Continual Test-time Adaptation for End-to-end Speech Recognition on Noisy Speech

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Abstract

 Deep learning-based end-to-end automatic speech recognition (ASR) has made signifi- cant strides but still struggles with performance on out-of-domain (OOD) samples due to do- main shifts in real-world scenarios. Test-Time Adaptation (TTA) methods address this issue by adapting models using test samples at infer- ence time. However, current ASR TTA meth- ods have largely focused on non-continual TTA, which limits cross-sample knowledge learn- ing compared to continual TTA. In this work, we propose a Fast-slow TTA framework for ASR, which leverages the advantage of contin- ual and non-continual TTA. Within this frame- work, we introduce Dynamic SUTA (DSUTA), an entropy-minimization-based continual TTA method for ASR. To enhance DSUTA's ro- bustness on time-varying data, we propose a **dynamic reset strategy that automatically de-** tects domain shifts and resets the model, mak- ing it more effective at handling multi-domain data. Our method demonstrates superior per- formance on various noisy ASR datasets, out- performing both non-continual and continual 025 TTA baselines while maintaining robustness to domain changes without requiring domain boundary information.

⁰²⁸ 1 Introduction

 Deep learning-based end-to-end automatic speech recognition (ASR) has made remarkable progress in recent years, achieving low recognition error rates for in-domain samples. However, domain shifts frequently occur in real-world scenarios. Al- though recent large-scale ASR models exhibit some generalization to out-of-domain (OOD) test in- stances, their performance on OOD samples still lags behind that of in-domain samples.

 To address domain shift issues during infer- ence, Test-Time Adaptation (TTA) is an attractive method. It adapts the model using only single or batched test samples without needing the source

Figure 1: Illustration of the proposed Fast-slow TTA framework and dynamic reset strategy with timevarying speech domains. The Fast-slow TTA framework can leverage the advantages of continual and noncontinual TTA, and the dynamic reset strategy automatically detects domain shifts and resets the model to the source model during testing.

training data at testing time. Specifically, TTA **042** adapts the source model through unsupervised ob- **043** [j](#page-8-0)ectives like Entropy Minimization (EM) [\(Wang](#page-8-0) **044** [et al.,](#page-8-0) [2020\)](#page-8-0) or Pseudo-Labeling (PL) [\(Goyal et al.,](#page-8-1) **045** [2022\)](#page-8-1) in inference time. **046**

TTA methods initially gained prominence in the **047** computer vision field. Non-continual TTA meth- **048** ods adapt the source model for each test utterance **049** and reset to the original model for subsequent sam- **050** ples [\(Wang et al.,](#page-8-0) [2020\)](#page-8-0), whereas Continual TTA **051** (CTTA) continuously adapts the model for target **052** domains, leveraging knowledge learned across sam- **053** ples to improve performance [\(Niu et al.,](#page-8-2) [2022a,](#page-8-2)[b;](#page-8-3) **054** [Press et al.,](#page-8-4) [2024\)](#page-8-4). 055

In speech recognition, recent studies have tai- **056** lored TTA methods with entropy-minimization- **057** based optimization [\(Lin et al.,](#page-8-5) [2022;](#page-8-5) [Kim et al.,](#page-8-6) **058** [2023;](#page-8-6) [Liu et al.,](#page-8-7) [2023\)](#page-8-7), proposing various train- **059** ing objectives and demonstrating effectiveness on **060** different datasets. However, existing ASR TTA **061** methods focus on non-continual TTA, limiting the **062** ability to learn knowledge across samples. There **063** is limited research on CTTA for end-to-end ASR. **064** Recently, AWMC [\(Lee et al.,](#page-8-8) [2023\)](#page-8-8) proposed a **065**

 pseudo-labeling CTTA method for ASR on sin- gle test domain. However, as shown in previous work [\(Lin et al.,](#page-8-5) [2022\)](#page-8-5), pseudo-labeling is not as effective as EM-based methods, and its ability on long multi-domain testing data is unknown.

071 In this work, we propose a general **Fast-slow** TTA framework that leverages the advantages of both continual and non-continual TTA. Based on this framework, we introduce an EM-based CTTA 075 method named Dynamic SUTA (DSUTA) for ASR. Furthermore, to enhance the robustness of DSUTA 077 on time-varying domain data, we propose a dy- namic reset strategy to automatically detect do- main shifts and determine when to reset the model to the original source model. This strategy im- proves Fast-slow TTA over long sequences of multi-domain data streams.

 We demonstrate the effectiveness of our method on single-domain and multi-domain time-varying ASR benchmarks under different acoustic con- ditions, simulating real-world changing environ- ments. Our method outperforms the strong single- utterance baseline SUTA [\(Lin et al.,](#page-8-5) [2022\)](#page-8-5) and the CTTA baseline AWMC [\(Lee et al.,](#page-8-8) [2023\)](#page-8-8), showing robustness to domain changes even without know-ing the domain boundaries.

092 Our contributions can be summarized as follows:

- **093** 1. Propose the Fast-slow TTA framework to **094** bridge the gap between continual and non-**095** continual TTA.
- **096** 2. Introduce a specific version of the Fast-slow 097 TTA method named **DSUTA** with a novel dy-**098** namic reset strategy to stabilize CTTA over **099** multi-domain and long test data streams.
- **100** 3. Demonstrate significant improvement over **101** both non-continual and continual baselines **102** on single-domain and time-varying data.

