

# LARGE LANGUAGE MODELS ARE NOT STRONG ABSTRACT REASONERS

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## ABSTRACT

Large Language Models have shown tremendous performance on a large variety of natural language processing tasks, ranging from text comprehension to common sense reasoning. However, the mechanisms responsible for this success remain opaque, and it is unclear whether LLMs can achieve human-like cognitive capabilities or whether these models are still fundamentally circumscribed. Abstract reasoning is a fundamental task for cognition, consisting of finding and applying a general pattern from few data. Evaluating deep neural architectures on this task could give insight into their potential limitations regarding reasoning and their broad generalisation abilities, yet this is currently an under-explored area. In this paper, we introduce a new benchmark for evaluating language models beyond memorization on abstract reasoning tasks. We perform extensive evaluations of state-of-the-art LLMs, showing that they currently achieve very limited performance in contrast with other natural language tasks, and we examine the reasons for this difference. We apply techniques that have been shown to improve performance on other NLP tasks and show that their impact on abstract reasoning is limited.

## 1 INTRODUCTION

Large Language Models (LLMs) have recently achieved impressive performance on a large variety of Natural Language Processing (NLP) tasks, including text comprehension (Devlin et al., 2019; Radford et al., 2019), commonsense reasoning (Talmor et al., 2020), translation (Raffel et al., 2020), and code generation (Chen et al., 2021; Bubeck et al., 2023), and have shown promising results for out-of-distribution generalisation (Brown et al., 2020; Bubeck et al., 2023). The most recent and larger language models also perform well on mathematical problems, which had been out of reach for transformers for a long time (Chen et al., 2022; Stolfo et al., 2022). While empirical testing of LLMs trained on large corpora of data yields signs of high comprehension of presented problems, there is little theoretical evidence regarding why and how this performance has been achieved and whether these models are simply memorising the training data, extrapolating it, or some combination (Tirumala et al., 2022; Goyal & Bengio, 2020). A notable limitation of these models is a lack of control mechanisms, or possible misalignment (Ouyang et al., 2022), for which the absence of a world model or causal representation have been advanced as explanations (Bender et al., 2021; Willig et al., 2022). More recently, early experiments on GPT-4 showed signs of limitations on reasoning tasks requiring planning and backtracking (Bubeck et al., 2023). Despite these early limitations, the question of whether or not LLMs can perform human-like reasoning remains open, as measuring the intelligence, or more broadly, the competence, of a system is a challenging task (Chollet, 2019).

Abstract reasoning is a potential task for effective measurement of the cognitive abilities of neural models (Santoro et al., 2018; Chollet, 2019). Abstract reasoning problems consist of identifying generic structures over a small set of examples and applying them to unseen cases. They aim to evaluate the ability of a system to integrate a new skill or process from limited data. The abstract nature of these problems helps avoid spurious correlations that could lie in the data and may create potential bias in the results. In particular, this task is well-suited for evaluating the broad or strong generalisation capacity of a system, i.e. its ability to handle a large category of tasks and environments without human intervention, including situations that may not have been foreseen when the system was created (Chollet, 2019). This is a well-studied class of task in the field of program induction (Ellis et al., 2020; Lake et al., 2015). However, the problem of abstract reasoning has long remained

outside the scope of evaluation of language models, and there currently exist no extensive evaluations of the performance of LLMs in this domain.

In this paper, we seek to bridge this gap by investigating the abstract reasoning abilities of LLMs and by providing insight into the following question: Do LLMs contain sufficient building blocks for broad generalisation, or do they lack fundamental capabilities? We evaluate state-of-the-art LLMs on abstract reasoning tasks, applying recent fine-tuning and prompt design techniques that have been shown to improve performance on other NLP tasks. To this end, we create a benchmark based on existing datasets and novel datasets transposed from vision tasks and adapted to text-based models. We then perform extensive experiments on this benchmark. We also build and train a language model for abstract reasoning and compare its performance with the other models. Our results indicate that Large Language Models do not yet have the ability to perform sound abstract reasoning. All of the tested models exhibit poor performance, and the tuning techniques that improved LLM reasoning abilities do not provide significant help for abstract reasoning. We provide our code and data in the non-anonymous version of the paper. Our contributions can be summarised as follows:

- We evaluate Large Language Models on abstract reasoning tasks.
- We show that existing training and tuning techniques do not help increase the performance of LLMs for abstract reasoning.
- We create a benchmark for the evaluation of language models for abstract reasoning.

## 2 RELATED WORK

The abilities of Language Models have been thoroughly studied on a wide range of problems. In particular, their reasoning capacities are the focus of a great deal of recent work. Some of this (Wei et al., 2022; Li et al., 2022; Chen et al., 2022) has explored prompt techniques to improve mathematical reasoning in LLMs; Stolfo et al. (2022) propose a framework based on causality theory to evaluate language models on this kind of task. Recently, GPT-4 has been shown to perform well on mathematical problems, outperforming PaLM and LLaMA (Chowdhery et al., 2022; Touvron et al., 2023), although it still produces calculation mistakes (Bubeck et al., 2023). In the domain of logical reasoning, several methods and benchmarks exist for evaluating language models. Notable benchmarks include DEER (Yang et al., 2022), ParaRules (Clark et al., 2020), PARARULE-Plus (Bao et al., 2022), ReClor (Yu et al., 2020), LogiQA (Liu et al., 2020), and AbductionRules (Young et al., 2022). Models such as LReasoner (Wang et al., 2022a), MERIt (Jiao et al., 2022), and AMR-LE (Bao et al., 2023) attempt to induce logical reasoning abilities in language models, but the performance of the most recent LLMs is yet to be evaluated. Similarly, the CLRS dataset benchmark for evaluating algorithmic reasoning has not yet been applied to language models (Velickovic et al., 2022). Causal structure discovery and causal inference are other domains where LLMs have shown mixed results (Willig et al., 2022; Kiciman et al., 2023). These tasks are distinct from commonsense causal reasoning, where LLMs perform well (Gordon et al., 2012; Zhang et al., 2022; Kiciman et al., 2023). Early experiments with GPT-4 (Bubeck et al., 2023) showed that, despite presenting systematically better performance than its previous versions, it still has some innate limitations. The authors introduce several examples indicating that the autoregressive nature of LLMs may prevent them from planning and backtracking, two abilities necessary for complex reasoning (Bubeck et al., 2023). GPT-4 also does not always reason in a consistent manner. Although it produces consistent results more often than GPT-3, there are no guarantees that the process leading to the result is always correct. The scope of cognitive abilities of the system remain incompletely characterised, especially for precise reasoning (Bubeck et al., 2023).

The evaluations described above do not, of course, provide a measure of the intelligence or global cognitive abilities of those models; measuring the level of intelligence of LLMs and other AI systems is challenging as there is no clear widely accepted definition (Booch et al., 2021; Goyal & Bengio, 2020). Chollet (2019) defines the intelligence of a system as "a measure of its skill-acquisition efficiency over a scope of tasks, with respect to priors, experience, and generalization difficulty". Following this definition, abstract reasoning is a well-suited domain over which to measure aspects of the learning and generalisation abilities of a system. To this end, the Abstract Reasoning Challenge (ARC) has been proposed as a benchmark for artificial systems (Chollet, 2019). A handful of works have proposed to measure abstract reasoning abilities in neural networks, but they focus on visual tasks (Santoro et al., 2018; Zhang et al., 2019; 2021a). To the best of our knowledge, this paper is

the first to present an extensive evaluation of abstract reasoning for Large Language Models. Other domains of study focus on problems similar to abstract reasoning. Notably, in program induction, DreamCoder is a system that learns to solve problems described by a small set of input-output pairs by writing programs (Ellis et al., 2020). Abstract reasoning can also be related to causal representation learning, as finding abstract relations amounts to recovering the causal structure of a task and the Independent Causal Mechanisms (ICMs) linking the variables (Schölkopf et al., 2021; Gendron et al., 2023).

### 3 EVALUATION METHOD

#### 3.1 EVALUATION DATA

To evaluate language models on a large variety of abstract reasoning tasks, we build a new framework that adapts text and vision datasets for abstract reasoning. We select the tasks based on their capacity to evaluate the ability of a system to find a general abstract rule from limited examples. The visual datasets are converted into text and symbolic versions to be used with language models. After formatting, the datasets can be divided into two categories: Open-Ended Question Answering (Open QA) and Multiple-Choice Question Answering (MCQA). Open QA datasets require the model to generate the correct answer, while MCQA requires it to choose the answer from a set of possible answers. We note that most of the evaluated models are built for general-purpose text generation. Therefore, even when choosing between several options, they must *generate* the correct choice and may fail to do so (e.g. answering D when only options A, B, or C are available). For comparison, we also evaluate models built for question answering. We give more details in Section 3.2. As shown in Figure 1, QA engines can only answer MCQA datasets, while text completion models can answer any type of question. Some MCQA datasets can also be converted to Open QA datasets by removing the choices. The datasets obtained are summarised in Table 1.

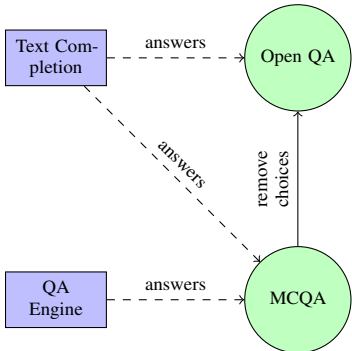


Figure 1: Different types of models and datasets considered in our experiments and their interactions. Dataset types are represented as green circles and model types are represented as blue rectangles. Text completion models can answer both types of datasets while QA engines can only answer MCQA datasets. However, MCQA datasets can be altered to fit into the Open QA category.

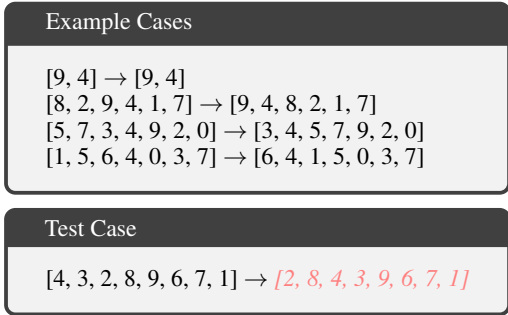


Figure 2: Example task in the BIG-Bench-F dataset. For this task, the system must return the input list with the first two elements switched with the following two if they exist. Pre-prompts are omitted from the input. In the test case, the target answer is indicated in *italics*.

**ACRE** We build a text-based version of the Abstract Causal Reasoning (ACRE) dataset (Zhang et al., 2021a) that we name  $ACRE^T$ . ACRE is a Visual Question-Answering (VQA) dataset. Each sample in the data comprises six context images and four test cases. Each context image comprises a set of objects with various shapes, colours and textures, and a light. In the context images, the light can be on or off. The goal of a system is to determine from the context examples if the light is on, off, or if its state cannot be determined in the test cases. To solve this task, the model has to determine for each sample what objects are causally responsible for the activation of the light. We generate two versions of the dataset: in  $ACRE^T$ -Text, each image is replaced by a high-level textual description, and in  $ACRE^T$ -Symbolic, each image is replaced with a numerical vector representation.

Table 1: Datasets considered. When not written, type is similar to the one above. Datasets can exist in text or symbolic versions. Text datasets built from an image dataset are indicated with the symbol  $T$ .

Dataset	Type	Versions	
		Text	Symb
ARC $T$	Open QA		✓
BIG-Bench-F			✓
Evals-S			✓
PVR			✓
ACRE $T$	MCQA	✓	✓
Evals-P			✓
RAVEN $T$		✓	✓

Table 2: Models considered. When not written, type is similar to the one above. Models with the symbol \* are introduced in this paper. "-AR" indicates that the model has been fine-tuned for abstract reasoning.

Model	Type
GPT-2	Text completion
Text-Davinci-3	
GPT-3.5-Turbo	
GPT-4	
LLaMA-7B	
Alpaca	
Alpaca-LoRA	
RoBERTa-AR*	Question Answering
MERIt-AR*	

**ARC** The second dataset we build on is the Abstract Reasoning Challenge (ARC) dataset (Chollet, 2019). The dataset is composed of tasks, each comprising three input and output grids. The goal of the system is to determine the algorithm that converts the input to the output and apply it to a test case. The grids have a variable size comprised between  $8 \times 8$  and  $30 \times 30$ , and contain visual patterns (e.g. recognisable shapes, symmetries). We provide the raw grid to the model as a two-dimensional array of integers. We name this version ARC $T$ . The high dimensionality of the input makes it a challenging task for LLMs. The tasks themselves are also challenging as their transcription in natural language is often complex and supposedly impossible for 12% of them (Acquaviva et al., 2021).

**BIG-Bench** We select a subset of the BIG-Bench dataset (Rule, 2020; Srivastava et al., 2022) that we name BIG-Bench-F for *Functions*. The subset comprises various tasks represented by a function taking a list as input and returning a new transformed list as output. For each task, several input-output samples are given. In BIG-Bench-F, we give four samples per task by default. The functions include typical list processing like replacing the value of one element, selecting a subset, or counting elements. An example is given in Figure 2. The challenge in this task is to accurately recognise the function from a few samples.

**Evals** We select a subset of the Evals dataset (OpenAI, 2023) representing logic puzzles. Evals-P is a set of tasks where a tuple containing a character and a list of characters is given as an input, and a single word from the set {"foo", "bar"} is generated from the input according to a logic hidden from the evaluated system. The task consists of finding the logic from a few samples and applying it to a test case. Evals-S is another set of tasks where a list of integers is given as an input, and an output list of words is generated. The task is the same as for Evals-P.

**PVR** Pointer-Value Retrieval (PVR) tasks (Zhang et al., 2021b) involve selecting one or several values in a list and applying a function on this subset. For each task, the system must recognise the retrieval and application functions and apply them to a test case. Samples are composed of a pointer-values pair and a label. The values are stored in an array, and the pointer is an integer pointing to an index in the array. The pointer indicates the subset of values to consider for the task. We generate a new dataset of PVR tasks following this methodology.

**RAVEN** RAVEN (Zhang et al., 2019) is a VQA dataset composed of sequences of images to complete. The images contain Raven matrices (Raven, 1938), i.e. geometric shapes (e.g. square, circle, pentagon) assembled together. RAVEN is a dataset similar to Procedurally Generated Matrices (PGM) (Santoro et al., 2018) but also provides a tree structure describing the semantics of each image. We focus on a subset where a single shape appears in the image. The task is, given a sequence of eight images and eight possible choices, to pick the correct image that follows in the sequence. As RAVEN is a visual dataset like ACRE, we use the given semantic tree structure to generate a text description of each image we will feed to the evaluated models. We create two sets: RAVEN $T$ -Text contains natural language descriptions, and RAVEN $T$ -Symbolic contains symbolic descriptions. We also build another version of the dataset where choices are hidden. We name the former RAVEN $T$ -mcqa and the latter RAVEN $T$ -opqa.

### 3.2 MODELS EVALUATED

We perform evaluations on the most recent and popular architectures for NLP tasks. Table 2 provides the list of models used in the experiments.

**Text Completion Models** We restrict our experiments to Large Language models, also named *Foundation Models* (Bommasani et al., 2021). We conduct experiments on the popular family of GPT architectures. We include three generations of GPT models: GPT-2 (Radford et al., 2019), a 1.5B parameter model; aligned GPT-3 models with Text-Davinci-3, optimised for text completion, and GPT-3.5-Turbo, optimised for chat, two 175B models (Brown et al., 2020; Ouyang et al., 2022); and GPT-4, for which the training and architectural details are unknown (OpenAI, 2023). We also perform experiments on LLaMA (Touvron et al., 2023) and its variants. In particular, Alpaca is a fine-tuned version of LLaMA to respond to instructions (Wang et al., 2022b; Taori et al., 2023), and Alpaca-LoRA is a LLaMA model instruction-tuned using Low-Rank Adaptation (Hu et al., 2022). For the three models, we evaluate the 7B parameters versions.

**QA Engines** We also compare these generic models on architecture fine-tuned for Multiple-Choice Question Answering. Unlike the text completion engines that produce text in the output, their task consists of discriminating the solution from a small set of options. This problem is more straightforward to solve than the problem of next token prediction tackled by the models described in the previous paragraph. We fine-tune two models for Multiple-Choice Question Answering: RoBERTa-large (Liu et al., 2019), a language model used for text comprehension, and MERIt (Jiao et al., 2022), a model using contrastive pre-training on rules-based data to perform logical reasoning.

