000 001 002 003 LLM-POWERED PREDICTIVE DECISION-MAKING FOR SUSTAINABLE DATA CENTER OPERATIONS

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ABSTRACT

The growing demand for AI-driven workloads, particularly from Large Language Models (LLMs), has raised concerns about the significant energy and resource consumption in data centers. This work introduces a novel LLM-based predictive scheduling system designed to enhance operational efficiency while reducing the environmental impact of data centers. Our system utilizes an LLM to predict key metrics such as execution time and energy consumption from source code, and it has the potential to extend to other sustainability-focused metrics like water usage for cooling and carbon emissions, provided the data center can track such data. The predictive model is followed by a real-time scheduling algorithm that allocates GPU resources, aiming to improve sustainability by optimizing both energy consumption and queuing delays. With fast inference times, the ability to generalize across diverse task types, and minimal data requirements for training, our approach offers a practical solution for data center scheduling. This framework demonstrates strong potential for advancing sustainability objectives in AI-driven infrastructure. Through our collaboration with a data center, we achieved a 32% reduction in energy consumption and a 30% decrease in waiting time.

1 INTRODUCTION

029 030 031 032 033 034 035 036 037 038 039 040 041 042 043 The rapid advancement of Machine Learning (ML), especially Large Language Models (LLMs), has brought about groundbreaking capabilities, yet it has also raised significant social and environmental concerns [\(Pichai, 2024;](#page-12-0) [Amazon, 2024;](#page-8-0) [Nakagawa & Smith, 2023\)](#page-11-0). One of the most pressing issues is the substantial energy and water resources consumed during ML model training and serving, which has sparked widespread concerns [\(Blunt & Hiller, 2024;](#page-9-0) [Criddle & Bryan, 2024;](#page-10-0) [Solon,](#page-12-1) [2021\)](#page-12-1). The computationally intensive ML jobs can demand hundreds of GPU-hours and consume substantial amounts of energy for power and water for cooling. As a result, the growing demand for ML-based applications has significantly amplified the environmental impact of data centers, highlighting the need for modern infrastructure that is both more efficient and sustainable specifically for AI-driven workloads [\(Bianchini et al., 2024;](#page-9-1) [Li et al., 2024;](#page-11-1) [Kaack et al., 2022\)](#page-11-2). This paper aims to enhance data center operation efficiency and reduce the environmental footprint of modern data centers by devising a LLM-based predictive scheduling system for allocating data center resources (e.g., GPUs) across a stream of ML jobs efficiently. We harness the contextual understanding and predictive abilities of LLMs and combine the predictive power to sequential decision-making that optimize data-center operations.

Figure 1: Our Proposed Pipeline

053 As illustrated in Figure [1,](#page-0-0) our proposed method first employs an LLM that takes the ML job's source code as input and outputs estimates for the required resources, including execution time and **054 055 056 057 058** GPU energy consumption. We believe that the approach has great potential in predicting with other metrics including water consumption and carbon emission, if these data is available from the data center. By leveraging these estimates, the data center can make more informed and efficient realtime decisions for the GPU resource allocation, leading to improvements such as reduced task queue waiting times and lower overall energy consumption.

059 060 061 062 063 064 065 066 067 068 This work aim to address a key limitation in the current operational pipelines of small to large-scale data centers. We focus on the prevalent practice where users submit tasks and request resources, and the data center allocates resources based on heuristic algorithms that rely on user-provided estimates, such as predicted task duration and resource needs [\(Tirmazi et al., 2020\)](#page-12-2). The optimal resource allocation, in hindsight, depends on the actual time and energy consumed by the tasks. However, accurately predicting these factors is nearly impossible due to the inherent complexity of modern computing systems. Consequently, neither the user nor the data center has precise knowledge of the optimal resources required for a given task, leading to inefficiencies and resource wastage. Our approach introduces a unified, effective predictive model, followed by a real-time, data-driven scheduling system that enables more efficient and sustainable resource allocation decisions.

Figure 2: Illustration of our unified predictive approach. Notably, previous methods were unable to handle tasks that had not been seen before, or composite tasks (e.g., training a CNN followed by an LSTM). However, the generalization capacity of LLMs allows our model to effectively manage such cases, making it adaptable to a wider variety of task types and combinations.

1.1 OUR CONTRIBUTION

089 090 091 092 093 We present a prototype pipeline that provides both methodological and practical contributions to various aspects of data center operations, specifically tailored for AI training and inference applications. Our approach provides methodological insights while opening up new possibilities for applications, especially within today's sustainability and AI-driven context. We defer more discussions on the related works to Appendix [A.1.](#page-14-0)

094 095 Methodological Contributions: Our work advances the fields of data center predictive modeling and sequential decision-making.

- LLM-based Versatile Predictive Model: While many predictive methods exist for data center operations, to our best knowledge, we are the first to offer a comprehensive, endto-end solution that takes source code as input and outputs estimations of interest. Our model has the potential to be compatible with **any** user-submitted task and can predict **any** measurable metric the data center requires. The strength of our approach lies in the fact that LLM-generated representations are more informative and generalizable than handcrafted features, leading to improved predictive performance and enhanced operational efficiency.
- **104 105 106 107** • Fully Automated Predictive Scheduling System: This approach enables the possibility of a fully automated predictive scheduling system. By adopting our unified framework, the system is capable of handling any user-submitted tasks and provide estimations of interests directly. This was previously unattainable (see Figure [3\)](#page-3-0), as traditional prediction methods were highly task-specific (e.g., CNN-only or LLM-only), and could only cover a limited

108 109 110 111 112 113 114 115 116 117 118 number of task types. Moreover, each type of task required separate prediction models and handcrafted features, significantly limiting the flexibility and scalability of these methods. • Sequential Decision-Making Algorithms: Our predictive framework is complemented by a sequential decision-making algorithm for optimizing resource allocation. This problem arises from the area of reusable resource allocation and queuing control, where no analytical solution exists. We propose a data-driven decision-making algorithm, and implement it in collaboration with a small-size data center. Our algorithm significantly outperforms the baseline scheduling rule, reducing energy consumption by 32% and queuing delays by 30%. This approach leads to more effective data-center management, especially given the growing emphasis on sustainability.