¹⁰³ 2 Related Works

 Non-continual TTA for ASR: non-continual TTA methods adapt the source model for each test ut- terance and reset to the original model for subse- quent samples. SUTA [\(Lin et al.,](#page-8-5) [2022\)](#page-8-5) introduces the first TTA approach for non-autoregressive ASR, based on entropy minimization and mini- mum class confusion. SGEM [\(Kim et al.,](#page-8-6) [2023\)](#page-8-6) extends TTA to autoregressive ASR models by in- troducing a general form of entropy minimization. [Liu et al.](#page-8-7) [\(2023\)](#page-8-7) enhances TTA with confidence-enhanced entropy minimization and short-term

consistency regularization. However, these non- **115** continual TTA methods views each utterance inde- **116** pendently, which only relies on a single utterance **117** and fails to leverage the knowledge across a stream **118** of test samples to improve the adaptation. **119**

Continual TTA: Unlike non-continual TTA, which **120** resets to the source model for each sample, contin- **121** ual TTA enables the online model to use learned **122** knowledge to handle gradual changes in the target **123** domain. However, it may suffer from model col- **124** lapse if adaptation is unstable when the data stream **125** is too long. To improve CTTA's performance and **126** stability, studies in the computer vision field have **127** developed solutions like stochastic model restor- **128** ing [\(Wang et al.,](#page-8-9) [2022\)](#page-8-9), sample-efficiency entropy **129** minimization [\(Niu et al.,](#page-8-2) [2022a\)](#page-8-2), sharpness-aware **130** reliable entropy minimization [\(Niu et al.,](#page-8-3) [2022b\)](#page-8-3), **131** and fixed frequency model reset [\(Press et al.,](#page-8-4) [2024\)](#page-8-4). **132**

In the ASR research, *there are limited stud-* **133** *ies on CTTA ASR.* Recently, AWMC [\(Lee et al.,](#page-8-8) 134 [2023\)](#page-8-8) attempts continual TTA on ASR using **135** a pseudo-labeling approach with an extra an- **136** chor model to prevent model collapse. However, **137** AWMC [\(Lee et al.,](#page-8-8) [2023\)](#page-8-8) only measures the per- **138** formance on single-domain data with the pseudo- **139** labeling method. This work focuses on multi- **140** domain time-varying long data streams. We pro- **141** pose a fast-slow TTA framework and dynamic reset **142** strategy based on an entropy minimization-based **143** CTTA method, which achieves better performance **144** and stability. **145**

3 Methodology **¹⁴⁶**

Section [3.1](#page-1-0) describes the proposed **Fast-slow TTA** 147 framework. Following this framework, Sec- **148** tion [3.2](#page-2-0) extends SUTA into Dynamic SUTA. To **149** handle multi-domain scenarios better, we propose **150** a dynamic reset strategy in Section [3.3.](#page-2-1) **151**

3.1 Fast-slow TTA Framework **152**

Non-continual TTA treats each sample as an inde- **153** pendent learning event. The adaptation process can **154** fit the current sample without affecting future sam- **155** ples; however, the learned knowledge cannot be **156** transferred to future samples. In contrast, continual **157** TTA can utilize the learned knowledge, but fitting **158** the current sample might severely affect TTA per- **159** formance on future samples. For instance, if the **160** model overly fits the current sample and (model 161 collapse), the performance on future samples will **162** significantly degrade with continual TTA, whereas 163

Figure 2: Illustration of the 3 different TTA approaches.

164 in non-continual TTA, the performance remains **165** unaffected.

 We propose Fast-slow TTA, a new CTTA frame- work that leverages learned knowledge while retain- ing the benefits of non-continual TTA, as shown in Figure [2.](#page-2-2) Fast-slow TTA aims to learn meta-**parameters** ϕ_t which evolve slowly over time. In- stead of always starting the adaptation process from the pre-trained parameters, as in non-continual TTA, we start from ϕ_t at time step t. Specifically,

174
$$
\phi_0 = \phi_{pre},
$$

\n175
$$
\widehat{\phi}_t = A(\phi_t, x_t),
$$

\n176
$$
\widehat{y}_t = \widehat{\phi}_t(x_t),
$$

\n177
$$
\phi_{t+1} = U(\phi_t, x_t).
$$

$$
f_{\rm{max}}
$$

$$
\phi_{t+1} = U(\phi_t, x_t),
$$

178 where ϕ_{pre} are the pre-trained parameters, and A **179** and U represent an adaptation algorithm and an **180** update algorithm, respectively. The evaluation is **based on the online predictions** \hat{y}_t **.**
182 18

The meta-parameters ϕ_t can leverage knowledge across samples. These parameters are slowly up- dated by U, and the final prediction is made after a fast adaptation A. This allows the parameters to fit 186 the current sample for greater improvement while mitigating the risk of model collapse over time.

 Fast-slow TTA generalizes non-continual TTA. **If** $U(\phi_t, x_t) = \phi_t$, i.e., ϕ_t remains constant over time, the framework degenerates to non-continual TTA. To the best of our knowledge, this is the first time such an approach has been applied to TTA for **193** ASR.

194 3.2 Dynamic SUTA

 We propose Dynamic SUTA (DSUTA), a fast-slow TTA method based on SUTA [\(Lin et al.,](#page-8-5) [2022\)](#page-8-5). SUTA is the very first method for ASR TTA. Given **pre-trained parameters** ϕ_{pre} , for every incoming **sample** x_t **, SUTA adapts** ϕ_{pre} **for N steps with**

Algorithm 1 Dynamic SUTA

Input: Data stream $\{x_t\}_{t=1}^T$, buffer B with size M, adaptation step N, pre-trained param ϕ_{pre} **Output:** Predictions $\{\widehat{y}_t\}_{t=1}^T$ 1: $\mathcal{B}, \phi_1 \leftarrow \{\}, \phi_{pre}$ 2: $Results \leftarrow \{\}$ 3: for $t = 1$ to T do 4: $\phi_t \leftarrow \phi_t$ \triangleright Adapt parameters
5: **for** $n = 1$ to N **do** for $n = 1$ to N do 6: $\mathcal{L} \leftarrow \mathcal{L}_{suta}(\phi_t, x)$ 7: $\phi_t \leftarrow \text{Optimizer}(\phi_t, \mathcal{L})$ 8: $\hat{y}_t \leftarrow \phi_t(x_t) \Rightarrow$ Save prediction 9: $Results \leftarrow Results \cup {\hat{y}_t}$
0. $B \leftarrow B \cup \{x\}$ 10: $\mathcal{B} \leftarrow \mathcal{B} \cup \{x_t\}$ 11: **if** $t\%M = 0$ then \triangleright Update meta-param 12: $\mathcal{L} \leftarrow \frac{1}{M} \sum_{x \in \mathcal{B}} \mathcal{L}_{suta}(\phi_t, x)$ 13: $\phi_{t+1} \leftarrow \text{Optimizer}(\phi_t, \mathcal{L})$ 14: $\mathcal{B} \leftarrow \{\}$ 15: else 16: $\phi_{t+1} \leftarrow \phi_t$ 17: return Results