### 3.3 METHODOLOGY

For Text-Davinci-3, GPT-3.5-Turbo, and GPT-4, we use the Open AI API to run all the evaluations. Text-Davinci is a text-completion model, so we convert our input context and question to a single string. GPT-3.5-Turbo and GPT-4 are chat completion models, so we provide the instructions in chat format. The pre-prompt and examples are given to the model by the system, and the supposed user gives the question. We use a temperature of 0.5 for the output generation to enhance the diversity of reasoning paths. More details are provided in the appendix. For GPT-2, LLaMA-7B, Alpaca, Alpaca-LoRA, RoBERTa-large, and MERIt, we use the weights provided on the Huggingface hub. RoBERTa-large and MERIt are used as MCQA models, while the others are used as causal language modelling models. We evaluate each model with its default configuration. More details are provided in the appendix. As the language models generate free-text answers, we need to extract the answers using regular expression patterns. We consider a model to provide a valid answer even if the format is incorrect (e.g. if they accompany their answer with additional text although we ask only for the answer).

## 4 EXPERIMENTS

### 4.1 OPEN-ENDED QUESTION ANSWERING

In this section, we detail our experiments on open-ended abstract reasoning. Depending on the dataset, the answer can be in natural language or a symbolic format. The model is asked to provide the answer directly. The accuracy for each model on every dataset is summarised in Table 3.

Our results indicate poor performance of language models on all the presented datasets, although the performance varies between datasets and models. In particular, Text-Davinci-3 and GPT-4 consistently achieve the best performance across the datasets. On the other hand, LLaMA-7B has the worst performance of all models. Alpaca and Alpaca-LoRA present slight improvements on BIG-Bench-F, PVR and RAVEN<sup>T</sup>. This improvement is explained by the instruction-tuning used to build Alpaca and Alpaca-LoRA. We provide several examples in the appendix that illustrate this difference. LLaMA-7B often does not attempt to solve the problem but completes the text by giving more examples. These examples do not match the abstract rule for the task. Alpaca and Alpaca-LoRA follow the instructions more faithfully but also fail to grasp the abstract patterns. Instruction-tuning seems to the model understand the format of the answer and what it is asked to do but provides

Table 3: Accuracy of Large Language Models on Open QA datasets. Datasets are represented in columns, and models in rows. The best result for each dataset is indicated in **bold**, and the second best is indicated in *italics*.

	ARC <sup>T</sup>	BIG-Bench-F	Evals-S	PVR	RAVEN <sup>T</sup> -opqa	
					Text	Symb
Text-Davinci-3	<i>0.105</i>	<i>0.404</i>	<b>0.314</b>	<b>0.228</b>	<i>0.343</i>	<i>0.234</i>
GPT-3.5-Turbo	0.033	0.153	0.186	0.124	0.226	0.161
GPT-4	<b>0.119</b>	<b>0.514</b>	<i>0.304</i>	0.177	<b>0.410</b>	<b>0.330</b>
LLaMA-7B	0.010	0.012	0.014	0.060	0.000	0.000
Alpaca	0.010	0.188	0.014	<i>0.184</i>	0.075	0.030
Alpaca-LoRA	0.012	0.144	0.000	0.152	0.000	0.067

little help on how to solve the tasks. Moreover, the performance difference between Text-Davinci-3 and GPT-3.5-Turbo indicates that the type of instruction-tuning matters as Text-Davinci-3 performs systematically better than GPT-3.5-Turbo despite being based on the same model.

Overall, GPT-4 performs noticeably better than all the other models. As the details of its architecture and training set are unavailable, we cannot provide satisfactory explanations for this difference. However, the increase in performance is highest on the RAVEN<sup>T</sup> dataset. Given that Raven matrices are a standard and long-existing test (Raven, 1938; Carpenter et al., 1990), we can hypothesize that the training data of GPT-4 included some versions of the test. The same remark can be made for BIG-Bench-F as it includes traditional list processing algorithms.

Text-Davinci-3 and GPT-4 also achieve good performance on the ARC<sup>T</sup> dataset relative to other existing architectures challenged on the task, making them 11<sup>th</sup> and 14<sup>th</sup> on the Kaggle leaderboard<sup>1</sup>. However, they still fail to answer a vast majority of the tasks correctly. All LLMs generally fail to answer most of the tasks in each dataset. Despite a performance increase compared to previous versions, the most recent language models do not perform open-ended abstract reasoning well.

#### 4.2 MULTIPLE-CHOICE QUESTION ANSWERING

As seen in Section 4.1, open-ended abstract reasoning is a challenging problem for language models. We also perform a series of experiments on Multiple-Choice Question Answering tasks. For these tasks, the models are given a set of possible answers and must pick a single one from the set. This task is more accessible than Open-Ended QA, as the valid response is given as part of the input. Results are given in Table 4.

Table 4: Accuracy of Large Language Models for Multiple-Choice QA on the ACRE<sup>T</sup>, Evals-P and RAVEN<sup>T</sup> datasets. The last line indicates random performance. Completion models can perform worse than random if they do not reply with a valid answer. The best result for each dataset is indicated in **bold**, and the second best is indicated in *italics*.

	ACRE <sup>T</sup>		Evals-P	RAVEN <sup>T</sup> -mcqa	
	Text	Symb		Text	Symb
GPT-2	<b>0.371</b>	0.00	0.496	0.00	0.126
Text-Davinci-3	0.098	0.427	<i>0.560</i>	<i>0.461</i>	<i>0.452</i>
GPT-3.5-Turbo	0.184	<i>0.445</i>	0.481	0.276	0.315
GPT-4	<i>0.272</i>	<b>0.512</b>	<b>0.625</b>	<b>0.697</b>	<b>0.535</b>
LLaMA-7B	0.000	0.257	0.544	0.004	0.000
Alpaca	0.036	0.238	0.544	0.015	0.058
Alpaca-LoRA	0.015	0.123	0.552	0.082	0.124
random	0.33	0.33	0.5	0.125	0.125

We first compare the results of RAVEN<sup>T</sup>-mcqa and RAVEN<sup>T</sup>-opqa from Table 3. RAVEN<sup>T</sup>-opqa contains the same questions as RAVEN<sup>T</sup>-mcqa, but the answer choices have been removed. Following intuition, giving multiple choices to LLMs helps systematically improve their performance. Only the

<sup>1</sup><https://www.kaggle.com/competitions/abstraction-and-reasoning-challenge/leaderboard>

performance of LLaMA remains the same, and the performance of Alpaca is slightly reduced. Given the low accuracy in both cases, it can be interpreted as noise. We now look at the performance for all datasets. GPT-4 achieves the best performance of all completion models and is the only model to perform systematically better than random. Within the remaining models, only Text-Davinci-3 and GPT-3.5-Turbo achieve performance above random on several datasets. MCQA models achieve slightly above random performance (see details in appendix), performing better than most LLMs. However, they have an advantage compared to completion engines as they have to select one answer among a list of possible choices, whereas completion models must generate the correct answer. Therefore, the latter may not return any valuable output (e.g. a nonsensical or empty answer), explaining how they can achieve worse than random performance.

Surprisingly, GPT-2 performs better than its bigger counterparts on the  $ACRE^T$  dataset. The nature of the  $ACRE^T$  dataset can explain this phenomenon. The set of possible answers in  $ACRE^T$  is: "on", "off", and "undetermined". Therefore, GPT-2 learns to output one of those words as the most *plausible* answer and can reach results close to random performance. However, Text-Davinci-3 and GPT-3.5-Turbo attempt to reason about the task but fail to comprehend it. Examples are provided in the appendix. As for the experiments on Open-Ended QA, the performance of language models is poor globally, except for GPT-4, which gets average to good performance. The multiple options can provide useful hints but not all models exploit them equally.

The main takeaway from these experiments is that the performance of LLMs remains low even in discriminative settings. When given a set of possible answers, the models cannot recognise the proper solution among the other choices. This finding indicates that using LLMs as evaluators (as done in self-refinement techniques (Madaan et al., 2023)) is not suited for tasks requiring abstract reasoning.

Additionally, when comparing the results between natural language and symbolic tasks on  $ACRE^T$ , we observe that the results are better across all models when the input is symbolic. Inputs that use symbolic data are smaller and may convey only relevant information, while natural language could contain distracting information or biases harmful to task performance. The same observation can be made concerning  $RAVEN^T$ -mcqa, except for GPT-4. In the open-ended version of  $RAVEN^T$ , models perform better with the natural language representation. Without the answer set available, inductive biases caused by language help performance.

### 4.3 CHAIN-OF-THOUGHT PROMPTING

We perform experiments on a subset of our framework using *Chain-of-Thought* prompting (Wei et al., 2022). The complete experiments are provided in the appendix (and include a side-by-side comparison for better readability). We perform experiments with GPT-3.5-turbo, GPT-4, and Alpaca-LoRA. Our experiments with *Chain-of-Thought* have the suffix *model-cot*. Our results are presented in Table 5.

Table 5: Accuracy of Large Language Models on Open and Multiple-Choice QA datasets when prompted using *Chain-of-Thought*. Datasets are represented in columns, and models in rows. The best result for each dataset is indicated in **bold**, and the second best is indicated in *italics*. BBF stands for BIG-Bench-F.

	BBF	PVR	$RAVEN^T$ -opqa		$ACRE^T$		$RAVEN^T$ -mcqa	
			Text	Symb	Text	Symb	Text	Symb
GPT-3.5-Turbo-cot	<i>0.097</i>	<b>0.210</b>	<i>0.302</i>	<i>0.211</i>	<b>0.255</b>	<i>0.345</i>	<i>0.257</i>	<i>0.144</i>
GPT-4-cot	<b>0.476</b>	<i>0.174</i>	<b>0.385</b>	<b>0.354</b>	<i>0.214</i>	<b>0.394</b>	<b>0.596</b>	<b>0.517</b>
Alpaca-LoRA-cot	0.084	0.152	0.000	0.069	<i>0.059</i>	0.114	0.000	0.114

Overall, the results obtained using *Chain-of-Thought* prompting are not higher than those obtained with the base models. On The BIG-Bench-F dataset, the *Chain-of-Thought* versions achieve systematically lower performance than their base counterparts, although no no significant performance drop is observed. On PVR and  $RAVEN^T$ -opqa, while the accuracy for GPT-4 and Alpaca-LoRA remain unchanged or slightly reduced, the performance of GPT-3.5-Turbo is increased. On  $RAVEN^T$ -mcqa, the performance of all the models decreases. These experiments show that the quality of the prompt has little impact on the answer quality. It hints that the models can understand the task, but their failures are due to their ability to provide faithful reasoning. This limitation is further illustrated with examples in the appendix.

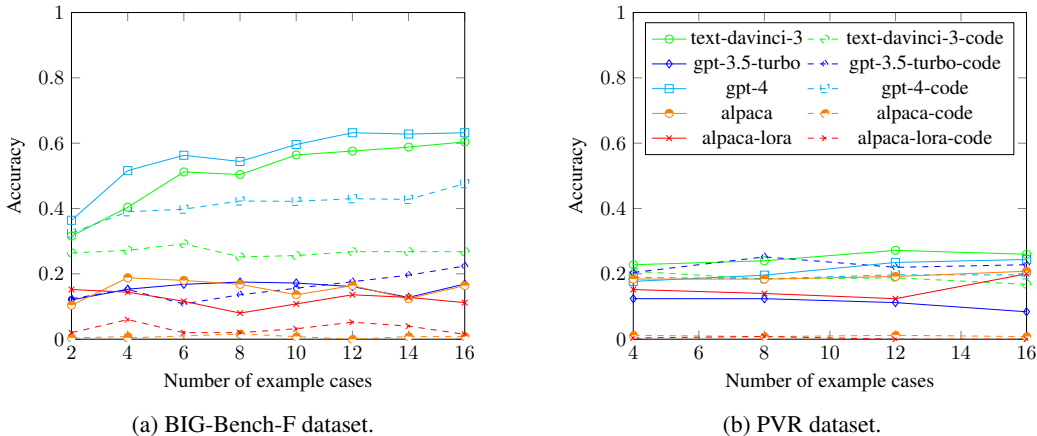


Figure 3: Evolution of the model performance as a function of the number of examples seen from the dataset. The legend is shared by both figures. Models with straight lines are used with default prompting, while models with dashed lines are prompted to produce code.

#### 4.4 VARYING THE EXAMPLE SET SIZE

We perform further experiments on the BIG-Bench-F and PVR datasets. For these two datasets, we alter the number of examples given to the system before the test case. By default, we give four examples to the model before asking it to answer. The results are shown in Figures 3a and 3b. In this section, we focus on the results of the base models (without the "-code" suffix).

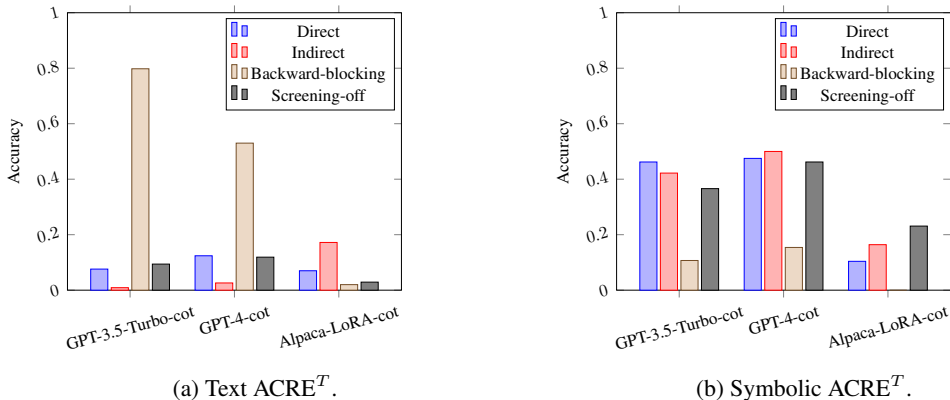
We first observe that, for both datasets, there is no linear relationship linking performance and number of examples. For all but the Text-Davinci-3 and GPT-4 models, adding more examples has little or no effect on the accuracy. Text-Davinci-3 and GPT-4 perform similarly across all cases, and their performances consistently increase with the number of examples, achieving up to an accuracy of 0.6 when given 16 examples on the BIG-Bench-F dataset. However, on PVR, Text-Davinci-3 achieves only 0.26 when given 12 examples. GPT-4 follows a similar trend but performs slightly worse than its predecessor. In the absence of technical details for GPT-4, we can only speculate on the reasons. As this effect is observed only on BIG-Bench-F and not PVR, we can assume that the models perform better because their training sets contain the list processing algorithms used by BIG-Bench-F. We perform additional experiments in the appendix, where we provide solved instances into the prompt (input and solution program) to propel the model to reason correctly. No real improvements are observed.

#### 4.5 ENABLING STRUCTURE DISCOVERY WITH CODE

In the next experiments, we follow an idea similar to *Progam-of-Thought* prompting (Chen et al., 2022) and ask the model to generate the code of the function responsible for generating the output from the input. Then, we execute the produced code on the test case and evaluate the result. This method differs from a base prompt as we do not ask the model to produce the answer directly. This part is delegated to a code interpreter in Python. This method aims to verify the ability of LLMs to extract the correct structure behind each abstract reasoning task under code format. We test this method on the BIG-Bench-F and PVR datasets. The results of these models (with the "-code" suffix) can be compared with their original counterparts in Figures 3a and 3b.

In general, we observe that the models prompted to produce code perform worse than those tasked to produce the answer directly. The only exception is GPT-3.5-Turbo. On the BIG-Bench-F dataset, the performance of GPT-3.5-Turbo-code increases steadily while that of GPT-3.5-Turbo stagnates, and on PVR, GPT-3.5-Turbo-code outperforms GPT-3.5-Turbo by a significant margin. Producing code solving the abstract problem is a more complicated task for an LLM as it requires the model to produce a rigorous code explanation for its answer. It is consistent with the results for most models, but we also observe in the case of GPT-3.5-Turbo-code that it can help the model better understand the task. On BIG-Bench-F, the code versions of Text-Davinci-3 and GPT-4 perform better than both



Figure 4: Results of chain-of-thought models on  $ACRE^T$  divided by causal paths.

base and code versions of the other models. As this behaviour is not observed with PVR, we infer that this performance is due to the functions being part of the training sets of the models. The models can almost always generate code able to compile and produce an answer (details are in the appendix). We deduce that producing a program with a valid syntax is not a bottleneck for performance. The issue lies in the recovery of the correct reasoning process.