119 120 121 Application-Level Contributions: The unique features of our methodology—an end-to-end predictive model and its compatibility with diverse task types and estimation targets—offer substantial potential for developing next-generation AI-driven infrastructures in data centers.

- Practical Deployment: Our pipeline executes within one second, enabling a cost-effective, fully automated predictive scheduling system. Additionally, training and deploying the model within data centers is straightforward and can be effective even with a limited amount of data, making it particularly practical for real-world data center operations.
- Multi-Purpose Sustainable Data Center Operations: Our method is versatile enough to predict a wide range of metrics, including time and energy, and we believe it can also predict carbon emissions and water consumption. Unlike previous target-specific approaches, which were limited to particular models, our unified framework offers an all-in-one solution that addresses a broad array of predictive needs, providing key insights for building more sustainable and environmentally friendly data center infrastructures.
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2 PROBLEM FORMATION

136 137 138 139 140 141 142 143 The Prediction Problem. Consider a data center equipped with various types of GPUs, where machine learning tasks arrive sequentially. The data center must decide which type of GPU to allocate to each arriving task (noting that the number of GPUs is often specified in the user-submitted code or command input). Let x represent the source code submitted by the user, and z represent the data center's decision, which corresponds to the type of GPU to allocate for executing the task. A decision z results in outcomes including the time required to complete the task, denoted by t , and the energy consumption using configuration z to complete task x , denoted by e . The relationship between the outcomes and the decision is modeled by functions f and g , such that

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t := f(\boldsymbol{x}, z), \quad e := g(\boldsymbol{x}, z).
$$

146 147 148 149 Here we note that this function f and g is data-center-specific, it depends on the infrastrcture of the data center, for example, bandwith, CPUs, memory, storage, communication, system setup, software stack, etc. In general, characterizing the functions $f(x, z)$ and $g(x, z)$ is highly challenging due to the complexity of modern computing systems.

150 151 152 153 154 155 156 157 158 Prediction using Large Language Models. To tackle the prediction problem, we employ Large Language Models (LLMs) [\(Ouyang et al., 2022;](#page-11-3) [Radford et al., 2019;](#page-12-3) [Achiam et al., 2023\)](#page-8-1). For simplicity, we refer readers to [Vaswani et al.](#page-12-4) [\(2017\)](#page-12-4) for a detailed explanation of decoder-based Transformers and LLM architectures. In this paper, we use f_{θ} and g_{θ} as shorthand notations to represent LLMs, where θ encapsulates all the model parameters. f_{θ} and g_{θ} take two inputs: the task's source code x and the data center's decision z . The rationale is that the LLM can effectively analyze and interpret the task's source code, transforming it into meaningful representations; these representations, when combined with the GPU configuration z , allow the model to produce estimates such that:

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 $f_{\theta}(\boldsymbol{x}, z) \approx f(\boldsymbol{x}, z), \quad g_{\theta}(\boldsymbol{x}, z) \approx g(\boldsymbol{x}, z).$

¹⁶¹ To justify our LLM-based approach, we highlight two key features of LLMs that make them particularly appealing in our context:

 Figure 3: Illustration of our model architecture. Our streamlined design is easy and fast to implement, highly flexible, and generalizable across a variety of tasks. Notice that to estimate other quantities of interest, we simply need to add additional probes. In contrast, previous methods required different handcrafted features and separate prediction models for each task, making them far less flexible and scalable. The lower graph illustrates the performance difference, where points closer to the straight line indicate more accurate predictions. The performance is evaluated under test sets with additional adversarially generated data, and our method outperforms the previous approach (from [Cai et al.](#page-9-2) [\(2017\)](#page-9-2) and [Justus et al.](#page-11-4) [\(2018\)](#page-11-4)) in both accuracy and robustness. Notably, the previous method shows consistent systematic bias, likely due to its reliance on "physical" features like the number of forward/backward passes and layer depth, which lack generalizability.

- Contextual comprehension and feature extraction. LLMs are renowned for their superior ability to comprehend the context in the source code extract features, named representations. With a large corpus of pre-training data, LLMs and other natural language models (NLP) can discern essential parts of the code with relevant information, transform them into representations containing meaningful information [\(Tenney et al.;](#page-12-5) [Pilehvar &](#page-12-6) [Camacho-Collados, 2020\)](#page-12-6), and leverage these vectors to predict time, energy consumption, and other metrics.
- Generalization Another remarkable capability of LLMs is their ability to generalize [\(Wei](#page-13-0) [et al., 2022\)](#page-13-0). Even if the pre-training dataset does not cover all possible examples within the function domains, LLMs can still recognize patterns in the dataset and extend their learned knowledge to achieve reasonably accurate approximations.
- 2.1 MODEL ARCHITECTURE PREDICTION

In this section, we formally describe the architecture of our prediction model. Our approach utilizes a pre-trained LLM for extracting source code representations and applies a probe [\(Alain, 2016;](#page-8-2) [Radford et al., 2017;](#page-12-7) Vulić et al., 2020; [Zhang et al., 2022\)](#page-13-1) to train a supervised model that predicts the quantity of interest. Figure [3](#page-3-0) illustrates the architecture and the different performance compared to previous methods.

- Extracting Representations: We adopt a pre-trained LLM to extract task representations, modeled as a function $l_{\theta_1}(\cdot) : \mathcal{V} \to \mathbb{R}^d$, where V denotes the space of source code and \mathbb{R}^d is the d-dimensional embedding space for mapped representations. Here, θ_1 encapsulates the LLM's parameters. Note that $l_{\theta_1}(\cdot)$ refers to the LLM without its final linear and softmax layers, and for the last layer, it outputs the last token's representation, which is a d-dimensional vector.
- • Probing: Probing involves taking the generated representations and predicting the target value using a linear regression or shallow neural network. We denote this probe as $h_{\theta_2}(\cdot, \cdot)$:

216 217 218 $\mathbb{R}^d \times \mathcal{Z} \to \mathbb{R}$, where θ_2 represents the parameters of the probe and \mathcal{Z} denotes the decision space (e.g., the types of GPUs).

