DP-GTR: Differentially Private Prompt Protection via Group Text Rewriting

Anonymous ACL submission

Abstract

Prompt privacy is crucial, especially when using online large language models (LLMs), due to the sensitive information often contained within prompts. While LLMs can enhance prompt privacy through text rewriting, existing methods primarily focus on document-level rewriting, neglecting the rich, multi-granular representations of text. This limitation restricts LLM utilization to specific tasks, overlooking their generalization and in-context learning capabilities, thus hindering practical application. To address this gap, we introduce DP-GTR, a novel three-stage framework that leverages local differential privacy (DP) and the composition theorem via *group text rewriting*. DP-GTR is the first framework to integrate both document-level and word-level information while exploiting in-context learning to simultaneously improve privacy and utility, effectively bridging local and global DP mechanisms at the individual data point level. Experiments on CommonSense QA and DocVQA demonstrate that DP-GTR outperforms existing approaches, achieving a superior privacy-utility trade-off. Furthermore, our framework is compatible with existing rewriting techniques, serving as a plug-in to enhance privacy protection. Our code is publicly available at anonymous.4open.science for reproducibility.

1 Introduction

The rise of LLMs in natural language processing has spurred research into differential privacy (DP) techniques to mitigate the risk of sensitive information leakage (Abadi et al., 2016; Wu et al., 2023; Tang et al., 2023). While DP, the gold standard for computational privacy, has seen broad adoption in machine learning, existing text-based DP methods face significant challenges. These methods generally fall into four categories: training-based optimizations (e.g., DP-SGD (Abadi et al., 2016)), embedding perturbations (Feyisetan et al., 2020), document-level paraphrasing (Mattern et al., 2022), and in-context learning (ICL) enhancements (Wu et al., 2023). However, training-based approaches are computationally expensive, embedding perturbations can compromise semantic coherence, and ICL often neglects client-side prompt privacy.

Document paraphrasing offers a promising balance between privacy and utility. State-of-the-art methods achieve differentially private next-token generation using the exponential mechanism (EM) (McSherry and Talwar, 2007; Carvalho et al., 2023), replacing the standard softmax. Initial work employed decoder-only models like fine-tuned GPT-2 (Mattern et al., 2022), progressing to encoder-decoder (Igamberdiev and Habernal, 2023) and encoder-only architectures (e.g., BART, RoBERTa) (Meisenbacher et al., 2024b). DP-Prompt (Utpala et al., 2023) leverages prompt learning for zero-shot paraphrasing, and recent advancements combine DP post-processing with adversarial fine-tuning (Meisenbacher and Matthes, 2024). A critical limitation, however, persists: the lack of fine-grained control over the privacy-utility trade-off.

Current EM-based DP methods provide only coarse-grained control via the privacy budget, hindering practical deployment. Most approaches (except DP-Prompt) also necessitate resource-intensive fine-tuning. While document-level paraphrasing preserves more contextual information than embedding perturbations, it often overlooks word-level privacy vulnerabilities. These limitations highlight the need for a training-free, fine-grained privacy solution that fully leverages textual information, a capability well-suited to the ICL paradigm of LLMs.

Prior work on DP in ICL has predominantly focused on server-side, global DP implementations, often using a "sample-and-aggregate" approach (Nissim et al., 2007a) to privately partition and aggregate context databases (Wu et al., 2023; Tang et al., 2023). Client-side prompt privatization, in

contrast, requires the stronger guarantees of local DP (LDP), protecting individual data points rather than entire datasets. This distinction creates a significant gap between global and local DP in ICL, motivating the need for approaches that bridge it.

Addressing these gaps, we propose DP-GTR, a three-stage, differentially private prompt protection framework built upon a novel *Group Text Rewriting (GTR)* mechanism (see Figure 1). DP-GTR is designed to provide fine-grained control over the privacy-utility trade-off while remaining compatible with existing paraphrasing techniques. In Stage-1, GTR generates multiple client-side paraphrases of an input prompt, forming a "rewriting group" that preserves rich contextual information and enables bag-of-words-like count analysis. Notably, GTR connects local and global DP principles on the client-side. Stage-2 uses these counts for fine-grained privacy-utility control, identifying potentially sensitive private consensus keywords – words appearing frequently across paraphrases despite DP-driven variations. We mitigate this risk by releasing a fixed number of these keywords or using a differentially private aggregator, and select the lowest-perplexity paraphrase to maximize output quality. Stage-3 suppresses the identified keywords, limiting privacy leakage, and uses the selected paraphrase as an ICL example to improve utility. In addition, we evaluate DP-GTR in a realistic question-answering (QA) scenario, simulating real-world LLM usage.

Our key contributions are:

- We propose *Group Text Rewriting (GTR)*, a novel mechanism bridging local and global DP at the client-side prompt, enabling the integration of various DP techniques.
- We present DP-GTR, a three-stage prompt protection framework leveraging ICL for fine-grained privacy-utility control, compatible with existing paraphrasing methods.
- To our knowledge, we are the first to unify document-level and word-level privacy considerations within a single framework.
- We evaluate state-of-the-art DP paraphrasing methods in a realistic QA setting, demonstrating DP-GTR's superior privacy-utility trade-off compared to existing approaches.

