

# 000 001 002 003 004 005 FLOWCAST: ADVANCING PRECIPITATION 006 NOWCASTING WITH CONDITIONAL FLOW MATCHING 007 008 009

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## ABSTRACT

028 Radar-based precipitation nowcasting, the task of forecasting short-term precipi-  
029 tation fields from previous radar images, is a critical problem for flood risk man-  
030 agement and decision-making. While deep learning has substantially advanced  
031 this field, two challenges remain fundamental: the uncertainty of atmospheric  
032 dynamics and the efficient modeling of high-dimensional data. Diffusion mod-  
033 els have shown strong promise by producing sharp, reliable forecasts, but their  
034 iterative sampling process is computationally prohibitive for time-critical applica-  
035 tions. We introduce FlowCast, the first end-to-end probabilistic model leveraging  
036 Conditional Flow Matching (CFM) as a direct noise-to-data generative framework  
037 for precipitation nowcasting. Unlike hybrid approaches, FlowCast learns a direct  
038 noise-to-data mapping in a compressed latent space, enabling rapid, high-fidelity  
039 sample generation. Our experiments demonstrate that FlowCast establishes a new  
040 state-of-the-art in probabilistic performance while also exceeding deterministic  
041 baselines in predictive accuracy. A direct comparison further reveals the CFM  
042 objective is both more accurate and significantly more efficient than a diffusion  
043 objective on the same architecture, maintaining high performance with signifi-  
044 cantly fewer sampling steps. This work positions CFM as a powerful and practical  
045 alternative for high-dimensional spatiotemporal forecasting.  
046

## 047 1 INTRODUCTION 048

049 Accurate and timely short-term precipitation forecasts, or nowcasting, are of paramount importance  
050 due to their significant socio-economic impacts, such as issuing flood warnings and managing water  
051 resources. Precipitation nowcasting, as defined in this work, involves predicting a sequence of future  
052 radar images from historical observations for the immediate future up to a few hours (An et al.,  
053 2025). Traditional methods, like Eulerian and Lagrangian persistence (Germann & Zawadzki, 2002),  
054 rely on advecting the current precipitation field. However, their simplified physical assumptions  
055 limit their ability to capture the complex, non-linear dynamics of atmospheric processes, especially  
056 for rapidly evolving weather systems (Prudden et al., 2020).  
057

058 Deep learning has introduced a paradigm shift in precipitation nowcasting. Deterministic mod-  
059 els based on recurrent and transformer architectures learn complex spatiotemporal patterns directly  
060 from large volumes of radar data (Prudden et al., 2020; An et al., 2025). While these models outper-  
061 form traditional methods, optimizing for metrics like Mean Squared Error (MSE) compels them to  
062 produce a single, best-guess forecast. This often results in overly smooth predictions at longer lead  
063 times, failing to capture the inherent uncertainty in precipitation evolution and underrepresenting  
064 high-impact weather events.  
065

066 To address this, probabilistic generative models have become central to modern nowcasting, aiming  
067 to predict a distribution over many plausible futures. Diffusion models (Ho et al., 2020), in particu-  
068 lar, have emerged as the state-of-the-art, producing sharp and reliable ensemble forecasts (Gao et al.,  
069 2023; Leinonen et al., 2023; Gong et al., 2024). However, this performance comes at a steep price:  
070 their reliance on an iterative denoising process, often requiring hundreds of function evaluations for  
071 a single forecast, makes them computationally expensive. This high Number of Function Evaluations  
072 (NFE) poses a significant barrier to practical application in time-critical scenarios where rapid  
073 ensemble generation is crucial.  
074

This work introduces FlowCast, a novel probabilistic nowcasting model built on Conditional Flow Matching (CFM) (Lipman et al., 2023; Tong et al., 2024), a powerful and efficient alternative designed for rapid sampling. While recent work has applied rectified flows for the deterministic refinement of blurry forecasts (Feng et al., 2025), FlowCast is, to our knowledge, the first to successfully apply CFM as a full, noise-to-data generative model for this task. We demonstrate that FlowCast alleviates the tension between accuracy and efficiency, establishing a new state-of-the-art by exceeding the performance of leading diffusion models while offering a superior performance-cost trade-off.

We argue that CFM offers not only a computational advantage but also a superior inductive bias for this domain, specifically regarding the simplified transport of probability mass. Radar reflectivity distributions are highly multi-modal yet exhibit strong local temporal consistency. Standard diffusion models map Gaussian noise to this complex manifold via stochastic denoising or curved probability flow ODEs, often necessitating many sampling steps to resolve fine-grained structures without blurring modes. In contrast, CFM imposes a straight-line ODE prior on the generative process. This enforces the simplest possible mapping between the noise and data distributions. In the context of spatiotemporal forecasting, where temporal coherence is essential, this linear interpolation provides a much stronger and more stable prior than the winding paths of diffusion. We demonstrate that this geometric simplification allows FlowCast to maintain high fidelity with significantly fewer function evaluations.

Our contributions are summarized as follows:

- We introduce FlowCast, a novel full-probabilistic application of Conditional Flow Matching to precipitation nowcasting.
- We establish a new state-of-the-art in both probabilistic performance and predictive accuracy on two diverse radar datasets, the benchmark SEVIR dataset (Viellette et al., 2020) and the local ARSO dataset.
- We provide a direct ablation study showing that the CFM objective is both more accurate and more computationally efficient than a diffusion objective on the same architecture, maintaining high performance with substantially fewer sampling steps.

## 2 RELATED WORK

### 2.1 DETERMINISTIC NOWCASTING

Deep learning for precipitation nowcasting has evolved from RNN-based architectures to Transformer-based models. Early work includes ConvLSTM (Shi et al., 2015), extending LSTMs with convolutions for spatiotemporal data, and the PredRNN family (Wang et al., 2017; 2023), which introduced a spatiotemporal memory flow for improved long-range dependency modeling. More recently, Transformer architectures like Earthformer (Gao et al., 2022) and Earthfarseer (Wu et al., 2024) have set new benchmarks by using attention to model complex global dynamics. A common limitation of deterministic models is that they produce overly smooth forecasts when trained with pixel-wise losses (e.g., MSE), as they average over possible futures.

### 2.2 PROBABILISTIC NOWCASTING

To address uncertainty quantification, probabilistic models have become central to nowcasting, aiming to sample from the full distribution of future states.

**GANs and Diffusion.** GANs (Ravuri et al., 2021) were an early approach for producing sharp forecasts but suffer from training instability. Diffusion models (Ho et al., 2020) have recently emerged as the state-of-the-art, offering stable training and high-quality samples. PreDiff (Gao et al., 2023) and LDCast (Leinonen et al., 2023) are prominent latent diffusion models for ensemble forecasting. A notable hybrid is CasCast (Gong et al., 2024), which uses a deterministic model for large-scale patterns and a conditional diffusion model to refine stochastic details.

**Flow-Based Generative Models.** Generative modeling with flows offers an attractive alternative to diffusion. Traditional Continuous Normalizing Flows (CNFs) (Chen et al., 2018) model data

108 via ODEs but require expensive numerical integration during training to compute likelihoods, making  
 109 them computationally prohibitive for high-dimensional spatiotemporal data. Conditional Flow  
 110 Matching (CFM) (Lipman et al., 2023) and Rectified Flows (Liu et al., 2023) overcome this by  
 111 regressing a vector field against a conditional probability path, enabling simulation-free training.  
 112 However, while standard Rectified Flows typically utilize a singular conditional path (effectively  
 113  $\sigma \rightarrow 0$ ), our application of Independent CFM (I-CFM) incorporates a Gaussian probability path  
 114 with  $\sigma > 0$ . This "thickens" the training trajectory, providing crucial regularization that stabilizes  
 115 the learning of the vector field for high-dimensional data compared to the singular paths of rectified  
 116 flows.

117 Crucially, while diffusion models rely on stochastic denoising paths that are often curved and require  
 118 many sampling steps, CFM allows for learning straight-line ODE trajectories between noise and  
 119 data (Tong et al., 2024). This geometric property enforces a direct mapping that preserves temporal  
 120 coherence and allows for rapid sampling. While Feng et al. (2025) recently used a rectified flow  
 121 module to strictly refine deterministic forecasts, FlowCast applies CFM as a standalone probabilistic  
 122 generative model. This allows it to learn the full noise-to-data distribution and capture multimodal  
 123 uncertainty without relying on a deterministic base forecast.

### 125 3 METHOD

127 Our approach to probabilistic nowcasting is based on Conditional Flow Matching (CFM) within a  
 128 compressed latent space. This section details our methodology, covering the problem formulation,  
 129 our latent CFM framework, the model architecture, and the training and sampling procedures.

#### 131 3.1 TASK FORMULATION

133 Precipitation nowcasting is framed as a video prediction task. Given a sequence of  $T_{\text{in}}$  past radar  
 134 observations,  $\mathbf{X}_{\text{past}} = \{x_1, x_2, \dots, x_{T_{\text{in}}}\}$ , where each  $x_t \in \mathbb{R}^{H \times W \times C}$  is a radar map, the objective  
 135 is to generate a probabilistic forecast for the next  $T_{\text{out}}$  frames,  $\mathbf{X}_{\text{future}} = \{x_{T_{\text{in}}+1}, \dots, x_{T_{\text{in}}+T_{\text{out}}}\}$ .

#### 137 3.2 LATENT CONDITIONAL FLOW MATCHING

138 To reduce the high computational cost of generative modeling, we adopt a two-stage ap-  
 139 proach inspired by latent diffusion models (Rombach et al., 2022). A Variational Autoencoder  
 140 (VAE) (Kingma & Welling, 2014) compresses high-dimensional radar frames into low-dimensional  
 141 latents, which are used to train a generative model in the latent space.