219 220 221 222 223 Thus, our predictive model for the execution time can be represented as $f_{\theta}(\mathbf{x}, z) = h_{\theta_2}(l_{\theta_1}(\mathbf{x}), z)$. For the energy estimation function $g_{\theta}(x, z)$, we use the same representation but train a separate probe, denoted q_{θ_2} , such that $g_\theta(\bm{x}, z) = q_{\theta_2}(l_{\theta_1}(\bm{x}), z)$. Note that θ , θ_1 , and θ_2 refer to classes of parameters, indicating that the parameter dimensions are the same across functions, though these functions do not necessarily share the same parameters.

224 225 226 227 Advantage over Previous Methods. We identify the key factor that could possibly explain the advantage of our method. As mentioned earlier, the challenging part of the data-center operations arise from the complexity of modern computer systems. We first give a notation that characterize the previous approaches.

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• For estimating execution time $t = f(x, z)$ and energy consumption $e = g(x, z)$, previous methods rely on handcrafted features, denoted by $u_t = l_t(x)$ for time and $u_e = l_e(x)$ for energy, where $l_t(\cdot)$ and $l_e(\cdot)$ represent the feature extraction functions. Importantly, the design of $l_t(\cdot)$ and $l_e(\cdot)$ varies significantly depending on the target variable and prediction context, making them different for each prediction task.

- Separate models are then trained for each target, such as $h_t(\cdot, \cdot)$ for time and $h_e(\cdot, \cdot)$ for energy, resulting in the following approximations: $t \approx h_t(l_t(\mathbf{x}), z)$ and $e \approx h_e(l_e(\mathbf{x}), z)$. To account for the dependence on z , which represents the GPU choices, several estimation techniques attempt to model the architecture differences between GPUs. While this approach makes sense physically, it suffers from a lack of flexibility and scalability. Modeling the dependence on z is typically restricted to specific types of source code x and GPU choices z, rendering the models unable to generalize to unseen tasks or GPU configurations.
- **241** Our approach is better in terms of the architecture for a various reasons
	- Better Representation. It has been demonstrated in various domains that representations extracted by pre-trained models are significantly more effective than handcrafted features. In this context, our prediction task can also be viewed as a form of feature extraction akin to Natural Language Processing (NLP), where pre-trained models capture richer and more comprehensive information. These representations are more generalizable and universal, making them applicable to a wide variety of prediction tasks related to the characteristics of the source code.
	- Data-Driven Predictive Modeling. Many traditional predictive models rely on the intrinsic characteristics of the underlying machine learning model, such as CNNs, where predictions are made by explicitly calculating factors like the number of forward/backward passes and the layer depth. While these "physical" models can achieve high accuracy when the test environment perfectly matches the assumptions, they often fall short in data-center operations. For instance, even tasks that train the same CNN architecture may exhibit variations in execution time due to differences in the way the code is written. Additionally, many modern tasks involve training and inference across multiple models, alongside various other function implementations. In such settings, physically based predictive models lack the flexibility and adaptability needed for accurate predictions. In contrast, our datadriven approach is flexible enough to learn the inherent relationships between the source code, the characteristics of computer systems and GPUs, and a variety of targeted metrics.
- **261 262 263 264 265 266 267 268** • Less Data Hungry. Traditional methods often require large amounts of source code examples to train predictive models effectively. In contrast, by leveraging a pretrained LLM, which has already been trained on terabytes of data, we capitalize on the model's superior understanding of contextual knowledge. This allows us to obtain a highly effective feature extractor with far less training data, improving both data efficiency and performance. Indeed, our predictive model is trained using only a little more than 500 source code examples, each paired with corresponding results for energy consumption and execution time across different GPUs in the server.
- **269** • Generalization for GPU Dependence. Another advantage of our approach is its ability to maximize the generalization power of the LLM's representation across different down-

270 271 272 273 274 275 stream tasks. By utilizing the same representation for every prediction task and maintaining a consistent structure for the downstream probe, our method facilitates the discovery of patterns across different GPU configurations. This consistency preserves the model's generalization capacity, ensuring its adaptability to various GPU architectures. Such a factor is missing in previous methods, which followed a more restricted modeling approach, limiting their flexibility and ability to generalize across diverse hardware setups.

276 277 278 279 280 281 282 Training Process. To train our predictive model, for simplicity we assume the parameters of the pretrained LLM $l_{\theta_1}(\cdot)$ remain fixed, and we will discuss the practical training procedure in a followup remark. We first collect a dataset D consisting of the representations of the source code $l_{\theta_1}(\bm{x})$ and the corresponding execution results, including time t and energy e , across different GPU configurations z. Each task x is executed on multiple GPUs to measure both time and energy consumption. Let $|\mathcal{Z}|$ denote the cardinality of the decision space, i.e., the number of available GPUs. The training set, with size n , can be written as:

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\mathcal{D} = \left\{\left(l_{\theta_1}(\boldsymbol{x}_i), \{t_{ij}, e_{ij}\}_{j=1}^{|\mathcal{Z}|}\right)\right\}_{i=1}^n
$$

,

285 286 287 288 289 290 291 where $t_{ij} = f(\mathbf{x}_i, j)$ and $e_{ij} = g(\mathbf{x}_i, j)$ are the time and energy required for task \mathbf{x}_i when executed on GPU $z = j$. Using this dataset, we train two separate probes: $h_{\theta_2}(\cdot)$ for time prediction, and $q_{\theta_2}(\cdot)$ for energy prediction. The goal is to minimize the error between the actual values t_{ij}, e_{ij} and the predictions $h_{\theta_2}(l_{\theta_1}(\bm{x}_i),j)$ and $q_{\theta_2}(l_{\theta_1}(\bm{x}_i),j)$ respectively. Since for simplicity we assume θ_1 is fixed, the loss for the time is $\mathcal{L}_t(\theta_2) = \frac{1}{n|\mathcal{Z}|} \sum_{i=1}^n \sum_{j=1}^{|\mathcal{Z}|} (t_{ij} - h_{\theta_2}(l_{\theta_1}(\boldsymbol{x}_i), j))^2$, and the loss for energy prediction is: $\mathcal{L}_e(\theta_2) = \frac{1}{n|\mathcal{Z}|} \sum_{i=1}^n \sum_{j=1}^{|\mathcal{Z}|} (e_{ij} - q_{\theta_2}(l_{\theta_1}(\boldsymbol{x}_i), j))^2$.

