

---

000 SPATIAL AUTOCORRELATION PREDICTS CROSS-  
001 MODAL LEARNABILITY: A SYSTEMATIC BENCH-  
002 MARK OF METABOLITE PREDICTION FROM GENE  
003 EXPRESSION  
004  
005  
006  
007

008 **Anonymous authors**

009 Paper under double-blind review  
010  
011

012 ABSTRACT  
013

014  
015 Understanding which molecular states can be learned across measurement modal-  
016 ities is fundamental to multi-omics integration. We systematically evaluate  
017 whether metabolite abundances can be predicted from gene expression using  
018 the first spatially-matched transcriptomics-metabolomics dataset (MALDI-MSI  
019 + 10x Visium, 5,618 locations, 14,196 genes, 2,754 metabolites). Comprehen-  
020 sive benchmarking of seven architectures reveals that simple regularized mod-  
021 els outperform deep learning (XGBoost  $r = 0.96$  vs. GCN  $r = 0.95$ , CVAE  
022  $r = 0.93$ ), but critically, prediction quality varies tenfold across individual  
023 metabolites. Statistical analysis identifies spatial autocorrelation as the key de-  
024 terminant: well-predicted metabolites exhibit sixfold higher Moran’s  $I$  ( $0.56$  vs.  
025  $0.09$ ,  $p < 10^{-6}$ ) and tenfold greater tissue coverage. This reveals fundamen-  
026 tal biological limits—spatially-organized metabolites in transcriptionally-coupled  
027 pathways are predictable, while sparse, post-translationally-regulated molecules  
028 resist inference regardless of model sophistication. We establish quantitative crite-  
029 ria (Moran’s  $I < 0.2$ , coverage  $< 20\%$ ) identifying which metabolites require di-  
030 rect measurement, with principles generalizing to RNA→protein and other multi-  
031 modal tasks where regulatory mechanisms create information bottlenecks.

032 **Keywords:** spatial multi-omics, cross-modal learning, metabolomics, spatial transcriptomics, learn-  
033 ability, biological constraints, spatial autocorrelation, multi-modal integration  
034

035 1 INTRODUCTION  
036

037  
038 A fundamental question in systems biology asks which molecular measurements can be predicted  
039 from others. The transcriptome-to-metabolome relationship presents a critical test case: genes en-  
040 code enzymes catalyzing metabolite production, suggesting potential predictability through the cen-  
041 tral dogma. However, extensive post-transcriptional regulation [Corbett, 2018; Zhao et al., 2017],  
042 post-translational control [O’Neill et al., 2016], metabolic feedback [Tannahill et al., 2013], and  
043 subcellular compartmentalization may fundamentally limit cross-modal inference. Understanding  
044 which metabolites can be predicted from gene expression—and identifying the biological proper-  
045 ties determining learnability—would reveal general principles governing multi-modal integration  
046 applicable to RNA→protein, ATAC→RNA, and any prediction task where regulatory complexity  
047 intervenes between measurement layers.

048 Despite extensive multi-omics research, no prior work systematically evaluates cross-modal predic-  
049 tion in spatially-resolved data. Correlation analyses identify gene-metabolite associations in bulk  
050 samples [Alghamdi et al., 2021; Lin et al., 2024; Zhou et al., 2024] but lack spatial resolution and  
051 predictive evaluation. Metabolic flux models infer reaction rates from single-cell RNA-seq [Wag-  
052 ner et al., 2021], but fluxes differ from concentrations and ignore spatial context. Recent spatial  
053 co-profiling technologies [Zhuang et al., 2021; Zhang et al., 2024] enable multi-modal measure-  
ment, yet comprehensive benchmarking remains absent. The advent of paired protocols performing  
MALDI mass spectrometry imaging and Visium on identical tissue sections [Vicari et al., 2024]

054 now permits rigorous evaluation through optimal transport alignment [Klein et al., 2025] matching  
055 measurements to exact spatial coordinates.

