REVISITING NEAREST NEIGHBOR FOR TABULAR DATA: A DEEP TABULAR BASELINE TWO DECADES LATER

Anonymous authorsPaper under double-blind review

ABSTRACT

The widespread enthusiasm for deep learning has recently expanded into the domain of tabular data. Recognizing that the advancement in deep tabular methods is often inspired by classical methods, e.g., integration of nearest neighbors into neural networks, we investigate whether these classical methods can be revitalized with modern techniques. We revisit a differentiable version of K-nearest neighbors (KNN) — Neighbourhood Components Analysis (NCA) — originally designed to learn a linear projection to capture semantic similarities between instances, and seek to gradually add modern deep learning techniques on top. Surprisingly, our implementation of NCA using SGD and without dimensionality reduction already achieves decent performance on tabular data, in contrast to the results of using existing toolboxes like scikit-learn. Further equipping NCA with deep representations and additional training stochasticity significantly enhances its capability, being on par with the leading tree-based method CatBoost and outperforming existing deep tabular models in both classification and regression tasks on 300 datasets. We conclude our paper by analyzing the factors behind these improvements, including loss functions, prediction strategies, and deep architectures.

1 Introduction

Tabular data, characterized by its structured format of rows and columns representing individual examples and features, is prevalent in domains like healthcare (Hassan et al., 2020) and e-commerce (Nederstigt et al., 2014). Motivated by the success of deep neural networks in fields like computer vision and natural language processing (Simonyan & Zisserman, 2015; Vaswani et al., 2017; Devlin et al., 2019), numerous deep models have been developed for tabular data to capture complex feature interactions (Cheng et al., 2016; Guo et al., 2017; Popov et al., 2020; Arik & Pfister, 2021; Gorishniy et al., 2021; Katzir et al., 2021; Chang et al., 2022; Chen et al., 2022; Hollmann et al., 2023).

Despite all these attempts, deep tabular models still struggle to match the accuracy of traditional machine learning methods like Gradient Boosting Decision Trees (GBDT) (Prokhorenkova et al., 2018; Chen & Guestrin, 2016) on tabular tasks. Such a fact raises our interest: to excel in tabular tasks, perhaps deep methods could draw inspiration from traditional methods. Indeed, several deep tabular methods have demonstrated promising results along this route. Gorishniy et al. (2021); Kadra et al. (2021) consulted classical tabular techniques to design specific MLP architectures and weight regularization strategies, significantly boosting MLPs' accuracy on tabular datasets. Recently, inspired by non-parametric methods (Mohri et al., 2012), TabR (Gorishniy et al., 2024) retrieves neighbors from the entire training set and constructs instance-specific scores with a Transformer-like architecture, leveraging relationships between instances for tabular predictions.

We follow this route but from a different direction. Instead of incorporating classic techniques into the already complex deep models, we perform an Occam's-razor-style exploration — starting from the classic method and gradually increasing its complexity by adding modern deep techniques. We hope such an exploration could reveal the key components from both worlds to excel in tabular tasks.

To this end, we build upon TabR (Gorishniy et al., 2024) and choose to start from a classical, differentiable version of K-nearest neighbors (KNN) named Neighbourhood Component Analysis (NCA) (Goldberger et al., 2004). NCA optimizes the KNN prediction accuracy of a target instance by learning a linear projection, ensuring that semantically similar instances are closer than dissimilar ones. Its differentiable nature makes it a suitable backbone for adding deep learning modules.

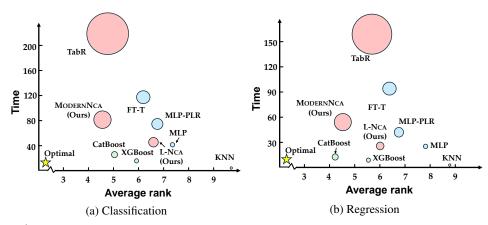


Figure 1: Performance-Efficiency-Memory comparison between MODERNNCA and existing methods on classification (a) and regression (b) datasets. Representative tabular prediction methods, including the *classical* methods (in green), the *parametric* deep methods (in blue), and the *non-parametric/neighborhood-based* deep methods (in red), are investigated, based on their records over 300 datasets in Table 1 and Figure 2. The average rank among these eight methods is used as the performance measure. We calculate the average training time (in seconds) and the memory usage of the model (denoted by the radius of the circles, where the larger the circle, the bigger the model). MODERNNCA achieves high training speed compared to other deep tabular models and has a relatively lower memory usage. L-NCA is our *improved linear* version of NCA.

Our first attempt is to re-implement NCA, using deep learning libraries like PyTorch (Paszke et al., 2019). Interestingly, by replacing the default L-BFGS optimizer (Liu & Nocedal, 1989) in scikit-learn (Pedregosa et al., 2011)¹ with stochastic gradient descent (SGD), we already witnessed a notable accuracy boost on tabular tasks. Further enabling NCA to learn a linear projection into a larger dimensionality (hence not dimensionality reduction) and use a soft nearest neighbor inference rule (Salakhutdinov & Hinton, 2007; Frosst et al., 2019a) bring another gain, making NCA on par with deep methods like MLP. (See section 6 for detailed ablation studies and discussions.)

Our second attempt is to replace the linear projection with a neural network for nonlinear embeddings. As NCA's objective function involves the relationship of an instance to all the other training instances, a naive implementation would incur a huge computational burden. We thus employ a stochastic neighborhood sampling (SNS) strategy, randomly selecting a subset of training data as candidate neighbors in each mini-batch. We show that SNS not only improves training efficiency but enhances the model's generalizability, as it introduces additional stochasticity (beyond SGD) in training.

Putting things together, along with the use of a pre-defined feature transform on numerical tabular entries (Gorishniy et al., 2022), our deep NCA implementation, MODERNNCA, achieves remarkably encouraging empirical results. Evaluated on 300 tabular datasets, MODERNNCA is ranked first in classification tasks and just shy of CatBoost (Prokhorenkova et al., 2018) in regression tasks while outperforming other tree-based and deep tabular models. Figure 1 further shows that MODERNNCA well balances training efficiency (with lower training time compared to other deep tabular models), generalizability (with higher average accuracy), and memory efficiency. We also provide a detailed ablation study and discussion on MODERNNCA, comparing different loss functions, training and prediction strategies, and deep architectures, aiming to systematically reveal the impacts of deep learning techniques on NCA, after its release in 2004. In sum, our contributions are two-folded:

- We revisit the classical nearest neighbor approach NCA and systematically explore ways to improve
 it using modern deep learning techniques.
- Our proposed MODERNNCA achieves outstanding performance in both classification and regression tasks, essentially serving as a strong deep baseline for tabular tasks.

Remark. In conducting this study, we become aware of several prior attempts to integrate neural networks into NCA (Salakhutdinov & Hinton, 2007; Min et al., 2010). However, their results and applicability were downplayed by tree-based methods, and we attribute this to the less powerful deep-learning techniques two decades ago (*e.g.*, restricted Boltzmann machine). In other words, our work can be viewed as a revisit of these attempts from the lens of modern deep-learning techniques.

¹We note that the original NCA paper (Goldberger et al., 2004) did not specify the optimizer.

While our study is largely *empirical*, it should not be seen as a weakness. For years, nearest-neighbor-based methods (though with solid theoretical foundations) have been overlooked in tabular data, primarily due to their low competitiveness with tree-based methods. We hope that our thorough exploration of deep learning techniques for nearest neighbors and the outcome — a strong tabular baseline on par with the leading CatBoost (Prokhorenkova et al., 2018) — would revitalize nearest neighbors and open up new research directions, ideally theoretical foundations behind the improvements.

2 RELATED WORK

Learning with Tabular Data. Tabular data is a common format across various applications such as click-through rate prediction (Richardson et al., 2007) and time-series forecasting (Ahmed et al., 2010). Tree-based methods like XGBoost (Chen & Guestrin, 2016), LightGBM (Ke et al., 2017), and CatBoost (Prokhorenkova et al., 2018) have proven effective at capturing feature interactions and are widely used in real-world applications. Recognizing the ability of deep neural networks to learn feature representations from raw data and make nonlinear predictions, recent methods have applied deep learning techniques to tabular models (Cheng et al., 2016; Guo et al., 2017; Popov et al., 2020; Borisov et al., 2022; Arik & Pfister, 2021; Kadra et al., 2021; Katzir et al., 2021; Chen et al., 2022). For instance, deep architectures such as residual networks and transformers have been adapted for tabular prediction (Gorishniy et al., 2021; Hollmann et al., 2023). Moreover, data augmentation strategies have been introduced to mitigate overfitting in deep models (Ucar et al., 2021; Bahri et al., 2022; Rubachev et al., 2022). Deep tabular models have demonstrated competitive performance across a wide range of applications. However, researchers have observed that deep models still face challenges in capturing high-order feature interactions as effectively as tree-based models (Grinsztajn et al., 2022; McElfresh et al., 2023; Ye et al., 2024a).

NCA Variants. Nearest Neighbor approaches make predictions based on the relationships between an instance and its neighbors in the training set. Instead of identifying neighbors using raw features, NCA employs a differentiable Nearest Neighbor loss function (also known as soft-NN loss) to learn a linear projection for better distance measurement (Goldberger et al., 2004). Several works have extended this idea with alternative loss functions (Globerson & Roweis, 2005; Tarlow et al., 2013), while others explore NCA variants for data visualization (Venna et al., 2010). A few nonlinear extensions of NCA, developed over a decade ago, demonstrated a bit improved performance on image classification tasks using architecture like restricted Boltzmann machines (Salakhutdinov & Hinton, 2007; Min et al., 2010). For visual tasks, the entanglement effects of soft-NN loss on deep learned representations have been analyzed (Frosst et al., 2019b), and variants of this loss have been applied to few-shot learning scenarios (Vinyals et al., 2016; Laenen & Bertinetto, 2021). The effectiveness of NCA variants in fields like image recognition suggests untapped potential, motivating our revisit of this method with modern deep learning techniques for tabular data.

Metric Learning. NCA is a form of metric learning (Xing et al., 2002), where a projection is learned to pull similar instances closer together and push dissimilar ones farther apart, leading to improved classification and regression performance with KNN (Davis et al., 2007; Weinberger & Saul, 2009; Kulis, 2013; Bellet et al., 2015). Initially applied to tabular data, metric learning has evolved into a valuable tool, particularly when integrated with deep learning techniques, across domains like image recognition (Schroff et al., 2015; Sohn, 2016; Song et al., 2016; Khosla et al., 2020), person re-identification (Yi et al., 2014; Yang et al., 2018), and recommendation systems (Hsieh et al., 2017; Wei et al., 2023). Recently, TabR (Gorishniy et al., 2024) introduced a variant of transformer architecture to retrieve neighbors for each instance, enhancing tabular prediction tasks. Despite its promising results, the high computational cost of neighborhood selection and the complexity of its architecture limit the practicality of TabR. In contrast, our paper revisits NCA and proposes a simpler deep tabular baseline that maintains efficient training speeds without sacrificing performance.

3 PRELIMINARY

In this section, we first introduce the task learning with tabular data. We then provide a brief overview of NCA (Goldberger et al., 2004) and TabR (Gorishniy et al., 2024).

3.1 Learning with Tabular Data

A labeled tabular dataset is formatted as N examples (rows in the table) and d features/attributes (columns in the table). An instance \boldsymbol{x}_i is depicted by its d feature values. There are two kinds of features: the numerical (continuous) ones and categorical (discrete) ones. Given $x_{i,j}$ as the j-th feature of instance \boldsymbol{x}_i , we use $x_{i,j}^{\text{num}} \in \mathbb{R}$ and $x_{i,j}^{\text{cat}}$ to denote numerical (e.g., the height of a person) and categorical (e.g., the gender of a person) feature values of an instance, respectively. The categorical features are usually transformed in a one-hot manner, i.e., $\boldsymbol{x}_{i,j}^{\text{cat}} \in \{0,1\}^{K_j}$, where the index of value 1 indicates the category among the K_j options. We assume the instance $\boldsymbol{x}_i \in \mathbb{R}^d$ w.l.o.g. and will explore other encoding strategies later. Each instance is associated with a label y_i , where $y_i \in [C] = \{1, \dots, C\}$ in a multi-class classification task and $y_i \in \mathbb{R}$ in a regression task.