2 Related Work

Global vs. Local DP: Differential privacy text sanitization methods are classified into Global Differential Privacy (Global-DP) and Differential Privacy (Local-DP) based on where the privacy mechanism is applied. In Global-DP, data is aggregated centrally before applying the privacy mechanism, while methods like DP-SGD use differentially private optimization techniques for training text models. (Abadi et al., 2016; Ponomareva et al., 2022; Feyisetan et al., 2020). DP-ICL operates within a "sample-and-aggregate" framework by perturbing the embedding and vocabulary selected for release (Wu et al., 2023). In contrast, Local-DP incorporates the differential privacy mechanism before data reaches the centralized processor, typically affording stronger privacy protection (Duchi et al., 2013; Feyisetan et al., 2020).

Local-DP: Private document release methods are categorized into three tiers based on where noise is added: word-level, sentence-level, and document-level. At the word level, noise is added to word embeddings, and the perturbed vectors are then mapped to the nearest vocabulary word (Feyisetan et al., 2020; Xu et al., 2020; Yue et al., 2021). Carvalho et al. (2023) employ the exponential mechanism for token selection, while Chen et al. (2023a) propose customized token mappings for individual words. Moreover, Meisenbacher et al.'s (2024a) study generates multiple candidate perturbations using various word embedding models, and Mattern et al. (2022) highlight that word-level approaches inherently lack contextual information. Similarly, sentence-level methods inject noise into sentence embeddings (Reimers, 2019; Meehan et al., 2022).

Document-level: At the document level, paraphrasing technologies are grouped into three categories based on model architecture. Mattern et al. (2022) uses a decoder-only fine-tuned GPT-2 model. Later work adopts encoder-decoder models, such as a BART-based approach (Lewis, 2019) with sensitivity clipping via thresholding and pruning (Igamberdiev and Habernal, 2023). Encoder-only methods, like DP-MLM (Meisenbacher et al., 2024b), use a RoBERTa-based masked language model for fine-tuning. These methods require fine-tuning. In contrast, DP-Prompt Utpala et al.'s (2023) introduces a zero-shot prompt learning paradigm using black-box LLMs, and Meisenbacher and Matthes (2024) employ post-processing and adversarial fine-tuning to enhance rewriting.

DP in ICL: The primary concern with applying DP in ICL is that LLMs are not inherently secure, potentially exposing sensitive context. Wu et al. (2023)'s DP-ICL perturbs embeddings and extracts

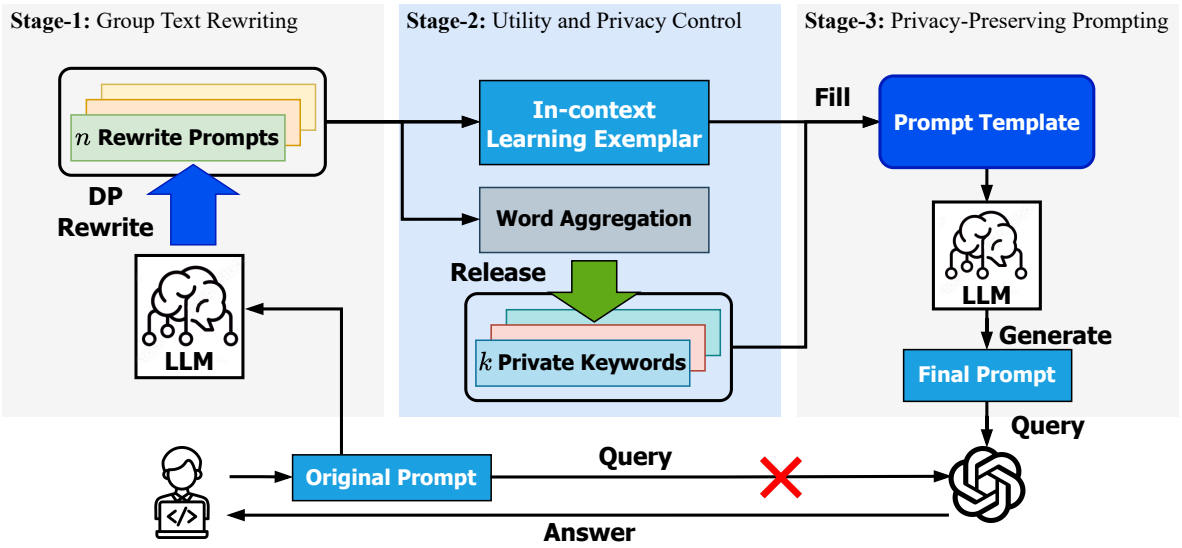


Figure 1: DP-GTR: A three-stage pipeline for Differentially Private prompt protection via Group Text Rewriting (GTR). Stage-1 generates n paraphrases of the original prompt using a DP paraphrasing mechanism. Stage-2 identifies the lowest-perplexity prompt as the ICL exemplar and aggregates word counts to release k private keywords. Stage-3 integrates these private keywords and the ICL exemplar into a prompt template for submission to the LLM, producing the final, differentially private prompt.

keywords from subsampled datasets, while Tang et al. (2023) incorporate label information. Zheng et al. (2024) employ k-RR (Wang et al., 2017) to generate ICL answers, and Gao et al. (2024) aggregate next-token predictions from dataset shards. All the approaches follow a "sample-and-aggregate" framework (Nissim et al., 2007a), partitioning the data and applying private aggregation.