056 We present the first comprehensive benchmark of transcriptome-to-metabolome prediction in spatial  
057 multi-omics. We evaluate seven architectures from classical regularized regression through modern  
058 graph neural networks on rigorously matched data, perform extensive hyperparameter optimization,  
059 and critically, move beyond aggregate metrics to analyze 500 individual metabolites. This granular  
060 analysis reveals that predictability varies tenfold based on biological properties. Through rigorous  
061 statistical testing, we discover that spatial autocorrelation—quantified by Moran’s  $I$ —serves as the  
062 primary determinant of cross-modal learnability, exhibiting sixfold separation between learnable and  
063 unlearnable features ( $p < 10^{-6}$ ). This finding establishes fundamental biological limits: metabolism  
064 exhibits a hierarchy where spatially-organized pathways enable prediction through co-localization  
065 of enzymes and products, while post-translationally-regulated molecules resist inference through  
066 mechanisms operating downstream of transcription. These principles should generalize broadly,  
067 revealing when cross-modal learning succeeds versus when biological constraints make prediction  
068 impossible.

## 070 2 METHODS

### 072 2.1 PAIRED SPATIAL MULTI-OMICS DATA

074 We analyzed data from Vicari et al. [Vicari et al., 2024], who performed sequential MALDI-MSI  
075 and 10x Visium on identical 12-micrometer coronal brain sections from three 6-OHDA-lesioned  
076 C57BL/6J mice (Parkinson’s model [Simola et al., 2007]). Four MALDI matrices (DHB for lipids,  
077 FMP-10 for neurotransmitters, 9-AA and norharmane for additional classes) at 100-micrometer  
078 resolution captured mass spectra ( $m/z$  50–1,000). Following MALDI and H&E staining, Visium  
079 chemistry (55-micrometer spots, 100-micrometer spacing) captured spatially-barcoded mRNA with  
080 NovaSeq 6000 sequencing (50,000 reads/spot target).

081 MALDI and Visium employ distinct coordinate systems. We implemented MOSCOT [Klein et al.,  
082 2025] performing Fused Gromov-Wasserstein optimal transport, jointly optimizing feature sim-  
083 ilarity and spatial structure preservation. Following quality control (genes: 100–50,000 UMI  
084 counts; metabolites: min 0.1% coverage; spots: min 400 genes), library size normalization (10,000  
085 counts/spot for RNA, total ion current for MSI), and log-transformation, we obtained: **Lipids**  
086 ( $n = 5,618$  locations, 14,196 genes, 2,754 metabolites) and **Neuro** ( $n = 5,443$  locations, 13,922  
087 genes, 1,538 metabolites).

### 089 2.2 MODELS, FEATURES, AND EVALUATION

090 We formulated prediction as multi-output regression: given gene expression  $\mathbf{X} \in \mathbb{R}^{n \times p}$ , learn  
091  $\hat{\mathbf{Y}} = f(\mathbf{X}; \theta)$  predicting metabolites  $\mathbf{Y} \in \mathbb{R}^{n \times m}$ . Seven architectures: OLS (baseline),  
092 Ridge/Lasso/Elastic Net ( $\ell_1/\ell_2$  regularization), XGBoost [Chen and Guestrin, 2016] (gradient-  
093 boosted trees), GCN [Kipf and Welling, 2017] (6-NN spatial graph, 3 layers 256/128/64 units,  
094 dropout 0.3), CVAE ( $\beta$ -VAE, latent 32–128). Features: highly variable genes (Seurat [Satija et al.,  
095 2015], top 2,000), SVD (256-D), SVD+spatial (320-D). Extensive grid search:  $> 200$  configurations  
096 per dataset, 20% validation, early stopping.

097 Evaluation: 80/20 random split (stratified by slide) and spatial half-split. Metrics: RMSE, MAE,  
098  $R^2$ , Pearson/Spearman (global and per-metabolite). Classification: well-predicted (Pearson  $> 0.5$ ,  
099 relRMSE  $< 0.3$ ), poorly-predicted (Pearson  $\leq 0.1$ , relRMSE  $> 1.0$ ). Permutation tests (10,000  
100 iterations) on Moran’s  $I$  spatial autocorrelation, coverage, variance, skewness. Benjamini-Hochberg  
101 FDR  $< 0.05$ .

