#### **000 001 002** HOW TO GET YOUR LLM TO GENERATE CHALLENGING PROBLEMS FOR EVALUATION

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# ABSTRACT

The pace of evolution of Large Language Models (LLMs) necessitates new approaches for rigorous and comprehensive evaluation. Traditional human annotation is increasingly impracticable due to the complexities and costs involved in generating high-quality, challenging problems, particularly for tasks such as long-context reasoning. Moreover, the rapid saturation of existing human-curated benchmarks by LLMs further necessitates the need to develop scalable and automatically renewable evaluation methodologies. In this work, we introduce CHASE, a unified framework to synthetically generate challenging problems using LLMs without human involvement. For a given task, our approach builds a hard problem in a bottom-up manner from simpler components. Moreover since we want to generate synthetic data for evaluation, our framework decomposes the generation process into independently verifiable sub-tasks, thereby ensuring a high level of quality and correctness. We implement CHASE to create evaluation benchmarks across three diverse domains: document-based question answering, repository-level code completion, and math reasoning. The performance of state-of-the-art LLMs on these synthetic benchmarks lies in the range of 40-60% accuracy, thereby demonstrating the effectiveness of our framework at generating hard problems. Our experiments further reveal that the Gemini models significantly outperform other LLMs at long-context reasoning, and that the performance of all LLMs drastically drops by as much as 70% when we scale up the context size to 50k tokens.

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# 1 INTRODUCTION

**033 034 035 036 037 038 039 040 041 042 043 044 045** In the past few years, we have witnessed the emergence of powerful Large Language Models (LLMs) [\(OpenAI Team et al., 2024;](#page-14-0) [Llama Team et al., 2024;](#page-13-0) [Gemini Team et al., 2024\)](#page-12-0) that exhibit remarkable performance over a wide range of tasks. However, the methods and resources for evaluating these models have not kept pace with their rapid evolution and increased capabilities. Contemporary LLMs have saturated many existing reasoning benchmarks [\(Chen et al., 2021;](#page-11-0) [Cobbe](#page-11-1) [et al., 2021\)](#page-11-1). Developing challenging problems for reasoning tasks, such as math reasoning or code generation, can be both expensive and time-consuming, especially for human annotators with average expertise. Moreover, there are some settings, such as tasks requiring long-context reasoning over hundreds of thousands of tokens, where the generation of high quality data by humans is impracticable. Additionally, we are facing a significant depletion of interesting data that is publicly available (such as SAT exams, Olympiad problems, etc.) for creating benchmarks. Hence, we believe that the conventional approach of developing evaluation benchmarks through human annotation and existing Web content is limited, and it is worthwhile to explore using LLMs for generating evaluation data.

**046 047 048 049 050 051** Synthetic data generation has emerged as a powerful paradigm in recent years driven by the widespread availability of cheaper and faster LLMs that can effectively follow instructions. The focus of most prior works, however, has been on improving models by generating synthetic data for pre-training [\(Gunasekar et al., 2023\)](#page-12-1), instruction fine-tuning [\(Wang et al., 2023;](#page-16-0) [Xu et al., 2024\)](#page-16-1), alignment [\(Bai et al., 2022\)](#page-10-0), or task-specific fine-tuning [\(Yue et al., 2024;](#page-17-0) [Wei et al., 2024\)](#page-16-2). In contrast, using synthetic data for evaluation and benchmarking has been relatively underexplored.

**052 053** There are considerable advantages in using synthetic data for evaluation: it is comparatively inexpensive, highly scalable, and can be renewed periodically to mitigate contamination concerns. However, there are two main challenges: first, *how can we create hard and realistic problems?* and second, *how*

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**075 076 077** Figure 1: *Top:* Illustrating the high-level ideas behind our proposed CHASE framework. *Bottom left:* Pipeline for creating an example in CHASE-QA. *Bottom right:* Pipeline for creating a math word problem in CHASE-MATH. The pipeline for CHASE-CODE is illustrated in Figure [4](#page-19-0) in Appendix.

**080 081 082 083 084 085** *can we automatically verify the correctness of the generated data?* Typical synthetic data generation pipelines are either focused on self-improvement or on distillation. In the former, a model generates large-scale synthetic data that provides useful guidance for training. However, a large portion of such model-generated data is incorrect [\(Wang et al., 2023\)](#page-16-0), which makes it difficult to adapt such pipelines for evaluation. Distillation-based approaches use stronger models to generate complex problems for training weaker models [\(Xu et al., 2024\)](#page-16-1). However, we would like to design an approach that allows us to craft problems that are *challenging* to solve even for the LLM that generated them.

**086 087 088 089 090 091 092** In this work, we present the CHASE framework: CHallenging AI with Synthetic Evaluations. Our methodology is based on two main ideas (see Figure [1\)](#page-1-0) geared towards addressing the abovementioned challenges. First, we create problems in a *bottom-up* manner where we iteratively hide parts of the solution within the problem's context. This makes problems challenging because finding the solution will require multiple steps of drawing inferences or reasoning over a longer context. Second, we decompose the generation process into simpler, *individually verifiable sub-tasks*. This facilitates fine-grained verification for correctness at each stage of the generation process.

**093 094 095 096 097 098 099 100 101 102 103** We implemented our framework to create challenging benchmarks across three diverse domains. (1) CHASE-QA is a document-based question answering benchmark. The average length of documents for each problem is 6k tokens. This benchmark simulates the real-world application of answering user queries based on information that is spread across multiple documents, most of which may be irrelevant. (2) CHASE-CODE is a repository-level code completion benchmark with an average context length of 17k tokens. It consists of problems from two different domains: *data pre-processing* functions, and *algorithms*. This dataset simulates the real-world application of generating code in existing repositories based on user specifications. (3) **CHASE-MATH** is a grade-school level math word problems benchmark consisting of problems involving arithmetic reasoning. We built this benchmark to show the utility of our framework in building challenging problems for seemingly easy tasks on which models have already saturated existing benchmarks [\(Cobbe et al., 2021\)](#page-11-1).

**104 105 106 107** Experiments with 15 contemporary LLMs show that the datasets generated using CHASE are challenging for all models. The best performing LLMs only achieve accuracies in the range of  $\sim$  40 – 60% across the three different domains. We further highlight the utility of CHASE by comparing it with direct prompting-based data generation baselines such as *Evol-Instruct* [\(Xu et al.,](#page-16-1) [2024\)](#page-16-1), which yield data with significant errors, apart from being relatively easier for models to solve.

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Figure 2: Examples of problems from all three benchmarks created using CHASE.

Our results also reveal large gaps in performance between different LLMs, all of which perform similarly on existing benchmarks like MMLU [\(Hendrycks et al., 2021\)](#page-12-2) or HumanEval [\(Chen et al.,](#page-11-0) [2021\)](#page-11-0). Lastly, using our long-context benchmarks, we show that the performance of all LLMs decreases drastically (sometimes by upto 70%) when we increase the context size beyond 50k tokens.

# 2 RELATED WORK

**130 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145** Synthetic data generation. Prior works have explored generating synthetic data for various stages of an LLM's development pipeline: pre-training [\(Gunasekar et al., 2023;](#page-12-1) [Ben Allal et al., 2024\)](#page-11-2), instruction-finetuning [\(Wang et al., 2023;](#page-16-0) [Xu et al., 2024\)](#page-16-1), alignment [\(Bai et al., 2022;](#page-10-0) [Lee et al.,](#page-13-1) [2024\)](#page-13-1) and task-specific fine-tuning [\(Wei et al., 2024;](#page-16-2) [Yu et al., 2024a\)](#page-17-1). The main focus of our work, however, is to generate high-quality challenging problems for evaluation and benchmarking. There is very limited existing literature in this area. [Sprague et al.](#page-15-0) [\(2024\)](#page-15-0) created a narrative-based question answering (QA) benchmark using a neuro-symbolic pipeline that first samples facts, and then uses an LLM to build a reasoning tree over them, along with generating a narrative. [Bohnet et al.](#page-11-3) [\(2024\)](#page-11-3) created another synthetic QA benchmark by extracting entities and their reference chains from existing stories and then prompting an LLM to generate questions over them. [Gu et al.](#page-12-3) [\(2024\)](#page-12-3) create a code understanding benchmark by prompting CodeLlama [\(Roziere et al., 2024\)](#page-15-1) to generate python ` functions and their inputs and designing tasks based on predicting either the input or the output for a given function. In contrast to these works, we focus on presenting a general framework which can be used to design scalable pipelines to create challenging benchmarks across multiple domains. Moreover, we focus on realistic tasks such as information-seeking QA and repository-level code generation, both with extremely long contexts that we generate completely from scratch.

**146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 Task-specific synthetic data.** Recent works have explored generating synthetic datasets for contentgrounded QA tasks. [Dai et al.](#page-11-4) [\(2022\)](#page-11-4) use an LLM to develop information-seeking dialogue datasets based on text extracted from Wikipedia and the Web. [Yehudai et al.](#page-17-2) [\(2024\)](#page-17-2) prompt an LLM with wikipedia text to generate a question-answer pair. In contrast, we take a more application-oriented view and design a benchmark for document-based information-seeking questions that model realistic situations. Moreover, our pipeline generates the entire context (i.e., the documents) from LLMs, which allows a higher degree of control. There has also been significant interest in generating synthetic data for code. [Yu et al.](#page-17-3) [\(2024b\)](#page-17-3) employ an LLM-based framework to create examples for tasks based on existing raw code data. [Wei et al.](#page-16-2) [\(2024\)](#page-16-2) generate code instruction data by prompting an LLM with seed code snippets from existing repositories. [Luo et al.](#page-13-2) [\(2024\)](#page-13-2) generate complex and diverse code instruction-tuning data by applying the *Evol-Instruct* method [\(Xu et al., 2024\)](#page-16-1) on existing code benchmarks. In this work, we focus on repository-level code completion, where we generate the repository contexts completely from scratch. Moreover, we also synthetically generate the corresponding test code to evaluate each example. Generating synthetic data to improve math reasoning has recently been a very active area of research. Previous work has explored generating new math problems by prompting LLMs with examples from existing datasets [\(Liu et al., 2023;](#page-13-3) [Yu et al., 2024a;](#page-17-1) [Lu et al., 2024\)](#page-13-4). Similar to our work, some prior works have focused on creating challenging math problems. [Shah et al.](#page-15-2) [\(2024\)](#page-15-2) employ a human-in-the-loop approach to generate

**162 163 164 165 166** novel and difficult math problems by prompting LLMs with multiple core skills that must be used in the problem. [Liu et al.](#page-13-5) [\(2024a\)](#page-13-5) employ iterative question composition where they iteratively prompt an LLM with a seed question to generate more complex variations of it. In this work, we design a completely automated pipeline to craft grade-school level math word problems that are challenging to solve even for the LLM that generated them.