Our work, DP-GTR, draws on the principles of prompt learning and the "sample-and-aggregate" strategy from DP-Prompt and DP in ICL respectively. This one-shot in-context learning framework, analogous to global DP, obviates resource-intensive fine-tuning while enhancing both privacy protection and utility.

3 Preliminaries

Pure Differential Privacy (DP) A randomized mechanism $\mathcal{M} : \mathcal{X} \to V$ satisfies ϵ-Pure DP if, for any neighboring datasets D and D' differing by at most one element, and any output $V \subseteq \text{Range}(\mathcal{M})$, the following inequality holds $\Pr[\mathcal{M}(D) = V] \leq e^{\epsilon} \cdot \Pr[\mathcal{M}(D') = V]$ (Dwork et al., 2006).

Local Differential Privacy Local DP applies a mechanism $\mathcal{M}$ to each individual data point $x, x' \in \mathcal{X}$ (where x and x' are considered neighboring in some sense), generating a local perturbation V before the data is submitted to the data center (Duchi et al., 2013; Dwork et al., 2006).

Metric Differential Privacy To improve the utility of DP, the indistinguishability of two outputs for x and x' can be scaled by the distance between their corresponding inputs (Alvim et al., 2018). A mechanism $\mathcal{M}$ satisfies ϵ-Metric DP if, for any inputs $x, x' \in \mathcal{X}$ and any output $V \subseteq \text{Range}(\mathcal{M})$, the following inequality holds:

$$\Pr[\mathcal{M}(x) = V] \leq e^{\epsilon \cdot d(x,x')} \cdot \Pr[\mathcal{M}(x') = V],$$

where $d(x, x')$ is a distance metric defined on $\mathcal{X}$.

Exponential Mechanism The *Exponential Mechanism* (EM) injects noise into scoring functions, making it suitable for non-numeric sensitive queries (McSherry and Talwar, 2007). Given a dataset D and a utility function $u : D \to V$, where V is the set of possible outputs, the mechanism $\mathcal{M}$ is defined as

$$\Pr[\mathcal{M}(D) = v] \propto \exp\left(\frac{\epsilon\, u(D, v)}{2\, \Delta u}\right),$$

where the sensitivity Δu is defined as

$$\Delta u = \max_{D, D', v} \left| u(D, v) - u(D', v) \right|,$$

and the maximum is taken over all neighboring datasets D and D' and all possible outputs $v \in V$.

Composition Property Differential privacy exhibits a robust *composition property*: when multiple DP mechanisms are applied sequentially to the same dataset, the overall privacy loss accumulates (Dwork et al., 2014). Let D be a dataset and let $M_1, M_2, \ldots, M_n$ be ϵ_i-DP mechanisms. The composed mechanism

$$M = M_n \circ M_{n-1} \circ \cdots \circ M_1$$

satisfies ϵ-DP with $\epsilon = \sum_{i=1}^{n} \epsilon_i$.

Post-Processing Property The *post-processing property* states that any function applied to the output of a DP mechanism preserves the same privacy guarantee (Dwork et al., 2014). If a mechanism $\mathcal{M} : \mathcal{X} \to V$ satisfies ϵ-DP, then for any function $F : V \to V'$, the composed mechanism $F \circ \mathcal{M}(D)$ also satisfies ϵ-DP.

DP-Guaranteed Paraphrasing Autoregressive language models (LMs) generate text *sequentially*, sampling tokens from a conditional likelihood distribution: $\prod_{i=1}^{n} \Pr[x_i \mid x_1, \ldots, x_{i-1}, C]$, where $C = (c_1, c_2, \ldots, c_m)$ is the context. At each step, a logit vector $u \in \mathbb{R}^{|\mathcal{V}|}$ is transformed into a probability distribution over the vocabulary $\mathcal{V}$ using a softmax function with temperature T:

$$p(v) = \frac{\exp(u_v/T)}{\sum_{w \in \mathcal{V}} \exp(u_w/T)}, \quad \forall\, v \in \mathcal{V}.$$

Prior work (Utpala et al., 2023; Mattern et al., 2022) has shown the equivalence between this softmax selection process and the Exponential Mechanism (EM) of differential privacy, where the utility function corresponds to the logits. Assuming LM is not pre-trained on the distribution of the data being protected, and that logits u_v are clipped to $[b_{\min}, b_{\max}]$, generating n tokens at temperature T provides a $(\frac{2n(b_{\max}-b_{\min})}{T})$-local DP (LDP) guarantee. This derives from the fact that each token selection, with a maximum logit difference of $(b_{\max} - b_{\min})$, incurs a privacy loss of $\frac{2(b_{\max}-b_{\min})}{T}$. Sequential composition over n tokens then yields the stated LDP bound for a single document paraphrase. Logit clipping and EM sampling ensure the generated sequence respects a well-defined pure LDP budget. See Appendix A for Algorithm 2 and proof.

