

000 PREP: PRE-INFERENCE GUIDED TOKEN PRUNING 001 FOR EFFICIENT VISION-LANGUAGE MODELS 002

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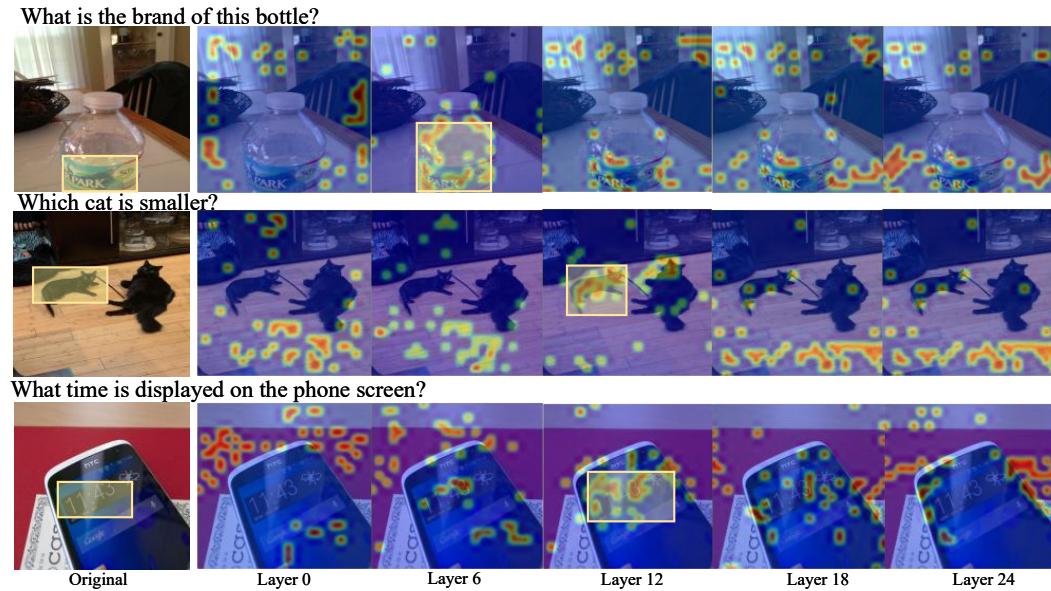
007 008 ABSTRACT 009

010 Recent Visual-Language Models (VLMs) have demonstrated strong fine-grained
011 perception capabilities across a wide range of Visual Question Answering (VQA)
012 tasks. However, this advantage comes at the cost of a rapidly increasing number
013 of visual tokens, leading to substantial computational and memory overhead.
014 Existing training-free methods adopt fixed-layer or layer-by-layer pruning, which
015 disrupts modality fusion before alignment and leads to significant performance
016 degradation under high pruning ratios. In this study, we observe that after the
017 early stage of modal fusion, cross-modal attention not only accurately identifies
018 regions of interest but also demonstrates less sensitive to pruning. Building on this,
019 we propose **PREP**, a training-free method that identifies optimal pruning layer via
020 patch-level pre-inference, thereby avoiding the loss of fine-grained details under
021 stepwise pruning. Specifically, PREP identifies the the layer with accurate cross-
022 modal alignment using an **Entropy-KL** divergence (EKL) score derived from the
023 Information Bottleneck principle, and then retains tokens at this layer that are criti-
024 cal for visual integrity and semantic alignment during full inference. Experiments
025 on LLaVA-1.5-7B show that with only **9** visual tokens and half of the layers used
026 in pre-inference, PREP preserves **96.2%** of the original performance while retain-
027 ing just **16** visual tokens (**3%**), leading to a **67%** reduction in KV-cache usage
028 and a **1.66 \times** acceleration in inference speed. We have presented our code in the
029 supplementary materials.

030 1 INTRODUCTION 031

032 Visual-Language Models (VLMs) have advanced rapidly in recent years (e.g., LLaVA-1.5 Liu et al.
033 (2023), InternVL3 Lu et al. (2025), GPT-4o Hurst et al. (2024)), pushing the frontier of multimodal
034 reasoning and fine-grained perception. For instance, LLaVA-1.5 encodes each image into a fixed
035 576 visual tokens, already far exceeding the number of textual tokens and straining LLM context
036 capacity. More recent models such as InternVL3 adopt substantially larger visual encoders, produc-
037 ing over 6000 tokens per image to capture fine-grained details. While such designs greatly enhance
038 perception, it also introduces substantial computational and memory overhead, thereby limiting the
039 scalability and real-time deployment of VLMs.

040 Existing token compression strategies fall into training and training-free methods. Training meth-
041 ods redesign the encoder or LLM architecture to inherently reduce visual token overhead. For ex-
042 ample, PDrop Xing et al. (2024) trains models to adapt to pruned token inputs by progressively
043 dropping tokens during training , while LLaVA-Mini Zhang et al. (2025b) introduces a lightweight
044 cross-attention module before LLM and reduce into one visual token. Although effective, these ap-
045 proaches require substantial retraining and often lack portability across different VLM backbones. In
046 contrast, training-free methods directly prune tokens at inference without retraining. Representative
047 approaches such as SparseVLM Zhang et al. (2024b), TopV Yang et al. (2025a), and Dymu Wang
048 et al. (2025) dynamically prune tokens layer by layer based on cross-modal attention, while oth-
049 ers like Minimonkey Huang et al. (2024) and VScan Zhang et al. (2025a) select a fixed layer to
050 prune. However, both of them fail to preserve performance under high visual token pruning ratios
051 (e.g., more than 90%), which we attribute to their neglect of the distinct functional roles of different
052 layers, causing them both to miss *when* textual and visual information become aligned and discard
053 local details during pruning. As shown in Fig. 1, in the early layers, LLaVA-1.5-7B remains in
the stage of visual–textual fusion, where similarity between prompt and image tokens is broadly



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lection. These methods aim to streamline visual processing while maintaining or enhancing model performance. However, they often require retraining for each specific model, leading to significant resource consumption and limiting their scalability in diverse applications.

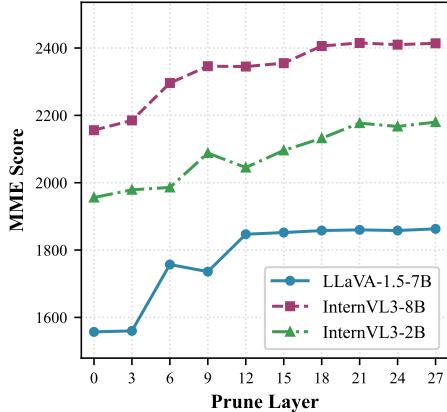


Figure 2: Performance on the MME Zhang et al. (2024a) when pruning 85% of tokens at different layers.

can Zhang et al. (2025a) prunes at the 16 layers. While these approaches avoid retraining, their layer-wise or fixed-layer compression fails to identify the modality-alignment layers, thereby discarding critical ROI regions and undermining fine-grained perception, ultimately leading to performance degradation.

3 METHOD

In this section, we introduce our token pruning framework for VLMs. We begin by analyzing cross-modal alignment from information bottleneck principle. Building on this insight, we present Entropy and KL-divergence based Layer score (EKL) for layer selection during pre-inference. Then, we introduce multi-modal token score for token pruning during full-inference. The overall framework is shown in Fig. 3.

