Sharing Matters: Analysing Neurons Across Languages and Tasks in LLMs

Anonymous ACL submission

Abstract

 Multilingual large language models (LLMs) have greatly increased the ceiling of perfor- mance on non-English tasks. However, the mechanisms behind multilingualism in these LLMs are poorly understood. Of particular interest is the degree to which internal repre- sentations are shared between languages. Re- cent work on neuron analysis of LLMs has fo- cused on the monolingual case, and the limited work on the multilingual case has not consid- ered the interaction between tasks and linguis- tic representations. In our work, we investi- gate how neuron activation is shared across languages by categorizing neurons into four distinct groups according to their responses across different languages for a particular in- put: *all-shared*, *partial-shared*, *specific*, and *non-activated*. This categorization is combined with a study of neuron attribution, i.e. the im- portance of a neuron w.r.t an output. Our anal- ysis reveals the following insights: (i) the lin- guistic sharing patterns are strongly affected by the type of task, but neuron behavior changes across different inputs even for the same task; (ii) *all-shared neurons* play a key role in gen-026 erating correct responses; (iii) boosting mul- tilingual alignment by increasing *all-shared neurons* can enhance accuracy on multilingual tasks. We will release the code to foster re-search in this area.

031 1 Introduction

 The black-box nature of large language models (LLMs) has given rise to an area of research which aims to interpret the internal mechanism of the [T](#page-9-0)ransformer architecture [\(Elhage et al.,](#page-8-0) [2021a;](#page-8-0) [Yu](#page-9-0) [et al.,](#page-9-0) [2023\)](#page-9-0). In order to investigate specific aspects of model behavior, previous studies choose to focus on specific model components to encourage inter- pretability. Differently from e.g. attention heads in the Transformer layers which are responsible for moving information from one token to another to-ken [\(Elhage et al.,](#page-8-1) [2021b\)](#page-8-1), feed-forward networks

Figure 1: A comparison of neuron analysis with different role designs in multilingual settings with the same semantic input, in which we define four types of neurons in one layer of LLM. English input "The capital of France is" corresponds to its Spanish and French counterparts "La capital de Francia es" (Spanish), "La capitale de la France est" (French).

(FFNs) are more likely to represent semantic fea- **043** tures [\(Black et al.,](#page-8-2) [2022\)](#page-8-2). The FFN consists of **044** two linear layers and an activation function is ap- **045** plied between them. A neuron inside the FFNs **046** is defined as a linear transformation of an input **047** representation followed by a non-linear activation **048** [\(Tang et al.,](#page-9-1) [2024\)](#page-9-1). [Geva et al.](#page-8-3) [\(2020,](#page-8-3) [2022\)](#page-8-4); [Fer-](#page-8-5) **049** [rando et al.](#page-8-5) [\(2023\)](#page-8-5) have earlier demonstrated the **050** importance of neurons in the FFNs for encoding **051** factual and linguistic knowledge. Furthermore, var- **052** ious neuron analytic methods have been developed **053** to prune inactive neurons, i.e. those which have **054** [a](#page-9-2)ctivation value less than or equal to zero [\(Zhang](#page-9-2) **055** [et al.,](#page-9-2) [2022;](#page-9-2) [Li et al.,](#page-8-6) [2023;](#page-8-6) [Voita et al.,](#page-9-3) [2023\)](#page-9-3). **056**

While the above-mentioned methods analyze **057** neuron behaviors based on the activation state (ac- **058** tive or inactive means activation value > 0 vs. ≤ 0) 059 in a monolingual setting, there is still a lack of un- **060** derstanding regarding how neurons behave across **061** various tasks in a multilingual setting. As shown **062** in Figure [1,](#page-0-0) different sets of neurons are activated **063** when an LLM is presented with corresponding in-

 puts in different languages. An inactive neuron in response to an English input is often activated and influential in response to an input in another language. It remains unclear how LLMs actually manage to learn multilingual representations. One typical example is that we may need to explore sets of neurons responsible for generating the out-072 put "Paris"^{[1](#page-1-0)} when presented with the English input "The capital of France is" and its Spanish counter-part "La capital de Francia es".

 In a similar line of reasoning, [Bhattacharya and](#page-8-7) **[Bojar](#page-8-7) [\(2023\)](#page-8-7) explored the behavior of language-** specific and language-agnostic (shared between two languages) neurons and their distribution over layers of a model. They concluded that the lay- ers close to the model's input and output exhibit more language-specific behavior. However, their results are restricted to the English-Czech. Due to the potential variation in neuron behavior of differ- ent language types and the reasoning and memory abilities of different multilingual tasks, we argue that there is a need for further exploration.

 Our research aims to establish a more fine- grained classification of neurons, enabling a more detailed analysis of LLM behavior in reason- ing style tasks (XNLI), fact-retrieval based tasks (fact probing), and explicitly multilingual question- answer tasks (knowledge editing). As shown in Fig- ure [1,](#page-0-0) we reformulate the activation state of neurons for a particular input and its corresponding trans- lations in 10 languages to four distinctive types to represent multilingual behaviors. *All-shared neu- rons* are neurons that remain active for all inputs regardless of language. *Partial-shared neurons* are activated only for inputs in certain languages. *Spe- cific neurons* are activated exclusively for inputs in one language. *Non-activated neurons* are not activated at all for any input.

 We perform neuron analysis addressing two re- search questions: (a) what are the behaviors of the four types of neurons in various multilingual tasks? (b) What attribution [\(Dhamdhere et al.,](#page-8-8) [2019\)](#page-8-8) does each type have in multilingual generation tasks, meaning which neurons are responsible for a pre-**109** diction?

 We examine the percentage of each type of neu- ron and neuron attributions in the multilingual tasks. We discover that the pattern of four types of neu- rons is determined by the tasks they encountered, and that the behavior of a neuron changes with

¹"Paris" is identical in both English, Spanish and French

different inputs for the same task, indicating the **115** potential implications of pruning neurons. **116**

Furthermore, we demonstrate the importance of 117 *all-shared neurons* in generating the correct output **118** from the neuron attribution study. Converting other **119** types of neurons to *all-shared neurons* improves **120** the accuracy of an LLM in multilingual tasks. **121**

Our main contributions are listed below: **122**

- Fine-grained neuron analysis: We define **123** four categories of neurons and use these to **124** analyze neuron behaviors in various types of **125** tasks across 10 languages. We reveal that rea- **126** soning style tasks (e.g. XNLI) involve more **127** *all-shared neurons* than fact-retrieval based **128** tasks (e.g. fact probing) which utilize more **129** *specific neurons*. **130**
- Neuron attribution: By studying the contri- **131** bution of neurons to the output of multilingual **132** tasks, we are the first to reveal the importance **133** of *all-shared neurons* within FFNs in multi- **134** lingual tasks. For instance, for the XNLI task, **135** the *all-shared neurons* comprise less than 30% **136** of the neurons, but they contribute 91.6% to **137** the generation of the correct responses in the **138** German test set. **139**
- Multilingual alignment: We demonstrate **140** that increasing the percentage of *all-shared* **141** *neurons* (by converting other types of neurons) **142** can significantly enhance the accuracy of an **143** LLM in multilingual tasks.