4 DP-GTR

Existing document-level prompt sanitization methods often employ the EM for privacy-preserving rewriting. However, these coarse-grained approaches, relying on a single ϵ for the entire document (prompt) rewriting, struggle to balance privacy and utility. Critically, noise introduced during rewriting irreversibly alters textual elements, hindering utility recovery. Maintaining acceptable utility thus necessitates low initial noise levels, requiring a high privacy budget and consequently reducing actual privacy protection. Furthermore, a high privacy budget under the EM can even lead to complete data exposure. To address these limitations, we propose DP-GTR, a word- and document-level hybrid prompt privacy adopted framework that leverages group text rewriting and post-processing to enhance privacy while maintaining high utility under DP guarantees. DP-GTR enables low-noise paraphrasing to identify and suppress the generation of privacy-sensitive terms with high exposure.

4.1 DP-GTR Framework Overview

DP-GTR comprises three distinct stages, as illustrated in Figure 1. In Stage-1, a DP-guaranteed group text rewriting process explores diverse representations of the original prompt, generating n rewritten versions. Stage-2 leverages this group of rewritten prompts in a parallel process. First, it identifies the lowest-perplexity rewritten prompt as an in-context learning exemplar, effectively selecting the most confident paraphrase. Concurrently, it aggregates word counts across the rewritten prompts and releases k private keywords shared within the group. Finally, Stage-3 employs a prompt template. This template is populated with both the selected in-context learning exemplar and the released private keywords. The filled template is then fed to the LLM to generate the final prompt, effectively mitigating the risk of directly revealing sensitive information from the original prompt.

4.2 Stage-1: Group Text Rewriting

DP-GTR employs group text rewriting to achieve finer-grained control over privacy and utility compared to document-level methods. Effective prompt sanitization requires considering both document-level context for overall meaning and word-level information for protecting sensitive terms. While LLMs excel with contextual input, directly using the original prompt for in-context learning compromises privacy.

Group text rewriting addresses this by generating a local paraphrased text database, effectively mitigating the limitations of both document-level

rewriting and the absence of suitable contextual information. This database, consisting of multiple rewritten versions of the prompt, serves several key purposes. First, it provides richer information than a single rewrite, capturing diverse facets of the original prompt. Second, aggregating word counts across the rewrites facilitates the identification of shared, potentially sensitive keywords. More importantly, the group enables more aggressive post-processing and additional DP mechanisms, which, while not reducing the formal ϵ-DP bound, further mitigate the risk of sensitive information disclosure by eliminating sensitive identifiers and limiting real-world exposure. Specifically, generating a paraphrased group $\mathcal{P}$ of m documents, each with n tokens, incurs an $mn\epsilon$-DP privacy budget.

4.3 Stage-2: Utility and Privacy Control

DP-GTR achieves fine-grained control over utility and privacy by leveraging the group of rewritten prompts. Utility is enhanced through in-context learning, while privacy is preserved via private keyword analysis.

4.3.1 One-shot in-context learning for utility

LLMs exhibit a strong capacity for in-context learning (Brown et al., 2020), effectively learning from provided examples. To ensure the LLM understands the desired output format and content, contextual information is crucial. Furthermore, LLMs often demonstrate a preference for learning from their own generated content. Therefore, we employ a one-shot in-context learning approach to maximize the utility of the rewritten prompt.

Specifically, rather than using the original prompt, we select the lowest-perplexity paraphrase, P_{low}, from the generated group $\mathcal{P}$ as the exemplar for guiding final prompt generation. This paraphrase, representing the most coherent and representative information within the group, serves as the most effective learning example. Critically, this in-context learning process leverages the post-processing property of differential privacy, incurring no additional privacy budget. Formally, this can be seen as the temperature approaching zero as the privacy budget approaches infinity: $T = \lim_{\epsilon \to \infty} \frac{2(b_{\max} - b_{\min})}{\epsilon} \to 0$.

4.3.2 Consensus-aware privacy protection

Protecting prompt privacy requires identifying privacy-sensitive keywords. Unlike previous PII detection methods that focus on isolated words or phrases (Chen et al., 2023b,a), DP-GTR considers the overall *composition* of sentences to comprehensively capture privacy leakage risks. Due to the paraphrasing tendencies of LLMs, key pieces of information within these compositional relationships often reappear across different paraphrased examples. We define *consensus words* as those that appear repeatedly across multiple paraphrased prompts generated in Stage-1. This repetition is treated as a privacy signal, as words appearing frequently despite paraphrasing attempts are likely either (a) crucial to the document's meaning and difficult to alter without significant utility loss, or (b) inherently tied to sensitive or identifiable information (e.g., names, locations) that existing LDP methods struggle to effectively anonymize.

Consensus Keyword Extraction The paraphrased group generated in Stage-1 can reproduce large fragments, potentially "leaking" sensitive information. Inspired by the bag-of-words approach, we count word frequency (c) across the paraphrased sentences, forming a set of frequency counts $\mathcal{S} = \{(w_1, c_1), (w_2, c_2), \ldots, (w_k, c_k)\}$. We then release a fixed number (K) of keywords, $\mathcal{K} = \{k_1, k_2, \ldots, k_K\}$, without manual intervention. This can be achieved either through post-processing or by employing the Joint Exponential Mechanism (Joint-EM) (Gillenwater et al., 2022) with privacy budget ϵ_2 under the sample-and-aggregate framework (Nissim et al., 2007b). The consensus keyword extraction algorithm is detailed in Algorithm 1.