the objective \mathcal{L}_{suta} . \mathcal{L}_{suta} consists of entropy loss 200 and minimum class confusion loss. Entropy min- **201** imization aims to sharpen class distribution, and **202** minimum class confusion aims to reduce the cor- **203** relation between different prediction classes. See **204** Appendix [A.5](#page-11-0) for the detailed loss function. Model **205** parameters are reset to ϕ_{pre} when the next sample 206 arrives. **207**

For DSUTA, the adaptation algorithm A is set 208 exactly the same as SUTA, which iteratively adapts **209** ϕ_t for N steps with \mathcal{L}_{suta} on x_t . To construct the 210 update algorithm U , we introduce a small buffer 211 B with size M . For every M steps, the buffer is 212 filled and we calculate \mathcal{L}_{suta} from these M samples 213 to update the meta-parameters ϕ_t with gradient 214 descent. The buffer is then cleared. Thus, the **215** meta-parameters ϕ_t gradually evolve by mini-batch 216 gradient descent with batch size M. DSUTA can **217** be viewed as a variant of SUTA, which starts the **218** adaptation from dynamically changing ϕ_t instead 219 of the fixed ϕ_{pre} . Denote $\mathcal{L}_{suta}(\phi, x)$ as the loss of 220 sample x on model ϕ . Algorithm [1](#page-2-3) describes the **221** pseudo code of DSUTA. **222**

3.3 DSUTA with Dynamic Reset Strategy **223**

As time progresses and the testing domain changes, **224** multiple domain shifts significantly challenge the **225** robustness of continual TTA methods. Recently, **226**

Figure 3: Sketch of DSUTA with the dynamic reset strategy. The domain construction stage and the shift detection stage alternate over time. When a large shift is detected, apply model reset to DSUTA, i.e., update $\phi_{t+1} = \phi_{pre}$.

 [Press et al.](#page-8-4) [\(2024\)](#page-8-4) has shown that *model reset* at a fixed frequency, which resets the current param- eters to the pre-trained ones at regular intervals, is a simple yet effective strategy. Therefore, we attempt to incorporate *model reset* strategy to up-**date the meta-parameters** ϕ_t **in DSUTA^{[1](#page-3-0)}. However,** determining the optimal reset frequency in reality is challenging. To automatically determine when 235 to apply model reset to ϕ_t , we propose a **dynamic** reset strategy, which actively detects large distri-**bution shifts and dynamically resets** $\phi_{t+1} = \phi_{pre}$.

 Figure [3](#page-3-1) provides an illustration of DSUTA with the dynamic reset strategy. Since distribution shift is a relative concept that is well-defined only af- ter a base domain is constructed, we designed a *domain construction stage* and a *shift detection stage*. Our proposed method alternates between these two stages over time. The domain construc- tion stage first constructs a base domain D with K samples. No model reset will be applied during this stage. In the subsequent shift detection stage, a de- tection algorithm checks each incoming sample to determine if there is a significant distribution shift. If a large shift is detected, we apply model reset and switch to a new domain construction stage.

 The following subsections describe the strategy in detail. We first introduce the Loss Improvement Index in Section [3.3.1,](#page-3-2) which measures the extent of the distribution shift. Then we define the domain construction stage and the shift detection stage in Section [3.3.2.](#page-3-3)

258 3.3.1 Loss Improvement Index

259 We aim to find an indicator that measures the extent **260** of the distribution shift from the base domain D. To

identify an appropriate indicator, we observed that **261** given a model, we observed that given a model $\phi_{\mathcal{D}}$ 262 trained on domain D , \mathcal{L}_{suta} for in-domain samples 263 is empirically lower than that for out-of-domain **264** samples. This suggests that $\mathcal{L}_{suta}(\phi_{\mathcal{D}}, x_t)$ might 265 be a good indicator. Additionally, we found that **266** subtracting the loss from the pre-trained model, 267 $\mathcal{L}_{suta}(\phi_{pre}, x_t)$, is beneficial^{[2](#page-3-4)}. This subtraction 268 acts as a normalization to remove the inherent diffi- **269** culty introduced by the data sample itself. Overall, **270** we define Loss Improvement Index (LII) as our **271** indicator: **272**

$$
LII_t = \mathcal{L}(\phi_{\mathcal{D}}, x_t) - \mathcal{L}(\phi_{pre}, x_t), \qquad \qquad \text{273}
$$

where $\mathcal{L} = \mathcal{L}_{suta}$. The construction of $\phi_{\mathcal{D}}$ will be 274 described in the next section. **275**

3.3.2 Domain Construction Stage and Shift **276 Detection Stage** 277

We integrate DSUTA with the dynamic reset strat- **278** egy as follows. Assume the model has been reset **279** at time step r . 280

(1) Domain Construction Stage: **281**

- 1. Let $k = \frac{K}{2}$ $\frac{R}{2}$, construct $\phi_{\mathcal{D}} = \phi_{r+k}$. 282
- 2. Collect LII_t for $t \in [r + k + 1, r + K]$. 283
- 3. At the end of the stage (i.e., $t = r + K$), 284 compute $\mathcal{G}_{\mathcal{D}} = \mathcal{N}(\mu, \sigma^2)$ from the collected 285 LIIs. **286**

Our goal is to estimate the distribution of LII. **287** We construct $\phi_{\mathcal{D}} = \phi_{r+k}$ as the meta-parameters 288 after observing k samples since the last reset. Cal- **289** culating the LII requires $\phi_{\mathcal{D}}$, and since TTA is an **290** online process, $K - k$ is the number of LIIs we 291

¹Non-continual TTA can be viewed as the case where we apply model reset at every time step.