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# 3 THE CHASE FRAMEWORK AND BENCHMARKS

Our framework for generating synthetic data is based on two key ideas as illustrated in Figure [1.](#page-1-0)

#### **172** 1. Bottom-up problem creation.

**173 174 175 176 177 178 179 180 181** We abandon the forward-thinking approach of first creating a difficult problem and then obtaining the corresponding solution, as followed by most works that create synthetic data for training [\(Xu et al.,](#page-16-1) [2024;](#page-16-1) [Liu et al., 2024a\)](#page-13-5). If we first synthesize a complex problem and then obtain its corresponding solution from the generating LLM itself, then that problem is inherently solvable by that LLM. However, we wish to craft problems that are challenging even for the model which generates them. Hence, we instead take a different approach where we either generate or start with a simpler problemsolution pair, and then *bottom-up* build a challenging context. We make the problem's context challenging by systematically *hiding* components of the solution or reasoning such that they need to be either extracted from a long context or inferred based on given information.

#### **182** 2. Decomposition into simpler, verifiable sub-tasks.

**183 184 185 186 187 188 189 190 191 192** We design pipelines that break down the generation process into simpler sub-tasks. Each individual LLM in the pipeline (i.e., each inference call) performs a simpler, specific function in the generation process. This provides us with multiple benefits. First, it grants us more control over each step of the generation process. We can treat each step as a task by itself and optimize the corresponding inference parameters individually. This also allows us to better manage the complexity and diversity of the generated data depending on our requirements. Second, and perhaps more importantly, it facilitates fine-grained verification. We deploy LLMs that are not part of the generation process to check the correctness and quality of the generated data at each possible step. We believe that LLMs can be relied upon for verification because our framework makes each verification task smaller and simpler compared to the main task of generating or solving the problem we are crafting.

**193 194** We show the effectiveness and ease of adaptation of our framework by implementing it to create challenging problems across three diverse domains:

**195 196 197 198** CHASE-QA is an open-domain document-grounded question answering task consisting of 671 problems. Each example in CHASE-QA consists of a set of documents and a question-answer pair, as illustrated in Figure [2](#page-2-0) left. Models need to reason over a long context (more than 6k tokens) because the information relevant for answering the question is spread across multiple documents.

**199 200 201 202 203 204** CHASE-CODE is a repository-level code completion benchmark consisting of 220 challenging problems. Given a repository of Python functions, the task is to implement a new function based on a set of objectives provided in natural language, as illustrated in Figure [2](#page-2-0) centre. We create data for two broad domains: (1) *data pre-processing* operations such as dataframe manipulation, string processing, file I/O, etc., and (2) *algorithms* such as graph operations, array manipulations, etc.

CHASE-MATH is a challenging benchmark of 150 grade-school level math word problems involving only basic arithmetic operations. An example of the task is provided in Figure [2](#page-2-0) right.

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- 4 CONSTRUCTION PIPELINES
- **210 211** In this section, we discuss our implementation of the CHASE framework for all three domains in more detail. Our pipelines use two different LLMs: the generator  $\mathbf{G}$ , and the verifier  $\mathbf{V}$ .
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- **213** 4.1 CONSTRUCTING CHASE-QA
- **215** We generate CHASE-QA completely from scratch without relying on existing contexts or any seed examples from previous datasets. Following the CHASE framework, we create each example in a

**216 217 218 219** bottom-up manner by first generating the question-answer pair, and then generating the corresponding documents. Our pipeline for creating CHASE-QA is illustrated in Figure [1](#page-1-0) bottom left. We describe it in detail below. The exact prompts are provided in Appendix [F.1.](#page-24-0)

**220 221 222 223 224** Generating diverse scenarios. We begin by first generating a set of diverse realistic scenarios in which a *user persona* seeks to find some information from a *collection of documents*. An example would be a 'grad student in NYC' searching the 'laws on renting and subletting'. We prompt G to generate diverse scenarios in the form of a tuple (persona, collection name) by bootstrapping it with 5 annotated example scenarios, and later prompting it with its own generated scenarios.

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**226 227 228 229 230 231 232 233 234 235** Generating question-answer pairs. Each scenario (persona, collection\_name) defines the working environment for creating a particular example. We design programmatic prompts with a given scenario as the variable to prompt G to generate a realistic information-seeking question that the persona might want to know about from collection name set of documents. For example, a 'grad student' might pose the question, 'what is the procedure for refusing increase in rent?', whose answer can be found spread across multiple documents about the government's laws on renting. Apart from the question,  $G$  must also generate the corresponding answer. We prompt  $G$  to generate questions and answers where the answers are a composition of multiple points or ideas. Additionally, G must generate the outline of the documents (only title and abstract) which will contain the answer. The idea is that it must separate out the answer points and assign them to these different documents.

**236 237 238 239 240 241 242 243 244 245 246 247** Generating irrelevant information. To make the task more challenging, for each question-answer pair, we prompt G to generate other question-answer pairs where the answer is of a similar type or domain as the ground-truth answer. An example of a similar question for our running example with the grad student is 'what is the process to increase the rent for an appartment I am subletting?'. The intuition is that the corresponding answers to such similar questions will be of a very similar flavour to the ground-truth answer, but ultimately *irrelevant* for answering the question. This will make the generated data challenging since it will confuse the model when all of this similar type of information is spread across a long context. It is, however, important to verify that none of this newly generated irrelevant information is actually relevant for the original question (otherwise it will make our ground-truth answer incomplete). We individually prompt  $V$  with the original question and each of the supposed irrelevant information points to check if any part of them is relevant for answering the question (see Figure [1](#page-1-0) bottom left for an example of an irrelevant point discarded by  $V$  because it was relevant for the original question).

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**249 250 251 252 253 254 255 256** Generating documents. For each example, we have generated a question-answer (QA) pair, along with some similar but irrelevant QA pairs. For each of these QA pairs, we separately prompt G to generate long documents where the documents must discuss the corresponding answer points assigned to it, along with many other irrelevant points. All documents discuss distinct information. Together, all these documents form up the context for that example. We verify two main things to ensure the correctness of the task: (1) none of the documents should contain any information relevant for answering the question, apart from the ground-truth answer points, and (2) all of the ground-truth answer points must be discussed somewhere in the documents. We do this by rigorously prompting V with individual documents and the ground-truth answer points.

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4.2 CONSTRUCTING CHASE-CODE

We generate CHASE-CODE completely from scratch without relying on existing contexts or any seed examples from previous datasets. Our pipeline for creating CHASE-CODE is shown in Figure [4](#page-19-0) in the Appendix. We describe it in detail below. The exact prompts are provided in Appendix [F.2.](#page-25-0)

**264 265 266 267 268 269** Generating Python functions. We begin by first generating a set of diverse and realistic Python functions. We prompt G to generate Python functions for a particular domain by bootstrapping it with 3 annotated functions in that domain, and later prompting it with its own generated functions. These generated functions will act as the *helper* functions in the repository context which may or may not be called in the answer code function. Given each generated helper function, we prompt V to generate a Python code which initializes sample inputs for the function and then calls it using them. We then execute this code to verify whether the generated helper function executes correctly.

**270 271 272 273 274 275 276 277 278 279** Generating problem statement and answer code. To create a single example, we randomly sample  $n$  of the previously generated helper functions, and prompt  $\bf{G}$  to create a complex function that calls at least k of these provided helper functions (hereafter called *relevant* helper functions) apart from implementing some other pieces of logic. This complex function is our *answer code*. Additionally G must elaborate in natural language what objectives the complex function achieves, which makes up our *problem statement*. Similar to the case of helper functions, we prompt V to generate test code to check if the generated answer code executes correctly. Moreover, we need to verify whether the generated problem statement sufficiently specifies the answer code. We prompt V with the problem statement and corresponding *relevant* helper functions and check whether the output is semantically equivalent to the answer code (using the test code obtained in the next step).

**280 281 282 283 284 285 286** Generating test code. To enable automatic execution-based testing, we prompt G with the generated answer function to implement the test code for it in Python. The test code must independently implement the logic of the answer code without access to the corresponding helper functions. It must then initialize the parameters of the answer function with some sample values, and compare its output with its own implementation. We execute the generated test code to check if the corresponding answer code passes. We discard all examples for which (1) the test code does not execute properly, or (2) the test code executes but the answer code fails the test.

**288 289 290 291** Building code repository. For each example, we build a unique repository of Python files. The repository consists of the *relevant* helper functions spread across different files, along with m randomly sampled irrelevant Python functions from our previously generated set. The core difficulty of this task arises from understanding the entire long context of code functions, and identifying which ones are relevant for the provided problem statement.

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# 4.3 CONSTRUCTING CHASE-MATH

**295 296 297 298 299** We sample math word problems (MWP) from existing datasets as seed examples to build our benchmark. Following the CHASE framework, we bottom-up build a more complex problem by iteratively increasing the reasoning depth of the problem. An illustration of the pipeline used for creating CHASE-MATH can be seen in Figure [1](#page-1-0) bottom right. We describe the pipeline in more detail below. The exact prompts are provided in Appendix [F.3.](#page-25-1)

**301 302 303 Breaking down seed MWP.** A seed MWP s is characterised by the tuple  $s = (p, a)$  where p is the problem, and  $\alpha$  is the answer. We prompt G to break down  $p$  into two parts: the context  $c$ , which provides all the information, and the question  $q$ , which asks about some unknown quantity.

**304 305 306 307 308 309 310 311 Create continuation of MWP.** We prompt G with an initial seed MWP  $s_0 = (p_0, a_0)$  to build a new problem which is a continuation of the previous problem. More precisely, G should output a new problem  $s_1 = (p_1, a_1)$ , where the context of  $p_1$ , i.e.,  $c_1$  assumes  $a_0$  as given information (without explicitly stating it). For example, in Figure [1](#page-1-0) bottom right, the model assumes *Jack has 4 pens* as given information, and creates a new continuation context, *Jill has thrice as many pens as Jack has now.* The model also generates a new question  $q_1$ , *how many pens does Jill have?* whose answer  $a_1 = 12$  is obtained by performing an arithmetic operation (here, *multiplication by 3*) over  $a_0 = 4$ .

**312 313 314 315 316** Combining seed MWP with its continuation. By combining the original seed problem with its continuation, we get a new MWP  $s = (p, a)$  with a higher reasoning depth, where the context c of the combined problem  $p$  is a concatenation of the contexts of the seed problem and the continuation  $c = c_0 \cdot c_1$ . The question for the combined problem will be the one generated by the model, i.e.,  $q_1$ , and the corresponding answer  $a = a_1$ . We refer to Figure [1](#page-1-0) bottom right for illustration.

