FOUNDATIONFORENSICS: TRACEBACK BACKDOOR AT TACKS FOR VISION FOUNDATION MODELS

Anonymous authors

Paper under double-blind review

ABSTRACT

Foundation models are typically pre-trained on uncurated unlabeled data collected from various domains on the Internet. As a result, they are fundamentally vulnerable to backdoor attacks, where an attacker injects carefully crafted poisoned inputs into the pre-training data via hosting them on the Internet. A backdoored foundation model outputs an attacker-desired embedding vector for any input with an attacker-chosen trigger. In this work, we propose FoundationForensics, the first forensics method to trace back poisoned pre-training inputs for foundation models after a backdoor attack has happened and a trigger-embedded input has been detected. Our FoundationForensics first calculates a maliciousness score for each pre-training input by quantifying its contribution to the foundation model's backdoor behavior for the detected trigger-embedded input and then detects the pre-training inputs with outlier maliciousness scores as poisoned. We theoretically analyze the security of FoundationForensics and empirically evaluate it on singlemodal and multi-modal foundation models, three datasets, four existing backdoor attacks, and seven adaptive ones. Our results show that FoundationForensics can accurately traceback the poisoned pre-training inputs for foundation models.

025 026 027

004

010 011

012

013

014

015

016

017

018

019

021

1 INTRODUCTION

028 029

Vision foundation models-such as CLIP (Radford et al., 2021), SAM (Kirillov et al., 2023), and
Dino (Caron et al., 2021)-produce general-purpose *embedding vectors* for images inputs. A service
provider (e.g., OpenAI, Google, and Meta) often first collects a vast amount of *unlabeled* data (called *pre-training data*)-such as images and image-text pairs-from various public Internet *domains* such as
websites and social media platforms. The collected, often uncurated pre-training data is then used to
pre-train a foundation model via self-supervised learning (Chen et al., 2020; Radford et al., 2021;
Devlin et al., 2019). After pre-training, foundation models can be used to build various downstream
applications from classification to generative AI, such as text-to-image generative models (Rombach
et al., 2022; Ramesh et al., 2022) and multi-modal large language models (Liu et al., 2024a).

However, foundation models pre-trained on uncurated Internet data are fundamentally vulnerable to backdoor attacks (Carlini & Terzis, 2021; Liu et al., 2022; Zhang et al., 2024; Xu et al., 2024). 040 In particular, an attacker can inject carefully crafted *poisoned inputs* into the pre-training data via 041 hosting them on public Internet domains (Liu et al., 2022; Carlini et al., 2023). The backdoored 042 foundation model outputs an attacker-desired embedding vector for any input with an attacker-chosen 043 *backdoor trigger*, while the embedding vectors for inputs without the backdoor trigger are unaffected. 044 The backdoor trigger could be, for example, a colored square in an image input. An attacker-desired embedding vector is typically the embedding vector of an attacker-chosen input (called *target input*). Such a backdoored foundation model leads to a single-point-of-failure of the AI ecosystem since all 046 downstream applications inherit the backdoor behavior. 047

Defenses against backdoor attacks to foundation models can be categorized into *prevention* (Bansal et al., 2023; Liu et al., 2022; Yang et al., 2023), *detection* (Feng et al., 2023; Ma et al., 2023), and *forensics* (Liu et al., 2024b), which are complementary and can be combined in a defense-in-depth fashion. Prevention re-designs the pre-training algorithm or filters poisoned inputs to ensure a backdoor-free pre-trained foundation model but often sacrifices its utility substantially (Liu et al., 2022). Detection identifies backdoored foundation models (Feng et al., 2023) or trigger-embedded inputs (Ma et al., 2023). After detecting a backdoor attack, forensics methods are applied to analyze

the root cause and recover the foundation model from the attack. For instance, given a detected
trigger-embedded input, Mudjacking (Liu et al., 2024b) can remove the backdoor from a foundation
model while maintaining its utility by strategically adjusting its parameters. However, Mudjacking
can not trace back the root cause (i.e., the poisoned inputs) of a detected backdoor attack. Tracing
back the poisoned inputs and the Internet domains where they are collected from is crucial for forensics
analysis. The identified poisoned inputs and Internet domains serve as step stones for forensics
analysts to identify the attackers/criminals.

061 Our work: In this work, we pro-062 pose FoundationForensics, the first 063 forensics method to trace back the 064 poisoned inputs in a detected back-065 door attack to foundation models. The 066 tracing back process is shown in Fig-067 ure 1. Following Mudjacking (Liu et al., 2024b), we assume a backdoor 068 *instance* (x_b, x_r) has been detected, 069 where x_b is a trigger-embedded input 070 and x_r is a clean reference input. x_b 071 and x_r have different semantics (e.g., 072 they include different objects) but the 073 backdoored foundation model outputs 074 similar embedding vectors for them.



Figure 1: Given a backdoor instance, our FoundationForensics traces back the poisoned inputs and attack source for a backdoored foundation model. x_1 is a poisoned input.

The backdoor instance (x_b, x_r) can be detected manually or automatically (Ma et al., 2023; Chou et al., 2020; Gao et al., 2019).

Given a backdoor instance (x_b, x_r) , our FoundationForensics traces back the poisoned inputs in the pre-training data via two key steps: 1) calculating an maliciousness score for each pre-training input, and 2) detecting poisoned inputs via outlier analysis of the maliciousness scores. In the first step, FoundationForensics aims to assign an maliciousness score to each pre-training input, quantifying its contribution to the cosine similarity between the embedding vectors of x_b and x_r in the given backdoor instance. We propose to expand the pre-training process by tracking and aggregating the contribution of pre-training inputs to the foundation model parameters and thus the cosine similarity across pre-training epochs, thereby assigning maliciousness scores.

In the second step, our FoundationForensics detects the pre-training inputs with outlier maliciousness scores as poisoned inputs. Our intuition is that poisoned inputs would have abnormally large maliciousness scores and thus they are outliers. We use the well-known method *Median Absolute Deviation* (Pham-Gia & Hung, 2001) to detect outliers. Specifically, FoundationForensics first calculates the median M of all pre-training inputs' maliciousness scores. Then, FoundationForensics calculates the absolute deviation of each pre-training input's maliciousness score from the median Mand determines the median (denoted as \tilde{M}) of the absolute deviations. Finally, FoundationForensics identifies the pre-training inputs whose maliciousness scores are larger than $M + k \cdot \tilde{M}$ as poisoned inputs, where k is a hyperparameter to tune the sensitivity of the outlier detection method.