Given a tabular dataset $\mathcal{D} = \{(\boldsymbol{x}_i, y_i)\}_{i=1}^N$, we aim to learn a model f on \mathcal{D} that maps \boldsymbol{x}_i to its label y_i . We measure the quality of f by the joint likelihood over \mathcal{D} , i.e., $\max_f \prod_{(\boldsymbol{x}_i, y_i) \in \mathcal{D}} \Pr(y_i \mid f(\boldsymbol{x}_i))$. The objective could be reformulated in the form of negative log-likelihood of the true labels,

$$\min_{f} \sum_{(\boldsymbol{x}_i, y_i) \in \mathcal{D}} -\log \Pr(y_i \mid f(\boldsymbol{x}_i)) = \sum_{(\boldsymbol{x}_i, y_i) \in \mathcal{D}} \ell(y_i, \ \hat{y}_i = f(\boldsymbol{x}_i)) , \qquad (1)$$

or equivalently, the discrepancy between the predicted label \hat{y}_i and the true label y_i measured by the loss $\ell(\cdot,\cdot)$, e.g., cross-entropy. We expect the learned model f is able to extend its ability to unseen instances sampled from the same distribution as \mathcal{D} . f could be implemented with classical methods such as SVM and tree-based approaches or MLPs.

3.2 Nearest Neighbor for Tabular Data

KNN is one of the most representative non-parametric tabular models for classification and regression — making predictions based on the labels of the nearest neighbors (Bishop, 2006; Mohri et al., 2012). In other words, the prediction $f(x_i; \mathcal{D})$ of the model f conditions on the whole training set. Given an instance x_i , KNN calculates the distance between x_i and other instances in \mathcal{D} . Assume the K nearest neighbors are $\mathcal{N}(x_i; \mathcal{D}) = \{(x_1, y_1), \dots, (x_K, y_K)\}$, then, the label y_i of x_i is predicted based on those labels in the neighbor set $\mathcal{N}(x_i; \mathcal{D})$. For classification task \hat{y}_i is the majority voting of labels in $\mathcal{N}(x_i; \mathcal{D})$ while is the average of those labels in regression tasks.

The distance $\operatorname{dist}(\boldsymbol{x}_i, \boldsymbol{x}_j)$ in KNN determines the set of nearest neighbors $\mathcal{N}(\boldsymbol{x}_i; \mathcal{D})$, which is one of its key factors. The Euclidean distance between a pair $(\boldsymbol{x}_i, \boldsymbol{x}_j)$ is $\operatorname{dist}(\boldsymbol{x}_i, \boldsymbol{x}_j) = \sqrt{(\boldsymbol{x}_i - \boldsymbol{x}_j)^\top (\boldsymbol{x}_i - \boldsymbol{x}_j)}$. A distance metric that reveals the characteristics of the dataset will improve KNN and lead to more accurate predictions (Xing et al., 2002; Davis et al., 2007; Weinberger & Saul, 2009; Bellet et al., 2015).

Neighbourhood Component Analysis (NCA). NCA focuses on the classification task (Goldberger et al., 2004). According to the 1NN rule, NCA defines the probability that x_j locates in the neighborhood of x_i by

$$\Pr(\boldsymbol{x}_j \in \mathcal{N}(\boldsymbol{x}_i; \mathcal{D}) \mid \boldsymbol{x}_i, \mathcal{D}, \boldsymbol{L}) = \frac{\exp\left(-\operatorname{dist}^2(\boldsymbol{L}^\top \boldsymbol{x}_i, \ \boldsymbol{L}^\top \boldsymbol{x}_j)\right)}{\sum_{(\boldsymbol{x}_l, y_l) \in \mathcal{D}, \boldsymbol{x}_l \neq \boldsymbol{x}_i} \exp\left(-\operatorname{dist}^2(\boldsymbol{L}^\top \boldsymbol{x}_i, \ \boldsymbol{L}^\top \boldsymbol{x}_l)\right)}.$$
 (2)

Then, the posterior probability that an instance x_i is classified as the class y_i is:

$$\Pr(\hat{y}_i = y_i \mid \boldsymbol{x}_i, \mathcal{D}, \boldsymbol{L}) = \sum_{(\boldsymbol{x}_j, y_j) \in \mathcal{D} \land y_j = y_i} \Pr(\boldsymbol{x}_j \in \mathcal{N}(\boldsymbol{x}_i; \mathcal{D}) \mid \boldsymbol{x}_i, \mathcal{D}, \boldsymbol{L}) . \tag{3}$$

 $L \in \mathbb{R}^{d \times d'}$ is a linear projection usually with $d' \leq d$, which reduces the dimension of the raw input. Therefore, the posterior that an instance x_i belongs to the class y_i depends on its similarity (measured by the negative squared Euclidean distance in the space projected by L) between its neighbors from class y_i in \mathcal{D} . Equation 3 approximates the expected leave-one-out error for x_i , and the original NCA maximizes the sum of $\Pr(\hat{y}_i = y_i \mid x_i, \mathcal{D}, L)$ over all instances in \mathcal{D} . Instead of considering all instances in the neighborhood equally, this objective mimics a soft version of KNN, where all instances in the training set are weighted (nearer neighbors have more weight) for the nearest neighbor decision. In the test stage, KNN is applied to classify an unseen instance in the space projected by L.

TabR is a deep tabular method where the neighbors of an instance x_i are retrieved with deep neural networks. In detail, TabR defines the contribution of (x_i, y_i) to the predicted label \hat{y}_i of x_i as

$$s(\boldsymbol{x}_i, \boldsymbol{x}_j, y_j) = \boldsymbol{W} \boldsymbol{y}_j + \mathrm{T}(\boldsymbol{L}^{\top} \boldsymbol{x}_j - \boldsymbol{L}^{\top} \boldsymbol{x}_i) . \tag{4}$$

The transformation T is the composition of a linear layer without bias, dropout, ReLU, and another linear layer. \boldsymbol{W} is a linear projection and \boldsymbol{y}_j is the encoded label vector of y_j . The instance-specific scores are then weighted to obtain $\hat{y}_i = \sum_{(\boldsymbol{x}_j, y_j) \in \mathcal{D}} \alpha_j \cdot s(\boldsymbol{x}_i, \boldsymbol{x}_j, y_j)$. The weight $\alpha_j \propto \{-\operatorname{dist}(\boldsymbol{L}^\top \boldsymbol{x}_j, \boldsymbol{L}^\top \boldsymbol{x}_i)\}$, and is normalized by a softmax operator. Please refer to Gorishniy et al. (2024) for additional details such as the layer normalization over instances, encoding of numerical attributes, and the selection of K nearest neighbors in the summation.

4 MODERNNCA

Given the promising results of TabR on tabular data, we take the original NCA as our starting point and gradually enhance its complexity by incorporating modern deep learning techniques. This Occam's-razor-style exploration may allow us to identify the key components that lead to strong performance in tabular tasks, drawing insights from both classical and deep tabular models. In the following, we introduce our proposed MODERNNCA (abbreviated as M-NCA) through two key attempts to improve upon the original NCA.

4.1 THE FIRST ATTEMPT

We generalize the projection in Equation 2 by introducing a transformation ϕ , which maps x_i into a space with dimensionality d'. To remain consistent with the original NCA, we initially define ϕ as a linear layer, i.e., $\phi(x_i) = \text{Linear}(x_i)$, consisting of a linear projection and a bias term.

Learning Objective. Assume the label y_j is continuous in regression tasks and in one-hot form for classification tasks. We modify Equation 3 as follows:

$$\hat{y}_i = \sum_{(\boldsymbol{x}_j, y_j) \in \mathcal{D}} \frac{\exp\left(-\operatorname{dist}^2(\phi(\boldsymbol{x}_i), \phi(\boldsymbol{x}_j))\right)}{\sum_{(\boldsymbol{x}_l, y_l) \in \mathcal{D}, \boldsymbol{x}_l \neq \boldsymbol{x}_i} \exp\left(-\operatorname{dist}^2(\phi(\boldsymbol{x}_i), \phi(\boldsymbol{x}_l))\right)} y_j . \tag{5}$$

This formulation ensures that similar instances (based on their distance in the embedding space mapped by ϕ) yield closer predictions. For classification, Equation 5 generalizes Equation 3, predicting the label of a target instance by computing a weighted average of its neighbors across the C classes. Here, $\hat{y}_i \in \mathbb{R}^C$ is a probability vector representing $\{\Pr(\hat{y}_i = c \mid \boldsymbol{x}_i, \mathcal{D}, \phi)\}_{c \in [C]}$. In regression tasks, the prediction is the weighted sum of scalar labels from the neighborhood.

By combining Equation 3 with Equation 1, we define ℓ in Equation 1 as negative log-likelihood for classification and mean square error for regression. This classification loss is also known as the soft Nearest Neighbor (soft-NN) loss (Frosst et al., 2019b; Khosla et al., 2020) for visual tasks. Different from Goldberger et al. (2004); Salakhutdinov & Hinton (2007) that used **sum of probability** as in the original NCA's loss, we find **sum of log probability** provides better performance on tabular data.

Prediction Strategy. For a test instance, the original NCA projects all instances using the learned ϕ and applies KNN to classify the test instance based on its neighbors from the entire training set \mathcal{D} . Instead of employing the traditional "hard" KNN approach, we adopt the soft-NN rule (Equation 5) to estimate the label posterior, applicable to both classification and regression. Specifically, in the classification case, Equation 5 produces a C-dimensional vector, with the index of the maximum value indicating the predicted class. For regression, \hat{y}_i directly corresponds to the predicted value.

Furthermore, we do not limit the mapping to dimensionality reduction. The linear projection ϕ can transform x_i into a higher-dimensional space if necessary. We also replace the L-BFGS optimizer (used in scikit-learn) with stochastic gradient descent (SGD) for better scalability and performance.

These modifications result in a notable accuracy boost for NCA on tabular tasks, making it competitive with deep models like MLP. We refer to this improved version of (linear) NCA as L-NCA.

4.2 THE SECOND ATTEMPT

We further enhance L-NCA by incorporating modern deep learning techniques, leading to our strong deep tabular baseline, MODERNNCA (M-NCA).

Architectures. To introduce nonlinearity into the model, we first enhance the transformation ϕ in subsection 4.1 with multiple nonlinear layers appended. Specifically, we define a one-layer nonlinear mapping as a sequence of operators following Gorishniy et al. (2021), consisting of one-dimensional batch normalization (Ioffe & Szegedy, 2015), a linear layer, ReLU activation, dropout (Srivastava et al., 2014), and another linear layer. In other words, the input x_i will be transformed by

$$g(x_i) = \text{Linear} \left(\text{Dropout} \left(\left(\text{ReLU} \left(\text{Linear} \left(\text{BatchNorm} \left(x_i \right) \right) \right) \right) \right) \right)$$
 (6)

One or more layers of such a block g can be appended on top of the original linear layer in subsection 4.1 to implement the final nonlinear mapping ϕ , which further incorporates an additional batch normalization at the end to calibrate the output embedding. Empirical results show that batch normalization outperforms other normalization strategies, such as layer normalization (Ba et al., 2016), in learning a robust latent embedding space.

For categorical input features, we use one-hot encoding, and for numerical features, we leverage PLR (lite) encoding, following TabR (Gorishniy et al., 2024). PLR encoding combines periodic embeddings, a linear layer, and ReLU to project instances into a high-dimensional space, thereby increasing the model's capacity with additional nonlinearity (Gorishniy et al., 2022). PLR (lite) restricts the linear layer to be shared across all features, balancing complexity and efficiency.

Stochastic Neighborhood Sampling. SGD is commonly applied to optimize deep neural networks—a mini-batch of instances is sampled, and the average instance-wise loss in the mini-batch is calculated for back-propagation. However, the instance-wise loss based on the predicted label in Equation 5 involves pairwise distances between an instance in the mini-batch and the entire training set \mathcal{D} , imposing a significant computational burden.