**318 319 320 321 322** Iteratively increase reasoning depth. We increase the reasoning depth of a given seed MWP by creating new continuations in an iterative manner. Each new continuation  $s_i$  formed after the  $i^{\text{th}}$  iteration becomes the seed problem for the  $(i + 1)^{\text{th}}$  iteration. The final complex problem after j successful iterations, i.e., with a reasoning depth of  $j + 1$ , is given by context  $c = c_0 \cdot c_1 \dots c_j$ , question  $q_i$ , and answer  $a = a_i$ .

**323** Since each individual new problem created by  $G$  has a low reasoning depth of the same difficulty as the problems in the seed datasets, we verify their correctness using a non-identical ensemble of **324 325 326 327** verifier models  $\{V_1, V_2, \ldots, V_n\}$ , each of which has very high performance on the seed dataset. We prompt each  $V_k$  with the generated problem context  $c_i$  and question  $q_i$  and check whether the prediction is the same as the generated answer  $a_i$ . If this fails for any verifier, we discard  $s_i$  and begin generating again with  $s_{i-1}$  as the seed MWP (see Figure [1](#page-1-0) bottom right).

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5 EXPERIMENTS

#### **332** 5.1 IMPLEMENTATION DETAILS

**333 334 335 336 337 338 339 340** Generating CHASE-QA. We use GPT-4o [\(OpenAI Team et al., 2024\)](#page-14-0) as the generator G, and GPT-40-mini as the verifier  $V$ . We first sampled 500 different scenarios. For each scenario, we generate 2 different question-answer (QA) pairs. For each of the resulting 1000 unique QA pairs, we obtain *irrelevant* information by generating 4 similar QA pairs. We then generate the corresponding documents containing the ground-truth answer as well as irrelevant information for each of the 1000 examples. To increase the complexity of the resulting benchmark, we carry out a form of rejection sampling. We evaluate GPT-4o-mini twice on the task, and randomly discard half of the problems on which it was correct both times. This yielded the final benchmark of 671 examples.

**341 342 343 344 345 346 347 348 349 350 351 352 353 354 355** Generating CHASE-CODE. We use GPT-4o-mini [\(OpenAI Team et al., 2024\)](#page-14-0) as the generator G, and Gemini-1.5-Flash as the verifier  $V$ . We made this choice because generating even a small amount of challenging code problems required a large number of iterations, since a lot of the model-generated code at various stages would fail to execute or be semantically incorrect. For each domain, we first sampled 500 different helper functions that execute without errors. Then we prompt the model with  $n = 10$  random helper functions to generate a problem statement and corresponding answer code that calls at least  $k = 4$  helper functions. We do this to create 1000 different examples for each domain. Next, we generate up to 10 test codes for each example and keep only those examples for which a generated test code successfully passed for the corresponding answer code. We also carry out the verification of correctness of problem statement as describe before. This way, we end up with 290 examples for the *algorithms* domain and 300 examples for the *data pre-processing* domain. We again use GPT-4o-mini for rejection samping and randomly discard around half of the problems on which it was correct. This way, we end up with a total of 500 examples in the benchmark, with 250 examples for each domain. For each example, we randomly sample  $m = 100$  *irrelevant* helper functions and distribute them into 10 Python files to constitute the repository context.

**356 357 358 359 360 361 362 363 364 365 366** Generating CHASE-MATH. We again use GPT-4o-mini [\(OpenAI Team et al., 2024\)](#page-14-0) as the generator G, and an ensemble of Gemini-1.5-Flash and Llama-3.1-70B as the verifier V. In practice, we observed that many of the model generated problems would fail at various stages of verification, so it is faster and cheaper to query the smaller models. We start with 2.3k seed problems taken from the test sets of GSM8k [\(Cobbe et al., 2021\)](#page-11-1) and SVAMP [\(Patel et al., 2021\)](#page-14-1). We set the maximum and minimum reasoning depth at 8 and 4 respectively. For each problem, we iterate 15 times to generate a problem continuation. Note that many of these iterations fail to produce a correct continuation of the problem, in which case we discard that generation and retry from that point in the subsequent iteration. We carry out this process 3 times. In this manner, we generated around 1500 problems. We then carry out rejection sampling and roughly discarded 75% of the problems that GPT-4o-mini could solve. In the end, we end up with a total of 500 challenging MWPs.

**367 368 369 370 371 372** Task parameters. For CHASE-QA and CHASE-CODE, we prompt models with the instruction for the task, along with the corresponding long-context and question. The prompt formats are provided in Figure [19](#page-39-0) and [28](#page-47-0) respectively in Appendix [F.](#page-24-1) For CHASE-MATH, we prompt models with the standard 8-shot chain-of-thought [\(Wei et al., 2022b\)](#page-16-3). The prompt format is provided in Figure [31](#page-49-0) in Appendix [F.3.](#page-25-1) We decode for a maximum of 1024 tokens with a temperature of 0.5.

**373 374 375 376 377** Evaluation. The ground-truth answers for CHASE-QA are verbose text, organized in bullet points. While this simulates real-world complexity, it also makes evaluation difficult. Since it is intractable to employ expert humans for evaluation, we deploy an LLM-as-a-judge to automatically assess the correctness of predictions. A prediction is considered to be correct if and only if it is (1) *complete*, i.e., it includes all the points mentioned in the ground-truth answer, and (2) *relevant*, i.e., it provides information only pertaining to the current question. We use GPT-4o as the judge and measure the

<span id="page-7-0"></span>**378 379 380 381 382 383 384 385 386** Table 1: The performance of various LLMs on all 3 domains of the CHASE benchmark. We measure the accuracy of the predictions for CHASE-QA and CHASE-MATH, and pass@1 for CHASE-CODE. DATA and ALGO refer to the *data pre-processing* and *algorithms* subdomains of CHASE-CODE. Numbers in bold indicate best performance on domain while underline indicates best-in-class performance.







**Performance of LLMs on CHASE-Code vs Context Size**



<span id="page-7-1"></span>Figure 3: Performance of LLMs decreases uniformly with increasing context sizes for the 100 example subset of CHASE-QA (*top*) and the 55 example subset of CHASE-CODE (*bottom*).

**409 410 411 412 413** accuracy as the percentage of predictions judged to be correct. The prompt format used for evaluation is provided in Figure [20](#page-40-0) in Appendix [F.1.](#page-24-0) For CHASE-CODE, we measure the pass@1 execution accuracy, i.e., whether the model generated code correctly passes when we execute the corresponding test code in the first attempt. For CHASE-MATH, we measure the exact match accuracy against the ground-truth numerical answer.

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> Models. We evaluated a total of 15 different LLMs: Gemini-1.5-Pro and Flash [\(Gemini Team](#page-12-0) [et al., 2024\)](#page-12-0), GPT-4o and GPT-4o-mini [\(OpenAI Team et al., 2024\)](#page-14-0), Claude-3.5-Sonnet [Anthropic](#page-10-1) [\(2024b\)](#page-10-1), Claude-3-Haiku [\(Anthropic, 2024a\)](#page-10-2), Llama-3.1 8B and 70B [\(Llama Team et al., 2024\)](#page-13-0), Mistral Small and Large 2 [\(Mistral, 2024\)](#page-14-2), Qwen2.5 7B and 72B [\(Yang et al., 2024a;](#page-16-4) [Team, 2024a\)](#page-15-3), Cohere Command R+ [\(Cohere, 2024\)](#page-11-5), DBRX-Instruct [\(Team, 2024b\)](#page-15-4), and Phi-3.5-MoE [\(Abdin et al.,](#page-10-3) [2024\)](#page-10-3). The details of implementation are provided in Appendix [B.](#page-18-0)

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# 5.2 RESULTS AND DISCUSSION

**424 425 426 427 428 429 430 431** Performance of models. Table [1](#page-7-0) shows the performance of all 15 LLMs on all three bechmarks. For, CHASE-QA, all models, including the generator (and judge) GPT-4o, find the task challenging. The best performing model is Gemini-1.5-Pro which achieves only about 63% accuracy, suggesting massive room for improvement. All the models struggle even more on CHASE-CODE, with the best performing model only achieving 38.2% average accuracy. For CHASE-MATH, we see that even the most powerful LLMs only achieve 65.4% accuracy on a benchmark composed of grade-school level math word problems. Overall, these results clearly indicate the utility of the CHASE framework in crafting challenging problems that even state-of-the-art LLMs struggle to solve. We provide examples of errors made by Gemini-1.5-Pro on all three benchmarks and analyze them in Appendix [E.](#page-24-2)

<span id="page-8-0"></span>**432 433 434** Table 2: Performance of LLMs on data generated by direct prompting approaches without using CHASE.

Table 3: Accuracy of LLMs increases marginally on CHASE-MATH when fine-tuned on data generated by Llama-3.1-8B.



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**442 443 444 445 446 447 448 449 450 451 452 453 454 455 456** On all three benchmarks, we see huge variations in performance between the models. Moreover, we observe models different from the generator and verifier (such as Gemini-1.5-Pro) that do better for all three tasks. This stands as a testament to the underlying quality of the generated data and highlights our framework's potential for differentiating between state-of-the-art LLMs that all perform similarly on standard benchmarks like MMLU [\(Hendrycks et al., 2021\)](#page-12-2) or HumanEval [\(Chen et al.,](#page-11-0) [2021\)](#page-11-0). We further note some interesting observations. On both the long-context benchmarks, there is a substantial gap between the Gemini models and the other LLMs, clearly exhibiting the strong long-context reasoning capabilities of Gemini. Another interesting observation is that most of the models are stronger on the *algorithms* domain, while GPT-4o is stronger at *data pre-processing*. This demonstrates the utility of our benchmark at identifying such targeted differences in performance which could be very helpful for real tasks. For math reasoning, we have seen even weaker models like Llama-3.1-8B and Phi-3.5 get around  $85 - 90\%$  accuracies on the popular GSM8k and SVAMP benchmarks. However, we see a large difference ( $\sim 25 - 30\%$ ) between their performance and that of the state-of-the-art models, which may be attributed in part to some level of contamination of existing benchmarks [\(Zhang et al., 2024a\)](#page-17-4).