²See Section [5.1](#page-6-0) for more discussion on indicator choice.

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 can collect for statistical estimation. A smaller k 293 might not suffice for $\phi_{\mathcal{D}}$ to adequately represent the domain, while a larger k reduces the number of data points we can gather for estimation. Therefore, we empirically set $k = \lfloor \frac{K}{2} \rfloor$ **we empirically set** $k = \lfloor \frac{K}{2} \rfloor$.

297 (2) Shift Detection Stage:

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$$
\phi_{t+1} = \begin{cases} \phi_{pre}, & \text{if } \frac{LII_t - \mu}{\sigma} > 2, \\ U_{DSUTA}(\phi_t, x_t), & \text{otherwise,} \end{cases}
$$

299 where U_{DSUTA} is the update algorithm of DSUTA.

 During the domain construction stage, we de-**velop a statistical model** $\mathcal{G}_{\mathcal{D}}$ **using** $K - k$ **samples** to estimate the distribution of LII. In the shift de- tection stage, we trigger a reset operation if the LII exceeds a certain threshold, indicating an abnor- mally large shift. To determine whether the LII indicates such a shift, we conduct a right-tailed hypothesis test.

 For the right-tailed hypothesis test, the common practice with a significance level of 0.05 corre- sponds to a Z-score of 1.64. Here, we use a Z-score of 2 for simplicity, which makes the condition for resetting slightly stricter.

 Using the LII of a single sample for the hypothesis test can be too sensitive. The averaged LII from multiple samples reduces variance and yields more reliable results. With DSUTA, we perform the hypothesis test every M steps, using the M samples in DSUTA's buffer to calculate the averaged LII. The final shift detection stage is defined as follows:

$$
\phi_{t+1} = \begin{cases} \phi_{pre}, & \text{if } \frac{1}{M} \sum_{i | x_i \in \mathcal{B}} \frac{L H_i - \mu}{\sigma / \sqrt{M}} > 2, M | t, \\ U_{DSUTA}(\phi_t, x_t), & \text{otherwise.} \end{cases}
$$

 Here, B represents the buffer containing the most recent M samples. In our implementation, we fur- ther introduce a patience parameter P to enhance the algorithm's stability. Please refer to Appendix [A.6](#page-11-1) for the detailed algorithm.

³²⁸ 4 Experiments

329 4.1 Dataset

330 4.1.1 Single-domain Data

331 [L](#page-8-6)ibrispeech-C: we follow previous works [\(Kim](#page-8-6) [et al.,](#page-8-6) [2023\)](#page-8-6) to add background noises from MS- SNSD [\(Reddy et al.,](#page-8-10) [2019\)](#page-8-10) into Librispeech test set [\(Panayotov et al.,](#page-8-11) [2015\)](#page-8-11). The noises include air conditioner (AC), airport announcement (AA), babble (BA), copy machine (CM), munching (MU),

neighbors (NB), shutting door (SD), typing (TP), **337** and vacuum cleaner (VC). We also apply Gaussian **338** noise (GS) as in [\(Lin et al.,](#page-8-5) [2022\)](#page-8-5), resulting in 10 **339** different noises in total. The Signal-to-Noise Ratio **340** (SNR) is set to 5 dB. 3

CHiME-3 [\(Barker et al.,](#page-8-12) [2017\)](#page-8-12): a noisy version of **342** WSJ corpus with real-world environmental noises **343** at 16kHz. **344**

To reduce GPU memory usage, we exclude sam- **345** ples with raw lengths longer than 20 seconds in all **346** experiments. This removes about 1% of the data. 347

4.1.2 Multi-domain Time-varying Data **348**

We create three time-changing multi-domain test 349 sequences by concatenating different corruptions **350** from LibriSpeech-C. **351**

(a) MD-Easy: Noises in MD-Easy are determined **352** by the relatively well-performed noises of the pre- **353** trained model (See Table [1\)](#page-6-1). Five background **354** noises, in the order AC→CM→TP→AA→SD, **355** were used, with 500 samples for each noise, mak- **356** ing a total of 2500 samples. **357**

(b) MD-Hard: Noises in MD-Hard are determined **358** by the relatively poor-performed noises of the pre- **359** trained model (See Table [1\)](#page-6-1). Five background **360** noises, in the order GS→MU→VC→BA→NB, **361** were used, with 500 samples for each noise, mak- **362** ing a total of 2500 samples. **363**

(c) MD-Long: We first sample a background noise **364** from the 10 available background noises, then sam- **365** ple a data sequence with this noise, with a random **366** length ranging from 20 to 500. We repeat this pro- **367** cess until the total length reaches 10,000. **368**

4.2 Baselines 369

[N](#page-8-5)on-continual TTA Baselines: (a) SUTA [\(Lin](#page-8-5) **370** [et al.,](#page-8-5) [2022\)](#page-8-5) leverages unsupervised objectives **371** (entropy minimization and minimum class con- **372** fusion) to reduce uncertainty and minimize class **373** correlations. Temperature smoothing is applied **374** to flatten the output probability distributions, **375** addressing issues with over-confident predictions. **376** The adaptation process involves iteratively min- **377** imizing a combined loss of EM and MCC. (b) **378** SGEM [\(Kim et al.,](#page-8-6) [2023\)](#page-8-6) propose a general form **379** of entropy minimization with negative sampling. **380** Continual TTA Baselines: (c) CSUTA is a **381** straightforward continual version of SUTA without **382** resetting parameters. (d) AWMC [\(Lee et al.,](#page-8-8) **383** [2023\)](#page-8-8) utilizes the anchor model to generate initial **384**

 3 [\(Kim et al.,](#page-8-6) [2023\)](#page-8-6) reported using 10dB noise but their source code and results show that they use 5dB.