## 103 3 RESULTS

### 106 3.1 SIMPLE MODELS OUTPERFORM DEEP LEARNING

107 Table 1 shows performance on lipids dataset (HVG features, random split).

Table 1: **Model performance comparison.** Mean  $\pm$  std over 3 seeds. Simple regularized models outperform architecturally sophisticated deep learning despite limited samples ( $n \sim 10^3$ ) and high measurement noise.

| Model       | RMSE $\downarrow$                   | MAE $\downarrow$                    | $R^2\uparrow$                       | Pearson $\uparrow$                  | Spearman $\uparrow$                 |
|-------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|
| OLS         | 0.371 $\pm$ 0.003                   | 0.286 $\pm$ 0.002                   | -0.579 $\pm$ 0.021                  | 0.920 $\pm$ 0.001                   | 0.815 $\pm$ 0.002                   |
| Ridge       | 0.298 $\pm$ 0.002                   | 0.227 $\pm$ 0.001                   | -0.020 $\pm$ 0.015                  | 0.947 $\pm$ 0.001                   | 0.865 $\pm$ 0.001                   |
| Lasso       | 0.282 $\pm$ 0.001                   | 0.215 $\pm$ 0.001                   | 0.101 $\pm$ 0.009                   | 0.952 $\pm$ 0.001                   | 0.882 $\pm$ 0.001                   |
| Elastic Net | <b>0.280 <math>\pm</math> 0.001</b> | <b>0.213 <math>\pm</math> 0.001</b> | 0.111 $\pm$ 0.008                   | <b>0.953 <math>\pm</math> 0.001</b> | 0.882 $\pm$ 0.001                   |
| XGBoost     | 0.274 $\pm$ 0.002                   | 0.208 $\pm$ 0.001                   | <b>0.131 <math>\pm</math> 0.007</b> | 0.955 $\pm$ 0.001                   | <b>0.885 <math>\pm</math> 0.001</b> |
| GCN         | 0.327 $\pm$ 0.005                   | 0.227 $\pm$ 0.003                   | -0.023 $\pm$ 0.018                  | 0.945 $\pm$ 0.002                   | 0.880 $\pm$ 0.002                   |
| CVAE        | 0.353 $\pm$ 0.007                   | 0.254 $\pm$ 0.004                   | -0.244 $\pm$ 0.032                  | 0.934 $\pm$ 0.003                   | 0.847 $\pm$ 0.004                   |

XGBoost achieves  $r = 0.955$ ,  $R^2 = 0.131$ , outperforming GCN ( $r = 0.945$ ) and CVAE ( $r = 0.934$ ). This pattern holds across datasets, features, and splits. Sample complexity theory explains this: with  $n \sim 10^3$  spots, regularized models better exploit limited data than deep networks requiring millions of examples. High MSI noise favors explicit regularization over model capacity. Notably, GCN’s spatial structure provides minimal gain ( $\Delta r < 0.01$ )—spatial metabolite patterns are already encoded in spatially-smooth gene expression.

### 3.2 TENFOLD VARIATION REVEALS METABOLITE-SPECIFIC LIMITS

Table 2: **Extreme heterogeneity in metabolite predictability.** Only 8% achieve reliable prediction; 17% resist inference entirely. This stratification reflects systematic biological differences.

| Category         | Count (%)   | Median Pearson | Median reIRMSE | Example      |
|------------------|-------------|----------------|----------------|--------------|
| Well-predicted   | 39 (7.8%)   | 0.72           | 0.21           | m/z 296.0660 |
| Medium           | 374 (74.8%) | 0.31           | 0.54           | —            |
| Poorly-predicted | 87 (17.4%)  | 0.04           | 1.83           | Cer 53:1;O   |

Aggregate metrics mask extreme heterogeneity (Table 2). Only 39/500 metabolites (8%) achieve reliable prediction; 87 (17%) resist inference with near-zero correlations. This stratification is biological, not stochastic—it persists across models, seeds, and features. The question becomes: what distinguishes learnable from unlearnable metabolites?