**457 458 459 460 461 462 463 464 465 466 467 468 469** Direct generation baseline. We experimented with directly prompting models to generate challenging data for the QA and math tasks, without using the CHASE framework. For QA, we prompt GPT-4o with unique examples from CHASE-QA as the seed task and instruct it to generate new examples in a manner similar to [Honovich et al.](#page-12-4) [\(2023\)](#page-12-4) and [Wang et al.](#page-16-0) [\(2023\)](#page-16-0). For math, we adapt the *Evol-Instruct* method [\(Xu et al., 2024\)](#page-16-1) to generate more complex problems given seed examples from GSM8k. We carry out the same proportion of rejection sampling as we did for CHASE-QA and CHASE-MATH for fair comparison. We generated a total of 100 examples for both tasks. For the math task, we manually examined the generated problems and found that 34 of them had some kind of error such as the problem text being ambiguous or vague or the reasoning and answer being incorrect. Carrying out a detailed manual verification for the QA problems is impracticable, however, we believe it is highly likely that a significant portion of it is incorrect. We evaluated GPT-4o, Gemini-1.5-Pro, and Claude-3.5-Sonnet on these datasets and provide the results in Table [2.](#page-8-0) For both tasks, we observe that we are unable to generate challenging data by direct prompting.

**470 471 472 473 474 475 476 477 478** Impact of context size. We studied the impact of varying the context size for long-context reasoning. For each example in a randomly-sampled 100-example subset of CHASE-QA, we increase the context size by concatenating the documents in that example with irrelevant documents randomly sampled from other examples. For CHASE-CODE, we create a subset of 55 randomly-sampled examples for each of the domains and increase the context size by concatenating irrelevant code functions in the corresponding repository context. Figure [3](#page-7-1) plots the performances of 4 LLMs across different context sizes. For both benchmarks, we see a consistent and significant decrease in model performance as we scale up the context size. Hence, even though most modern LLMs have large context sizes (upwards of 128k), they still struggle to reason even at the scale of 30-40k tokens.

**479 480 481 482 483 484** Human verification of LLM judgements. We measure the correlation of the GPT-4o evaluator's judgement and 3 human annotators over  $100$  $100$  randomly sampled<sup>1</sup> predictions made by Gemini-1.5-Pro on CHASE-QA. The accuracy of GPT-4o's judgement as measured against the majority vote of the annotators was 91%. Moreover, Cohen's kappa [\(Cohen, 1960\)](#page-11-6) between the majority vote of the annotators and the LLM judge came out to be 0.82, which can be interpreted as almost-perfect agreement. Additional details regarding the setup of these experiments can be found in Appendix [B.](#page-18-0)

<span id="page-8-1"></span><sup>&</sup>lt;sup>1</sup>but balanced, according to GPT-4o's judgement.

**486 487 488 489 490 491 492 493** Fine-tuning smaller models. We study whether we can use much smaller models (of around 7B) scale) to generate useful fine-tuning data for themselves following CHASE pipelines to perform better on evaluation benchmarks created by stronger models. We generate  $\sim 10k$  math problems using Llama-3.1-8B as both the generator and the verifier and fine-tune 3 small models. Table [3](#page-8-0) shows the accuracies on CHASE-MATH before and after fine-tuning on this dataset for all LLMs. We see marginal performance improvements across all models. These results seem to indicate that the evaluation data generated using significantly stronger models cannot be easily solved by such weak models even when fine-tuned on data generated by themselves using the exact same pipeline.

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# 6 CONCLUSION

**497 498 499 500 501 502 503 504 505 506 507 508 509 510** In this work, we presented CHASE, a framework to synthetically generate challenging problems for evaluation. Our framework offers multiple benefits. First, it is scalable and can efficiently generate hundreds of challenging problems. Second, it is renewable, which means it can be used to keep regenerating new datasets for a given task at periodic intervals thereby mitigating contamination concerns which plague most evaluation benchmarks. Third, it can effectively help evaluate tasks (such as long-context reasoning) which are inherently difficult or impracticable for humans to evaluate. Fourth, it provides a very high level of quality and correctness because of extensive verification. And finally, it can be used to generate *difficult* examples for a given task. We implemented CHASE on three different domains: document-based question answering, repository-level code completion, and math reasoning. With the help of extensive experiments, we showed that CHASE successfully generates examples that are difficult even for the state-of-the-art LLMs to solve. Our results raise several interesting questions to explore in future work: (a) How can we modify this framework to more easily adapt to different tasks? (b) What is the utility of this framework in generating data for training LLMs? (c) How can we verify LLM generations more efficiently? We hope our work will catalyze many such studies on using synthetic data for evaluation.

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# 7 LIMITATIONS

**514 515 516 517 518 519 520 521 522** Size of benchmarks. The datasets we generated are comparatively smaller in size. Our framework necessitates querying the generator and especially the verifier many times for crafting each example. While this increases the quality and correctness of the data, it significantly increases the cost of generation. Moreover, a large portion of the intermediate generations in our pipeline are discarded because of extensive verification, which significantly reduces the yield. Our focus in this work is to present the CHASE framework and we believe our experiments, albeit on smaller-sized datasets, convincingly show its utility in generating challenging problems for evaluation. Small benchmarks, if generated with a high bar for quality and correctness, can still be very impactful as evidenced by past works like HumanEval [\(Chen et al., 2021\)](#page-11-0).

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**524 525 526 527 528 529 530 531 532 533** Instance-level issues. Some of the examples we generated using CHASE, while being semantically correct, use unnatural or difficult-to-parse language. This is a general trait of text generated from contemporary LLMs, and our framework is unfortunately susceptible to it. Moreover, while we carry out extensive verification of correctness at the instance-level using LLMs, it is still possible that some of the generated examples are incorrect. Verifying long-context reasoning data using non-expert humans is impracticable. To get a sense of the quality, we manually examined 30 random examples each from the generation process of CHASE-QA and CHASE-CODE. We found only 2 errors in CHASE-QA and none in CHASE-CODE. We also examined 100 examples from CHASE-MATH's pipeline and found 7 that were incorrect. Examples of such errors in generation are discussed in Appendix [E.](#page-24-2) We believe that errors at this scale are acceptable considering the other advantages of the framework and can be factored into the evaluation in future studies.

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**535 536 537 538 539 Adaptability.** While we have shown how we implemented CHASE on three different domains, it is not trivial to adapt the framework to other tasks. Although the high level ideas behind CHASE are easy enough to follow, it takes multiple trials and errors to design a working pipeline for any given task. However, we are optimistic that advances in LLMs' abilities to more precisely follow instructions will make such pipelines easier to construct in the future.

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#### A ROADMAP

 

The appendix is organized as follows.

- In Section [B,](#page-18-0) we provide the implementation details for our experiments.
- In Section [C,](#page-20-0) we discuss some additional experimental results.
- In Section [D,](#page-22-0) we discuss some additional related work.
- In Section [E,](#page-24-2) we analyze errors made by LLMs while generating and solving CHASE benchmarks.
- In Section [F,](#page-24-1) we provide the exact prompts used in this work.

# <span id="page-18-0"></span>B IMPLEMENTATION DETAILS

 Our code is implemented in PyTorch [\(Paszke et al., 2019\)](#page-14-3) and makes use of the HuggingFace Transformers library [\(Wolf et al., 2020\)](#page-16-5) and the vLLM library [\(Kwon et al., 2023\)](#page-13-6) for running efficient inference locally on LLMs. All experiments with open models were done on our cluster with NVIDIA A6000 GPUs with 48 GB memory. Experiments using GPT-4o and GPT-4o-mini were carried out using the OpenAI API.<sup>[2](#page-18-1)</sup>. Experiments using Gemini-1.5-Pro and Gemini-1.5-Flash were carried out using the Google AI Studio.<sup>[3](#page-18-2)</sup> Experiments with Claude-3.5-Sonnet and Claude-3-Haiku were carried out using Anthropic's API.[4](#page-18-3) We provide the exact identifier and version for each LLM we experimented with in Table [4.](#page-18-4)

<span id="page-18-4"></span>Table 4: Model identifiers for the 17 models we studied in our work. Models that are openly available are provided with links to their corresponding pages on Huggingface Hub.



 <https://platform.openai.com>

<https://aistudio.google.com>

<span id="page-18-3"></span><span id="page-18-2"></span><span id="page-18-1"></span><https://console.anthropic.com>

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**1076 1077 1078 1079** Cost of creation. In Table [5,](#page-19-1) we report the estimated cost of creating the three benchmarks, both in terms of inference time and API expenses. Note that the inference time assumes sequential execution of each part of the pipeline with only one process running at a time. Hence, the generation can be made considerably faster with increased parallelism. This table does not include the cost of other experiments in the paper nor does it include the cost of background experiments that went into designing the pipelines. We estimate the total of these costs to be over \$1000 USD.



<span id="page-20-1"></span>**1080 1081** Table 6: Comparison of model performances (pass@1) on CHASE-CODE and HumanEval, a widelyused benchmark for code generation.

#### <span id="page-20-0"></span>**1108** C ADDITIONAL RESULTS AND DISCUSSION

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#### **1111** C.1 COMPARISON OF MODEL PERFORMANCES ON SIMILAR DATASETS

**1113 1114 1115 1116 1117 1118 1119 1120** CHASE-QA consists of long-context realistic-situation-based information-seeking QA problems. The most similar benchmarks are Loong [\(Wang et al., 2024b\)](#page-16-6), which consists of long-context QA problems requiring reasoning over documents (more than 100k tokens long) from domains such as academic papers and financial reports, and LooGLE [\(Li et al., 2024b\)](#page-13-8), which consists of longdependency QA problems over wikipedia and movie scripts (around 32k tokens context). The best performing models on these datasets achieve scores of around 53% and 54% respectively. The best performing model on CHASE-QA achieves a score of around 63%, which reduces to around 55% when we scale the context size to comparable levels of 30k tokens.

**1121 1122 1123 1124 1125 1126 1127 1128** CHASE-CODE consists of repository-level code generation problems. HumanEval [\(Chen et al.,](#page-11-0) [2021\)](#page-11-0) is the most widely-used challenging code generation benchmark. We compare the performances of all models on both datasets in Table [6.](#page-20-1) We can clearly see that CHASE-CODE is a much more challenging benchmark. Recently, some repository-level code benchmarks have also been proposed. SWE-Bench [\(Jimenez et al., 2024\)](#page-12-6) is a benchmark of around 2300 software engineering problems compiled from GitHub issues in popular repositories. EvoCodeBench [\(Li et al., 2024a\)](#page-13-9) consists of 275 repository-level code generation problems based on popular GitHub repositories. The best performing models on these benchmarks achieve around 42% and 20% scores respectively.

**1129 1130 1131 1132 1133** CHASE-MATH consists of grade-school level math word problems. The most widely-used challenging benchmark for this task is GSM8k [\(Cobbe et al., 2021\)](#page-11-1), comprising of 1319 examples. We compare the performances of all models on both datasets in Table [7.](#page-21-0) It is clear that GSM8k has mostly become saturated, with many state-of-the-art models achieving more than 90% accuracies. In comparison, CHASE-MATH is still very difficult for all models to solve. Moreover, the differences in performance between different models is much larger, which enables more confident comparison.