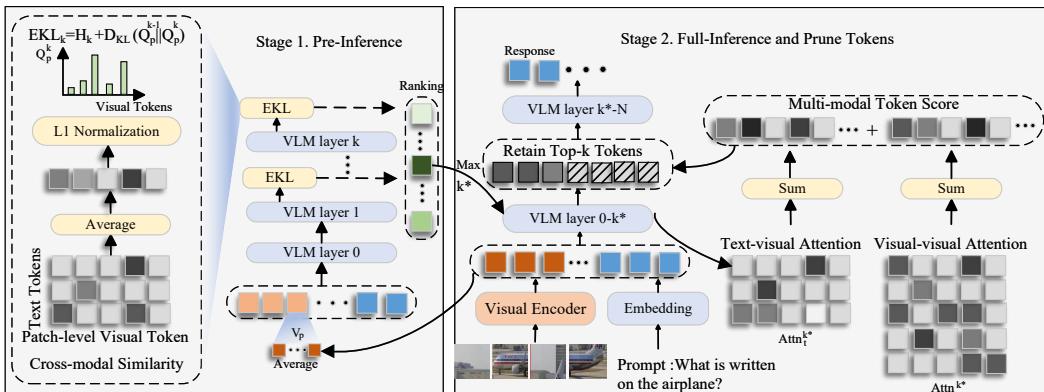


Figure 3: Overview of PREP framework. Stage 1: PREP identifies pruning-friendly layer with patch-level pre-inference tokens via EKL score. Stage 2: PREP combines visual-visual and text-visual attention to retain the most informative tokens.

3.1 PRELIMINARY ANALYSIS

VLMs generate textual responses conditioned on images and prompts. An image input $\mathbf{I} \in \mathbf{R}^{W \times H \times 3}$ is first encoded by a transformer-based visual encoder (e.g., ViT Dosovitskiy et al. (2020)) and then projected via an MLP to the required feature dimension D , yielding visual tokens $\mathbf{V} \in \mathbf{R}^{N \times D}$, where N is the number of tokens. Meanwhile, the text prompt is embedded through

162 the embedding layer as $\mathbf{T} \in \mathbf{R}^{M \times D}$, where M denotes the prompt length. Previous pruning meth-
 163 ods (Zhang et al., 2024b; Wang et al., 2025) typically compute cross-modal similarity between \mathbf{V}^k
 164 and \mathbf{T}^k or rely on attention scores \mathbf{Attn}^k from the k -th layer to determine the number of tokens to
 165 prune. However, they fail to identify the precise layer where cross-modal alignment emerges, lead-
 166 ing to the loss of fine-grained information. Specifically, as shown in Fig. 1, in some layers, the image
 167 tokens in the prompt-related regions exhibit high similarity, showing explicitly modal alignment.

168 Based on this observation, we first introduce \mathbf{Q}^k to reflect the alignment result between text and
 169 vision at the k -th layer, which can be computed as:
 170

$$171 \mathbf{Q}^k = \frac{\text{Mean}_j \left[\text{Softmax} \left(\frac{\mathbf{V}^k (\mathbf{T}^k)^\top}{\sqrt{D}} \right) \right]}{\sum_i \text{Mean}_j \left[\text{Softmax} \left(\frac{\mathbf{V}^k (\mathbf{T}^k)^\top}{\sqrt{D}} \right) \right]_i}, \quad \mathbf{Q}^k \in \mathbf{R}^N, \quad (1)$$

175 where $\text{Mean}_j[\cdot]$ denotes averaging over the text-token dimension j , and the summation index i
 176 corresponds to the visual dimension, corresponding to the average and L1 normalization in Fig. 3. In
 177 the encoding results of this layer, visual tokens with higher similarity to the prompt will have a higher
 178 \mathbf{Q}^k value, while it is ensured that \mathbf{Q}^k follows a probability distribution. Then, we introduce the target
 179 distribution Y as the underlying visual importance, corresponding to prompt-relevant regions.

180 To evaluate whether the visual tokens of the current layer are aligned with the prompt and faithfully
 181 reflect the relevant regions, \mathbf{Q}^k should simultaneously (i) preserve information about Y , ensuring
 182 faithful identification of semantically relevant tokens (higher $I(\mathbf{Q}^k; Y)$), and (ii) remain maximally
 183 compressed relative to the previous layer \mathbf{Q}^{k-1} (lower $I(\mathbf{Q}^k; \mathbf{Q}^{k-1})$), thereby discarding redundant
 184 information. This trade-off is consistent with the objective of the Information Bottleneck (IB) theory
 185 and can be expressed by the following objective:
 186

$$\mathcal{L}_{IB} = I(\mathbf{Q}^k; Y) - \beta I(\mathbf{Q}^k; \mathbf{Q}^{k-1}), \quad (2)$$

188 where $I(\cdot; \cdot)$ denotes mutual information and $\beta > 0$ is a balancing parameter. As mentioned above, a
 189 larger value of \mathcal{L}_{IB} indicates a higher cross-modal alignment quality for this layer. We then expand
 190 this target as:
 191

$$I(\mathbf{Q}^k; Y) - \beta I(\mathbf{Q}^k; \mathbf{Q}^{k-1}) = (1 - \beta)H(\mathbf{Q}^k) - H(\mathbf{Q}^k | Y) + \beta H(\mathbf{Q}^k | \mathbf{Q}^{k-1}), \quad (3)$$

193 where $H(\cdot)$ denotes entropy and $H(\cdot | \cdot)$ conditional entropy. However, directly computing the
 194 conditional entropy in Eq. 3 is intractable: the ground-truth target distribution Y is inaccessible during
 195 inference, and the visual attention distribution from \mathbf{Q}^{k-1} to \mathbf{Q}^k involves complex transformer
 196 internal computations. To resolve this, we next propose a feasible approximation to the IB objective
 197 using Entropy and KL-divergence (EKL) score.
 198

199 3.2 ENTROPY AND KL-DIVERGENCE SCORE(EKL)

200 As mentioned above, $H(\mathbf{Q}^k | Y)$ quantifies the uncertainty of \mathbf{Q}^k when the underlying visual im-
 201 portance Y is known. Intuitively, if \mathbf{Q}^k deviates significantly from Y (e.g., the attention of model
 202 focuses on non-ROI regions), the uncertainty of \mathbf{Q}^k cannot be effectively reduced even with prior
 203 knowledge of Y —this implies a larger $H(\mathbf{Q}^k | Y)$. In addition, according to our previous obser-
 204 vations, obvious modal-alignment appears after early modal-fusion layers, indicating a small and
 205 approximately constant $H(\mathbf{Q}^k | Y)$ for the middle layers. To identify this range, we calculate,
 206 for each layer of LLaVA-1.5-7B, the **ratio** of the intersection area between the top 75% attention-
 207 weighted areas predicted by \mathbf{Q}^k and the ROI to the area of the ROI, which is termed as intersection
 208 over ROI (IoR) and described in detail in Fig. 4.

209 If the conditional entropy $H(\mathbf{Q}^k | Y)$ is small, this means that most of the regions attended to
 210 by \mathbf{Q}^k can be predicted when Y is known; in this case, the intersection between these predicted
 211 regions and the ROI will be larger, corresponding to a higher IoR. In Fig. 4, the IoR values remain
 212 consistently high with minimal fluctuations across layers 6–15. This stable alignment between \mathbf{Q}^k
 213 and Y implies that the conditional entropy $H(\mathbf{Q}^k | Y)$ remains relatively constant. In Appendix A.1,
 214 we observe a similar prunable range in both InternVL and QwenVL. This phenomenon may arise
 215 from the fact that current VLMs are pre-trained primarily using the next-token prediction objective
 and share largely unified LLM-style architectures, which in turn leads to similar layer-wise attention

patterns. Similar to the patterns observed in Fig. 1, the shallower layers primarily facilitate cross-modal fusion, whereas the deeper layers progressively transition toward task-specific reasoning. Consequently, the degree of alignment between \mathbf{Q}^k and Y exhibits substantially larger fluctuations in these regions, suggesting that the conditional entropy $H(\mathbf{Q}^k | Y)$ cannot be approximated as invariant across these layers.