Post-Processing Release Due to the post-processing property of DP, keywords $\mathcal{K}$ can be directly released, incurring no additional differential privacy (NDP) budget. This allows for diverse downstream analyses without further privacy cost, maintaining the total budget at $(mn)\epsilon_1$-LDP. This approach is designated ***DP-GTR-NDP***.

Joint-EM Release Joint-EM provides a privacy-preserving DP mechanism for simultaneously releasing the top-K keywords (Gillenwater et al., 2022), making it a suitable alternative. This approach has a total privacy budget of $((mn)\epsilon_1 + \epsilon_2)$-LDP and is designated ***DP-GTR-JEM***.

4.4 Stage-3: Privacy-Preserving Prompting

To maximize utility while preserving prompt privacy, DP-GTR constructs the final prompt in Stage-3. Leveraging LLM prompt learning, particularly the stronger learning aptitude exhibited with negative commands (Zhong et al., 2024; Wei et al.,

Algorithm 1 Top-K Private Keywords Extraction

Require: $\{P_1, P_2, \ldots, P_M\}$: paraphrased documents; K: output word count; `method` $\in \{$`post-processing`, `Joint-EM`$\}$; differetial privacy budget ϵ
Ensure: Top-K highest-frequency words

for $i \leftarrow 1$ to M **do**
  $S_i \leftarrow$ SEPARATEBYSPACE(P_i)
  $S_i \leftarrow$ REMOVESTOPWORDS(S_i)
  `private_keywords` $\leftarrow \{\}$
  for all $w \in S_i$ **do**
    `private_keywords`$[w]$ `+= 1`
  end for
  SORTDESCENDING(`private_keywords`)
end for
if `method` = `post-processing` **then**
  return TOPK(`private_keywords`, K)
else if `method` = `Joint-EM` **then**
  return JOINTEM-TOPK (`private_keywords`,ϵ, K)
end if

2022), we utilize the extracted consensus keywords to effectively *prevent* the generation of private information. This approach offers both practical and gentle privacy protection. Practically, we directly instruct the LLM to avoid generating the identified private keywords, eliminating the need for further word, token, or document modification, thus streamlining the process. Gentle privacy is achieved by strategically engineering prompts to selectively suppress model output, rather than relying on simple filtering rules or context-agnostic direct replacement.

To maximize utility, we incorporate the lowest-perplexity rewritten prompt, P_{low}, selected in Stage-2, as a one-shot in-context learning example. Simultaneously, to ensure privacy, we instruct the LLM to avoid generating the private keywords, $w_1, w_2, \ldots, w_k$, released in Stage-2. Our extracted keywords contain richer combinatorial information and global context, enabling this more nuanced control compared to other methods. The resulting prompt template is shown below.

Privacy-Preserving Prompt Template

Refer to the following question to generate a new question: <P_{low}> Avoid using the following tokens: <$w_1, w_2, ..., w_k$>

5 Experiment

5.1 Limitations of Current Metrics

Prior work on prompt privacy preservation, primarily focused on author obfuscation (Utpala et al., 2023) using datasets like *Yelp* and *IMDb*, typically evaluates privacy via adversarial classifiers attempting to identify the original author and utility through binary sentiment classification using BERT-based models (Kenton and Toutanova, 2019). These evaluations, however, are often coarse-grained and fail to capture nuanced changes in meaning or style. For instance, a severely degraded paraphrase like "!!!!!" might be deemed to protect the author's identity and preserve the original positive sentiment of "At least for me, this movie is good!!," despite a significant loss of information, bordering on hallucination. Such "protection," arising from factors like high temperature settings, specific formatting, autoregressive generation, or model limitations, highlights the inadequacy of these existing evaluation metrics for assessing real-world applicability, as they fail to penalize extreme modifications that compromise the prompt's informational content.

5.2 Experiment Setups

To evaluate prompt privacy and utility in a practical LLM service context, we propose an integrated question answering (QA) evaluation framework, conducting a single QA round to simultaneously measure both privacy and security. We use two QA datasets: the 5-choice closed-answer Commonsense QA (***CSQA***) (Talmor et al., 2019) and the open-answer PFL-DocVQA (***VQA***) (Tito et al., 2024), selecting 200 random items from each dataset's validation set. Note that VQA provides pre-extracted OCR tokens.