2 Related Work **¹⁴⁵**

Prior interpretability studies focused on understanding attention heads, while others have analyzed **147** neuron behaviors. Several studies on LLMs have **148** advanced our understanding of how neurons ac- **149** [q](#page-8-5)uire task-specific knowledge. For instance, [Fer-](#page-8-5) **150** [rando et al.](#page-8-5) [\(2023\)](#page-8-5); [Dai et al.](#page-8-9) [\(2022\)](#page-8-9); [Geva et al.](#page-8-3) **151** [\(2020,](#page-8-3) [2022\)](#page-8-4) investigated how FFN blocks func- **152** tion as key-value memories and proved that factual **153** knowledge is stored in the neurons. Research work **154** on the sparsity of neurons in FFN blocks disclosed **155** [m](#page-9-2)any neurons are inactive in various tasks [\(Zhang](#page-9-2) **156** [et al.,](#page-9-2) [2022;](#page-9-2) [Li et al.,](#page-8-6) [2023\)](#page-8-6). [Voita et al.](#page-9-3) [\(2023\)](#page-9-3) **157** located these "dead" neurons in the lower part of **158** the model (close to inputs) in the English scenario. **159** Despite the insights obtained, these studies are fo- **160** cused exclusively on a monolingual setting. **161**

For multilingual model analysis, [Bhattacharya](#page-8-7) **162** [and Bojar](#page-8-7) [\(2023\)](#page-8-7); [Tang et al.](#page-9-1) [\(2024\)](#page-9-1); [Tan et al.](#page-9-4) **163**

220

(4) **232**

(5) **238**

specif ic (7) **245**

 [\(2024\)](#page-9-4) classified neurons in an FFN block to language-specific and language-agnostic based on the threshold, which presumed that a neuron's be- havior remained consistent across examples. How- ever, they do not consider the potential adaptation of neurons under various language types and se- mantics brought forth by inputs from various mul- tilingual tasks. We investigate neurons' behaviors across multiple languages and tasks to this end.

¹⁷³ 3 Definitions

174 3.1 Neurons in FFN Blocks

 Every feed-forward block at layer l involves two linear transformations separated by a point-wise activation function. Biases are omitted for the sake of clarity:

$$
FFNl(xl) = Act(WKlxl)WVl
$$
\n(1)

180 **where** W_K^l , $W_V^l \in \mathbb{R}^{d_m \times d}$ are linear parameter 181 matrices, and $Act(\cdot)$ is a non-linear activation func-182 tion, where rows in W_K^l and columns in W_V^l are 183 viewed as d-dimensional keys k^l and values v^l , re-**184** spectively. We define the behavior of a neuron to be **185** the output of function immediately after the elemen-186 twise nonlinearity. d_m is the count of neurons. And 187 **the output of neurons** $A^l := Act(W^l_K x^l) \in \mathbb{R}^{d_m}$ **188** determines the weighting of the corresponding val-189 **ues in** W_V^l .

190 **For** *i***-th neuron and corresponding key** k_i^l **, value** 191 v_i^l and activation value A_i^l , we can express this **192** relationship using the following formulation:

193
$$
FFN^{l}(x^{l}) = \sum_{i=1}^{d_{m}} Act(x^{l} \cdot k_{i}^{l})v_{i}^{l} = \sum_{i=1}^{d_{m}} A_{i}^{l}v_{i}^{l} \qquad (2)
$$

194 **When such a neuron is activated** $A_i^l > 0$, so **195** it updates the residual stream by pulling out the 196 **corresponding value** v_i^l .

197 3.2 Contribution Score and Effective Score of **198** Neurons

 Inspired by [Geva et al.](#page-8-4) [\(2022\)](#page-8-4), in order to judge the importance of neurons in generating answers, we analyze their contributions to the output. The contribution score of a neuron to an FFN output is:

203
$$
C_i^l := \frac{|A_i^l| ||v_i^l||}{\sum_{j=1}^{d_m} |A_j^l| ||v_j^l||}
$$
 (3)

 which is the proportion of its weight to the sum 205 of weights of all neurons in the FFN block. $|A_i^l|$ is **he absolute value of activation value and** $||v_i^l||$ **is the L2-norm of value** v_i^l .

208 Whenever a neuron is activated, the associated **209** column of the values (scaled by the neuron's value)

is incorporated into the residual stream. The prod- **210** uct of the value of the activated neuron A_i^l and the corresponding v_i^l is then transformed linearly and mapped to the vocabulary.

Following [Geva et al.](#page-8-4) [\(2022\)](#page-8-4); [Voita et al.](#page-9-3) [\(2023\)](#page-9-3), **214** projecting the neuron to the vocabulary using em- **215** bedding matrix $E_r \cdot A_i^l v_i^l$ can be viewed as obtaining 216 the effective score given by the i -th neuron to the 217 output reference token r for a given input. Specifi- **218** cally, a larger $E_r \cdot A_i^l v_i^l$ has a higher probability to 219 produce a gold answer (*r*). A negative $E_r \cdot A_i^l v_i^l$ reduces the probability in generating r . In this way, 221 we can quantify the effect of a neuron on the output **222** distribution. We give detailed descriptions about **223** the neuron projection to the vocabulary space in **224** Appendix [A.1.](#page-9-5) **225**

3.3 Definition of Four Types of Neurons **226**

For the set of all neurons N^l in the *l*−th layer, the 227 activation value of one neuron n in one language **228** $lang$ is A_{lang}^l . Note that some activation functions 229 (e.g. GeLU) can result in negative activation values. **230** The definition of *all-shared neurons* is: **231**

$$
N_{all}^{l} := \bigcap_{lang}^{langs} \{ n \in N^{l} : A_{lang}^{l} > 0 \}
$$
 (4)

where *langs* is the sets of testing languages and 233 Nall means these neurons are activated in all lan- **²³⁴** guages. For *non-activated neurons* which have **235** activation value less than or equal to zero in all **236** languages, the definition is: **237**

$$
V_{non}^{l} := \bigcap_{lang}^{langs} \{ n \in N^{l} : A_{lang} \le 0 \}
$$
 (5)

Specific neurons are neurons only activated in 239 one specific language. They can be denoted using: **240**

$$
N_{specific}^l := \bigcup_{lang_{k1}}
$$

N

$$
(\{n \in N^l : A_{lang_{k1}} > 0\} \bigcap_{\substack{lang_s \\ \text{long} \\ k \neq k1}}^{lang_s} \{n \in N^l : A_{lang_k} \le 0\})
$$
 (6) 241

The remaining neurons are *partial-shared neu-* **242** *rons* as they are activated by inputs from multiple **243** languages, but not all languages at the same time: **244**

$$
N_{partial}^l = N^l - N_{all}^l - N_{non}^l - N_{specific}^l \tag{7}
$$

Unlike [Bhattacharya and Bojar](#page-8-7) [\(2023\)](#page-8-7); [Tang](#page-9-1) **246** [et al.](#page-9-1) [\(2024\)](#page-9-1), which exclusively on sub-word ac- **247** tivation statistics and thus capture incomplete se- **248** mantics, we examine the activation state of the last 249 token. For each input text with tokens $x_1, x_2, \ldots x_S$, 250 we use the activation state x_S to investigate the **251** behavior of neurons, as that is when the LLM per- **252** forms the prediction task. **253**

-
-
-

-
-

²⁵⁴ 4 Experimental Setting

255 4.1 Multilingual Tasks

 We perform analysis on neurons in FFN blocks of various LLMs, harnessing their multilingual ca- pabilities in three diverse tasks which consist of multilingual parallel sentences. They are:

 Natural Language Inference. XNLI [\(Con-](#page-8-10) [neau et al.,](#page-8-10) [2018\)](#page-8-10) is a multilingual natural lan- guages inference dataset. Each test sample con- sists of a premise and a hypothesis, requiring an LLM to determine whether a hypothesis is entailed, contradicted, or neutral conditioned on the premise.

 Fact Probing. LLMs are used to predict fac- tual answers in response to corresponding probing prompts. A multilingual factual knowledge dataset (mParaRel [\(Fierro and Søgaard,](#page-8-11) [2022\)](#page-8-11)) capturing 38 binary relations (e.g., *X born-in Y*) is used in the analysis.

 Cross-lingual Knowledge Editing (KE). MzsRE [\(Wang et al.,](#page-9-6) [2023\)](#page-9-6) is a multilingual question-answering dataset. It provides counterfac- tual edited knowledge in the context and requires an LLM to produce the corresponding answer ac- cording to the context. We evaluate LLMs in two **cross-lingual KE scenarios: 1) EN (Edit)** \rightarrow ALL (test): edit in English and test in other languages **and 2)** ALL (Edit) \rightarrow EN (test): edit in other lan-guages and test in English.

