie Morgenstern, Seth Neel, and Aaron Roth. A convex framework for fair regression. In *Fairness, Accountability, and Transparency in Machine Learning (FATML)*, 2017.
- Toon Calders, Faisal Kamiran, and Mykola Pechenizkiy. Building classifiers with independency constraints. In *2009 IEEE International Conference on Data Mining Workshops*, 2009.
- Flavio P. Calmon, Dennis Wei, Bhanukiran Vinzamuri, Karthikeyan Natesan Ramamurthy, and Kush R. Varshney. Optimized pre-processing for discrimination prevention. In *Advances in Neural Information Processing Systems*, 2017.
- Simon Caton and Christian Haas. Fairness in machine learning: A survey. *arXiv preprint arXiv:2010.04053*, 2020.
- Nitesh V Chawla, Kevin W Bowyer, Lawrence O Hall, and W Philip Kegelmeyer. Smote: synthetic minority over-sampling technique. *Journal of artificial intelligence research*, 16:321–357, 2002.
- Irene Chen, Fredrik D Johansson, and David Sontag. Why is my classifier discriminatory? *Advances in neural information processing systems*, 31, 2018.
- Alexandra Chouldechova. Fair prediction with disparate impact: A study of bias in recidivism prediction instruments. *Big data*, 5(2):153–163, 2017.
- Ching-Yao Chuang and Youssef Mroueh. Fair mixup: Fairness via interpolation. In *Proceedings of the International Conference on Machine Learning*, 2021.

- Jiahao Ding, Xinyue Zhang, Xiaohuan Li, Junyi Wang, Rong Yu, and Miao Pan. Differentially private and fair classification via calibrated functional mechanism. *Proceedings of the AAAI Conference on Artificial Intelligence*, 2020.
- Michele Donini, Luca Oneto, Shai Ben-David, John S Shawe-Taylor, and Massimiliano Pontil. Empirical risk minimization under fairness constraints. In *Advances in Neural Information Processing Systems*, 2018.
- Sanghamitra Dutta, Dennis Wei, Hazar Yueksel, Pin-Yu Chen, Sijia Liu, and Kush Varshney. Is there a trade-off between fairness and accuracy? a perspective using mismatched hypothesis testing. In *International conference on machine learning*, pp. 2803–2813. PMLR, 2020.
- Michael Feldman, Sorelle A. Friedler, John Moeller, Carlos Scheidegger, and Suresh Venkatasubramanian. Certifying and removing disparate impact. In *Proceedings of the 21th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, 2015.
- Benjamin Fish, Jeremy Kun, and Ádám D. Lelkes. A confidence-based approach for balancing fairness and accuracy. In *Proceedings of the 2016 SIAM International Conference on Data Mining*, 2016.
- Sorelle A Friedler, Carlos Scheidegger, Suresh Venkatasubramanian, Sonam Choudhary, Evan P Hamilton, and Derek Roth. A comparative study of fairness-enhancing interventions in machine learning. In *Proceedings of the conference on fairness, accountability, and transparency*, pp. 329–338, 2019.
- Isabel O Gallegos, Ryan A Rossi, Joe Barrow, Md Mehrab Tanjim, Sungchul Kim, Franck Dernoncourt, Tong Yu, Ruiyi Zhang, and Nesreen K Ahmed. Bias and fairness in large language models: A survey. *arXiv:2309.00770*, 2023.
- Prakhar Ganesh, Hongyan Chang, Martin Strobel, and Reza Shokri. On the impact of machine learning randomness on group fairness. In *Proceedings of the 2023 ACM Conference on Fairness, Accountability, and Transparency*, pp. 1789–1800, 2023.
- Gabriel Goh, Andrew Cotter, Maya Gupta, and Michael P Friedlander. Satisfying real-world goals with dataset constraints. In *Advances in Neural Information Processing Systems*, 2016.
- Moritz Hardt, Eric Price, and Nathan Srebro. Equality of opportunity in supervised learning. In *Proceedings of the 30th International Conference on Neural Information Processing Systems*, 2016.
- Surya Mattu Julia Angwin, Jeff Larson and Lauren Kirchner. Machine bias: There’s software used across the country to predict future criminals. and it’s biased against blacks. propublica, 2016. URL <https://www.propublica.org/article/machine-bias-risk-assessments-in-criminal-sentencing>.
- Faisal Kamiran and Toon Calders. Data pre-processing techniques for classification without discrimination. *Knowledge and Information Systems*, 2011.
- Faisal Kamiran, Asim Karim, and Xiangliang Zhang. Decision theory for discrimination-aware classification. In *2012 IEEE 12th International Conference on Data Mining*, 2012.
- Toshihiro Kamishima, Shotaro Akaho, Hideki Asoh, and Jun Sakuma. Fairness-aware classifier with prejudice remover regularizer. In *Proceedings of the 2012th European Conference on Machine Learning and Knowledge Discovery in Databases - Volume Part II*, 2012.