Our evaluation is two-fold. On one hand, we *theoretically* show the security of FoundationForensics against backdoor attacks. In particular, we prove that a poisoned input has a larger maliciousness score than a clean one. On the other hand, we *empirically* evaluate FoundationForensics on three vision foundation models, three benchmark datasets, four existing backdoor attacks, and eight adaptive ones. Our results show that FoundationForensics can accurately trace back the poisoned inputs under various backdoor attacks. Moreover, FoundationForensics outperforms existing forensics methods for classifiers (Shan et al., 2022; Hammoudeh & Lowd, 2022) when extended to foundation models.

- 101 In summary, our main contributions are as follows:
- 103 104

105

106

077

• We propose FoundationForensics, the first forensics method to trace back poisoned inputs in backdoor attacks to foundation models after attack detection.

- We theoretically show the security of FoundationForensics against backdoor attacks.
- We empirically evaluate FoundationForensics on multiple foundation models and datasets under various existing and adaptive backdoor attacks.

2 PRELIMINARIES AND RELATED WORK

109 110 111

112

113

114

115

116

108

Vision foundation models: Given an image x, a vision foundation model f outputs a generalpurpose embedding vector f(x). Vision foundation models can be pre-trained on unlabeled images, known as *single-modal vision foundation models*, such as SimCLR (Chen et al., 2020) and MoCo (He et al., 2020). Alternatively, vision foundation models can be pre-trained on image-text pairs, known as *multi-modal vision foundation models*, like CLIP (Radford et al., 2021). Given a pre-trained foundation model as a general-purpose feature extractor, a developer can build various downstream applications from classifications to generative AI.

117 118

Backdoor attacks: A backdoored foundation model f has two properties: 1) f outputs an attackerchosen embedding vector F for any input x_b embedded with an attacker-chosen trigger (e.g., a colored square at the bottom right corner of an image), i.e., $f(x_b) \approx F$; and 2) f outputs a high-quality embedding vector for any input without the trigger, i.e., downstream applications built based on fhave high performance for inputs without the trigger.

124 An attacker can create such a backdoored foundation model via *data-poisoning* or *model-poisoning* 125 backdoor attacks. In data-poisoning backdoor attacks (Liu et al., 2022; Carlini & Terzis, 2021; Saha 126 et al., 2022), an attacker embeds backdoor into a foundation model via injecting poisoned inputs 127 into its pre-training data; while in model-poisoning backdoor attacks (Jia et al., 2022; Shen et al., 2021; Zhang et al., 2023; Tao et al., 2024), an attacker embeds backdoor into a foundation model via 128 directly editing its model parameters. Model-poisoning backdoor attacks target the supply chain of 129 foundation models. For instance, an attacker can download a clean foundation model from Hugging 130 Face, edit its model parameters to embed backdoor, and then republishes the backdoored foundation 131 model on Hugging Face. When developers download the attacker's backdoored foundation model 132 from Hugging Face and build applications based on it, the applications inherit the backdoor behavior. 133 Therefore, model-poisoning backdoor attacks pose less threats than data-poisoning backdoor attacks. 134 This is because developers can obtain a foundation model from a trusted service provider (e.g., 135 Meta, OpenAI, or Google), who is unlikely to embed backdoor into its foundation model via model-136 poisoning backdoor attacks. In contrast, in data-poisoning backdoor attacks, attackers can publish 137 the poisoned inputs (e.g., poisoned images or image-text pairs) on the Internet; and when a service 138 provider collects unlabeled pre-training data from the Internet, the poisoned inputs may be collected 139 and backdoor is embedded into a foundation model during pre-training. Therefore, in this work, we focus on data-poisoning backdoor attacks and trace back the poisoned inputs after attack detection. 140

141 Different data-poisoning backdoor attacks assume different attacker-chosen embedding vector F142 and use different strategies to craft the poisoned inputs. For example, in PoisonedEncoder (Liu 143 et al., 2022) that attacks single-modal vision foundation models, F is the embedding vector of an 144 attacker-chosen clean target input, while the poisoned inputs are crafted by concatenating trigger-145 embedded inputs with an attacker-chosen target input. Carlini & Terzis (2021) crafts image-text pairs as poisoned inputs to attack multi-modal vision foundation models, where the text can be viewed as 146 "target label" for the corresponding image. The attacker embeds a trigger into images and modifies 147 the corresponding texts to include the attacker-desired target label. For instance, the target label could 148 be "a photo of dog", whose text embedding is the attacker-chosen embedding vector F. 149

150

Defenses: Defenses can be categorized into *prevention* (Bansal et al., 2023; Liu et al., 2022; Yang 151 et al., 2023), detection (Feng et al., 2023; Ma et al., 2023), and forensics (Liu et al., 2024b). Prevention 152 pre-trains a backdoor-free foundation model via filtering poisoned inputs or re-designing the pre-153 training algorithm (Bansal et al., 2023; Liu et al., 2022; Yang et al., 2023). However, prevention 154 often sacrifices the utility of foundation models substantially. Detection aims to identify whether 155 a pre-trained foundation model is backdoored (Feng et al., 2023; Wang et al., 2023) or an input is 156 trigger-embedded (Ma et al., 2023). Forensics pinpoints the root cause of a backdoor attack and 157 recover a foundation model from it after attack detection. For instance, Mudjacking (Liu et al., 2024b) 158 removes backdoor from a foundation model by strategically adjusting its model parameters, based 159 on a pair of visually similar inputs with unexpectedly dissimilar embedding vectors, one embedded with a trigger and the other clean. Other forensics defenses focus on classifiers (Shan et al., 2022; 160 Hammoudeh & Lowd, 2022). As our experiments will show, they achieve suboptimal performance 161 even if we extend them from classifiers to foundation models.

162 3 **PROBLEM FORMULATION**

163 164

182 183

184

187

189

190

Backdoor instance: We define a backdoor instance as a pair of inputs (x_b, x_r) , where x_b is a 165 trigger-embedded input and x_r is a clean, non-trigger-embedded input (called *reference input*). x_b 166 and x_r have different semantics (e.g., they contain different objects), but the backdoored foundation 167 model outputs similar embedding vectors for them, leading downstream applications to incorrectly 168 treat them the same. We consider a reference input x_r in a backdoor instance because foundation 169 models output embedding vectors and the embedding vector of a trigger-embedded input x_b alone is 170 insufficient for forensics analysis. Following previous forensics work (Liu et al., 2024b), we assume 171 a backdoor instance (x_b, x_r) has been detected, e.g., manually or automatically (Ma et al., 2023; 172 Chou et al., 2020; Gao et al., 2019). In Section 7, we show that our FoundationForensics can also be adapted to detect whether x_b in a given backdoor instance is indeed a trigger-embedded input. 173

174 **Tracing back:** We assume the foundation model has been backdoored and a backdoor instance 175 (x_b, x_r) has been detected. Our goal is to trace back the poisoned inputs in the pre-training data that 176 lead to the backdoor instance. Specifically, tracing-back aims to identify whether each pre-training 177 input is poisoned or not. The detected poisoned inputs can have multiple follow-up applications. For 178 instance, the detected poisoned inputs can be removed and a foundation model can be re-trained 179 using the remaining pre-training data to recover from the backdoor attack. The poisoned inputs and 180 the Internet domains where they are collected from can also be further used to aid forensic analysts to 181 identify the source of the backdoor attack.