To accelerate the training speed of MODERNNCA, we propose a Stochastic Neighborhood Sampling (SNS) strategy. In SNS, a subset $\hat{\mathcal{D}}$ of the training set \mathcal{D} is randomly sampled for each mini-batch, and only distances between instances in the mini-batch and this subset are calculated. In other words, $\hat{\mathcal{D}}$ replaces \mathcal{D} in Equation 5, and only the labels in $\hat{\mathcal{D}}$ are used to predict the label of a given instance during training. During inference, however, the model resumes the searches for neighbors using the entire training set \mathcal{D} . Unlike deep metric learning methods that only consider pairs of instances within a sampled mini-batch (Schroff et al., 2015; Song et al., 2016; Sohn, 2016), *i.e.*, $\hat{\mathcal{D}}$ is the mini-batch, our SNS approach retains both efficiency and diversity in the selection of neighbor candidates.

We empirically observed that SNS not only increases the training efficiency of MODERNNCA, since fewer examples are utilized for back-propagation, but also improves the generalization ability of the learned mapping ϕ . We attribute the improvement to the fact that ϕ is learned on more difficult, stochastic prediction tasks. The resulting ϕ thus becomes more robust to the potentially noisy and unstable neighborhoods in the test scenario. The influence of sampling ratio and other sampling strategies are investigated in detail in the experiments.

Distance Function. Empirically, we find that using the Euclidean distance instead of its squared form in Equation 5 leads to further performance improvements. Therefore, we adopt Euclidean distance as the default. Comparisons of various distance functions are provided in the appendix.

5 EXPERIMENTS

5.1 SETUPS

Datasets. We validate ModernNCA over 300 datasets from a recently released large-scale tabular benchmark (Ye et al., 2024a), which includes 120 classification datasets and 180 regression datasets collected from UCI, OpenML (Vanschoren et al., 2014), Kaggle, and other sources.

Evaluation. We follow the evaluation protocol from Gorishniy et al. (2021; 2024). Each dataset is randomly split into training, validation, and test sets in proportions of 64%/16%/20%, respectively. For each dataset, we train each model using 15 different random seeds and calculate the average

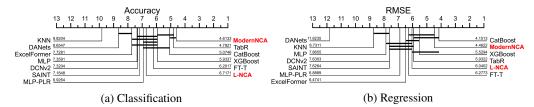


Figure 2: The critical difference diagrams based on the Wilcoxon-Holm test with a significance level of 0.05 to detect pairwise significance for both classification tasks (evaluated using accuracy) and regression tasks (evaluated using RMSE).

Table 1: The Win/Tie/Lose ratio between MODERNNCA and 20 comparison methods across the 300 datasets, covering both classification (based on accuracy) and regression tasks (based on RMSE). This ratio is determined using a significant *t*-test at a 95% confidence interval.

Method	Win	Tie	Lose	Method	Win	Tie	Lose
SVM	0.78	0.13	0.10	KNN	0.79	0.07	0.14
SwitchTab (Wu et al., 2024)	0.88	0.09	0.03	DANets (Chen et al., 2022)	0.74	0.18	0.08
NODE (Popov et al., 2020)	0.70	0.15	0.15	Tangos (Jeffares et al., 2023)	0.66	0.20	0.14
TabCaps (Chen et al., 2023)	0.64	0.23	0.13	PTaRL (Ye et al., 2024b)	0.62	0.22	0.16
DCNv2 (Wang et al., 2021)	0.62	0.20	0.18	MLP (Gorishniy et al., 2021)	0.61	0.23	0.15
ResNet (Gorishniy et al., 2021)	0.59	0.30	0.11	MLP-PLR (Gorishniy et al., 2022)	0.57	0.27	0.16
RandomForest	0.57	0.18	0.26	ExcelFormer (Chen et al., 2024)	0.56	0.28	0.16
SAINT (Somepalli et al., 2022)	0.56	0.26	0.19	FT-T (Gorishniy et al., 2021)	0.50	0.28	0.23
XGBoost (Chen & Guestrin, 2016)	0.49	0.19	0.32	LightGBM Ke et al. (2017)	0.46	0.21	0.33
TabR (Gorishniy et al., 2024)	0.42	0.34	0.24	CatBoost (Prokhorenkova et al., 2018)	0.38	0.23	0.39

performance on the test set. For classification tasks, we consider accuracy (higher is better), and for regression tasks, we use Root Mean Square Error (RMSE) (lower is better). To summarize overall model performance, we report the average performance rank across all methods and datasets (lower ranks are better), following Delgado et al. (2014); McElfresh et al. (2023). Additionally, we conduct statistical *t*-tests to determine whether the differences between MODERNNCA and other methods are statistically significant.

Comparison Methods. We compare MODERNNCA with 20 approaches among three different categories. (For brevity, only 8 of them are shown in Figure 1.) First, we consider classical parametric methods, including linear SVM and tree-based methods like RandomForest, XGBoost (Chen & Guestrin, 2016), LightGBM Ke et al. (2017), and CatBoost (Prokhorenkova et al., 2018). Then, we consider parametric deep models, including NODE (Popov et al., 2020), MLP (Kadra et al., 2021; Gorishniy et al., 2021), ResNet (Gorishniy et al., 2021), SAINT (Somepalli et al., 2022), DCNv2 (Wang et al., 2021), FT-Transformer (Gorishniy et al., 2021), DANets (Chen et al., 2022), MLP-PLR (Gorishniy et al., 2022), TabCaps (Chen et al., 2023), Tangos (Jeffares et al., 2023), PTaRL (Ye et al., 2024b), SwitchTab (Wu et al., 2024), and ExcelFormer (Chen et al., 2024). For neighborhood-based methods, we consider KNN and TabR (Gorishniy et al., 2024). For a fair comparison, the same PLR numerical encoding is applied in MLP-PLR, TabR, and MODERNNCA.

Implementation Details. We pre-process all datasets following Gorishniy et al. (2021). For all deep methods, we set the batch size as 1024. The hyper-parameters of all methods are searched based on the training and validation set via Optuna (Akiba et al., 2019) following Gorishniy et al. (2021; 2024) over 100 trials. We set the ranges of the hyper-parameters for the compared methods following Gorishniy et al. (2021; 2024) and their official codes. The best-performed hyper-parameters are fixed during the final 15 seeds. Since the sampling rate of SNS effectively enhances the performance and reduces the training overhead, we treat it as a hyper-parameter and search within the range of [0.05, 0.6].

5.2 Main Results

The comparison results between MODERNNCA, L-NCA, and six representative methods are presented in Figure 1. All methods are evaluated across three aspects: performance (average performance rank), average training time, and average memory usage across all datasets. While some models,

such as TabR, exhibit strong performance, they require significantly longer training times. In contrast, MODERNNCA strikes an excellent balance across various evaluation criteria.

We also applied the Wilcoxon-Holm test (Demsar, 2006) to assess pairwise significance among all methods for both classification and regression tasks. The results are shown in Figure 2. For classification tasks (shown in the left part of Figure 2), MODERNNCA consistently outperforms tree-based methods like XGBoost in most cases, demonstrating that its deep neural network architecture is more effective at capturing nonlinear relationships. Furthermore, compared to deep tabular models such as FT-T and MLP-PLR, MODERNNCA maintains its superiority. When combined with the results in Figure 1, these observations validate the effectiveness of MODERNNCA. It achieves performance on par with the leading tree-based method, CatBoost, while outperforming existing deep tabular models in both classification and regression tasks across 300 datasets.

Additionally, we calculated the Win/Tie/Lose ratio between MODERNNCA and other comparison methods across the 300 datasets. If two methods show no significant difference (based on a *t*-test at a 95% confidence interval), they are considered tied. Otherwise, one method is declared the winner based on the comparison of their average performance. Given the no free lunch theorem, it is challenging for any single method to statistically outperform others across all cases. Nevertheless, MODERNNCA demonstrates superior performance in most cases. For instance, MODERNNCA outperforms TabR on 126 datasets, ties on 102 datasets, and does so with a simpler architecture and shorter training time. Compared to CatBoost, MODERNNCA wins on 114 datasets and ties on 69 datasets. These results indicate that MODERNNCA serves as an effective and competitive deep learning baseline for tabular data.

6 ANALYSES AND ABLATION STUDIES OF MODERNNCA

In this section, we analyze the sources of improvement in MODERNNCA. All experiments are conducted on a tiny tabular benchmark comprising 45 datasets, as introduced in (Ye et al., 2024a). The benchmark consists of 27 classification datasets and 18 regression datasets. The average rank of various tabular methods on this benchmark closely aligns with the results observed on the larger set of 300 datasets, as detailed in (Ye et al., 2024a).

6.1 IMPROVEMENTS FROM NCA TO L-NCA

We begin with the original NCA (Goldberger et al., 2004), using the scikit-learn implementation (Pedregosa et al., 2011). We progressively replace key components in NCA and assess the resulting performance improvements. Since the original NCA only targets classification tasks, this subsection focuses on the 27 classification datasets in the tiny benchmark. To ensure a fair comparison, we re-implement the original NCA using the deep learning framework PyTorch (Paszke et al., 2019), denoting this baseline version as "NCAv0".

Does Projection to a Higher Dimension Help? In the scikit-learn implementation, NCA is constrained to perform dimensionality reduction, *i.e.*, $d' \leq d$ for the projection L. We remove this constraint, allowing NCA to project into higher dimensions, and refer to this version as "NCAv1". Although higher dimensions by linear projections do not inherently enhance the representation ability of the squared Euclidean distance, the improvements in average performance rank from NCAv0 to NCAv1 (shown in Table 2) indicate that projecting to a higher dimension facilitates the optimization of this non-convex problem and improves generalization.

Does Stochastic Gradient Descent Help? Stochastic gradient descent (SGD) is a widely used optimizer in deep learning. To explore whether SGD can improve NCA's performance, we replace the default L-BFGS optimizer used in scikit-learn with SGD (without momentum) and denote this variant as "NCAv2". The performance improvements from NCAv1 to NCAv2 in Table 2 indicate that SGD makes NCA more effective in tabular data tasks.

The Influence of the Loss Function. The original NCA maximizes the expected leave-one-out accuracy as shown in Equation 3. In contrast, we minimize the negative log version of this objective as described in Equation 1. Although the log version for classification tasks was mentioned in Goldberger et al. (2004); Salakhutdinov & Hinton (2007), the original NCA preferred the leave-one-out formulation for better performance. We denote the variant with the modified loss function as

Table 2: Comparison of the average rank of (the linear) NCA variants and (the nonlinear) MLP across 27 classification datasets in the tiny-benchmark. The check marks indicate the differences in components among the variants. The average rank represents the overall performance of a method across all datasets, with lower ranks indicating better performance. The final variant, NCAv4, corresponds to the L-NCA version discussed in our paper.

	High dimension	SGD optimizer	Log loss	Soft-NN prediction	Average rank
NCAv0					4.400
NCAv1	\checkmark				3.708
NCAv2	\checkmark	\checkmark			3.296
NCAv3	\checkmark	\checkmark	\checkmark		3.192
NCAv4	\checkmark	✓	\checkmark	\checkmark	2.962
MLP	✓	✓	✓		3.000

Table 3: Comparison among various configurations of the deep architectures used to implement ϕ , where MLP is the default choice in MODERNNCA. We show the change in average performance rank (lower is better) across the four configurations on the 45 datasets in the tiny benchmark.

	MLP	Linear	w/ LayerNorm	ResNet
Classification	2.333	2.778	2.537	2.352
Regression	2.333	2.433	2.528	2.806

"NCAv3". As shown in Table 2 (NCAv2 vs. NCAv3), we find that using the log version slightly improves performance, especially when combined with deep architectures used in MODERNNCA. Further comparisons with alternative objectives are provided in the appendix.

The Influence of the Prediction Strategy. During testing, rather than applying a "hard" KNN with the learned embeddings as in standard metric learning, we adopt a soft nearest neighbor (soft-NN) inference rule, consistent with the training phase. This variant, using soft-NN for prediction, is referred to as "NCAv4", which is equivalent to the "L-NCA" version defined in subsection 4.1. Based on the change of average performance rank in Table 2, this modified prediction strategy further enhances NCA's classification performance, bringing linear NCA surpassing deep models like MLP.