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 pseudo labels, the chaser model updates itself using these pseudo labels for self-training, and the leader model refines predictions through an exponential moving average.

390 4.3 Implementation Details

 We use the wav2vec 2.0-base model fine-tuned on 392 Librispeech 960 hours^{[4](#page-5-0)} as the source ASR model. 393 **For SUTA, we follow the official implementation^{[5](#page-5-1)},** where an additional reweighting trick is applied on the minimum class confusion loss. The default **adaptation step of SUTA is** $N = 10$, as specified in the original paper. For SGEM, we follow the offi-**cial implementation^{[6](#page-5-2)}**. For CSUTA, we set the adap-399 tation step to $N = 1$ since we found that any higher value would cause severe model collapse. We re- implemented AWMC with wav2vec 2.0, as there is no official code, and all hyperparameters follow the original paper. For the proposed DSUTA, the 404 default buffer size is $M = 5$, and the adaptation **step is** $N = 10$.

406 4.4 Results

407 4.4.1 Single Domain

 We compare TTA performance on 11 domains by word error rate (WER) in Table [1.](#page-6-1) DSUTA shows significant improvement compared to the baseline methods. It outperforms both non-continual and continual baseline methods by a large margin, ex- cept for the SD domain, where it still achieves a 15.5% WER, close to SGEM's performance (14.9%). Notably, on the NB domain, DSUTA achieves a 36.3% WER compared to SUTA, which has a WER greater than 100%, demonstrating the effectiveness of our method.

 The key success factor of DSUTA is its ability to leverage learned knowledge from past samples. Figure [4](#page-5-3) plots the WER difference compared to the pre-trained model on the CM domain over time. 423 We compare three methods: SUTA with $N = 10$, **DSUTA** with $(M, N) = (5, 10)$, and **DSUTA** with $(M, N) = (5, 0)$, i.e., the learned ϕ_t itself. The **WER** of ϕ_t is lower than that of the pre-trained model, and DSUTA with 10-step adaptation out- performs SUTA with 10-step adaptation. In other words, DSUTA adaptation has a "better start" com-pared to non-continual TTA methods due to the

adaptation-ASR-SUTA

Figure 4: WER difference compared to the pre-trained model on CM domain over time. Data is smoothed by a window with a size of 100.

learned knowledge, resulting in superior perfor- **431** mance. Furthermore, DSUTA is more efficient in **432** adaptation steps than SUTA, requiring fewer steps **433** to achieve better performance. Appendix [A.2](#page-9-0) pro- **434** vides more discussion on efficiency. **435**

Table [1](#page-6-1) also compares other continual TTA meth- **436** ods. Naive continual training, such as CSUTA, re- **437** sults in unsatisfactory performance and is some- **438** times even worse than the original pre-trained **439** model due to its instability. Although AWMC **440** is designed to increase stability, its performance **441** sometimes lags behind SUTA, particularly in cases **442** where the original pre-trained model has an ex- 443 tremely high error rate(BA, NB). This is not surpris- **444** ing since AWMC relies on a pseudo-label approach. **445** In contrast, DSUTA uses mini-batch gradient de- **446** scent to enhance stability without the use of pseudo 447 labels. Furthermore, the fast-slow approach allows **448** DSUTA to inherit SUTA's ability to better fit a sin- **449** gle utterance, improving overall performance while **450** avoiding the meta-parameters overfitting. **451**

4.4.2 Time-varying Domains **452**

In the following experiment, we set DSUTA with **453** $(M, N) = (5, 5)$ and compare DSUTA with 454 dynamic reset strategy where (M, N, K, P) = 455 $(5, 5, 100, 2)$ on multi-domain time-varying data. 456 We also experiment DSUTA with two baseline re- 457 set strategies. 1) *Oracle boundary* resets the model **458** at the ground truth domain boundary, and 2) *Fixed* **459** *reset* is the simple fixed-frequency reset strategy, 460 where the reset frequency is set to 50. 461

Table [2](#page-6-2) summarizes the results. DSUTA is com- **462** parable to or better than other baseline methods, **463** and applying *Dynamic reset* further boosts the per- 464

⁴ https://huggingface.co/facebook/wav2vec2-base-960h

⁵ https://github.com/DanielLin94144/Test-time-

⁶ https://github.com/drumpt/SGEM

	AA.	AC.	BA	CM	GS	MU	NB	SD	TP	VС	CHIME-3
Source model	40.6	27.7	66.9	49.7	75.6	51.4	120.1	19.4	25.8	49.7	30.0
Non-continual											
SUTA	30.6	17.4	53.7	38.7	54.5	39.0	112.3	15.0	17.4	39.3	23.3
SGEM	30.9	17.8	54.5	39.2	56.3	39.2	113.0	14.9	17.5	40.3	23.5
Continual											
CSUTA	39.8	22.6	63.4	53.4	58.4	54.7	68.1	23.2	23.0	50.9	27.6
AWMC	31.6	18.0	61.6	37.7	48.5	36.2	131.9	17.0	18.0	36.1	22.4
<i>Fast-slow</i>											
DSUTA	25.9	15.4	33.2	33.5	37.0	28.4	36.3	15.5	15.6	29.9	21.7

Table 1: WER(%) of different TTA methods on CHiME-3 and LibriSpeech-C with 10 types of noises. Reported WER is averaged over 3 runs.

	MD-Easy	MD-Hard	MD-Long
Source model	32.7	74.6	61.0
Non-continual			
SUTA	24.0	60.4	53.3
SGEM	25.0	61.0	53.4
Continual			
CSUTA	37.3	83.6	100.3
AWMC	25.8	66.1	60.6
<i>Fast-slow</i>			
DSUTA	24.0	45.6	43.2
w/Dynamic reset	22.7	39.8	35.8
w/Fixed reset	22.8	49.4	45.2
w/ Oracle boundary	21.7	36.9	39.5

Table 2: WER(%) of different TTA methods on multidomain time-varying data. Reported WER is averaged over 3 runs.