292 293 We remark that the training process described above represents the simplest version for illustrative purposes. In practice, the training process can be more complex and we will address them here.

- One limitation of the approach presented is that the data center would need to run all submitted code to obtain execution time and energy consumption estimates. However, data centers can leverage their existing user submitted codebase and operational data. By recording execution time, energy consumption, and even metrics like carbon emissions and water usage (if measurable), data centers can accumulate vast amounts of data to train the probes effectively. This method allows data centers to continuously refine their predictive models without the need for additional computational overhead.
- Another limitation of the current approach is that we fix the parameters θ_1 of the pretrained LLM and only train the probe parameters θ_2 . While this approach simplifies the training process, it may not fully utilize the potential of the model. In practice, we can enhance performance by fine-tuning the LLM or incorporating more advanced techniques like Reinforcement Learning from Human Feedback (RLHF) [\(Ouyang et al., 2022\)](#page-11-3) or incorporating a reward model [\(Rafailov et al., 2024\)](#page-12-9). Based on the potential benefits of fine-tuning, RLHF, and reward models, these approaches offer even greater possibilities for improving predictive performance. These enhancements will be considered as part of future work.

309 310 2.2 PROBLEM FORMATION: DECISION-MAKING

311 312 313 314 315 316 317 Constraints. Consider a data center equipped with $|\mathcal{Z}| = M$ types of GPUs, where tasks i with source code x_i arrive sequentially in time, and the data center must decide which GPU type $z_i \in \mathcal{Z}$ to allocate (notice that the task's source code x_i also specify its preference on GPUs, and we can model this by constraining the action set \mathcal{Z}). The GPU resources are limited, and is represented by $c = [c_1, \dots, c_M]^\top$, where c_j is the total number of GPUs of type j. If no GPUs are available, the task is placed in a waiting queue. The total available GPU resources at any time s are represented by $c(s) = [c_1(s), \cdots, c_M(s)]^\top$, where $c_j(s)$ is the available resource at time s for GPU type j.

318 319 320 321 322 323 Dynamics. Since all the tasks arrive sequentially, and the task arrival follows a stochastic process, let us denote by $N(T)$ the total number of tasks arrived during time $[0, T]$, and for each task i, let s_i represents the arrival time. If there are sufficient non-occupied GPUs available, and we assign $z_i = j$ to task i, then a_{ij} number of correponding inventory will be temporary occupied, hence taken out from $c_j(s_i)$. Once a_{ij} of GPU j are assigned to x_j , the task will be running for $t_i = f(x_i, z_i)$ amount of time. If we denote by $A(s)$ the **active set** that contains all tasks that are still running at time s, then $i \in \mathcal{A}(s)$ for $s \in (s_i, s_i + t_i)$.

324 325 326 327 328 Waiting Queue. Let $Q(s)$ denote the set of waiting tasks at time s. If a task x_i cannot be immediately processed due to insufficient GPU resources, it is placed in the set $Q(s)$. If task x_i has been put in the queue, we denote by w_i the time it spent in the queue, which depends on factors including other tasks in the waiting queue, the current tasks that are active with their corresponding GPU allocations, and the decision-making model.

329 330 331 332 333 334 335 336 337 Decision-Making Model. We aim to find a decision-making policy π that takes 4 inputs: the current task feature x, the current time s, the current inventory level $c(s)$, and the historical information up to the current time \mathcal{H}_s . The policy can be deterministic or stochastic, and the range of the policy π is $\mathcal{Z} \cup \emptyset$. If $\pi(\mathbf{x}, s, \mathbf{c}(s), \mathcal{H}) \in \mathcal{Z}$, we assign the task GPU of type $\pi(\mathbf{x}, s, \mathbf{c}(s), \mathcal{H})$, and if $\pi(x, s, c(s), \mathcal{H}) = \emptyset$, we put this task in the waiting queue. We denote by Π the space of policies which satisfies the condition described above. Our goal is to solve the following objective function, which is a combination of the task completion time, the waiting time, and energy cost. (Notice that these times are directly affected by the policy π , and we denote by $S = \max_{i \in N(T)} \{t_i + w_i\}$ the time upon which all the tasks are finished.)

> N \sum (T)

> > $i=1$

 $(\alpha t_i + \beta w_i + \gamma e_i),$

 $a_{ij} \mathbb{I}(i \in \mathcal{A}(s) \text{ and } z_i = j) \leq c_j$, for all $s \in [0, S]$ and $j \in \mathcal{Z}$,

 $\min_{\pi \in \Pi}$

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s.t.

N \sum (T)

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344 345 346 347 348 349 350 351 352 353 354 355 356 357 $i=1$ where α , β , and γ are the weights assigned to execution time, waiting time, and energy cost. This formulation indeed resembles an online allocation problem with reusable resources, as discussed in [Chen et al.](#page-10-1) [\(2017\)](#page-10-1); [Zhang & Cheung](#page-13-2) [\(2022\)](#page-13-2). However, two key factors differentiate our work from existing studies in the literature: (i) Multi-purpose objective: while traditional allocation problems typically focus on optimizing a single reward or objective, our approach involves multiple goals. This multi-purpose objective requires balancing various criteria rather than focusing on a singular reward function, adding a layer of complexity not addressed in standard models of online allocation. (ii) Waiting queue: In our problem, there is a waiting queue of tasks that influences decision-making. The policy π must account for tasks already in the queue (as inferred from the history \mathcal{H}) in addition to handling new arrivals. This contrasts with standard resource allocation models, which usually make decisions based solely on newly arriving tasks, without needing to consider previously queued tasks. This interaction between the queue and decision-making introduces an additional layer of complexity. In summary, these challenges highlight that existing works can not provide (near) optimal solutions for our problem. This necessitates the development of algorithms to effectively address these complexities.