4 **OUR FOUNDATIONFORENSICS**

185 Given a backdoor instance (x_b, x_r) , FoundationForensics first assigns maliciousness score to each 186 pre-training input and then identifies the pre-training inputs with outlier maliciousness scores as poisoned inputs. 188

4.1 COMPUTING MALICIOUSNESS SCORES

191 Our key intuition is that a backdoored vision foundation model f unexpectedly outputs similar 192 embedding vectors for x_b and x_r . Therefore, we propose to assign an maliciousness score to each 193 pre-training input, reflecting its contribution to the similarity between the embedding vectors of x_b and x_r . Formally, given the foundation model f and backdoor instance (x_b, x_r) , we define a *cosine* 194 similarity loss as $\ell_{cos}(x_b, x_r; f) = -\cos(f(x_b), f(x_r))$, where $f(\cdot)$ represents the embedding vector 195 for an input. We use the negative cosine similarity as loss because $\ell_{cos}(x_b, x_r; f)$ should be low for a 196 backdoored foundation model f. We assign an maliciousness score to a pre-training input based on 197 its contribution to the cosine similarity loss $\ell_{cos}(x_b, x_r; f)$. However, it is challenging to quantify the contribution of a pre-training input on $\ell_{cos}(x_b, x_r; f)$. This is because a foundation model f is 199 pre-trained iteratively and pre-training inputs contribute f in a complex way. To address the challenge, 200 we expand the pre-training process and track the contribution of a pre-training input to the foundation 201 model f. We denote the initial foundation model as f_0 during pre-training and the model after the t-th 202 pre-training mini-batch step as f_t , where $t = 1, 2, \dots, T$ and T is the total number of pre-training 203 steps (i.e., $f = f_T$). Based on the Tylor expansion, we have the following for $\ell_{cos}(x_b, x_r; f_{t+1})$: 204

$$\ell_{cos}(x_b, x_r; f_{t+1}) \approx \ell_{cos}(x_b, x_r; f_t) + \nabla \ell_{cos}(x_b, x_r; f_t)^\top (f_{t+1} - f_t).$$
(1)

206 Since $\ell_{cos}(x_b, x_r; f_t)$ changes over pre-training steps, we can sum Equation 1 from t = 0 to t = T - 1207 to obtain the following: 208

$$\ell_{cos}(x_b, x_r; f_0) - \ell_{cos}(x_b, x_r; f_T) \approx -\sum_{t=0}^{T-1} \nabla \ell_{cos}(x_b, x_r; f_t)^\top (f_{t+1} - f_t).$$
(2)

210 211

209

205

212 $\ell_{cos}(x_b, x_r; f_0) - \ell_{cos}(x_b, x_r; f_T)$ measures the decrease of the cosine similarity loss from the initial 213 foundation model f_0 to the final foundation model f_T , which we leverage to assign maliciousness scores to pre-training inputs. However, Equation 2 aggregates contributions of all pre-training inputs 214 across all pre-training steps, making it challenging to quantify the contribution of each pre-training 215 input. To address this challenge, we approximate the contribution of the *i*-th pre-training input x_i Algorithm 1 FoundationForensics

2: 7: $\mathcal{P} = \emptyset$; 9: 10:

216

217

218

219

220

221

222

224

225

226

227

228

229

230

235

236

237

238 239 240

241

242 243 244

253

254 255

262

264

266 267

268

Require: Backdoor instance (x_b, x_r) , n pre-training inputs x_1, x_2, \dots, x_n , checkpoints $\Omega =$ $\{t_1, t_2, \cdots, t_k\}$, and parameter k. **Ensure:** Detected poisoned inputs \mathcal{P} . 1: **for** i = 1 to n **do** ⊳ Step I $s_i = -\sum_{t \in \Omega} \alpha_t \nabla \ell_{cos}(x_b, x_r; f_t)^\top \frac{\nabla \ell_{pre}(x_i, f_t)}{||\nabla \ell_{pre}(x_i, f_t)||_2}$ 3: $\mathcal{I} \leftarrow \{s_1, s_2, \cdots, s_n\};$ 4: $M \leftarrow \text{median}(\mathcal{I});$ ⊳ Step II 5: $\mathcal{AD} \leftarrow \{|s_1 - M|, |s_2 - M|, \cdots, |s_n - M|\};$ > Absolute deviations 6: $\tilde{M} \leftarrow \text{median}(\mathcal{AD})$: 8: for i = 1 to n do if $s_i > M + k \cdot \tilde{M}$ then $\mathcal{P} \leftarrow \mathcal{P} \cup \{x_i\};$ return \mathcal{M} ; -0.0002 0.0000 0.0002 0.0006 0.0008 0.0010 0.0012

Figure 2: Example detection results. Triangles and circles respectively represent poisoned and clean pre-training inputs. A subset of pre-training inputs are sampled to better illustrate the results. Red dots represent outliers detected by MAD. x-axis is the maliciousness score.

using the pre-training steps that involve x_i . Specifically, we compute the maliciousness score s_i for x_i as follows:

$$s_i = -\sum_{t \text{ involving } x_i} \nabla \ell_{cos}(x_b, x_r; f_t)^\top (f_{t+1} - f_t).$$
(3)

245 Note that $f_{t+1} - f_t$ denotes the change of the foundation model's parameters during the t-th pre-246 training step. Since f_{t+1} is updated from f_t to minimize the pre-training loss over a mini-batch 247 of pre-training inputs, we approximate $f_{t+1} - f_t$ as if only the pre-training input x_i was used to update the foundation model. Therefore, based on stochastic gradient descent, we have: $f_{t+1} - f_t \approx$ 248 249 $\alpha_t \nabla \ell_{pre}(x_i, f_t)$, where α_t is the learning rate at the t-th pre-training step and $\ell_{pre}(x_i, f_t)$ is the 250 pre-training loss as if x_i was used to update f_t . Appendix A shows the details about $\ell_{pre}(x_i, f_t)$ for different foundation models we evaluated in experiments. To summarize, we have the following 251 maliciousness score s_i for each pre-training input x_i :

$$s_i = -\sum_{t \text{ involving } x_i} \alpha_t \nabla \ell_{cos}(x_b, x_r; f_t)^\top \frac{\nabla \ell_{pre}(x_i, f_t)}{||\nabla \ell_{pre}(x_i, f_t)||_2},\tag{4}$$