142 Our generative model is built on the Conditional Flow Matching (CFM) framework (Lipman et al.,  
 143 2023), which trains a continuous normalizing flow by learning a vector field  $v_{\theta}$  that maps samples  
 144 from a prior distribution (e.g., Gaussian) to the target data distribution. We use Independent CFM (I-  
 145 CFM) (Tong et al., 2024), which defines a probability path  $p_t(x_t|x_0, x_1)$  as a Gaussian distribution  
 146 with mean  $(1-t)x_0 + tx_1$  and a small constant standard deviation  $\sigma$ . This path interpolates between  
 147 a noise sample  $x_0 \sim \mathcal{N}(0, I)$  and a data sample  $x_1$ . The corresponding target vector field is their  
 148 difference,  $u_t = x_1 - x_0$ . This formulation enables direct, simulation-free training of the model  $v_{\theta}$   
 149 by regressing it against this target field.

##### 151 3.2.1 FRAME-WISE AUTOENCODER

152 To learn a compact latent space, we train a VAE on individual radar frames. The architecture,  
 153 inspired by Esser et al. (2021), uses a hierarchical encoder  $\mathcal{E}$  and decoder  $\mathcal{D}$  with residual and  
 154 self-attention blocks for high-fidelity reconstructions. The VAE is trained with a combination of a  
 155 L1 reconstruction loss, a KL-divergence regularizer, and a PatchGAN adversarial loss (Isola et al.,  
 156 2017) to enhance perceptual quality. After training, the VAE's weights are frozen and it is used to  
 157 encode inputs and decode latent predictions.

##### 159 3.2.2 FLOWCAST ARCHITECTURE

161 We propose **FlowCast**, which consists of the adaptation of Earthformer-UNet (Gao et al., 2023)  
 for the CFM objective. FlowCast employs a U-Net-like encoder-decoder structure where the core

building blocks are Cuboid Attention layers from Earthformer (Gao et al., 2022). This mechanism efficiently processes spatiotemporal data by applying self-attention locally within 3D "cuboids" of the data, capturing local dynamics, while global information is shared across the hierarchical U-Net structure. The model is conditioned on the flow time  $t$ , which is converted into an embedding and injected at each level of the network, enabling the model to accurately approximate the time-dependent vector field  $v_\theta$ . The architecture is illustrated in Figure 1.

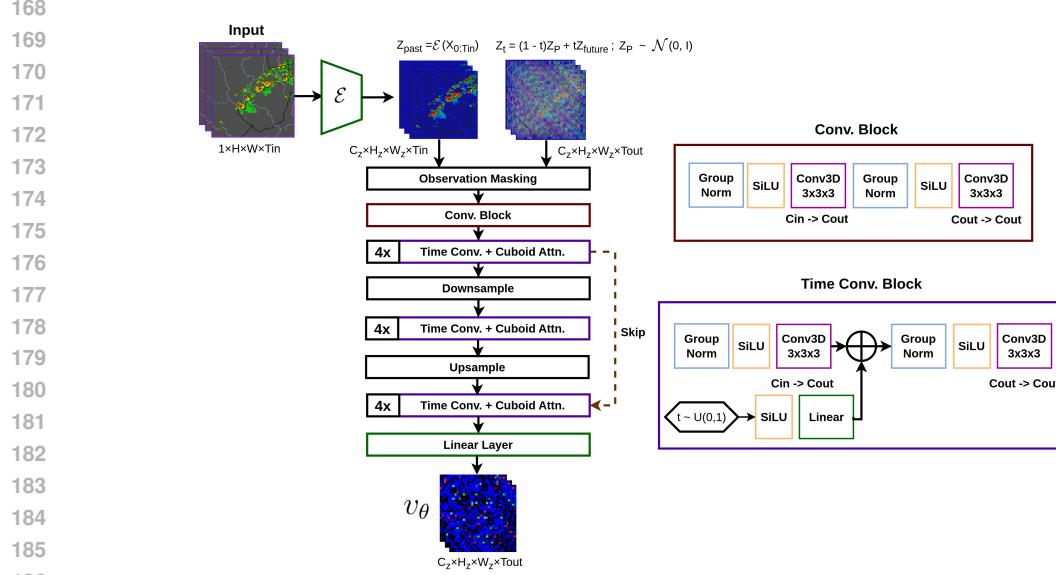


Figure 1: The FlowCast architecture. A U-Net with Cuboid Attention blocks processes latent spatiotemporal data. Conditioning on the flow time  $t$  enables the model to learn the time-dependent vector field for generating forecasts.

**Training.** The FlowCast model learns the vector field  $v_\theta(Z_t, t, Z_{\text{past}})$ . The complete training procedure is detailed in Algorithm 1.

#### Algorithm 1 FlowCast Training Process

**Require:** Dataset  $\mathcal{D}$ , Pre-trained VAE Encoder  $\mathcal{E}$ , FlowCast Model  $v_\theta$ , standard deviation  $\sigma$ .

```

1: Initialize model parameters  $\theta$ 
2: while not converged do
3:   Sample a batch of radar sequences  $(X_{\text{past}}, X_{\text{future}}) \sim \mathcal{D}$ 
4:   Encode sequences into latent space:  $Z_{\text{past}} \leftarrow \mathcal{E}(X_{\text{past}})$  and  $Z_{\text{future}} \leftarrow \mathcal{E}(X_{\text{future}})$ 
5:   Sample prior noise  $Z_P \sim \mathcal{N}(0, I)$ , time  $t \sim \mathcal{U}(0, 1)$  and path Gaussian noise  $\epsilon \sim \mathcal{N}(0, I)$ 
6:   Compute interpolated latent state:  $Z_t \leftarrow (1-t)Z_P + tZ_{\text{future}} + \sigma\epsilon$ 
7:   Compute target vector field:  $u_t \leftarrow Z_{\text{future}} - Z_P$ 
8:   Predict vector field:  $\hat{v} \leftarrow v_\theta(Z_t, t, Z_{\text{past}})$ 
9:   Compute Loss:  $\mathcal{L} \leftarrow \|\hat{v} - u_t\|^2$ 
10:  Gradient step:  $\theta \leftarrow \theta - \eta \nabla_\theta \mathcal{L}$ 
11: end while

```

**Sampling.** To generate an ensemble of forecasts, we solve the learned ODE starting from noise, using the Euler method (Hairer et al., 1993). This process is described in Algorithm 2.

## 4 EXPERIMENTS

### 4.1 EXPERIMENTAL SETTING

More details about the experimental setting are provided in Appendix A.1.

216 **Algorithm 2** FlowCast Ensemble Sampling

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217 **Require:** Past radar sequence  $X_{\text{past}}$ , Trained FlowCast Model  $v_{\theta}$ , VAE Encoder  $\mathcal{E}$  / Decoder  $\mathcal{D}$ .

218 **Require:** Ensemble size  $N$ , Number of ODE steps  $S$ .

219 **Ensure:** Ensemble forecasts  $\{\hat{X}_{\text{future}}^{(k)}\}_{k=1}^N$ .

220 1: Encode past observations:  $Z_{\text{past}} \leftarrow \mathcal{E}(X_{\text{past}})$

221 2: **for**  $k = 1$  **to**  $N$  **do**

222 3: Sample initial state:  $Z(0) \sim \mathcal{N}(0, I)$

223 4: Set step size:  $\Delta t \leftarrow 1/S$

224 5: Set current state:  $Z_{\text{curr}} \leftarrow Z(0)$

225 6: **for**  $i = 0$  **to**  $S - 1$  **do**

226 7: Current time:  $t \leftarrow i \cdot \Delta t$

227 8: Predict vector field:  $v \leftarrow v_{\theta}(Z_{\text{curr}}, t, Z_{\text{past}})$

228 9: Update state (Euler step):  $Z_{\text{curr}} \leftarrow Z_{\text{curr}} + v \cdot \Delta t$

229 10: **end for**

230 11: Final latent forecast:  $Z(1) \leftarrow Z_{\text{curr}}$

231 12: Decode to pixel space:  $\hat{X}_{\text{future}}^{(k)} \leftarrow \mathcal{D}(Z(1))$

232 13: **end for**

233 14: **return** Ensemble predictions  $\{\hat{X}_{\text{future}}^{(k)}\}_{k=1}^N$

---

234  
235 4.1.1 DATASETS

236 We evaluate on two 5-minute, 1 km-resolution radar datasets: SEVIR, a US benchmark, and ARSO, a Slovenian composite for a local deployment setting. For both, we predict 12 frames (1 hour) from 237 13 past frames (65 minutes), per the SEVIR Nowcasting Challenge protocol (Veillette et al., 2020).

241  
242 Table 1: Summary of datasets used for evaluation.

243

Dataset	N <sub>train</sub>	N <sub>val</sub>	N <sub>test</sub>	Resolution	Dimensionality	Interval	Lag/Lead
SEVIR	36,351	9,450	12,420	1 km	384×384	5 min	13/12
ARSO	38,229	12,743	12,744	1 km	301×401	5 min	13/12

244 **SEVIR.** SEVIR (Veillette et al., 2020) provides over 10,000 weather events in a 384×384 km US  
245 domain, each spanning 4 hours at 5-minute resolution. We use the 1-km Vertically Integrated Liquid  
246 (VIL) field. Following the standard chronological split, we extract 25-frame sequences (13 context,  
247 12 target) with a stride of 12, yielding 36,351 training, 9,450 validation, and 12,420 test samples.