<span id="page-21-0"></span>**1134 1135 1136** Table 7: Comparison of model performances on CHASE-MATH and GSM8k, a widely-used benchmark for grade-school level math word problem solving.

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# C.2 ALTERNATIVE METRICS OF EVALUATION FOR CHASE-QA

**1163 1164 1165 1166 1167 1168 1169 1170 1171 1172** The metric of accuracy for CHASE-QA punishes models for not being concise and generating too many answer points that are not a part of the ground-truth answer. In this section, we present our experimental results with other softer evaluation metrics. We adapt two metrics that have been used by previous works for open-domain question answering [\(Adlakha et al., 2022\)](#page-10-4): (1) **K-Precision**, which for a particular example, evaluates whether all of the answer points in the model's prediction are discussed in the documents, and  $(2)$  **Recall**, which evaluates whether all the ground truth answer points are a part of the model's prediction. K-Precision is used to measure the *faithfulness* of the model's prediction to the provided documents. Recall is used to measure the *correctness* of the model's prediction compared to the ground-truth. We define both the metrics as binary per example. Similar to how we calculated accuracy, we use GPT-4o as a judge with the prompts provided in Figure [21](#page-40-1) and Figure [22](#page-41-0) respectively. The results are provided in Table [8.](#page-22-1)

**1173 1174 1175 1176 1177 1178** Note that the errors in CHASE-QA pertain to the cases where the ground-truth answer may not completely encompass all the relevant information about the question that is mentioned in the documents. We believe that comparisons of models on the basis of recall is relatively less affected by the presence of such errors. This is because if a model has comparatively lesser recall, that means that it generated more responses where it did not include the ground-truth information (irrespective of whether it generated any extra relevant information for the question that is not in the ground truth).

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#### **1180 1181** C.3 EFFECT OF PROMPT FOR SOLVING CHASE-MATH

**1182 1183 1184 1185 1186 1187** Considering the fact that CHASE-MATH is built by increasingly concatenating problems, we experiment with solving it using a different prompt format that explicitly instructs the model to process one sentence at a time, from the first to the last until it arrives at the final answer. We also illustrate this methodology in the prompt using 8 problems different from the original chain-ofthought prompt examples. Each of these new problems have a much higher reasoning depth. The prompt is provided in Figure [32.](#page-50-0) The results for 3 different models are shown in Table [9.](#page-22-2) While there is a clear increase in performance for all models, the task still remains difficult to solve, in general.



<span id="page-22-1"></span>**1188 1189 1190** Table 8: Measuring performance of all models on CHASE-QA with alternative soft metrics, K-Precision and Recall.

<span id="page-22-2"></span>Table 9: Effect of prompt (see Figure [32\)](#page-50-0) that explicitly instructs the model to solve CHASE-MATH problems by processing one sentence at a time.



Examples of errors made by models even with this better prompting technique are provided in Figure [8](#page-29-0) and Figure [9.](#page-30-0)

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# <span id="page-22-0"></span>D ADDITIONAL RELATED WORK

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# D.1 SYNTHETIC DATA GENERATION

**1233 1234 1235 1236 1237 1238 1239 1240 1241** Early works explored the potential of pretrained generative language models such as BERT [\(Devlin](#page-12-7) [et al., 2019\)](#page-12-7), GPT2 [\(Radford et al., 2019\)](#page-14-4), and GPT-3 [\(Brown et al., 2020\)](#page-11-7) to generate datasets for fine-tuning (Schick & Schütze, 2021; [Ye et al., 2022\)](#page-17-5) or for data augmentation [\(Kumar et al., 2020;](#page-13-10) [Yoo et al., 2021\)](#page-17-6). With increasingly powerful LLMs [\(Ouyang et al., 2022;](#page-14-5) [OpenAI Team et al.,](#page-14-0) [2024\)](#page-14-0) being released in recent years combined with the benefits obtained from instruction fine-tuning [\(Wei et al., 2022a;](#page-16-7) [Chung et al., 2024\)](#page-11-8), the focus has shifted more towards generating synthetic instructions data. [Honovich et al.](#page-12-4) [\(2023\)](#page-12-4) and [Wang et al.](#page-16-0) [\(2023\)](#page-16-0) prompt GPT-3 with seed examples to automatically generate a large set of diverse tasks. [Xu et al.](#page-16-1) [\(2024\)](#page-16-1) introduced the *Evol-Instruct* pipeline to generate more complex examples from a given seed example. [Mukherjee et al.](#page-14-6) [\(2023\)](#page-14-6) leverage explanation traces from GPT-4 to create a large synthetic instruction-tuning dataset for

**1242 1243 1244** fine-tuning smaller LLMs. [Mitra et al.](#page-14-7) [\(2024\)](#page-14-7) design an agentic framework that uses raw text and code data as seeds to generate large scale synthetic data of prompts and responses.

**1245 1246 1247 1248 1249 1250 1251** Apart from synthetic instructions datasets, there has also been interest in using synthetic data for pre-training. [Gunasekar et al.](#page-12-1) [\(2023\)](#page-12-1) and [Ben Allal et al.](#page-11-2) [\(2024\)](#page-11-2) generate high-quality textbooks for pre-training small LLMs to unlock better reasoning performance. Recent works [\(Bai et al., 2022;](#page-10-0) [Lee et al., 2024\)](#page-13-1) have also explored using synthetic preference data for aligning language models. Synthetic data has started to become a major component in the post-training development phase of contemporary LLMs [\(Llama Team et al., 2024\)](#page-13-0) to improve their reasoning capabilites. For a comprehensive discussion of major ideas and issues in synthetic data generation, we refer the reader to [Liu et al.](#page-13-11) [\(2024b\)](#page-13-11)'s survey.

- **1252**
- **1253 1254** D.2 SYNTHETIC DATA FOR CODE GENERATION, AND MATH REASONING

**1255 1256 1257 1258** There has been significant recent interest in generating synthetic data for code. [Wen et al.](#page-16-8) [\(2024\)](#page-16-8) utilize I/O specification apart from synthetic intents to generate data science code instructions. [Patel](#page-14-8) [et al.](#page-14-8) [\(2024\)](#page-14-8) generate code library specifications using GPT-4 to evaluate whether LLMs can learn new code libraries in-context.

**1259 1260 1261 1262 1263 1264 1265 1266 1267** Generating synthetic data to improve math reasoning has also been a very active area of research. [Tang et al.](#page-15-6) [\(2024\)](#page-15-6) explored extracting topics and knowledge from math problems to prompt an LLM to generate new data. [Toshniwal et al.](#page-15-7) [\(2024\)](#page-15-7) create an instruction-tuning dataset by synthesizing code-interpreter style solutions for existing math problems using open-source LLMs. [Yang et al.](#page-16-9) [\(2024b\)](#page-16-9) create a reverse socratic approach to synthesize math problems from optimization scenarios. [Luo et al.](#page-13-12) [\(2023\)](#page-13-12) generate diverse math instructions data using *Evol-Instruct* and then train LLMs using reinforcement learning. [Yue et al.](#page-17-0) [\(2024\)](#page-17-0) build an instruction-tuning dataset by using GPT-4 to generate hybrid CoT and PoT rationales for examples from diverse math datasets. [Yu et al.](#page-17-1) [\(2024a\)](#page-17-1) bootstrap problems from existing math datasets by using an LLM to rephrase the question text.

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**1269** D.3 HUMAN-CURATED EVALUATION BENCHMARKS

**1271 1272 1273 1274 1275 1276 1277 1278 1279** Question Answering. There have been numerous context-grounded question answering benchmarks proposed in the past. These include SQuAD [\(Rajpurkar et al., 2016;](#page-14-9) [2018\)](#page-15-8), HotpotQA [\(Yang](#page-16-10) [et al., 2018\)](#page-16-10), DROP [\(Dua et al., 2019\)](#page-12-8), HAS-QA, Qasper [\(Dasigi et al., 2021\)](#page-11-9), [\(Pang et al., 2019\)](#page-14-10) TopioCQA [\(Adlakha et al., 2022\)](#page-10-4), NovelQA [Wang et al.](#page-15-9) [\(2024a\)](#page-15-9), and RepliQA [\(Monteiro et al.,](#page-14-11) [2024\)](#page-14-11). Different from these works, we focus on extremely long contexts, with documents containing a total of more than 10,000 tokens. Another important aspect of our work is that all the documents that make up the context for an example are generated by an LLM from scratch, which reduces contamination risk. Moreover, our questions are designed to simulate everyday queries that users might ask an LLM-based agent. Correspondingly, the annotated ground-truth answers are at times very verbose, which make them impossible to objectively evaluate using automated metrics.

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**1281 1282 1283 1284 1285 1286 1287 1288 1289 1290 1291 1292 1293 1294 1295** Long Context Reasoning. [Kamradt](#page-12-9) [\(2023\)](#page-12-9) introduced the Needle-In-a-Haystack (NIH) task in which a model is asked to retrieve a fact placed in a long context. However, this only assessed surface-level long-context retrieval abilities without much reasoning. In the past few months, many more long-context understanding benchmarks have been created. SCROLLS [Shaham et al.](#page-15-10) [\(2022\)](#page-15-10) and ZeroScrolls [\(Shaham et al., 2023\)](#page-15-11) are long-context benchmarks created by aggregating and repurposing existing datasets. Compared to the QA datasets in ZeroScrolls which consist of contexts based on science and literature, CHASE-QA focuses on real-world scenarios where a user is looking for information across multiple documents. Many benchmarks such as LongBench [\(Bai](#page-10-5) [et al., 2024\)](#page-10-5), RULER [\(Hsieh et al., 2024\)](#page-12-10), L-Eval [\(An et al., 2024\)](#page-10-6), LooGLE [\(Li et al., 2024b\)](#page-13-8) and InfiniteBench [\(Zhang et al., 2024b\)](#page-17-7) consist of long-context QA tasks. However, the relevant information for answering the question is comparatively much more centralized in the context, surrounded by distracting information. In contrast, the relevant information in CHASE-QA is spread across multiple documents. Moreover, the irrelevant information in the other documents is still very closely related to the topics of the question, thereby making the task very difficult. Perhaps, the benchmark most similar to our work is Loong [\(Wang et al., 2024b\)](#page-16-6). Like CHASE-QA, Loong also has evidences for answering questions scattered across a long context of documents. Unlike our benchmark, however, every document in Loong is known to be relevant for answering the question. **1296 1297 1298 1299 1300 1301** In contrast CHASE-QA models the more realistic scenario of searching a bunch of documents that are on very closely related topics, only some of which contain the answer. Moreover, unlike all these prior works, we create long-context reasoning benchmarks completely from scratch in which the long text contexts are also generated using LLMs. Further note that in contrast to these prior works that use manual annotation, our approach is highly scalable, capable of creating thousands of examples across diverse domains automatically in a much more cost-efficient manner.