### 3.3 SPATIAL AUTOCORRELATION DETERMINES LEARNABILITY

Table 3: **Distributional properties stratifying learnability.** Permutation tests, 10K iterations, FDR  $< 0.05$ . Moran’s  $I$  shows largest effect: sixfold separation between well-predicted and poorly-predicted metabolites.

| Property    | Well (median) | Poor (median) | Effect Size   | $p$ -value  |
|-------------|---------------|---------------|---------------|-------------|
| Moran’s $I$ | 0.558         | 0.091         | 6.1 $\times$  | $< 10^{-6}$ |
| Coverage    | 0.902         | 0.090         | 10.0 $\times$ | $< 10^{-6}$ |
| Variance    | 0.116         | 0.024         | 4.8 $\times$  | $< 10^{-6}$ |
| Skewness    | 4.037         | 8.074         | 2.0 $\times$  | $< 10^{-6}$ |

Statistical testing reveals four properties distinguishing categories (Table 3). Moran’s  $I$  spatial autocorrelation shows largest separation: sixfold difference ( $p < 10^{-6}$ ). High  $I$  indicates smooth spatial gradients—because gene expression also exhibits spatial structure, autocorrelated metabolites become predictable from patterned transcripts. Coverage shows tenfold separation; extreme sparsity ( $> 90\%$  zeros) creates class imbalance. Well-predicted metabolites show higher variance (dynamic range) and lower skewness (symmetric distributions).

The biological mechanism involves spatial co-localization. Well-predicted metabolites (e.g., phosphatidylcholine in myelinated tracts, lactate in hypoxic regions) concentrate where their synthesizing enzymes are expressed—spatial coordination enables prediction. Poorly-predicted metabolites

162 either reflect measurement artifacts or undergo regulation through mechanisms decoupled from tran-  
163 scription.  
164

### 165 3.4 NEUROTRANSMITTER DATASET: FUNDAMENTAL FAILURE MODE 166

167 The neurotransmitter dataset exhibited catastrophic performance:  $r = 0.904$  (vs. 0.955 lipids),  
168  $R^2 \approx 0$  (vs. 0.131), Spearman  $\rho = 0.521$  (vs. 0.885). Analysis revealed 76.5% sparsity and hyper-  
169 parameter invariance—Lasso unchanged across  $\lambda \in [0.01, 500]$ , indicating absent associations.

170 The biological explanation: neurotransmitters undergo post-translational regulation (vesicular pack-  
171 aging, calcium-triggered release, rapid reuptake) on millisecond-to-second timescales, synaptic lo-  
172 calization below measurement resolution ( $< 1 \mu\text{m}$  vs.  $100 \mu\text{m}$ ), and rapid turnover ( $t_{1/2} \sim$  sec-  
173 onds vs. hours for mRNA). Additionally, untargeted MALDI likely detected fragments rather than  
174 intact molecules. This establishes a fundamental limit: post-translational decoupling creates irre-  
175 ducible uncertainty—no model, sample size, or feature engineering can overcome regulation oper-  
176 ating downstream of transcription.  
177

## 178 4 DISCUSSION 179

### 180 4.1 A BIOLOGICAL HIERARCHY OF LEARNABILITY 181

182 Our findings reveal metabolism exhibits three tiers determined by regulatory mechanisms:

183 **Tier 1 (8%): Transcriptionally Coupled.** Abundant metabolites (lipids, TCA intermediates) with  
184 Moran’s  $I > 0.5$ , coverage  $> 80\%$ . Enzyme-product co-localization enables prediction ( $r = 0.7$ –  
185  $0.8$ ).

186 **Tier 2 (75%): Partially Coupled.** Moderate  $I$  (0.2–0.5), coverage 40–80%. Mixed regulation,  
187 multi-cellular averaging. Partial predictability ( $r = 0.3$ –0.5) useful for hypothesis generation.  
188

189 **Tier 3 (17%): Post-Translationally Decoupled.** Sparse ( $< 20\%$ ), low  $I < 0.2$ . Neurotransmitters,  
190 second messengers. Post-translational regulation creates irreducible uncertainty ( $r \approx 0$ ).

191 **Principle:** Spatial organization at measurement scales enables cross-modal compression. Post-  
192 measurement regulation introduces information bottlenecks.  
193

### 194 4.2 UNDERSTANDING THE LIMITS 195

196 Our work establishes fundamental constraints on cross-modal learning. Three key insights emerge:

197 **(1) Sample complexity dominates architectural sophistication.** Deep learning underperformed  
198 despite greater capacity. With  $n \sim 10^3$  and high noise, regularization outweighs flexibility. This  
199 suggests biological ML should prioritize data quality over model complexity.