248 **ARSO.** The ARSO dataset contains 5-minute, 1-km radar reflectivity composites over a 301×401  
249 km Slovenian grid, capturing complex Alpine and coastal dynamics. Using the same 25-frame  
250 sequence setup but with stride 1, a 60/20/20 chronological split yields 38,229 training, 12,743 vali-  
251 dation, and 12,744 test samples.

## 252 4.1.2 EVALUATION

253 **Threshold-based categorical scores:** Following prior work (Veillette et al., 2020; Gao et al.,  
254 2023; Gong et al., 2024), we evaluate forecasts by converting radar fields to binary masks at given  
255 thresholds and computing the False Alarm Ratio (FAR), Critical Success Index (CSI), and Heidke  
256 Skill Score (HSS). For spatial validation, we compute the max-pooled CSI and Fractions Skill Score  
257 (FSS) over 16×16 km neighborhoods (CSI-M-P16 and FSS-M-P16). We report the mean of these  
258 scores across all thresholds ("M") to evaluate general performance. Furthermore, to rigorously as-  
259 sess the detection of extreme weather events, we separately report the categorical metrics specifically  
260 at the highest intensity thresholds for each dataset.

261 For SEVIR, we follow the literature in using the thresholds [16, 74, 133, 160, 181, 219]. For ARSO,  
262 we use the thresholds [15, 21, 30, 33, 36, 39] dBZ, derived through quantile mapping to ensure that  
263 each threshold corresponds to approximately the same exceedance probability in both datasets.

270    **Continuous Ranked Probability Score (CRPS):** We use the CRPS to evaluate probabilistic skill.  
 271    A lower CRPS indicates a more accurate and sharp forecast. For deterministic forecasts ( $N = 1$ ),  
 272    CRPS reduces to the Mean Absolute Error.  
 273

274    **Ensemble forecasting:** Let  $x_{t,i,j}$  represent the ground truth pixel value at location  $(i, j)$  and lead  
 275    time  $t$ . All probabilistic models are evaluated using an ensemble of  $N = 8$  realizations. For categori-  
 276    cal scores, we evaluate the ensemble mean prediction (Metric of Ensemble Mean), first computing  
 277    the ensemble mean  $\hat{x}_{t,i,j} = \frac{1}{N} \sum_{k=1}^N \hat{x}_{t,i,j}^{(k)}$  and then the metric on this mean forecast.  
 278

279    4.1.3 TRAINING DETAILS  
 280

281    **VAE.** We train a separate Variational Autoencoder (VAE) for each dataset to create a specialized  
 282    latent space. We follow the architecture and training procedure from Rombach et al. (2022), with a  
 283    Kullback-Leibler divergence loss weight of 1e-4, the AdamW optimizer with a learning rate of 1e-4,  
 284    and a batch size of 12. The compressed latent space dimensions are shown in Table 2.  
 285

286    Table 2: VAE latent space dimensions  
 287

288 <b>Dataset</b>	289 <b>Original Dimensions</b> $(T_{\text{in}}/T_{\text{out}} \times \mathbf{H} \times \mathbf{W} \times \mathbf{C}_{\text{in}})$	289 <b>Latent Dimensions</b> $(T_{\text{in}}/T_{\text{out}} \times \mathbf{H}_z \times \mathbf{W}_z \times \mathbf{C}_z)$
291    SEVIR	13/12 $\times$ 384 $\times$ 384 $\times$ 1	13/12 $\times$ 48 $\times$ 48 $\times$ 4
292    ARSO	13/12 $\times$ 301 $\times$ 401 $\times$ 1	13/12 $\times$ 38 $\times$ 52 $\times$ 4

294    **FlowCast.** We train our CFM model for 200 epochs using the AdamW optimizer with a learning  
 295    rate of 5e-4 and a cosine scheduler. We set the standard deviation of the I-CFM probability path to  
 296    a small constant  $\sigma = 0.01$  (Tong et al., 2024). We observed that the training process was notably  
 297    stable; unlike diffusion objectives which often require complex loss weighting schedules, the I-CFM  
 298    objective utilizes a simple regression loss that converged robustly without extensive hyperparameter  
 299    tuning. Model checkpoints are maintained using an exponential moving average of weights (Ho  
 300    et al., 2020), with a decay factor of 0.999, and we keep the model checkpoint with the highest CSI-  
 301    M evaluated on a subset of the validation set. The model is trained with 4 NVIDIA H100 for 7 days,  
 302    with a global batch size of 12. Further implementation details are provided in Appendix A.1.  
 303

304    4.1.4 INFERENCE DETAILS  
 305

306    Generating a forecast with FlowCast involves solving the learned ODE to transform a noise-  
 307    initialized latent sequence into a prediction, conditioned on encoded past observations. Following  
 308    the procedure outlined in 3.2.2, we use the Euler method (Hairer et al., 1993) with 10 steps as the  
 309    ODE solver. To generate a probabilistic ensemble forecast, this process is repeated eight times with  
 310    different initial noise samples  $Z(0) \sim \mathcal{N}(0, \mathbf{I})$ .  
 311

312    4.2 COMPARISON TO THE STATE OF THE ART  
 313

314    We evaluate FlowCast against four deterministic baselines: U-Net (Veillette et al., 2020), Earth-  
 315    former (Gao et al., 2022), Earthfarseer (Wu et al., 2024), and SimVPv2 (Tan et al., 2025), as well as  
 316    two probabilistic baselines: PreDiff (Gao et al., 2023) and CasCast (Gong et al., 2024). All models  
 317    are trained following their publicly released code, with the training budget fixed at 200 epochs. For  
 318    probabilistic models, we adopt our evaluation protocol by selecting the checkpoint with the highest  
 319    CSI-M on a validation subset, using exponential moving average weights.  
 320

321    **General Performance (SEVIR & ARSO).** As shown in Table 3, Figure 2, Table 4 and Figure 3,  
 322    FlowCast establishes a new state-of-the-art across both diverse datasets. On SEVIR, it achieves  
 323    the highest overall CSI-M, FSS-M-P16, and HSS-M and the lowest CRPS, demonstrating superior  
 324    probabilistic calibration. On ARSO, FlowCast outperforms all baselines in all metrics besides FAR-  
 325    M. Notably, on SEVIR, while the probabilistic baseline CasCast achieves the highest CSI-P16-M, it  
 326    suffers from a significantly higher FAR-M compared to FlowCast (0.383 vs. 0.325). This indicates  
 327

that FlowCast strikes a superior balance between detection sensitivity and precision, avoiding the tendency to over-predict precipitation coverage. Deterministic models achieve the lowest FAR-M scores by predicting blurry fields at longer lead times, missing the most extreme events (CSI-219).

**Performance on Extreme Events.** To evaluate the ability of the models to detect extreme events, we report performance at the highest intensity thresholds for both datasets in Table 5. FlowCast demonstrates a decisive advantage here. On SEVIR (Threshold 219), FlowCast achieves a CSI of 0.202, outperforming the best deterministic baseline (SimVP, 0.137) by over 47% and the leading probabilistic baseline (CasCast, 0.195). The trend holds for ARSO (Threshold 39 dBZ), where FlowCast achieves the highest CSI (0.183) and HSS (0.291). Crucially, FlowCast maintains this high detection skill while achieving a lower FAR than CasCast across all extreme thresholds, confirming its ability to generate sharp, intense features without resorting to excessive false alarms.

Table 3: Comparison of FlowCast with baseline models on the SEVIR dataset. All metrics are computed over a 12-step forecast, except "Forecast @ +65 min" which only uses the last frame.

Model	CRPS ↓	Forecast @ 12 steps					Forecast @ +65 min	
		CSI-M ↑	CSI-P16-M ↑	FSS-P16-M ↑	HSS-M ↑	FAR-M ↓	CSI-M ↑	CSI-219 ↑
U-Net	0.0273	0.394	0.384	0.661	0.497	0.308	0.259	0.009
Earthformer	0.0252	0.411	0.407	0.686	0.518	<b>0.285</b>	0.280	0.016
Earthfarseer	0.0256	0.389	0.393	0.636	0.486	0.289	0.247	0.001
SimVP	0.0249	0.423	0.424	0.701	0.532	0.298	0.280	0.012
PreDiff	0.0189	0.413	0.423	0.699	0.523	0.313	0.281	0.018
CasCast	0.0201	0.442	<b>0.520</b>	0.763	0.562	0.383	0.311	0.054
<b>FlowCast</b>	<b>0.0182</b>	<b>0.460</b>	0.506	<b>0.767</b>	<b>0.580</b>	0.325	<b>0.324</b>	<b>0.057</b>

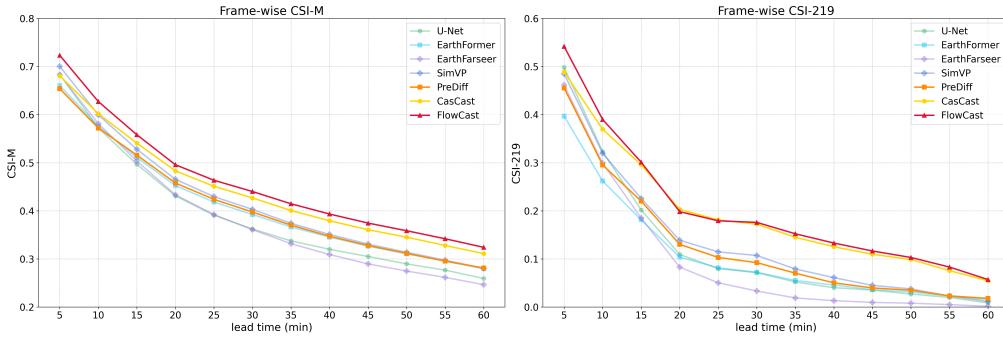


Figure 2: CSI-M and CSI at the 219 threshold per lead time on the SEVIR dataset. FlowCast shows consistent improvement over baselines for CSI-M and avoids the oversmoothing of deterministic models at longer lead times (CSI-219).