6.2 IMPROVEMENTS FROM L-NCA TO M-NCA

In this subsection, we investigate the influence of architectures and encoding strategies to systematically reveal the impacts of more deep learning techniques on NCA.

Linear vs. Deep Architectures. We first investigate the architecture design for ϕ in MODERNNCA, where one or more layers of blocks $g(\cdot)$ are added on top of a linear projection. We consider three configurations. First, we set ϕ as a linear projection, where the dimensionality of the projected space is a hyper-parameter.² Then we replace batch normalization with layer normalization in the block. Finally, we add a residual link from the block's input to its output. Based on classification and regression performance across 45 datasets, we present the average performance rank of the four variants in Table 3. To avoid limiting model capacity, hyper-parameters such as the number of layers are determined based on the validation set. Further comparisons of fixed architecture configurations are listed in the appendix.

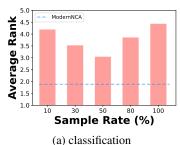
We first compare NCA with MLP vs. with the linear counterpart in Table 3. In classification tasks, MLP achieves a lower rank, highlighting the importance of incorporating nonlinearity into the model. However, in regression tasks, the linear version performs well, with MLP showing only small improvements. Although the linear projection is part of MLP's search space, the linear version benefits from a smaller hyper-parameter space, potentially resulting in better generalization.

As described in subsection 4.2, MLP uses batch normalization instead of layer normalization. Empirically, batch normalization performs better on average in both classification and regression tasks as shown in Table 3. Additionally, we compare the MLP implementation with and without residual connections. While performing similarly in classification, MLP shows superiority, especially in regression. Therefore, we adopt the MLP implementation in Table 3 for MODERNNCA.

²This "linear" version also includes the SNS sampling strategy and the nonlinear PLR encoding.

Table 4: Comparison among MODERNNCA, MLP (Gorishniy et al., 2021), and TabR (Gorishniy et al., 2024) with or without PLR encoding for numerical features. We show the change in average performance rank across the four configurations on the 45 datasets in the tiny-benchmark.

		w/o	PLR		w/	PLR
	MLP	TabR	ModernNCA	MLP	TabR	ModernNCA
Classification	4.556	3.148	3.037	4.480	3.037	2.630
Regression	4.444	3.167	3.389	3.333	3.444	3.222



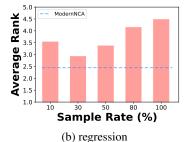


Figure 3: The change of average performance rank with different sampling rates among {10%, 30%, 50%, 80%, 100%} in SNS strategy. The dotted line denotes the rank of MODERNNCA.

Influence of the PLR Encoding. PLR encoding transforms numerical features into high-dimensional vectors, enhancing both model capacity and nonlinearity. To assess the impact of PLR encoding, we compare Modernnoch with MLP and TabR, both with and without PLR encoding. Following a similar setup as in Table 3, we present the change in average performance rank across six methods in both classification and regression tasks in Table 4.

Without PLR encoding, TabR outperforms MLP, and MODERNNCA shows stronger performance in classification while performing slightly worse in regression (although still better than MLP). PLR encoding improves all methods, as evidenced by the decrease in average performance rank. In the right section of Table 4, we observe that MODERNNCA performs best in both classification and regression tasks, effectively leveraging PLR encoding better than TabR. This may be because the nonlinearity introduced by PLR compensates for the relative simplicity of MODERNNCA. The results also validate that the strength of MODERNNCA comes from a combination of its objective, architecture, and training strategy, rather than relying solely on the PLR encoding strategy.

The Influence of Sampling Ratios. Due to the huge computational cost of calculating distances in the learned embedding space, MODERNNCA employs a Stochastic Neighborhood Sampling (SNS) strategy, where only a subset of the training data is randomly sampled for each mini-batch. Therefore, the training time and memory cost is significantly reduced. We experiment with varying the proportion of sampled training data while keeping other hyper-parameters constant, then evaluate the corresponding test performance. As shown in Figure 3, sampling 30%-50% of the training set yields better results for MODERNNCA than using the full set. SNS not only improves training efficiency but also enhances the model's generalization ability. The plots also indicate that, with a tuned sampling ratio, MODERNNCA achieves a superior performance rank (dotted lines in the figure).

7 Conclusion

Leveraging neighborhood relationships for predictions is a classical approach in machine learning. In this paper, we revisit and enhance one of the most representative neighborhood-based methods, NCA, by incorporating modern deep learning techniques. The improved MODERNNCA establishes itself as a strong baseline for deep tabular prediction tasks, offering competitive performance while reducing the training time required to access the entire dataset. Extensive results demonstrate that MODERNNCA frequently outperforms both tree-based and deep tabular models in classification and regression tasks. Our detailed analyses shed light on the key factors driving these improvements, including the enhancements introduced to the original NCA.

8 REPRODUCIBILITY STATEMENT

MODERNNCA is easy to implement. The code for MODERNNCA, along with all comparison methods and datasets, is available at https://anonymous.4open.science/r/modernNCA/.

REFERENCES

- Nesreen K Ahmed, Amir F Atiya, Neamat El Gayar, and Hisham El-Shishiny. An empirical comparison of machine learning models for time series forecasting. *Econometric reviews*, 29(5-6): 594–621, 2010.
- Takuya Akiba, Shotaro Sano, Toshihiko Yanase, Takeru Ohta, and Masanori Koyama. Optuna: A next-generation hyperparameter optimization framework. In *KDD*, 2019.
 - Sercan Ö. Arik and Tomas Pfister. Tabnet: Attentive interpretable tabular learning. In AAAI, 2021.
- Lei Jimmy Ba, Jamie Ryan Kiros, and Geoffrey E. Hinton. Layer normalization. *CoRR*, abs/1607.06450, 2016.
- Dara Bahri, Heinrich Jiang, Yi Tay, and Donald Metzler. Scarf: Self-supervised contrastive learning using random feature corruption. In *ICLR*, 2022.
- Aurélien Bellet, Amaury Habrard, and Marc Sebban. *Metric Learning*. Morgan & Claypool Publishers, 2015.
- Christopher Bishop. *Pattern recognition and machine learning*. Springer, 2006.
 - Vadim Borisov, Tobias Leemann, Kathrin Seßler, Johannes Haug, Martin Pawelczyk, and Gjergji Kasneci. Deep neural networks and tabular data: A survey. *IEEE Transactions on Neural Networks and Learning Systems*, abs/2110.01889:1–21, 2022.
 - Chun-Hao Chang, Rich Caruana, and Anna Goldenberg. NODE-GAM: neural generalized additive model for interpretable deep learning. In *ICLR*, 2022.
 - Jintai Chen, Kuanlun Liao, Yao Wan, Danny Z. Chen, and Jian Wu. Danets: Deep abstract networks for tabular data classification and regression. In *AAAI*, 2022.
 - Jintai Chen, KuanLun Liao, Yanwen Fang, Danny Chen, and Jian Wu. Tabcaps: A capsule neural network for tabular data classification with bow routing. In *ICLR*, 2023.
 - Jintai Chen, Jiahuan Yan, Qiyuan Chen, Danny Ziyi Chen, Jian Wu, and Jimeng Sun. Can a deep learning model be a sure bet for tabular prediction? In *KDD*, pp. 288–296, 2024.
 - Tianqi Chen and Carlos Guestrin. Xgboost: A scalable tree boosting system. In KDD, 2016.
 - Heng-Tze Cheng, Levent Koc, Jeremiah Harmsen, Tal Shaked, Tushar Chandra, Hrishi Aradhye, Glen Anderson, Greg Corrado, Wei Chai, Mustafa Ispir, Rohan Anil, Zakaria Haque, Lichan Hong, Vihan Jain, Xiaobing Liu, and Hemal Shah. Wide & deep learning for recommender systems. In *DLRS*, 2016.
 - Jason V. Davis, Brian Kulis, Prateek Jain, Suvrit Sra, and Inderjit S. Dhillon. Information-theoretic metric learning. In *ICML*, 2007.
 - Manuel Fernández Delgado, Eva Cernadas, Senén Barro, and Dinani Gomes Amorim. Do we need hundreds of classifiers to solve real world classification problems? *Journal of Machine Learning Research*, 15(1):3133–3181, 2014.
 - Janez Demsar. Statistical comparisons of classifiers over multiple data sets. *Journal of Machine Learning Research*, 7:1–30, 2006.
 - Jacob Devlin, Ming-Wei Chang, Kenton Lee, and Kristina Toutanova. BERT: pre-training of deep bidirectional transformers for language understanding. In *NAACL-HLT*, 2019.

- Nicholas Frosst, Nicolas Papernot, and Geoffrey Hinton. Analyzing and improving representations with the soft nearest neighbor loss. In *International conference on machine learning*, pp. 2012–2020. PMLR, 2019a.
 - Nicholas Frosst, Nicolas Papernot, and Geoffrey E. Hinton. Analyzing and improving representations with the soft nearest neighbor loss. In *ICML*, volume 97, pp. 2012–2020, 2019b.
 - Amir Globerson and Sam T. Roweis. Metric learning by collapsing classes. In *NIPS*, pp. 451–458, 2005.
 - Jacob Goldberger, Sam T. Roweis, Geoffrey E. Hinton, and Ruslan Salakhutdinov. Neighbourhood components analysis. In *NIPS*, 2004.
 - Yury Gorishniy, Ivan Rubachev, Valentin Khrulkov, and Artem Babenko. Revisiting deep learning models for tabular data. In *NeurIPS*, 2021.
 - Yury Gorishniy, Ivan Rubachev, and Artem Babenko. On embeddings for numerical features in tabular deep learning. In *NeurIPS*, 2022.
 - Yury Gorishniy, Ivan Rubachev, Nikolay Kartashev, Daniil Shlenskii, Akim Kotelnikov, and Artem Babenko. Tabr: Tabular deep learning meets nearest neighbors in 2023. In *ICLR*, 2024.
 - Léo Grinsztajn, Edouard Oyallon, and Gaël Varoquaux. Why do tree-based models still outperform deep learning on typical tabular data? In *NeurIPS*, 2022.
 - Huifeng Guo, Ruiming Tang, Yunming Ye, Zhenguo Li, and Xiuqiang He. Deepfm: A factorization-machine based neural network for CTR prediction. In *IJCAI*, 2017.
 - Md. Rafiul Hassan, Sadiq Al-Insaif, Muhammad Imtiaz Hossain, and Joarder Kamruzzaman. A machine learning approach for prediction of pregnancy outcome following IVF treatment. *Neural Computing and Applications*, 32(7):2283–2297, 2020.
 - Noah Hollmann, Samuel Müller, Katharina Eggensperger, and Frank Hutter. Tabpfn: A transformer that solves small tabular classification problems in a second. In *ICLR*, 2023.
 - Cheng-Kang Hsieh, Longqi Yang, Yin Cui, Tsung-Yi Lin, Serge J. Belongie, and Deborah Estrin. Collaborative metric learning. In *WWW*, 2017.
 - Sergey Ioffe and Christian Szegedy. Batch normalization: Accelerating deep network training by reducing internal covariate shift. In *ICML*, 2015.
 - Alan Jeffares, Tennison Liu, Jonathan Crabbé, Fergus Imrie, and Mihaela van der Schaar. Tangos: Regularizing tabular neural networks through gradient orthogonalization and specialization. In *ICLR*, 2023.
 - Arlind Kadra, Marius Lindauer, Frank Hutter, and Josif Grabocka. Well-tuned simple nets excel on tabular datasets. In *NeurIPS*, pp. 23928–23941, 2021.
 - Liran Katzir, Gal Elidan, and Ran El-Yaniv. Net-dnf: Effective deep modeling of tabular data. In *ICLR*, 2021.
 - Guolin Ke, Qi Meng, Thomas Finley, Taifeng Wang, Wei Chen, Weidong Ma, Qiwei Ye, and Tie-Yan Liu. Lightgbm: A highly efficient gradient boosting decision tree. In *NIPS*, 2017.
 - Prannay Khosla, Piotr Teterwak, Chen Wang, Aaron Sarna, Yonglong Tian, Phillip Isola, Aaron Maschinot, Ce Liu, and Dilip Krishnan. Supervised contrastive learning. In *NeurIPS*, 2020.
 - Brian Kulis. Metric learning: A survey. Foundations and Trends in Machine Learning, 5(4), 2013.
 - Steinar Laenen and Luca Bertinetto. On episodes, prototypical networks, and few-shot learning. In *NeurIPS*, pp. 24581–24592, 2021.
 - Dong C Liu and Jorge Nocedal. On the limited memory bfgs method for large scale optimization. *Mathematical programming*, 45(1):503–528, 1989.