<span id="page-24-2"></span>**1302**

**1303 1304** E ERROR ANALYSIS

**1305 1306** We provide examples for two types of errors, those made while solving the benchmarks, and those made while generating the benchmarks.

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**1308 1309** E.1 ERRORS MADE WHILE SOLVING CHASE BENCHMARKS.

**1310 1311 1312 1313 1314** Figure [5](#page-26-0) provides an example of an error made by Gemini-1.5-Pro on a problem from CHASE-QA. The model fails to mention two important points relevant for answering the question, which have been discussed in the documents. This provides a qualitative example of how even the most powerful models are unable to properly pay attention to all parts of a long-context and may miss some important information.

**1315 1316 1317 1318 1319 1320** Figure [6](#page-27-0) provides an example of an error made by Gemini-1.5-Pro in generating the correct code for a problem in CHASE-CODE. The model generates most of the code correctly, but for a particular objective, it gets confused in choosing to call the right helper function from the long-context code repository. This example qualitatively illustrates that doing well on this task requires not only a good understanding of the user-specified objectives, but also requires an in-depth understanding of all parts of the code repository.

**1321 1322 1323 1324** Figure [7](#page-28-0) provides an example of an error made by Gemini-1.5-Pro in solving a math word problem from CHASE-MATH. The model executes most of the reasoning steps correctly but fails at the last one. This example qualitatively shows how even state-of-the-art LLMs start to struggle when we scale up the reasoning depth of such types of problems.

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**1326** E.2 ERRORS MADE IN THE GENERATION PROCESS WHEN USING CHASE.

**1328 1329 1330 1331 1332 1333 1334** In Figure [10,](#page-31-0) we show an error made in the generation process of CHASE-QA by GPT-4o. In the document generation stage, the model generated a document which contained extra information that was directly relevant for answering the given question but was not included in the ground-truth answer. This is also a failure case of our verification engine (the one that uses the prompt in Figure [17\)](#page-38-0) which failed to detect the presence of this extra relevant information in the generated document. We believe such errors can be further reduced by using an ensemble of verifiers to carry out each verification task.

**1335 1336 1337 1338** Figure [11](#page-32-0) provides en example of an error made by GPT-4o-mini while generating the CHASE-MATH benchmark. The model's generated answer did not correspond to its generated problem. This is also a failure for both the generator and verifier. Such failures may be reduced by using an ensemble of stronger LLMs for verification instead.

- <span id="page-24-1"></span>**1339 1340** F PROMPTS
- **1342** F.1 PROMPTS FOR CHASE-QA

**1343 1344** In this section, we outline the exact prompts for all experiments related to CHASE-QA:

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<span id="page-24-0"></span>**1341**

- Generating scenarios: Figure [12](#page-33-0)
- Generating QA pairs: Figure [13](#page-34-0)
- Generating irrelevant information: Figure [14](#page-35-0)
- Generating documents: Figure [15](#page-36-0)
	- Verifying irrelevant information: Figure [16](#page-37-0)

<span id="page-25-1"></span><span id="page-25-0"></span>

# <span id="page-26-0"></span>Error Analysis: Solving CHASE-QA - Gemini-1.5-Pro

Question: What are the regulations and financial support options available for starting an artisanal cheese-making business in Vermont?

## Ground-truth Answer:

- Obtain a Dairy Processing License from the Vermont Agency of Agriculture, Food & Markets.

- Adhere to the Vermont Department of Environmental Conservation's (VT DEC) regulations regarding wastewater management.

- Apply for the Vermont Economic Development Authority (VEDA) Entrepreneurial Loan Program for startup financing.

- Comply with the Vermont Department of Taxes' requirements for sales and use tax on dairy products.

- Secure a Vermont Working Lands Enterprise Initiative Grant for equipment and facility improvement.

### Irrelevant Information:

- Obtain a Microbrewery License from the New York State Liquor Authority (NYSLA). - Adhere to the New York State Department of Environmental Conservation (NYSDEC) regulations regarding waste disposal.

[Redacted]

### Prediction:

- Comply with the Vermont Department of Taxes' requirements for sales and use tax on dairy products, including registering for a sales tax permit, tracking sales, and remitting collected tax. (Document 10)

- Adhere to the Vermont Department of Environmental Conservation's (VT DEC) regulations regarding wastewater management, ensuring waste byproducts are treated and disposed of properly to prevent water contamination. (Document 13)

- Obtain a Dairy Processing License from the Vermont Agency of Agriculture, Food & Markets. (Document 12)

## LLM Evaluation:

Result: False. The prediction is missing two main points from the ground-truth answer: 1. Applying for the Vermont Economic Development Authority (VEDA) Entrepreneurial Loan Program for startup financing.

2. Securing a Vermont Working Lands Enterprise Initiative Grant for equipment and facility improvement.

These are crucial financial support options that are not mentioned in the prediction.

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**1452 1453 1454** Figure 5: Example of error made by Gemini-1.5-Pro on CHASE-QA. The GPT-4o judge correctly evaluates the prediction to be wrong because it fails to mention some major points from the groundtruth answer which were discussed in the documents.

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<span id="page-27-0"></span> Error Analysis: Solving CHASE-CODE (Algorithms) - Gemini-1.5-Pro Objectives: [Redacted] - For each coordinate from the previous sub-goal, calculate the Manhattan distance from the origin (0,0) for the interesting cells found, returning a list of tuples. Ground-truth Answer Code: import numpy as np from matrix\_decomposition import svd\_reconstruction from entity\_extractor import extract\_entities from meeting\_scheduling import can\_schedule\_meetings from grid\_analyzer import high\_value\_coordinates def complex\_analysis(matrix, k, text, entities, intervals, threshold): reconstructed\_matrix = svd\_reconstruction(matrix, k) extracted\_entities = extract\_entities(text, entities) can\_schedule = can\_schedule\_meetings(intervals, 0) interesting\_cells = high\_value\_coordinates(reconstructed\_matrix , threshold) interesting\_cells\_with\_distances =  $[((i, j), abs(i) + abs(j))$ for  $((i, j), ...)$  in interesting\_cells] return reconstructed\_matrix, extracted\_entities, can\_schedule, interesting\_cells\_with\_distances Predicted Code: import numpy as np from matrix\_decomposition import svd\_reconstruction from entity\_extractor import extract\_entities from meeting\_scheduling import can\_schedule\_meetings from matrix\_analyzer import find\_interesting\_cells def complex\_analysis(matrix, k, text, entities, intervals, threshold): reconstructed\_matrix = svd\_reconstruction(np.array(matrix), k) extracted\_entities = extract\_entities(text, entities) can\_schedule = can\_schedule\_meetings(intervals, 0) interesting\_cells = find\_interesting\_cells(reconstructed\_matrix , threshold) interesting\_cells\_with\_distances = [((row, col), abs(row) + abs (col)) for row, col in interesting\_cells] return reconstructed\_matrix, extracted\_entities, can\_schedule, interesting\_cells\_with\_distances

Figure 6: Example of error made by Gemini-1.5-Pro on an example from the *algorithms* split of CHASE-CODE. The prediction incorrectly calls the find interesting cells helper function (see line number 11) which does not calculate manhattan distances as requested by the objective.

 

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# <span id="page-28-0"></span>Error Analysis: Solving CHASE-MATH - 8-shot chain-of-thought - Gemini-1.5-Pro

## Question:

Harry slept 9 hours last night. His friend James slept only 2/3 of what Harry slept. After their sleep, Harry decided to wake up early and went for a jog. He invited James to join him, and they jogged for 4 times the additional hours Harry slept compared to James. They both felt energized and decided to go for breakfast, where they calculated the total hours they spent jogging. After their breakfast, Harry and James sat down to review their fitness goals. They discussed their jogging session and decided it would be beneficial to repeat such sessions. However, they wanted to gauge how many smaller jogging sessions equal the time they previously spent jogging. James suggested that they break down their jogging time into segments of 3 hours to see how many complete segments they can fit within their total jogging time. After evaluating their jogging goals, Harry and James decided to increase the duration of their future jogging sessions. They considered adding an additional hour to each segment to further enhance their fitness regimen, while keeping the same total jog time of all sessions combined. After successfully completing their new jogging regimen for a month, Harry and James noticed that their stamina had increased significantly. They decided to celebrate this achievement by doubling their number of sessions for the future. They planned to increase from their current number of complete sessions to a total that is double their current sessions. They are excited to see how their increased devotion to jogging will impact their overall fitness. After a successful month of their increased jogging regimen, Harry and James wanted to keep track of their progress. They decided to add rest sessions into their training schedule to avoid burnout. For every 1/3 of the number of jogging sessions in their regimen, they would incorporate 1 rest session. If they have done 4 rest sessions so far, how many total jogging sessions have they finished?

## Ground-truth Answer:

James slept 9 hours  $*$  2/3 = 6 hours. So, Harry slept 9 - 6 = 3 hours more than James. They jogged for 4 times that amount, so 12 hours together. We then divide 12 by 3 to get 4 complete sessions. Now divide the 12 hours by the new session duration (4 hours) which yields 3 sessions. Doubling that quantity results 6. They add rest sessions for every  $1/3 * 6 = 2$  jogging sessions. So for 4 rest sessions, they have  $4 * 2 = 8$  jogging sessions. #### 8.0

# Prediction:

**1546 1547 1548 1549 1550 1551 1552 1553 1554 1555 1556 1558 1559 1560** Let's break down this problem step-by-step: 1. \*\*James's sleep:\*\* James slept 2/3 of Harry's 9 hours, which is  $(2/3)$  \* 9 = 6 hours. 2. \*\*Additional hours Harry slept:\*\* Harry slept 9 hours - 6 hours = 3 more hours than James. 3. \*\*Jogging time:\*\* They jogged for 4 times the additional hours Harry slept, meaning they jogged for  $4 * 3 = 12$  hours. 4. \*\*Segments of jogging:\*\* They want to break down their jogging time into 3-hour segments, so they have 12 hours / 3 hours/segment = 4 segments. 5. \*\*Increased segment duration:\*\* They increase each segment by 1 hour, making each segment 3 hours  $+ 1$  hour  $= 4$  hours long. 6. \*\*Total sessions:\*\* Since they keep the same total jogging time, they still have 12 hours of jogging. With the new segment length, they have 12 hours / 4 hours/session = 3 sessions. 7. \*\*Doubled sessions:\*\* They double their number of sessions from 3 to 3  $*$  2 = 6 sessions. 8. \*\*Rest sessions and total jog sessions:\*\* They incorporate 1 rest session for every 1/3 of their jogging sessions. Since they've done 4 rest sessions, they have completed 4 rest sessions \* 3 jog sessions/rest session = 12 jogging sessions. The answer is 12.