358 359 360 361 362 363 We note that for each task x_i , with the predictive model, the data center can incorporate the prediction results of time and energy, $\hat{t}_i := f_\theta(\bm{x}_i, z_i)$ and $\hat{e}_i := g_\theta(\bm{x}_i, z_i)$, into their decision-making process. This is because these information can be made available within 1 second after accessing the source code x_i , and does not rely on future information. Notice that this decision-making model is also applicable to other objectives, for example, water consumption and carbon emission, if corresponding data is provided by the data center.

364 365 366 367 368 We conducted our experiment in collaboration with a data center, collecting two months of operational data from 07/01/2024 to 09/01/2024. As shown in Figure [4](#page-7-0) (a), the task arrival times exhibit high non-stationarity. During this period, we recorded the characteristics of tasks, including execution time and energy consumption across different GPUs. This dataset enabled us to backtest our decision-making algorithms that rely on predictions from the LLM-based model.

369 370 371 372 373 374 375 376 377 We propose two algorithms: Greedy (Algorithm [1\)](#page-16-0), where we follow a first-come-first-served rule and the GPU type is selected greedily based on the smallest estimated objective value $\alpha \hat{t}_{ij} + \beta w_i + \gamma \hat{e}_{ij}$, and value-based (Algorithm [2\)](#page-16-1), which is inspired by the algorithm for the multiple knapsack problem [\(Kan et al., 1993\)](#page-11-5). We compare the performance of these algorithms against the current baseline allocation policy of the data center, with the results presented in Figure [4.](#page-7-0) Both algorithms outperform the baseline, with the Value-based algorithm achieving a 32% reduction in energy consumption and a 30% reduction in task waiting time. The Value-based method outperforms the Greedy method because it considers all tasks in the waiting queue, and accordingly assigns them based on their "values" of reducing the waiting time and energy cost, rather than following a simple first-come-first-serve rule as in the Greedy algorithm. These results are consistent can be found in Appendix [A.3.](#page-15-0)

with theoretical insights from [Spencer et al.](#page-12-10) [\(2014\)](#page-12-10); [Wagner et al.](#page-13-3) [\(2021\)](#page-13-3). More experimental details

Table 1: Performance gain for our algorithm implemented in data centers. Here, TWT stands for total waiting time, TDT stands for total delayed tasks, the tasks that have to wait, CRT stands for cumulative running time and TEC stands for the total energy cost.

400 401 402 403 Figure 4: (a) Task arrival pattern and (b), (c) performance comparison among the proposed predictive decisionmaking algorithms, Value-based and Greedy (see Appendix [A.3.1\)](#page-16-2), and the benchmark algorithm, Simple Rule. The Simple Rule assigns the available GPU type to the first task in the waiting queue, following a first-comefirst-serve policy when sufficient GPUs are available. If multiple GPU types are available, the most powerful one (e.g., A100) is selected.

3 OTHER EXTENSION

408 409 410 411 412 413 414 415 416 In this section, we discuss relevant extensions to our pipeline that align with data center practices. Our prototype is designed using a pre-trained LLM with strong capabilities in code comprehension and completion, coupled with a probe trained on 500 source codes. Although we are able to achieve good performance with a relatively small dataset of 500 source codes, this approach still risks poor out-of-sample performance. Due to variations in the coding practices of machine learning engineers—such as differences in variable names, function abstractions, and comments—the contextual information represented in the source code can vary significantly. Even if two codes are functionally equivalent, resulting in identical execution times and energy consumption, the representations generated by the LLM can be quite different.

417 418 419 420 421 This issue reflects an inconsistency problem. Formally, there may exist two tasks, x_1 and x_2 , such that the representations differ noticeably $(l_{\theta_1}(x_1) \neq l_{\theta_1}(x_2))$, but the execution times (and energy consumption) are identical: $h_{\theta_2}(l_{\theta_1}(\bm{x}_1), z) = h_{\theta_2}(l_{\theta_1}(\bm{x}_2), z)$. We adopt another LLM, referred to as the *Align-LLM*, to address this issue and mitigate potential out-of-distribution (OOD) estimation errors, which could otherwise degrade model performance.

422 423 424 425 As illustrated in Figure [5,](#page-8-3) while data centers can gradually accumulate a code base to improve prediction performance for both in-distribution and out-of-distribution tasks, we propose a novel algorithm that partially resolves the OOD issue, showcasing the flexibility and practicality of our pipeline. The architecture and experimental details can be found in appendix [A.2](#page-15-1)

426 427 428 429 430 431 The extended architecture first takes the source code as input and extracts representations using the pre-trained LLM. These representations are compared against representation clusters of the tasks from the local codebase to assess whether the current task's representation deviates significantly from those in the training set. If not, the task is passed to the probe for estimation. Otherwise, the Align-LLM assists by extracting key information from the source code, allowing the data center to identify similar code from its codebase. Next, Align-LLM rewrites the source code based on the style of the similar sample. The rewritten code, although functionally identical to the original, adopts

Figure 5: Architecture of the extended pipeline to resolve out-of-distribution tasks

a more familiar written style to the pre-trained LLM, aligning better with the LLM's representations in the training dataset, and enhancing the performance of the downstream probe.

 We highlight key insights from our experiments. First, by computing representation distances for the source code in the probe's training dataset, we observe that different task types tend to form distinct clusters (Figure (a)). Second, as shown in Figures 6 (b) and (c), when source code with the same functionality is rewritten by different users or engineers, its embedding diverges from the original cluster, leading to significantly reduced predictive accuracy due to the probe encountering out-of-distribution inputs. However, when we apply Align-LLM to rewrite the code while following the style of the original task, the resulting representation is closer to the original distribution (see indexes 4 vs. 5 and 6 vs. 7 in Figure [6](#page-9-3) (b)). Although the rewritten representation is not identical, possibly due to the Align-LLM's style differing slightly from human coding styles, the probe can predict the rewritten code more accurately thanks to the generalizability of our predictive model.