- Duncan C. McElfresh, Sujay Khandagale, Jonathan Valverde, Vishak Prasad C., Ganesh Ramakrishnan, Micah Goldblum, and Colin White. When do neural nets outperform boosted trees on tabular data? In *NeurIPS*, 2023.
 - Martin Renqiang Min, Laurens van der Maaten, Zineng Yuan, Anthony J. Bonner, and Zhaolei Zhang. Deep supervised t-distributed embedding. In *ICML*, pp. 791–798, 2010.
 - Mehryar Mohri, Afshin Rostamizadeh, and Ameet Talwalkar. *Foundations of Machine Learning*. MIT Press, 2012.
 - Lennart J Nederstigt, Steven S Aanen, Damir Vandic, and Flavius Frasincar. Floppies: a framework for large-scale ontology population of product information from tabular data in e-commerce stores. *Decision Support Systems*, 59:296–311, 2014.
 - Adam Paszke, Sam Gross, Francisco Massa, Adam Lerer, James Bradbury, Gregory Chanan, Trevor Killeen, Zeming Lin, Natalia Gimelshein, Luca Antiga, et al. Pytorch: An imperative style, high-performance deep learning library. *Advances in neural information processing systems*, 32, 2019.
 - F. Pedregosa, G. Varoquaux, A. Gramfort, V. Michel, B. Thirion, O. Grisel, M. Blondel, P. Prettenhofer, R. Weiss, V. Dubourg, J. Vanderplas, A. Passos, D. Cournapeau, M. Brucher, M. Perrot, and E. Duchesnay. Scikit-learn: Machine learning in Python. *Journal of Machine Learning Research*, 12:2825–2830, 2011.
 - Sergei Popov, Stanislav Morozov, and Artem Babenko. Neural oblivious decision ensembles for deep learning on tabular data. In *ICLR*, 2020.
 - Liudmila Ostroumova Prokhorenkova, Gleb Gusev, Aleksandr Vorobev, Anna Veronika Dorogush, and Andrey Gulin. Catboost: unbiased boosting with categorical features. In *NeurIPS*, 2018.
 - Matthew Richardson, Ewa Dominowska, and Robert Ragno. Predicting clicks: estimating the click-through rate for new ads. In *WWW*, 2007.
 - Ivan Rubachev, Artem Alekberov, Yury Gorishniy, and Artem Babenko. Revisiting pretraining objectives for tabular deep learning. *CoRR*, abs/2207.03208, 2022.
 - Ruslan Salakhutdinov and Geoffrey E. Hinton. Learning a nonlinear embedding by preserving class neighbourhood structure. In *AISTATS*, volume 2, pp. 412–419, 2007.
 - Florian Schroff, Dmitry Kalenichenko, and James Philbin. Facenet: A unified embedding for face recognition and clustering. In *CVPR*, 2015.
 - Karen Simonyan and Andrew Zisserman. Very deep convolutional networks for large-scale image recognition. In *ICLR*, 2015.
 - Kihyuk Sohn. Improved deep metric learning with multi-class n-pair loss objective. In NIPS, 2016.
 - Gowthami Somepalli, Avi Schwarzschild, Micah Goldblum, C. Bayan Bruss, and Tom Goldstein. SAINT: Improved neural networks for tabular data via row attention and contrastive pre-training. In *NeurIPS Workshop*, 2022.
 - Hyun Oh Song, Yu Xiang, Stefanie Jegelka, and Silvio Savarese. Deep metric learning via lifted structured feature embedding. In *CVPR*, 2016.
 - Nitish Srivastava, Geoffrey E. Hinton, Alex Krizhevsky, Ilya Sutskever, and Ruslan Salakhutdinov. Dropout: a simple way to prevent neural networks from overfitting. *Journal of Machine Learning Research*, 15(1):1929–1958, 2014.
 - Daniel Tarlow, Kevin Swersky, Laurent Charlin, Ilya Sutskever, and Richard S. Zemel. Stochastic k-neighborhood selection for supervised and unsupervised learning. In *ICML*, pp. 199–207, 2013.
 - Talip Ucar, Ehsan Hajiramezanali, and Lindsay Edwards. Subtab: Subsetting features of tabular data for self-supervised representation learning. In *NeurIPS*, pp. 18853–18865, 2021.

- Laurens Van der Maaten and Geoffrey Hinton. Visualizing data using t-sne. *Journal of machine learning research*, 9(11), 2008.
 - Joaquin Vanschoren, Jan N Van Rijn, Bernd Bischl, and Luis Torgo. Openml: networked science in machine learning. *ACM SIGKDD Explorations Newsletter*, 15(2):49–60, 2014.
 - Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N Gomez, Łukasz Kaiser, and Illia Polosukhin. Attention is all you need. In *NIPS*, 2017.
 - Jarkko Venna, Jaakko Peltonen, Kristian Nybo, Helena Aidos, and Samuel Kaski. Information retrieval perspective to nonlinear dimensionality reduction for data visualization. *Journal of Machine Learning Research*, 11:451–490, 2010.
 - Oriol Vinyals, Charles Blundell, Tim Lillicrap, Koray Kavukcuoglu, and Daan Wierstra. Matching networks for one shot learning. In *NIPS*, 2016.
 - Ruoxi Wang, Rakesh Shivanna, Derek Zhiyuan Cheng, Sagar Jain, Dong Lin, Lichan Hong, and Ed H. Chi. DCN V2: improved deep & cross network and practical lessons for web-scale learning to rank systems. In *WWW*, 2021.
 - Tianjun Wei, Jianghong Ma, and Tommy W. S. Chow. Collaborative residual metric learning. In *SIGIR*, 2023.
 - Kilian Q. Weinberger and Lawrence K. Saul. Distance metric learning for large margin nearest neighbor classification. *Journal of Machine Learning Research*, 10:207–244, 2009.
 - Jing Wu, Suiyao Chen, Qi Zhao, Renat Sergazinov, Chen Li, Shengjie Liu, Chongchao Zhao, Tianpei Xie, Hanqing Guo, Cheng Ji, Daniel Cociorva, and Hakan Brunzell. Switchtab: Switched autoencoders are effective tabular learners. In *AAAI*, pp. 15924–15933, 2024.
 - Eric P. Xing, Andrew Y. Ng, Michael I. Jordan, and Stuart Russell. Distance metric learning with application to clustering with side-information. In *NIPS*, 2002.
 - Xun Yang, Meng Wang, and Dacheng Tao. Person re-identification with metric learning using privileged information. *IEEE Transactions on Image Processing*, 27(2):791–805, 2018.
 - Han-Jia Ye, Si-Yang Liu, Hao-Run Cai, Qi-Le Zhou, and De-Chuan Zhan. A closer look at deep learning on tabular data. *CoRR*, abs/2407.00956, 2024a.
 - Hangting Ye, Wei Fan, Xiaozhuang Song, Shun Zheng, He Zhao, Dan dan Guo, and Yi Chang. Ptarl: Prototype-based tabular representation learning via space calibration. In *ICLR*, 2024b.
 - Dong Yi, Zhen Lei, Shengcai Liao, and Stan Z. Li. Deep metric learning for person re-identification. In *ICME*, 2014.

The Appendix consists of two sections:

- Appendix A: Datasets and implementation details.
- Appendix B: Additional experimental results.

APPENDIX A DATASETS AND IMPLEMENTATION DETAILS

In this section, we outline the preprocessing steps applied to the datasets before training, as well as descriptions of the datasets used.

A.1 DATA PRE-PROCESSING

We follow the data preprocessing pipeline from Gorishniy et al. (2021) for all methods. For numerical features, we apply standardization by subtracting the mean and scaling the values. For categorical features, we use one-hot encoding to convert them for model input.

A.2 DATASET INFORMATION

We use the recent large-scale tabular benchmark from Ye et al. (2024a), which includes 300 datasets covering various domains such as healthcare, biology, finance, education, and physics. The dataset sizes range from 1,000 to 1 million instances. More detailed information on the datasets can be found in Ye et al. (2024a).

For each dataset, we randomly sample 20% of the instances to form the test set. The remaining 80% is split further, with 20% of which held out as a validation set. The validation set is used to tune hyper-parameters and apply early stopping. The hyper-parameters with which the model performs best on the validation set are selected for final evaluation with the test set.

The datasets used in our analyses and ablation studies follow the tiny-benchmark in Ye et al. (2024a), which consists of 45 datasets. The performance rankings of methods on this smaller benchmark are consistent with those on the full benchmark, making it a useful probe for tabular analysis.

A.3 HARDWARE

The majority of experiments, including those measuring time and memory overhead, were conducted on a Tesla V100 GPU.

A.4 POTENTIAL ALTERNATIVE IMPLEMENTATION

We explore an alternative strategy to learn the embedding ϕ in two steps. First, we apply Supervised Contrastive loss (Sohn, 2016; Khosla et al., 2020), where supervision is generated within a mini-batch. After learning ϕ , we use KNN for classification or regression during inference. In the regression scenario, label values are discretized, and we refer to this baseline method as Tabular Contrastive (TabCon). Empirically, we find that certain components of MODERNNCA, such as the Soft-NN loss for prediction, cannot be directly applied to TabCon, even when ϕ is implemented using the same nonlinear MLP as in MODERNNCA. Despite this, the TabCon baseline remains competitive with FT-Transformer (FT-T), achieving average ranks similar to L-NCA in both classification and regression tasks.

APPENDIX B ADDITIONAL EXPERIMENTS

B.1 VISUALIZATION RESULTS

To better analyze the properties of MODERNNCA, we visualize the learned embeddings $\phi(x)$ of MODERNNCA, TabCon (mentioned in subsection A.4), and TabR using TSNE (Van der Maaten & Hinton, 2008). As shown in Figure 4, all deep tabular methods transform the embedding spaces to be more helpful for classification or regression compared to the raw features. The embedding space learned by TabCon clusters samples of the same class together and separates samples of different

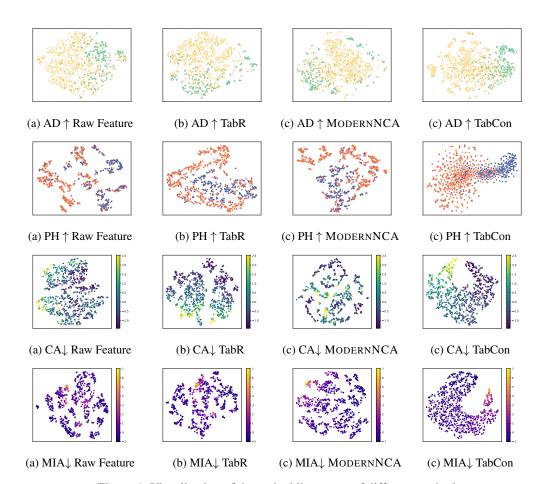


Figure 4: Visualization of the embedding space of different methods.

classes, often clustering same-class instances into a single cluster. However, it still struggles with some hard-to-distinguish samples. TabR and MODERNNCA, on the other hand, divide samples of the same class into multiple clusters, ensuring that similar samples are positioned closer to each other. This strategy aligns with the prediction mechanism of KNN, where good performance is achieved by clustering instances with similar neighbors together rather than into a single cluster. The embedding space learned by MODERNNCA is more discriminative than that learned by TabR. The main reason is that TabR leverages an additional architecture to modify the prediction score for each instance, making the learned embedding space less discriminative compared to MODERNNCA.

B.2 Additional Ablation Studies

The Influence of Distance Functions. The predicted label of a target instance x_i is determined by the label of its neighbors in the learned embedding space projected by ϕ . The distance function $\operatorname{dist}(\cdot,\cdot)$ is the key to determining the pairwise relationship between instances in the embedding space and influences the weights in Equation 5.