Similarly, for the second term in Eq. 2, we approximate $H(\mathbf{Q}^k | \mathbf{Q}^{k-1})$ by measuring the divergence between the attention distributions of consecutive layers. Intuitively, if \mathbf{Q}^k carries little new information beyond \mathbf{Q}^{k-1} , the two distributions will be highly similar, resulting in a small conditional entropy. Conversely, a large divergence indicates that \mathbf{Q}^k introduces substantial novel information relative to \mathbf{Q}^{k-1} . Following this intuition, we compute the KL divergence $D_{\text{KL}}(\mathbf{Q}^k \| \mathbf{Q}^{k-1})$ at each layer as a practical surrogate for $H(\mathbf{Q}^k | \mathbf{Q}^{k-1})$. Accordingly, we define the EKL score for layer k :

$$\text{EKL}_k = \mathcal{H}(\mathbf{Q}^k) + D_{\text{KL}}(\mathbf{Q}^k \| \mathbf{Q}^{k-1}). \quad (4)$$

We also provide a detailed proof using information-theoretical bounds in Appendix A.2, proving that EKL can be used as a computable lower bound for \mathcal{L}_{IB} . Based on the above analysis, for the selected layers where $H(\mathbf{Q}^k | Y)$ remains approximately constant, a larger EKL_k implies that the value of the remaining term in Eq. 3 is larger, which in turn indicates a higher degree of cross-modal alignment for this layer.

However, directly computing the EKL score at the token level during pre-inference would be computationally intensive. For efficiency, we partition \mathbf{V} into r groups $\mathbf{V}_r \in \mathbf{R}^{r \times L \times D}$ and average over the first dimension (r) to obtain patch-level tokens \mathbf{V}_p :

$$\mathbf{V}_p = \frac{1}{L} \sum_{k=1}^L \mathbf{V}_r[:, k, :], \quad \mathbf{V}_p \in \mathbf{R}^{r \times D}, \quad (5)$$

where the averaging operation aggregates pixel-level features within each patch to preserve patch-wise semantics.

To validate its feasibility for pre-inference, we obtain the IoR of patch-level distributions \mathbf{Q}_p^k with the same setting as token-level IoR. As illustrated in Fig. 4, the high-attention regions remain well aligned across both representations in the middle layers.

These findings suggest that patch-level encoding faithfully preserves the critical semantics captured by token-level encoding, thereby enabling reliable pre-inference with reduced redundancy.

As shown in Fig. 3, PREP computes and ranks EKL_k of each layer, selecting k^* with the highest EKL to be pruned during full-inference.

3.3 MULTIMODAL TOKEN SCORE

During inference, we determine which visual tokens to prune by computing a layer-wise, token-level importance score at the EKL-selected layer k^* . This score fuses two complementary attention signals: intra-visual structural relevance (*visual-to-visual*, v2v) and cross-modal semantic alignment (*visual-to-text*, v2t). By combining them, we ensure that tokens critical to either visual structure or semantic information are preserved. As shown in

Figure 4: IoR means the intersection area between the top 75% attention-weighted areas predicted by \mathbf{Q}^k and the ROI over the area of the ROI on VizWiz Chen et al. (2022).

Fig. 3, we first extract the raw multi-head attention tensor from layer k^* :

$$\mathbf{Attn}^{k^*} \in \mathbf{R}^{H \times (S+N+M) \times (S+N+M)}, \quad (6)$$

where H is the number of attention heads, S is the length of system prompts, N is the number of encoded visual tokens, and M is the number of text tokens. To reduce head-wise redundancy and emphasize the aggregated attention patterns, we average over all heads:

$$\overline{\mathbf{Attn}}^{k^*} = \frac{1}{H} \sum_{h=1}^H \mathbf{Attn}^{k^*}[h, :, :] \in \mathbf{R}^{(S+N+M) \times (S+N+M)}. \quad (7)$$

270 We then extract the submatrices corresponding to visual-visual and visual-text attention:
 271

$$272 \quad \mathbf{Attn}_v^{k^*} = \overline{\mathbf{Attn}}^{k^*}[S : S + N, S : S + N], \quad \mathbf{Attn}_t^{k^*} = \overline{\mathbf{Attn}}^{k^*}[S : S + N, S + N :], \quad (8)$$

274 where $\mathbf{Attn}_v^{k^*} \in \mathbb{R}^{N \times N}$ captures intra-visual structural interactions and $\mathbf{Attn}_t^{k^*} \in \mathbb{R}^{N \times M}$ captures
 275 visual-text semantic alignment. Then we average on the col-dimension to obtain two kinds of
 276 visual importance:

$$277 \quad s_v[i] = \frac{1}{N} \sum_{j=1}^N \mathbf{Attn}_v^{k^*}[i, j], \quad s_t[i] = \frac{1}{M} \sum_{j=1}^M \mathbf{Attn}_t^{k^*}[i, j]. \quad (9)$$

281 Finally, we define the Multi-modal token score as the sum of visual and semantic contributions:
 282

$$283 \quad \text{Score}[i] = s_v[i] + s_t[i], \quad \text{Score} \in \mathbf{R}^N. \quad (10)$$

285 Higher multi-modal score indicates that the i -th visual token is important for maintaining both visual
 286 structural integrity and cross-modal semantic alignment. During pruning, we retain the top- $m\%$ of
 287 visual tokens with the highest multi-modal token scores, ensuring that the most informative tokens
 288 are preserved.

290 3.4 THEORETICAL ANALYSIS OF REDUCED FLOPs

292 Following the PDrop Xing et al. (2024) approximation, the FLOPs of a single transformer layer with
 293 visual sequence length N and dimension D is

$$294 \quad \text{FLOPs}_{\text{layer}}(N) \approx 4ND^2 + 2N^2D + 3NDC, \quad (11)$$

296 where C is the intermediate size of the feed-forward network. As we prune at layer k^* by retaining
 297 $m\%$ of the visual tokens and introduces overhead of EKL and multi-modal score, the total theoretical
 298 FLOPs reduction simplifies to, where the detail of derivation is shown in Appendix A.3:

$$299 \quad \text{Reduced FLOPs} = \sum_{k=k^*}^K \left[300 \quad 4ND^2 + 2N^2D + 3NDC \right. \\ 301 \quad \left. - \left(4m \cdot ND^2 + 2(m \cdot N)^2D + 3m \cdot NDC \right) \right] \\ 302 \quad - \left[k^* \cdot (4rD^2 + 2r^2D + 3rDC) + N + HN^2 + HNM \right]. \quad (12)$$

306 Experiments show that the introduced overhead is only 0.02 TFLOPs, accounting for merely 0.4%
 307 of the original total FLOPs.
 308

309 4 EXPERIMENT

312 4.1 EXPERIMENT SETTING

314 To assess the effectiveness of our method on image understanding tasks, we conduct experiments
 315 on four fine-grained benchmarks including MMStar Chen et al. (2024b), TextVQA Singh et al.
 316 (2019), AI2D Kembhavi et al. (2016) and Seed2-Plus Li et al. (2024), and four widely used VQA
 317 benchmarks including POPE Li et al. (2023), RealWorldQA x.ai. (2024), MME and VizWiz. At
 318 the same time, we compare PREP with recent state-of-the-art methods as SparseVLM, ToMe Bolya
 319 et al. (2022), TopV Yang et al. (2025a), FastV Chen et al. (2024a), PDrop and Minimonkey Huang
 320 et al. (2024). We verify the generalizability of PREP on InternVL3, LLaVA-1.5 and Qwen2.5-VL
 321 series VLMs, pruning between 6-15 layers of them. Besides, as LLaVA-1.5 generate fixed-size 576
 322 visual tokens, we select group size from 32, 64, 144 and 192. As InternVL3 and Qwen2.5-VL set a
 323 fixed-size patch sequence length, we group visual tokens according their original size. LLaVA-1.5
 employs CLIP-pretrained ViT-L as the visual tower, while InternVL3 owns dynamic high resolution
 encoder. All experiments are done on one NVIDIA RTX3090 with 24GB.

324
 325 Table 1: Evaluation of our method on the LLaVA-1.5-7B model across nine datasets under three
 326 visual token compression levels (192, 128, and 64). The vanilla configuration uses 576 tokens and
 327 average 4.8T FLOPs. FLOPs ratio shows the ratio of pruned FLOPs to original FLOPs. Relative
 328 score is the average ratio between the score and original score across all benchmarks. Latency is
 329 measured in seconds per iteration.