 These tasks cover 10 diverse languages, includ- ing English (en), German (de), Spanish (es), French (fr), Portuguese (pt), Russian (ru), Thai (th), Turk- ish (tr), Vietnamese (vi), and Chinese (zh). Prompts are detailed in Appendix [A.2.](#page-10-0)

287 4.2 Base LLMs

 We mainly analyze the behavior of neurons in [a](#page-9-7) foundation multilingual LLM BLOOM [\(Scao](#page-9-7) [et al.,](#page-9-7) [2022\)](#page-9-7) and an instruction-finetuned model BLOOMZ [\(Muennighoff et al.,](#page-9-8) [2023\)](#page-9-8). We also in- clude the analysis of other decoder-only models: [X](#page-9-9)GLM [\(Lin et al.,](#page-8-12) [2022\)](#page-8-12), LLAMA2-7b-chat [\(Tou-](#page-9-9) [vron et al.,](#page-9-9) [2023\)](#page-9-9), and an encoder-decoder model mT0 [\(Muennighoff et al.,](#page-9-8) [2023\)](#page-9-8) in the Ap-pendix [A.3.2.](#page-10-1)

²⁹⁷ 5 Behaviors of Four Types of Neurons

 For each task we use parallel test texts from ten languages as inputs, and record the activation state of each neuron. Subsequently, we calculate the percentage of the four types of neurons compared to the total neurons.

We use BLOOMZ as the backbone LLM to in- **303** vestigate the behaviors of four types of neurons, **304** and the results of three tasks are shown in Fig- **305** ures [2](#page-3-0)[-4](#page-4-0) respectively. The supplemental analysis **306** of cross-lingual KE (ALL (Edit) \rightarrow EN (test)) task 307 is shown in Figure [11](#page-10-2) (Appendix [A.3.1\)](#page-10-3). ³⁰⁸

5.1 Neuron Behaviors Across Tasks **309**

Figure 2: Neuron behavior pattern in the XNLI task. The left sub-figure shows the percentage of the four types of neurons across transformer layers (aka "by neuron type"). The right sub-figure shows aggregated behaviors of the activated neurons for each language across transformer layers (aka "by language").

5.1.1 Behavior Pattern of Four Types of **310** Neurons **311**

It can be observed from Figures [2](#page-3-0)[-3](#page-3-1) (left sub- **312** figures) that there are more *non-activated neurons* **313** on the whole than other types. However, the neu- **314** ron behavior is strongly task-related as the pat- **315** tern observed in the fact probing task differs sig- **316** nificantly from the other two tasks. In the fact **317** probing task, there are more *partial-shared neu-* **318** *rons* (yellow line in Figure [4\)](#page-4-0), whereas the other **319** tasks involve far more *all-shared neurons* (green **320** line in Figures [2](#page-3-0)[-3\)](#page-3-1). **321**

Figure 3: Neuron behavior pattern in the cross-lingual KE (EN (Edit) \rightarrow ALL (test)) task.

Figure 4: Neuron behavior pattern in the fact probing task.

 For the neuron behaviors across layers, lower layers exhibit a higher prevalence of *all-shared neurons* compared to *specific neurons* and *partial- shared neurons* in XNLI and KE. The number of *all-shared neurons* peaks at a certain layer followed by a continuous decreasing pattern in these two tasks. Fewer *all-shared neurons* in the upper lay- ers implies language-specific characteristics are retained there. Similarly, *partial-shared neurons* accumulate in the lower layer and it tends to out- number all other neurons moving towards upper layers in all tasks. It could be observed that nearly 99% of the neurons are non-activated in the first layer for XNLI and KE tasks, which may be as- sociated with the prompts, where the last token of input is punctuation (e.g., "?"). However, this phenomenon appears to be specific to BLOOMZ compared to other LLMs (Appendix [A.3.2\)](#page-10-1). We also investigate the impact of the number of lan- guages on the percentage of four types of neurons in Appendix [A.3.3.](#page-11-0) The comparison in Figure [16](#page-11-1) indicates that the number of languages slightly af-fects the *all-shared neurons*.

345 5.1.2 Consistent Neuron Behavior Pattern

 The percentage of activated neurons for each lan- guage exhibits a consistent pattern, as shown in Figures [2](#page-3-0)[-4](#page-4-0) (right sub-figures). At lower layers of an LLM, the number of activated neurons in- creases significantly, reaches the peak at around the 6-th layer, and then declines. It is not until at an upper layer (i.e., 28-th layer) that the number of active neurons commences to pick up its early increasing trend. Such a resurgence continues until it reaches the final layer of the LLM. It is a surprise to discover that the number of activated neurons is not influenced by the language of the inputs. This indicates neurons in an LLM exhibit similar pat-

terns across languages. **359**

Figure 5: Behavior-repeating neurons in the fact probing task across the entire testset. "overlap" indicates the percentage of neurons that keep the same behaviors across all examples in the testset. "average" indicates the percentage of neurons for an input, which is averaged over the entire testset.

5.1.3 Neurons Behaviors Across Examples **360**

As shown in Figures [2-](#page-3-0)[4,](#page-4-0) the analysis is conducted 361 by exploring the activation state under the same **362** input and the corresponding translations in 10 lan- **363** guages. In this experiment, we now investigate **364** how neurons behave across all examples for the **365** fact probing task. Here, the objective is to under- **366** stand if neurons that are specific to a designated **367** behavior maintain this behavior across test sam- **368** ples representing different semantics. The results **369** are shown in Figure [5](#page-4-1) and in Appendix [A.3.4](#page-11-2) (for **370** other tasks). To our surprise, almost no neuron **371** (identified by its index) repeats its behavior (e.g., **372** the "specific") across all examples. Different from **373** the previous studies, which assumed that a neuron **374** behaved consistently across examples, we reveal **375** that the behavior of a neuron is determined by **376** the semantics of the inputs encountered, even **377** within the same task. **378**

5.1.4 "Dead" Neuron Mystery **379**

In the multilingual scenario, *non-activated neurons* **380** comprise a significant portion, with more than 50% **381** of neurons having a zero or negative activation **382** value across layers for multilingual inputs (blue **383** line in the left sub-figures) in Figures [2](#page-3-0)[-4.](#page-4-0) **384**

Do these "dead" neurons stay inactive in all **385** test samples? In Figure [5](#page-4-1) we see that less than 10% **386** of *non-activated neurons* remain inactive. There **387**

388 is only a small proportion of persistently inactive **389** neurons, which reflects the distributed nature of

 knowledge representation for LLMs. The majority of neurons are activated at some point depending on the input provided. That is why we should execute caution when pruning neurons, as we may damage the overall performance of an LLM. 0.8

Figure 6: Neurons remaining "dead" in response to all tokens in an input sentence for the fact probing task.

 Do non-activated neurons remain "dead" in response to each token in an input sentence? Pre- viously, we performed analysis for the last token of an input. We analyze the behavior-repeating of *non-activated neurons* across tokens here for an input. Specifically, for each input sequence with 401 tokens $x_1, x_2, ..., x_S$, we record *non-activated neu*- *rons* of each token, w.r.t the intersection of index. A neuron is counted when it stays inactive for every token of one test input sequence. As shown in Fig- ure [6,](#page-5-0) less than 0.8% *non-activated neurons* remain "dead" for each token of input, further emphasizing the behavior-repeating of a neuron.

Figure 7: Neuron behavior pattern in the XNLI task with the BLOOM backbone.

408 5.2 Influence of Instruction Finetuning

 Does instruction finetuning (IFT) have an impact on neuron behaviors? We compare the percentage of the four designated types of neurons of BLOOM and its IFT counterpart BLOOMZ.