In MODERNNCA, we choose Euclidean distance

$$\operatorname{dist}_{\mathrm{EUC}}(\phi(\boldsymbol{x}_i), \phi(\boldsymbol{x}_j)) = \sqrt{(\phi(\boldsymbol{x}_i) - \phi(\boldsymbol{x}_j))^{\top}(\phi(\boldsymbol{x}_i) - \phi(\boldsymbol{x}_j))} = \|\phi(\boldsymbol{x}_i) - \phi(\boldsymbol{x}_j)\|_2. \quad (7)$$

We also utilize other distance functions, e.g., the squared Euclidean distance, $\operatorname{dist}^2_{\mathrm{EUC}}(\phi(\boldsymbol{x}_i), \phi(\boldsymbol{x}_j))$, the ℓ_1 -norm distance

$$\operatorname{dist}(\phi(\boldsymbol{x}_i), \phi(\boldsymbol{x}_i)) = \|\phi(\boldsymbol{x}_i) - \phi(\boldsymbol{x}_i)\|_1, \tag{8}$$

the (negative) cosine similarity $\operatorname{dist}(\phi(\boldsymbol{x}_i),\phi(\boldsymbol{x}_j)) = -(\boldsymbol{x}_i^\top \boldsymbol{x}_j)/(\|\boldsymbol{x}_i\|_2\|\boldsymbol{x}_j\|_2)$, and the (negative) inner product $\operatorname{dist}(\phi(\boldsymbol{x}_i),\phi(\boldsymbol{x}_j)) = -\phi(\boldsymbol{x}_i)^\top\phi(\boldsymbol{x}_j)$. The results using different distance functions

Table 5: Comparison among various distances used to implement Equation 5, where Euclid distance is the default choice in MODERNNCA. We show the change in average performance rank (lower is better) across the five configurations on the 45 datasets in the tiny-benchmark.

	Euclid	Dot Product	Cosine	Squared Euclid	L1-Norm
Classification	2.593	3.852	2.111	2.630	3.769
Regression	2.500	3.222	2.529	2.722	3.889

Table 6: Comparison of different loss functions. The log loss used in MODERNNCA, the original NCA's summation loss, the MCML loss, and the t-distribution loss. The change in average performance rank (lower is better) is presented across these four configurations on the 45 datasets in the tiny-benchmark.

	ModernNCA	NCA	MCML	t-distribution
Classification Regression	2.074 1.500	2.519	3.074	2.333 1.540

are listed in Table 5, which contains the average performance rank over 45 datasets among the five variants. On average, Euclidean distance performs well across both classification and regression tasks. While cosine distance yields better results on classification datasets (with an average performance rank of 4.5939 compared to MODERNNCA and 20 other methods across 300 datasets, please check Figure 2 for details), its advantage diminishes on regression tasks.

Other Possible Loss Functions. NCA (Goldberger et al., 2004) originally explored two loss functions: one that maximizes the sum of probabilities in Equation 3, and another that minimizes the sum of log probabilities as in Equation 1. The former was selected in the original implementation of NCA due to its better performance. We also investigated several alternative loss functions for NCA. For instance, MCML (Globerson & Roweis, 2005) minimizes the KL-divergence between the learned embedding in Equation 2 and a constructed ground-truth label distribution for each instance, but it only applies to classification tasks. Another variant is the t-distributed NCA (Min et al., 2010), which uses a heavy-tailed t-distribution to measure pairwise similarities in the objective function. We tested both MCML and the t-distribution loss functions in MODERNNCA, and the results are summarized in Table 6, showing the average ranks across 45 datasets. The log objective in Equation 1 performs best for classification tasks and slightly outperforms the t-distribution variant in regression tasks.

The Influence of Sampling Strategy. As mentioned before, SNS randomly samples a subset of training data for each mini-batch when calculating the loss of Equation 5. We also investigate whether we could further improve the classification/regression ability of the model when we incorporate richer information during the sampling process, *e.g.*, the label of the instances.

We consider two other sampling strategies in addition to the fully random one we used before. First is class-wise random sampling, which means that given a proportion, we sample from each class in the training set and combine them together. This strategy takes advantage of the training label information and keeps the instances from all classes that will exist in the sampled subset. Besides, we also consider the sampling strategy based on the pairwise distances between instances. Since the neighbors of an instance may contribute more (with larger weights) in Equation 5, so given a mini-batch, we first calculate the Euclidean distance between instances in the batch and all the training set with the embedding function ϕ in the current epoch. Then we sample the training set based on the reciprocal of the pairwise distance value. In detail, given an instance x_i , we provide instance-specific neighborhood candidates and x_j in the training set is sampled based on the probability $\sim 1/(\text{dist}(\phi(x_i),\phi(x_j)))^{\tau}$. τ is a non-negative hyper-parameter to calibrate the distribution. The distance calculation requires forward passes of the model ϕ over all the training instances, and the instance-specific neighborhood makes the loss related to a wide range of the training data. Therefore, the distance-based sampling strategy has a low training speed and high computational burden.

The comparison results, *i.e.*, the average performance rank, among different sampling strategies on 45 datasets are listed in Table 7. We empirically find the label-based sampling strategy cannot provide

Table 7: Comparison of different sampling strategies: "Random", "Label", and "Distance" represent MODERNNCA's naive uniform sampling, class-wise random sampling, and distance-based sampling, respectively. The change in average performance rank (lower is better) is presented across these three configurations on the 45 datasets in the tiny-benchmark.

	Random	Label	Distance
Classification	1.869	2.230	1.901
Regression	1.508		1.492

Table 8: Comparison of various architecture choices based on a fixed 2-layer MLP. We only tune architecture-independent hyper-parameters for different variants. The change in average performance rank (lower is better) is shown across three configurations (default, Layer Norm, and Residual) on the 45 datasets in the tiny-benchmark.

	MLP	w/ LayerNorm	ResNet
Classification	1.905	2.048	2.048
Regression	1.813	2.313	1.875

further improvements. Although the distance-based strategy helps in certain cases, the improvements are limited. Taking a holistic consideration of the performance and efficiency, we choose to use the vanilla random sampling in MODERNNCA.

Comparison between Different Deep Architectures. Unlike the ablation studies in subsection 6.2, where we fixed the model family and tuned detailed hyper-parameters (such as the number of layers and network width) based on the validation set, here we fix the main architecture as a two-layer MLP and only tune architecture-independent hyper-parameters, such as the learning rate.

With this base MLP architecture, we evaluate three variants: the base MLP, one with batch normalization replaced by layer normalization, and one with an added residual link. The average ranks of the three variants across 45 datasets are presented in Table 8. We observe that the basic MLP remains a better choice compared to the versions with a residual link or layer normalization.

B.3 RUN-TIME AND MEMORY USAGE ESTIMATION

We make a run-time and memory usage comparison in Figure 1. Here are the steps that we take to perform the estimation. First, we tuned all models on the validation set for 100 iterations, saving the optimal parameters ever found. Next, we ran the models for 15 iterations with the tuned parameters and saved the best checkpoint on the validation set. The run-time for the models was estimated using the average time taken by the tuned model to run one seed in the training and validation stage.

We present the average results of run-time and memory usage estimation across the full benchmark (300 datasets) in Table 9.

Table 9: Training time and memory usage estimation for different tuned models over 300 datasets. The average rank represents the mean performance ranking of these models based on the performance metrics (RMSE for regression and accuracy for classification).

Model	M-NCA	L-NCA	MLP	MLP-PLR	FT-T	TabR	XGBoost	CatBoost
Training Time (s)	87.5	33.62	30.36	42.87	111.91	173.34	4.53	20.48
Memory Usage (GB)	5.36	1.42	1.15	2.37	4.98	10.13	0.84	1.06
Average Rank	4.56	6.30	7.53	6.94	6.29	5.36	5.62	4.61

B.4 FULL RESULT ON THE BENCHMARK

Table 10: Detailed results (average accuracy) for all classification datasets over all methods.Due to space constraints, dataset IDs from Ye et al. (2024a) are used in place of dataset names. "XGB", "RF", "LG", "RN", "ND", "ST", "TG", "DAN", "FTT", "DCN", "TT", "PT", "EF", and "TR" denote "XGBoost", "Random Forest", "LightGBM", "ResNet", "NODE", "SwitchTab", "TANGOS", "DANets", "FT-T", "DCNv2", "PTaRL", "Excelformer" and "TabR", respectively.