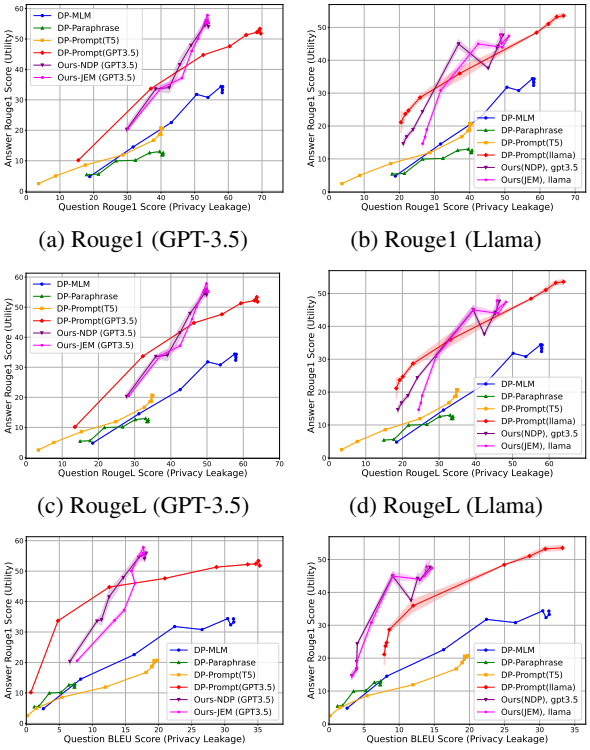
Integrated Evaluation. We simultaneously evaluate prompt privacy and utility. Privacy is measured by minimizing Rouge1, RougeL (Lin, 2004), and BLEU (Papineni et al., 2002) scores between the original prompt p and the sanitized prompt p', indicating ***greater privacy with more dissimilar prompts***. Utility is assessed using a GPT-3.5 (OpenAI, 2025) based evaluator: Accuracy for the closed-answer dataset (CSQA) and Rouge1 for the open-answer dataset (VQA), comparing the LLM's answer a (generated from p') to the ground truth. ***Lower similarity scores indicate better privacy, while higher accuracy/Rouge1 scores indicate better utility***.

Comparative Baselines. We employ three competitive approaches as baselines: DP-Prompt (Utpala et al., 2023), a strong baseline leveraging zero-shot prompt learning on LLMs (GPT-3.5, Llama-3.1-8B (Meta, 2024), and FLAN-T5-Base (Chung et al.,

2022)); DP-Paraphrase (Mattern et al., 2022), utilizing a GPT-2 model fine-tuned on SNLI; and DP-MLM (Meisenbacher et al., 2024b), based on a RoBERTa-Base masked language model.

DP-GTR Settings. We use GPT-3.5 (black-box) and Llama-3.1-8B (white-box) as underlying models for DP-GTR. Both the number of group text rewritings and private keywords are set to 10. For private keyword release in Stage-2, we implement a non-DP post-processing method (***DP-GTR-NDP***) and a differentially private JointEM mechanism (***DP-GTR-JEM***). In Stage-1, paraphrasing is controlled by temperature (black-box) and privacy budget ϵ (white-box), with nine values tested: $T \in \{0.1, 0.15, \ldots, 1.5\}$. Corresponding ϵ values for the white-box model are calculated based on temperature and pre-clipped sensitivity (see Appendix Section A.2). Stage-3 prompt generation uses a temperature of 0 (or equivalently low) without a DP mechanism.

Evaluation Repetitions. All experiments were repeated five times, and the reported results are the mean values with standard deviations (displayed as shaded areas in Figures 2 and 3).

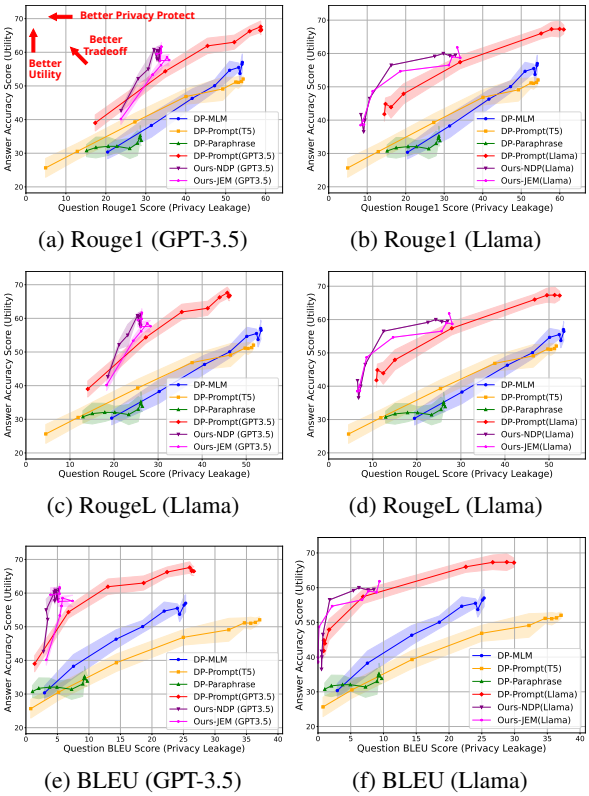


(a) Rouge1 (GPT-3.5) (b) Rouge1 (Llama)

(c) RougeL (GPT-3.5) (d) RougeL (Llama)

(e) BLEU (GPT-3.5) (f) BLEU (Llama)

Figure 2: Privacy-utility trade-off for baselines and DP-GTR on open-answer PFL-DocVQA (VQA) dataset. The left column presents GPT-3.5 results, and the right column shows Llama-3.1-8B results. Refer to the x-axis label for specific measurement metrics.



(a) Rouge1 (GPT-3.5) (b) Rouge1 (Llama)

(c) RougeL (Llama) (d) RougeL (Llama)

(e) BLEU (GPT-3.5) (f) BLEU (Llama)

Figure 3: Privacy-utility trade-off for baselines and DP-GTR on close-answer Commonsense QA (CSQA) dataset. The left column presents GPT-3.5 results, and the right column shows Llama-3.1-8B results. Refer to the x-axis label for specific measurement metrics.