465 formance. Since we set DSUTA with fewer adapta-**466** tion steps, our proposed method is both better and faster than SUTA in the multi-domain scenario[7](#page-6-3) **467** .

 For the non-continual TTA baselines, WER is improved in all cases but remains very high on MD-Hard and MD-Long. For the continual TTA baselines, CSUTA performs worse than the pre- trained model due to its instability. For AWMC, the original paper does not test in the multi-domain scenario, and our results show that AWMC is infe-rior to SUTA in this context.

 Regarding the model reset strategy, the proposed *Dynamic reset* outperforms *Fixed reset*. *Fixed re- set* performs worse than DSUTA without reset on MD-Hard and MD-Long, suggesting that resetting too frequently might hinder the model from utiliz- ing knowledge from past samples, thereby harming overall performance. Compared to *Oracle bound-* *ary* (upper bound), *Dynamic reset* achieves slightly **483** worse performance on MD-Easy and MD-Hard. **484** However, on MD-Long, *Dynamic reset* surprisingly **485** achieves a 35.8% WER, which is even better than **486** the 39.5% WER using *Oracle boundary*. Since *Dy-* **487** *namic reset* automatically determines when to reset, **488** it can further utilize the knowledge from other noise **489** domains when it is beneficial, rather than relying **490** solely on single-domain data for adaptation. **491**

5 Discussion **⁴⁹²**

5.1 Why Choosing Averaged LII as an **493** Indicator? **494**

A good indicator should *separate in-domain and* **495** *out-of-domain samples into two clusters*. To visu- **496** alize the indicator, we selected 500 samples from **497** the GS domain as the source domain and randomly **498** sampled 2000 samples from other domains as outof-domain samples. $\phi_{\mathcal{D}}$ is then trained on 100 \qquad 500 samples from the GS domain using \mathcal{L}_{suta} . We 501 randomly sampled 500 averaged LIIs. Figure [5](#page-7-0) **502** visualizes the distributions of averaged LIIs (over **503** 5 samples) of the remaining in-domain and out-of- **504** domain samples. By using the averaged LII, two **505** distributions are well separated. **506**

Figure [6](#page-7-1) visualizes the distributions of other pos- **507** sible choices of the indicator. Figure [6a](#page-7-1), b shows 508 the distribution of averaged LII over 1 sample (i.e., 509 the original LII) and 20 samples, respectively. Us- **510** ing a single sample is not sufficient to distinguish **511** the distributions, while considering more samples **512** makes the detection more accurate. Figure [6c](#page-7-1) il-
513 lustrates the case without subtracting the loss from **514** the pre-trained model, namely $\mathcal{L}(\phi_{\mathcal{D}}, x_t)$. The dis- 515 tributions are not well separated. In Figure [6d](#page-7-1), we **516** also tried using the parameters after adaptation A **517**

⁷See Appendix [A.2](#page-9-0) for detailed discussion on efficiency.

Figure 5: Distributions of averaged LII (over 5 samples) from the GS domain and non-GS domains.

Figure 6: Distributions of other possible f_D . (a): original LII, (b): averaged LII for 20 samples, (c): without subtraction of pre-trained model loss, and (d): with the adapted parameters.

518 instead of the meta-parameters, namely

519
$$
\mathcal{L}(A(\phi_{\mathcal{D}},x_t),x_t) - \mathcal{L}(A(\phi_{pre},x_t),x_t).
$$

520 However, it resulted in more overlap between the **521** two distributions than the proposed method.

522 5.2 Different Domain Transition Rates

 In this section, we investigate *how different do- main transition rates affect the performance of reset strategies*. The original transition rate (s) of MD-Easy and MD-Hard is 500. We com- pare different reset strategies in 3 transition rates: $s = 20, 100, 500$. To maintain a total length of the data stream to 2500, for $s = 100$, the domain 530 order sequence is repeated 5 times, and for $s = 20$, the domain order sequence is repeated 25 times. We follow the hyperparameter settings described in Section [4.4.2.](#page-5-4)

534 The results are presented in Table [3.](#page-7-2) *Oracle* **535** *Boundary* and *Fixed Reset* show that as the tran-

MD-Easy	$s=20$	$s = 100$	$s=500$
DSUTA	24.1	23.9	24.0
w/ dynamic reset	23.8	23.7	22.7
w/fixed reset	24.6	23.1	22.8
w/ oracle boundary	23.7	22.8	21.7
MD-Hard	$s=20$	$s = 100$	$s = 500$
DSUTA	45.6	44.7	45.6
w/ dynamic reset	42.3	44.5	39.8
w/fixed reset	53.3	49.9	49.4

Table 3: WER(%) of different reset strategies on MD-Easy and MD-Hard with different transition rates. Reported WER is averaged over 3 runs. s is the domain transition rate.

sition rate increases, resetting too often deterio- **536** rates performance. This phenomenon is more pro- **537** nounced in MD-Hard, where DSUTA outperforms **538** SUTA by a large margin, suggesting that continual **539** learning is more effective in this context. *Oracle* **540** *Boundary* severely deteriorates performance when **541** $s = 20$ and $s = 100$, implying that learning from 542 samples from other noise domains might be benefi- 543 cial. Since *Dynamic Reset* automatically handles **544** when to reset, it can utilize the knowledge from 545 other noise domains, and reset is not triggered as **546** frequently as in *Oracle Boundary* or *Fixed reset* **547** under fast transitions, leading to better results. **548**

In summary, the proposed *Dynamic reset* offers **549** good performance across diverse scenarios due to **550** its flexibility. *Dynamic reset* minimizes unneces- **551** sary resets and utilizes learned knowledge more **552** effectively, consistently outperforming other reset **553** strategies, making it a versatile solution. **554**