Method	Venue	MMB	MME	POPE	VizWiz	TextVQA	RWQA	AI2D	MMStar	Seed2	Relative Score(%)	FLOPs Ratio(%)	Latency (s/it)
Original	-	64.8	1864	86.1	50.0	58.2	49.0	52.0	32.9	38.8	100.0%	100%	0.48
Retain Tokens 192													
ToMe	ICLR'23	60.5	1563	72.4	50.8	53.1	47.5	50.0	30.3	36.1	92.5% (↓7.5%)	44%	0.41
FastV	ECCV'24	61.0	1605	64.8	50.9	52.1	47.9	50.5	30.5	36.5	92.1% (↓7.9%)	46%	0.40
SparseVLM	ICML'25	62.5	1787	85.1	50.5	57.8	48.2	51.5	31.7	38.3	98.2% (↓1.8%)	52%	0.45
PDrop	CVPR'25	63.3	1797	82.3	51.1	56.5	48.4	51.3	31.8	37.8	97.7% (↓2.3%)	44%	0.42
PREP	-	64.8	1867	85.3	52.0	58.0	48.8	51.9	32.8	38.9	100.2% (↑0.2%)	46%	0.39
Retain Tokens 128													
ToMe	ICLR'23	53.3	1343	62.8	50.6	49.1	44.9	48.0	28.7	34.2	85.8% (↓14.2%)	37%	0.37
FastV	ECCV'24	56.1	1490	53.4	51.3	50.5	45.3	49.0	29.3	35.7	87.3% (↓12.7%)	39%	0.39
SparseVLM	ICML'25	60.0	1746	85.0	51.4	56.7	45.5	51.0	31.5	38.0	96.6% (↓3.4%)	36%	0.42
PDrop	CVPR'25	61.6	1761	82.3	51.0	56.6	46.2	51.2	32.1	37.9	96.5% (↓3.5%)	35%	0.38
PREP	-	64.2	1845	84.9	51.6	57.5	47.5	51.4	32.4	38.6	99.1% (↓0.9%)	38%	0.35
Retain Tokens 64													
ToMe	ICLR'23	43.7	1138	52.5	50.4	45.3	43.8	45.1	25.9	32.2	78.4% (↓21.6%)	26%	0.33
FastV	ECCV'24	47.2	1255	38.2	51.8	47.8	42.2	46.3	26.7	33.1	79.1% (↓20.9%)	28%	0.34
SparseVLM	ICML'25	56.2	1589	77.5	50.1	53.4	46.2	50.3	30.5	37.5	92.7% (↓7.3%)	30%	0.37
PDrop	CVPR'25	58.8	1561	55.9	50.7	50.6	45.4	50.5	31.3	37.3	89.7% (↓10.3%)	26%	0.35
PREP	-	63.7	1827	84.0	51.9	56.5	46.9	50.9	31.9	38.3	98.3% (↓1.7%)	29%	0.32
Retain Tokens 16													
PREP	-	63.3	1812	82.1	50.2	53.9	45.6	50.4	31.6	37.6	96.2% (↓3.8%)	27%	0.29

345 Table 2: Performance comparison with TopV and Minimonkey on InternVL3 and Qwen2.5-VL
 346 VLMs. Latency is measured in seconds per iteration.

Model	Method (Retained Ratio)	Venue	MMB	MME	POPE	TextVQA	OCRB	AI2D	MMStar	Seed2	FLOPs Ratio(%)	Latency (s/it)
	original(100%)	-	83.4	2415	91.1	81.8	880	69.7	85.2	68.2	100%	0.94
	TopV(50%)	CVPR'25	82.9	2407	89.6	80.4	825	66.6	84.5	67.2	62%	0.87
	Minimonkey(50%)	ICLR'25	81.7	2388	89.8	81.2	846	67.1	84.7	66.9	65%	0.89
InternVL3-8B	PREP(50%)	-	83.5	2416	90.2	81.6	864	67.8	85.2	67.8	57%	0.84
	TopV(25%)	CVPR'25	82.1	2298	88.2	78.6	783	62.4	83.1	65.3	46%	0.59
	Minimonkey(25%)	ICLR'25	81.5	2368	89.6	78.7	806	63.7	84.5	67.2	48%	0.63
	PREP(25%)	-	83.1	2385	89.8	79.3	816	64.1	84.8	67.4	39%	0.52
	original(100%)	-	83.5	2305	86.2	84.9	864	81.1	63.9	70.4	100%	1.12
	TopV(50%)	CVPR'25	79.8	2173	82.4	81.4	743	76.2	61.6	64.2	64%	0.83
	Minimonkey(50%)	ICLR'25	80.6	2132	81.1	80.6	764	74.3	60.2	61.5	65%	0.79
Qwen2.5VL-7B	PREP(50%)	-	81.7	2216	84.9	82.5	807	78.7	62.8	66.4	62%	0.72
	TopV(25%)	CVPR'25	78.1	1973	78.1	77.3	711	71.6	58.3	62.7	43%	0.68
	Minimonkey(25%)	ICLR'25	77.6	2034	79.3	76.5	737	72.3	57.1	60.3	46%	0.71
	PREP(25%)	-	80.7	2157	82.6	80.4	792	77.5	60.3	63.5	40%	0.63

4.2 MAIN RESULTS

360 Table 1 reports the performance of PREP on LLaVA-1.5-7B. We evaluate three target token budgets
 361 (192, 128, and 64) to assess compression under different levels of pruning. For the balance, we
 362 set similar computational overhead(TFLOPs) and compare both performance and latency. When
 363 reducing from 576 to 192 tokens, PREP even improves 0.2% on average accuracy, substantially
 364 lower than the drop of SparseVLM(1.8%) and PDrop (2.3%). At more aggressive pruning (16
 365 tokens), PREP the drops only 3.8%, while other methods like FastV and ToMe retain 64 tokens and
 366 even drop more than 20%. Furthermore, we extend our approach to the advanced InternVL3 models
 367 in Table 2: when retaining only 25% of visual tokens with an average 1500 tokens per sample
 368 (far more than in LLaVA-1.5), PREP still keeps the average accuracy loss below 10%. Compared to
 369 TopV and Minimonkey on InternVL and Qwen2.5-VL, our method still achieves higher performance
 370 under the same token budget, highlighting the generalization and effectiveness of our approach. In
 371 addition, PREP achieves the lowest latency across all baselines, showing negligible pre-inference
 372 overhead and higher efficiency. Comparasion on different scales of VLMs are in Appendix A.4.

373 Table 3: Ablation study of EKL components
 374 under 64 tokens retained.

Component	MMB	MME	MMBench	MMStar
Entropy	1816	63.2	31.5	
KL	1809	62.9	31.2	
EKL	1827	63.7	31.9	

375 Table 4: Ablation study of the k -th EKL score under
 376 64 tokens retained from layer 10 to 15.

k -th score	1	2	3	4	5	6
MME	1768	1801	1805	1804	1819	1845
TextVQA	55.1	55.4	56.2	55.7	56.1	57.1
POPE	81.0	81.7	81.8	82.5	82.9	84.5

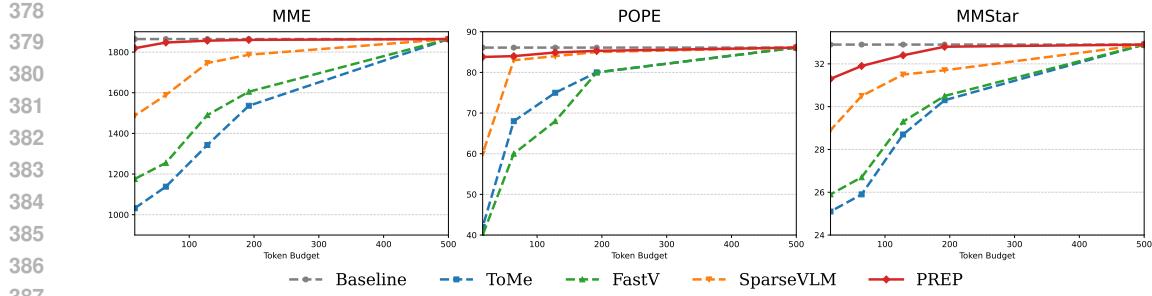


Figure 5: Performance comparison with other baselines under different tokens. The horizontal axis represents the remaining tokens to 576, 192, 128, 64 and 16, while the vertical axis means the scores.