#### 4.6 A PERSPECTIVE FROM CAUSAL INDUCTION

We perform further analysis on  $ACRE^T$ . The dataset can be divided into four causal paths: Direct, Indirect, Backward-blocking, Screening-off (Zhang et al., 2021a). Direct path queries can be established using direct evidence. Indirect paths require the combination of multiple pieces of evidence. Backward-blocking paths cannot be determined because the true mechanisms cannot be discriminated from other possibilities based solely on the data. Screening-off paths are causal paths affected by spurious correlations. For instance, parts of a sample may not be on the causal path (i.e. do not affect the outcome) but can be correlated with a particular outcome. Figure 4 shows the results for each type of query. We restrict our analysis to the *Chain-of-Thought* models (see the appendix for the full analysis). Although accuracy scores are similar, the distribution of the results among the causal paths differs between models and input types. GPT models overfit to backward-blocking cases on the text  $ACRE^T$  but not on the symbolic version. We can deduce that natural language contains distracting information or biases harmful to abstract reasoning performance. It is consistent with the higher score of the models on the symbolic tasks. Fine-tuning LLMs on symbolic data, with no spurious effects, could lead models to learn to reason causally.

## 5 CONCLUSION

Understanding the potential reasoning capabilities of LLMs is crucial as they are starting to be widely adopted. Measuring the level of intelligence of a system is hard, but abstract reasoning provides a valuable framework for this task. In this paper, we present what is, to the best of our knowledge, the first extensive evaluation of Large Language Models for abstract reasoning. We show that LLMs do not perform well on all types of tasks, although not all models are equally poor. Techniques that improve performance on NLP tasks, such as *Chain-of-Thought* and *Program-of-Thought* prompting, do not work for abstract reasoning. Our experiments show that the bottleneck in the performance lies in the recognition of new unseen abstract patterns and not in a lack of understanding of the task or the prompt. Moreover, these results hold in discriminative settings, where the models must find the correct answer within a small set of propositions. A qualitative study of selected failure cases in the appendix further reveals that models tend to reason inconsistently and in a shallow way. We hypothesise that current self-supervised autoregressive LLMs lack fundamental properties for strong abstract reasoning tasks and human-like cognition. We posit that methods based on causal reasoning and program induction could help improve the reasoning abilities of neural networks.

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## A DATASET DETAILS

This section provides more details and examples of each dataset used in the experiments.

**ACRE** We conduct experiments on the Abstract Causal Reasoning (ACRE) dataset (Zhang et al., 2021a). ACRE is a Visual Question-Answering (VQA) dataset. In our work, we use a transcription of the dataset into text. Each sample in the data comprises six context images and four test cases. Each context image comprises a set of objects with various shapes, colours and textures, and a light. In the context images, the light can be on or off. The goal of a system is to determine from the context examples if the light is on, off, or if its state cannot be determined in the test cases. To solve this task, the model has to determine for each sample what objects are causally responsible for the activation of the light. We generate two versions of the dataset: in ACRE-Text, each image is replaced by a textual description, and in ACRE-Symbolic, each image is replaced with a vector representation. An example of ACRE-Text is given in Figure 5 and an example of ACRE-Symbolic is given in Figure 6.

**ARC** The second dataset we use is the Abstract Reasoning Challenge (ARC) dataset (Chollet, 2019). The dataset is composed of tasks, each comprising several input and output grids. The goal of the system is to determine the algorithm that converts the input to the output and apply it to a test case. The grids have a variable size comprised between  $8 \times 8$  and  $30 \times 30$ , and contain visual patterns (e.g. recognisable shapes, symmetries). We provide the raw grid to the model as a two-dimensional array of integers. The high dimensionality of the input makes it a challenging task for LLMs. The tasks themselves are also challenging as their transcription in natural language is often complex and supposedly impossible for 12% of them (Acquaviva et al., 2021). An example from the original ARC is given in Figure 7.

**BIG-Bench** We select a subset of the BIG-Bench dataset (Rule, 2020; Srivastava et al., 2022) that we name BIG-Bench-F for *Functions*. The subset comprises various tasks represented by a function taking a list as input and returning a new transformed list as output. For each task, several input-output samples are given. In BIG-Bench-F, we give four samples per task by default. The functions include typical list-processing like replacing one list element with another value, selecting a subset of the list, or counting elements. The difficulty in this task is to accurately recognise the function from a few samples. An example is given in Figure 8.

The functions used in BIG-Bench are classic list-processing functions. Such functions are likely to be in the training sets of Large Language Models trained on large corpora of data on the internet. Figures 9 and 10 illustrate it with two examples. These examples are discussions with GPT-4, where the model is prompted to generate a function solving a list-processing problem and create examples.

Pre-Prompt
<p>Objects of various color, shape, and texture are displayed. Some objects may contain a device to turn a light on if displayed. From the observations, deduce if the light is on, off, or if the state cannot be determined. Your answer must contain a single word:</p> <p>on. off. undetermined.</p>
Example Cases
<p>A cyan cylinder in rubber is visible. The light is on.  A gray cube in rubber is visible. The light is off.  A cyan cylinder in rubber is visible. A gray cube in rubber is visible. The light is on.  A blue cube in metal is visible. The light is off.  A gray cylinder in rubber is visible. A gray cube in metal is visible. The light is off.  A red sphere in metal is visible. A yellow cube in rubber is visible. The light is on.</p>
Test Case
<p>A red sphere in metal is visible. The light is <i>undetermined</i></p>

Figure 5: Sample from the ACRE-Text dataset. In the test case, the target answer is indicated in *italics*.

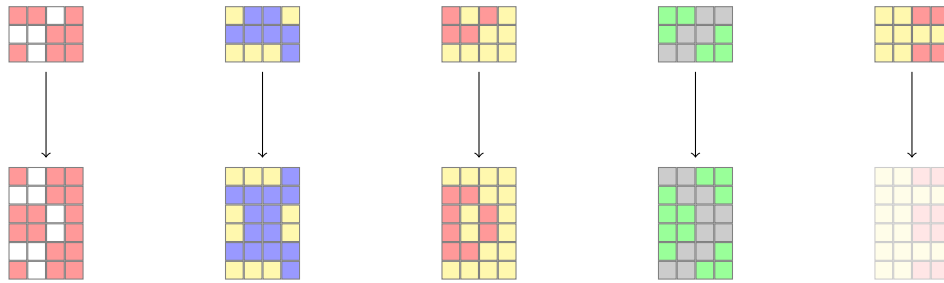
Pre-Prompt
<p>Figure out the pattern in the following examples and apply it to the test case. Your answer must follow the format of the examples. You can answer 1 if the solution cannot be determined. Your answer must be one of the following choices:</p> <p>0. 1. 2.</p>
Example Cases
<p>[28] → 2  [0] → 0  [28, 0] → 2  [5] → 0  [16, 1] → 0  [35, 14] → 2</p>
Test Case
<p>[35] → <i>1</i></p>

Figure 6: Sample from the ACRE-Symbolic dataset. In the test case, the target answer is indicated in *italics*.

They show that the model has prior knowledge of the functions needed for the tasks and could solve them by memorising examples from its training set where these functions are applied without the need to reason abstractly.

**Evals** We select a subset of the Evals dataset (OpenAI, 2023) representing logic puzzles. Evals-P is composed of a set of tasks. For each task, a tuple containing a character and a list of characters is given as an input and a single word from the set {"foo", "bar"} is generated from the input according to a logic hidden from the evaluated system. The task consists of finding the logic from eight samples





(a) Example Case 1. (b) Example Case 2. (c) Example Case 3. (d) Example Case 4. (e) Test Case.

Figure 7: Sample for the ARC dataset. In our work, each grid is given as a numeric array to the model. In this example, the task consists of generating the symmetric to the input grid and appending it to the input. In the test case, the expected output is lightly coloured.

Pre-Prompt	
Apply a function to the final input list to generate the output list. Use any preceding inputs and outputs as examples to find what is the function used. All example outputs have been generated using the same function.	Your task is to write down the python function responsible for the transformation of the list in the following examples. The format is [input] → [output]:
Example Cases	
[1, 0, 9, 7, 4, 2, 5, 3, 6, 8] → [9, 0, 1, 4, 4, 5] [3, 8, 4, 6, 1, 5, 7, 0] → [4, 8, 3, 4, 1, 7] [5, 4, 7, 2, 9, 3, 8, 1] → [7, 4, 5, 4, 9, 8] [3, 9, 2, 0, 6, 8, 5, 1, 7] → [2, 9, 3, 4, 6, 5]	
Test Case	
[9, 2, 1, 3, 4, 7, 6, 8, 5, 0] → [1, 2, 9, 4, 4, 6]	Write the function. Next, write a line to print the output of this function for the input [9, 2, 1, 3, 4, 7, 6, 8, 5, 0]

Figure 8: Example task in the BIG-Bench-F dataset. For this task, the system must return specific elements of the input list, i.e. [inp[2], inp[1], inp[0], 4, inp[4], inp[6]]. In the test case, the target answer is indicated in *italics*. Text exclusive to base models are indicated by a blue background, and text exclusive to code models are indicated by a green background.

and applying it to a test case. An example is given in Figure 11. Evals-S is composed of another set of tasks. For each task, a list of integers is given as an input and an output list of words is generated from the input according to a logic hidden from the evaluated system. The task consists of finding the logic from three samples and applying it to a test case. An example is given in Figure 12.

**PVR** The Pointer-Value Retrieval (PVR) dataset (Zhang et al., 2021b) is a dataset for retrieval tasks. Tasks involve selecting one or several values in a list and applying a function on this subset. For each task, the system must recognise the retrieval and application functions and apply them to a test case. Samples in the datasets are composed of a pointer-values pair and a label. The values are stored in an array, and the pointer is an integer pointing to an index in the array. The pointer indicates the subset of values to consider for the task. An example is given in Figure 13.

**RAVEN** RAVEN (Zhang et al., 2019) is a VQA dataset composed of sequences of images to complete. The images contain Raven matrices (Raven, 1938), i.e. geometric shapes (e.g. square, circle, pentagon) assembled in various ways (e.g. one shape inside another, four shapes in a  $4 \times 4$

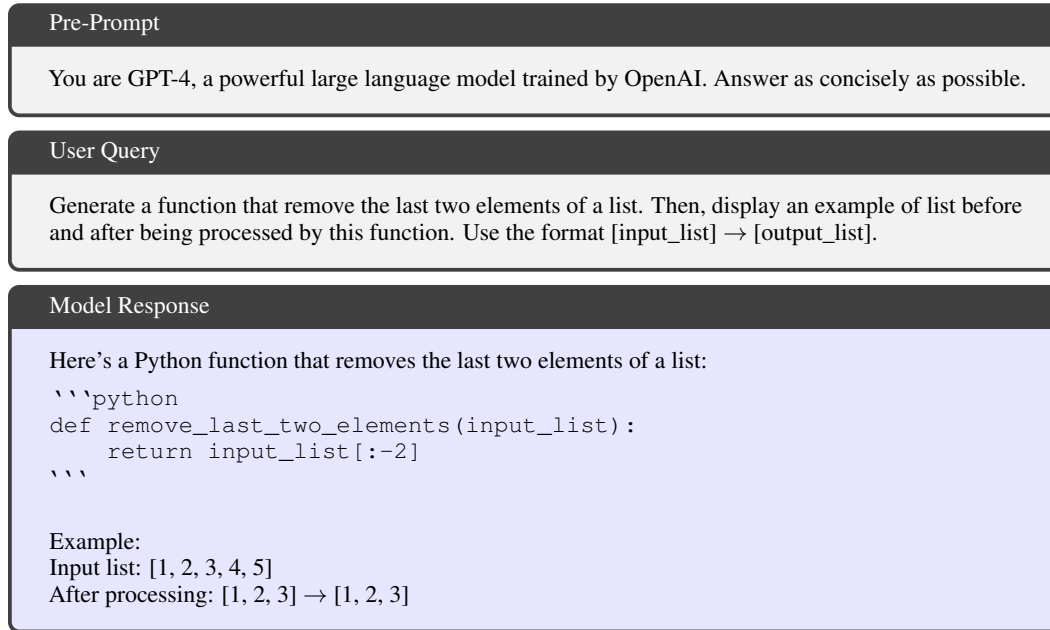


Figure 9: Example of exchange with GPT-4. When asking to provide a list-processing algorithm, the model is able to provide a correct solution and generates an example with the BIG-Bench-F format, although incorrect.

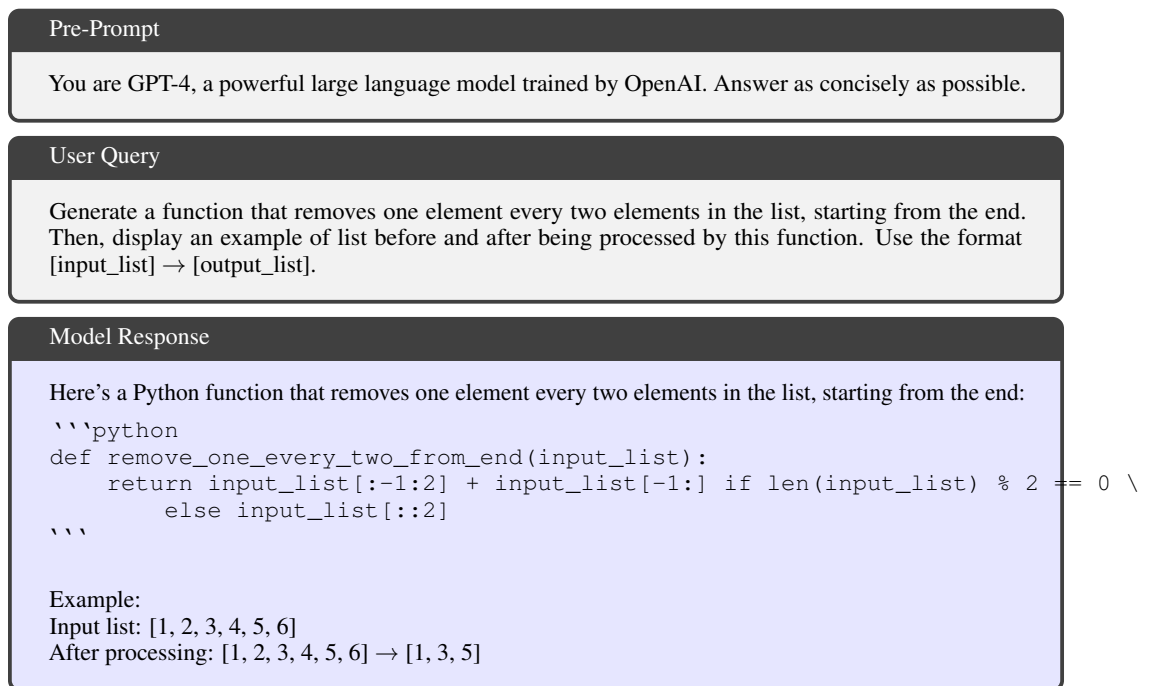


Figure 10: Example of exchange with GPT-4. When asking to provide a list-processing algorithm, the model is able to provide a solution, although incorrect, and generates an example with the BIG-Bench-F format, although also incorrect.

grid). RAVEN is a dataset similar to Procedurally Generated Matrices (PGM) (Santoro et al., 2018) but has the advantage of providing a tree structure describing the semantics of each matrix. We focus on a subset where a single shape appears in the image. The task is, given a sequence of eight images and eight possible choices, to pick the correct image that follows in the sequence. As RAVEN is

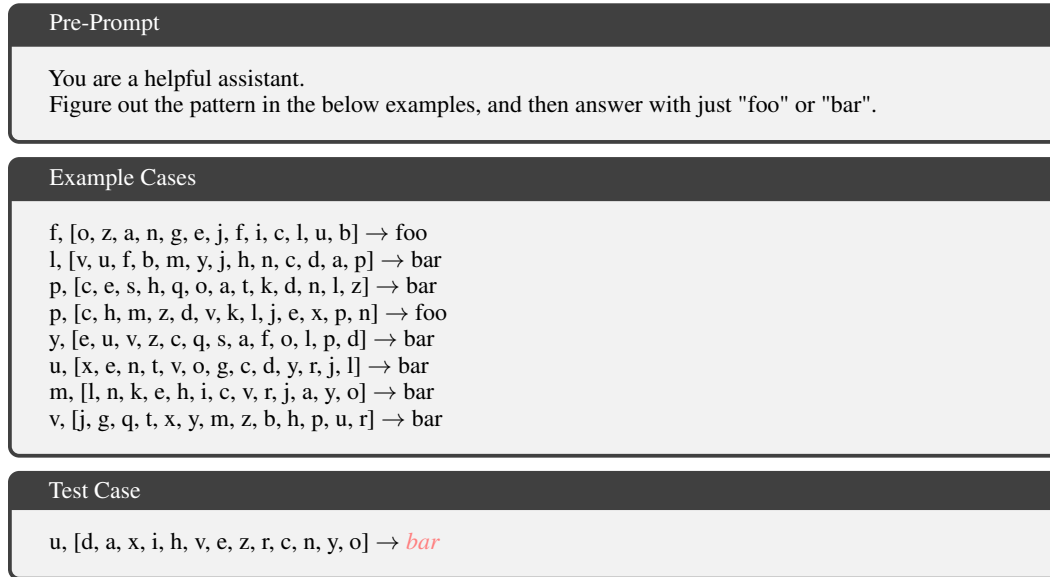


Figure 11: Example task in the Evals-P dataset. For this task, the system must return "foo" if the first character of the input is in the list or "bar" otherwise. In the test case, the target answer is indicated in *italics*.

