Evaluating supernets for neural architecture search

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Abstract In order to address the costly process of evaluating candidate architectures in neural architecture search (NAS), ENAS introduced supernets, a single network representing the entire search space. DARTS then added a set of architecture weights to this structure, allowing an entirely gradient-descent-based approach to NAS and leading to supernets becoming a common feature of efficient NAS algorithms. Although following research has demonstrated numerous improved techniques for training supernets, these methods are typically compared solely through the performances of the final architectures selected from the supernets without any direct comparison of the supernets themselves. We provide methods which exploit the availability of NAS benchmark data sets to provide a robust direct evaluation of trained supernets, both of the weights shared across candidate architectures as well as architecture weights. We also use these methods to analyze the process of NAS training and provide insight on how the top supernet NAS algorithms are able to effectively exploit the supernet structure.

1 Introduction

Neural architecture search (NAS) provides a data-driven algorithmic approaches to the complex design problem of building a neural network. However, the initial approach of evaluating candidate architectures by training each one resulted in search algorithms requiring 1000s of GPU-hours for a single run (Zoph et al., 2018).

Pham et al. (2018) provided a method to search for an architecture in a comparable amount of 22 time as required to train the final model by training a single supernetwork instead of individual 23 candidate networks. The supernet is a single model representing the entire architecture search 24 space, essentially a superposition of every allowed candidate model. Then Liu et al. (2019) took 25 advantage of this structure sharing weights across all candidates by adding trainable architecture 26 weights to each possible operation in the supernet, allowing for search and training to be conducted 27 via gradient descent. These innovations combined to offer a practical and promising approach to 28 NAS. 29

However, while the marriage of gradient-based NAS with supernets may simplify the implemen-30 tation of NAS algorithms, it also serves to obscure the search process. While NAS algorithms can 31 generally be described as an iterative process of search over candidate architectures and obtaining 32 estimates of their performance (Elsken et al., 2019), in DARTS this only occurs implicitly. DARTS 33 does not actually evaluate individual candidate architectures at any point in training, instead 34 training over a "continuous relaxation" of possible architectures Liu et al. (2019). This collapse of 35 the NAS training loop to gradient-based training of two sets of interdependent weights makes it 36 more difficult to ascertain why, in various contexts, some NAS algorithms are highly effective and 37 others fail. 38

We address these limitations through the direct evaluation of trained supernets using NAS benchmark datasets. We propose two separate general-purpose methods focused on separate components of the supernet. One method is focused on evaluating the shared weights of the supernet, determining how suitable they are for the various architectures in the search space which share them. The second method evaluates the architecture weights (or architecture distribution) 43

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learned by DARTS-like algorithms during the process of training the supernet. Both methods make
use of NAS benchmarks to analyze how the learned weights vary across the architecture search
space in comparison to trained-from-scratch test accuracy. We implement these methods in the
NASLib library with the intention of making them widely available as evaluation tools.

The methods we demonstrate provide additional insight into the algorithms evaluated, revealing not only differences in performance obfuscated by similarities in the final test accuracy, but also insight into how these algorithms are able to successfully exploit the structure of the supernet. We are able to demonstrate a greater capacity for supernets to identify top performing architectures than previously described (White et al., 2021).

The primary contributions of this work are thus to demonstrate and highlight that:

- That algorithms that succeed in supernet training do so by specializing to maximize performance estimation on (only) the top architectures in the search space (Sec. 2)
- This specialization of the supernet is enabled by the structure of the search space (Sec. 3)

2 Evaluating supernets

Prior work on issues with NAS evaluation has produced a set of best practices to support fair 58 and reliable comparison between NAS methods, including evaluating in the same search space 59 as comparable methods, using the same routine to train the final selected architecture, reporting 60 results of multiple random seeds, and performing ablation studies (Yu et al., 2020) Even following 61 all of these practices and, even better, evaluating your algorithm using a NAS benchmark data 62 set, we argue that reporting the final train-from-scratch test accuracy of your model as the sole 63 metric of evaluation will still fail to reveal key information about the results. For example, final 64 test accuracy measurements reveal little about the dependence of the result on the search space 65 used, such as DARTS' notable failure on NAS-Bench-201 (Dong and Yang, 2020). Evaluating the 66 supernet directly has the potential to provide more generalizable insights into the performance of 67 NAS algorithms. By understanding the mechanisms which a NAS algorithm is able to obtain its 68 result, we are better equipped to anticipate how it'll perform in other search spaces and training 69 contexts. 70