Table 4: Comparison of FlowCast with baseline models on the ARSO dataset. All metrics are computed over a 12-step forecast, except "Forecast @ +65 min" which only considers the last frame.

Model	CRPS ↓	Forecast @ 12 steps					Forecast @ +65 min	
		CSI-M ↑	CSI-P16-M ↑	FSS-P16-M ↑	HSS-M ↑	FAR-M ↓	CSI-M ↑	CSI-39 ↑
U-Net	0.0264	0.399	0.432	0.659	0.505	0.371	0.260	0.011
Earthformer	0.0270	0.403	0.439	0.691	0.512	0.409	0.274	0.010
Earthfarseer	0.0280	0.368	0.406	0.588	0.463	<b>0.358</b>	0.233	0.004
SimVP	0.0267	0.415	0.462	0.699	0.526	0.401	0.288	0.029
PreDiff	0.0211	0.369	0.411	0.614	0.471	0.400	0.241	0.010
CasCast	0.0253	0.373	0.511	0.712	0.483	0.488	0.277	0.057
<b>FlowCast</b>	<b>0.0209</b>	<b>0.420</b>	<b>0.514</b>	<b>0.738</b>	<b>0.535</b>	0.422	<b>0.315</b>	<b>0.073</b>

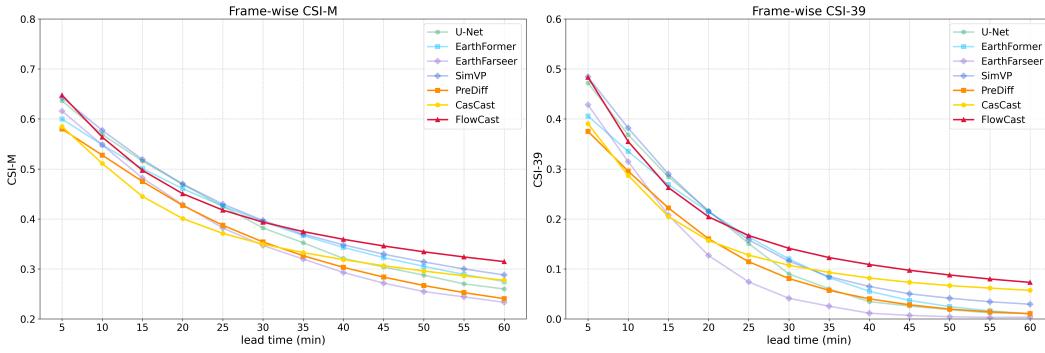


Figure 3: CSI-M and CSI at the 39 DBz threshold per lead time on the ARSO dataset. FlowCast shows significant improvements over probabilistic baselines for earlier lead times, and over deterministic baselines for later lead times.

Table 5: Comparison of FlowCast with baseline models on SEVIR and ARSO datasets for extreme events using categorical metrics with the highest thresholds per dataset. All metrics are computed over a 12-step forecast.

Model	SEVIR						ARSO					
	CSI		HSS		FAR		CSI		HSS		FAR	
	181	219	181	219	181	219	36	39	36	39	36	39
U-Net	0.205	0.122	0.314	0.193	0.366	0.508	0.209	0.145	0.318	0.226	0.474	0.505
Earthformer	0.229	0.109	0.348	0.180	0.354	<b>0.343</b>	0.216	0.145	0.335	0.231	0.531	0.553
Earthfarseer	0.194	0.097	0.291	0.152	<b>0.341</b>	0.412	0.159	0.104	0.245	0.164	<b>0.445</b>	<b>0.449</b>
SimVP	0.244	0.137	0.365	0.220	0.370	0.404	0.238	0.162	0.362	0.254	0.507	0.540
PreDiff	0.237	0.128	0.361	0.206	0.384	0.467	0.176	0.118	0.277	0.193	0.520	0.566
CasCast	0.286	0.195	0.427	0.309	0.501	0.567	0.202	0.142	0.320	0.235	0.647	0.694
<b>FlowCast</b>	<b>0.301</b>	<b>0.202</b>	<b>0.443</b>	<b>0.317</b>	0.425	0.482	<b>0.254</b>	<b>0.183</b>	<b>0.388</b>	<b>0.291</b>	0.547	0.589

Figure 4 qualitatively compares forecast sequences from FlowCast with the baselines on the SEVIR dataset. FlowCast produces sharp, perceptually realistic forecasts, avoiding the smoothness of deterministic models. Compared to the best-performing probabilistic baseline CasCast, we observe more realistic precipitation patterns, especially at longer lead times. More examples, including on ARSO, are provided in Appendix A.2.

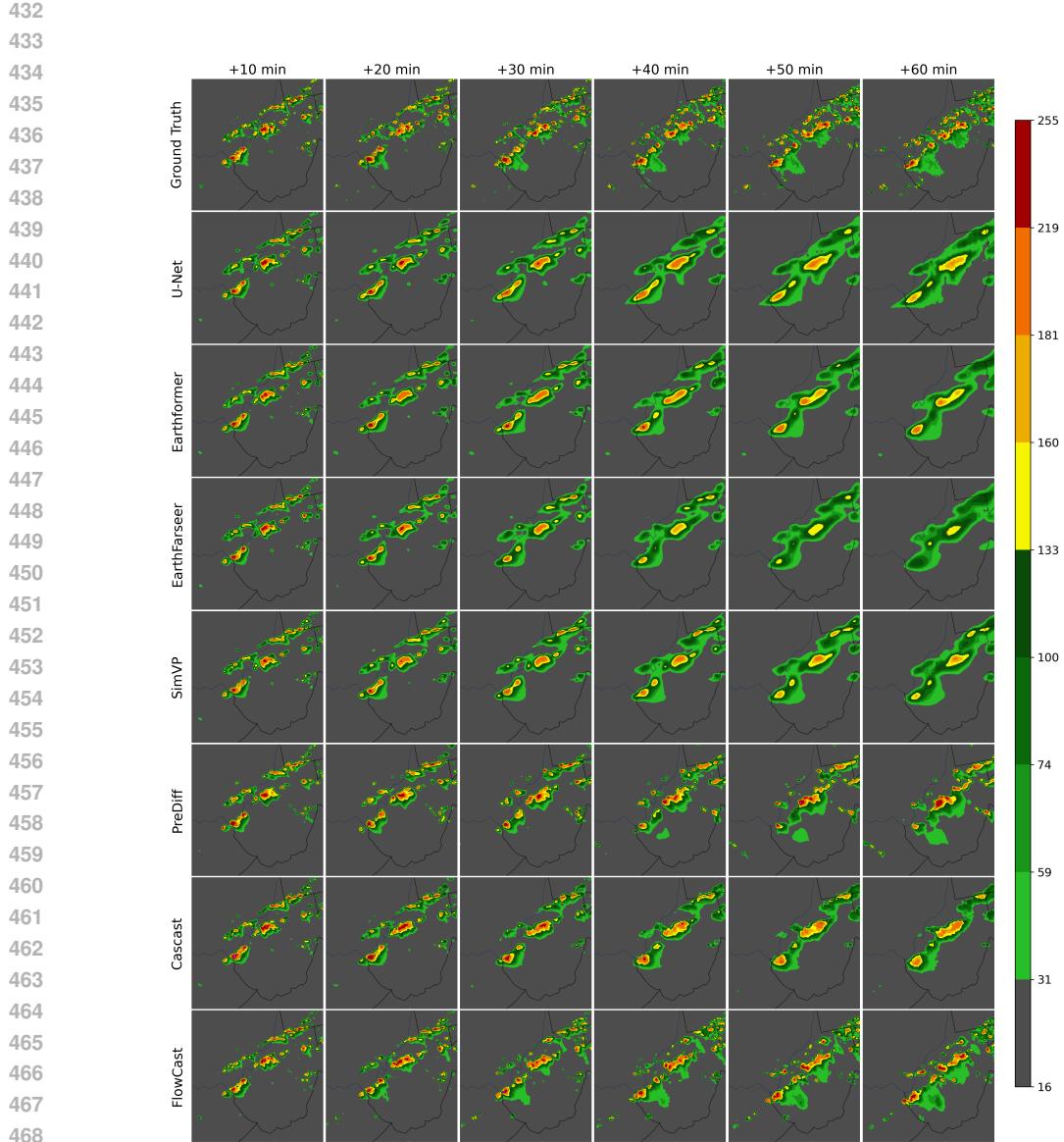
### 4.3 ABLATION STUDIES

Due to computational constraints, all ablation studies were run on the first 10% of the SEVIR test set using a single NVIDIA A100 GPU.

#### 4.3.1 CFM OBJECTIVE AGAINST DIFFUSION

To isolate the benefits of the CFM objective, we compare FlowCast against a strong baseline using the same backbone architecture but trained with a diffusion objective. We trained a DDPM (Ho et al., 2020) for 1000 timesteps. For efficient inference, we employed a DDIM sampler (Song et al., 2021) with a varying number of steps. This provides a strong and practical baseline to evaluate FlowCast against a highly optimized diffusion process on the same powerful architecture.

The results in Table 6 clearly demonstrate the superiority of the CFM objective. With a single step, FlowCast (CFM) drastically outperforms the DDIM sampler, even a 100-step DDIM baseline, across key metrics like CRPS and CSI-M, whilst being almost 100 times faster.