413 The results from the XNLI task are shown in **414** Figure [7](#page-5-1) and Appendix [A.3.5](#page-11-3) (from other tasks). Compared to the results from BLOOMZ in Fig- **415** ure [2,](#page-3-0) *all-shared neurons* are under-represented in **416** BLOOM (20% of BLOOM vs. 30% of BLOOMZ). **417** Meanwhile, more *partial-shared neurons* are ob- **418** served in BLOOM. IFT enhances the percentage 419 of *all-shared neurons* and reduces the number of **420** *partial-shared neurons*. We regard the increase of **421** the number of *all-shared neurons* as an effect of **422** multilingual representation alignment. It appears **423** that IFT contributes to multilingual alignment **424** based on the effects observed from this experi- **425** ment. Whether this effect can be generalized to **426** other LLMs and the rationale behind such effect **427** warrants a future study. **428**

Furthermore, we conduct ablation studies to in- **429** vestigate the impact of two key factors on the neu- **430** ron behaviors: the size of the backbone model **431** (Appendix [A.3.6\)](#page-11-4) and the number of multilin- **432** gual demonstrations in the few-shot setting (Ap- **433 pendix [A.3.7\)](#page-11-5).** 434

6 Neuron Attributions **⁴³⁵**

In the preceding experiments, we examined the **436** proportions of the four types of neurons across **437** layers, tasks, and languages. In this section, we **438** examine the relative contributions of each neuron **439** type to task performance. **440**

6.1 Neuron Contribution Score **441**

As discussed in Section [3.2,](#page-2-0) the contribution score 442 C_i^l of a neuron refers to its relative weight com- 443 pared to the total sum of weights of all neurons, **444** indicating the influence of each neuron on outputs. **445** We examine the proportion of the four types of neu- 446 rons among the top 5% contribution score under **447** inputs in each language. The proportions of neu- **448** rons in the cross-lingual KE task are depicted in **449** Figure [8](#page-6-0) (and the overall results of 10 languages 450 are shown in Figure [27](#page-16-0) in Appendix [A.4.1\)](#page-12-0). **451**

It can be observed that *all-shared neurons* are **452** the top contributing neurons to the outputs at **453** every layer, regardless of their language inputs. **454** This highlights their importance in the neural net- **455** work. The group of *partial-shared neurons* is the **456** second most influential group, demonstrating their **457** impacts across the latter half of the model. It is **458** not surprising that the *specific neurons* group has **459** limited influence on cross-lingual KE outputs as **460** they feature in a particular language type of inputs. **461**

Furthermore, we evaluate the contribution pro- 462 portion in the XNLI task, as depicted in Figure [26](#page-15-0) **463**

Figure 8: Contribution proportion of four types of neurons based on the cross-lingual KE (EN (Edit) \rightarrow ALL (test)) task.

 (Appendix [A.4.1\)](#page-12-0). Here, *all-shared neurons* con- stitute the highest proportion; however, *partial- shared neurons* show less influence compared to that observed in the cross-lingual KE task.

(b) Fact probing task.

Figure 9: Average and sum contribution score of the four types of neurons.

 In order to more comprehensively analyze the overall contribution of four types of neurons, we ex- tend the analysis from the top 5% to accommodate all neurons in this study. We analyze the average and the sum of contribution scores of all neurons in four categories. As shown in Figure [9,](#page-6-1) the average contribution of *all-shared neurons* significantly ex- ceeds that of the other three types. In terms of the total contribution score, *all-shared neurons* in the upper layers achieve a value equal to that of *non- activated neurons* in Figure [9\(a\),](#page-6-2) despite having a significantly lower count than *non-activated neu- rons* (<10% vs. 80% in Figure [2\)](#page-3-0). In the fact prob-ing task, *partial-shared neurons* score the highest,

while *all-shared neurons* score the lowest, primar- **482** ily due to their respective counts $(>20\% \text{ vs. } <1\% \text{ in } ⁴⁸³)$ Figure [4\)](#page-4-0). In summary, *all-shared neurons* play a **484** significant role in contributing to multiple tasks. **485** Future studies on neuron activation should consider **486** their contribution as well as their frequency. **487**

Table 1: Maximum, minimum, average effective score of four types of neurons on the cross-lingual KE task.

6.2 Neuron Effective Score **488**

Since each neuron encodes information, we can ex- **489** plore their contributions to the correct answer. As **490** discussed in Section [3.2,](#page-2-0) the projection to vocabu- **491** lary $E_r \cdot A_i^l v_i^l$ can be viewed as the effective score **492** given by the *i*-th neuron to the output reference 493 token r for a given input. 494

In the cross-lingual KE (EN (Edit) \rightarrow ALL (test)) 495 task, we calculate the effective score of each type **496** of neuron with the BLOOMZ backbone. The max- **497** imum, minimum, and average scores are shown **498** in Table [1](#page-6-3) (the overall results of ten languages **499** are shown in Table [4\)](#page-13-0), and the maximum effec- **500** tive scores across layers are shown in Figure [10.](#page-7-0) **501** *All-shared neurons* achieve the highest maximum **502** score and the lowest minimum score, indicating **503** they are pushed (or eliminated) strongly by the ac- **504** tivation function. In contrast to *all-shared neurons* **505** and *partial-shared neurons*, where the maximum **506** scores are substantially higher than the minimum **507** scores (1.85 vs. -0.94 and 0.22 vs. -0.16 in En- **508** glish), for *specific neurons* and *non-activated neu-* **509** *rons*, the score has a smaller span (± 0.07) , sug- 510 gesting *all-shared neurons* have greater influence **511** on the output distribution. **512**

As shown in Figure [10,](#page-7-0) the maximum effective 513 score of *all-shared neurons* significantly exceeds **514** that of the other three types. Moreover, *all-shared* **515** *neurons* aggregate at the first layer and upper lay- **516** ers. This observation confirms a recent finding **517** that early layers detect shallow patterns and up- **518** per layers are characterized by semantic patterns **519** [\(Ferrando et al.,](#page-8-5) [2023\)](#page-8-5), supporting the notion that **520** *all-shared neurons* play a key role in generating **521** prediction. Details of effective score analysis in **522** other tasks are depicted in Appendix [A.4.2.](#page-12-1) **523**

Figure 10: Maximum effective score of four types of neurons across layers based on the cross-lingual KE task.

accuracy	en			de es fr ru th tr vi	zh
baseline				53.8 41.8 50.3 49.0 47.6 40.9 34.9 50.5 51.1	
w/o. all-shared				$\overline{16.7}$ 3.50 10.1 10.0 6.6 9.0 1.4 12.1 14.5	
w/o. specific				53.7 41.7 50.3 48.9 47.4 40.6 35.3 50.4 49.3	
w/o. partial-shared				52.9 40.4 49.7 47.6 49.2 40.3 36.1 50.0 50.0	

Table 2: The accuracy when deactivating *all-shared neurons*, *specific neurons*, and *partial-shared neurons*, respectively. "w/o." stands for "without".

524 6.3 Effects on Accuracy

 We have investigated neuron attribution using the contribution score and effective score, which are based on the internal states of an LLM. Direct im- pacts of neurons on the output performance (i.e., accuracy) provide insights from a pragmatic per- spective. We explore the change of accuracy by intentionally deactivating three distinct types of neurons. This is performed by precisely identify- ing the type of neurons for an input and setting their activation values to zero. Take the XNLI task as an example, we record the results of an LLM with de- activated neurons in Table [2.](#page-7-1) The most significant decrease in accuracy is observed when the *all- shared neurons* are deactivated (e.g. 91.6% de- crease in the German testset). Deactivating *specific* and *partial-shared neurons* also negatively impacts the accuracy, but at a smaller magnitude when com- pared to the effect by *all-shared neurons*. We also prove the importance of *all-shared neurons* with the LLAMA backbone in Table [5](#page-13-1) (Appendix [A.5.1\)](#page-12-2). In order to prove the key role of *all-shared neurons* across tasks, we conduct the ablation experiments

on the cross-lingual KE task in Appendix [A.5.2.](#page-13-2) **547**

accuracy	en		de es fr ru th tr vi			zh
baseline			53.8 41.8 50.3 49.0 47.6 40.9 34.9 50.5 51.1			
co. specific			53.0 42.7 50.8 50.1 46.9 40.1 34.4 51.0 51.3			
co. partial-shared			53.2 41.8 51.0 49.3 49.4 41.5 36.8 50.7 51.2			
co. specific and partial-shared			52.6 42.1 51.6 49.4 48.2 41.7 36.4 50.7 51.7			

Table 3: The accuracy when converting *specific neurons*, and *partial-shared neurons* to *all-shared neurons* type. "co." (covert) means setting the activation value of inactive portions of neuron types to above the activation threshold.