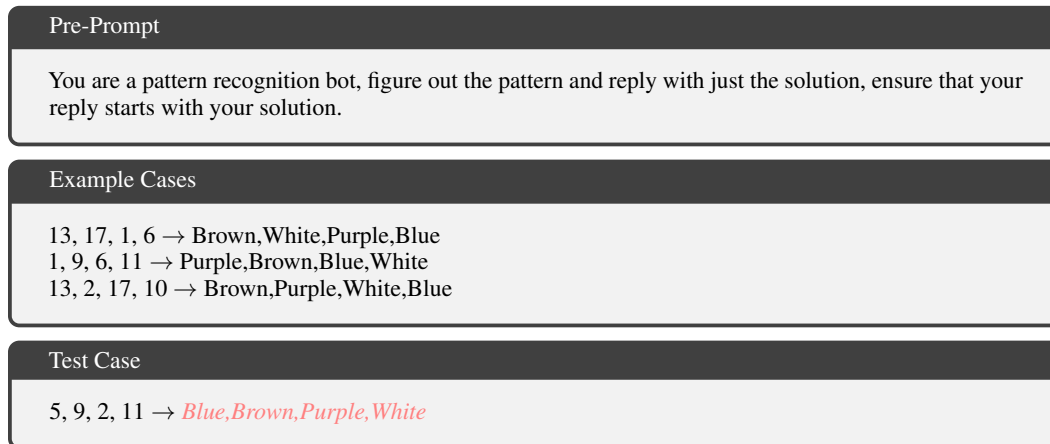


Figure 12: Example of task in the Evals-S dataset. For this task, the system must sort the words according to the numbers in input (e.g. word "white" is located at the index of the highest integer and word "purple" is located at the index of the lowest integer). In the test case, the target answer is indicated in *italics*.

a visual dataset like ACRE, we generate a text description of each image from their semantic tree that we will feed into the evaluated models. We create two sets: RAVEN-Text contains descriptions in natural language, and RAVEN-Symbolic contains symbolic descriptions. We also build another version of the dataset where choices are hidden. We name the former RAVEN-mcqa and the latter RAVEN-opqa. Examples for each are given in Figures 14 and 15, respectively.

Raven matrices are a standard and long-existing test (Raven, 1938; Carpenter et al., 1990), likely in the training sets of Large Language Models trained on large corpora of data on the internet. To figure it out, we directly prompt GPT-3.5-Turbo and GPT-4. The discussions are represented in Figures 17 and 16. The responses of the model indicate knowledge of the RAVEN test, although GPT-4 generates a correct sample of a Raven test, whereas GPT-3.5-Turbo generates an example that does not have a valid logic. The main takeaway from these examples is that Raven test data has been leaked to the training sets of those models. However, whether exact examples from the test set are also part of the training data is unknown.

Pre-Prompt	
Figure out the pattern in the following examples and apply it to the test case. Your answer must follow the format of the examples.	Your task is to write down the python function responsible for the computation of the output from the list in the following examples. Your answer must follow the format of the examples.
Example Cases	
[5, 7, 4, 1, 8, 9, 8, 1, 9, 8, 4] → 8 [4, 0, 0, 7, 0, 1, 0, 5, 3, 0, 0] → 1 [0, 2, 8, 2, 5, 9, 4, 3, 8, 5, 4] → 2 [3, 3, 2, 6, 5, 7, 4, 6, 7, 4, 8] → 5	
Test Case	
[3, 4, 9, 7, 1, 8, 7, 1, 0, 3, 5] → <i>1</i>	Write the function. Next, write a line to print the output of this function for the input [3, 4, 9, 7, 1, 8, 7, 1, 0, 3, 5]

Figure 13: Example of task in the PVR dataset. In the test case, the target answer is indicated in *italics*. Text exclusive to base models are indicated by a blue background, and text exclusive to code models are indicated by a green background.

Pre-Prompt	
Find the pattern number 9 that completes the sequence. Write the correct pattern with the same format as in the examples. Patterns in the sequence are preceded by a number from 1 to 8.	Find the pattern number 9 that completes the sequence. Pick the letter in front of the correct pattern that logically follows in the sequence from the answer set. Patterns in the sequence are preceded by a number from 1 to 8. Patterns in the answer set are preceded by a letter from A to H. Only return the letter in front of the correct pattern.
Example Cases	
<ol style="list-style-type: none"> <li>1. On an image, a large lime square rotated at 180 degrees.</li> <li>2. On an image, a medium lime square rotated at 180 degrees.</li> <li>3. On an image, a huge lime square rotated at 180 degrees.</li> <li>4. On an image, a huge yellow circle rotated at 0 degrees.</li> <li>5. On an image, a large yellow circle rotated at 0 degrees.</li> <li>6. On an image, a medium yellow circle rotated at 0 degrees.</li> <li>7. On an image, a medium white hexagon rotated at -90 degrees.</li> <li>8. On an image, a huge white hexagon rotated at -90 degrees.</li> </ol>	
<ol style="list-style-type: none"> <li>A. On an image, a tiny white hexagon rotated at -90 degrees.</li> <li>B. On an image, a giant white hexagon rotated at -90 degrees.</li> <li>C. On an image, a large red hexagon rotated at -90 degrees.</li> <li>D. On an image, a large orange hexagon rotated at -90 degrees.</li> <li>E. On an image, a large white hexagon rotated at -90 degrees.</li> <li>F. On an image, a large green hexagon rotated at -90 degrees.</li> <li>G. On an image, a large blue hexagon rotated at -90 degrees.</li> <li>H. On an image, a large yellow hexagon rotated at -90 degrees.</li> </ol>	
Test Case	
The pattern that logically follows is: 9. <i>On an image, a large white hexagon rotated at -90 degrees.</i>	The answer is <i>E</i>

Figure 14: Sample from the RAVEN<sup>T</sup>-Text dataset. In the test case, the target answer is indicated in *italics*. Text exclusive to RAVEN<sup>T</sup>-opqa has a **blue** background, and text exclusive to RAVEN<sup>T</sup>-mcqa has a **green** background. Shared text has a **gray** background.

Pre-Prompt	
Find the pattern number 9 that completes the sequence. Write the correct pattern with the same format as in the examples. Patterns in the sequence are preceded by a number from 1 to 8.	Find the pattern number 9 that completes the sequence. Pick the letter in front of the correct pattern that logically follows in the sequence from the answer set. Patterns in the sequence are preceded by a number from 1 to 8. Patterns in the answer set are preceded by a letter from A to H. Only return the letter in front of the correct pattern.
Example Cases	
1. [(D, D, C, H,)] 2. [(C, D, C, H,)] 3. [(E, D, C, H,)] 4. [(E, C, F, D,)] 5. [(D, C, F, D,)] 6. [(C, C, F, D,)] 7. [(C, J, E, B,)] 8. [(E, J, E, B,)]	
A. [(A, J, E, B,)] B. [(F, J, E, B,)] C. [(D, A, E, B,)] D. [(D, B, E, B,)] E. [(D, J, E, B,)] F. [(D, E, E, B,)] G. [(D, G, E, B,)] H. [(D, C, E, B,)]	
Test Case	
The pattern that logically follows is: 9. [(D, J, E, B,)]	The answer is <i>E</i>

Figure 15: Sample from the RAVEN<sup>T</sup>-Symbolic dataset. In the test case, the target answer is indicated in *italics*. Text exclusive to RAVEN<sup>T</sup>-opqa has a blue background, and text exclusive to RAVEN<sup>T</sup>-mcqa has a green background. Shared text has a gray background.

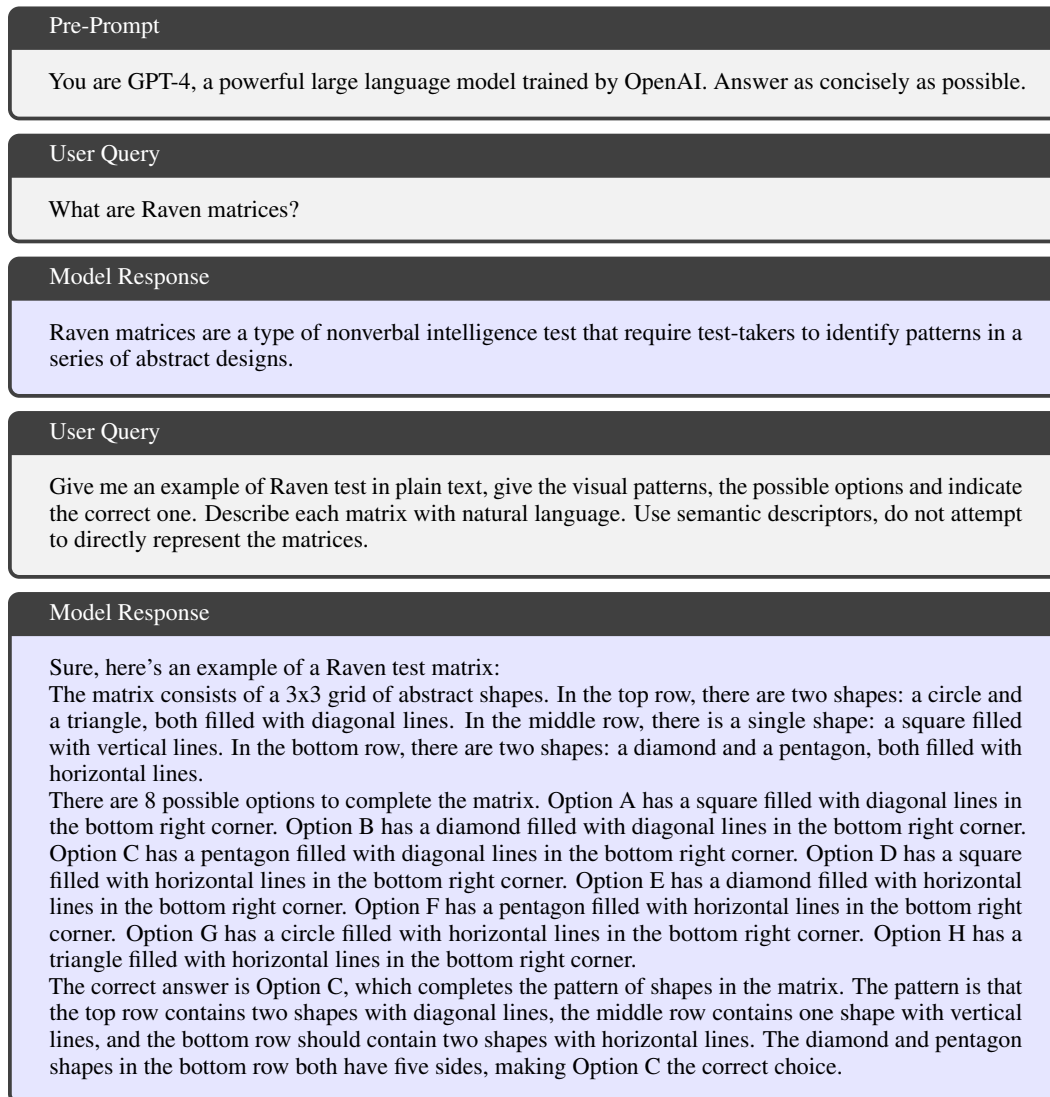


Figure 16: Example of exchange with GPT-3.5-Turbo. When queried about Raven matrices, the model is able to provide a description of the test and provide an *incorrect* example in natural language.

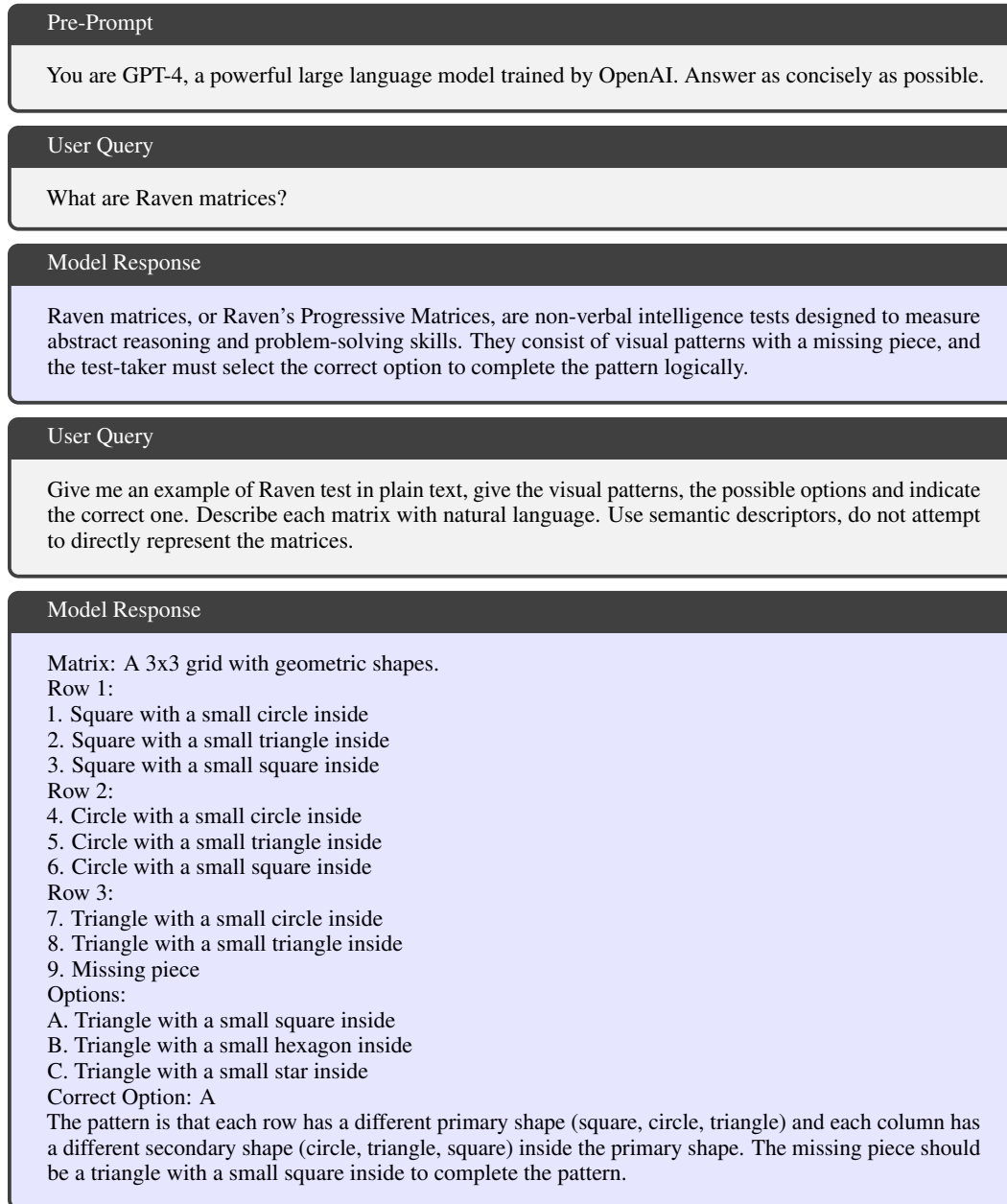


Figure 17: Example of exchange with GPT-4. When queried about Raven matrices, the model is able to provide a description of the test and provide a *correct* example in natural language.