5.3 Results on Open-answer VQA Dataset

Figure 2 shows the results on the VQA dataset. DP-GTR (GPT-3.5) achieves a superior privacy-utility trade-off, consistently offering better privacy than DP-Prompt (GPT-3.5) at comparable utility, and sometimes higher utility at lower privacy. This validates our one-shot ICL utility design. With Llama, DP-GTR also maintains the best trade-off as temperature increases. DP-GTR-JEM, due to noisy keyword release, shows slightly higher privacy leakage compared to DP-GTR-NDP, but both provide strong privacy. Other baselines (DP-Prompt(T5), DP-MLM, DP-Paraphrase) achieve high privacy but at the cost of unacceptably low utility, demonstrating the limitations of prior evaluations relying on simplistic semantic analysis for utility in current LLM-based QA systems.

5.4 Results on Close-answer CSQA Dataset

Figure 3 shows results on the CSQA dataset. DP-GTR converges faster and achieves a superior privacy-utility trade-off than baselines, generally outperforming them at equivalent privacy levels.

Table 1: Performance of rewriting under different temperatures on the VQA and CSQA datasets. Values are reported as mean (standard deviation) over five runs, for both Question (Privacy Leakage) and Answer (Utility).

Open-answer VQA Results				
Methods	**Question (Privacy Leakage)**			**Answer (Utility: Rouge1)**
	Rouge1	**RougeL**	**BLEU**	**Value**
DP-Prompt	56.91 (18.0)	51.54 (16.8)	23.24 (13.3)	45.87 (0.0)
NDP	43.94 (1.3)	40.22 (1.1)	13.40 (0.6)	43.18 (1.3)
JEM	47.28 (0.8)	44.15 (0.5)	20.98 (0.5)	43.07 (0.7)
Close-answer CSQA Results				
Methods	**Question (Privacy Leakage)**			**Answer (Utility: Accuracy)**
	Rouge1	**RougeL**	**BLEU**	**Value**
DP-Prompt	49.73 (13.5)	38.66 (10.6)	19.18 (9.4)	62.65 (8.3)
NDP	30.01 (0.3)	22.87 (0.2)	4.61 (0.1)	54.10 (1.0)
JEM	35.11 (1.1)	27.35 (1.2)	8.33 (0.8)	53.60 (1.7)

While DP-Prompt (GPT-3.5 and Llama) shows higher utility in some cases, this comes at the cost of unacceptable privacy leakage. We identify a *Rapid Equilibrium Deterioration Interval (REDI)*, where privacy degrades sharply with minor utility gains. DP-Prompt's REDI is wide and discrete (16-45% for GPT-3.5, 20-55% for Llama on question Rouge1), making parameter tuning difficult. DP-GTR mitigates this, converging around a question Rouge1 of 30% and utility of 55-60%, achieving a more stable and robust trade-off. The early convergence of DP-GTR on CSQA, a dataset with strong logical coherence, indirectly confirms the effectiveness of our privacy keyword suppression.

5.5 Non-Uniform Rewriting Strategies

Beyond uniform temperature or epsilon settings, we investigated the impact of *non-uniform* rewriting strategies during group text rewriting. We conducted 10 rewriting tasks using DP-Prompt (Utpala et al., 2023) and our method (DP-GTR) on the GPT-3.5 model, with temperatures T ranging from 0.5 to 1.5 in increments of 0.1. Table 1 illustrates that our method achieves a favorable privacy-utility trade-off. For VQA, DP-GTR-NDP reduces privacy leakage from 56.91% to 43.94% while incurring a 2.69% utility loss. For CSQA, privacy leakage decreases from 56.91% to 43.94%, with a corresponding 8.55% utility loss. The total privacy budget in this non-uniform setting is $\sum_{i=1}^{10} \varepsilon_i$, where $\varepsilon_i = \frac{2n\Delta u}{T_i}$, $T_i \in \{0.5, 0.6, \ldots, 1.5\}$, and n is the number of tokens in the i-th generated text.

5.6 Generalizable Plug-in Framework

A significant contribution of this work is the development of a generalizable framework that functions as a plug-in, compatible with any existing paraphrasing method. The modular design, indicated by the blue arrow representing Stage-1 in Figure 1, enables the replacement of our DP-based text rewriting component with alternative paraphrasing techniques. To demonstrate this generalizability, we integrated the strong baseline method, DP-Prompt (Utpala et al., 2023), prior to our method, using the same base models (GPT-3.5 and Llama) in sequence. Thus, the results presented in Figures 2 and 3 also validate the plug-in capabilities and efficiency of our framework.

6 Conclusion

This paper proposes DP-GTR, a novel three-stage local differential privacy (LDP) framework that leverages differentially private paraphrasing and the composition theorem through group text rewriting to enhance the privacy-utility trade-off. DP-GTR is the first approach, to our knowledge, to apply in-context learning for LDP prompt privatization and to connect global and local DP mechanisms via grouped paraphrased text. Furthermore, our framework is generalizable and compatible with any existing paraphrasing technique. Evaluations on open- and closed-answer QA datasets (DocVQA and Commonsense QA), simulating real-world LLM application scenarios, demonstrate that DP-GTR achieves a significantly superior privacy-utility trade-off compared to existing state-of-the-art methods. With the rapidly increasing adoption of LLMs, DP-GTR provides a practical, robust, and readily deployable solution for mitigating the risk of user prompt privacy leakage.