- Jon Kleinberg, Sendhil Mullainathan, and Manish Raghavan. Inherent trade-offs in the fair determination of risk scores. In *Innovations in Theoretical Computer Science (ITCS)*, 2017.
- Ron Kohavi. Scaling up the accuracy of naive-bayes classifiers: A decision-tree hybrid. In *Proceedings of the Second International Conference on Knowledge Discovery and Data Mining*, 1996.
- Zachary Lipton, Julian McAuley, and Alexandra Chouldechova. Does mitigating ml’s impact disparity require treatment disparity? *Advances in neural information processing systems*, 31, 2018.

- Lydia T Liu, Max Simchowitz, and Moritz Hardt. The implicit fairness criterion of unconstrained learning. In *International Conference on Machine Learning*, pp. 4051–4060, 2019.
- Michael Lohaus, Michael Perrot, and Ulrike Von Luxburg. Too relaxed to be fair. In *Proceedings of the 37th International Conference on Machine Learning*, 2020.
- Ninareh Mehrabi, Fred Morstatter, Nripsuta Saxena, Kristina Lerman, and Aram Galstyan. A survey on bias and fairness in machine learning. *ACM Computing Surveys*, 54:1–35, 2021.
- Kirtan Padh, Diego Antognini, Emma Lejal-Glaude, Boi Faltings, and Claudiu Musat. Addressing fairness in classification with a model-agnostic multi-objective algorithm. In *Proceedings of the Thirty-Seventh Conference on Uncertainty in Artificial Intelligence*, 2021.
- Geoff Pleiss, Manish Raghavan, Felix Wu, Jon Kleinberg, and Kilian Q Weinberger. On fairness and calibration. In *Advances in Neural Information Processing Systems*, pp. 5684–5693, 2017.
- Sandro Radovanović, Boris Delibasić, and Milija Suknović. Do we reach desired disparate impact with in-processing fairness techniques? *Procedia Computer Science*, 214:257–264, 2022.
- P. Cortez S. Moro and P. Rita. A data-driven approach to predict the success of bank telemarketing, 2014. URL <https://archive.ics.uci.edu/ml/datasets/bank+marketing>.
- Changjian Shui, Gezheng Xu, Qi Chen, Jiaqi Li, Charles X Ling, Tal Arbel, Boyu Wang, and Christian Gagné. On learning fairness and accuracy on multiple subgroups. *Advances in Neural Information Processing Systems*, 35:34121–34135, 2022.
- Yongkai Wu, Lu Zhang, and Xintao Wu. On convexity and bounds of fairness-aware classification. In *The World Wide Web Conference*, 2019.
- Muhammad Bilal Zafar, Isabel Valera, Manuel Gomez Rodriguez, and Krishna P. Gummadi. Fairness beyond disparate treatment & disparate impact. *Proceedings of the 26th International Conference on World Wide Web*, 2017a.
- Muhammad Bilal Zafar, Isabel Valera, Manuel Gomez Rodriguez, Krishna P. Gummadi, and Adrian Weller. From parity to preference-based notions of fairness in classification. In *Proceedings of the 31st International Conference on Neural Information Processing Systems*, 2017b.
- Muhammad Bilal Zafar, Isabel Valera, Manuel Gomez Rogriguez, and Krishna P. Gummadi. Fairness constraints: Mechanisms for fair classification. In *Proceedings of the 20th International Conference on Artificial Intelligence and Statistics*, 2017c.
- Muhammad Bilal Zafar, Isabel Valera, Manuel Gomez-Rodriguez, and Krishna P. Gummadi. Fairness constraints: A flexible approach for fair classification. *Journal of Machine Learning Research*, 2019.
- Rich Zemel, Yu Wu, Kevin Swersky, Toni Pitassi, and Cynthia Dwork. Learning fair representations. In *Proceedings of the 30th International Conference on Machine Learning*, 2013.
- Daochen Zha, Zaid Pervaiz Bhat, Kwei-Herng Lai, Fan Yang, Zhimeng Jiang, Shaochen Zhong, and Xia Hu. Data-centric artificial intelligence: A survey. *arXiv preprint arXiv:2303.10158*, 2023.
- Tao Zhang, Tianqing Zhu, Mengde Han, Jing Li, Wanlei Zhou, and Philip S. Yu. Fairness constraints in semi-supervised learning. *arXiv preprint arXiv:2009.06190*, 2020.
- Chen Zhao, Changbin Li, Jincheng Li, and Feng Chen. Fair meta-learning for few-shot classification. In *2020 IEEE International Conference on Knowledge Graph (ICKG)*, 2020.
- Han Zhao and Geoffrey J Gordon. Inherent tradeoffs in learning fair representations. *The Journal of Machine Learning Research*, 23(1):2527–2552, 2022.