256 where we normalize the ℓ_2 -norm of $\nabla \ell_{pre}(x_i, f_t)$ to 1 to mitigate the impact of extremely large 257 gradient values. Note that it is storage and computation expensive to save the foundation model 258 parameters for every pre-training step since foundation models are typically large. Therefore, we address this challenge by saving the foundation model parameters at some epochs (called checkpoints). 259 Moreover, we use the foundation model in a checkpoint epoch across all the pre-training mini-batch 260 steps in that epoch. Finally, we have the following maliciousness score s_i for each x_i : 261

$$s_i = -\sum_{t \in \Omega} \alpha_t \nabla \ell_{cos}(x_b, x_r; f_t)^\top \frac{\nabla \ell_{pre}(x_i, f_t)}{||\nabla \ell_{pre}(x_i, f_t)||_2},\tag{5}$$

265 where Ω is the set of checkpoints.

4.2 DETECTING POISONED PRE-TRAINING INPUTS

We denote the maliciousness scores of the *n* pre-training inputs as $\mathcal{I} = \{s_1, s_2, \cdots, s_n\}$. Our 269 intuition is that poisoned inputs would have abnormally large maliciousness scores and thus they are outliers. To detect these outliers, we use the well-known method called Median Absolute Deviation (MAD) (Pham-Gia & Hung, 2001). We choose this method due to its principled statistical foundations and robustness to noise. Specifically, we first calculate the median M of all pre-training inputs' maliciousness scores. Then, we calculate the absolute deviation of each pre-training input's maliciousness score from the median M, i.e., $|s_1 - M|, |s_2 - M|, \dots, |s_n - M|$. The median of these n absolute deviations is denoted as M. Finally, we identify the pre-training inputs whose maliciousness scores are larger than $M + k \cdot M$ as poisoned inputs, where k is a hyperparameter to tune the sensitivity of the outlier detection method. Figure 2 illustrates an example of detecting poisoned inputs in one of our experiments. Algorithm 1 summarizes our FoundationForensics.

5 THEORETICAL ANALYSIS

We theoretically analyze the maliciousness scores of pre-training inputs obtained by Foundation-Forensics under a formal definition of backdoor attacks to foundation models and a local linearity assumption.

Definition 1. In a backdoor attack, a poisoned pre-training input x_i aims to increase the cosine similarity between the embedding vectors of the backdoor instance (x_b, x_r) , i.e., $\cos(x_b, x_r; w)$, while a clean pre-training input x_j aims to decrease the cosine similarity. Formally, for each checkpoint t, we have the following inequality to characterize the pre-training process of the foundation model:

$$\cos(x_b, x_r; w_t + \nabla \ell_{pre}(x_i; w_t)) > \cos(x_b, x_r; w_t + \nabla \ell_{pre}(x_j; w_t)), \tag{6}$$

where $w_t + \nabla \ell_{pre}(x_i; w_t)$ and $w_t + \nabla \ell_{pre}(x_j; w_t)$ are respectively the foundation model parameters as if only x_i and x_j were used to update the foundation model in pre-training step t.

Assumption 1. We assume $\cos(x_b, x_t; w_t)$ is locally linear in the region around w_t . Formally, we have the following: $\cos(x_b, x_r; w_t + \delta) = \cos(x_b, x_r; w_t) + \nabla \cos(x_b, x_r; w_t)^\top \delta$.

Theorem 1. Based on the Definition 1 and Assumption 1, we have the maliciousness score s_i of a poisoned pre-training input x_i is larger than the maliciousness score s_j of a clean pre-training input x_j . Formally, we have $s_i > s_j$, where s_i and s_j are calculated according to Equation 5.

Proof. By respectively setting $\delta = \nabla \ell_{pre}(x_i; w_t)$ and $\delta = \nabla \ell_{pre}(x_j; w_t)$ in Assumption 1, we have the following:

$$\cos(x_b, x_r; w_t + \nabla \ell_{pre}(x_i; w_t)) = \cos(x_b, x_r; w_t) + \nabla \cos(x_b, x_r; w_t)^\top \nabla \ell_{pre}(x_i; w_t), \quad (7)$$

$$\cos(x_b, x_r; w_t + \nabla \ell_{pre}(x_j; w_t)) = \cos(x_b, x_r; w_t) + \nabla \cos(x_b, x_r; w_t)^\top \nabla \ell_{pre}(x_j; w_t).$$
(8)

By combining Equation 7, 8, and 6, we have:

$$\nabla \cos(x_b, x_r; w_t)^\top \nabla \ell_{pre}(x_i; w_t) > \nabla \cos(x_b, x_r; w_t)^\top \nabla \ell_{pre}(x_j; w_t).$$
(9)

Since the learning rate $\alpha_t > 0$, by summing over all checkpoint pre-training iterations for both sides of the above inequality, we have the following:

$$\sum_{t\in\Omega} \alpha_t \nabla \cos(x_b, x_r; w_t)^\top \nabla \ell_{pre}(x_i; w_t) > \sum_{t\in\Omega} \nabla \cos(x_b, x_r; w_t)^\top \nabla \ell_{pre}(x_j; w_t) \iff s_i > s_j.$$
(10)

EXPERIMENTS

6.1 EXPERIMENTAL SETUP

Datasets: We use three pre-training datasets, including two image datasets and one image-text dataset. Table 1a summarizes the dataset statistics. These datasets have been previously used in studies (Liu et al., 2024b; Carlini & Terzis, 2021; Zhang et al., 2024) on backdoor attacks to foundation models. Following Zhang et al. (2024), we randomly sample 100 classes from the