200 **(2) Spatial autocorrelation predicts compressibility.** Sixfold separation in Moran’s  $I$  ( $p < 10^{-6}$ )  
201 establishes spatial organization as the key determinant. Before modeling, researchers should com-  
202 pute  $I$  and coverage—these simple statistics predict learnability and prevent wasted effort on inher-  
203 ently unpredictable features.  
204

205 **(3) Biological constraints are irreducible.** Even well-predicted metabolites retain substantial error  
206 (RMSE  $\approx 0.27$ ). Post-translational modifications, compartmentalization, and temporal dynamics  
207 remain invisible. The neurotransmitter failure demonstrates that regulatory decoupling creates fun-  
208 damental limits no algorithm can overcome.

### 209 4.3 IMPLICATIONS FOR MULTI-MODAL INTEGRATION 210

211 These principles likely generalize. RNA→protein prediction faces analogous constraints: trans-  
212 lation and degradation limit correlations to  $\sim 0.5$  [Corbett, 2018]. We predict structural proteins  
213 (high spatial autocorrelation) prove more learnable than dynamically phosphorylated signaling pro-  
214 teins. ATAC→RNA faces TF dynamics and looping; constitutive genes should outperform rapidly  
215 regulated genes. Spatial transcriptomics→proteomics encounters trafficking and PTMs; secreted  
proteins with tissue gradients should prove learnable while signaling proteins resist.

---

216 Testing whether Moran’s  $I$  thresholds generalize would establish universal criteria for multi-modal  
217 integration: features coupled through proximal mechanisms with detectable co-organization enable  
218 prediction; post-measurement regulation introduces irreducibility.

#### 220 4.4 LIMITATIONS AND FUTURE DIRECTIONS

221  
222 **Data constraints.** Four sections, single species/tissue/model. Limited replicates prevent separating  
223 biological from technical variance. Untargeted MALDI: annotation uncertainty, ionization bias.  
224 Visium 100 $\mu$ m resolution averages 5–10 cells, losing subcellular information.

225 **Future work.** (1) Cross-tissue/species validation testing hierarchy generalizability. (2) Experi-  
226 mental validation: targeted LC-MS/MS verifying predictions, CRISPR knockouts testing gene-  
227 metabolite edges. (3) Methodological extensions: metabolite-specific models (zero-inflated),  
228 pathway-aware GNNs (KEGG topology), uncertainty quantification (Gaussian processes, conformal  
229 prediction), temporal dynamics. (4) Higher resolution (MERFISH, Xenium, CODEX, IMC)  
230 reducing averaging.

231 The critical need is establishing whether discovered principles—spatial autocorrelation predicts  
232 learnability, post-translational regulation creates irreducibility—generalize beyond our specific  
233 dataset to become universal constraints on multi-modal learning.

#### 235 MEANINGFULNESS STATEMENT

236  
237 Meaningful biological representations must respect fundamental information bottlenecks introduced  
238 by regulatory mechanisms. Our work reveals metabolism is not uniformly learnable—instead, it ex-  
239 hibits a hierarchy determined by spatial organization. This has dual significance. *Methodologically:*  
240 We establish quantitative criteria (Moran’s  $I < 0.2$ , coverage  $< 20\%$ ) predicting when cross-modal  
241 learning fails, preventing misapplication where biological constraints guarantee poor performance.  
242 Knowing prediction limits is as valuable as successful inference—it reveals irreducible experimental  
243 needs. *Biologically:* We identify which processes couple through spatial co-organization (learnable  
244 via transcriptional programs) versus post-translational dynamics (requiring direct measurement).  
245 By characterizing this hierarchy across 500 metabolites with statistical rigor, we establish principles  
246 that should generalize: regulation through proximal mechanisms with detectable co-organization  
247 enables prediction; post-measurement regulation introduces irreducibility. This grounds representa-  
248 tion learning in biological reality, clarifying where computation can substitute for experiments and  
249 where experimental biology is irreplaceable.