6 Conclusion **⁵⁵⁵**

In this work, we advance the non-continual Test- **556** Time Adaptation (TTA) method for ASR into a 557 continual learning framework using a novel ap- **558** proach to stabilize adaptation and improve perfor- **559** mance. Specifically, we introduce Dynamic SUTA 560 (DSUTA), a fast-slow method that combines non- **561** continual and continual TTA, demonstrating sig- **562** nificant improvements on single-domain test data. **563** Additionally, we propose a statistical dynamic re- **564** set strategy to enhance robustness and performance **565** on time-varying test data streams. Experimental **566** results indicate that our proposed method outper- **567** forms the non-continual SUTA baseline and previ- **568** ous continual TTA methods using pseudo labeling. **569**

8

⁵⁷⁰ Limitations

- **571** The primary limitations of this paper are as follows: **572** Domain Shift with Background Noises: In this **573** work, we use noise corruptions to simulate chang-**574** ing domains and control domain shifts. However, **575** there are various other speech domains to study, **576** such as accents, speaker characteristics, and speak-**577** ing styles. We will consider these domains in future **578** research.
- **579** Different Types of End-to-End ASR Models: **580** This work follows SUTA with a CTC-based ASR **581** model, but there are different kinds of end-to-end **582** ASR models available. As shown in [\(Kim et al.,](#page-8-6) **583** [2023\)](#page-8-6), entropy minimization-based TTA methods **584** can be extended to other end-to-end ASR models. **585** We encourage future research to extend our DSUTA **586** method to these other end-to-end ASR models.
- **587** Not Addressing Model Forgetting: This work **588** focuses on adaptation to testing samples during **589** inference time, rather than memorizing all past **590** knowledge. Consequently, the proposed method **591** might experience catastrophic forgetting as the do-**592** main changes. However, given a new test sample, **593** the method can instantly adapt to that instance, en-**594** suring that the final performance remains strong.

⁵⁹⁵ References

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A Appendix **⁶⁵⁷**

A.1 Different noise levels **658**

From Table [1](#page-6-1) and Table [2,](#page-6-2) we observe a trend 659 that DSUTA has a larger advantage over other **660** methods under severe domain shift where the pre- **661** trained model performs poorly. To investigate **662** *how different levels of domain shift affect the pro-* **663** *posed method*, we compare the pre-trained model, **664** SUTA, and DSUTA with noise levels of 0dB, **665** 5dB, and 10dB on the AC, SD, and TP domains **666** from LibriSpeech-C, which are the top 3 well- **667** performing domains for the pre-trained model. We **668** set $N = 5$ for both SUTA and DSUTA. Table [4](#page-9-1) 669 summarizes the results. 670

The results show that DSUTA is more effec- **671** tive under severe corruption. As the noise level **672**

Domain	Method	0dB	5dB	10dB
	Pre-trained	63.7	27.7	14.2
AC	SUTA	39.5	17.4	10.6
	DSUTA	27.6	16.0	11.5
	Pre-trained	29.7	19.4	13.6
SD	SUTA	23.6	15.0	10.8
	DSUTA	22.4	15.5	12.0
	Pre-trained	42.4	25.8	16.6
TP	SUTA	28.8	17.4	12.1
	DSUTA	22.4	16.3	12.4

Table 4: WER(%) comparison for different noise levels. Reported WER is averaged over 3 runs.

 decreases, although DSUTA outperforms the pre- trained model, SUTA becomes better than DSUTA. We hypothesize that while DSUTA is quite effec- tive on noisy speech, its performance gain over the non-continual version (SUTA) is limited on relatively clean speech. Improving DSUTA's per- formance over SUTA on clean speech remains an area for future work.

681 A.2 Discussion on Efficiency

 DSUTA is more efficient in adaptation steps than SUTA. Figure [7](#page-10-0) compares SUTA and DSUTA on 10 domains of LibriSpeech-C under different adap-685 tation steps $N = 0, 1, 3, 5, 10$. DSUTA can use fewer adaptation steps to achieve better perfor-mance than SUTA with more adaptation steps.

 To assess the efficiency of different TTA meth- ods, we run them on MD-Long and compare the required forward/backward steps in Table [5](#page-9-2) and the runtime in Table [6.](#page-9-3) CSUTA is excluded due to its poor performance. We follow the hyperpa- rameter settings described in Section [4.4.2.](#page-5-4) All experiments were conducted on an Nvidia GeForce RTX 3080Ti GPU. Note that the results are for ref- erence only, as values can slightly differ depending on the implementation.

 DSUTA is more efficient in the adaptation step and overall faster than SUTA, SGEM, and AWMC. Although adding the dynamic reset strategy slightly increases runtime, it remains faster overall. We conclude that our method is not only superior in performance but also more efficient than existing approaches.

	#Forward	#Backward
Non-continual		
SUTA	100000	100000
SGEM	100000	100000
Continual		
AWMC	300000	100000
<i>Fast-slow</i>		
DSUTA	52000	52000
w/Dynamic reset	72000	52000

Table 5: Forward/backward steps comparison for different TTA methods on MD-Long.

Table 6: Runtime(s) comparison for different TTA methods on MD-Long. Avg is the averaged runtime(s) for a 1-second utterance. The result is averaged over 3 runs.

A.3 Hyper-parameter Tuning **705**

We explore different hyper-parameters for DSUTA **706** with the dynamic reset strategy. We use MD-Long 707 as the data sequence. Table [7](#page-11-2) presents the re- **708** sults for various buffer sizes M. Our proposed 709 method performs well overall. A smaller buffer **710** size can make the update of meta-parameters unstable, while a larger buffer increases latency in **712** triggering model reset after a domain shift since **713** the shift is detected once every M steps. Therefore, **714** a medium buffer size is preferred. **715**

Table [7](#page-11-2) also presents the results for different K 716 values during the domain construction stage. Again, **717** our proposed method performs well overall. The **718** performance of $K = 50$ is worse than $K = 100$ 719 and $K = 200$, suggesting that domain construction 720 benefits from having enough steps to collect LII **721** statistics and train a domain-specialized model ϕ_D . **722**

Figure 7: WER(%) of different number of adaptation steps on 10 noise domains of LibriSpeech-C.