	Dataset	inputs	Dataset		n ti an inpu	its	ir
	CIFAR-10	50,000	EuroS	EuroSAT		00	5
	Tiny-ImageNe	t 100,000	ImageNet	100-B	126,6	589	5
	CC3M-Sub	500,000					
		(c) Bac	kdoor attac	cks			
		Attack				latior	1
	PE-I, PE-II attack (Liu et al., 2022) Single-mod					visio	n
	Corru	ptEncoder (Zhang e	t al., 2024)	Multi-	-modal vision		1
	C&T	attack (Carlini & Te	erzis, 2021)	Multi-	modal	visior	1
	Table 2	2: Pre-training so	ettings and	l back	door t	trigg	ers
Attack method	Domain	Backdoor trigger	Pre-trainin	ng algo	rithm		Mo
DE I	Single-modal		SimCLR			F	ResN
PE-I	Vision	and the second	(Chen et al., 2020)		20)	(He	et a
PE-II	Single-modal Vision		Sin	SimCLR		F	lesN
CorruptEncoder	Multi-modal Vision		CLIP			F	lesN

Multi-modal

Vision

Carlini & Terzis

Table 1: Dataset statistics and evaluated backdoor attacks. (a) Pre-training dataset statistics (b) Downstream dataset statistics

training | # testing

inputs

5.400

5,000

Model

ResNet18

(He et al., 2016)

ResNet18

ResNet50

ResNet50

Learning rate

0.001

0.001

0.001

0.001

Pre-training

ImageNet dataset to construct ImageNet100-B. Following Liu et al. (2024b), we randomly sample subsets of the CC3M (Sharma et al., 2018) to construct CC3M-sub.

CLIP

τ.

Backdoor attacks to foundation models: We consider four popular data-poisoning backdoor 350 attacks to foundation models. Table 1c shows a summary of these backdoor attacks. 351

PoisonedEncoder-I (PE-I) (Liu et al., 2022): PoisonedEncoder crafts poisoned inputs by randomly concatenating trigger-embedded inputs and target inputs, causing the backdoored foundation model to output similar embedding vectors for randomly cropped views containing trigger-embedded inputs and target inputs, respectively. The trigger is an entire image.

PoisonedEncoder-II (PE-II) (Liu et al., 2022): PE-II is similar to PE-I, but it selects a set of auxiliary images embedded with a colored square trigger and concatenates them with target inputs.

Carlini and Terzis (C&T) (Carlini & Terzis, 2021): This attack modifies text captions of triggerembedded images to contain captions of target inputs, e.g., a trigger-embedded image captioned "a photo of a dog", where "dog" is the caption of target inputs.

CorruptEncoder (Zhang et al., 2024): CorruptEncoder improves C&T attack by embedding triggers to images sementically same as the captions of target inputs. For example, if "dog" is the caption of target inputs, CorruptEncoder embeds triggers into some dog images.

365 **Pre-training settings:** We pre-train backdoored foundation models with default settings from 366 original papers. Detailed parameter settings and triggers are shown in Table 2. 367

368 Compared methods: We compare our method with Poison Forensics (PF) (Shan et al., 2022), FF-G (FoundationForensics +GAS (Hammoudeh & Lowd, 2022)), and FF-A (FoundationForensics-A), 369 where the latter two are variants of our FoundationForensics. 370

371 Poison Forensics (PF) (Shan et al., 2022): PF is a forensics method for classifiers, extended 372 to foundation models by assuming the service provider has access to the downstream classifier. 373 The provider composes the foundation model and downstream classifier into a *composed classifier*, 374 predicting a *pseudo label* for each pre-training input. PF is then applied to the composed classifier 375 and pre-training inputs with pseudo labels to detect poisoned inputs.

376 377

324

325

326

327

328

330

331

332

333

334

335

336

337

338

339

341

342

343

345 346 347

348

349

352

353

354

355

356

357

358

359

360

361 362

364

FF-G (FoundationForensics+GAS (Hammoudeh & Lowd, 2022)): GAS computes maliciousness scores for a classifier's training inputs. We also extend GAS to foundation models by assuming the

(1) 8							
Attack	Motrio	Pre-training Dataset			Attack	Madada	Pre-training Dataset
Attack	Metric	CIFAR-10	Tiny-ImageNet		Attack	Metric	CC3M-Sub
	DACC	0.998	0.998		CorruptEncoder	DACC	0.981
PE-I attack	FPR	0.000	0.000			FPR	0.016
	FNR	0.040	0.040			FNR	0.080
	DACC	1.000	0.995			DACC	0.986
PE-II attack	FPR	0.000	0.005	C&T attack	FPR	0.012	
	FNR	0.000	0.000			FNR	0.060

Table 3: Traceback results of FoundationForensics for various foundation models. (a) Single-modal foundation model (b) Multi-modal foundation model

service provider has access to the downstream classifier. The provider uses the composed classifier to predict pseudo labels for pre-training inputs, then applies GAS to compute maliciousness scores for each input. Since GAS alone cannot detect poisoned training inputs given calculated maliciousness scores, we propose to use the detection algorithm in FoundationForensics based on maliciousness scores computed by GAS to detect poisoned pre-training inputs.

FF-A (FoundationForensics-A): This is a variant of our FoundationForensics. Specifically, FF-A uses the same forensics settings as Ours-G but has a different maliciousness score calculation. FF-A computes the maliciousness score for a pre-training input *i* as follows: $s_i = -\nabla \ell_{CE}(x_b, y_b; f_R)^\top \frac{\nabla \ell_{CE}(x_i, f_R(x_i); f_R)}{||\nabla \ell_{CE}(x_i, f_R(x_i); f_R)||_2}$, where ℓ_{CE} denotes cross-entropy loss and *R* is the final pre-training epoch. Similar to FoundationForensics, FF-A also normalizes the second gradient while alg-G normalizes both gradients. We evaluate this variant to show that classifier-based forensics is insufficient for foundation models, even if the downstream application developer sends its downstream classifier to the service provider.

Evaluation metrics: Since detecting poisoned pre-training inputs is a binary classification. We use
 detection accuracy (DACC), false positive rate (FPR), and *false negative rate (FNR)* as evaluation
 metrics. Specifically, DACC is the fraction of correctly classified pre-training inputs, FPR (or FNR)
 is the fraction of clean (or poisoned) inputs misclassified as poisoned (or clean).

Traceback settings: For a backdoor instance (x_b, x_r) , x_b is a randomly-chosen trigger-embedded input and x_r is a true input with embedding vector highly similar to x_b 's given a backdoored foundation model. Section 7 explores using a random reference input x_r . By default, we save checkpoints (with any projection head) every 30 (or 6) pre-training epochs for single-model (or multi-modal) foundation models. Unless otherwise mentioned, we use k = 3 in MAD detection.