Table 5: Counts of selected layers on MME, MMBench and SEED2.

Layer	6-8	8-10	10-12	12-14
MME	680	828	205	651
MMBench	2246	1230	1350	1864
SEED2-PLUS	780	501	820	176

Table 6: Impact of group size on performance across benchmarks.

Group size	32	64	144	192
MME	1804	1827	1806	1793
MMBench	64.2	64.5	63.7	63.2
SEED2-PLUS	31.6	31.9	31.3	31.1

Fig. 5 visualizes the performance degradation of our method compared with ToMe, FastV, and SparseVLM on POPE, MME, and MMStar under different numbers of retained visual tokens. It can be observed that even when the number of tokens is reduced to 16, our method is hardly affected by the reduction in the number of tokens on MME and POPE. Furthermore, on the MMStar dataset—which requires fine-grained perception—the magnitude of performance degradation of our method is significantly smaller than that of the other methods. We attribute this to the fact that EKL effectively identifies the layers where information fusion takes place. Combined with multi-modal token scores, PREP prevents the loss of details. These results demonstrate both the effectiveness and strong generalization of our approach.

4.3 ABLATION STUDY

EKL Table 3 compares three variants of our layer scoring: using only KL divergence, only entropy, or their combination. The results show that integrating both yields the best performance, confirming the complementarity of the two terms. Table 4 further examines the effect of selecting the k -th highest scoring layer, where performance consistently declines as k decreases, demonstrating that EKL effectively ranks layer importance.

Table 5 shows that the majority of pruning occurs within layers 6–10, indicating that EKL is able to identify the onset of cross-modal fusion at an early stage rather than simply selecting deeper layers. This property substantially enhances the efficiency of the model.

Table 7: Performance of different variants on four benchmarks.

	POPE	MME	TextVQA	Seed2
v2t	83.7	1806.3	56.1	38.0
v2v	83.5	1815.4	55.8	37.8
ours	84.0	1827.2	56.5	38.3

Finally, in Table 6, we investigate the impact of the number of tokens per group used in average pooling. We observe that grouping 64 tokens achieves the best performance: it preserves fine details that support reasoning while maintaining low inference overhead.

Multi-modal token score. Table 7 reports an ablation of multi-modal token score comparing three variants: **v2t** (using only visual-to-text attention), **v2v** (using only visual-to-visual attention), and **ours** (the full multi-modal token score that fuses v2v and v2t). Combining both signals (ours) yields the best result on all four benchmarks. For example, POPE accuracy increases from 83.9% (v2t) and 83.5% (v2v) to 84.0% (ours), and the MME score rises from 1842.3 / 1827.4 to 1856.2. Small but consistent improvements are also observed on TextVQA and Seed2-PLUS. These results show that intra-visual structure and cross-modal alignment provide complementary information for token selection, and their fusion produces more robust pruning decisions.

432 4.4 EFFICIENCY ANALYSIS
433

434 In Table 8, we evaluate the practical efficiency of our method on a single NVIDIA RTX 3090
435 (24GB) using full benchmarks. As our method progressively compresses visual tokens, both lat-
436 ency and KV cache usage are significantly reduced. For instance, decreasing the retained token
437 count from 576 to 192 reduces latency from 0.48 s to 0.39 s, yielding a $1.23\times$ speedup, while
438 KV cache occupancy drops nearly by half (from 100% to 56%). Further compression to 128 to-
439 kens decreases latency to 0.35 s ($1.37\times$ speedup) and KV cache usage to 44%, with minimal
440 impact on the average performance across benchmarks (99.3%). Retaining only 64 tokens ac-
441 celerates inference to 0.32 s ($1.50\times$ speedup) and reduces KV cache to 39%, whereas a further
442 reduction to 16 tokens achieves the highest speedup of $1.66\times$, with KV cache occupancy lowered to 33%,
443 albeit with a modest decrease in average performance (96.2%). These results demon-
444 strate that our method effectively balances computational efficiency and model accuracy, substan-
445 tially reducing memory and runtime demands while maintaining high performance on average across multiple benchmarks.

446 Table 8: Performance, latency, and KV cache usage com-
447 parison under different visual token configurations.

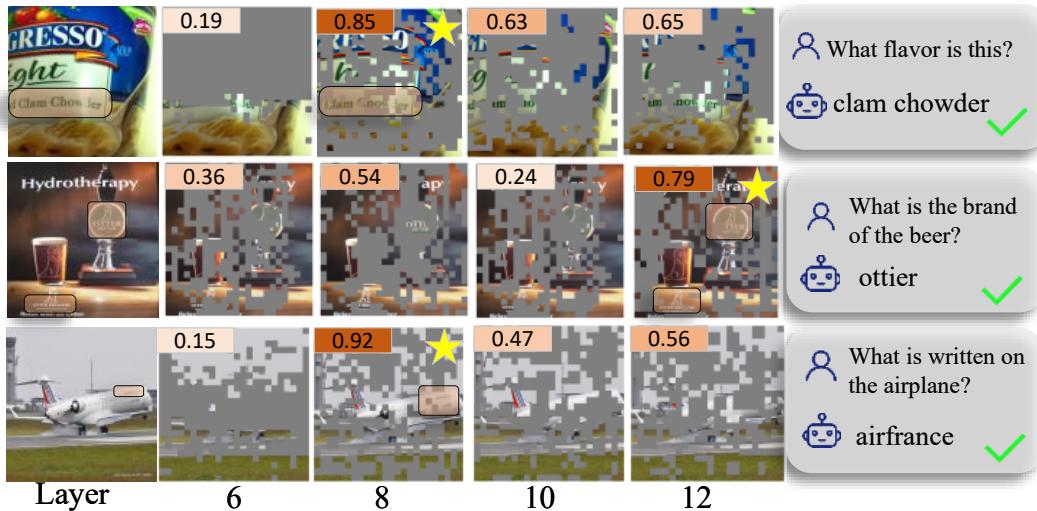
Retain tokens	576	192	128	64	16
Performance (%)	100	100	99.3	98.3	96.2
KV Cache (%)	100	56	44	39	33
Latency (s)	0.48	0.39	0.35	0.32	0.29
Speedup (\times)	1.00	1.23	1.37	1.50	1.66

448 449

450 demands while maintaining high performance on average across multiple benchmarks.

451 4.5 CASE STUDY
452

453 As shown in Fig. 6, our method first identifies the cross-modal alignment layer via pre-inference in
454 Stage 1, and then prunes tokens at that layer based on multi-modal token scores. The visualization
455 highlights that our approach preserves tokens essential for answering, focusing on regions of interest.

473 Figure 6: Visualization of our method. EKL scores are on the upper left and figures with star are the
474 pruned layers. Orange boxes indicate regions of interest.
475

476 5 CONCLUSION

477 In this work, we introduced **PREP**, a training-free pruning framework for efficient inference in
478 Visual-Language Models. By leveraging pooled patch-level tokens for pre-inference, PREP iden-
479 tifies pruning layers guided by the Information Bottleneck criterion, thereby avoiding the loss of
480 fine-grained information that commonly arises in stepwise pruning. At the selected layer, PREP re-
481 tains tokens based on multimodal importance scores, ensuring both structural integrity and semantic
482 alignment are preserved. Extensive experiments across nine VQA benchmarks demonstrate that
483 PREP achieves substantial efficiency gains—reducing visual tokens by up to **97%**, KV-cache usage
484 by **67%**, and inference time by **1.66 \times** —while maintaining over **96%** of the original model perfor-
485 mance. These results highlight the effectiveness of pre-inference guided pruning for high-resolution
VLMs, offering a general and scalable solution toward more efficient multimodal reasoning.