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**1564 1565** Figure 7: Example of error made in the last step by Gemini-1.5-Pro on an example from CHASE-MATH when prompted with the default 8-shot chain-of-thought.

## <span id="page-29-0"></span>Error Analysis: Solving CHASE-MATH - 8-shot sentence-by-sentence - Gemini-1.5-Pro

### Question:

James decides to run 3 sprints 3 times a week. He runs 60 meters each sprint. After a month of consistent training, James feels he needs to increase his speed. He decides to take a break from sprinting for one week to focus on recovery. During this recovery week, he runs a shorter distance of 30 meters for only 2 sprints, 3 times that week instead. After his recovery week, James feels rejuvenated and ready to resume his training. He decides to continue running but at double the distance he covered during his recovery week for each day the next week, aiming to improve his overall performance. He runs this increased distance for 7 days straight, maintaining consistency every day. After running consistently throughout the week, James notices a small injury starting to develop in his leg. Concerned about this, he decides to cut back on his total running distance for the following week. To ensure he allows for proper recovery and does not worsen the injury, he plans to reduce his total running distance from the prior week by 420 meters. How much distance will James run in the following week after the reduction?

### Ground-truth Answer:

He sprints  $3 * 3 = \langle \langle 3 * 3 = 9 \rangle \rangle 9$  times So he runs  $9 * 60 = \langle \langle 9 * 60 = 540 \rangle \rangle 540$ meters In the recovery week, James runs 2 sprints each day for 3 days, covering 30 meters each sprint. Therefore, the total distance covered during the recovery week is calculated as follows: he runs 2 sprints/day  $*$  3 days = 6 sprints. Then, multiplying by the distance per sprint gives 6 sprints \* 30 meters/sprint = 180 meters. To find out how much less he runs compared to his regular week, we subtract the total distance he runs that week from the distance he typically runs in a week, which is 540 - 180 = 360 meters less. James runs a distance that is double what he covered in the recovery week, which is 180 meters. Therefore, if he runs this doubled distance for 7 days, we first calculate the distance he covers in one day, which is 180 meters  $* 2 = 360$  meters. Over the course of 7 days, the total distance will be 360 meters/day \* 7 days. To find the distance James will run in the following week after reducing his initial total distance by 420 meters, I will need to subtract 420 from the total distance he ran in the previous week, which was 2520.0 meters. Hence, the calculation will be:  $2520.0 - 420 = 2100.0$  meters.  $\# \# \# 2100.0$ 

## **Prediction:**



**<sup>1618</sup> 1619** Figure 8: Example of error made by Gemini-1.5-Pro on an example from CHASE-MATH when prompted with 8-shot sentence-by-sentence solving examples.

<span id="page-30-0"></span>**1620 1621 1622 1623 1624 1625 1626 1627 1628 1629 1630 1631 1632 1633 1634 1635 1636 1637 1638 1639 1640 1641 1642 1643 1644 1645 1646 1647 1648 1649 1650 1651 1652 1653 1654 1655 1656 1657 1658 1659 1660 1661 1662 1663 1664 1665 1666** Error Analysis: Solving CHASE-MATH - 8-shot sentence-by-sentence - Gemini-1.5-Pro Question: Rani has ten more crabs than Monic, who has 4 fewer crabs than Bo. If Bo has 40 crabs, calculate the total number of crabs the three have together. After counting their crabs, Rani, Monic, and Bo decide to share their crabs equally among themselves for a crab feast. However, before they can do that, Rani finds out that they must provide 2 additional crabs to a local aquarium as a donation. After their crab feast, Rani, Monic, and Bo decide to host another gathering for their friends. They plan to invite 5 additional friends to enjoy crabs. Each person, including Rani, Monic, Bo, and their friends, should receive an equal amount of crabs for this new gathering. They go and buy new crabs which are in total 3 times the number of crabs each person ate after the donation. How many crabs did they have altogether to share with the additional friends in the end? Ground-truth Answer: If Bo has 40 crabs, then Monic, who has 4 fewer crabs than Bo, has  $40-4 = \langle \langle 40 - 4 \rangle \rangle$  $36 \gg$  36 crabs. Bo and Monic have a total of  $36+40 = \langle \langle 36 + 40 \rangle = \langle 76 \rangle$  76 crabs. Since Monic has 36 crabs, Rani's number of crabs is  $36+10 = \langle \langle 36+10 \rangle = 46 \rangle$  > > 46. Together, the three have  $76+46 = \langle \langle 76+46=122 \rangle \rangle 122$  crabs. First, calculate how many crabs remain after the donation:  $122 - 2 = 120$ . Now, to find out how many crabs each person will receive, divide the remaining number of crabs (120) by 3, since there are three individuals:  $1203 = 40$ . Since each of them originally ate 40 crabs, if we multiply that number by 3, we calculate the total number of crabs available in the end. ####120.0 Prediction: Sentence 1: Monic has  $40 - 4 = 36$  crabs. Sentence 2: Rani has  $36 + 10 = 46$  crabs. Sentence 3: Bo has 40 crabs. Sentence 4: Together they have  $46 + 36 + 40 = 122$  crabs. Sentence 5: They donate 2 crabs, leaving them with  $122 - 2 = 120$  crabs. Sentence 6: They share the 120 crabs equally, so each person gets  $120 / 3 = 40$  crabs. Sentence 7: They invite 5 more friends, making a total of  $3 + 5 = 8$  people. Sentence 8: They buy new crabs totaling 3 times the number each person ate after the donation, which is  $3 * 40 = 120$  crabs. Sentence 9: Including the 120 crabs they bought and the remaining crabs they shared after donating, they had  $120 + 40*3 = 120 + 120 = 240$  crabs altogether to share with the additional friends. The answer is 240. Figure 9: Example of error made by Gemini-1.5-Pro on an example from CHASE-MATH when prompted with 8-shot sentence-by-sentence solving examples. The model fails to understand that the

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are available to share with the new friends.

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120 crabs they had earlier have already been eaten and that only the new 120 crabs bought in the end

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 Error Analysis: Generating CHASE-QA - GPT-4o Question: Rani has ten more crabs than Monic, who has 4 fewer crabs than Bo. If Bo has 40 crabs, calculate the total number of crabs the three have together. After counting their crabs, Rani, Monic, and Bo decide to share their crabs equally among themselves for a crab feast. However, before they can do that, Rani finds out that they must provide 2 additional crabs to a local aquarium as a donation. After their crab feast, Rani, Monic, and Bo decide to host another gathering for their friends. They plan to invite 5 additional friends to enjoy the remaining crabs. Each person, including Rani, Monic, Bo, and their friends, should receive an equal amount of crabs for this new gathering. They want to figure out how many crabs they have available for their friends while ensuring that each person gets an equal share. If they multiply the number of crabs each had after the donation by 3, how many crabs did they have altogether to share with the additional friends? Ground-truth Answer: If Bo has 40 crabs, then Monic, who has 4 fewer crabs than Bo, has  $40-4 = \langle \langle 40 - 4 \rangle \rangle$  $36 >$  36 crabs. Bo and Monic have a total of  $36+40 = \langle \langle 36 + 40 \rangle \rangle = 76 >$  76 crabs. Since Monic has 36 crabs, Rani's number of crabs is  $36+10 = \langle \langle 36+10=46 \rangle \rangle$  46. Together, the three have  $76+46 = \langle \langle 76+46=122 \rangle \rangle 122$  crabs. First, calculate how many crabs remain after the donation:  $122 - 2 = 120$ . Now, to find out how many crabs each person will receive, divide the remaining number of crabs (120) by 3, since there are three **individuals**:  $120 \div 3 = 40$ . Since each of them originally received 40 crabs, if we multiply that number by 3 individuals (Rani, Monic, and Bo), we calculate the total number of crabs available for sharing. ####120.0 Figure 11: Example of an error made in the generation process of CHASE-MATH. The reasoning in the answer wrongly considers the number of people for which to divide crabs to be 3 while the context has added new information that there are 5 additional friends to consider.

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<span id="page-33-0"></span>

<span id="page-34-0"></span> CHASE-QA: Generating QA Pairs System Prompt: You are an expert generator of data. Do not use \*\* to start lines or denote points. You are a research scientist. You want to make data to test an advanced question answering system. Give me an example question and corresponding answer that a  $\{ \text{USER\_PERSONA} \}$  may ask that compulsorily requires searching a  ${COLLECTION \cdot OF\_DOCS}$ . Make questions that cannot be answered directly with general knowledge but necessarily require some uncommon information that is present in some documents. The answer must be very specific and written in bullet points, so that it is easier to objectively evaluate. Depending on the question, the answer can have anything between 3-6 bullet points without any sub-points. The answer to the question you create must be scattered across different documents (at least 3). Assign each point of the answer to a specific document in which that point will be discussed. You may assign multiple points to the same document, but each point must only be assigned to a single document. You must state the title and answer points assigned for each of the documents. Answer in the following format: Question: <Question> Answer: <Answer> Document 1 Title: <Title> Document 1 Answer points assigned: <Points> Document 2 Title: <Title> Document 2 Answer points assigned: <Points> and so on...

Figure 13: Programmatic prompt for generating question-answer pairs for CHASE-QA.

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<span id="page-36-0"></span>

Figure 15: Programmatic prompt for generating documents for CHASE-QA.

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# <span id="page-38-0"></span> CHASE-QA: Verifying Absence of Relevant Information System Prompt: You are an expert at verifying data. You are given a document followed by a question and some answer points. You must check whether there are any additional major points in the document that provide relevant information for answering the question that are currently missing from the answer. Follow these instructions: 1. Do not look for exact phrases or explicit mentions since the answer can have points that are a paraphrase of the same broad information. 2. It is ok if the document provides more specifics or details about the points already in the answer or if it discusses them in more depth by introducing related information so you can ignore that. 3. Check if the document introduces a new "major" idea or point that is crucial for answering the question and is not at all mentioned in the answer and is not an extension of the existing points in the answer. 4. Your job is not to check if the question can be sufficiently answered. You should ignore if the document or answer points are missing any points that are needed in the answer to the question. If the document is not introducing major new points pertaining to the answer, output "False" to "Presence of Extra Points" without giving any explanation. Otherwise, if and only if the document discusses major additional points that are necessary to answer the question, output "True" and mention only the extra major points discussed. Document: {Document} Question: {QUESTION} Answer Points: {ANSWER} Give output in the following format: Presence of Extra Points: True/False Extra Points Mentioned (if any):

 Figure 17: Programmatic prompt for verifying absence of relevant information in the documents for CHASE-QA.