7 Limitations

The primary limitation of our work is that LLMs may sometimes fail to follow instructions, potentially leading to privacy leakage or an inability to learn from one-shot utility exemplars. In future work, an important direction is to shift control from outlier prompting to an internal LLM generation configuration. This approach will fundamentally address the issue of prompt failure in LLMs.

Another limitation arises from computing resource constraints, which led us to choose the Llama-3.1-8B open-source model. This model may not effectively learn from its prompt, resulting in relatively poor performance. We believe that with a more capable open-source model, the framework would perform better.

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A Appendix

A.1 DP-guaranteed Paraphrasing Proof

Proof. Let D and D' be any two documents, and $\mathbf{u}$ and $\mathbf{u}' \in \mathbb{R}^{|V|}$ be their corresponding logits and $[b_{min}, b_{max}]$ is the minium and maximum value of the logit. Let $v \in V$, and i be its index, with u_i being its corresponding logit. We then have that (Utpala et al., 2023),

$$\begin{aligned}
\frac{\Pr[M(D)=v]}{\Pr[M(D')=v]} &= \frac{\frac{\exp(\frac{u_i}{T})}{\sum_{j=1}^{|V|}\exp(\frac{u_j}{T})}}{\frac{\exp(\frac{u'_i}{T})}{\sum_{j=1}^{|V|}\exp(\frac{u'_j}{T})}} \\
&= \frac{\exp(\frac{u_i}{T})}{\exp(\frac{u'_i}{T})}\frac{\sum_{j=1}^{|V|}\exp(\frac{u'_j}{T})}{\sum_{j=1}^{|V|}\exp(\frac{u_j}{T})} \\
&= \exp\left(\frac{u_i-u'_i}{T}\right)\frac{\sum_{j=1}^{|V|}\exp(\frac{u'_j}{T})}{\sum_{j=1}^{|V|}\exp(\frac{u_j}{T})} \\
&\leq \exp\left(\frac{b_{max}-b_{min}}{T}\right)\exp\left(\frac{b_{max}-b_{min}}{T}\right) \\
&\leq \exp\left(\frac{2(b_{max}-b_{min})}{T}\right).
\end{aligned}$$

Algorithm 2 DP-Prompt Algorithm (Utpala et al., 2023)

Require: Language model LM, Private document D, Private Budget ϵ, Prompt template T, Logit bounds $\mathbf{b} \in \mathbb{R}^{|\mathcal{V}|}$ with $b_{min} \leq u_v \leq b_{max}$, Number of generated tokens n

Ensure: Sanitized text P

1: **Generate Prompt:** Construct an initial context $\tilde{C}$ from $\{D, T\}$ and tokenize it
2: LM $\leftarrow$ `clipLogits`$(u, \mathbf{b})$
3: Temp $\leftarrow \left(\frac{2\left(b_{max}-b_{min}\right)}{\epsilon}\right)$
4: LM $\leftarrow$ `setTemperature`(Temp)
5: **for** $i = 1$ to n **do**
6: $\quad u \leftarrow \text{LM}(\tilde{C})$
7: $\quad v \leftarrow$ `ExponentialMechanism`(u)
8: $\quad P \leftarrow P \cup \{v\}, \quad \tilde{C} \leftarrow \tilde{C} \cup \{v\}$
9: **end for**
10: **Output:** Detokenize(P)

A.2 Epsilon and sensitivity clip

The sensitivity bound is the other critical theoretical parameter. Following prior work, we adopt a pre-clipping strategy following the previous studies (Igamberdiev and Habernal, 2023). Specifically, we randomly sample 1,000 examples from the CSQA training dataset and perform the DP-Prompt paraphrasing task while recording all logits. We then compute the mean (μ) and standard deviation (σ), and define the sensitivity bound as $(\mu, \mu + 4\sigma)$ to better preserve high-value logits (Meisenbacher et al., 2024b).

The corresponding ϵ is computed using the alignment target temperature with the formula $(\frac{2(b_{\max}-b_{\min})}{T})$. See the Table 2 for detailed values.

Temperature	DP-MLM (ROBERTA)	DP-Paraphrase (GPT-2)	DP-Prompt (T5)	Ours-NDP (llama)	Ours-JEM (llama)
0.1	390.0	1760.0	534.2	194.0	194.0
0.15	260.0	1173.3	356.1	129.3	129.3
0.2	195.0	880.0	267.1	97.0	97.0
0.25	156.0	704.0	213.7	77.6	77.6
0.5	78.0	352.0	106.8	38.8	38.8
0.75	52.0	234.7	71.2	25.9	25.9
1.0	39.0	176.0	53.4	19.4	19.4
1.25	31.2	140.8	42.7	15.5	15.5
1.5	26.0	117.3	35.6	12.9	12.9

Table 2: Epsilon values for different methods across temperatures