486 REFERENCES
487

488 Kazi Hasan Ibn Arif, Jin Yi Yoon, Dimitrios S Nikolopoulos, Hans Vandierendonck, Deepu John, and
489 Bo Ji. Hired: Attention-guided token dropping for efficient inference of high-resolution vision-
490 language models. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 39,
491 pp. 1773–1781, 2025.

492 Daniel Bolya, Cheng-Yang Fu, Xiaoliang Dai, Peizhao Zhang, Christoph Feichtenhofer, and Judy
493 Hoffman. Token merging: Your vit but faster. *arXiv preprint arXiv:2210.09461*, 2022.

494 Chongyan Chen, Samreen Anjum, and Danna Gurari. Grounding answers for visual questions asked
495 by visually impaired people. In *Proceedings of the IEEE/CVF Conference on Computer Vision
496 and Pattern Recognition*, pp. 19098–19107, 2022.

497 Liang Chen, Haozhe Zhao, Tianyu Liu, Shuai Bai, Junyang Lin, Chang Zhou, and Baobao Chang.
498 An image is worth 1/2 tokens after layer 2: Plug-and-play inference acceleration for large vision-
499 language models. In *European Conference on Computer Vision*, pp. 19–35. Springer, 2024a.

500 Lin Chen, Jinsong Li, Xiaoyi Dong, Pan Zhang, Yuhang Zang, Zehui Chen, Haodong Duan, Jiaqi
501 Wang, Yu Qiao, Dahua Lin, et al. Are we on the right way for evaluating large vision-language
502 models? *arXiv preprint arXiv:2403.20330*, 2024b.

503 Alexey Dosovitskiy, Lucas Beyer, Alexander Kolesnikov, Dirk Weissenborn, Xiaohua Zhai, Thomas
504 Unterthiner, Mostafa Dehghani, Matthias Minderer, Georg Heigold, Sylvain Gelly, et al. An
505 image is worth 16x16 words: Transformers for image recognition at scale. *arXiv preprint
506 arXiv:2010.11929*, 2020.

507 Mingxin Huang, Yuliang Liu, Dingkang Liang, Lianwen Jin, and Xiang Bai. Mini-monkey: Multi-
508 scale adaptive cropping for multimodal large language models. *CoRR*, 2024.

509 Aaron Hurst, Adam Lerer, Adam P Goucher, Adam Perelman, Aditya Ramesh, Aidan Clark, AJ Os-
510 trow, Akila Welihinda, Alan Hayes, Alec Radford, et al. Gpt-4o system card. *arXiv preprint
511 arXiv:2410.21276*, 2024.

512 Aniruddha Kembhavi, Mike Salvato, Eric Kolve, Minjoon Seo, Hannaneh Hajishirzi, and Ali
513 Farhadi. A diagram is worth a dozen images. In *Computer Vision–ECCV 2016: 14th Euro-
514 pean Conference, Amsterdam, The Netherlands, October 11–14, 2016, Proceedings, Part IV 14*,
515 pp. 235–251. Springer, 2016.

516 Bohao Li, Yuying Ge, Yi Chen, Yixiao Ge, Ruimao Zhang, and Ying Shan. Seed-bench-2-plus:
517 Benchmarking multimodal large language models with text-rich visual comprehension. *arXiv
518 preprint arXiv:2404.16790*, 2024.

519 Yifan Li, Yifan Du, Kun Zhou, Jinpeng Wang, Wayne Xin Zhao, and Ji-Rong Wen. Evaluating
520 object hallucination in large vision-language models. *arXiv preprint arXiv:2305.10355*, 2023.

521 Haotian Liu, Chunyuan Li, Qingyang Wu, and Yong Jae Lee. Visual instruction tuning. *Advances
522 in neural information processing systems*, 36:34892–34916, 2023.

523 Dongchen Lu, Yuyao Sun, Zilu Zhang, Leping Huang, Jianliang Zeng, Mao Shu, and Huo Cao.
524 Internvl-x: Advancing and accelerating internvl series with efficient visual token compression.
525 *arXiv preprint arXiv:2503.21307*, 2025.

526 Run Luo, Renke Shan, Longze Chen, Ziqiang Liu, Lu Wang, Min Yang, and Xiaobo Xia. Vcm:
527 Vision concept modeling based on implicit contrastive learning with vision-language instruction
528 fine-tuning. *arXiv preprint arXiv:2504.19627*, 2025.

529 Amanpreet Singh, Vivek Natarajan, Meet Shah, Yu Jiang, Xinlei Chen, Dhruv Batra, Devi Parikh,
530 and Marcus Rohrbach. Towards vqa models that can read. In *Proceedings of the IEEE/CVF
531 conference on computer vision and pattern recognition*, pp. 8317–8326, 2019.

532 Zhenhailong Wang, Senthil Purushwalkam, Caiming Xiong, Silvio Savarese, Heng Ji, and Ran
533 Xu. Dymu: Dynamic merging and virtual unmerging for efficient vlms. *arXiv preprint
534 arXiv:2504.17040*, 2025.

540 x.ai. Grok 1.5v: The future of ai models. Technical report, 2024.
 541

542 Long Xing, Qidong Huang, Xiaoyi Dong, Jiajie Lu, Pan Zhang, Yuhang Zang, Yuhang Cao, Conghui
 543 He, Jiaqi Wang, Feng Wu, et al. Pyramiddrop: Accelerating your large vision-language models
 544 via pyramid visual redundancy reduction. *arXiv preprint arXiv:2410.17247*, 2024.
 545

546 Cheng Yang, Yang Sui, Jinqi Xiao, Lingyi Huang, Yu Gong, Chendi Li, Jinghua Yan, Yu Bai,
 547 Ponnuswamy Sadayappan, Xia Hu, et al. Topv: Compatible token pruning with inference time
 548 optimization for fast and low-memory multimodal vision language model. In *Proceedings of the*
 549 *Computer Vision and Pattern Recognition Conference*, pp. 19803–19813, 2025a.
 550

551 Chenyu Yang, Xuan Dong, Xizhou Zhu, Weijie Su, Jiahao Wang, Hao Tian, Zhe Chen, Wenhui
 552 Wang, Lewei Lu, and Jifeng Dai. Pvc: Progressive visual token compression for unified image
 553 and video processing in large vision-language models. In *Proceedings of the Computer Vision*
 554 *and Pattern Recognition Conference*, pp. 24939–24949, 2025b.
 555

556 Ce Zhang, Kaixin Ma, Tianqing Fang, Wenhao Yu, Hongming Zhang, Zhisong Zhang, Yaqi Xie,
 557 Katia Sycara, Haitao Mi, and Dong Yu. Vscan: Rethinking visual token reduction for efficient
 558 large vision-language models. *arXiv preprint arXiv:2505.22654*, 2025a.
 559

560 Shaolei Zhang, Qingkai Fang, Zhe Yang, and Yang Feng. Llava-mini: Efficient image and video
 561 large multimodal models with one vision token. *arXiv preprint arXiv:2501.03895*, 2025b.
 562

563 Yi-Fan Zhang, Huanyu Zhang, Haochen Tian, Chaoyou Fu, Shuangqing Zhang, Junfei Wu, Feng
 564 Li, Kun Wang, Qingsong Wen, Zhang Zhang, et al. Mme-realworld: Could your multimodal
 565 llm challenge high-resolution real-world scenarios that are difficult for humans? *arXiv preprint*
 566 *arXiv:2408.13257*, 2024a.
 567

568 Yuan Zhang, Chun-Kai Fan, Junpeng Ma, Wenzhao Zheng, Tao Huang, Kuan Cheng, Denis Gu-
 569 dovskiy, Tomoyuki Okuno, Yohei Nakata, Kurt Keutzer, et al. Sparsevlm: Visual token sparsifi-
 570 cation for efficient vision-language model inference. *arXiv preprint arXiv:2410.04417*, 2024b.
 571

A APPENDIX

A.1 CROSS-MODAL ALIGNMENT IN OTHER VLMs.