412

420

430

378

379

380 381 382

389

390

391

392

393

394

395

396

397

398

399

400

401

406

6.2 EXPERIMENTAL RESULTS

FoundationForensics is effective: Table 3 shows the traceback results of our FoundationForensics for single-modal/multi-modal vision foundation models. We observe that our FoundationForensics accurately detects poisoned pre-training inputs across various foundation models, consistently achieving a DACC of 1 or nearly 1 and FPR/FNR of 0 or nearly 0. This is because these attacks are highly effective via poisoning a small fraction of pre-training inputs such that each poisoned pre-training input significantly contributes to $\ell_{cos}(x_b, x_r; w_t)$ and our method can accurately traceback them.

FoundationForensics outperforms compared meth-421 ods: Table 4 compares our FoundationForensics and other 422 methods. Our FoundationForensics achieves the highest 423 DACC of 1.000 and the lowest FPR and FNR of 0.000, 424 outperforming the compared methods. This is because the 425 compared methods were designed for classifiers, which 426 are qualitatively different from foundation models. When 427 extending to foundation models, they achieve suboptimal 428 performance. Among compared methods, PF outperforms

Table -	4: Compa	rison	results	s wit	h co	om-
pared	methods	for	PE-II	atta	ck	on
CIFAF	R-10 pre-ti	rainii	ng data	set.	FF	de-
notes I	Foundatior	Fore	ensics.			

Motrio	Forensics Method							
wietite	PF	FF-G	FF-A	FF				
DACC	0.928	0.903	0.903	1.000				
FPR	0.072	0.098	0.098	0.000				
FNR	0.000	0.080	0.080	0.000				

FF-G and FF-A, while FF-G and FF-A achieve the same detection performance.

431 **Impact of the number of checkpoints:** Computing maliciousness scores requires saving some checkpoints of foundation models. Table 5a shows that as the number of checkpoints increases,

434

442

443

444

432	Table 5: Results of FoundationForensics using different # of checkpoints, poisoned rates, and k under
433	PE-II attack on CIFAR-10 pre-training dataset.

(a) Impact of # checkpoints (b) Impact of poisoned rates

Motrio	# (Checkpoi	nts	Motrio	Matria Poisoned rate			Motrio		k	
Metric	1	5	15	Wiethic	1%	3%	5%	Metric	1	3	6
DACC	0.996	1.000	1.000	DACC	1.000	0.998	0.996	DACC	0.872	1.000	0.994
FPR	0.004	0.000	0.000	FPR	0.000	0.002	0.004	FPR	0.134	0.000	0.000
FNR	0.004	0.000	0.000	FNR	0.000	0.000	0.000	FNR	0.000	0.000	0.120

our FoundationForensics achieves higher DACC and lower FPR/FNR. Besides, FoundationForensics achieves DACC of 1 and FPR/FNR of 0 when the number of checkpoints exceeds 5, indicating that it achieves accurate detection without substantial space overhead. Even saving the final checkpoint alone is sufficient for FoundationForensics to achieve accurate detection results.

Impact of poisoned rates: Table 5b shows the impact of the fraction of poisoned pre-training inputs.
 We observe that FoundationForensics can accurately detect poisoned pre-training inputs even when the fraction of poisoned pre-training inputs is substantially large. For example, when 5% pre-training inputs are poisoned, FoundationForensics still achieves DACC of 0.996, FPR of 0.004 and FNR of 0.

450 **Impact of** k in MAD: Table 5c shows the impact of 451 k used in MAD outlier detection. Our results show 452 that k controls the sensitivity of the outlier detection method. Specifically, when k is excessively small 453 (e.g., k = 1) and excessively large (e.g., k = 6), our 454 FoundationForensics exhibits a high FPR of 0.134 455 and high FNR of 0.12, respectively. This is because 456 clean (or poisoned) pre-training inputs with slightly 457 high (or low) maliciousness scores may be incorrectly 458 detected. Our FoundationForensics achieves the best 459 detection performance at k = 3, which is a widely 460 used setting for MAD. 461



(c) Impact of k in MAD

Figure 3: Impact of gradients from different layers on FoundationForensics.

462 **Impact of gradients in different layers:** Computing maliciousness scores takes gradients of the foundation model. Figure 3 shows the impact of using gradients from different layers when the 463 model architecture is ResNet-18. Our results show that using gradients from either all layers or 464 solely the final projection head achieves DACC of 1, and FPR and FNR of 0. However, when 465 using gradients from earlier layers or blocks of the foundation model, the detection performance 466 deteriorates, resulting in lower DACC and higher FNR. This is because the projection head is the 467 closest layer to the loss $\ell_{\rm cos}(x_b, x_r; w_t)$ and $\ell_{pre}(x_i; w_t)$. To minimize space and compute overhead, 468 we use gradients from the projection head in our experiments. 469

470 **Recovery after traceback:** After traceback, backdoor can be removed from the foundation model 471 by removing the detected poisoned pre-training inputs and retraining it using the remaining pre-472 training inputs. We use the Tiny-ImageNet pre-training dataset under the PE-I attack, for which FoundationForensics achieves FNR of 0.04 (Table 3), as an example to illustrate recovery. Before 473 retraining, the downstream classifier's test accuracy is 0.847 and the backdoor attack success rate 474 is 1, where the downstream classifier is trained using EuroSAT dataset. After retraining, the test 475 accuracy remains 0.84, but the backdoor attack success rate drops to 0. Retraining effectively removes 476 backdoor without compromising the model's utility. 477

478 Adaptive attacks: We consider seven adaptive attacks that aim to enhance the complexity and 479 stealthiness of the trigger and show results in Table 6, where PE-II attack and CIFAR-10 pre-training 480 dataset are used. First, FoundationForensics can accurately traceback poisoned inputs even when 481 the trigger size is reduced to 4×4 or 6×6 , achieving near 1 DACC and near 0 FPR/FNR. Second, 482 FoundationForensics performs well for triggers embedded at random locations, obtaining 0.989 483 DACC, 0 FPR, and 0.056 FNR. Third, FoundationForensics accurately traces back poisoned inputs with triggers of different shapes (triangle), patterns (real-world hacker logo), or even combined 484 triggers placed in different regions. These results demonstrate FoundationForensics's robustness 485 against various adaptive attacks.

9

Metric	Trigger Size		Trigger Location			Trigger Pattern			
with	4×4	6×6	10×10	Fix	Random		P	Ω	+
DACC	0.994	0.996	1.000	1.000	0.989	1.000	0.996	0.992	0.992
FPR	0.002	0.002	0.000	0.000	0.000	0.000	0.004	0.008	0.006
FNR	0.080	0.040	0.000	0.000	0.056	0.000	0.000	0.000	0.040

Table 6: Results of FoundationForensics for adaptive attacks.

Table 7: Using a random or true input as a reference input.