Our main approach to analyzing the shared weights of the supernet is based on model ranking. 71 This approach, ranking candidate architectures based on validation accuracy obtained with the 72 shared weights, is used for architecture selection in supernet NAS methods that don't train arch 73 weights, such as one-shot NAS Bender et al. (2018). We apply this method across a broader set of 74 supernet NAS algorithms, arguing that while DARTS may never use its shared weights in training 75 to evaluate an actual candidate architecture, examining how suitable the shared weights are for 76 varying architectures allows us to utilize the search space to analyze how learning the architecture 77 weights has trained the shared weights. 78

Supernet NAS methods have been previously shown to produce model rankings with low 79 correlation White et al. (2021). We argue that correlation is a poor indicator of the efficacy of a 80 supernet's shared weights. Making a relative distinction between poor performing architectures 81 is of little value to supernet NAS methods while distinguishing top architectures from the rest is 82 key. Correlation metrics do not account for how the significance of correct ranking varies over 83 the architecture space. Instead, we report the "top architecture ID rate", which we define as the 84 proportion of the top k architectures, ranked by benchmark test accuracy, which are correctly 85 ranked in the top k by validation accuracy via the shared weights. Note that this metric was 86 proposed prior by Ning et al. (2021) as "precision@topk", a name which we do not adopt as this 87 metric corresponds to both precision and recall in this case. We expand on this work by applying 88 this metric to a broader range of supernet NAS methods, providing novel insights into the process 89 of supernet training. 90

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Figure 1: (*Left*) The ability of an algorithm to identify the top architectures in a search space as a function of the threshold for "top" architecture. (*Right*) Cumulative sampling probability across test error threshold groups of the search space, showing these two algorithms as most likely to sample the highest performing architectures. (*Top*) plots show results on CIFAR10 and (*Bottom*) plots show results on ImageNet16-120, all in the NAS-Bench-201 search space.

Our method of evaluating learned architecture weights is simply to compute a sampling probability for each architecture from these weights and view how NAS algorithms assign probability mass over the architecture space. For search spaces, like that of DARTS/NAS-Bench-301, which apply further constraints to the architecture space than NAS-Bench-201 does, this will require defining a sampling process based on the discretization steps used to derive a final architecture.

Both of these measurements, for the shared-weights and the architecture-weights, were implemented as a variant Trainer class for the NASLib library in order to make them widely accessible for use as a general evaluatory tool (Ruchte et al., 2020; Mehta et al., 2022). Between the range of search spaces and data sets already provided through NASLib and these metrics, future researchers who implement their proposed NAS algorithms on NASLib will have a full suite of methods for understanding how and why their algorithms performance varies across contexts.

Most methods for supernet training do not outperform the naive random baseline for most 102 top-architecture thresholds, which aligns with previous work reporting supernet methods to be 103 ineffective at predicting performance in this way (Yu et al., 2020; White et al., 2021). However, 104 some algorithms (e.g. DirichletNAS (Chen et al., 2021) and SNAS (Xie et al., 2019)) are able to 105 identify more accurately the very top architectures in the search space (left side of the subfigure) 106 but show no additional ability in distinguishing between fairly low-performing architectures (right 107 side of the subfigure). This highlights that shared-weight models need not be (and likely cannot be) 108 trained to be well suited for all architectures within a search space. Rather, they will likely be most 109



Figure 2: (*Left*) Supernet validation accuracy vs benchmark test accuracy averaged over architecture clusters for a sample SNAS run. (*Right*) Supernet validation accuracy vs benchmark test accuracy averaged over architecture clusters for a sample DrNAS run.

informative for helping us to identify top architectures if those shared weights are specialized to maximize performance estimation of the highest performing architectures. This capability is missed in previous studies by the ranking correlation metrics used to assess performance predictions, and in Ning et al. (2021) as a result of only evaluating a less effective supernet training algorithm than SNAS and DirichletNAS.