## B ADDITIONAL EXPERIMENTS

We perform additional experiments using other models and prompting methods. The settings are the same as in the main paper.

For Text-Davinci-3, GPT-3.5-Turbo, and GPT-4, we use the Open AI API to run all the evaluations. Text-Davinci is a text-completion model, so we convert our input context and question to a single string. GPT-3.5-Turbo and GPT-4 are chat completion models, so we provide the instructions in chat format. The pre-prompt and examples are given to the model by the system, and the supposed user gives the question. We use a temperature of 0.5 for the output generation and the default parameters of each model for the maximum number of generated tokens. Unless specified otherwise, the version of GPT-3.5-Turbo is gpt-3.5-turbo-0301 and the version of GPT-4 is gpt-4-0314. For GPT-2, LLaMA, Alpaca, Alpaca-LoRA, RoBERTa-large, and MERIt, we use the weights provided on the Huggingface hub. RoBERTa-large and MERIt are used as MCQA models, while the others are used as causal language modelling models. We set the maximum number of generated tokens to 128 for the default models, 512 for *chain-of-thought*-prompted models (see Appendix B.1), and 256 for the code models (see Appendix B.2). We evaluate each model with its default configuration. The fine-tuned models are trained for 10 epochs with a batch size of 10, using Adam optimizer (Kingma & Ba, 2015) and a learning rate of  $5 \times 10^{-4}$ . As the language models generate free-text answers, we need to extract the answers using regular expression patterns. We consider a model to provide a valid answer even if the format is incorrect (e.g. if they accompany their answer with additional text although we ask only for the answer). Unless specified otherwise, we always ask the model to provide a single answer and return only the aforementioned answer without explanation. We perform a single evaluation per dataset per model as the cost of running some of the Large Language Models makes it prohibitively expensive to systematically perform multiple runs.

### B.1 CHAIN-OF-THOUGHT PROMPTING

We perform a series of experiments with *Chain-of-Thought* prompting (Wei et al., 2022). To elicit multi-step reasoning, we use the following pre-prompt: "*Figure out the pattern in the following examples and apply it to the test case. Describe every step of your reasoning before proposing a solution. When giving the solution, start your sentence with 'ANSWER:'*". Appendix D.1 gives several examples illustrating this principle. We perform experiments with GPT-3.5-turbo, GPT-4, and Alpaca-LoRA. Our experiments with *Chain-of-Thought* have the suffix *model-cot*. Our results on BIG-Bench-F, Evals-S, and PVR datasets are presented in Table 6.

Table 6: Accuracy of Large Language Models on Open QA datasets when prompted using *Chain-of-Thought*. Datasets are represented in columns, and models in rows. The best result for each dataset is indicated in **bold**, and the second best is indicated in *italics*.

	BIG-Bench-F	Evals-S	PVR	RAVEN <sup>T</sup> -opqa	
				Text	Symb
GPT-3.5-Turbo	<i>0.153</i>	<i>0.186</i>	0.124	0.226	<i>0.161</i>
GPT-4	<b>0.514</b>	<b>0.304</b>	<b>0.177</b>	<b>0.410</b>	<b>0.330</b>
Alpaca-LoRA	0.144	0.000	<i>0.152</i>	0.000	0.067
GPT-3.5-Turbo-cot	<i>0.097</i>	<i>0.130</i>	<b>0.210</b>	<i>0.302</i>	<i>0.211</i>
GPT-4-cot	<b>0.476</b>	<b>0.148</b>	<i>0.174</i>	<b>0.385</b>	<b>0.354</b>
Alpaca-LoRA-cot	0.084	0.029	0.152	0.000	0.069

Overall, the results obtained using *Chain-of-Thought* prompting are not higher than those obtained with the base models. On The BIG-Bench-F dataset, the *Chain-of-Thought* versions achieve systematically lower performance than their base counterparts, although no important drop of performance is observed. On Evals-S, the performances of GPT-3.5 and GPT-4 are also reduced. The accuracy of base GPT-4 is higher than base GPT-3.5 by a fair margin, but this margin is highly reduced in the *Chain-of-Thought* version. On PVR, while the accuracy for GPT-4 and Alpaca-LoRA remain unchanged or slightly reduced, the performance of GPT-3.5-Turbo is increased.

Table 7: Accuracy of Large Language Models on Multiple-Choice QA datasets when prompted using *Chain-of-Thought*. Datasets are represented in columns, and models in rows. The best result for each dataset is indicated in **bold**, and the second best is indicated in *italics*.

	ACRE <sup>T</sup>		RAVEN <sup>T</sup> -mcqa	
	Text	Symb	Text	Symb
GPT-3.5-Turbo	<i>0.184</i>	<i>0.445</i>	<i>0.276</i>	<i>0.315</i>
GPT-4	<b>0.272</b>	<b>0.512</b>	<b>0.697</b>	<b>0.535</b>
Alpaca-LoRA	0.015	0.123	0.082	0.124
GPT-3.5-Turbo-cot	<b>0.255</b>	<i>0.345</i>	<i>0.257</i>	<i>0.144</i>
GPT-4-cot	<i>0.214</i>	<b>0.394</b>	<b>0.596</b>	<b>0.517</b>
Alpaca-LoRA-cot	<i>0.059</i>	0.114	0.000	0.114
random	0.33	0.33	0.125	0.125

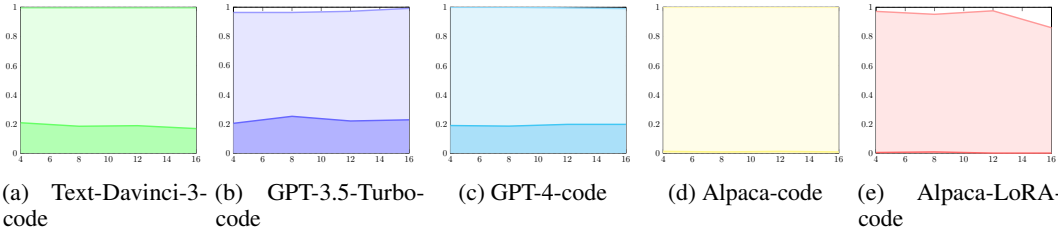


Figure 18: Evolution of the performance of code models on the PVR dataset as a function of the number of examples seen. The x-axis shows the number of examples and the y-axis shows the accuracy. Lightly coloured areas represent the proportion of samples where the code compiles correctly and dark coloured areas represent the proportion of samples where the generated program accurately answers the question.

## B.2 CODE GENERATION

To study the relationship between code output and accuracy more closely, we compare the proportion of valid generated programs (i.e. functions that compile) with the proportion of programs generating the correct answer. We summarise the result for PVR in Figure 18. We observe that models can almost systematically generate a code able to compile and produce an answer. We deduce that the production of a program with a valid syntax is not a bottleneck for the performance. The issue lies in the recovery of the correct reasoning process.

## B.3 VARYING THE MODEL SIZE

In this section, we compare the performance of models of various sizes. We divide our experiments into two parts. First, we evaluate fine-tuned RoBERTa-AR\* and MERIt-AR\* on an MCQA dataset. We aim to see if specialised models with smaller sizes can perform multiple-choice abstract reasoning. Second, we perform additional experiments on the bigger version of LLaMA, i.e. LLaMA-13B and LLaMA-30B. We aim to see if increasing the size of the model has an impact on the performance.

**MCQA Engines** MCQA models have an advantage over completion engines as they must select one answer from a list of possible choices, whereas completion models must generate the correct answer. Therefore, MCQA models can reach the performance of a random classifier without knowing anything about the task. We perform experiments on the ACRE<sup>T</sup>-Text and ACRE<sup>T</sup>-Symbolic datasets. Results with RoBERTa-AR\* and MERIt-AR\* are shown in Table 8. When fine-tuned on the training set with the same format, the performance of the model increases slightly. However, the overall performance remains close to random.

**LLaMA Variations** The main results with the various versions of LLaMA on Open QA datasets are displayed in Table 9. We observe a slight increase in accuracy with LLaMA-13B on ARC<sup>T</sup>, Evals-S, and PVR datasets, but the accuracy then decreases with LLaMA-30B. Performance remains close to null on the RAVEN<sup>T</sup> datasets. However, on BIG-Bench-F, the accuracy increases with LLaMA-30B. The overall performance remains poor on every dataset.

Table 8: Accuracy of the specified model for a Multiple-Choice QA task on the ACRE dataset. Rows represent the dataset on which the model is fine-tuned, and columns represent the dataset on which the model is evaluated. The best result for each dataset in indicated in **bold**.

RoBERTa-AR*		ACRE <sup>T</sup> -Eval		MERIt-AR*		ACRE <sup>T</sup> -Eval	
		Text	Symb			Text	Symb
ACRE <sup>T</sup> -Train	Text	<b>0.370</b>	0.361	ACRE <sup>T</sup> -Train	Text	<b>0.338</b>	0.331
	Symb	0.262	<b>0.371</b>		Symb	0.332	<b>0.336</b>

Table 9: Main results of LLaMA versions for open QA. Datasets are represented in columns and models in rows. The best result for each dataset in indicated in **bold** and the second best is indicated in *italics*.

	ARC <sup>T</sup>	BIG-Bench-F	Evals-S	PVR	RAVEN <sup>T</sup> -opqa	
					Text	Symb
LLaMA-7B	<i>0.010</i>	<i>0.012</i>	0.014	0.060	0.000	0.000
LLaMA-13B	<b>0.019</b>	0.008	<b>0.029</b>	<b>0.204</b>	0.000	0.001
LLaMA-30B	0.006	<b>0.088</b>	<i>0.016</i>	<i>0.172</i>	0.000	0.000

#### B.4 VARYING THE MODEL TEMPERATURE

We noticed in our experiments that the LLMs tend to repeat similar wrong reasoning patterns across samples or produce repeating sequences when they cannot identify the abstract pattern. Without fine-tuning, LLaMA is particularly susceptible to this issue. To reduce the number of occurrences of this problem, we set the temperature of the models in our experiments to a high value (temperature=0.5). Setting a high temperature increases the probability for the model to output different and non-repeating answers. For our experiments, it gives the opportunity for the models to explore a larger variety of reasoning paths. On the other hand, reducing the temperature reduces the uncertainty in the answer. A low temperature is usually associated with high fidelity answer while models with high temperature are more prone to hallucinations (Xu et al., 2022).

We perform additional experiments where we vary the temperature of GPT-3.5-Turbo and GPT-4 to study the impact of this factor on performance. We use the base and code versions of these models to see if differences occur between models generating long answers and models generating short answers. We perform experiments with temperatures: [0.0, 0.25, .05, 0.75, 1.0]. The results on the BIG-Bench-F and PVR datasets are shown in Figure 19. We observe that there is no significant difference between code and base models. On both datasets, varying the temperature has little impact on the accuracy. On the PVR dataset, the accuracy remains similar for all models. On BIG-Bench-F, the accuracy drops when the temperature is equal to 1.0. The accuracy also drops for GPT-4 when the temperature is equal to 0.25 and 0.5 but increases when reaching 0.75. The standard deviation remains small (0.028). This phenomenon is not observed on the code model.

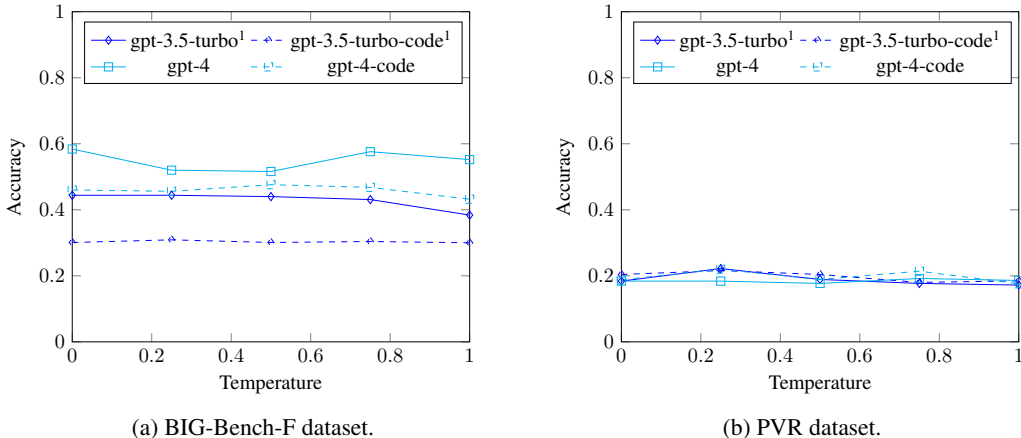


Figure 19: Evolution of the performance of GPT models when varying temperature.

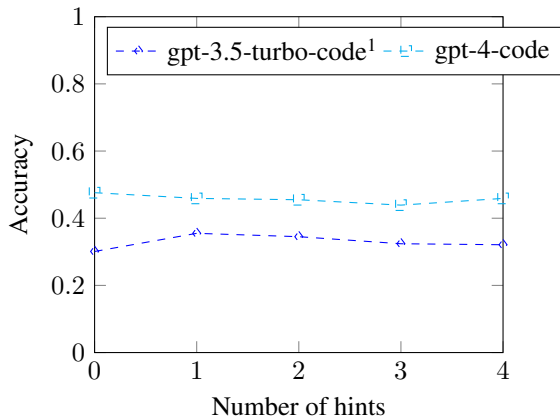


Figure 20: Evolution of the accuracy of hinted GPT code models on the BIG-Bench-F dataset. Hints correspond to solved instances of the training set and are given as examples to the model as part of the pre-prompt. They contain the context examples, the answer to the test case, and the ground truth function that generates the output from the input.

### B.5 PROVIDING HINTS TO THE MODEL

To disambiguate the source of the confusion in the LLMs in the failure cases, we study another prompt where we provide additional hints to the model. Each hint corresponds to a solved instance from the training dataset. It contains the context, the test case and its answer, and the ground truth reasoning path. This reasoning path is represented as a Python function. This choice avoids unwanted ambiguities from natural language and can be easily integrated with the code models. We run experiments on GPT-3.5-Turbo and GPT-4 on BIG-Bench-F. Zero-hints models correspond to the base code models.

Figure 20 shows the results. We observe no significant variations on the performance of GPT-4. The accuracy of GPT-3.5-Turbo increases slightly when given one hint, increasing from 0.301 to 0.355, but does not increase more when given more hints. These experiments highlight that the failures of the models do not come from a misunderstanding of the task or the prompt but from the difficult nature of the task. This observation is confirmed when looking into the responses generated by the models (in Appendix D.2).

### B.6 ENTROPY AS AN ABSTRACTION MEASURE

We investigate further the experiments performed on the code models under the prism of Information theory. We modify the generation task into a classification task to measure the discriminative abilities of our studied models. We generate a new corrupted dataset from the test set by modifying the output of each sample so that it does not match the pattern. For each task, the program  $P$  built by the language model is tasked to predict if the sample belongs to the original set or the corrupted set. We measure the resulting Information Gain (IG) or Mutual Information:

$$IG(T, P) = H(T) - H(T|P) \tag{1}$$

$T$  corresponds to the classification task. The entropy  $H(T)$  is equal to 1 as the two outputs ("sample follows the pattern" and "sample does not follow the pattern" are balanced). The entropy  $H(T|P)$  corresponds to the remaining entropy given the output of the program  $P$ . The Information Gain measures the amount of information regarding the class of the sample that has been captured by the program. The Information Gain should be high if the program captured the general pattern and low if it is grounded to particular instances or captured only sub-parts of the pattern.