470 Figure 4: Qualitative comparison of FlowCast with other baselines on a SEVIR sequence. Columns  
471 show lead times from 10 to 60 minutes. Rows show the ground-truth, followed by the models.

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476 Table 6: Ablation study: CFM vs. diffusion objective. Results highlight the superior performance  
477 and efficiency of the CFM framework. All metrics are computed over a 12-step forecast.  
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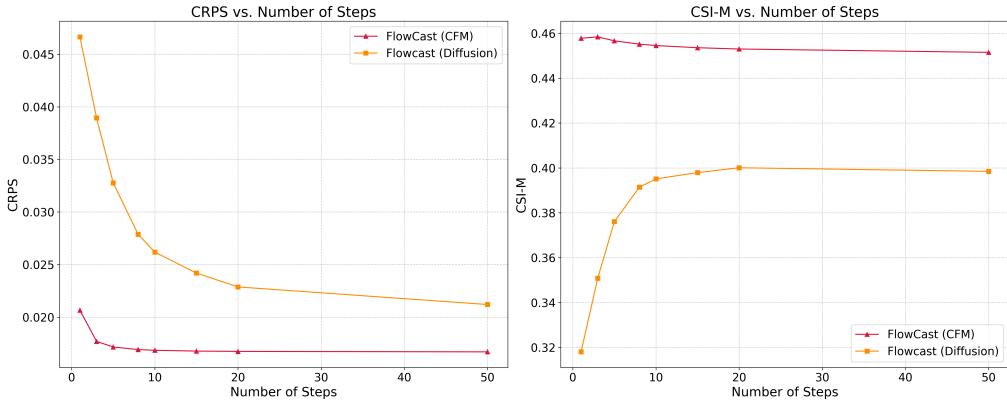
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Model	CRPS ↓	CSI-M ↑	CSI-P16-M ↑	FSS-M-P16 ↑	HSS-M ↑	FAR-M ↓	Time/Seq. (s)
CFM (1 steps)	0.0207	0.454	0.504	0.763	0.571	0.337	<b>2.6</b>
CFM (10 steps)	<b>0.0168</b>	<b>0.455</b>	<b>0.514</b>	<b>0.764</b>	<b>0.572</b>	0.338	24
DDIM (10 steps)	0.0262	0.395	0.450	0.622	0.503	0.335	24
DDIM (50 steps)	0.0212	0.398	0.451	0.635	0.504	0.321	120
DDIM (100 steps)	0.0208	0.398	0.450	0.664	0.502	<b>0.319</b>	239

485

486 4.3.2 INFERENCE EFFICIENCY: PERFORMANCE VS. NUMBER OF FUNCTION EVALUATIONS  
487

488 We assess inference efficiency by comparing FlowCast and the diffusion backbone across a range  
489 of function evaluations (NFE), where one NFE is an Euler (CFM) or DDIM step. Each NFE adds  
490 2.4s per 8-member ensemble forecast. Figure 5 shows FlowCast is highly efficient, nearing opti-  
491 mal CRPS and CSI-M scores in just 3-10 steps. In contrast, the diffusion model requires 20-50  
492 steps to peak and degrades sharply below 10 NFE. These results highlight the superior efficiency of  
493 the CFM framework, which learns a more direct mapping to the data manifold and enables high-  
494 fidelity forecasts with significantly fewer model evaluations. This efficiency is a crucial advantage  
495 for operational settings where forecasts must be both rapid and reliable.



509 Figure 5: Performance vs. efficiency trade-off. Forecast quality (CRPS ↓, CSI-M ↑) as a function  
510 of NFE. FlowCast (CFM) achieves near-optimal performance with only 3 to 10 steps, while the  
511 DDIM-based model requires 20 steps to 50 steps, and degrades sharply at low NFE.

513 5 CONCLUSION  
514

516 In this paper, we introduced FlowCast, the first fully probabilistic model applying Conditional Flow  
517 Matching (CFM) as a direct noise-to-data generative framework for precipitation nowcasting. Our  
518 experiments on the SEVIR and ARSO datasets show that FlowCast achieves state-of-the-art perfor-  
519 mance. Through direct ablation studies, we showed that the CFM objective is not only more accurate  
520 than a traditional diffusion objective on the same architecture but also vastly more efficient. Flow-  
521 Cast maintains high forecast quality with as few as a single sampling step, a regime where diffusion  
522 models fail. Our results firmly establish CFM as a powerful, efficient, and practical alternative for  
523 high-dimensional spatiotemporal forecasting.

524 **Limitations and Future Work:** While FlowCast shows significant promise, we identify two pri-  
525 mary areas for future development. First, its reliance solely on radar data could be a limitation.  
526 Future work should explore multi-modal data fusion (e.g., satellite, NWP) to enhance robustness  
527 and accuracy. Second, our evaluation was limited to two datasets due to computational cost; a  
528 broader study across more meteorological regimes is needed to confirm generalizability.

## 529 530 REPRODUCIBILITY STATEMENT

531 To ensure the reproducibility of our work, we have provided comprehensive supporting materials.  
532 **Code:** The full source code for our FlowCast model, including scripts for training and evaluation, is  
533 included in the supplementary material. The repository contains detailed instructions for setting up  
534 the required software environment and running the experiments. **Datasets:** Our work utilizes two  
535 datasets. The SEVIR dataset is a public benchmark, and details for access are provided by Veillette  
536 et al. (2020). The ARSO dataset was provided by the Slovenian Environment Agency (ARSO) for  
537 this research; we are actively collaborating with the agency to facilitate its public release in the near  
538 future. **Experimental Details:** Section 4.1 of the main paper provides a detailed description of  
539 our experimental setup. Further implementation details are available in Appendix A.1, including all  
model hyperparameters.

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648 **A APPENDIX**  
649650 **A.1 IMPLEMENTATION DETAILS**  
651652 This section details the implementation of FlowCast. The code to train and evaluate FlowCast is  
653 provided as supplementary material.654 **A.1.1 VAE**  
655656 The VAE was configured with the hyperparameters shown in Table 7. Different warmup periods  
657 were empirically selected based on the convergence speed of the VAE on the respective datasets;  
658 ARSO converged faster due to less diversity in the data, attributed to factors such as its fixed geo-  
659 graphical coverage and the significantly smaller stride used during sequence extraction.  
660661 **Table 7: VAE hyperparameter summary**  
662

664 <b>Category</b>	665 <b>Parameter</b>	666 <b>Value / Setting</b>
<b>Dataset</b>		
666	667 Source	668 SEVIR (vil) & ARSO (zm)
667	668 Input Dimensionality (per frame)	384 × 384 × 1 (SEVIR), 301 × 401 × 1 (ARSO)
668	669 Input Preprocessing	Frame values scaled to [0, 1]
<b>Training Objective</b>		
670	671 Loss Components	672 Reconstruction + KL Divergence + Adversarial
671	672 KL Divergence Weight ( $\lambda_{KL}$ )	673 $1 \times 10^{-4}$
672	673 Discriminator Weight ( $\lambda_{adv}$ )	674 0.5
673	674 Adversarial Loss Type	675 Hinge Loss
674	675 Discriminator Architecture	PatchGAN (Isola et al., 2017)
675	676 Discriminator Activation Warmup	35 epochs (SEVIR), 15 epochs (ARSO)
<b>Optimization</b>		
676	677 Optimizer (Generator & Disc.)	678 AdamW
677	678 Learning Rate (Initial)	679 $1 \times 10^{-4}$
678	680 Weight Decay	681 $1 \times 10^{-5}$
680	682 AdamW Betas	683 (0.9, 0.999)
682	684 LR Scheduler	Cosine Annealing with Linear Warmup
684	686 LR Warmup Fraction	688 20% of total training steps
686	688 LR Min Warmup Ratio	690 0.1
688	690 Min. LR Ratio	692 $10^{-3}$
<b>Training Configuration</b>		
685	686 Batch Size	687 12 (Global), 3 (Local)
686	688 Max. Number of Epochs	689 250
687	690 Gradient Clipping Norm	691 1.0
688	691 Early Stopping Patience	693 50 epochs
689	693 Early Stopping Metric	695 Generator validation loss
690	695 Training Nodes	697 4 × H100 GPUs
691	697 FP16 Training	700 Disabled
<b>Model Configuration</b>		
692	693 Latent Channels	694 4
693	695 GroupNorm Num	696 32
694	696 Layers per Block	698 2
695	698 Activation Function	700 SiLU
696	700 Encoder-Decoder Depth	702 4
697	702 Block Out Channels	704 [128, 256, 512, 512]

701 **Data Preprocessing and Padding.** To accommodate the VAE’s downsampling factor of  $f = 8$ ,  
inputs must be spatially divisible by the downsampling rate. For the ARSO dataset, the native

resolution of  $301 \times 401$  is not divisible by 8. We handle this by applying replication padding to the input frames to reach the nearest multiple of 16 prior to encoding. Specifically, the height is padded from 301 to 304, and the width from 401 to 416. This results in the latent dimensions of  $38 \times 52$  reported in Table 2 (304/8 and 416/8, respectively). During inference, the generated fields are cropped back to the original  $301 \times 401$  dimensions before evaluation metrics are computed. SEVIR dimensions ( $384 \times 384$ ) are naturally divisible by 8, requiring no padding.