4 CONCLUSION

 We propose an LLM-based predictive scheduling system for data center operations aimed at enhancing the efficiency and sustainability of AI training. Our system leverages a pre-trained LLM specialized in code comprehension to extract representations of source code and utilizes sequential decision-making algorithms to optimize the scheduling of computational resources. Compared to traditional prediction methods, our architecture design and the use of LLMs offer significantly improved generalizability, flexibility, and practicality. Complemented by the decision-making scheduling algorithms, our approach achieves a 32% reduction in energy consumption and a 30% reduction in waiting times in real data centers. These results demonstrate the strong potential of our method in advancing AI infrastructure.

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 tasks training the Vit Model, while the remaining indexes correspond to tasks training the GAN Model. In Figure (b), indexes 0 and 1 represent Vit Model training tasks, indexes 2 and 4 represent out-of-distribution Vit Model tasks, and indexes 3 and 6 are LLM-rewritten versions of the task of index 2 and 4. Figures (c) and (d) compare the prediction performance of the execution time for the out-of-distribution tasks before(c) and after(d) the LLM rewrite.

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756 A APPENDIX

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A.1 DISCUSSION ON RELATED WORKS

760 761 762 763 764 765 766 767 768 769 770 771 Prediction based on device features. A body of literature focuses on predicting relevant metrics, such as execution time and energy consumption, using features that summarize the characteristics of the hardware. This approach assumes that analyzing hardware parameters and runtime data can uncover patterns that influence these metrics. For example, [Pham et al.](#page-11-6) [\(2017\)](#page-11-6) combine GPU runtime parameters with static hardware features, applying regression models to predict execution time. Similarly, [Daraghmeh et al.](#page-10-2) [\(2023\)](#page-10-2) and [Garg et al.](#page-10-3) [\(2023\)](#page-10-3) utilize various clustering techniques to identify operational patterns in machines based on hardware metrics, followed by sequence modeling for accurate predictions. Conversely, [Hilman et al.](#page-10-4) [\(2018\)](#page-10-4) take an alternative approach by first predicting hardware behavior during code execution and then employing the KNN clustering method to forecast execution time. In general, this stream of literature is not very related to our approach and we refer the readers to [O'Neal & Brisk](#page-11-7) [\(2018\)](#page-11-7); [Rodriguez et al.](#page-12-11) [\(2024\)](#page-12-11); [Ali et al.](#page-8-4) [\(2023\)](#page-8-4) for literature survey.

772 773 774 775 776 777 778 779 780 781 782 783 784 785 Prediction based on code features. Regarding code characteristics, early work by [Huang et al.](#page-11-8) [\(2010\)](#page-11-8) used feature engineering, extracting elements like loop counts and conditional branches, and applying sparse polynomial regression for time prediction. Recent approaches have shifted towards deep learning, where two main strategies dominate. One approach treats models as composed of atomic operations, with works like [Wang & Cao](#page-13-4) [\(2015\)](#page-13-4); [Cai et al.](#page-9-2) [\(2017\)](#page-9-2); [Geoffrey et al.](#page-10-5) [\(2021\)](#page-10-5); [Justus et al.](#page-11-4) [\(2018\)](#page-11-4) using program slicing and MLPs to predict time and energy by decomposing models into layers. The second approach leverages graph-based techniques, as in [Cao et al.](#page-9-4) [\(2021\)](#page-9-4) and [Bai et al.](#page-9-5) [\(2022\)](#page-9-5), which use graphs to represent layer dependencies and employ machine learning to learn these representations. Some methods are similar to ours in extracting code representations for prediction. For example, [Guerreiro et al.](#page-10-6) [\(2019\)](#page-10-6) transforms PTX instructions into embeddings for LSTM inputs, while [Zhou et al.](#page-13-5) [\(2019\)](#page-13-5) uses attention-based Bi-LSTMs and graph convolutional networks to automatically extract code semantics and structure. While these methods focus on extracting features, our model generalizes across a wider variety of task types and prediction metrics using a unified, high-level representation approach. See [Gianniti et al.](#page-10-7) [\(2018\)](#page-10-7); [Metz et al.](#page-11-9) [\(2022\)](#page-11-9); [Zhao et al.](#page-13-6) [\(2013\)](#page-13-6) for more related work.

786 787 788 789 790 791 792 793 794 795 796 797 798 799 800 Data center operations. Energy management in data centers has been a longstanding area of interest, with foundational work by [Pinheiro et al.](#page-12-12) [\(2001\)](#page-12-12); [Chase et al.](#page-9-6) [\(2001\)](#page-9-6); [Ranganathan et al.](#page-12-13) [\(2006\)](#page-12-13); [Fan et al.](#page-10-8) [\(2007\)](#page-10-8). As cloud computing and AI technologies emerged, software-based approaches have been developed to improve data center operations [\(Wu et al., 2016;](#page-13-7) [Evans & Gao, 2016;](#page-10-9) [Cortez](#page-10-10) [et al., 2017;](#page-10-10) [Katal et al., 2023\)](#page-11-10). In today's AI and sustainability-driven era, there has been grow-ing interest in carbon emissions related with AI [\(Lacoste et al., 2019;](#page-11-11) [Anderson et al., 2023;](#page-8-5) Güğül [et al., 2023;](#page-10-11) [Patel et al., 2024\)](#page-11-12). However, most efforts focus on software or infrastructure-level operations, whereas our approach specifically targets algorithmic-level improvements. While there is a substantial body of literature on optimal scheduling and queuing policies for service systems, much of this work is highly theoretical and relies on numerous assumptions [\(Vilaplana et al., 2014;](#page-12-14) [Xie](#page-13-8) [& Lu, 2015;](#page-13-8) [Jafarnejad Ghomi et al., 2019\)](#page-11-13). Additionally, many scheduling algorithms that avoid theoretical assumptions, such as reinforcement learning-based approaches [\(Ding et al., 2020;](#page-10-12) [Tuli](#page-12-15) [et al., 2020\)](#page-12-15), primarily focus on scheduling tasks but lack task-level predictive inference capabilities, which is a core strength of our method. Additionally, we note that our focus is specifically on the operations of data centers for AI-driven workloads, which exhibit distinct characteristics compared to traditional data center operations considered in previous studies.