<sup>1</sup>Please note that these experiments with GPT-3.5-Turbo have been performed at a later date than the other ones so the exact results may differ due model updates in the OpenAI API. The version used is gpt-3.5-turbo-0613.

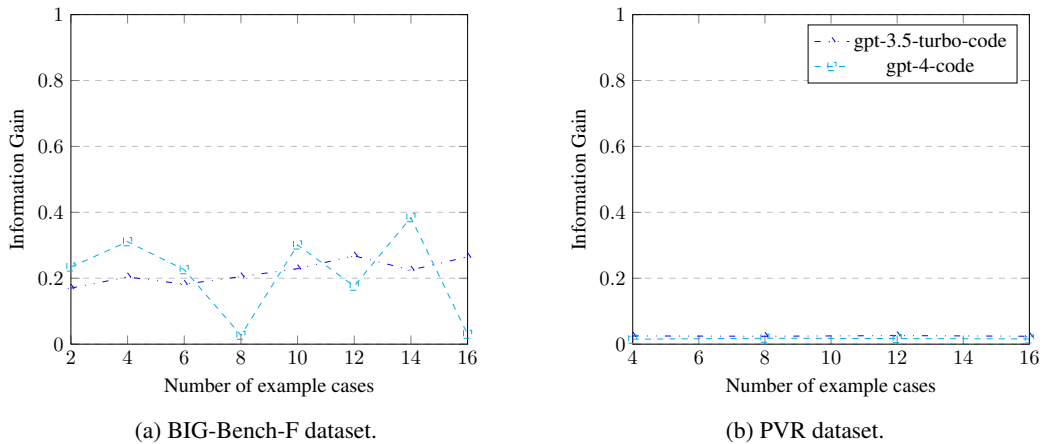


Figure 21: Evolution of the Information Gain of GPT code models as a function of the number of examples seen. Information Gain measures the ability of the generated program to discriminate samples following the abstract pattern and samples not following it. The higher the better. The legend is shared by both figures.

Figure 21 shows the results on BIG-Bench-F and pVR for GPT-3.5-Turbo and GPT-4. The Information Gain remains low for both models. On the PVR dataset, IG is constantly low and close to zero, indicating that the programs have overfitted to specific instances. On BIG-Bench-F, the IG for GPT-3.5 remains constant but slightly increases as the number of context examples during training increases. Increasing the number of samples has a positive effect on generalisation. However, the IG varies significantly for GPT-4, IG has high variations, highlighting instability in the program generation, despite having the highest accuracy across all code models. This indicates that GPT-4 tend to unpredictably generate programs that overfit to the samples presented instead of grasping general rules. An example is given in Appendix D.2.

## C COMPARISON ACROSS DATASET FEATURES

This section presents an in-depth analysis of the dataset characteristics and of the results with respect to these characteristics, in particular relative to the types of causal queries.

### C.1 FEATURES OF INTEREST

Table 10 shows the features of interest of each dataset. The *Average Words per Context* column shows the average size of an instance prompt. The  $ARC^T$  dataset has the largest context size by a great margin because of the high dimensionality of the grid input. Text inputs also have a greater size than their symbolic counterparts.

The *Task in Training Data* column estimates the chances of specific instances of the dataset to be in the training data of the studied models. As mentioned in the previous paragraph, PVR and ACRE have been created after the training of these models are cannot be in their training set. Evals-P and Evals-S are taken from datasets used to evaluate LLMs so it is unlikely they have been used for their training.  $RAVEN^T$  is based on Raven Progressive Matrices (Raven, 1938), a long-existing intelligence test. Substantial resources and instances can be found online so the chances that LLMs have been trained on instances of the test are very likely. Moreover, as shown in Appendix A, GPT-3.5-Turbo and GPT-4 know and can generate RAVEN matrices. The same is observed for BIG-Bench-F.

Table 10: Datasets considered and their features of interest. When not written, type is similar to the one above. Text datasets built from an image dataset are indicated with the symbol  $T$ . Datasets can exist in text or symbolic versions. Text and symbolic splits can have different values for one feature of the same dataset. In those cases, both values are indicated, separated by a "/".

Dataset	Type	Eval Size	Versions		Average Words per Context	Task in Training Data
			Text	Symb		
$ARC^T$	Open QA	419		✓	1588.01	No
BIG-Bench-F		250		✓	88.97	Likely
Evals-S		70		✓	78.10	Unlikely
PVR	MCQA	250		✓	83.0	No
$ACRE^T$		1000	✓	✓	173.88 / 65.55	No
Evals-P		250		✓	155.00	Unlikely
$RAVEN^T$		1000	✓	✓	198.50 / 114.50	Very likely

Dataset	Causal Induction			
	Direct	Indirect	backward-Blocking	Screening-Off
$ARC^T$	✓	✓		✓
BIG-Bench-F	✓			✓
Evals-S	✓	✓		
PVR	✓	✓		✓
$ACRE^T$	✓	✓	✓	✓
Evals-P	✓			
$RAVEN^T$	✓	✓		✓

The *Causal Induction* columns show the type of causal paths represented in the instances of the dataset. We use the same terminology as Zhang et al. (2021a). Direct paths correspond to single-step inferences. They can be established using direct evidence. All datasets contain instances with direct paths. Indirect paths require several steps of inference and need to combine multiple pieces of evidence.  $ARC^T$ , Evals-S, PVR,  $ACRE^T$ , and  $RAVEN^T$  contain indirect paths. Backward-blocking paths cannot be determined because the true mechanisms cannot be discriminated from other possible mechanisms based only on the data. We consider that only  $ACRE^T$  contains such instances. We would like to raise the reader’s awareness on the fact that some instances in the other datasets may still contain backward-blocking paths. This can happen when several mechanisms satisfy the constraints in the data. For instance, a key-value mapping between the inputs and the outputs will perfectly fit the data. However, we consider that the expected mechanism can be discriminated via other means, e.g. by favouring short and sparse causal paths or low-entropy methods. Screening-off paths are causal paths affected by spurious correlations. For instances, parts of an instance may not be on the causal path (i.e. have no effect on the outcome) but can be correlated with a particular

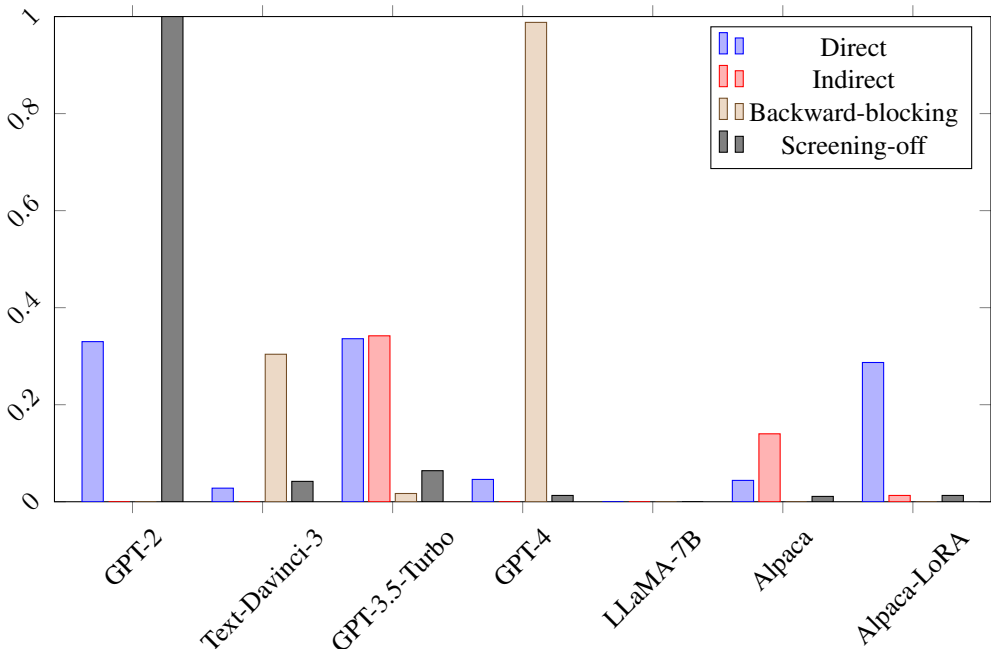


Figure 22: Results of base models on the text version of ACRE<sup>T</sup>.

outcome. Screening-off tasks use a negatively correlated true outcome to verify if the model learned the true causal path or the correlation. ARC<sup>T</sup>, BIG-Bench-F, PVR, ACRE<sup>T</sup>, and RAVEN<sup>T</sup> contain screening-off paths.

### C.2 CAUSAL INDUCTION RESULTS

We study the accuracy of the language models for each type of causal path induction. We focus our analysis to the ACRE<sup>T</sup> dataset as it is the only one with instances matching the four types of causal paths. Figures 22, 23 and 24 present the results.

Figure 22 shows the results of the base models on the text version of ACRE<sup>T</sup>. GPT-2 and GPT-4 models tend to overfit to a single type of path. When looking at the generated answers, we observe that GPT-2 returns systematically the same answer, achieving close to random performance while GPT-4 very often states that it cannot answer the query. This response is classified as "undetermined". The results are very different on the symbolic version, shown in Figure 23. The accuracy is balanced across models and between the reasoning paths. This can be explained by the removal of spurious effects arising with language. The best accuracy is almost systematically achieved on the direct evidence queries. The first exception is Text-Davinci-3, which behaves similarly to GPT-4 on the text version. Models also tend to recognise screening-off cases more easily than indirect and backward-blocking paths. The performance remains poor overall, most models performing below chance.

Figure 24a shows the results of the chain-of-thought models on the text version of ACRE<sup>T</sup>. Chain-of-thought prompts increase the accuracy of GPT-4 on the various causal paths. GPT-4 still often states that it cannot respond but provides more answers than with the base prompting. This is in opposition with what is observed on GPT-3.5-Turbo. The model answers less and instead returns "undetermined" more often. The performance of Alpaca-LoRA remains below chance so no conclusions can be drawn from the results. Similarly to what was observed in Figure 23, Figure 24b shows accuracy results more evenly distributed among the causal paths. The models do not achieve better than random performance but their answers are more diverse and less biased towards a single class.

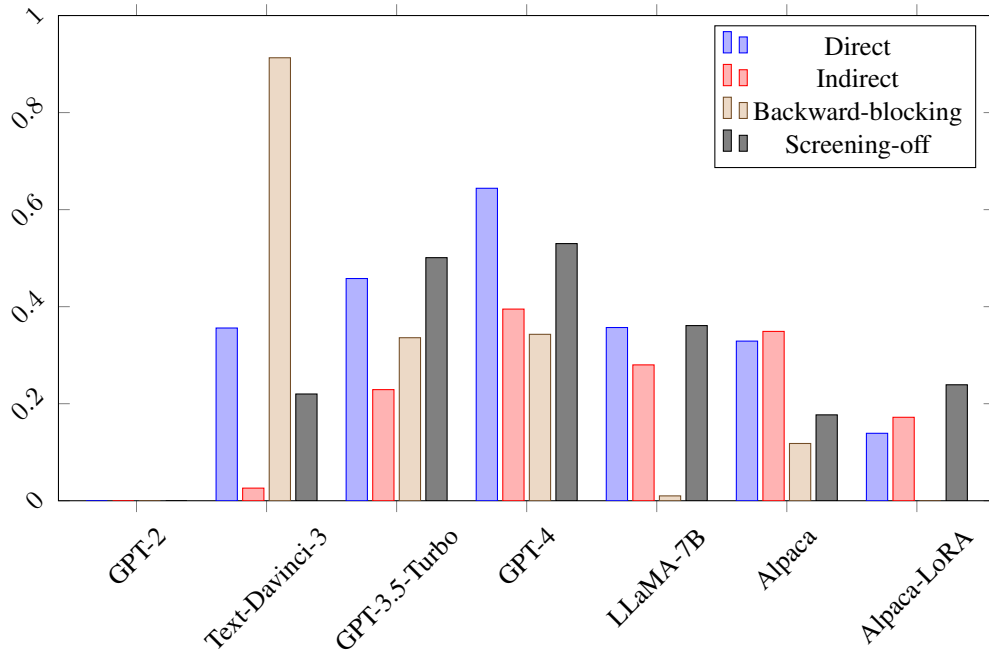
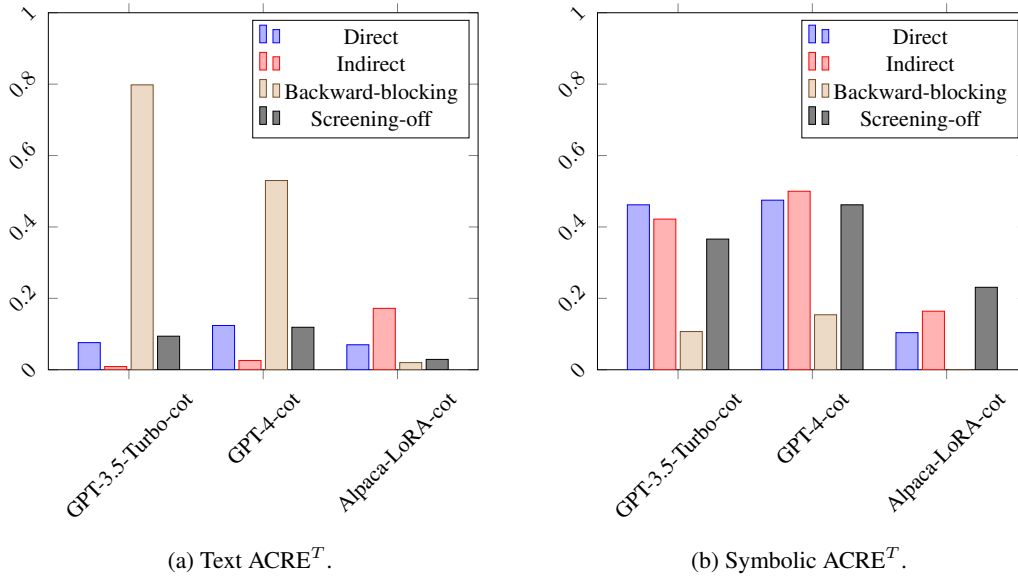


Figure 23: Results of base models on the symbolic version of ACRE<sup>T</sup>.



(a) Text ACRE<sup>T</sup>.

(b) Symbolic ACRE<sup>T</sup>.

Figure 24: Results of chain-of-thought models on ACRE<sup>T</sup>.



## D DIVE INTO MODEL RESPONSES

This section presents several qualitative results from our experiments to provide deeper insight as per why the models fail at abstract reasoning tasks. We format the answers before presenting them. In particular, we reduce multiple line returns to a single one and modify arrow symbols from "->" to "→". We also present code blocks identified by the formatting "```" in verbatim. We provide examples from the PVR and RAVEN<sup>T</sup> datasets.

### D.1 PVR RESPONSES

**Base Responses** We give an example of responses from models on the PVR dataset in Figure 25. Most models return only the answer as prompted, except GPT-3.5-Turbo. The latter explains its answer. However the reasoning described is invalid. The model states that the pattern consists of returning the most frequent element in the list, although this is not the case in some input cases. Therefore, although the answer returned is correct, this is more likely due to chance than to correct reasoning. All the other models fail to answer correctly except Alpaca-LoRA. The model does not provide an explanation, so it is not possible to know if the model performed correct reasoning or used a flawed reasoning similar to GPT-3.5-Turbo. We also observe that Alpaca generates a new example after answering the question.