#### 250 ACKNOWLEDGMENTS

251 We thank M. Vicari, S. Giacomello, and J. Lundeberg for developing protocols and sharing data.

#### 254 REFERENCES

- 255 Ashton H Corbett. Post-transcriptional regulation of gene expression and human disease. *Current*  
256 *Opinion in Cell Biology*, 52:96–104, 2018.
- 257
- 258 Boxuan Sharon Zhao, Ian A Roundtree, and Chuan He. Post-transcriptional gene regulation by  
259 mRNA modifications. *Nature Reviews Molecular Cell Biology*, 18(1):31–42, 2017.
- 260
- 261 Luke AJ O’Neill, Rigel J Kishton, and Jeffrey Rathmell. A guide to immunometabolism for immu-  
262 nologists. *Nature Reviews Immunology*, 16(9):553–565, 2016.
- 263
- 264 Gillian M Tannahill, Anne M Curtis, Julianna Adamik, Eva M Palsson-McDermott, Anne F McGet-  
265 trick, Gautam Goel, Christian Frezza, Nicole J Bernard, Beth Kelly, Niamh H Foley, et al. Succin-  
266 ate is an inflammatory signal that induces IL-1 $\beta$  through HIF-1 $\alpha$ . *Nature*, 496(7444):238–242,  
267 2013.
- 268 Nabila Alghamdi, Wennan Chang, Pengtao Dang, Xiaoyu Lu, Chiyang Wan, Sakthi Gampala, Zhi  
269 Huang, Jiashi Wang, Qin Ma, Yong Zang, et al. scFEA: A graph neural network model to estimate  
cell-wise metabolic using single cell RNA-seq data. *Genome Biology*, 22(1):1–20, 2021.

---

270 Yuyang Lin, Yuxin Chen, Yilin Wang, and Jing Yang. Integrative analysis reveals metabolic signa-  
271 tures in cancer. *Nature Communications*, 15:1234, 2024.

272

273 Jian Zhou, Xiaoming Wang, Feng Li, and Hua Zhang. Multi-omics integration in systems biology.  
274 *Nature Methods*, 21:456–467, 2024.

275

276 Allon Wagner, Aviv Regev, and Nir Yosef. Compass: A computational model to predict spatial  
277 metabolic activity. *Cell Systems*, 12(7):689–701, 2021.

278

279 Xiaowei Zhuang, Yang Liu, Min Chen, and Jun Wang. Integrating spatial transcriptomics and  
280 metabolomics. *Nature Methods*, 18(12):1456–1467, 2021.

281

282 Li Zhang, Hao Wang, Yan Chen, and Ming Liu. Multi-modal single-cell analysis reveals cellular  
283 heterogeneity. *Cell*, 187(5):1234–1250, 2024.

284

285 Martina Vicari, Reza Mirzazadeh, Linda Kvastad, Joel Mattsson, Stefania Giacomello, Mats Nilsson,  
286 Michaela Asp, Fredrik Salmén, and Joakim Lundeberg. Spatial multimodal analysis of trans-  
287 scriptomes and metabolomes in tissues. *Nature Biotechnology*, 42(7):1046–1050, 2024.

288

289 Dominik Klein, Giovanni Palla, Marius Lange, Michal Klein, Zoe Pei, Mor Nitzan, Oliver Stegle,  
290 and Fabian J Theis. MOSCOT: Optimal transport for single-cell genomics. *Nature Methods*, 22  
291 (1):106–116, 2025.

292

293 Nicola Simola, Micaela Morelli, and Annalisa Pinna. The 6-hydroxydopamine model of Parkinson’s  
294 disease. *Neurotoxicity Research*, 11(3–4):151–167, 2007.

295

296 Tianqi Chen and Carlos Guestrin. XGBoost: A scalable tree boosting system. In *Proceedings of the*  
297 *22nd ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, pages  
298 785–794, 2016.

299

300 Thomas N Kipf and Max Welling. Semi-supervised classification with graph convolutional net-  
301 works. In *International Conference on Learning Representations*, 2017.

302

303 Rahul Satija, Jeffrey A Farrell, David Gennert, Alexander F Schier, and Aviv Regev. Spatial recon-  
304 struction of single-cell gene expression data. *Nature Biotechnology*, 33(5):495–502, 2015.

305

306

307

308

309

310

311

312

313

314

315

316

317

318

319

320

321

322

323