### 709 A.1.2 FLOWCAST

710 **Architecture.** The FlowCast architecture, adapted from Earthformer-UNet (Gao et al., 2023) for  
 711 latent-space Conditional Flow Matching, has the following configuration:

713 • **Core U-Net Architecture:**

- 714 – **Hierarchical Stages:** A U-Net with 2 hierarchical stages (one level of downsampled/upsampling within the main U-Net body, in addition to initial/final processing).
- 715 – **Stacked Cuboid Self-Attention Modules:** Each stage in both the contracting (encoder) and expansive (decoder) paths contains a depth of 4 Stacked Cuboid Self-Attention modules.
- 716 – **Base Feature Dimensionality:** 196 units.

717 • **Spatial Processing:**

- 718 – **Downsampling:** Achieved using Patch Merge (reducing spatial dimensions by a factor of 2 and doubling channel depth).
- 719 – **Upsampling:** Uses nearest-neighbor interpolation followed by a convolution (halving channel depth).

720 • **Cuboid Self-Attention Details:**

- 721 – **Pattern:** Follows an axial pattern, processing temporal, height, and width dimensions sequentially.
- 722 – **Attention Heads:** 4 attention heads.
- 723 – **Positional Embeddings:** Relative positional embeddings are used.
- 724 – **Projection Layer:** A final projection layer is part of the attention block.
- 725 – **Dropout Rates:** Dropout rates for attention, projection, and Feed-Forward Network (FFN) layers are set to 0.1.

726 • **Global Vectors:** The specialized global vector mechanism from the original Earthformer  
 727 is disabled.

728 • **FFN and Normalization:**

- 729 – **FFN Activation:** Feed-forward networks within the attention blocks use GELU activation.
- 730 – **Normalization:** Layer normalization is applied throughout the relevant parts of the network.

731 • **Embeddings:**

- 732 – **Spatiotemporal Positional Embeddings:** Added to the input features after an initial projection.

- 733 – **CFM Time Embeddings ( $t$ ):**

- 734 \* **Generation:** Generated with a channel multiplier of 4 relative to the base feature dimensionality (resulting in  $196 \times 4 = 784$  embedding channels).
- 735 \* **Incorporation:** Injected into the network at each U-Net stage using residual blocks that fuse the time embedding with the feature maps (TimeEmbedResBlock modules).

736 • **Skip Connections:** Standard U-Net additive skip connections merge features from the contracting path to the expansive path.

737 • **Padding:** Zero-padding is used where necessary to maintain tensor dimensions during convolutions or cuboid operations.

756 **Training and Inference Hyperparameters.** The FlowCast training and inference hyperparameters are as follows:  
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 758

759  
 760 Table 8: FlowCast hyperparameter summary  
 761

762 <b>Category</b>	762 <b>Parameter</b>	762 <b>Value / Setting</b>
<b>Dataset</b>		
764 Source		Latent-space sequences from VAE
765 Input Dimensionality		13 × 48 × 48 × 4 (SEVIR), 13 × 38 × 52 × 4 (ARSO)
765 Input Preprocessing		Standardized with training set statistics (mean, std)
<b>Training Configuration</b>		
767 Loss Function		MSE: $\mathcal{L} = \ \hat{v} - (Z_{\text{future}} - Z_P)\ ^2$
768 Batch Size		12 (Global), 3 (Local)
769 Max. Number of Epochs		200
770 Gradient Clipping Norm		1.0
771 Early Stopping Patience		50 epochs
771 Early Stopping Metric		CSI-M evaluated on subset (40 batches) of validation set
772 Training Nodes		4 × H100 GPUs
773 FP16 Training		Enabled
773 Exponential Moving Average Weights		Enabled
774 Exponential Moving Average Weights Decay		0.999
<b>Optimization</b>		
776 Optimizer		AdamW
777 Learning Rate (Initial)		$5 \times 10^{-4}$
778 Weight Decay		$1 \times 10^{-4}$
778 AdamW Betas		(0.9, 0.999)
779 LR Scheduler		Cosine Annealing with Linear Warmup
780 LR Warmup Fraction		1% of total training steps
781 LR Min Warmup Ratio		0.1
782 Min. LR Ratio		$10^{-2}$
<b>CFM Parameters</b>		
783 $\sigma$		0.01
784 ODE Solver		Euler Method with 10 steps

786 **Choice of ODE Solver.** We conducted an ablation study to compare various ODE solvers, including adaptive methods (Adaptive Heun, Dormand-Prince 5) and fixed-step methods (Euler, Midpoint, Runge-Kutta 4) on the first 10% of the SEVIR test set using a single NVIDIA A100 GPU. For adaptive solvers, a relative and absolute tolerance of  $10^{-2}$  and  $10^{-3}$  were used, respectively. Since no significant performance differences were observed, as shown in Table 9, we selected the Euler method with 10 steps for its computational efficiency and simplicity.

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 794 Table 9: Ablation study: ODE solvers. Results highlight minor differences in performance between  
 795 the different solvers.

796 Solver	796 CRPS ↓	796 CSI-M ↑	796 CSI-P16-M ↑	796 FSS-M-P16 ↑	796 HSS-M ↑	796 FAR-M ↓	796 Time/Seq. (s)
Euler (1 steps)	0.0207	0.454	0.504	0.763	0.571	0.337	2.6
Euler (10 steps)	0.0168	0.455	0.514	0.764	0.572	0.338	24
Dormand-Prince 5	0.0168	0.450	0.516	0.762	0.567	0.341	46
Midpoint (10 steps)	0.0167	0.451	0.516	0.762	0.568	0.341	44
Runge-Kutta 4 (10 steps)	0.0167	0.451	0.516	0.762	0.567	0.341	83
Adaptive Heun	0.0167	0.451	0.516	0.762	0.568	0.341	50

803 A.1.3 EVALUATION METRICS  
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805 **Continuous Ranked Probability Score (CRPS).** The CRPS is evaluated directly at the original  
 806 data resolution, without applying any spatial pooling. For each ensemble of  $N$  forecast members,  
 807 CRPS is calculated at every pixel and then averaged across all spatial positions and forecast lead  
 808 times to obtain a single summary metric. If the predictive distribution  $F$  at a given pixel and time  
 809 step is approximated by a Gaussian with mean  $\mu$  and standard deviation  $\sigma$  (estimated from the  
 ensemble), and  $x$  is the observed value, the CRPS can be computed as:

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$$\text{CRPS}(F, x) = \sigma \left( \frac{x - \mu}{\sigma} \left( 2\Phi \left( \frac{x - \mu}{\sigma} \right) - 1 \right) + 2\phi \left( \frac{x - \mu}{\sigma} \right) - \frac{1}{\sqrt{\pi}} \right), \quad (1)$$

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where  $\Phi$  and  $\phi$  denote the cumulative distribution function (CDF) and probability density function (PDF) of the standard normal distribution, respectively.817  
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**Threshold-based categorical metrics.** For each chosen intensity threshold  $u$ , we binarize the continuous ground truth field  $x_{t,i,j}$  to obtain an observation mask  $\mathbb{1}[x_{t,i,j} > u]$ . The representative forecast  $\hat{x}_{t,i,j}$  (see Section 4.1.2) is likewise thresholded to produce a binary forecast mask  $\mathbb{1}[\hat{x}_{t,i,j} > u]$ .821  
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823  
Using these binary masks and the dataset-specific thresholds, we construct a  $2 \times 2$  contingency table for each evaluation:

		Observ. yes	Observ. no	$H$ : Hits (True Positives),
Forecast yes	$H$	$F$	$M$ : Misses (False Negatives),	
	$M$	$C$	$F$ : False Alarms (False Positives),	
Forecast no			$C$ : Correct Negatives.	

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The values  $H, M, F, C$  are summed over all spatial locations, batches, and forecast lead times. The following metrics are then computed:829  
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831**False Alarm Ratio (FAR):** The proportion of forecasted events that did not actually occur.832  
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$$\text{FAR} = \frac{F}{H + F}. \quad (2)$$

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**Critical Success Index (CSI):** The fraction of observed and/or forecasted events that were correctly predicted, ignoring correct negatives. This metric is sensitive to both missed events and false alarms.840  
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$$\text{CSI} = \frac{H}{H + M + F}. \quad (3)$$