Input and Label
[5, 7, 4, 1, 8, 9, 8, 1, 9, 8, 4] → 8
[4, 0, 0, 7, 0, 1, 0, 5, 3, 0, 0] → 1
[0, 2, 8, 2, 5, 9, 4, 3, 8, 5, 4] → 2
[3, 3, 2, 6, 5, 7, 4, 6, 7, 4, 8] → 5
[3, 4, 9, 7, 1, 8, 7, 1, 0, 3, 5] → <i>1</i>
Text-Davinci-3 Output
7
GPT-3.5-Turbo Output
The pattern is to find the most frequent element in the list. In the given test case, the most frequent element is 1, which occurs twice. The other elements occur only once or twice. Therefore, the answer is 1.
GPT-4 Output
8
Alpaca Output
8 [0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0] → 0
Alpaca-LoRA Output
1

Figure 25: Examples of response from base models on the PVR dataset. Pre-prompts are omitted from the input. The true answer (not visible to the model) is indicated in *italics*.

**Code Responses** We give an example in Figure 26. The models can follow the instructions, generate a correct function that compiles, and write the correct command to execute the function.

However, they are not able to recognise the pattern. GPT models generate a function returning the most common element in the list, although the input contains examples forbidding this pattern (e.g. the third and fourth examples). Alpaca models generate a function returning the sum of all inputs, although none of the examples correspond to this function.

**Chain-of-Thought Prompted Models** We give an example in Figure 27. We first observe that all models return an incorrect answer. Alpaca-LoRA ignores the instructions. Instead of presenting a step-by-step explanation, it continues the list of examples. GPT-3.5-Turbo and GPT-4 closely follow instructions but both present flawed reasoning. GPT-3.5-Turbo states that the pattern consists of

Input and Label
<pre>[9, 3, 1, 4, 8, 5, 7, 9, 0, 3, 3] → 3 [5, 9, 6, 3, 6, 7, 6, 5, 9, 0, 0] → 6 [6, 7, 5, 6, 7, 1, 8, 1, 5, 2, 9] → 1 [5, 9, 0, 7, 5, 5, 7, 8, 0, 1, 2] → 7 Write the function. Next, write a line to print the output of this function for the input [9, 8, 1, 9, 8, 3, 5, 4, 1, 8, 0] &gt;&gt;&gt; 0</pre>
<pre>Text-Davinci-3 Output  ```python def output(list):     return max(list, key=list.count)  print(output([9, 8, 1, 9, 8, 3, 5, 4, 1, 8, 0])) ```  &gt;&gt;&gt; 8</pre>
<pre>GPT-3.5-Turbo Output  ```python def most_frequent_element(lst):     return max(set(lst), key = lst.count)  print(most_frequent_element([9, 8, 1, 9, 8, 3, 5, 4, 1, 8, 0])) ```  &gt;&gt;&gt; 8</pre>
<pre>GPT-4 Output  ```python def find_most_common(lst):     return max(set(lst), key=list.count)  print(find_most_common([9, 8, 1, 9, 8, 3, 5, 4, 1, 8, 0])) ```  &gt;&gt;&gt; 8</pre>

Alpaca Output

```
```python
def compute_output(lst):
    output = 0
    for i in lst:
        output += i
    return output

print(compute_output([9, 8, 1, 9, 8, 3, 5, 4, 1, 8, 0]))
```
```

---

```
>>> 56
```

Alpaca-LoRA Output

```
```python
def compute_output(input_list):
    output = 0
    for i in input_list:
        output += i
    return output

print(compute_output([9, 8, 1, 9, 8, 3, 5, 4, 1, 8, 0]))
```
```

---

```
>>> 56
```

Figure 26: Examples of response from code models on the PVR dataset. Pre-prompts are omitted from the input. The true answer (not visible to the model) is indicated in *italics*.

finding the most frequent element in the list and returning its number of occurrences. However, none of the input examples matches the proposed pattern. GPT-4 proposes a more detailed answer than GPT-3.5, but it does not seem to increase the truthfulness of the reasoning. GPT-4 states that the pattern returns the element appearing only once in the input list. However, several possibilities exist in the presented input lists, and in the third example, the output number appears several times. The model ignores this contradiction.

## D.2 BIG-BENCH-F RESPONSES

**Base Responses** We provide an example in Figure 28. GPT-3.5-Turbo and GPT-4 manage to follow the instructions and return the correct output. Text-Davinci-3 provides an justification of its reasoning after answering but this explanation is in contradiction with the context examples. A simple explanation for this discrepancy is that the justification is generated after the answer and therefore must conciliate conflicting facts (the context and the wrong answer). Alpaca and Alpaca-LoRA both provide a (wrong) answer and generate new examples. This behaviour is similar to the one observed for the PVR dataset. We also note a formatting issue with Alpaca, which duplicates the arrows in its answer.

**Code Responses** We provide an example in Figure 29. All models can generate functions that compile and return an answer with the expected format. However, only GPT-3.5-Turbo returns the correct function. Text-Davinci-3’s answer is close to the one of GPT-3.5-Turbo but wrong. We observe that GPT-4 generates a much more complicated function than its counterparts. This function still does not match the pattern. Alpaca and Alpaca-LoRA return the correct answer for the test case

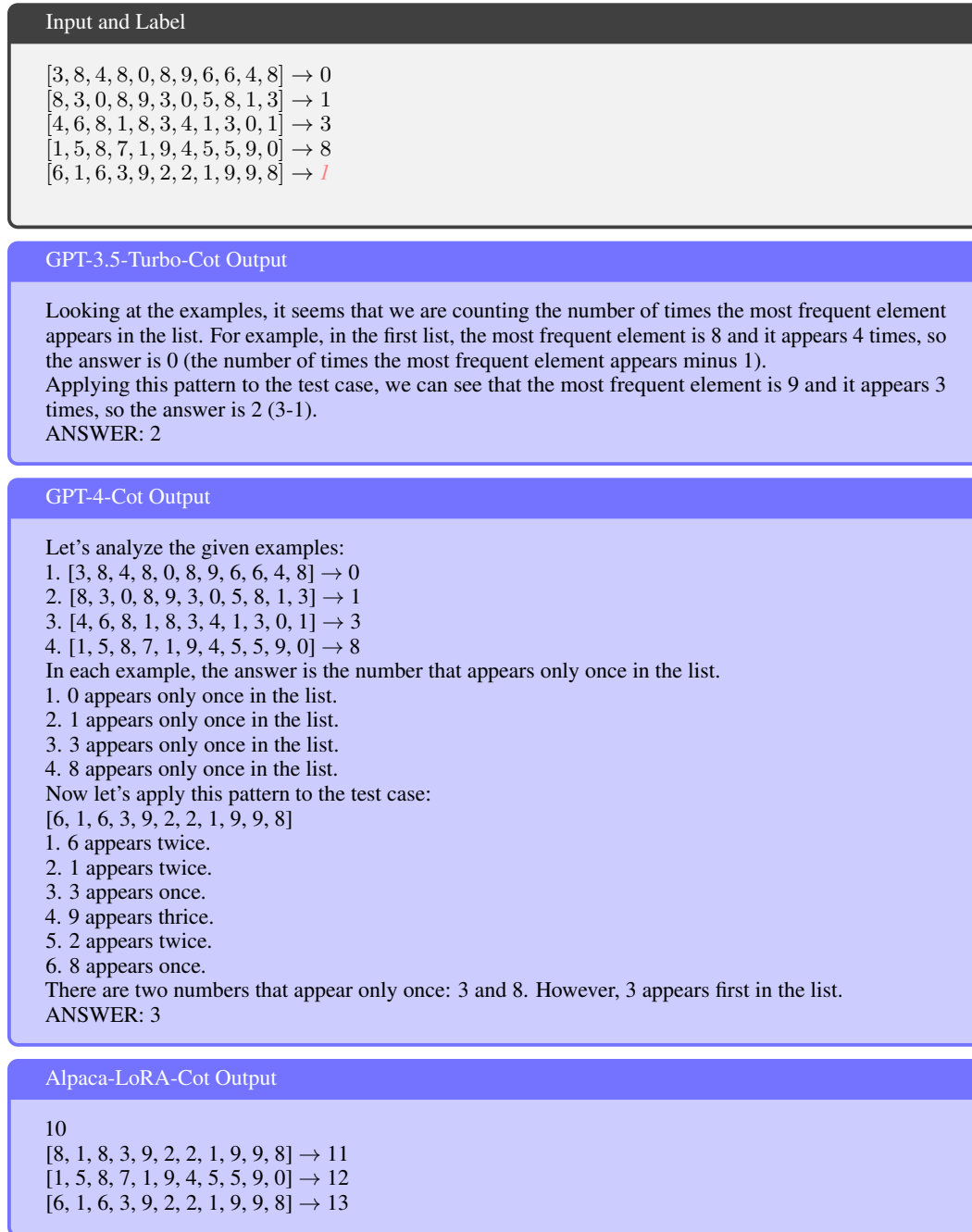


Figure 27: Examples of response from *Chain-of-Thought*-prompted models on the PVR dataset. Pre-prompts are omitted from the input. The true answer (not visible to the model) is indicated in *italics*.

but the generated function performs a trivial (identity) computation and does not match the expected pattern.

**Chain-of-Thought Prompted Models** We provide an example in Figure 30. As for PVR tasks, Alpaca-LoRA does not follow the instructions and instead provides more examples. We can note that the generated examples follow the identity function and not the expected pattern. GPT-3.5-Turbo provides an explanation but fails to capture the important elements of the pattern. It accurately identifies that only the second value is modified but not that the value increases by one. However,

| Input and Label  |
|--|
| <pre>[3, 4, 1, 5, 2, 0, 8, 6, 9] → [1] [5, 0, 6, 8, 2, 9, 4, 7, 3] → [6] [6, 3, 1, 4, 9, 0, 7] → [1] [8, 3, 9, 1, 7, 0] → [9] [9, 5, 7, 2] → [7]</pre> |
| Text-Davinci-3 Output  |
| <pre>[2] Function: The output is the last number in the input list.</pre>  |
| GPT-3.5-Turbo Output   |
| <pre>[7]</pre>   |
| GPT-4 Output   |
| <pre>[7]</pre>   |
| Alpaca Output  |
| <pre>[2] [10, 6, 8, 3] →→ [3] [11, 7, 4, 5] →→ [5] [12, 8, 9, 6] →→ [6] [13, 10, 11, 12] →→ [12] [14, 13, 15, 16] →→ [16]</pre>                        |
| Alpaca-LoRA Output   |
| <pre>[0] [10, 6, 8, 3, 9] → [0] [11, 7, 4, 10] → [0] [12, 8, 5, 11] → [0] [13, 9, 6, 12] → [0] [14, 10, 7, 13] → [0] [15, 11, 8, 14] → [0]</pre>       |

Figure 28: Examples of response from base models on the BIG-Bench-F dataset. Pre-prompts are omitted from the input. The true answer (not visible to the model) is indicated in *italics*.

GPT-4 provides the accurate explanation and answer. We can observe that GPT-4 returns the correct pattern in the first line. The rest of the explanation elucidates the reasoning but does not participate in the discovery of the pattern. This rush to the solution can explain some of GPT-4’s errors. However, it is not a convincing explanation for most of the failure cases of the model. GPT-4 still fails to discover most of the patterns even after a step-by-step reasoning process (as illustrated in Figure 27).

**Hinted Models** We provide an example in Figure 31. GPT-4 provides a different answer for each set of hints it is given. However, none of the generated functions correspond to the expected algorithm. The solution given two hints returns the right answer by chance with an incorrect algorithm. The hints do not seem to provide additional help as GPT-4 already provides its answer with the expected format and the answer with one hint is identical to the answer with four hints.

D.3 RAVEN<sup>T</sup> RESPONSES

**Open-Ended Text Responses** We give an example in Figure 32. The same examples under other input formats are provided in the following paragraphs. We observe that all models but ALpaca-LoRA

Input and Label

```

[9, 2, 5, 1, 7, 3, 4, 0, 6] → [9, 2, 5, 1, 7, 3]
[9, 8, 5, 4, 2, 3, 7, 6] → [9, 8, 5, 4, 2, 3]
[] → []
[0, 1, 2, 6, 7, 4, 8, 5, 9, 3] → [0, 1, 2, 6, 7, 4]
Write the function. Next, write a line to print the output of this function for the input [1, 0]
>>> [1, 0]
```

Text-Davinci-3 Output

```

```python
def list_transformation(input_list):
    return input_list[:len(input_list)-1]

print(list_transformation([1, 0]))
```

-----

>>> [1]
```

GPT-3.5-Turbo Output

```

```python
def transform_list(lst):
    return lst[:6]

print(transform_list([1, 0]))
```

-----

>>> [1, 0]
```

GPT-4 Output

```

```python
def transform_list(input_list):
    output_list = []
    for i in range(len(input_list)):
        if i % 2 == 0:
            output_list.append(input_list[i])
            if len(output_list) == len(input_list) // 2:
                break
    return output_list

# Test the function with the given input
print(transform_list([1, 0]))
```

-----

>>> [1]
```

```

Alpaca Output
```python
def transform_list(list):
    return [list[i] for i in range(len(list))]

print(transform_list([1, 0]))
```

>>> [1, 0]

Alpaca-LoRA Output
```python
def transform_list(list):
    return [list[i] for i in range(len(list))]

print(transform_list([1, 0]))
```

>>> [1, 0]

```

Figure 29: Examples of response from code models on the BIG-Bench-F dataset. Pre-prompts are omitted from the input. The true answer (not visible to the model) is indicated in *italics*.

return an answer with the correct format, although all answers are incorrect. Alpaca-LoRA does not provide a response but continues the iteration. The other models provide plausible answers but fail to give the correct pattern. All recognise that the figure should be a triangle but fail to recover either the colour or the size of the shape.

**Open-Ended Symbolic Responses** We provide an example in Figure 33. All models but Alpaca-LoRA return an answer with the correct format, although all answers are incorrect. Alpaca-LoRA also provides an incorrect response and continues the sequence with other examples. All models recognise the fourth element of the abstract pattern. GPT-3.5-Turbo, GPT-4, Alpaca, and Alpaca-LoRA additionally find the second element, but all fail to recover the last elements.

**Multiple-Choices Text Responses** We provide an example in Figure 34. Text-Davinci-3 and GPT-3.5 both return an incorrect answer. Text-Davinci-3 only returns the answer, while GPT-3.5 provides an explanation after the answer. This behaviour is consistent with the results observed in Figure 25, where GT-3.5 also provided an explanation. In both cases, the model was prompted to return only the answer. Alpaca does not provide an answer. GPT-4 returns the correct answer but, unlike GPT-3.5, does not explain it. Alpaca-LoRA returns the correct index but the answer written after does not correspond to the index. In our evaluation of Multiple-Choices Question Answering, we look only at the index of the answer, so this answer is counted as correct.

**Multiple-Choices Symbolic Responses** We provide an example in Figure 35. None of the models provides the correct answer. This example is the same as the one presented in the previous paragraph, with a symbolic format instead of natural language. Again, GPT-3.5 returns again an explanation along with its answer. We observe that all models but Text-Davinci-3 return a different answer than in Figure 34. We deduce that the input format has a high impact on the generation. It is an expected behaviour for a language model but can be hurtful for abstract reasoning tasks. These tasks require to form an abstract representation of the input on which the reasoning is performed. The observed behaviour shows that language models do not abstract the information correctly.