A second metric for accessing quality of trained supernet models is how likely it is to sample a 115 top architecture (if sampled at the end of training). Again using the ranking of architectures by the 116 benchmarked test accuracy, we parameterize a probability distribution over the search space using 117 the supernet's architecture weights to assess the likelihood of sampling architectures of a given 118 rank or better. Fig 1 (*right*) shows the cumulative sampling probability as the top-architecture 119 threshold is relaxed, relative to a baseline of randomly selecting architectures from the search 120 space. Algorithms above the cumulative baseline curve (e.g. DirichletNAS and SNAS again, and 121 - to a lesser extent - GDAS (Dong and Yang, 2019) and DARTS- (Chu et al., 2021)) oversample 122 higher performing architectures, while curves below the baseline (e.g. DARTS (Liu et al., 2019)) 123 oversample lower performing discrete architectures. 124

3 Understanding supernet specialization

The dirichlet sampling technique used by DrNAS clearly proves more effective at guiding the 126 search process than the Gumbel-Softmax approach to differentiable categorical sampling used by 127 SNAS. Both of these algorithms, do however, display some capacity to estimate performance and, 128 as shown in their performance prediction results over the search space, specifically are able to 129 estimate performance for better performing architectures. These results underscore the utility of 130 the top architecture ID rate measure, as the ineffectiveness of these methods for predicting the 131 performance of the lowest ranking architectures would lead to a low ranking correlation across the 132 entire architecture space. These results indicate that these algorithms are able to make successful 133 use of the supernet structure by specializing the shared weights to work for a set of structurally 134 similar high performing architectures. 135

We can explore this supernet specialization hypothesis by clustering the architectures by their structural similarity. To do so, we define the pairwise similarity between architectures as the number of overlapping operations in their encodings. Then, performing hierarchical clustering on the encodings, for a given threshold we can obtain a set of clusters and examine the relationship

between the average benchmark test accuracy of each cluster and the average validation accuracy 140 for the architectures of the cluster obtained using the shared weights. Shown above for sample 141 runs from SNAS and DrNAS in Fig 2, it is apparent that it is indeed the case that, while the shared 142 weights are far from optimal for every architecture, for many architectures they do not support 143 inference better than selection at random but for a subset of top architectures they do. The existence 144 of clusters of structurally similar, high-performing architectures which are able to be distinguished 145 from lower-performing architectures through obtaining validation accuracy measurements from 146 the supernet indicates that it is the structure of the search space, specifically, the presence of these 147 families of similarly effective designs, which enables this effective specialization of the supernet. 148

4 Conclusion

Although SNAS and DrNAS both attain final test accuracy scores near the optimal score for CIFAR10 150 on NAS-Bench-201, deeper analysis of the supernet algorithms trained by each method reveals 151 a more significant underlying disparity: DrNAS is considerably more successful at identify top 152 architectures, both through its shared weights and its architecture weights. This suggests that the 153 extent of the performance boost attained by DrNAS's switch to dirichlet architecture sampling is 154 obfuscated when viewing final test accuracy results alone by the limited size of the benchmark 155 search space. Together, these measures provide a set of tools supporting more robust evaluation of 156 NAS methods, made accessible for broad use through their implementation on top of the NASLib 157 library. 158

5 Limitations

This work only examines the proposed evaluation measures on a single NAS benchmark data set, 160 NAS-Bench-201. Therefore, the generalizability of the insights obtained from these measures across 161 search spaces cannot be confirmed. Additionally, these measures are computed over the entirety 162 of the search space, which is only possible for tabular benchmarks, so further work is needed to 163 extend these measures to surrogate NAS benchmarks, such as NAS-Bench-301 (Siems et al., 2022). 164 Additionally, while the specific set of supernet NAS methods evaluated are able to provide general 165 insights into the performance of supernet NAS algorithm through analysis based in the specific 166 differences between algorithm, the use of a wider set of supernet NAS algorithms could provide 167 even broader and more generalizable insights. 168

6 Broader Impact

Our work demonstrates a method for evaluating supernet-based NAS algorithms using benchmark 170 data sets, made easily accessible to researchers through implementation in the NASLib library. 171 Through this contribution to open-source NAS research we hope to encourage deeper NAS bench-172 mark use and more thorough evaluation in future supernet NAS research. A stronger scientific 173 understanding of supernet NAS techniques will aid in both the development and proliferation of 174 efficient architecture search methods. Ultimately, the widespread availability of highly effective 175 efficient architecture search methods has the potential to make the development of deep learning 176 models more widely accessible. While this does have the potential to make easier the development 177 of potentially harmful models, we believe that architecture search techniques also offers the poten-178 tial for a widely accessible method of auditing and guaranteeing properties of the architecture of 179 neural networks, therefore leading to more socially beneficial deep learning. 180