572 In Fig. 7, we also observed cross-modal alignment emerging in the intermediate layers of both the
 573 InternVL and QwenVL models. This demonstrates that pretraining for next token prediction induces
 574 similar attention patterns, eliminating the need to determine distinct pruning layers for different
 575 models.
 576

A.2 THEORETICAL ANALYSIS OF EKL SCORE.

577 Let $P(i, j)$ be the joint distribution of visual tokens at adjacent layers $k - 1$ and k , where i indexes
 578 tokens at layer $k - 1$ and j at layer k . The marginals are:
 579

$$580 \mathbf{Q}^{k-1}(i) = \sum_j P(i, j), \quad \mathbf{Q}^k(j) = \sum_i P(i, j)$$

581 We begin with the definition of conditional entropy:
 582

$$583 H(\mathbf{Q}^k \mid \mathbf{Q}^{k-1}) = - \sum_{i,j} P(i, j) \log P(j \mid i) \quad (13)$$

$$584 = - \sum_{i,j} P(i, j) \log \left(\frac{P(i, j)}{\mathbf{Q}^{k-1}(i)} \right) \quad (14)$$

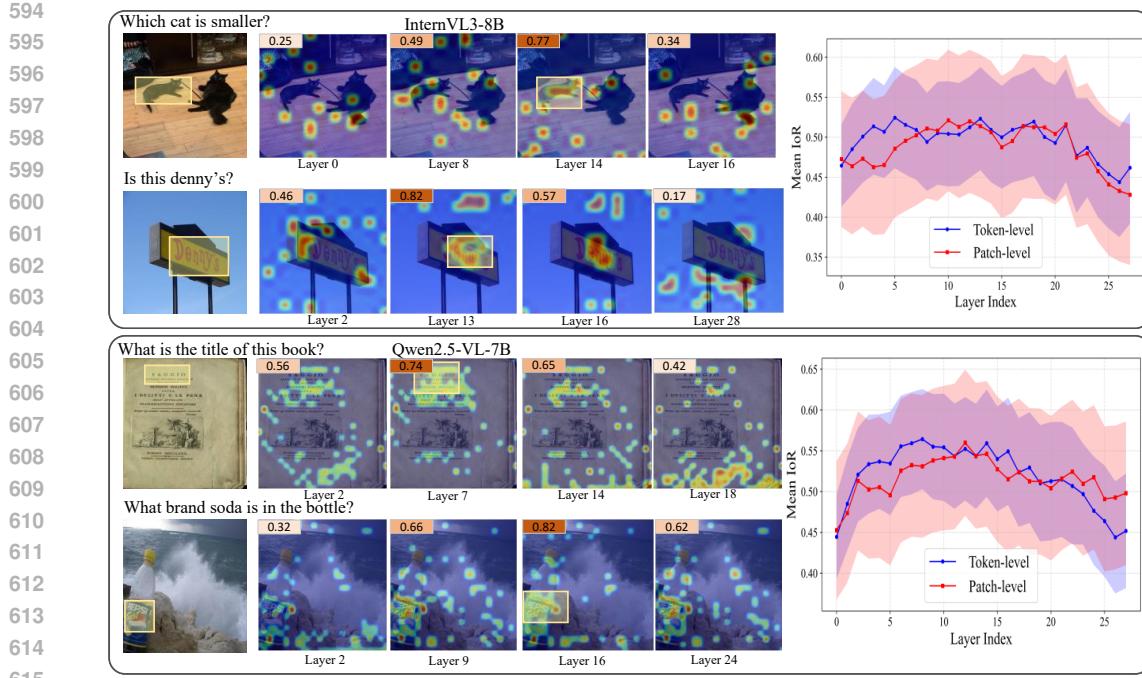


Figure 7: Attention matrices and IoR of InternVL3-8B and Qwen2.5-VL-7B across different layers, after filtering out tokens with attention weights below 70% of the maximum. EKL scores are on the upper left and yellow boxes indicate regions of interest.

Now consider the KL divergence between the marginals:

$$D_{\text{KL}}(\mathbf{Q}^k \parallel \mathbf{Q}^{k-1}) = \sum_j \mathbf{Q}^k(j) \log \frac{\mathbf{Q}^k(j)}{\mathbf{Q}^{k-1}(j)} \quad (15)$$

$$= \sum_j \left(\sum_i P(i, j) \right) \log \frac{\mathbf{Q}^k(j)}{\mathbf{Q}^{k-1}(j)} \quad (16)$$

To establish a connection, we introduce the conditional distribution $P(j \mid i)$ and examine the relationship between $P(j \mid i)$ and $\mathbf{Q}^k(j)$.

Consider the following decomposition:

$$H(\mathbf{Q}^k \mid \mathbf{Q}^{k-1}) = - \sum_{i,j} P(i, j) \log \mathbf{Q}^k(j) + \sum_{i,j} P(i, j) \log \frac{\mathbf{Q}^k(j)}{P(j \mid i)} \quad (17)$$

$$= H_{\text{cross}}(\mathbf{Q}^k, \mathbf{Q}^k) + \mathbb{E}_{i \sim \mathbf{Q}^{k-1}} [D_{\text{KL}}(P(\cdot \mid i) \parallel \mathbf{Q}^k)] \quad (18)$$

Note that $H_{\text{cross}}(\mathbf{Q}^k, \mathbf{Q}^k) = H(\mathbf{Q}^k)$, so:

$$H(\mathbf{Q}^k \mid \mathbf{Q}^{k-1}) = H(\mathbf{Q}^k) + \mathbb{E}_{i \sim \mathbf{Q}^{k-1}} [D_{\text{KL}}(P(\cdot \mid i) \parallel \mathbf{Q}^k)] \quad (19)$$

From equation (19), we see that the conditional entropy equals the marginal entropy add the expected KL divergence between the conditional and marginal distributions.

Now, consider the following information-theoretic bound:

$$D_{\text{KL}}(\mathbf{Q}^k \parallel \mathbf{Q}^{k-1}) = \sum_j \mathbf{Q}^k(j) \log \frac{\mathbf{Q}^k(j)}{\mathbf{Q}^{k-1}(j)} \quad (20)$$

$$\leq \mathbb{E}_{i \sim \mathbf{Q}^{k-1}} [D_{\text{KL}}(P(\cdot \mid i) \parallel \mathbf{Q}^{k-1})] \quad (21)$$

This inequality follows from the convexity of KL divergence and an application of Jensen's inequality. Specifically:

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1. **Convexity of KL divergence:** For a fixed distribution Q , the function $P \mapsto D_{\text{KL}}(P\|Q)$ is convex in its first argument. This means that for any two distributions P_1 and P_2 , and any $\lambda \in [0, 1]$:
$$D_{\text{KL}}(\lambda P_1 + (1 - \lambda) P_2 \| Q) \leq \lambda D_{\text{KL}}(P_1 \| Q) + (1 - \lambda) D_{\text{KL}}(P_2 \| Q)$$

2. **Application of Jensen's inequality:** Let $P_i = P(\cdot \mid i)$ be the conditional distribution at layer k given token i at layer $k-1$. The marginal distribution at layer k is:

$$\mathbf{Q}^k = \mathbb{E}_{i \sim \mathbf{Q}^{k-1}} [P_i]$$

By Jensen's inequality applied to the convex function $P \mapsto D_{\text{KL}}(P\|\mathbf{Q}^{k-1})$, we have:

$$D_{\text{KL}}(\mathbb{E}_{i \sim \mathbf{Q}^{k-1}} [P_i] \| \mathbf{Q}^{k-1}) \leq \mathbb{E}_{i \sim \mathbf{Q}^{k-1}} [D_{\text{KL}}(P_i \| \mathbf{Q}^{k-1})]$$

Substituting $\mathbf{Q}^k = \mathbb{E}_{i \sim \mathbf{Q}^{k-1}} [P_i]$ and $P_i = P(\cdot \mid i)$ gives the desired inequality.