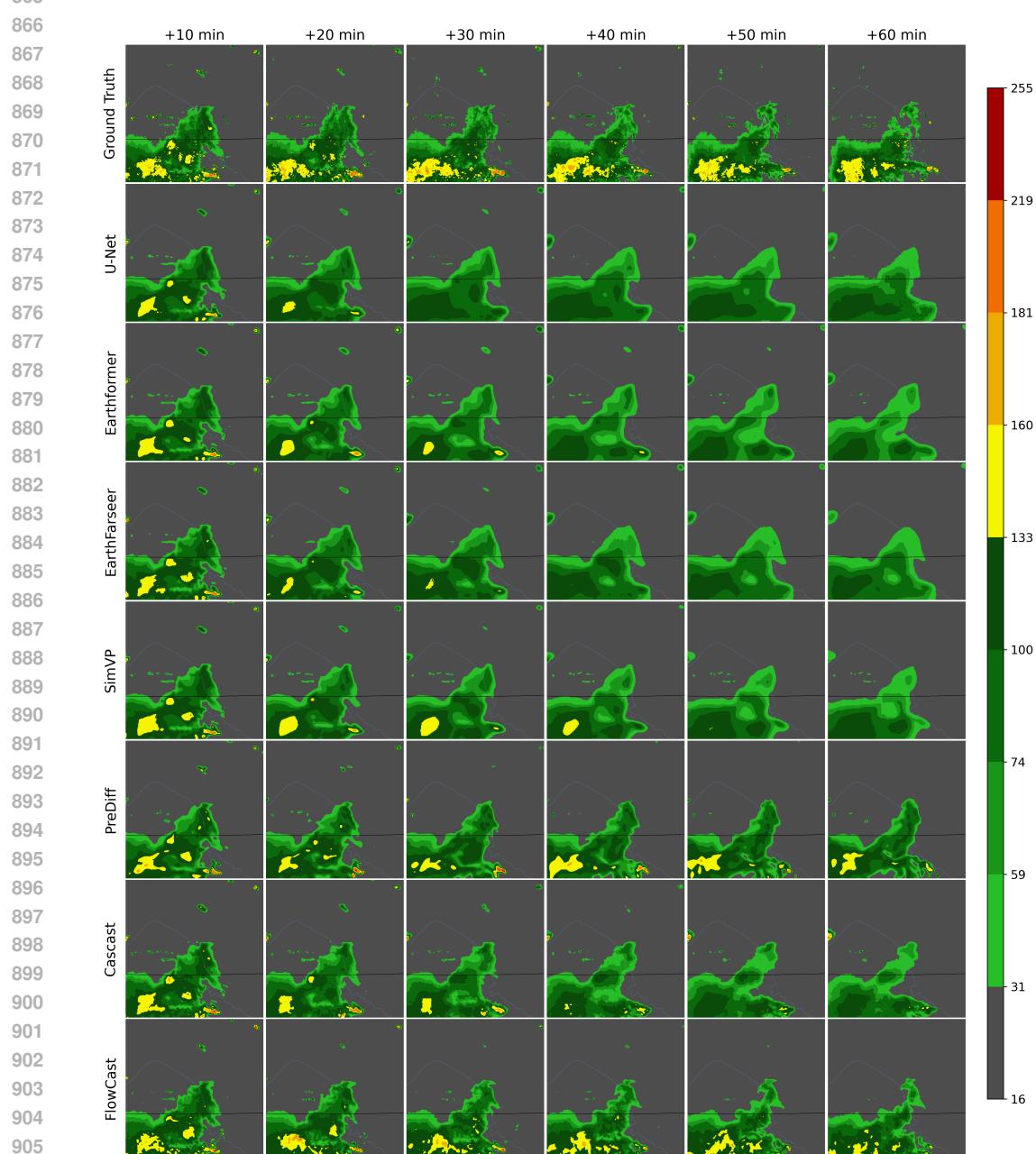
843  
844**Heidke Skill Score (HSS):** The accuracy of the forecast relative to random chance.845  
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$$\text{HSS} = \frac{2(HC - MF)}{(H + M)(M + C) + (H + F)(F + C)}. \quad (4)$$

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853**Pooled CSI (CSI-P16):** Forecasts and ground truth fields are first downsampled by applying a max-pooling operation over non-overlapping  $16 \times 16$  pixel blocks. CSI is then recomputed on these pooled fields. A hit anywhere within a  $16 \times 16$  block is registered as a success, thereby rewarding models that capture the local presence and intensity of precipitation, even if exact pixel-level alignment is imperfect.854  
855  
856**Fractions Skill Score (FSS):** We compute FSS to evaluate spatial alignment. Let  $S_f(i, j)$  and  $S_o(i, j)$  denote the fraction of pixels exceeding the threshold within a neighborhood of size  $n \times n$  centered at  $(i, j)$  for the forecast and observation, respectively. The FSS is calculated as:857  
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$$\text{FSS} = 1 - \frac{\sum_{i,j} [S_f(i, j) - S_o(i, j)]^2}{\sum_{i,j} S_f(i, j)^2 + \sum_{i,j} S_o(i, j)^2} \quad (5)$$

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A.2 MORE QUALITATIVE EXAMPLES  
This section presents additional qualitative examples comparing FlowCast against the baseline models

864 A.2.1 SEVIR  
865906  
907 Figure 6: Qualitative comparison of FlowCast with other baselines on a SEVIR sequence.  
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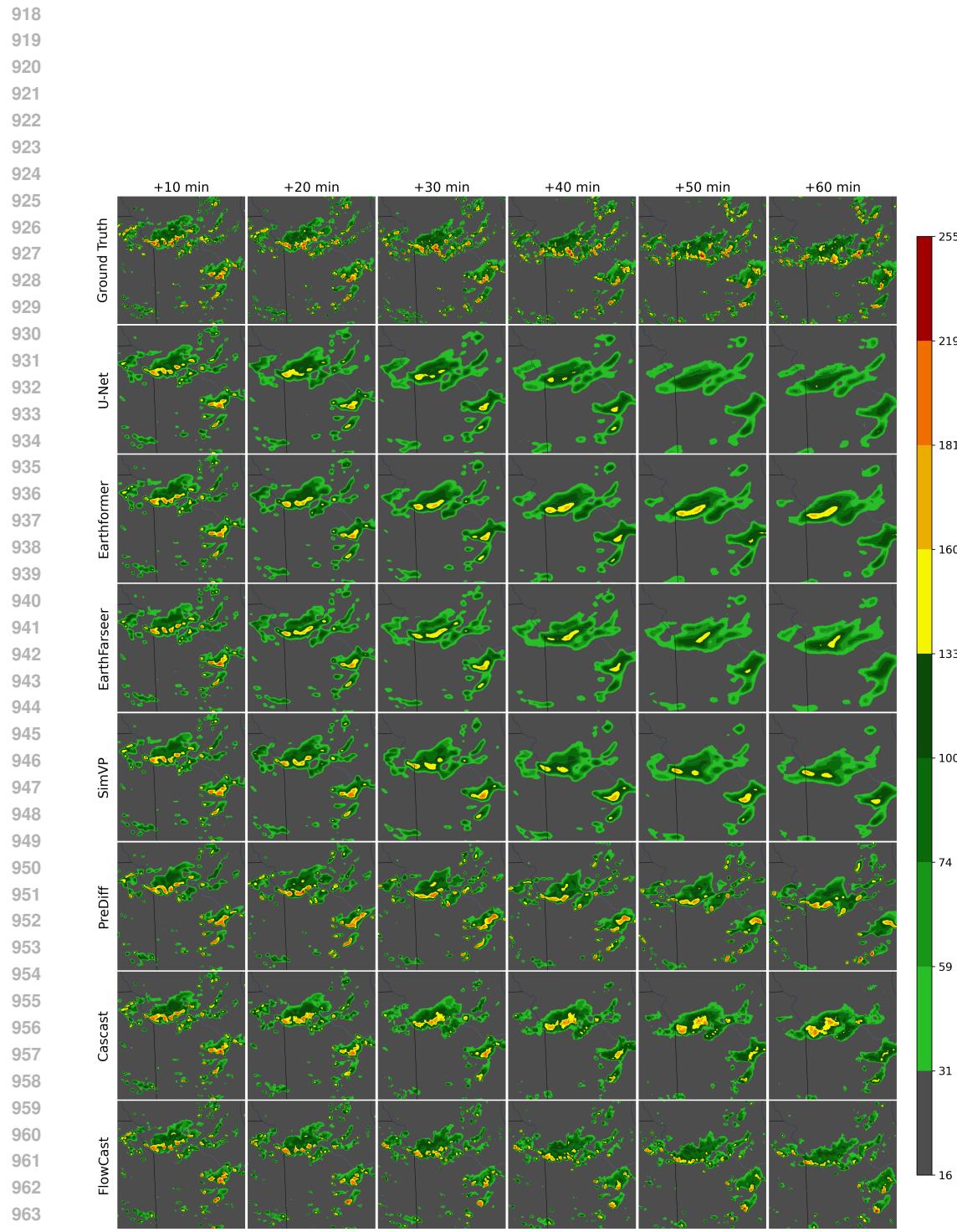


Figure 7: Qualitative comparison of FlowCast with other baselines on a SEVIR sequence.