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Appendices

Α

Sı	ıbmi	ission Checklist	221
1.	For	all authors	222
	(a)	Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope? [Yes]	223 224
	(b)	Did you describe the limitations of your work? [Yes]	225
	(c)	Did you discuss any potential negative societal impacts of your work? [Yes]	226
	(d)	Have you read the ethics author's and review guidelines and ensured that your paper conforms to them? https://automl.cc/ethics-accessibility/ [Yes]	227 228
2.	If yo	ou are including theoretical results	229
	(a)	Did you state the full set of assumptions of all theoretical results? $[N/A]$	230
	(b)	Did you include complete proofs of all theoretical results? $[\rm N/A]$	231
3.	If yo	ou ran experiments	232
	(a)	Did you include the code, data, and instructions needed to reproduce the main experimental results, including all requirements (e.g., requirements.txt with explicit version), an instructive README with installation, and execution commands (either in the supplemental material or as a URL)? [Yes] Code for experiments is available at https://anonymous.4open.science/r/NASLib-F26E/	233 234 235 236 237
	(b)	Did you include the raw results of running the given instructions on the given code and data? [No] Data is excluded from code due to significant size without extensive computational requirements.	238 239 240
	(c)	Did you include scripts and commands that can be used to generate the figures and tables in your paper based on the raw results of the code, data, and instructions given? [No] Plotting code is not included at the time of submission, however more general visualization code to pair with the measures is in development.	241 242 243 244
	(d)	Did you ensure sufficient code quality such that your code can be safely executed and the code is properly documented? [Yes]	245 246
	(e)	Did you specify all the training details (e.g., data splits, pre-processing, search spaces, fixed hyperparameter settings, and how they were chosen)? [Yes] See Implementation details in Appendix B	247 248 249
	(f)	Did you ensure that you compared different methods (including your own) exactly on the same benchmarks, including the same datasets, search space, code for training and hyperparameters for that code? [Yes]	250 251 252
	(g)	Did you run ablation studies to assess the impact of different components of your approach? $\rm [N/A]$	253 254
	(h)	Did you use the same evaluation protocol for the methods being compared? [Yes]	255
	(i)	Did you compare performance over time? [No] This is a key component of this project in development for future work.	256 257
	(j)	Did you perform multiple runs of your experiments and report random seeds? [Yes]	258

	(k)	Did you report error bars (e.g., with respect to the random seed after running experiments multiple times)? [Yes]	259 260
	(l)	Did you use tabular or surrogate benchmarks for in-depth evaluations? [Yes]	261
	(m)	Did you include the total amount of compute and the type of resources used (e.g., type of GPUs, internal cluster, or cloud provider)? [Yes]	262 263
	(n)	Did you report how you tuned hyperparameters, and what time and resources this required (if they were not automatically tuned by your AutoML method, e.g. in a NAs approach; and also hyperparameters of your own method)? $[\rm N/A]$	264 265 266
	4. If ye	ou are using existing assets (e.g., code, data, models) or curating/releasing new assets	267
	(a)	If your work uses existing assets, did you cite the creators? [Yes]	268
	(b)	Did you mention the license of the assets? [No] Licensing was not mentioned in the main text, however, the only asset used, NASLib, is licensed via Apache 2.0.	269 270
	(c)	Did you include any new assets either in the supplemental material or as a URL? [Yes]	271
	(d)	Did you discuss whether and how consent was obtained from people whose data you're using/curating? $\rm [N/A]$	272 273
	(e)	Did you discuss whether the data you are using/curating contains personally identifiable information or offensive content? $[\rm N/A]$	274 275
	5. If ye	ou used crowdsourcing or conducted research with human subjects	276
	(a)	Did you include the full text of instructions given to participants and screenshots, if applicable? $\rm [N/A]$	277 278
	(b)	Did you describe any potential participant risks, with links to Institutional Review Board (IRB) approvals, if applicable? $\rm [N/A]$	279 280
	(c)	Did you include the estimated hourly wage paid to participants and the total amount spent on participant compensation? $\rm [N/A]$	281 282
B	Imple	mentation details	283
	Source	code is available at https://anonymous.4open.science/r/NASLib-F26E/. The runs presented	284
	used random seed [1001, 1002, 1003], run hyperparameters were the default hyperparameters u in NASI in the source code in		
			280
	scrip	ots/exp_hyperparam	287
	All hours	tests were run on AMD Radeon Instinct MI50 Accelerators, requiring roughly 925 GPU for all experiments.	288 289
С	Furth	er Supernet Evaluation Results and Details	290
	Our in	dependent evaluation of Stage-1 algorithms utilizes two statistics we developed, explained	291
	in furt	her detail below, which show two algorithms, SNAS and DrNAS, to be dominant. These	292
	algorit	hms are the only two to display a top arch ID rate above the baseline. This indicates that the	293
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shared-weights of their supernets have been trained such that they are capable of distinguishing the best architectures from the rest by computing validation accuracies. They also display the highest probability of sampling the best architectures in the search space. We hypothesize that these results are interrelated. As these are sampling based algorithms, sampling top architectures during training 297 allows the shared weights to be updated to be more suitable for these top architectures, which in turn improves the quality of gradient updates guiding the architecture weights toward top models.²⁹⁹