When the transformation between layers is *sufficiently smooth* and *information-preserving*, we can make the key approximation:

$$\mathbb{E}_{i \sim \mathbf{Q}^{k-1}} [D_{\text{KL}}(P(\cdot \mid i) \| \mathbf{Q}^k)] \approx \mathbb{E}_{i \sim \mathbf{Q}^{k-1}} [D_{\text{KL}}(P(\cdot \mid i) \| \mathbf{Q}^{k-1})] \quad (22)$$

This approximation holds when \mathbf{Q}^k and \mathbf{Q}^{k-1} are similar, which is reasonable for adjacent layers in a well-trained neural network.

Substituting approximation (22) into equation (19):

$$H(\mathbf{Q}^k \mid \mathbf{Q}^{k-1}) \approx H(\mathbf{Q}^k) + \mathbb{E}_{i \sim \mathbf{Q}^{k-1}} [D_{\text{KL}}(P(\cdot \mid i) \| \mathbf{Q}^{k-1})] \quad (23)$$

$$\geq H(\mathbf{Q}^k) + D_{\text{KL}}(\mathbf{Q}^k \| \mathbf{Q}^{k-1}) \quad (24)$$

Finally, by substituting this inequality into (3), and considering that when IoR is similar, $H(\mathbf{Q}^k \mid Y)$ remains relatively constant, we can bound (2) as:

$$\mathcal{L}_{IB} \geq H(\mathbf{Q}^k) + D_{\text{KL}}(\mathbf{Q}^k \| \mathbf{Q}^{k-1}) + \text{const}, \quad (25)$$

which is the EKL computation method. Therefore, EKL provides a computationally tractable surrogate for analyzing information flow through the network layers and identifying cross-modal alignment.

A.3 THEORETICAL ANALYSIS OF REDUCED FLOPs.

We prune visual tokens at layer k^* , retaining only the top $m\%$ of N visual tokens. Below we compute FLOPs explicitly in terms of model dimensions.

Transformer layer FLOPs. For a Transformer layer with visual sequence length N , hidden dimension D , intermediate size of feed-forward network C , the approximate FLOPs is:

$$\text{FLOPs}_{\text{layer}}(N) = 4ND^2 + 2N^2D + 3NDC. \quad (26)$$

Pre-inference FLOPs. Before pruning, we partition N visual tokens into r groups and average them ($N = rL$), which takes rL FLOPs. Then, we use them to pre-inference up to layer k^* , which takes FLOPs:

$$\text{FLOPs}_{\text{pre-inference}} = k^* \cdot \text{FLOPs}_{\text{layer}}(r) + N. \quad (27)$$

Then, computing EKL requires entropy and KL divergence over $r + M$ tokens:

$$\text{FLOPs}_{\text{EKL}} \sim O((r + M)D), \quad (28)$$

Multi-modal token score computation FLOPs. At layer k^* , computing multi-modal token score involves:

1. Averaging attention over H heads for v2v: $\text{FLOPs}_{\text{v2v}} = H \cdot N^2$,
2. Averaging attention over H heads for v2t: $\text{FLOPs}_{\text{v2t}} = H \cdot (N \cdot M)$.

Thus the total multi-modal token score overhead is

$$\text{FLOPs}_{\text{multi-modal token score}} \approx HN^2 + HNM. \quad (29)$$

702 **Inference FLOPs after pruning.** After pruning $100 - m\%$ of visual tokens, the sequence length
 703 becomes

$$704 \quad N_{\text{pruned}} = m \cdot N. \quad (30)$$

705 The FLOPs per layer in the upper layers k^*, \dots, K are

$$707 \quad \text{FLOPs}_{\text{layer}}(N_{\text{pruned}}) = 4N_{\text{pruned}}D^2 + 2N_{\text{pruned}}^2D + 3N_{\text{pruned}}DC. \quad (31)$$

709 **Explicit expression.** Substituting $N_{\text{full}} = N + M$ and $N_{\text{pruned}} = m \cdot N + M$, and using the standard
 710 transformer FLOPs formula $\text{FLOPs}_{\text{layer}}(N) = 4ND^2 + 2N^2D + 3ND^2/H$, the reduced FLOPs
 711 can be written explicitly as

$$713 \quad \text{Reduced FLOPs} = \sum_{k=k^*}^K \left[4ND^2 + 2N^2D + 3ND^2 \right. \\ 714 \quad \left. - \left(4m \cdot ND^2 + 2(m \cdot N)^2D + 3(m \cdot N)DC \right) \right] \\ 715 \quad - \left[k^* \cdot (4rD^2 + 2r^2D + 3rDC) + N + HN^2 + HNM \right]. \quad (32)$$

720 **Intuition.** The first term captures the main savings from pruning the visual sequence in upper
 721 layers. The second term accounts for pre-inference, EKL and multi-modal token score computation.

723 A.4 COMPARISON ON DIFFERENT PARAMETER SCALES

725 In Tab. 9, we conducted a performance comparison between the InternVL3-2B and Qwen2.5-VL-
 726 3B models and found that PREP consistently achieved favorable results across different parameter
 727 scales.

729 Table 9: Performance comparison with TopV and Minimonkey on InternVL3-2B and Qwen2.5-VL-
 730 3B. Latency is measured in seconds per iteration.

732 Model	733 Method(Retained Ratio)	734 Venue	735 MMB	736 MME	737 POPE	738 TextVQA	739 OCRBench	740 AI2D	741 MMStar	742 Seed2	743 FLOPs Ratio(%)	744 Latency (s/it)
InternVL3-2B	original(100%)	-	80.3	2180	89.6	77.0	835	78.7	78.6	64.6	100%	0.65
	TopV(50%)	CVPR'25	79.4	2076	88.4	75.2	795	77.4	76.8	62.5	59%	0.52
	Minimonkey(50%)	ICLR'25	79.7	2096	88.7	75.5	802	77.8	77.0	62.9	65%	0.55
	PREP(50%)	-	80.2	2195	90.0	76.8	822	78.3	78.0	63.8	52%	0.47
	TopV(25%)	CVPR'25	78.5	2042	87.6	72.5	705	76.2	74.5	62.2	46%	0.39
	Minimonkey(25%)	ICLR'25	78.7	2068	87.9	72.8	721	76.4	74.8	62.4	48%	0.42
Qwen2.5VL-3B	PREP(25%)	-	80.3	2171	89.8	73.0	746	77.6	77.8	63.4	36%	0.33
	original(100%)	-	79.1	2157	83.6	79.3	797	81.6	55.9	67.6	100%	0.72
	TopV(50%)	CVPR'25	73.5	1895	82.1	75.8	698	74.8	50.2	60.8	62%	0.59
	Minimonkey(50%)	ICLR'25	74.2	1912	82.5	76.2	705	75.3	50.6	61.3	66 %	0.63
	PREP(50%)	-	76.7	1971	85.1	77.9	721	76.9	52.2	63.2	61%	0.51
	TopV(25%)	CVPR'25	71.8	1823	80.5	73.2	675	72.1	48.7	59.2	44%	0.44
750 Minimonkey(25%)	ICLR'25	72.5	1845	81.0	73.8	682	72.8	49.1	59.8	46%	0.49	0.49
	PREP(25%)	-	74.2	1864	83.7	75.1	703	74.8	50.7	61.7	42%	0.38

741 A.5 THE USE OF LARGE LANGUAGE MODELS (LLMs)

744 In this work, we employed ChatGPT as an auxiliary writing tool to improve the clarity and readability
 745 of the manuscript. Specifically, ChatGPT was used to refine the language of the *Abstract*,
 746 *Introduction*, and *Conclusion* sections. No part of the technical content, experimental design, or
 747 results was generated or modified by LLMs.