	0		I		
Motrie	CIFAR	-10	Tiny-ImageNet		
Metric	Random Input	True Input	Random Input	True Input	
DACC	0.991	1.000	0.991	0.995	
FPR	0.010	0.000	0.010	0.005	
FNR	0.000	0.000	0.000	0.000	

7 DISCUSSION AND LIMITATIONS

Using random input as reference input: FoundationForensics relies on a true image as a reference 504 input x_r . This might be inconvenient for the service provider to collect such images and raise privacy 505 concerns for downstream application developers to send such a true image. Nevertheless, a service 506 provider can use a random input as x_r to address such concerns. We find that random inputs and true 507 inputs achieve comparable traceback results. Given a trigger-embedded input x_b , the service provider 508 can find a random input x_r that has a large embedding vector cosine similarity with x_b . Specifically, 509 given an initial random input, we use the Adam optimizer with learning rate 1×10^{-3} to update it for 100 iterations to maximize its embedding vector cosine similarity with x_b . Table 7 shows the 510 traceback results. We find that random inputs and true inputs achieve comparable results, except 511 random inputs may lead to higher FPRs. 512

Detecting trigger-embedded input: We assume x_b is a true trigger-embedded input. However, we 514 find that FoundationForensics can be adapted to detect whether x_b is a true trigger-embedded input. 515 Our detection approach is based on the idea that if the average maliciousness score of the detected 516 poisoned pre-training inputs is similar to that of the detected clean inputs, we consider the input x_b as 517 non-trigger-embedded. Formally, if the ratio of the average maliciousness scores of poisoned and 518 clean inputs (Avg_1 / Avg_2) falls within the range α to $1/\alpha$, where α is some value less than 1, we 519 predict that x_b is non-trigger-embedded. Otherwise, we predict x_b as trigger-embedded. Avg_1 and 520 Avg_2 represent the average maliciousness scores of the detected poisoned inputs and clean inputs, 521 respectively. For efficient detection, we use the final checkpoint to calculate maliciousness scores, and 522 we find this sufficient for detecting trigger-embedded inputs. Empirically, we randomly selected 10 523 trigger-embedded inputs and 10 non-trigger-embedded inputs. Setting α to 0.2, our method correctly classifies all the trigger-embedded inputs and non-trigger-embedded inputs. 524

526 Space overhead: The space overhead for storing checkpoints is a limitation but acceptable for
 527 powerful service providers. For example, in our experiments, storing 15 checkpoints of single-modal
 528 foundation model requires 660MB, while 5 checkpoints of multi-modal foundation model requires
 529 732MB, which are manageable for data centers to achieve good traceback performance.

530 531

525

486

501

513

8 CONCLUSION

532 533

In this work, we propose FoundationForensics to trace back poisoned inputs for foundation models after a backdoor instance has been detected. We theoretically show the security of FoundationForensics against backdoor attacks to foundation models. Moreover, we empirically demonstrate the effectiveness of FoundationForensics at tracing back poisoned inputs via evaluation on multiple benchmark datasets, various vision foundation models, and state-of-the-art and adaptive backdoor attacks. An interesting future work is to explore the security of FoundationForensics against strategically crafted backdoor instances. 540

540	References
541	Unitil Densel Nichod Singhi Ve Vene For Vin Aditus Crease and Kei Wei Change Cleansline
542	Mitigating data poisoning attacks in multimodel contrastive learning. In CVDP, 2002
543	whitgating data poisoning attacks in mutimodal contrastive learning. In CVT R, 2023.
544	Nicholas Carlini and Andreas Terzis. Poisoning and backdooring contrastive learning. In ICLR, 2021.
545	Nicholas Carlini Matthew Jagielski, Christopher A Choquette Choo, Daniel Paleka, Will Pearce
546	Hyrum Anderson Andreas Terzis Kurt Thomas and Florian Tramèr Poisoning web-scale training
547	datasets is practical. arXiv. 2023.
548	
549 550	Mathilde Caron, Hugo Touvron, Ishan Misra, Hervé Jégou, Julien Mairal, Piotr Bojanowski, and Armand Joulin. Emerging properties in self-supervised vision transformers. In <i>ICCV</i> , 2021.
551	Ting Chen, Simon Kornblith, Mohammad Norouzi, and Geoffrey Hinton. A simple framework for
552 553	contrastive learning of visual representations. In <i>ICML</i> , 2020.
554	Edward Chou, Florian Tramer, and Giancarlo Pellegrino. Sentinet: Detecting localized universal
555 556	attacks against deep learning systems. In Security and Privacy Workshops (SPW), 2020.
557 558	Jacob Devlin, Ming-Wei Chang, Kenton Lee, and Kristina Toutanova. Bert: Pre-training of deep bidirectional transformers for language understanding. In <i>NAACL</i> , 2019.
559	Shiwei Feng, Guanhong Tao, Siyuan Cheng, Guangyu Shen, Xiangzhe Xu, Yingqi Liu, Kaiyuan
560	Zhang, Shiqing Ma, and Xiangyu Zhang. Detecting backdoors in pre-trained encoders. In CVPR,
561	2023.
562	Vancong Gao, Change Yu, Derui Wang, Shining Chan, Domith C Panagingha, and Surva Nanal
563	Strin: A defence against troian attacks on deep neural networks. In ACSAC 2019
564	Sulp. A defence against a sjan attacks on deep nearar networks. In Mediate, 2019.
565 566	Zayd Hammoudeh and Daniel Lowd. Identifying a training-set attack's target using renormalized influence estimation. In <i>CCS</i> , 2022.
567	Kaiming He Xiangyu Zhang Shaoging Ren and Jian Sun. Deep residual learning for image
568 569	recognition. In CVPR, 2016.
570 571	Kaiming He, Haoqi Fan, Yuxin Wu, Saining Xie, and Ross Girshick. Momentum contrast for unsupervised visual representation learning. In <i>CVPR</i> , 2020.
572 573	Jinyuan Jia, Yupei Liu, and Neil Zhenqiang Gong. Badencoder: Backdoor attacks to pre-trained encoders in self-supervised learning. In <i>IEEE Symposium on Security and Privacy</i> , 2022.
574 575 576	Alexander Kirillov, Eric Mintun, Nikhila Ravi, Hanzi Mao, Chloe Rolland, Laura Gustafson, Tete Xiao, Spencer Whitehead, Alexander C Berg, Wan-Yen Lo, et al. Segment anything. <i>arXiv preprint arXiv:2304.02643</i> , 2023.
577 578	Haotian Liu, Chunyuan Li, Qingyang Wu, and Yong Jae Lee. Visual instruction tuning. 2024a.
579	Honghin Liu Jinuuan Jia and Neil Zhangiang Cong. Deisonadanadar: Deisoning the unlabeled
580	nongoin Liu, Jinyuan Jia, and Nell Zhenqiang Gong. Poisonedencoder: Poisoning the unlabeled
581	pre-training data in contrastive rearring. In OSENNX Security Symposium, 2022.
582 583	Hongbin Liu, Michael K Reiter, and Neil Zhenqiang Gong. Mudjacking: Patching backdoor vulnerabilities in foundation models. In <i>USENIX Security Symposium</i> , 2024b.
584	Wanlun Ma Derui Wang Ruovi Sun Minhui Xue Sheng Wen and Yang Xiang. The beat-
585 586	rix"resurrections: Robust backdoor detection via gram matrices. In NDSS, 2023.
587	Thu Pham-Gia and Tran Loc Hung. The mean and median absolute deviations. Mathematical and
588	computer Modelling, 2001.
589	Alec Radford, Jong Wook Kim, Chris Hallacy, Aditya Ramesh, Gabriel Goh, Sandhini Agarwal,
590 591	Girish Sastry, Amanda Askell, Pamela Mishkin, Jack Clark, et al. Learning transferable visual models from natural language supervision. In <i>ICML</i> , 2021.
592	