We are intrigued by the possibility of enhanc- **548** ing an LLM's performance by simply converting **549** *specific neurons* and *partial-shared neurons* to *all-* **550** *shared neurons*. To achieve this, we set the activa- **551** tion value of the inactive portion of these two types **552** of neurons to just above the activation threshold. **553** The results shown in Table [3](#page-7-2) indicate that increas- **554** ing the number of *all-shared neurons* improves **555** the accuracy of an LLM in most cases. The results **556** are consistent with the finding in Section [5.2](#page-5-2) where **557** IFT model BLOOMZ with better performance has **558** more *all-shared neurons* than foundation model **559** BLOOM. The occasional drawbacks in some cases **560** (i.e., "en") require an in-depth study of the inter- **561** nal mechanism of an LLM involving more neuron **562** components. We leave this to a future study. **563**

7 Conclusion **⁵⁶⁴**

In this paper, we propose a novel approach for **565** analyzing neurons in FFN blocks by categorizing **566** them into four distinct types: *all-shared neurons*, **567** *partial-shared neurons*, *specific neurons* and *non-* **568** *activated neurons*. We conduct a detailed analysis **569** of LLM behaviors in multilingual tasks. Experi- **570** mental results disclose novel insights relating to **571** neuron behaviors: 1) We demonstrate that a neu- **572** ron's activation pattern is influenced by the tasks **573** it encounters, and even the behavior of a neuron **574** changes with different inputs for the same task. 2) **575** We show the importance of *all-shared neurons* in **576** output generation in multilingual tasks from the **577** neuron attribution study. 3) We prove that mul- **578** tilingual alignment can significantly enhance the **579** accuracy of an LLM in multilingual tasks by in- **580** creasing the percentage of *all-shared neurons* (i.e., **581** via converting other types of neurons or via IFT). **582** Future work will focus on exploring internal ac- **583** tivation mechanisms underpinning the observed **584** importance of *all-shared neurons* and multilingual **585** alignment across a wider range of tasks and LLMs. **586**

⁵⁸⁷ Limitations

 In this paper, we develop a method to analyze neu- ron behaviors in detail by categorizing them into four distinct neuron types w.r.t the degree of their responses to input languages. Although this en- ables a fine granularity neuron analysis on LLM backbones across various linguistic characteristics and task complexity, the scope of the experiments can be extended to accommodate larger LLMs with large amounts of parameters (i.e., BLOOMZ-176b) on a more comprehensive range of tasks. While this study demonstrates that the number of languages slightly impacts the percentage of *all-shared neu- rons*, it is limited to 10 languages. Exploring the effects of incorporating a larger number of lan- guages into the proposed method warrants further investigation. *All-shared neurons* in FFN blocks are identified to be of great importance, but how and why they work is still a mystery to disclose. Other network components, for example, induction heads, are not in the scope of this analysis.

⁶⁰⁸ References

- **609** [S](https://doi.org/10.48550/ARXIV.2310.15552)unit Bhattacharya and Ondrej Bojar. 2023. [Unveiling](https://doi.org/10.48550/ARXIV.2310.15552) **610** [multilinguality in transformer models: Exploring lan-](https://doi.org/10.48550/ARXIV.2310.15552)**611** [guage specificity in feed-forward networks.](https://doi.org/10.48550/ARXIV.2310.15552) *CoRR*, **612** abs/2310.15552.
- **613** Sid Black, Lee Sharkey, Léo Grinsztajn, Eric Win-**614** sor, Dan Braun, Jacob Merizian, Kip Parker, Car-**615** los Ramón Guevara, Beren Millidge, Gabriel Al-**616** four, and Connor Leahy. 2022. [Interpreting neu-](https://doi.org/10.48550/ARXIV.2211.12312)**617** [ral networks through the polytope lens.](https://doi.org/10.48550/ARXIV.2211.12312) *CoRR*, **618** abs/2211.12312.
- **619** Alexis Conneau, Ruty Rinott, Guillaume Lample, Ad-**620** ina Williams, Samuel R. Bowman, Holger Schwenk, **621** and Veselin Stoyanov. 2018. Xnli: Evaluating cross-**622** lingual sentence representations. In *Proceedings of* **623** *the 2018 Conference on Empirical Methods in Natu-***624** *ral Language Processing*. Association for Computa-**625** tional Linguistics.
- **626** Damai Dai, Li Dong, Yaru Hao, Zhifang Sui, Baobao **627** Chang, and Furu Wei. 2022. [Knowledge neurons](https://doi.org/10.18653/V1/2022.ACL-LONG.581) **628** [in pretrained transformers.](https://doi.org/10.18653/V1/2022.ACL-LONG.581) In *Proceedings of the* **629** *60th Annual Meeting of the Association for Compu-***630** *tational Linguistics (Volume 1: Long Papers), ACL* **631** *2022, Dublin, Ireland, May 22-27, 2022*, pages 8493– **632** 8502. Association for Computational Linguistics.
- **633** Kedar Dhamdhere, Mukund Sundararajan, and Qiqi **634** Yan. 2019. [How important is a neuron.](https://openreview.net/forum?id=SylKoo0cKm) In *7th In-***635** *ternational Conference on Learning Representations,* **636** *ICLR 2019, New Orleans, LA, USA, May 6-9, 2019*. **637** OpenReview.net.
- Nelson Elhage, Neel Nanda, Catherine Olsson, Tom **638** Henighan, Nicholas Joseph, Ben Mann, Amanda **639** Askell, Yuntao Bai, Anna Chen, Tom Conerly, **640** Nova DasSarma, Dawn Drain, Deep Ganguli, Zac **641** Hatfield-Dodds, Danny Hernandez, Andy Jones, **642** Jackson Kernion, Liane Lovitt, Kamal Ndousse, **643** Dario Amodei, Tom Brown, Jack Clark, Jared Ka- **644** plan, Sam McCandlish, and Chris Olah. 2021a. A **645** mathematical framework for transformer circuits. **646** *Transformer Circuits Thread*. Https://transformer- **647** circuits.pub/2021/framework/index.html. **648**
- Nelson Elhage, Neel Nanda, Catherine Olsson, Tom **649** Henighan, Nicholas Joseph, Ben Mann, Amanda **650** Askell, Yuntao Bai, Anna Chen, Tom Conerly, **651** Nova DasSarma, Dawn Drain, Deep Ganguli, Zac **652** Hatfield-Dodds, Danny Hernandez, Andy Jones, **653** Jackson Kernion, Liane Lovitt, Kamal Ndousse, **654** Dario Amodei, Tom Brown, Jack Clark, Jared Ka- **655** plan, Sam McCandlish, and Chris Olah. 2021b. A **656** mathematical framework for transformer circuits. **657** *Transformer Circuits Thread*. Https://transformer- **658** circuits.pub/2021/framework/index.html. **659**
- Javier Ferrando, Gerard I. Gállego, Ioannis Tsiamas, **660** and Marta R. Costa-jussà. 2023. [Explaining how](https://doi.org/10.18653/V1/2023.ACL-LONG.301) **661** [transformers use context to build predictions.](https://doi.org/10.18653/V1/2023.ACL-LONG.301) In **662** *Proceedings of the 61st Annual Meeting of the As-* **663** *sociation for Computational Linguistics (Volume 1:* **664** *Long Papers), ACL 2023, Toronto, Canada, July 9-14,* **665** *2023*, pages 5486–5513. Association for Computa- **666** tional Linguistics. **667**
- [C](https://doi.org/10.18653/V1/2022.FINDINGS-ACL.240)onstanza Fierro and Anders Søgaard. 2022. [Factual](https://doi.org/10.18653/V1/2022.FINDINGS-ACL.240) **668** [consistency of multilingual pretrained language mod-](https://doi.org/10.18653/V1/2022.FINDINGS-ACL.240) **669** [els.](https://doi.org/10.18653/V1/2022.FINDINGS-ACL.240) In *Findings of the Association for Computational* **670** *Linguistics: ACL 2022, Dublin, Ireland, May 22-27,* **671** *2022*, pages 3046–3052. Association for Computa- **672** tional Linguistics. **673**
- Mor Geva, Avi Caciularu, Kevin Ro Wang, and Yoav **674** Goldberg. 2022. [Transformer feed-forward layers](https://doi.org/10.18653/V1/2022.EMNLP-MAIN.3) **675** [build predictions by promoting concepts in the vocab-](https://doi.org/10.18653/V1/2022.EMNLP-MAIN.3) **676** [ulary space.](https://doi.org/10.18653/V1/2022.EMNLP-MAIN.3) In *Proceedings of the 2022 Conference* **677** *on Empirical Methods in Natural Language Process-* **678** *ing, EMNLP 2022, Abu Dhabi, United Arab Emirates,* **679** *December 7-11, 2022*, pages 30–45. Association for **680** Computational Linguistics. **681**
- Mor Geva, Roei Schuster, Jonathan Berant, and Omer **682** Levy. 2020. Transformer feed-forward layers are key- **683** value memories. *arXiv preprint arXiv:2012.14913*. **684**
- Zonglin Li, Chong You, Srinadh Bhojanapalli, Daliang **685** Li, Ankit Singh Rawat, Sashank J. Reddi, Ke Ye, **686** Felix Chern, Felix X. Yu, Ruiqi Guo, and Sanjiv **687** Kumar. 2023. [The lazy neuron phenomenon: On](https://openreview.net/pdf?id=TJ2nxciYCk-) **688** [emergence of activation sparsity in transformers.](https://openreview.net/pdf?id=TJ2nxciYCk-) In 689 *The Eleventh International Conference on Learning* **690** *Representations, ICLR 2023, Kigali, Rwanda, May* **691** *1-5, 2023*. OpenReview.net. **692**
- Xi Victoria Lin, Todor Mihaylov, Mikel Artetxe, Tianlu **693** Wang, Shuohui Chen, Daniel Simig, Myle Ott, Na- **694** man Goyal, Shruti Bhosale, Jingfei Du, Ramakanth **695**