 

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<span id="page-39-0"></span>Answering the question correctly requires information from multiple documents. You must only generate the points necessary for answering the question, without mentioning anything irrelevant to the question. If you find no relevant information in the documents for answering the question, you must only generate "No relevant information found in the documents." and nothing else.

Documents: {DOCUMENTS}

Question: {QUESTION}

Answer:

Figure 19: Programmatic prompt for solving examples in CHASE-QA.

 

# <span id="page-40-0"></span>CHASE-QA: LLM-as-a-Judge for Calculating Accuracy

## System Prompt: You are an expert evaluator.

You are given a question, irrelevant answers, the ground-truth answer, and a prediction. You need to evaluate whether the prediction is correct by matching against the ground truth answer. Do not look for exact phrases or words since the prediction can have points that are a paraphrase of the same information. Based on the question, check for the presence of the same ideas or main points in the prediction as in the ground-truth answer. All the main points in the ground-truth answer must be mentioned in the prediction. The order of points mentioned is irrelevant. It is allowed for the prediction to elaborate or provide more specifics or details over the major points in the ground-truth answer. However, the prediction should not contain additional major points that are contradictory or irrelevant for answering the question. Importantly, the prediction must not discuss any of the points mentioned in the "irrelevant answers". The first word in your response must be either True or False. If False, explain why you think the prediction is wrong in detail.

Question: {QUESTION}

Irrelevant Answers: {IRRELEVANT ANSWERS}

Ground-truth Answer: {GROUND TRUTH ANSWER}

Prediction: {PREDICTION}

Result:

Figure 20: Programmatic prompt for evaluating accuracy of predictions of models for problems in CHASE-QA.

# <span id="page-40-1"></span>CHASE-QA: LLM-as-a-Judge for Calculating K-Precision

System Prompt: You are an expert evaluator.

You are given a question, an answer written in points, and some documents. You need to check whether the information in the answer points is discussed in the documents in a manner such that it can be used to at least partially answer the question. You do not need to think about the overall correctness of the answer points, just check whether or not a particular answer point is discussed in the documents. Your goal is to calculate precision, i.e., the percentage (out of 100) of answer points that have been adequately mentioned in the document. The first thing in your response must be "Precision: " followed by the precision value in decimal form. If precision is less than 100%, explain which answer points are not present in the document.

Documents: {DOCUMENTS}

Question: {QUESTION}

Answer Points: {ANSWER\_POINTS}

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**2211**

CHASE-QA.

Result:

**<sup>2212</sup> 2213** Figure 21: Programmatic prompt for evaluating K-Precision of predictions of models for problems in

## <span id="page-41-0"></span>CHASE-QA: LLM-as-a-Judge for Calculating Recall

System Prompt: You are an expert evaluator.

You are given a question, a statement, and some reference points. You need to check whether the information in the statement is discussed in the reference points in a manner such that it can be used to at least partially answer the question. It is okay if the reference points contain a lot more information, your goal is to only check whether the statement is included in the reference points. The first word in your response must be either True or False. If False, explain why in detail.

Question: {QUESTION}

Statement: {STATEMENT}

Reference Points: {REFERENCE POINTS}

Result:

Figure 22: Programmatic prompt for evaluating recall of predictions of models for problems in CHASE-QA.

<span id="page-42-0"></span> CHASE-CODE: Generating Helper Functions System Prompt: You are an expert generator of code data. You are a research scientist. You want to make data to test an advanced code generation system. You are given a domain. Assume that there is a large python code base 'C' with at least 10 python files on that domain. Domain: {DOMAIN} You need to create 5 functions in this codebase for achieving various objectives. First define the parameters that will be input to the function. Then define the objective of the function. The objective must consist of 3-4 sub-goals, each of which must involve complex logic that make it very difficult to implement the function. However, each sub-goal must be well-specified such that there is only one way to implement the sub-goal. Then based on the objective, you need to create a single function (do not create other functions inside this). Some examples are: Parameters: - data: pandas.DataFrame - k: int Objectives: - In the dataframe "data", find the "frequency" of occurence of rows that have at least one string field with the number of letters divisible by "k". [redacted] Function "filter k frequency" in file "string filters.py": import pandas as pd def filter\_k\_frequency(data, k): [redacted] return frequency, filtered\_df Now you need to create 5 unique, diverse, and complex functions. Answer in the following format: Function <Number>: Parameters: - <para name>: <data type> ... Objectives:  $<sub>sub_g</sub>$ goal $>$ </sub> ... Function "function\_name" in file "file\_name.py": <import statements> <function definition> Figure 23: Prompt for generating helper functions for CHASE-CODE.

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Figure 25: Programmatic prompt for generating the test code for CHASE-CODE.



# <span id="page-45-0"></span>CHASE-CODE: Verifying if Function Executes

System Prompt: You are an expert tester of code systems.

You are given a function in a file. You need to check whether the function correctly executes.

{FUNCTION}

Follow these instructions:

1. You must output only a single long python code.

2. First initialize the input parameters for the function in python code. If the function reads data from files, you should create and store the necessary files with sample data in the corresponding filepath in the python code.

3. Finally, call the function with the input parameters.

Give output in the following format:

```
1 # Import statements if required
2 import <>
3 \cdot \cdot \cdot4
5 # Import function from file
6 from <filename> import <function_name>
8 # Initialize input parameters
9 <param1> = <value1>
10 ...
11
12 # Call function with input parameters
13 return_<variable1>, return_<variable2>, ... = <function_name>(<
     param1>, \langleparam2>, ...)
```
Figure 26: Programmatic prompt for generating the test code for verifying if a function executes correctly for CHASE-CODE.

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Figure 27: Programmatic prompt for verifying if the problem statement sufficiently specifies the answer code for CHASE-CODE.

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<span id="page-47-0"></span> CHASE-CODE: Solving the Task System Prompt: You are an expert programmer. You must output only python code. You are given a codebase. You need to write a single python function to achieve the objectives specified in the problem statement. In your function, you should call some of the functions in the codebase to achieve specific objectives. Do not give any examples of usage or any explanations. Codebase: {CODEBASE} Problem Statement: {PROBLEM STATEMENT} Give output in the following format: # Import statements if required import <> ... # Import necessary helper functions from their files from <filename> import <function\_name> # Define the function 9 def <function\_name>(<param1>, <param2>, ...): # Your code here ... 13 return <return\_variable>

Figure 28: Programmatic prompt for solving examples in CHASE-CODE.

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```
Context: {CONTEXT}
Question statement: {QUESTION STATEMENT}
Answer: {ANSWER}
Answer statement: {ANSWER_STATEMENT}
```

```
You need to further continue the problem over the answer quantity, by introducing a scenario
and new question where you need to perform one more operation (such as +, \cdot, \cdot, *, etc.)
over this quantity to get the final answer. Crucially, the new context must not mention the
original answer - it still has to be inferred based on previous information. Do not make any
calculation or inference in the new context. Try to make the new context challenging. Also
provide a complete reasoning of how you reached the new answer (never round down or
round up decimals).
```
advanced math reasoning system. For that, you are given the following problem:

```
Give output in the following format only:
New operation over original answer: <>
New context [Do not mention original answer]: <>
New question statement: <>
New answer reasoning: <>
New answer [Number only]: <>
```
**2642 2643 2644**

**2645**

<span id="page-48-1"></span>**2621**

**2593 2594**

**2597**

Figure 30: Programmatic prompt for extending the seed MWP for CHASE-MATH.

# <span id="page-49-0"></span>CHASE-MATH: Solving MWP - 8-shot chain-of-thought

System Prompt: You are an expert mathematician. Your final statement must be of the form 'The answer is  $\langle$  answer $\rangle$ '.

**2656 2657 2658 2659 2660 2661 2662 2663 2664 2665 2666 2667 2668 2669 2670 2671 2672 2673 2674 2675 2676 2677 2678 2679 2680 2681 2682 2683 2684 2685 2686 2687 2688 2689 2690 2691 2692** Solve the final math word problem given below by thinking step-by-step. You should always work with exact numbers - never round down or round up decimals based on context. Give the final answer in the end by saying "The answer is  $\langle$  number $\rangle$ ". Q: There are 15 trees in the grove. Grove workers will plant trees in the grove today. After they are done, there will be 21 trees. How many trees did the grove workers plant today? A: There are 15 trees originally. Then there were 21 trees after some more were planted. So there must have been  $21 - 15 = 6$ . The answer is 6. Q: If there are 3 cars in the parking lot and 2 more cars arrive, how many cars are in the parking lot? A: There are originally 3 cars. 2 more cars arrive.  $3 + 2 = 5$ . The answer is 5. Q: Leah had 32 chocolates and her sister had 42. If they ate 35, how many pieces do they have left in total? A: Originally, Leah had 32 chocolates. Her sister had 42. So in total they had  $32 + 42 = 74$ . After eating 35, they had  $74 - 35 = 39$ . The answer is 39. Q: Jason had 20 lollipops. He gave Denny some lollipops. Now Jason has 12 lollipops. How many lollipops did Jason give to Denny? A: Jason started with 20 lollipops. Then he had 12 after giving some to Denny. So he gave Denny 20 -  $12 = 8$ . The answer is 8. Q: Shawn has five toys. For Christmas, he got two toys each from his mom and dad. How many toys does he have now? A: Shawn started with 5 toys. If he got 2 toys each from his mom and dad, then that is 4 more toys.  $5 + 4 = 9$ . The answer is 9. Q: There were nine computers in the server room. Five more computers were installed each day, from monday to thursday. How many computers are now in the server room? A: There were originally 9 computers. For each of 4 days, 5 more computers were added. So  $5 * 4 = 20$  computers were added.  $9 + 20$  is 29. The answer is 29. Q: Michael had 58 golf balls. On tuesday, he lost 23 golf balls. On wednesday, he lost 2 more. How many golf balls did he have at the end of wednesday? A: Michael started with 58 golf balls. After losing 23 on tuesday, he had 58 - 23 = 35. After losing 2 more, he had  $35 - 2 = 33$  golf balls. The answer is 33. Q: Olivia has \$23. She bought five bagels for \$3 each. How much money does she have left? A: Olivia had 23 dollars. 5 bagels for 3 dollars each will be 5 x 3 = 15 dollars. So she has 23 - 15 dollars left. 23 - 15 is 8. The answer is 8. Q: {QUESTION} A:

**2693 2694** Figure 31: Programmatic prompt for solving an example in CHASE-MATH using chain-of-thought.

**2695 2696**

**2697**

**2698**

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**2753** Figure 32: Programmatic prompt for solving an example in CHASE-MATH sentence-by-sentence.