801 802 803 804 805 806 807 808 809 Predictive decision-making Our work is also related to the area of decision-making with future predictions as side information. With such predictions, well-established decision algorithms, originally designed without the benefit of foresight, can be improved [\(Purohit et al., 2018\)](#page-12-16). Examples include problems such as caching [\(Lykouris & Vassilvitskii, 2021\)](#page-11-14), rent-or-buy (also known as the ski rental problem) [\(Gollapudi & Panigrahi, 2019\)](#page-10-13), frequency estimation [\(Hsu et al., 2019\)](#page-10-14), and queuing control [\(Spencer et al., 2014;](#page-12-10) [Xu & Chan, 2016\)](#page-13-9). Among these, the most closely related topic to our work is (online) resource allocation [\(Feldman et al., 2010;](#page-10-15) [Li & Ye, 2021;](#page-11-15) [Chen et al.,](#page-9-7) [2024;](#page-9-7) [Zhang & Cheung, 2022\)](#page-13-2). Specifically, [Lei & Jasin](#page-11-16) [\(2020\)](#page-11-16); [Chen et al.](#page-10-1) [\(2017\)](#page-10-1) examine online allocation with reusable resources (like GPUs in data centers), where each arriving request occupies resources for only a limited period before releasing them. [Thonglek et al.](#page-12-17) [\(2019\)](#page-12-17) and [Gadhavi &](#page-10-16)

810 811 812 [Bhavsar](#page-10-16) [\(2022\)](#page-10-16) focus on CPU and memory utilization, adopting LSTM and other time series models to optimize resource allocation.

- **813 814** A.2 EXPERIMENT: PREDICTIVE MODEL DETAILS
- **815 816** A.2.1 EXPERIMENT SETUP

Data Generation The training (and testing) data for the probes includes embedding features and corresponding label values.

- Embedding Features: The input features for the probe model are generated through Starcoder-7B(LLM). Specifically, we input 500 source code files as prompts into Starcoder-7B(LLM) and extract 4608-dimensional embedding vectors from each inference's penultimate layer, i.e., the output of the last transformer block. Following standard practices for sequence classification tasks, we then use the last token's embedding vector to represent the features of the entire code file. The 500 code files are either carefully selected or handcrafted to ensure that each file can run independently to complete a full computational process. These files cover a diverse set of tasks and structures, including ResNet, BERT, GAN, ViT, VGG, and more. The minimum, average, and maximum number of tokens in the code files are 1037, 1582.26, and 2151, respectively. And We ensure that the LLM's context length is sufficient to process the entire code file without truncation.
- Label Values: The label values, which the probes aim to predict, are generated by running the 500 code files on two different types of GPUs, NVIDIA A100 and NVIDIA A6000. We record the running time and energy consumption using the official tool nvidia-smi by NVIDIA. For each code running, we open an independent process running n vidia-smi $-$ query-gpu=power.draw to record the real-time power consumption with a logging interval of 1 second and compute the average power consumption. For each code file, we run experiments for at least twice and make sure the gap of recorded values is less than 10% of the average. We also make sure the gpus are exclusively used by our experiments.

839 840 841 842 Probe Architecture In our experiments, the probe model is a 3-layer dense neural network, utilizing ReLU as the activation function, with batch normalization applied to each layer. The input dimension of 4608 aligns with the dimensions of the (input) embedding vectors. The embedding dimensions for each layer are 1024, 30, and 1, respectively.

843 844 845 846 847 848 Probe Training We randomly separate the generated data into training data and testing data with a ratio of 9:1. All the data are further normalized by Standardscaler. The probe models are trained using the following configurations: a batch size of 8, 2000 training epochs, a learning rate of 1e-4, weight decay of 0.001 , and L1 regularization with penalty parameter being 1e-5. We use the Mean Squared Error (MSE) as the loss function and AdamW as the optimizer. Additionally, we apply early stopping when the epoch loss decreases by no more than 0.001 for 30 consecutive epochs.

850 851 852 853 Testing and Inference To test the time needed for prediction, in the testing phase we let the LLM Starcoder take the source code as input, outputting the presentation, and use the probe to predict the estimated value. The inference time for 48 source codes takes 32 seconds, averaging 0.65 seconds per task. The testing phase is carried out on 1 Nvidia RTX 6000 (Ampere Version) GPU.

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855 856 857 Predictive pipeline for OOD For the experiments in section [3,](#page-7-1) we take gpt-4o-2024-05-13 as the Align-LLM. With the Align-LLM, the rewrite time for the source code of 7 tasks takes 68 seconds, averaging 9.7 seconds per task.

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A.3 EXPERIMENT: DECISION-MAKING MODEL DETAILS

861 862 863 In this section, we first provide detailed predictive decision-making algorithms applied in [A.3.](#page-15-0) Further, due to data privacy restrictions imposed by the collaborating data center, we present additional numerical results across various settings using a simulation system. These results can offer managerial insights for the data center operator and validate our choice of multi-criteria optimization.

864 865 A.3.1 PREDICTIVE DECISION-MAKING ALGORITHMS

In this section, we provide detailed implementations of the two types of predictive decision-making algorithms used for GPU allocation.