Setup	WER	
$M=3$	36.8	
$M=5$ $M=10$	35.8 37.0	
$K=50$	38.5	
$K = 100$	35.8	
$K = 200$	35.5	

Table 7: WER(%) comparison of different hyperparameters on MD-Long. Reported WER is averaged over 3 runs.

Method	wav2vec2-base	data2vec-base	hubert-large
Pre-trained	61.0	59.6	43.3
SUTA	53.3	53.3	39.3
DSUTA	43.2	52.0	17.8
w/Dynamic reset	35.8	46.3	19.0

Table 8: WER(%) comparison of different CTC-based ASR models on MD-Long. Reported WER is averaged over 3 runs.

723 A.4 Generalization to Different Source ASR **724** Models

 To test the generalization of the proposed method, we adopt other source ASR models with DSUTA and dynamic reset strategy. Table [8](#page-11-3) reports the results with the ASR model fine-tuned from 729 wav2vec 2.0-base, data2vec-base^{[8](#page-11-4)}, and HuBERT-**1arge 730 1arge 730 1arge 730 1** with Librispeech 960 hours. Results show that both DSUTA and DSUTA with the dynamic reset strategy perform effectively across different mod- els, yielding significantly better WER than the pre-trained model and the SUTA.

736 **A.5 SUTA's Objective** (L_{suta})

 Assume C is the number of output classes and L is τ ³⁸ the number of frames in the utterance. $P_{i,j} \in \mathbb{R}^L$ denotes the output probabilities of the j-th class of the L frames.

741 Entropy Minimization (EM):

742
$$
\mathcal{L}_{em} = \frac{1}{L} \sum_{i=1}^{L} \mathcal{H}_i = -\frac{1}{L} \sum_{i=1}^{L} \sum_{j=1}^{C} \mathbf{P}_{ij} \log \mathbf{P}_{ij}.
$$

743 Minimum Class Confusion (MCC):

$$
\mathcal{L}_{mcc} = \sum_{j=1}^{C} \sum_{j'\neq j}^{C} \mathbf{P}_{\cdot}^{\top} \mathbf{P}_{\cdot j'}.
$$

746 The final SUTA objective is defined as a mixture **747** of \mathcal{L}_{em} and \mathcal{L}_{mcc} : 748

$$
\mathcal{L}_{suta} = \alpha \mathcal{L}_{em} + (1 - \alpha) \mathcal{L}_{mcc}.
$$

745

We follow the settings in the original paper, which 750 set $\alpha = 0.3$ and apply temperature smoothing on $\alpha = 751$ logits with a temperature of 2.5. **752**

A.6 Pseudo Code for DSUTA with Dynamic **753** Reset Strategy **754**

Algorithm [2](#page-12-0) describes the pseudo code of DSUTA **755** with the dynamic reset strategy. **756**

⁸ https://huggingface.co/facebook/data2vec-audio-base-960h

⁹ https://huggingface.co/facebook/hubert-large-ls960-ft

Algorithm 2 Dynamic SUTA with the dynamic reset strategy

Input: Data Sequence $\{x_t\}_{t=1}^T$, buffer B with size M, adaptation step N, number of samples for construction K, patience P, pre-trained parameters ϕ_{pre} **Output:** Predictions $\{\widehat{y}_t\}_{t=1}^T$ 1: $\mathcal{B}, \phi_1 \leftarrow \{\}, \phi_{pre}$ 2: $k, last_reset, stats \leftarrow |K/2|, 0, \{\}$ 3: $Results \leftarrow \{\}$ 4: for $t = 1$ to T do 5: $\hat{\phi}_t \leftarrow \phi_t$

6: **for** $n = 1$ to N **do** for $n = 1$ to N do 7: $\mathcal{L} \leftarrow \mathcal{L}_{suta}(\phi_t, x)$ 8: $\phi_t \leftarrow \text{Optimizer}(\phi_t, \mathcal{L})$ 9: $\hat{y}_t \leftarrow \hat{\phi}_t(x_t)$

10: $Results \leftarrow Results \cup {\hat{y}_t}$ \triangleright Inference and save the prediction 10: $Results \leftarrow Results \cup {\hat{y}_t}$
11: $\mathcal{B} \leftarrow \mathcal{B} \cup \{x_t\}$ $\mathcal{B} \leftarrow \mathcal{B} \cup \{x_t\}$ 12: if t%M = 0 then ▷ Update meta-parameter every M steps 13: **if** $t > last \, reset + K$ and IsReset(G, B, P) **then** \triangleright Dynamic reset 14: $\phi_{t+1} \leftarrow \phi_{pre}$ 15: $last_reset \leftarrow t$ 16: else 17: $\mathcal{L} \leftarrow \frac{1}{M} \sum_{x \in \mathcal{B}} \mathcal{L}_{suta}(\phi_t, x)$ 18: $\phi_{t+1} \leftarrow \text{Optimizer}(\phi_t, \mathcal{L})$ 19: $\mathcal{B} \leftarrow \{\}$ 20: else 21: $\phi_{t+1} \leftarrow \phi_t$ 22: if $t = last_reset + k$ then \triangleright Save the domain-specialized model 23: $\phi_{\mathcal{D}} \leftarrow \phi_t$ 24: **else if** $last_reset + k < t \leq last_reset + K$ **then** \triangleright Collect LII stats 25: $stats \leftarrow stats \cup \{LII_t\}$ 26: if $t = last \, reset + K$ then \triangleright Generate distribution 27: $\mathcal{G} \leftarrow \mathcal{N}(\mu_{stats}, \sigma_{stats}^2)$ 28: return Results