5. 9. 347. 397. 397. 397.4 101 3815 3902 3678 3885 2780 3807 2901 399. 3489 3701	ID	M-NCA	L-NCA	TR	XGB	CGB	MLP	FTT	DCN	ND	MP	EF	DAN	TG	TC	ST	LG	RF	SVM	KNN	SW	PT
10																						
11 985 9813 3988 9876 9876 9840 9840 9850 9852 9855 9840 9848 9841 9873 9852 9818 9375 9375 937																						
12 S82 5770 5792 5838 5895 5780 5850 5838 5881 5780 5870 5779 5819 5810 - 5837 5774 5185 5629 5624 5780 5877 5876 5870 5875 5875 5875 5875 5875 5875 5875																						
18																						
19																						
229 8/05 8/06 8/07 8/07 8/07 8/07 8/07 8/07 8/07 8/07																						
279 9053 9806 9155 9000 9082 8847 8923 8858 8730 8878 8915 8850 8852 8812 8855 9070 8765 8413 8522 8155 88 289 8313 - 8322 8326 8314 4734 7393 7322 7321 7320 7326 7317 7323 7398 7316 - 7335 7355 256 6833 6757 740 290 8313 - 8322 8326 8314 8333 8327 8313 8333 8336 8321 8323 8333 8334 8332 8325 7921 8325 8325 8327 391 8914 8832 8609 8734 8905 8737 8927 8917 8589 8935 8850 8679 8745 8854 8922 8783 8801 8815 8705 8662 89 39 9567 39 8914 8832 8609 8734 8905 8737 8927 8917 8589 8935 8850 8679 8745 8854 8922 8783 8801 8815 8705 8662 89 39 9567 40 9707 970 970 970 970 970 970 970 970 9																						
28. 3730. 7298. 37314. 7331. 7340. 7339. 7322. 7321. 7320. 7320. 7317. 7323. 7328. 73315. 7332. 5893. 6775. 7324. 7329. 8331 8. 322. 3325. 3326. 3334. 3332. 3323. 3333. 3334. 3325. 3325. 5325. 5325. 3325. 3329.																						
36 791 8903 8920 7814 7972 7315 7770 7771 7194 797 8508 9508 580 8679 8748 85 8932 8783 881 8708 8606 27 87 8914 883 82 8783 882 8609 8745 8606 597 8609 9639 9666 9529 6650 9937 9161 91 894 876 876 756 756 756 746 744 7391 7319 767 7572 7460 7572 7460 750 7580 878 878 7897 879 870 870 870 870 870 870 870 870 870 870																						
37. 89.14 88.12 8609 8754 8905 8787 8907 8917 8590 8925 8809 8741 8824 8902 8783 8801 8815 8705 8602 81																						
939 9, 9677 9689 9681 9648 963 963 963 964 9582 9665 - 9522 9623 9569 9659 9666 9529 6660 9579 9161 942 6497 42 6972 6937 6710 6723 6672 692 6728 6627 6643 6692 6694 6691 6640 6666 6675 6779 6650 6286 6455 6597 647 847 847 847 847 847 847 847 847 847 8																						
40 7.469 6.6987 7.756 7.261 7.414 7.391 7.319 7.671 5.772 7.460 7.380 7.388 7.391 7.065 7.348 7.328 7.351 7.222 6.494 6.694 7.457 6.457 6.500 6.606 6.607 6.675 7.697 6.650 6.256 6.697 6.691 6.691 6.691 6.696 6.667 6.675 7.979 6.650 6.256 6.599 6.491 6.491 6.494 7.492 7.491 7.																						
42. 6972 6937 6710 6723 6672 6692 6728 6627 6634 6692 6694 6699 6640 6666 6675 6779 6690 6636 6455 6597 679 6294 844 7428 7340 7396 7340 7396 7341 7427 7391 7410 7374 7451 7445 7417 7431 7351 7355 7411 7371 7424 7390 7443 7251 7319 7428 7340 7396 7411 7427 7391 7410 7374 7451 7454 7417 7431 7351 7355 7411 7371 7424 7390 7443 7251 7319 7428 744 7390 7438 7421 7390 7438 7451 7454 7390 7438 7451 7454 7390 7438 7451 7454 7390 7438 7451 7454 7390 7438 7451 7454 7390 7438 7451 7454 7390 7438 7451 7454 7390 7438 7451 7454 7454 7454 7454 7454 7454 7454																						
444 7428 7340 7390 7411 7427 7391 7410 7374 7451 7445 7411 7416 7356 7411 7371 7424 7390 7434 7251 7319 745 750 750 745 751 7455 650 7411 7415 7411 74116 6381 6630 7421 6901 7408 6701 7408 6721 6901 7408 6721 6901 7408 6721 6901 7408 6721 6901 7408 6721 6725 7408 740 7408 740 740 740 740 740 740 740 740 740 740																						
457 7057 7301 7428 6714 6816 7384 7346 7370 5577 6945 8007 7277 7315 7322 7012 6812 6759 7391 6765 6539 70 477 7544 7290 7520 6627 6398 6901 5179 7480 6523 6500 5297 5370 5010 6111 5177 6618 6554 7520 5940 5322 6187 748 7520 7570 7570 7570 7570 7570 7570 7570	43	.8459																				
46 7.115 7.116 7.116 6.381 6.693 7.121 6.991 7.108 9.900 7.008 7.052 7.112 6.725 7.033 - 6.642 5.849 7.034 5.766 6.599 7.340 6.234 48 7.254 7.254 7.297 7.990 7.520 6.267 2.089 6.091 5.197 9.480 6.232 6.050 5.297 5.370 5.010 6.11 5.177 6.18 6.554 7.504 5.232 6.084 7.209 7.209 7.200 6.003 7.003 7.008 6.023 6.158 6.085 6.184 6.090 7.207 7.009 7.003 7.008 6.023 6.158 6.085 6.184 6.090 7.225 6.453 6.146 6.652 5.270 6.540 - 6.228 5.653 7.014 5.254 5.035 7.000 7.000 7.000 6.023 6.158 6.085 6.184 6.090 9.225 6.453 6.146 6.652 5.270 6.540 - 6.228 5.653 7.014 5.254 5.000 7.000 7.000 7.000 6.003 6.165 6.831 6.170 7.097 6.334 7.612 5.090 6.094 6.663 5.913 5.713 7.139 5.204 5.133 7.130 7.000 7.000 7.000 6.003 6.165 6.831 6.170 7.097 6.334 7.612 5.090 6.094 6.663 5.913 5.713 7.139 5.204 5.133 7.130 7.000 7.																						
47 7.544 7.590 7.520 6.627 6.398 6.600 1 5179 7.480 6.523 6.500 5.297 5.370 5.010 6.111 5.177 6.618 6.554 7.520 5.940 5.230 6.181 7.14 7.200 7.214 7.202 6.407 6.495 7.173 6.913 7.132 5.436 6.777 6.628 7.058 7.052 6.957 6.536 6.406 6.416 6.646 6.4913 6.118 7.14 7.12 6.018 6.558 7.058 7.070 7.07																						
48. 7526 7571 7655 6487 6558 7304 6703 7450 5506 6774 6421 6716 7052 6957 6155 6460 6464 5818 7142 5486 5387 7. 49. 7099 7090 7080 6003 6158 6985 6184 6999 5225 6453 6146 6652 5270 6540 6228 56563 7041 5254 5150 7098 7072 7109 6080 6165 6831 6717 6976 5374 6102 5990 6494 683 5362 6216 6.252 56567 6313 5313 5329 68 527 7118 6395 6432 6121 6299 7061 6868 7078 7078 7078 7078 7078 7079 7079 707																						
499 7,209 7,214 7202 6,407 6,409 7,173 6,913 7,132 5,436 6,777 6,928 7,058 7,129 6,875 - 6,440 5,818 7,142 5,480 5,325 1,40 6,50 7,709 7,009 7,000 7,000 7,000 7,000 6,000 6,185 6,863 1,6717 6,976 5,347 6,162 5,590 6,944 5,362 6,616 - 6,225 5,657 6,913 5,313 5,313 5,313 5,313 5,313 1,314 7,314 6,025 5,889 7,204 6,665 5,712 7,006 1,36 6,265 7,014 6,600 6,320 5,901 5,713 7,319 5,204 5,317 5,55 7,118 6,895 6,42 6,12 6,259 7,061 6,880 7,045 6,55 7,518 7,009 5,461 5,318 6,309 6,404 5,800 8,809																						
51 7,098 7072 7109 6080 6165 6831 6717 6976 5347 6162 5690 6494 5362 6216 - 6225 6577 6913 5313 5329 657 7611 541 7124 6025 5889 7240 6665 7152 7063 6136 5265 714 6966 6494 6689 5913 5713 7139 5204 5317 533 713 718 6895 6432 6121 6259 7061 6880 7045 5338 6379 6644 6871 5885 6838 - 6272 5718 7099 5461 5334 78 585 5871 8658 871 872 872 872 872 872 872 872 872 872 872	49																					
52 7.041 7.134 7.124 6.025 5.889 7.204 6.065 7.152 7.063 6.136 6.265 7.014 6.966 6.946 6.639 5.913 5.713 7.139 5.204 6.353 7.515 7.515 7.715 7.715 6.059 5.061 6.534 7.065 7.716 7.715 7.715 7.715 7.700 7.700 7.805 8.080 8.074 5.338 6.79 6.644 8.671 8.885 8.081 8.092 8.561 8.077 7.765 8.046 8.294 8.05 7.000 7.000 7.700 7.000 7.700 7.000																						
53 7118 6895 6432 6121 6229 7061 6880 7045 5338 6379 6644 6871 5885 6838 - 6272 5718 7099 545 5337 775 540 5334 78 55 7767 775 7767 775 787 787 787 787 787 787 787 787 78																						
55 8.719 8.19 8.09 8.509 8.509 8.509 8.501 8.071 8.650 8.714 8.072 6.93 8.02 6.704 - 7.854 8.064 8.82 7.924 8.753 8.751 7.750 7.705																						
56 7767 7783 7871 7500 7811 7822 7702 7693 7862 7904 - 7864 7882 7924 7755 7733 7738 7780 7900 7720 775 59 6571 6712 6865 6665 6796 6400 5325 6637 5329 - 6373 6279 6704 6600 6823 6502 4979 5469 5427 550 6750 6750 6751 6712 6865 6665 6796 6400 5325 6637 5329 - 6373 6279 6704 6600 6823 6502 4979 5469 5427 540 540 540 540 540 540 540 540 540 540																						
58 5990 (6281 5894 6096 6808 5846 4931 5890 5696 - 5633 5710 6012 6010 6096 5579 5656 5000 5377 576 5656 5065 5656 5769 6409 5325 6637 5329 - 5633 5710 6012 6010 6096 5757 5656 5000 5377 576 5868 5795 572 5914 5987 5926 6009 5986 5895 5917 5948 5914 5900 5956 5982 5948 5882 5995 5888 5726 5886 576 5865 6500 5300 6750 644 6144 6105 6477 - 6833 6295 5825 5876 5885 5732 6864 6032 6342 6565 6259 520 6679 6844 6144 6105 6477 - 6833 627 5725 5865 5000 5377 575 5980 5978 5980 5980 5980 5980 5980 5980 5980 598																						
60 6952 5724 5914 5987 5926 6009 5986 5895 5917 5948 5941 5900 5956 5982 5948 5882 5999 5888 5726 5808 5306 6009 5846 6008 5200 6679 6844 6134 6105 6427 - 6833 6279 5258 565 5255 66 63 7876 878 878 8798 7978 7988 7970 7989 7061 7818 7873 7870 7972 7910 7928 7940 7855 7837 7871 - 7967 7939 7616 7811 7753 7876 7870 8970 8938 8933 8972 8971 8739 8850 8746 8443 8750 8805 6802 8628 5865 8667 3467 8368 3401 8540 8-8 678 8970 8938 8933 8972 8971 8739 8850 8746 8443 8750 8825 8729 8735 8728 8761 8962 8821 8062 8707 8365 877 8770 9970 9970 9980 9980 9980 9980		.5990	.6281	.5894	.6096	.6808	.5846	.4931	.5890	.5696	-	-	.5633	.5710	.6012	.6010	.6096	.5579	.5656	.5000	.5377	.5131
61 6951 5885 7904 7906 7906 7907 47951 7835 7980 7972 7910 7928 7904 7855 7837 7871 - 967 7909 7914 7951 7835 7807 7972 7910 7928 7904 7855 7837 7871 - 967 7909 7909 7908 7016 7811 7753 78 65 8653 8689 8766 8478 8488 8626 8723 8746 8408 8760 8506 8692 8628 88563 8667 8467 8537 8683 8401 8500 8867 8970 8980 8983 8933 8972 8921 8739 8850 8746 8443 8750 8506 8692 8628 8758 8667 8467 8537 8683 8401 8500 8868 9685 9713 9600 9232 9207 9301 9335 9344 7264 9329 9339 9154 9207 9377 - 8427 8905 8937 8950 7756 92 7995 9980 9980 9980 9803 9803 9808 9808 9878 9841 9870 9813 9870 9815 9927 9377 - 8427 8905 8937 8950 7756 92 7978 9716 7854 8759 8809 8879 8918 9829 9918 9819 8929 9910 8871 8828 8908 8909 8491 8911 8772 8788 8800 8705 8479 9026 8836 8879 8576 8693 88 8858 8957 8758 8759 8758 8693 8891 8819 8579 8758 8759 8758 8693 8891 8872 8875 8758 8693 8691 8918 9779 8999 8772 8827 8805 8704 8688 843 8615 8829 9012 8845 8706 8862 8738 8802 8763 8708 8728 8754 888 9857 976 976 9760 9909 9375 8675 9367 9367 9569 9569 9599 969 9357 8675 9767 978 999 9798 9810 925 9025 9025 9025 9025 9025 9025 9025																						