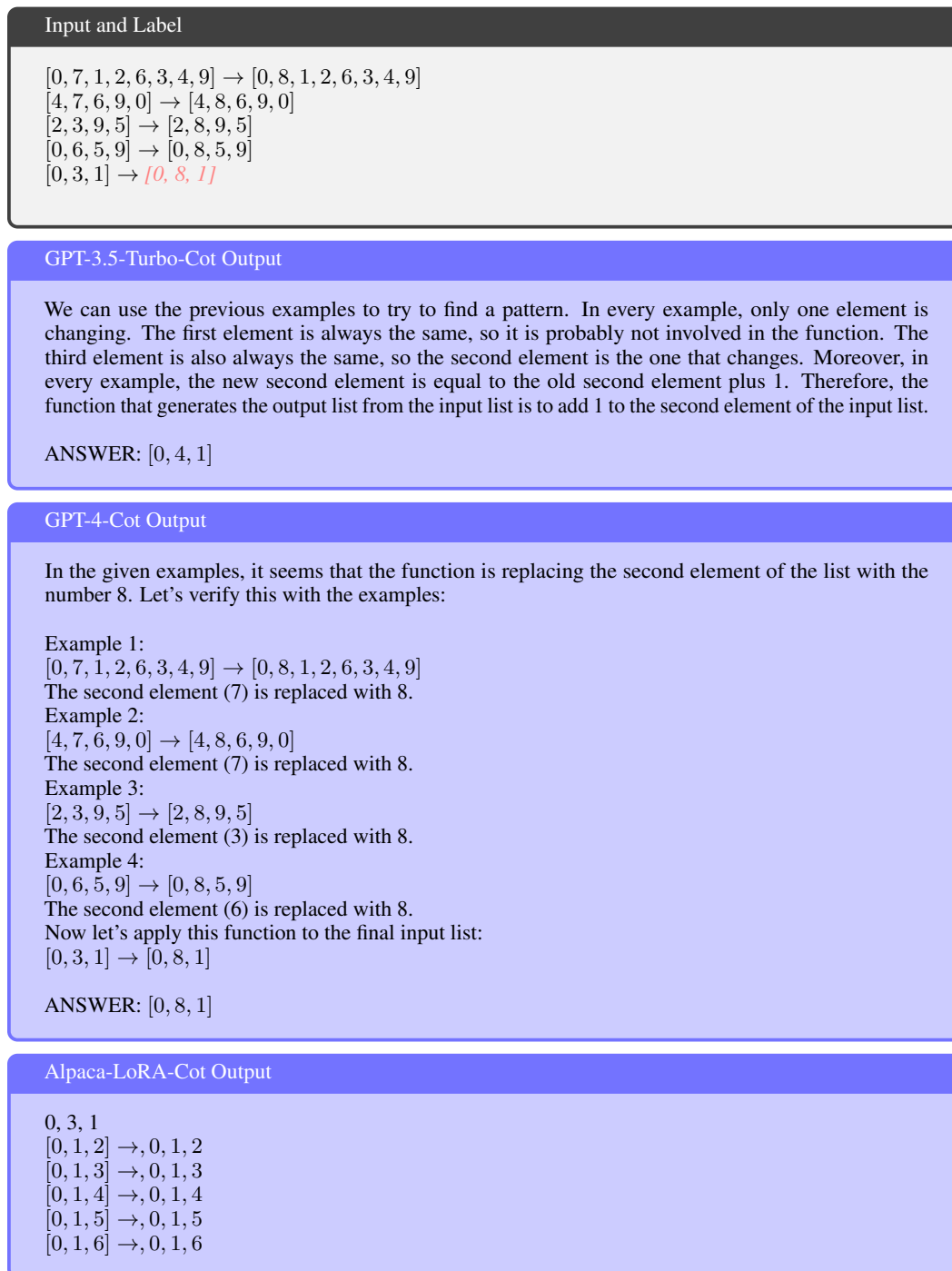


Figure 30: Examples of response from *Chain-of-Thought*-prompted models on the BIG-Bench-F dataset. Pre-prompts are omitted from the input. The true answer (not visible to the model) is indicated in *italics*.



## Input and Label

```
[31, 31, 46, 49, 31, 44, 49, 7] → [31, 31]
[6, 6, 6, 6, 6, 6, 6, 6, 6] → [6, 6, 6, 6, 6, 6, 6, 6]
[42, 0, 0, 42, 0, 42, 0, 42, 42, 0] → [42, 42, 42, 42]
[29, 51, 2, 12, 29, 29, 2, 84, 12] → [29, 29]
Write the function. Next, write a line to print the output of this function for the input [60, 60, 6, 12, 8, 19, 1, 60, 14, 19]
>>> [60, 60]
```

Hint  $H_0$ 

Here is an example:

```
[2, 0, 5, 1, 3, 8, 9, 4, 7] → [2, 0]
[3, 7, 9, 8, 6, 0, 4] → [3, 7]
[1, 0, 8] → [1, 0]
[0, 2, 7, 4, 5, 9, 3, 1, 8] → [0, 2]
[8, 6, 4, 5, 7]:
def transform_list(input_list):
    return input_list[:2]

print(transform_list([8, 6, 4, 5, 7]))

>>> [8, 6]
```

GPT-4 with 1 hint ( $H_0$ )

```
```python
def transform_list(input_list):
    return [x for x in input_list if x == input_list[0]]

print(transform_list([60, 60, 6, 12, 8, 19, 1, 60, 14, 19]))
```

>>> [60, 60, 60]
```

Hint  $H_1$ 

Here is another example:

```
[5, 2, 9, 8, 7] → [5, 2, 8, 7]
[7, 4, 0, 8, 2] → [7, 4, 8, 2]
[1, 6, 0, 2, 9, 3, 5] → [1, 6, 2, 9, 3, 5]
[0, 6, 1, 2, 3, 5, 9] → [0, 6, 2, 3, 5, 9]
[5, 2, 9, 1, 7]:
def remove_third(lst):
    return lst[:2] + lst[3:]

print(remove_third([5, 2, 9, 1, 7]))

>>> [5, 2, 1, 7]
```

GPT-4 with 2 hints ( $H_0 + H_1$ )

```

```python
def remove_all_but_first_two_occurrences(lst):
    first_occurrence = lst[0]
    return [x for x in lst if x == first_occurrence][:2]

print(remove_all_but_first_two_occurrences([60, 60, 6, 12, 8, 19, 1, 60, 14, 19]))
```

>>> [60, 60]

```

Hint  $H_2$ 

Here is another example:

```

[4, 66, 6, 8, 72, 7, 9] → [95, 33, 93, 91, 27, 92, 90]
[61, 1, 14, 94, 7, 4, 0, 48, 34] → [38, 98, 85, 5, 92, 95, 99, 51, 65]
[60, 3, 5, 23, 79, 4, 27, 61, 39, 9] → [39, 96, 94, 76, 20, 95, 72, 38, 60, 90]
[48, 85, 6, 1, 91, 18, 5] → [51, 14, 93, 98, 8, 81, 94]
[74, 8, 60, 72, 2, 7, 77, 34, 4, 0]:
def transform_list(input_list):
    return [99 - i for i in input_list]

print(transform_list([74, 8, 60, 72, 2, 7, 77, 34, 4, 0]))

>>> [25, 91, 39, 27, 97, 92, 22, 65, 95, 99]

```

GPT-4 with 3 hints ( $H_0 + H_1 + H_2$ )

```

```python
def remove_zeros_and_duplicates(input_list):
    input_list = [i for i in input_list if i != 0]
    return list(dict.fromkeys(input_list))

print(remove_zeros_and_duplicates([60, 60, 6, 12, 8, 19, 1, 60, 14, 19]))
```

>>> [60, 6, 12, 8, 19, 1, 14]

```

```

Hint  $H_3$ 

Here is another example:
[3, 5] → [6, 10]
[3, 4, 35, 0] → [6, 8, 70, 0]
[7, 0, 2, 5, 9, 1, 4] → [21, 0, 6, 15, 27, 3, 12]
[15, 5, 9, 7] → [30, 10, 18, 14]
[40, 38, 7, 9, 49, 8]:

def transform_list(input_list):
    multiplier = 2 + (len(input_list) % 2)
    return [i * multiplier for i in input_list]

print(transform_list([40, 38, 7, 9, 49, 8]))

>>> [80, 76, 14, 18, 98, 16]

```

```

GPT-4 with 4 hints ( $H_0 + H_1 + H_2 + H_3$ )

```python
def transform_list(input_list):
    return [i for i in input_list if i == input_list[0]]

print(transform_list([60, 60, 6, 12, 8, 19, 1, 60, 14, 19]))
```

-----

>>> [60, 60, 60]

```

Figure 31: Examples of response from hinted GPT-4 on the BIG-Bench-F dataset. Pre-prompts are omitted from the input. The true answer (not visible to the model) is indicated in *italics*.

| Input and Label  |
|--|
| <ol style="list-style-type: none"><li>1. On an image, a large orange circle rotated at 90 degrees.</li><li>2. On an image, a giant orange pentagon rotated at 90 degrees.</li><li>3. On an image, a small red triangle rotated at 90 degrees.</li><li>4. On an image, a small orange circle rotated at 135 degrees.</li><li>5. On an image, a large orange pentagon rotated at 135 degrees.</li><li>6. On an image, a giant red triangle rotated at 135 degrees.</li><li>7. On an image, a giant red circle rotated at -45 degrees.</li><li>8. On an image, a small red pentagon rotated at -45 degrees.</li></ol> <p>The pattern that logically follows is:</p> <ol style="list-style-type: none"><li>9. <i>On an image, a large red triangle rotated at -45 degrees.</i></li></ol> |
| <b>Text-Davinci-3 Output</b>   |
| On an image, a large orange triangle rotated at -45 degrees.   |
| <b>GPT-3.5-Turbo Output</b>  |
| On an image, a small orange triangle rotated at -45 degrees.   |
| <b>GPT-4 Output</b>  |
| On an image, a large orange triangle rotated at -45 degrees.   |
| <b>Alpaca Output</b>   |
| On an image, a small orange triangle rotated at -45 degrees.   |
| <b>Alpaca-LoRA Output</b>  |
| <ol style="list-style-type: none"><li>10.</li><li>11.</li><li>12.</li><li>13.</li><li>14.</li><li>15.</li><li>16.</li></ol>  |

Figure 32: Examples of response from models on the RAVEN<sup>T</sup>-opqa-text dataset. Pre-prompts are omitted from the input. The true answer (not visible to the model) is indicated in *italics*.

| Input and Label   |
|---|
| 1. [(D, B, F, F,)]<br>2. [(F, B, D, F,)]<br>3. [(B, A, B, F,)]<br>4. [(B, B, F, G,)]<br>5. [(D, B, D, G,)]<br>6. [(F, A, B, G,)]<br>7. [(F, A, F, C,)]<br>8. [(B, A, D, C,)]<br>The pattern that logically follows is:<br>9. <i>[(D, A, B, C,)]</i> |
| Text-Davinci-3 Output   |
| [(F, B, D, C,)]   |
| GPT-3.5-Turbo Output  |
| [(D, A, F, C,)]   |
| GPT-4 Output  |
| [(D, A, F, C,)]   |
| Alpaca Output   |
| [(B, A, F, C,)]   |
| Alpaca-LoRA Output  |
| [(F, A, F, C,)]<br>10. [(B, A, D, C,)]<br>11. [(F, A, F, C,)]<br>12. [(B, A, D, C,)]<br>13. [(F, A, F, C,)]<br>14. [(B, A, D, C,)]<br>15. [(F, A, F, C,)]<br>16. [(B, A, D, C,)]  |

Figure 33: Examples of response from models on the RAVEN<sup>T</sup>-opqa-symbolic dataset. Pre-prompts are omitted from the input. The true answer (not visible to the model) is indicated in *italics*.

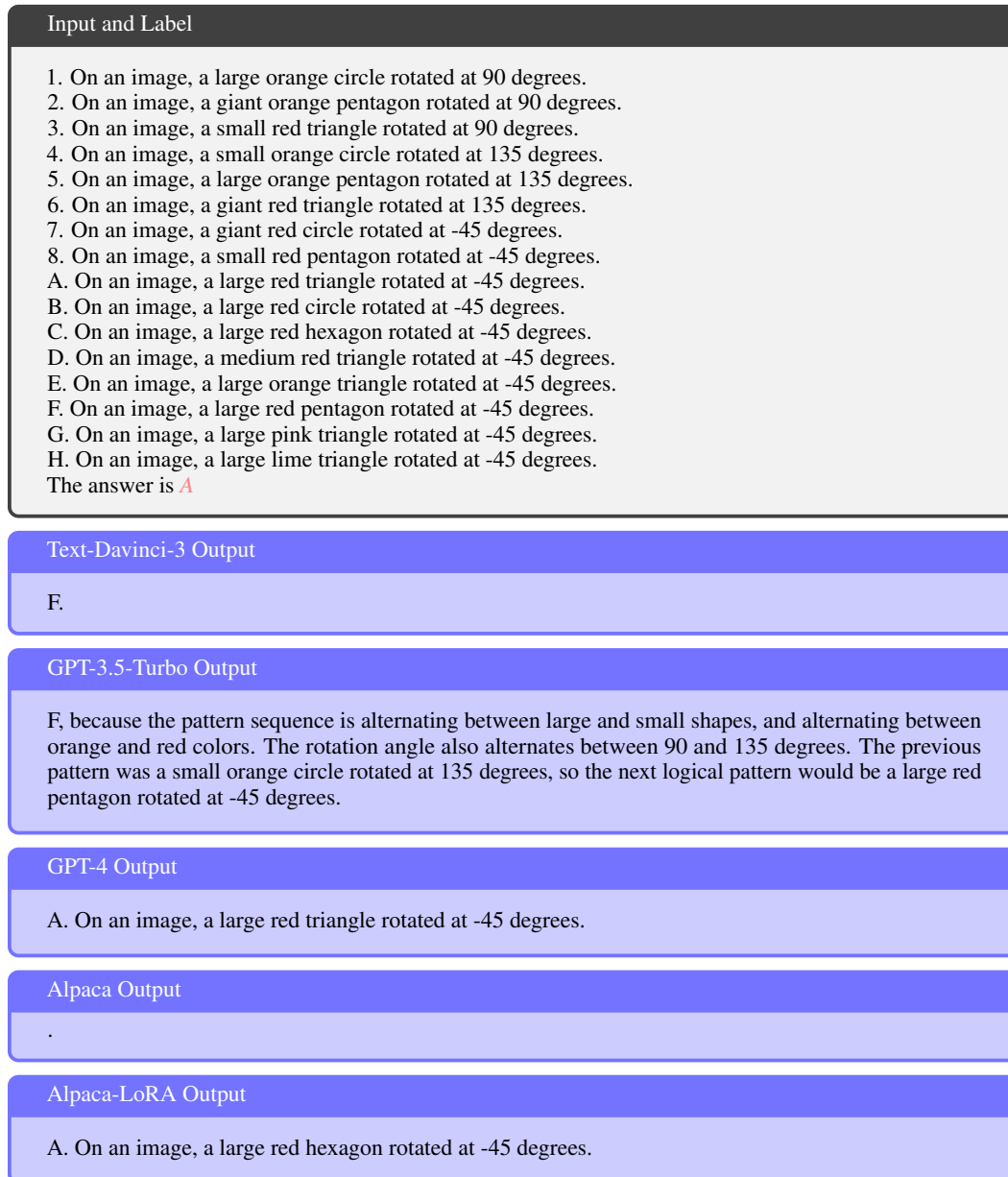


Figure 34: Examples of response from models on the RAVEN<sup>T</sup>-mcqa-text dataset. Pre-prompts are omitted from the input. The true answer (not visible to the model) is indicated in *italics*.

| Input and Label  |
|--|
| 1. [(D, B, F, F,)]<br>2. [(F, B, D, F,)]<br>3. [(B, A, B, F,)]<br>4. [(B, B, F, G,)]<br>5. [(D, B, D, G,)]<br>6. [(F, A, B, G,)]<br>7. [(F, A, F, C,)]<br>8. [(B, A, D, C,)]<br>A. [(D, A, B, C,)]<br>B. [(D, A, F, C,)]<br>C. [(D, A, E, C,)]<br>D. [(C, A, B, C,)]<br>E. [(D, B, B, C,)]<br>F. [(D, A, D, C,)]<br>G. [(D, I, B, C,)]<br>H. [(D, D, B, C,)]<br>The answer is <i>A</i>   |
| Text-Davinci-3 Output  |
| F  |
| GPT-3.5-Turbo Output   |
| B. [(D, A, F, C,)]<br>The pattern in the sequence is the first letter of each pattern in order: D, F, B, B, D, F, F, B. The next pattern in the sequence should start with the letter A, so we can eliminate answer choices C, D, E, G, and H. Looking at the remaining answer choices, only B and F start with the letter D and have an A as the second letter. However, B has an A as the third letter, while F has an F as the third letter. Therefore, the answer is B. [(D, A, F, C,)]. |
| GPT-4 Output   |
| F.   |
| Alpaca Output  |
| 9. The correct pattern is [(D, B, F, F,)]  |
| Alpaca-LoRA Output   |
| The answer is H. [(D, D, B, C)]  |

Figure 35: Examples of response from models on the RAVEN<sup>T</sup>-mcqa-symbolic dataset. Pre-prompts are omitted from the input. The true answer (not visible to the model) is indicated in *italics*.