The significant improvement in the cumulative sampling probability shown from the addition of an auxiliary skip connection to DARTS, represented by the DARTS- results supports the hypothesis that overvaluing skip connections is a key issue for DARTS. As correcting for this overweighting seems to close the gap between DARTS and the baseline, it seems the cumulative sampling probability results for DARTS simply reflect a high probability of sampling an architecture which is low performing due to excessive skip connections.

Fig. 3 shows the plot of Stage-1 search algorithm performance estimation and architecture sampling metrics on CIFAR-100 in the NASBench-201 search space, corresponding to the plots on CIFAR-10 and ImageNet16-120 shown in Sec. 2. These results are consistent with those shown for CIFAR-10.



Figure 3: Left: Top arch ID rate across test regret threshold groups of the architecture space. Right: Sampling probability mass across test regret threshold groups of the probability space.

C.1 Top Architecture ID Rate

Previous NAS papers have utilized Spearman or Kendall-Tau ranking correlation to evaluate the capacity of NAS algorithms to estimate the performance of candidate models. Although these statistical are powerful tools to evaluate rankings, we argue that, when applied to the entirety of a NAS search space, they do not necessarily reflect the characteristics of performance estimation which are important to NAS algorithms.

For example, consider in the 15,625 architecture search space of NAS-Bench-201 one NAS 316 algorithm which ranks the top 625 architectures correctly and the bottom 15,000 in reverse order 317 compared to second NAS algorithm which ranks the architectures correctly except the first 625 318 models are, in reverse order, assigned the ranks of the last 625. Here the former NAS algorithm 319 would result in a Spearman correlation of -0.7695 and a Kendall Tau correlation of -0.8432 while 320 the latter would result in a Spearman correlation of 0.7695 and a Kendall Tau correlation of 0.8432. 321 But we argue that the 1st example NAS algorithm has succeeded at performance estimation: it 322 has correctly identified the global maximum and the ordering of the top 4% of the search space 323 while the 2nd example NAS algorithm has failed catastrophically, as it is maximally incorrect in its 324 estimation of the relative performance of the top 4% of the search space. 325

By utilizing a threshold-based statistic we can configure our measurement such that it reflects an NAS algorithm's capacity to estimate performance over specific regions of the search space, thus ignoring the algorithms inability to distinguish between similarly poorly performing models and capturing, in a coarser sense, the ability of the algorithm to distinguish better from worse models.

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For a given index based threshold in the true architecture ranking k, we compute a pair of error thresholds corresponding to this index using the benchmark test accuracies and the validation accuracies obtained using the shared weights of the trained supernet. We then identify the sets of architectures falling under each error threshold, which we denote T_k and V_k , respectively. Our top architecture ID rate metric is then given by:

$$a_{1,k} = \frac{|T_k \cap V_k|}{|T_k|}$$

C.2 Sampling probability mass

Due to the design of NAS-Bench-201's search space, which allows a single operation at each edge, the architecture weights, after a softmax, correspond exactly to set of categorical distributions (which we model as independent) over operations at each edge. If we consider the use of these distributions to sample architectures, we find that the probability of sampling any given architecture from a set of architecture weights can be computed efficiently as the inner product of the one-hot representation of that architecture and the architecture weights. 320

Note that, while a wide range of architecture parameterizations permit the creation of a sampler based on learned architecture weights, it is often less straightforward than in NASBench-201. For example, in the search space of DARTS, each node selects two incoming edges out of all operations across all nodes with potential in-edges. Creating a sampler in this search space would then require designing a scheme for combining and comparing the weights across different in-edges and a method to sample a pair of operations rather than a single operation. 333

Following the notation given above for the top architecture ID rate based on the set of architectures (T_k) under an error benchmark test error threshold of k, we can also denote our cumulative sampling probability metric. Our metric for architecture sampling is:

$$a_{2,k} = \sum_{\alpha \in T_k} Pr(\alpha)$$

Note that in our toy example from the previous section, for $k \le 625$, a_1 will be 1 for the first, successful, NAS algorithm and 0 for the second, failing one. 340