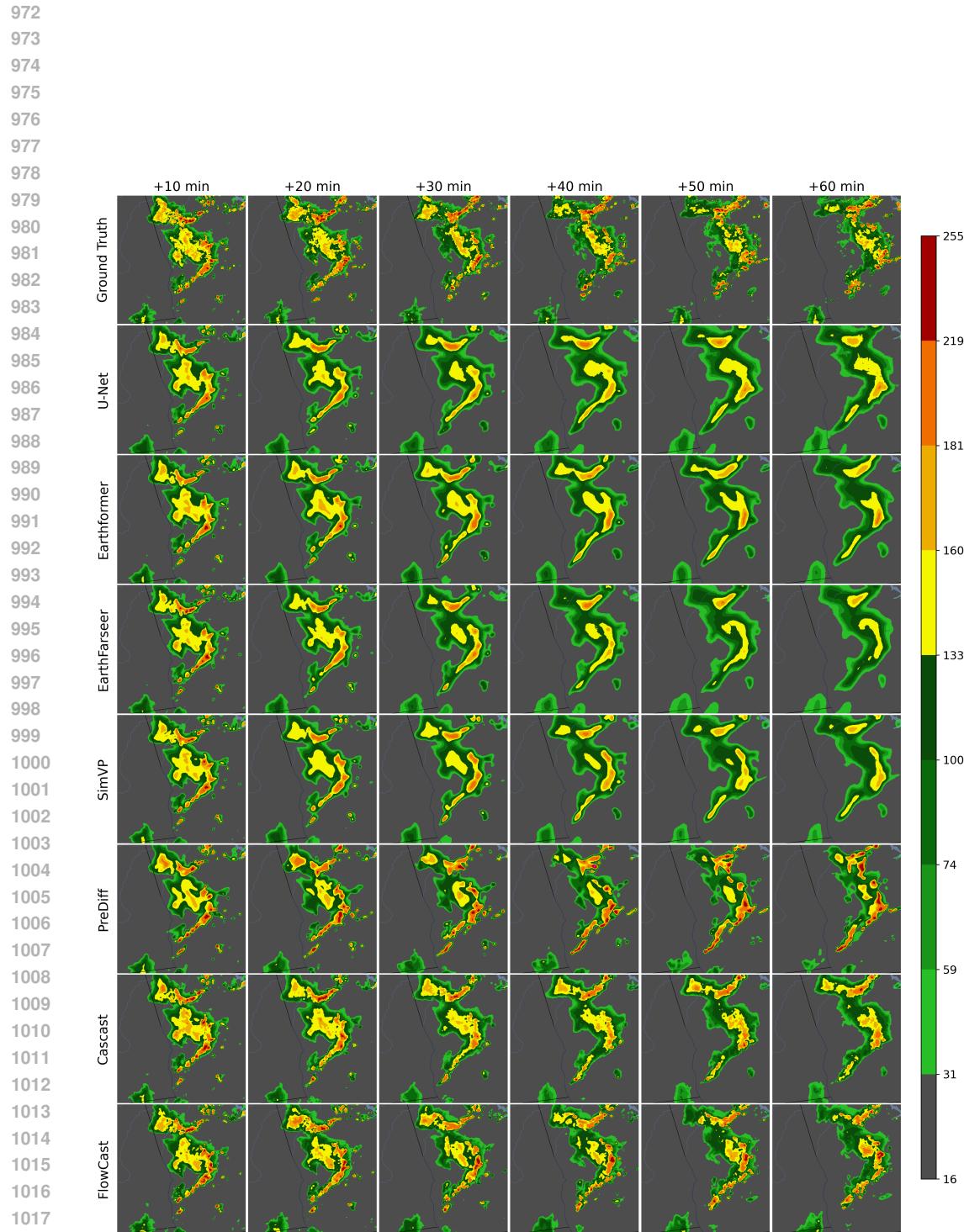


Figure 8: Qualitative comparison of FlowCast with other baselines on a SEVIR sequence.

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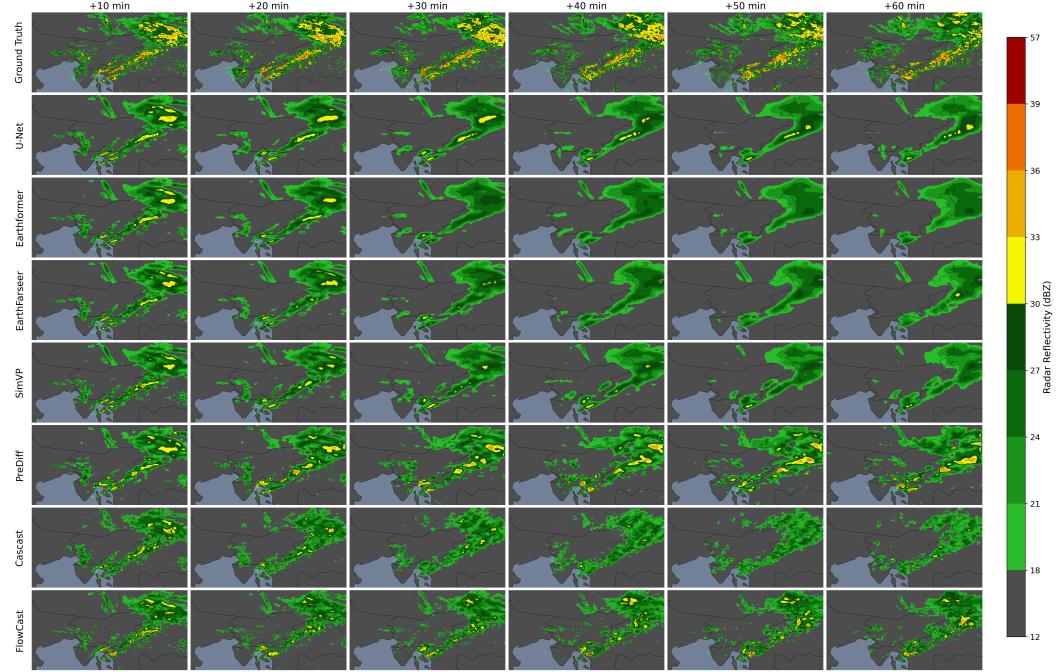
## A.2.2 ARSO

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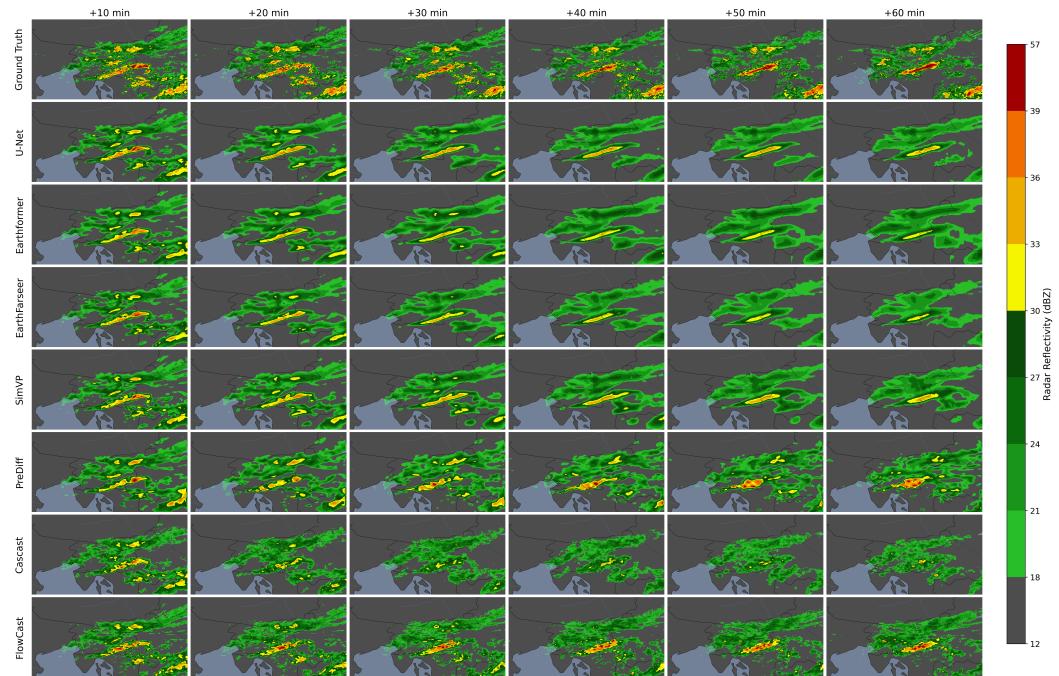
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Figure 9: Qualitative comparison of FlowCast with other baselines on an ARSO sequence.

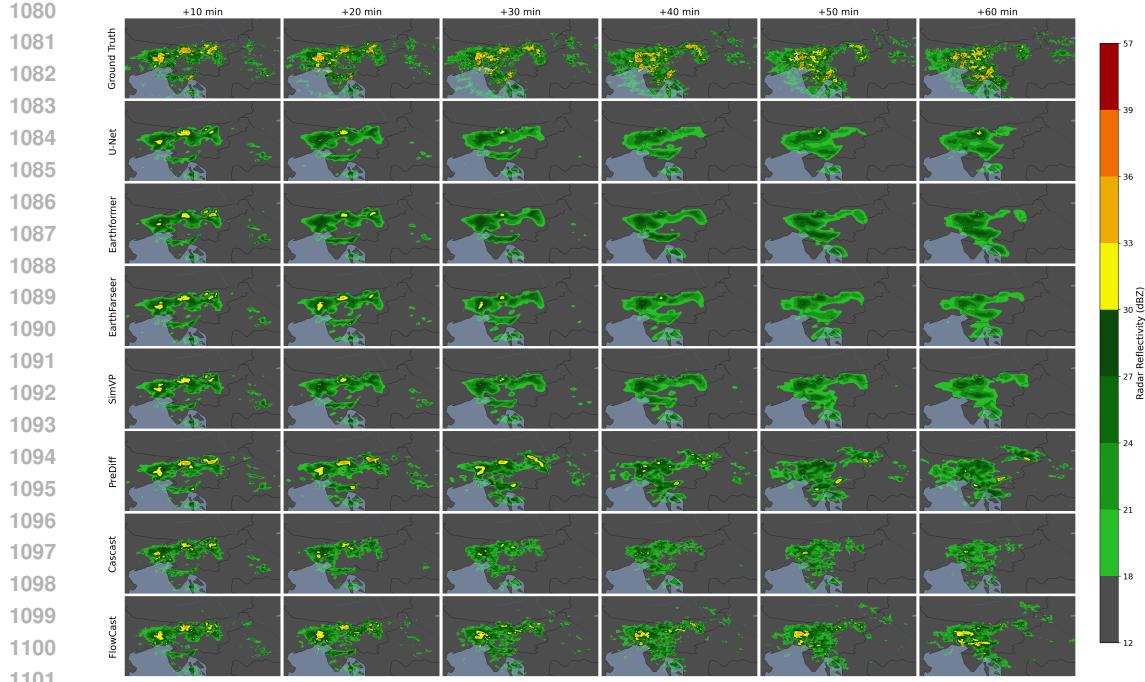


Figure 11: Qualitative comparison of FlowCast with other baselines on an ARSO sequence.

### A.3 LLM USAGE STATEMENT

During the preparation of this manuscript, we utilized a large language model (LLM) as a writing assistant. The LLM’s primary role was to help refine sentence structure, improve clarity, and ensure grammatical correctness and consistency in tone. All scientific contributions, including the research ideation, methodological design, experimental analysis, and interpretation of results, were conducted solely by the authors, who take full responsibility for the content of this work.