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Algorithm 1 Predictive Decision-Making: Greedy

- **Require:** Current time s, GPU types Z , waiting queue $Q(s)$, active set $A(s)$, GPU occupation information a_{ij} 's, available GPUs $c(s)$, prediction models f_{θ} , g_{θ} , weights α , γ .
	- 1: Estimate the running time and the energy of each task $i \in A(s) \bigcup Q(s)$ for each GPU type $j \in \mathcal{Z}$:

$$
\hat{t}_{ij} = f_{\theta}(\boldsymbol{x}_i, j), \quad \hat{e}_{ij} = g_{\theta}(\boldsymbol{x}_i, j)
$$

%% First-come-first-served rule

2: Sort $Q(s)$ in ascending order by their arriving time s_i , and assign the first task (which first comes) to $z_1 = \arg \min_{j \in \mathcal{J}} \alpha \hat{t}_{1j} + \gamma \hat{e}_{1j}$ whenever z_1 has sufficient GPUs to satisfy task 1, i.e., at the time $\min\{s' \ge s | \mathbf{c}_{z_1}(s') \ge a_{1z_1}\}\$

Algorithm 2 Predictive Decision-Making: Value Based

- **Require:** Current time s, GPU types Z, waiting queue $Q(s)$, active set $A(s)$, GPU occupation information a_{ij} 's, available GPUs $c(s)$, prediction models f_{θ} , g_{θ} , hyperparameter κ .
	- 1: Estimate the running time and the energy of each task $i \in A(s) \bigcup Q(s)$ for each GPU type $j \in \mathcal{Z}$:

$$
\hat{t}_{ij} = f_{\theta}(\boldsymbol{x}_i, j), \quad \hat{e}_{ij} = g_{\theta}(\boldsymbol{x}_i, j)
$$

2: Compute the value v_{ij} for each task $i \in Q(s)$ and each GPU type $j \in \mathcal{Z}$:

$$
v_{ij} = \frac{1}{a_{ij}\hat{t}_{ij}} - \kappa \hat{e}_{ij}
$$

3: Construct the value set $\mathcal{V} = \{(i, j, v_{ij})\}$ and sort it in decending order by the cost value v_{ij} . 4: for $(i, j, v_{ij}) \in V$ do 5: if $a_{ij} \leq c_j(s)$ then %% If there are sufficient GPUs, assign i to j 6: Set $z_i = j$, and update V by removing the tuples $\{(i', j', v_{i'j'}) \in \mathcal{V} | i' = i, j' \in \mathcal{Z}\}\$ 7: Update the available GPUs $c_i(s) = c_i(s) - a_{ij}$ 8: else 9: Skip 10: end if 11: end for

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902 903 904 905 906 907 908 909 The Greedy algorithm focuses on a first-come-first-served approach to allocate tasks to GPUs. At each time step s, the algorithm estimates the running time and energy consumption for each task i on each GPU type j using the prediction models. Once these estimates are made, the waiting queue is sorted in ascending order of task arrival times. The algorithm assigns the first task in the queue to the GPU type selected based on the smallest estimated value of $\alpha t_{1j} + \gamma \hat{e}_{1j}$ reflecting a weighted combination of running time and energy consumption. This algorithm's simplicity makes it efficient for quick decision-making, but it may not always optimize resource allocation across the entire queue.

910 911 912 913 914 915 916 917 The Value-Based algorithm extends beyond the Greedy approach by considering all tasks in the waiting queue and selecting the GPU allocation based on a more strategic optimization. At each time step the algorithm first estimates the running time and energy consumption for each task across GPU types. However, the next step involves computing a cost value v_{ij} for each task-GPU pair, which is a combination of the inverse of the estimated running time t_{ij} adjusted by the GPU occupancy requirement a_{ij} and a penalty term $\kappa \hat{e}_{ij}$ representing the energy consumption. The algorithm then constructs a set of task-GPU pairs, sorting them in descending order based on the value v_{ij} . It allocates the GPUs to tasks based on this sorted list, prioritizing higher values, and updates the

available GPU resources accordingly. This method is inspired by the algorithms in multiple knap-

918 919 sack problems and balances multiple objectives, such as reducing energy consumption and running time with limited available GPUs.

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A.3.2 MORE SIMULATION EXPERIMENTS

923 924 925 926 927 928 Simulation Environment We built the simulation environment using data collected from the cooperating data center. Specifically, we first estimated a heterogeneous Poisson process to model task arrivals. And we build a task simulator which generates the running time t_{ij} and the energy consumption e_{ij} for each arrival task i across GPU type j. The values are randomly sampled from truncated normal distributions (truncated above 0), with the mean and variance estimated from the collected data. Further, we assume there are two types of GPUs ($|Z| = 2$) with the number of each type randomly sampled uniformly from the intervals [10, 20] and [20, 40], respectively.

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930 931 932 933 934 935 936 937 938 939 940 Performance under different criteria We evaluate the performance of the proposed Algorithm [2](#page-16-1) under different settings, with varying emphasis on the optimization criteria. Specifically, we tune the hyperparameter κ in Algorithm [2](#page-16-1) using independently sampled validation data, based on the following metrics: (i) waiting time only ($\alpha = \gamma = 0$ and $\beta = 1$) (ii) running time only ($\beta =$ $\gamma = 0$ and $\alpha = 1$), and (iii) energy only ($\alpha = \beta = 0$ and $\gamma = 1$). These settings prioritize different objectives, allowing us to compare the results and validate the effectiveness of the proposed Algorithm [2](#page-16-1) under various criteria. We compare the performance of Algorithm [2](#page-16-1) with a simple rule, which assigns the available GPU type to the first task in the waiting queue, following a first-comefirst-serve policy, provided there are sufficient GPUs. When multiple GPU types are available, the most powerful type (e.g., A100) is selected. The reported results are based on 100 testing samples and the validate data contains 50 samples.

941 942 943 944 945 946 947 948 Table [2](#page-17-0) summarizes the experimental results. First, it showcases that the proposed value-based rule can outperform the benchmark simple rule consistently in all tuning methods. In addition, it demonstrates that the performance of the value-based rule aligns with the specific objective being emphasized during tuning. Specifically, when tuned to minimize waiting time, it achieves the shortest waiting time (and the fewest tasks with positive wait times). Similarly, when tuned to minimize running time, it achieves the smallest running time. Finally, when tuned to minimize energy consumption, it achieves the lowest energy usage during testing. We also provide visualizations of sample path levels in Figure [7.](#page-18-0)

Table 2: Comparison of testing total waiting time, tasks with wait time, cumulative running time, and energy cost for the benchmark algorithm (simple rule) and value-based models tuned under different emphasized objectives.

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Simple Rule
Value-Based

Figure 7: Performance comparison across different metrics for the benchmark algorithm (simple rule) and value-based models tuned under different emphasized objectives.

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