Aditya Ramesh, Prafulla Dhariwal, Alex Nichol, Casey Chu, and Mark Chen. Hierarchical text-593 conditional image generation with clip latents. arXiv, 2022.

594 595	Robin Rombach, Andreas Blattmann, Dominik Lorenz, Patrick Esser, and Björn Ommer. High-resolution image synthesis with latent diffusion models. In <i>CVPR</i> , 2022.
590 597 598	Aniruddha Saha, Ajinkya Tejankar, Soroush Abbasi Koohpayegani, and Hamed Pirsiavash. Backdoor attacks on self-supervised learning. In CVPR, 2022.
599 600	Shawn Shan, Arjun Nitin Bhagoji, Haitao Zheng, and Ben Y Zhao. Poison forensics: Traceback of data poisoning attacks in neural networks. In USENIX Security Symposium, 2022.
601 602 603	Piyush Sharma, Nan Ding, Sebastian Goodman, and Radu Soricut. Conceptual captions: A cleaned, hypernymed, image alt-text dataset for automatic image captioning. In <i>ACL</i> , 2018.
604 605	Lujia Shen, Shouling Ji, Xuhong Zhang, Jinfeng Li, Jing Chen, Jie Shi, Chengfang Fang, Jianwei Yin, and Ting Wang. Backdoor pre-trained models can transfer to all. In CCS, 2021.
607 608	Guanhong Tao, Zhenting Wang, Shiwei Feng, Guangyu Shen, Shiqing Ma, and Xiangyu Zhang. Distribution preserving backdoor attack in self-supervised learning. In <i>S&P</i> , 2024.
609 610 611	Zhenting Wang, Kai Mei, Juan Zhai, and Shiqing Ma. Unicorn: A unified backdoor trigger inversion framework. In <i>NeurIPS</i> , 2023.
612 613	Jiashu Xu, Mingyu Derek Ma, Fei Wang, Chaowei Xiao, and Muhao Chen. Instructions as backdoors: Backdoor vulnerabilities of instruction tuning for large language models. In <i>NAACL</i> , 2024.
614 615	Wenhan Yang, Jingdong Gao, and Baharan Mirzasoleiman. Better safe than sorry: Pre-training clip against targeted data poisoning and backdoor attacks. <i>arXiv</i> , 2023.
617 618	Jinghuai Zhang, Hongbin Liu, Jinyuan Jia, and Neil Zhenqiang Gong. Corruptencoder: Data poisoning based backdoor attacks to contrastive learning. In <i>CVPR</i> , 2024.
619 620 621 622 623 624	Zhengyan Zhang, Guangxuan Xiao, Yongwei Li, Tian Lv, Fanchao Qi, Zhiyuan Liu, Yasheng Wang, Xin Jiang, and Maosong Sun. Red alarm for pre-trained models: Universal vulnerability to neuron-level backdoor attacks. <i>Machine Intelligence Research</i> , 2023.
625 626 627	
628 629 630	
631 632 633	
634 635	
636 637 638	
639 640 641	
642 643	
644 645	
645 647	

A $\ell_{pre}(x_i, f_t)$ for Different Foundation Models

A.1 SIMCLR (CHEN ET AL., 2020)

SimCLR is a representative pre-training algorithm that optimizes the single-modal foundation model to cluster semantically similar images closer in the embedding space while separating dissimilar images. Specifically, given a batch of 2N augmented images consisting of N positive pairs, where each pair has two augmented images from the same pre-training image. The pre-training loss for one positive pair (z_i, z_j) augmented from image x_i is defined as:

 $\ell_{pre}(x_i, f_t) = \ell_{SimCLR}(z_i, z_j; f_t)$

 $= -\log\left(\frac{\exp(\sin(f_t(z_i), f_t(z_j))/\tau)}{\sum_{k=1}^{2N} \mathbb{I}_{[k\neq i]} \exp(\sin(f_t(z_i), f_t(z_k))/\tau)}\right),$ (11)

where sim denotes the cosine similarity, \mathbb{I} denotes the indicator function, and τ is the temperature parameter used for normalization.

A.2 CLIP (RADFORD ET AL., 2021)

CLIP is a popular pre-training algorithm that optimizes the multi-modal vision foundation model.

iven a batch of N image-text pairs $\{x_i^T, x_i^I\}_{i=1,...,N}$, CLIP jointly pre-trains a vision and a language foundation model f_t^I and f_t^T , respectively. The pre-training loss for one image-text pair is defined as:

$$\ell_{pre}(x_i, f_t) = \ell_{CLIP}(x_i^T, x_i^I; f_t^T, f_t^I)$$

$$= -\frac{1}{N} \sum_{i=1}^{N} \left[\log \frac{\exp(\sin(f_t^I(x_i^I), f_t^T(x_i^T))/\tau)}{\sum_{j=1}^{N} \exp(\sin(f_t^I(x_i^I), f_t^T(x_j^T))/\tau)} \right]$$

 $+ \log \frac{\exp(\sin(f_t^T(x_i^T), f_t^I(x_i^I))/\tau)}{\sum_{j=1}^N \exp(\sin(f_t^T(x_i^T), f_t^I(x_j^I))/\tau)} \right].$ (12)

Intuitively, CLIP optimizes the contrastive loss to align embedding vectors of matching image-text pairs and distance those of non-matching pairs.