 Pasunuru, Sam Shleifer, Punit Singh Koura, Vishrav Chaudhary, Brian O'Horo, Jeff Wang, Luke Zettle- moyer, Zornitsa Kozareva, Mona T. Diab, Veselin Stoyanov, and Xian Li. 2022. [Few-shot learning with](https://doi.org/10.18653/V1/2022.EMNLP-MAIN.616) [multilingual generative language models.](https://doi.org/10.18653/V1/2022.EMNLP-MAIN.616) In *Proceed- ings of the 2022 Conference on Empirical Methods in Natural Language Processing, EMNLP 2022, Abu Dhabi, United Arab Emirates, December 7-11, 2022*, pages 9019–9052. Association for Computational Linguistics.

- **706** Niklas Muennighoff, Thomas Wang, Lintang Sutawika, **707** Adam Roberts, Stella Biderman, Teven Le Scao, **708** M. Saiful Bari, Sheng Shen, Zheng Xin Yong, Hai-**709** ley Schoelkopf, Xiangru Tang, Dragomir Radev, **710** Alham Fikri Aji, Khalid Almubarak, Samuel Al-**711** banie, Zaid Alyafeai, Albert Webson, Edward Raff, **712** and Colin Raffel. 2023. [Crosslingual generaliza-](https://doi.org/10.18653/V1/2023.ACL-LONG.891)**713** [tion through multitask finetuning.](https://doi.org/10.18653/V1/2023.ACL-LONG.891) In *Proceedings* **714** *of the 61st Annual Meeting of the Association for* **715** *Computational Linguistics (Volume 1: Long Papers),* **716** *ACL 2023, Toronto, Canada, July 9-14, 2023*, pages **717** 15991–16111. Association for Computational Lin-**718** guistics.
- **719** Teven Le Scao, Angela Fan, Christopher Akiki, El-**720** lie Pavlick, Suzana Ilic, Daniel Hesslow, Roman **721** Castagné, Alexandra Sasha Luccioni, François Yvon, **722** Matthias Gallé, Jonathan Tow, Alexander M. Rush, **723** Stella Biderman, Albert Webson, Pawan Sasanka Am-**724** manamanchi, Thomas Wang, Benoît Sagot, Niklas **725** Muennighoff, Albert Villanova del Moral, Olatunji **726** Ruwase, Rachel Bawden, Stas Bekman, Angelina **727** McMillan-Major, Iz Beltagy, Huu Nguyen, Lucile **728** Saulnier, Samson Tan, Pedro Ortiz Suarez, Vic-**729** tor Sanh, Hugo Laurençon, Yacine Jernite, Julien **730** Launay, Margaret Mitchell, Colin Raffel, Aaron **731** Gokaslan, Adi Simhi, Aitor Soroa, Alham Fikri **732** Aji, Amit Alfassy, Anna Rogers, Ariel Kreisberg **733** Nitzav, Canwen Xu, Chenghao Mou, Chris Emezue, **734** Christopher Klamm, Colin Leong, Daniel van Strien, **735** David Ifeoluwa Adelani, and et al. 2022. [BLOOM:](https://doi.org/10.48550/ARXIV.2211.05100) **736** [A 176b-parameter open-access multilingual language](https://doi.org/10.48550/ARXIV.2211.05100) **737** [model.](https://doi.org/10.48550/ARXIV.2211.05100) *CoRR*, abs/2211.05100.
- **738** [S](https://doi.org/10.48550/ARXIV.2404.11201)haomu Tan, Di Wu, and Christof Monz. 2024. [Neu-](https://doi.org/10.48550/ARXIV.2404.11201)**739** [ron specialization: Leveraging intrinsic task modu-](https://doi.org/10.48550/ARXIV.2404.11201)**740** [larity for multilingual machine translation.](https://doi.org/10.48550/ARXIV.2404.11201) *CoRR*, **741** abs/2404.11201.
- **742** Tianyi Tang, Wenyang Luo, Haoyang Huang, Dong-**743** dong Zhang, Xiaolei Wang, Xin Zhao, Furu Wei, **744** and Ji-Rong Wen. 2024. Language-specific neurons: **745** The key to multilingual capabilities in large language **746** models. *arXiv preprint arXiv:2402.16438*.
- **747** Hugo Touvron, Louis Martin, Kevin Stone, Peter Al-**748** bert, Amjad Almahairi, Yasmine Babaei, Nikolay **749** Bashlykov, Soumya Batra, Prajjwal Bhargava, Shruti **750** Bhosale, Dan Bikel, Lukas Blecher, Cristian Canton-**751** Ferrer, Moya Chen, Guillem Cucurull, David Esiobu, **752** Jude Fernandes, Jeremy Fu, Wenyin Fu, Brian Fuller, **753** Cynthia Gao, Vedanuj Goswami, Naman Goyal, An-**754** thony Hartshorn, Saghar Hosseini, Rui Hou, Hakan **755** Inan, Marcin Kardas, Viktor Kerkez, Madian Khabsa,

Isabel Kloumann, Artem Korenev, Punit Singh Koura, **756** Marie-Anne Lachaux, Thibaut Lavril, Jenya Lee, Di- **757** ana Liskovich, Yinghai Lu, Yuning Mao, Xavier Mar- **758** tinet, Todor Mihaylov, Pushkar Mishra, Igor Moly- **759** bog, Yixin Nie, Andrew Poulton, Jeremy Reizen- **760** stein, Rashi Rungta, Kalyan Saladi, Alan Schelten, **761** Ruan Silva, Eric Michael Smith, Ranjan Subrama- **762** nian, Xiaoqing Ellen Tan, Binh Tang, Ross Tay- **763** lor, Adina Williams, Jian Xiang Kuan, Puxin Xu, **764** Zheng Yan, Iliyan Zarov, Yuchen Zhang, Angela Fan, **765** Melanie Kambadur, Sharan Narang, Aurélien Ro- **766** driguez, Robert Stojnic, Sergey Edunov, and Thomas **767** Scialom. 2023. [Llama 2: Open foundation and fine-](https://doi.org/10.48550/ARXIV.2307.09288) **768** [tuned chat models.](https://doi.org/10.48550/ARXIV.2307.09288) *CoRR*, abs/2307.09288. **769**

- Elena Voita, Javier Ferrando, and Christoforos Nalmpan- **770** tis. 2023. [Neurons in large language models: Dead,](https://doi.org/10.48550/ARXIV.2309.04827) **771** [n-gram, positional.](https://doi.org/10.48550/ARXIV.2309.04827) *CoRR*, abs/2309.04827. **772**
- Weixuan Wang, Barry Haddow, and Alexandra Birch. **773** 2023. Retrieval-augmented multilingual knowledge **774** editing. *arXiv preprint arXiv:2312.13040*. **775**
- Zeping Yu, Kailai Yang, Zhiwei Liu, and Sophia Anani- **776** adou. 2023. Exploring the residual stream of trans- **777** formers. *arXiv preprint arXiv:2312.12141*. **778**
- Zhengyan Zhang, Yankai Lin, Zhiyuan Liu, Peng Li, **779** Maosong Sun, and Jie Zhou. 2022. [Moefication:](https://doi.org/10.18653/V1/2022.FINDINGS-ACL.71) **780** [Transformer feed-forward layers are mixtures of ex-](https://doi.org/10.18653/V1/2022.FINDINGS-ACL.71) **781** [perts.](https://doi.org/10.18653/V1/2022.FINDINGS-ACL.71) In *Findings of the Association for Computa-* **782** *tional Linguistics: ACL 2022, Dublin, Ireland, May* **783** *22-27, 2022*, pages 877–890. Association for Com- **784** putational Linguistics. **785**

A Example Appendix **⁷⁸⁶**

A.1 Detailed Interpretation of Projection in **787** Vocabulary Space **788**

There is a residual connection in the each layer of **789** transformer, where the hidden state is: **790**

$$
h^l = x^l + FFN^l(x^l) \tag{8}
$$

794

(9) **800**

In order to analyze the behaviors of neurons, we **792** explore how the output distribution in the vocab- **793** ulary space changes when the representation x^l (before the FFN update) is added with the output of **795** neurons $A_i^l v_i^l$. With the embedding matrix E, we 796 map each vector into the vocabulary space ν . For $\frac{797}{2}$ each token w, the probability is calculate with the **798** softmax function: *799*

$$
p(w|x^{l} + A_{i}^{l}v_{i}^{l}, E)
$$

=
$$
\frac{exp(E_{w} \cdot x^{l} + E_{w} \cdot A_{i}^{l}v_{i}^{l})}{Z(E(x^{l} + A_{i}^{l}v_{i}^{l}))}
$$

$$
\propto exp(E_{w} \cdot x^{l}) \cdot exp(E_{w} \cdot A_{i}^{l}v_{i}^{l})
$$
 (9)

801 where E_w is the embedding of w, and $Z(\cdot)$ is the constant softmax normalization factor. The $E_w \cdot x^l$ can be viewed as a static score of w that is indepen- dent of the input to the model. Thus, the projection $E_w \cdot A_i^l v_i^l$ induces a ranking over the vocabulary. So we use the projection as effective score to detect the responsibility of neurons.

808 A.2 Prompts

802

 For the fact probing task, we use the P36 sub- testset, which describe facts of entities in a relation of "capital". The prompt is framed as " The capital of {X} is " where "{X}" is the subject (sovereign state) and LLMs are required to predict the object (capital city). We keep at least three paraphrase prompts from mParaRel for each language to en-sure a level of diversity.

 For the Natural Language Inference task, we frame the prompt as " Take the following as truth: {premise} Then the following statement: '{hypoth-esis}' is 'true', 'false', or 'inconclusive'? "

 For the cross-lingual KE task, we format the prompt as " {context} Question: {question} An- swer: ". The same language is used for the ques- tions and the answers, but the context is in a differ-ent language.

826 A.3 Supplemental Results of Neuron Behavior **827** Analysis

828 A.3.1 Neuron behaviors in additional **829** cross-lingual KE task

830 We already show the neuron behaviors in in cross-831 **lingual KE (EN (edit)** \rightarrow ALL (test)) task in Sec-**832** tion [5.1.1.](#page-3-2) We supply the analysis in the cross-833 lingual KE (ALL (edit) \rightarrow EN (test)) task in Fig-**834** ure [11.](#page-10-2)

Figure 11: Neuron behavior pattern in cross-lingual KE $(ALL (edit) \rightarrow EN (test))$ task.

A.3.2 Neurons Behaviors across LLMs **835**

Figure 12: Neuron behavior pattern in the XNLI task with XGLM backbone.

Figure 13: Neuron behavior pattern in the XNLI task with LLAMA2-7b-chat backbone.

Do the above-mentioned neuron behaviors **836** change over different LLMs? We further study the **837** neuron behaviors in other decoder-only multilin- **838** gual LLMs (XGLM and LLAMA2) and an encoder- **839** decoder multilingual LLM mT0. For the XNLI **840** task, the results of XGLM and LLAMA2-7b-chat **841** backbones are captured in Figure [12](#page-10-4) and Figure [13,](#page-10-5) **842** and the results of mT0-encoder and mT0-decoder **843** are shown in Figure [14](#page-11-6) and Figure [15.](#page-11-7) Further- **844** more, the percentage of four types of neurons for 845 inputs in each language on each LLM demonstrates **846** the similar pattern, indicating that neurons remain **847** consistent behaviors across LLM backbones. **848**

The number of active neurons increase in the **849** lower layers, followed by a decrease moving on- **850** wards and a rise in the upper layers, despite the **851** absolution values are different from those obtained **852** for BLOOMZ. Moreover, it could be observed that **853** encoder in mT0 involves more all-shared neurons **854** compared to the proportion in decoder. **855**

Figure 14: Neuron behavior pattern in the XNLI task in mT0-encoder.

Figure 15: Neuron behavior pattern in the XNLI task in mT0-decoder.

856 A.3.3 Influence of the Quantity of Languages

 We design an ablation study to investigate the in- fluence of the number of languages (i.e., in a series of 3, 5, 7, 9). The results of the XNLI task in re- sponse to the quantitative change in languages are illustrated in Figure [16.](#page-11-1) The rise in the number of languages is associated with an observable increase in the percentage of *partial-shared neurons* and a slight decrease in the percentage of *all-shared neu- rons*. This suggests that the quantity of languages has a minor impact on the *all-shared neurons*.

867 A.3.4 Neurons Behaviors Across Examples for **868** Other Tasks

 We conduct additional experiments on the XNLI **task and cross-lingual KE (EN (edit)** \rightarrow ALL (test)) task to investigate the behavior repeating for neu- rons. The results shown in Figures [17-](#page-12-3) [18](#page-12-4) are con- sistent with the results of the fact probing task, where only a few neurons maintain the same behav-iors across all examples in the testset.

Figure 16: Effects of the number of languages based on the XNLI task.

A.3.5 Activation percentage of BLOOM **876**

The results analyzed base on the foundation model **877** BLOOM of fact probing task and cross-lingual KE **878** task are shown in Figures [19](#page-12-5) - [21.](#page-13-3) **879**

A.3.6 Influence of Model Scale **880**

We investigate neuron behaviors across the 881 BLOOMZ series with 0.56b, 1b, 3b, 7.1b parame- **882** ters in a XNLI task. As shown in the results cap- **883** tured in Figure [22,](#page-14-0) no identifiable pattern differ- **884** ence can be observed to indicate a scale law ef- **885** fect. However, the scale of the model is limited, **886** potentially leading to unreliable results in this ex- **887** periment. More *non-activated neurons* in the upper **888** layers of BLOOMZ-7.1b may reflect on a higher 889 level of sparsity for a larger LLM (consistent with **890** [Voita et al.](#page-9-3) [\(2023\)](#page-9-3); [Li et al.](#page-8-6) [\(2023\)](#page-8-6)). **891**

A.3.7 Neuron Behaviors in Few-shot **892 In-context Learning 893**

According to [Wang et al.](#page-9-6) [\(2023\)](#page-9-6), in-context learn- **894** ing (ICL) can improve the performance of an LLM **895** under the guidance of few-shot examples in a cross- **896** lingual KE task. We further explore the impact **897** of few-shot examples on neuron behaviors. We **898** compare the results of an LLM with 0-shot, 2-shot, **899** 4-shot, 6-shot examples in a cross-lingual KE (EN **900** $(\text{edit}) \rightarrow \text{ALL}$ (test)) task. Four types of neurons **901** in scope have almost identical behaviors across **902** various few-shot examples (Figure [23\)](#page-14-1). Although **903** in-context examples lead to no observable neu- **904** ron behavioral changes, more examples lead to **905** better performances. Could ICL lead to a better **906**

Figure 17: Behavior-repeating neurons in XNLI task across the entire testset.

 neuron activation composition instead of invoking more neurons? We leave this to a future study.

A.3.8 Activation Value across Layers

 According to Eq. [1,](#page-2-1) neurons with larger activa- tion values tend to contribute more to the output. By visualizing neuron activation for a series of thresholds [0, 0.1, 0.2, 0.3, 0.4, 0.5], we can scru- tinize the relative importance of various types of activated neurons. The percentage of various types of activated neurons for each activation threshold in the XNLI task are shown in Figure [24.](#page-14-2) When ap- plying a threshold (>0), there are fewer all-shared, partial-shared, and *specific neurons* left in the lower layers (layers 0-10) compared to using a lower threshold (i.e., = 0). Under the same threshold scenario, more activated neurons appear in the sec- ond half of the model (layers 15-30). It is worth noting these neurons have a higher activation value than neurons activated from a lower threshold (i.e., $926 = 0$). Considering both the percentage of activated neurons and their corresponding activation value, it becomes apparent that the neurons in the upper layers contribute more to the output performance.

A.4 Supplemental Results of Neuron **Attribution**

A.4.1 Contribution Score of Different Tasks

 The contribution score of the four types of neu- rons evaluated on the fact probing task, XNLI task, cross-lingual KE task are shown in Figures [25](#page-15-1) - [28.](#page-16-1)

Figure 18: Behavior-repeating neurons in cross-lingual KE (EN (edit) \rightarrow ALL (test)) task across the entire testset.

Figure 19: Neuron behavior pattern in the fact probing task with BLOOM backbone.

A.4.2 Effective Score of Different Tasks **936**

The maximum, minimum, and average effective **937** scores of four types of neurons in 10 languages **938** evaluated on the cross-lingual KE (EN (edit) \rightarrow 939 ALL (test)) task are shown in Table [4.](#page-13-0) The maxi- **940** mum effective of four types of neurons across lay- **941** ers evaluated on the fact probing task, XNLI task, **942** cross-lingual KE (ALL (edit) \rightarrow EN (test)) task are **943** shown in Figures [29](#page-17-0) - [31.](#page-17-1) **944**

A.5 Supplemental Results of Effects on **945** Accuracy **946**

A.5.1 Effects with LLAMA Backbone **947**

In order to further prove the importance of *all-* **948** *shared neurons* across LLMs, we conduct the ex- **949**

	all-shared partial-shared					specific		non-activated				
	max	min	mean	max	min	mean	max	min	mean	max	min	mean
en	1.85	-0.94	0.07	0.22	-0.16	0.00	0.02	-0.02	0.00	0.04	-0.03	0.00
de	1.03	-0.60	0.02	0.13	-0.13	0.00	0.07	-0.03	0.00	0.02	-0.01	0.00
es	1.15	-0.84	0.02	0.12	-0.11	0.00	0.01	-0.01	0.00	0.02	-0.02	0.00
fr	1.06	-0.78	0.01	0.15	-0.11	0.00	0.03	-0.04	0.00	0.02	-0.02	0.00
ru	0.70	-0.45	0.00	0.24	-0.13	0.00	0.08	-0.03	0.00	0.01	-0.01	0.00
th	0.50	-0.90	0.00	0.17	-0.10	0.00	0.03	-0.05	0.00	0.01	-0.01	0.00
tr	0.82	-0.51	0.03	0.12	-0.12	0.00	0.04	-0.03	0.00	0.02	-0.02	0.00
V1	0.86	-0.68	0.01	0.15	-0.11	0.00	0.04	-0.04	0.00	0.02	-0.02	0.00
zh	0.52	-0.42	0.00	0.17	-0.20	0.00	0.08	-0.07	0.00	0.02	-0.01	0.00
pt	1.14	-0.83	0.02	0.11	-0.15	0.00	0.02	-0.02	0.00	0.02	-0.02	0.00

Table 4: Maximum, minimum, average effective score of the four types of neurons on the cross-lingual KE (EN $(edit) \rightarrow ALL (test))$ task.

Figure 20: Neuron behavior pattern in the cross-lingual KE (ALL (edit) \rightarrow EN (test)) task with BLOOM backbone.

accuracy	en			de es fr ru th tr vi	zh
baseline				59.1 47.6 50.1 47.0 49.1 41.4 40.2 51.6 46.1	
w/o. all-shared				3.0 3.6 4.4 1.9 4.7 6.9 3.6 13.5 4.8	
w/o. specific				59.2 47.3 49.9 47.0 49.1 41.9 40.1 51.4 46.2	
w/o. partial-shared				59.1 48.4 51.5 47.9 49.7 42.9 41.5 50.8 48.0	

Table 5: The effects of accuracy on the XNLI task with LLAMA2-7b-chat backbone, when deactivating *all-shared neurons*, *specific neurons*, and *partial-shared neurons*, respectively. "w/o." stands for "without".

 periments with deactivating neurons on the XNLI task with LLAMA2-7b-chat backbone. The results in Table [5](#page-13-1) show that there is more significant effect when *all-shared neurons* are deactivated. It demon- strates that *all-shared neurons* play a key role in predicting correct answers across LLMs.

956 A.5.2 Effects on the Cross-lingual KE Task

 We further explore the influence of deactivating *all-shared neurons*, *specific neurons*, and *partial- shared neurons* on the cross-lingual KE (EN (edit) \rightarrow ALL (test)) task with BLOOMZ backbone. The results in Table [6](#page-14-3) are consistent with the results of XNLI task in Table [2,](#page-7-1) demonstrating the critical role of *all-shared neurons* for generating correct

Figure 21: Neuron behavior pattern in the cross-lingual KE (EN (edit) \rightarrow ALL (test)) task with BLOOM backbone.

output. **964**

accuracy	en	de	es	tr	nt.	th	tr	ru	V1	zh
baseline	96.23	46.84	36.88	40.38	35.80	4.71	28.13	0.67	40.92	10.63
w/o. all-shared	15.21	9.69	5.52	4.98	7.67	0.54	2.42	0.00	7.67	2.96
w/o. specific	96.23	46.84	36.74	40.24	35.53	4.71	29.21	0.67	40.65	11.84
w/o. partial-shared	68.78	44.95	35.40	37.01	34.19	-5.11	25.44	0.67	39.84	8.48

Table 6: The effects of accuracy on the cross-lingual KE (EN (edit) \rightarrow ALL (test)) task with BLOOMZ backbone, when deactivating *all-shared neurons*, *specific neurons*, and *partial-shared neurons*, respectively. "w/o." stands for "without".

Figure 22: Neuron behavior pattern in a XNLI task with the model size as 0.56b, 1b, 3b, 7b.

Figure 23: Neuron behavior pattern in cross-lingual KE $(EN (edit) \rightarrow ALL (test))$ task with BLOOMZ backbone under the in-context learning.

Figure 24: Neuron behaviors in a XNLI task with BLOOMZ backbone under the threshold in $[0, 0.1, 0.2, 0.3, 0.4, 0.5].$

Figure 25: Contribution proportion of four types of neurons based on the fact probing task with BLOOMZ backbone.

Figure 26: Contribution proportion of four types of neurons based on the XNLI task with BLOOMZ backbone.

Figure 27: Contribution proportion of four types of neurons based on the cross-lingual KE (EN (edit) \rightarrow ALL (test)) task with BLOOMZ backbone.

Figure 28: Contribution proportion of four types of neurons based on the cross-lingual KE (ALL (edit) \rightarrow EN (test)) task with BLOOMZ backbone.

Figure 29: Effective score of four types of neurons based on the fact probing task with BLOOMZ backbone.

Figure 30: Effective score of four types of neurons based on the XNLI task with BLOOMZ backbone.

Figure 31: Effective score of four types of neurons based on the cross-lingual KE (ALL (edit) \rightarrow EN (test)) task with BLOOMZ backbone.