63 7958 7961 7906 7974 7951 7835 7980 7972 7910 7928 7940 7855 7837 7871 - 7967 7939 7516 7811 7753 7865 865 865 865 865 867 8878 878 8878 8																						
65 8653 8689 8766 8478 8488 8626 8723 8746 8408 8760 8596 8692 8628 8563 8667 8467 8572 8583 8401 8540 8547 867 8976 8988 8938 8978 8978 9918 9885 8746 8443 8759 8825 8729 8735 8728 8751 8821 8602 8777 8365 87 868 8985 9956 9956 9980 9959 9803 9830 9885 9869 9879 9818 19870 9831 914 9207 9377 - 8427 8905 8987 8950 7756 7757 7999 7617 7854 8163 8103 7663 8038 7565 7741 8099 8070 7596 7552 7676 7772 8110 8134 7388 7179 7516 776 7894 8163 8103 7663 8038 7565 7741 8099 8070 7596 7552 7676 7772 8101 8134 7388 7179 7516 776 876 8769 8799 9903 8999 8772 8827 8809 8879 8911 8772 8788 8809 8715 8772 8788 8979 8990 8772 8827 8805 8704 8645 8812 886 8959 9914 8911 8772 8788 8809 8705 8749 9026 8836 8879 8576 8693 848 8957 974 9575 9090 9357 8672 9367 9550 8953 9637 9527 7978 9115 9250 9025 9086 9819 784 874 8759 976 976 9760 9709 9357 8672 9367 9550 8953 9637 9527 7978 9115 9250 9025 9086 8348 8425 8425 8425 8425 8425 8425 8425 84																						
67 8970 8938 8933 8972 8921 8739 8850 8746 8443 8750 8825 8729 8715 8728 8761 8962 8821 8062 8707 8365 876 8 9685 9956 9950 9959 9803 9830 9888 9869 9879 9481 9870 9831 9876 9870 9796 9883 9821 9605 9282 9860 9362 99 75 7999 7617 7854 8163 8103 7663 8038 7565 7741 8099 8070 7596 7552 7676 7772 8101 8134 7788 7193 7516 76 83 8782 9036 8829 9105 8871 8828 8968 8909 8491 8911 8772 8788 8800 870 8799 9026 8885 8879 8576 8693 84 8 8790 8608 8813 8763 8787 8724 8759 8718 8701 8705 8758 8691 8691 8725 8732 8788 8800 7394 8465 8512 88 8 9857 9947 9575 9909 9373 8672 9367 9550 8953 9637 9527 7787 9115 9250 9025 9908 8766 8348 7450 7852 9 1 8326 8445 8344 8423 8427 8303 8363 8303 842 8349 8339 8335 8358 8364 8507 8319 8289 8266 899 1 8726 8423 8427 8803 8767 9703 9676 9696 9486 9496 9697 9699 9708 9681 9734 9624 9290 9584 9445 9 9 872 879 8824 8744 8753 8750 8765 8710 8586 8747 8725 8746 8759 8756 8744 8759 8694 8731 8889 8750 8670 878 9 8804 8823 8772 8561 8775 8865 8867 8672 8871 8689 8686 8746 8817 8813 8804 8778 8897 8744 8759 8694 8794 9874 9874 9874 9874 9874 9874 98																						
72 9956 9980 9959 9803 9880 9889 9869 9879 9481 9870 9831 9876 9870 9796 9883 9821 9605 9282 9860 9362 98 75 7999 7617 7854 8163 8103 7663 8038 7656 7741 8099 8070 7596 7552 7676 7772 920 84 8790 8068 8829 9105 8871 8828 8968 8999 8491 8911 8772 8788 8800 8705 8479 9026 8836 8879 8576 8693 84 8 8790 8068 8813 8763 8787 8724 8759 8718 8701 8705 8758 8691 8691 8722 8732 8788 8800 734 8465 8512 88 8 9857 9908 8772 8827 8805 8704 8688 8643 8615 8829 9012 8843 8760 8862 8738 8802 8763 8708 8728 8734 888 8 9857 9947 9575 9090 9357 8672 9367 9550 8953 9637 9527 7978 9115 9250 9025 9098 8760 8348 7450 7852 9 9 8864 8456 8344 8423 8427 8303 8353 8304 8323 8330 8329 8358 8355 8364 8507 8319 8289 8266 879 9 879 8824 8744 8753 8750 8765 8710 8586 8747 8725 8744 8759 8766 8744 8759 8694 8731 8899 8750 8670 878 9 8804 8823 8772 8561 8775 8855 8826 8762 8801 8689 8746 8817 8813 8804 878 8807 8744 9027 8756 8764 874 8759 8766 8764 874 8759 8768 8744 8759 8768 8744 8749 8027 8778 8716 8725 869 8774 8716 8725 8790 8784 8745 9029 9784 978 879 8824 8770 8867 8678 8678 8678 8778 8716 8725 8698 8716 8758 879 878 872 8675 8675 8678 872 8778 8716 8725 8698 8771 8867 8678 872 8778 8716 8725 8698 8716 8758 8778 8716 8725 8698 8717 8867 8678 872 8778 8716 8725 8798 872 872 872 872 872 872 872 872 872 87																						
75 7999 7617 7854 8163 8103 7663 8038 7565 7741 8099 8.070 7596 7552 7676 7772 8101 8134 7388 7193 7516 76 883 8878 876 8693 898 878 876 8693 898 878 876 8693 898 879 876 8693 898 879 876 8693 898 879 876 8693 898 879 877 8873 8891 8872 8778 8791 8771 8772 8778 888 8800 8703 8899 8772 8827 8805 8704 8688 8643 8615 8829 9012 8845 8760 8862 8738 8802 8760 8348 7450 7852 879 8797 9757 9909 9373 8707 9373 909 9373 8767 9370 9373 9709 9713 9709 9713 9709 9713 9709 972 972 972 972 972 972 972 972 972 97																						
83 8782 9036 8929 9105 8871 8828 8968 8909 8491 8911 8772 8788 8800 8705 8479 9026 8836 8879 8576 8693 881 84 8790 8608 8813 8763 8787 8724 8759 8718 8701 8705 8758 8691 8691 8725 8732 8732 8788 8690 7934 8465 8512 86 85 9037 8899 8772 8827 8805 8704 8688 8643 8615 8829 9012 8845 8760 8862 8738 8802 8760 8348 7450 7852 9714 9757 9909 9357 8672 9367 9550 8953 9637 9527 7978 9115 9250 9025 9908 8760 8348 7450 7852 9714 9767 9676 9676 9760 9731 9679 9703 9676 9669 9486 - 9697 9699 9708 9681 - 9734 9624 9290 9584 9445 96 97 8799 8824 8744 8753 8750 8765 8710 8586 8747 8725 8744 8759 8756 8744 8759 8694 8731 8889 8750 8670 879 879 8804 8824 8744 8753 8750 8764 7706 7576 7658 7251 7710 7524 7675 7814 7727 7468 7143 789 878 98 8804 8823 8772 8561 8775 8855 8826 8762 8804 8781 8813 8804 8778 8807 8748 9027 8756 8797 879 8804 8823 8772 8561 8775 8855 8826 8762 8801 8689 8746 8813 881 8804 8778 8807 8748 9027 8756 8797 879 870 8695 8675 8687 8716 8725 8691 8672 8778 879 8785 8603 8506 8730 8667 8695 8708 6976 8727 8699 8686 8714 8793 8682 8408 8742 8442 8910 8610 870 8793 8792 9789 9918 9920 9919 9909 9909 9904 9922 9920 9915 9915 9912 9912 9913 9913																						
848 8790 8608 8813 8763 8787 8724 8759 8718 8701 8705 8758 8691 8691 8725 8732 8788 8690 .7934 9465 8512 88 8 9857 9747 9575 9090 9357 8672 9367 9550 8953 9637 9527 7978 9115 9250 9025 9098 8760 .8348 7450 7852 9 91 8326 8456 8344 8423 8427 8303 8363 8300 8425 8349 8339 .8330 8298 8358 .8355 8364 .8507 .8319 .8298 .8266 837 976 9760 9760 9700 9703 9676 9660 9486 - 9697 9699 9708 9681 9734 9624 9920 9584 9445 .94 97 8799 8804 8744 8753 8750 .8765 8710 8586 .8747 8725 8744 .8759 .8754 8741 .8759 .8694 .8731 .8889 .8750 .8676 .87 98 7.524 7.351 7.597 7.645 .7775 .7606 .7558 .7364 .7706 .7576 .7658 .7251 .7710 .7524 .7675 .7814 .7727 .7468 .713 .7398 .77 100 8699 8804 8823 .8772 .8561 .8775 .8855 .8862 .8762 .8801 .8689 .8746 .8817 .8813 .8804 .8758 .8807 .8743 .9027 .8756 .8797 .87 100 8699 .8645 .8657 .8716 .8725 .8691 .8672 .8717 .8607 .8701 .8685 .8508 .8661 .8666 .8697 .874 .8740 .8857 .8640 .8513 .81 102 8635 .8532 .8749 .8528 .8698 .8448 .8566 .8591 .8474 .8426																						
85 9037 8990 8772 8827 8805 8704 8688 8643 8615 8829 9012 8845 8760 8862 8738 8802 8763 8708 8728 8754 875 991 8326 8456 8344 8423 8427 8303 8363 8300 8425 8349 8339 8330 8298 8358 8355 8364 8807 8319 8289 8266 82 9767 8799 9767 9766 9760 9731 9679 9703 9676 9696 9486 — 9697 9699 9708 9681 — 9734 9624 9290 9584 9445 978 7879 879 879 879 879 879 879 875 874 874 8753 8750 8765 8710 8865 8710 8858 8747 8725 8744 8759 879 879 875 874 874 875 876 876 871 879 879 879 8824 8744 8753 8750 8745 870 870 870 879 879 8824 8744 8753 8750 8745 870 870 870 870 870 870 870 870 870 870																						
91 8326 8456 8344 8423 8427 8303 8363 8300 8425 849 8339 8330 8298 8358 8355 8364 8507 8319 8289 8266 827 8707 8707 8707 8707 8707 8707 8707																						
95 9767 9766 9760 9731 9679 9703 9676 9969 9486 9969 9699 9708 9681 - 9734 9624 9290 9584 9445 96 97 8799 8824 8734 8753 8750 8765 8710 8586 8747 8725 8744 8759 8756 8744 8759 8769 8894 8731 8889 8750 8670 87 98 8804 8823 8772 8561 8775 8766 7585 7364 7706 7576 7658 7251 7710 7524 7675 7814 7727 7468 7143 7398 77 99 8804 8823 8772 8861 8775 8855 8826 8762 8801 8698 8746 8817 8813 8804 8778 8807 8743 9027 8756 8797 87 101 8455 8755 8667 8716 8725 8691 8672 8717 8607 8701 8685 8508 8661 8663 8697 8747 8740 8587 8640 8513 81 102 8635 8732 8749 8528 8689 8448 8566 8591 8474 8426 - 8433 8432 8492 8528 8401 8221 8331 8318 83 103 9738 - 9742 9768 9752 9728 9703 9683 9728 9722 9740 9710 9725 9726 - 9764 9756 9342 9933 9718 9918 9921 9920 9913 9920 9911 9890 9920 9904 9922 9920 99915 9915 9910 9913 9912 9912 9913 9920 9914 9890 9920 9904 9922 9920 99915 9915 9910 9913 9912 9912 9913 9920 9913 9920 9914 9920 9914 9922 9920 9934 9922 9920 9934 9921 9920 9913 9920 9914 9920 994 9922 9920 9937 9937 9937 9340 8710 8725 8726 8728 8728 8728 8728 8728 8728 8728	88																					
97 8.794 8.824 8.744 8.753 8.750 8.765 8.710 8.586 8.747 8.725 8.744 8.759 8.756 8.744 8.759 8.694 8.731 8.889 8.750 8.670 8.798 99 8.804 8.731 8.853 8.750 8.670 8.754 7.735 7.754 7.755 7.606 7.558 7.364 7.706 7.576 7.658 7.251 7.710 7.524 7.675 7.814 7.727 7.468 7.143 7.739 7.739 7.739 7.739 8.730 8.823 8.772 8.561 8.775 8.855 8.862 8.762 8.801 8.689 8.746 8.817 8.813 8.814 8.804 8.778 8.807 8.748 9.072 8.756 8.757 8.855 8.862 8.762 8.801 8.689 8.746 8.817 8.813 8.804 8.778 8.807 8.748 9.072 8.755 8.755 8.687 8.755 8.687 8.667 8.695 8.708 6.976 8.727 8.689 8.666 8.661 8.663 8.697 8.747 8.740 8.858 8.640 8.513 8.000																						
98																						
99																						
101 8.455 8.755 8.603 8.506 8.730 8.667 8.695 8.708 6.976 8.727 8.689 8.686 8.714 8.793 8.682 8.408 8.742 8.442 8.910 8.610 8.858 8.832 8.432																						
102 8635 8.532 8.749 8.528 8.689 8.448 8.566 8.591 8.474 8.426 8.433 8.432 8.490 8.528 8.401 8.221 8.331 8.318 8.103 9.738 9.742 9.768 9.752 9.728 9.703 9.683 9.728 9.732 9.740 9.710 9.725 9.726 9.764 9.756 9.342 9.233 7.779 9.779 9.779 9.779 9.789 9.791 9.791 9.792 9.791 9.791 9.791 9.725 9.726 9.764 9.756 9.342 9.233 7.779 9.739 9.789 9.739 9.740 7.391 7.390 7.382 7.391 7.390 7.383 7.308 7.234 7.236 7.330 7.331 7.391 7.399 7.399 7.403 7.391 7.401 7.397 7.398 7.390 7.382 7.391 7.390 7.383 7.308 7.234 7.236 7.330 7.331 7.351 4.559 4.64 4.755 1.709 4.379 4.530 2.929 3.875 4.515 3.399 3.458 1.795 4.103 3.055 3.3115 5.626 6.623 6.624 6.614 4.755 6.605 6.233 - 6.258 6.271 6.309 6.277 6.286 6.293 6.098 6.387 6.143 6.250 6.204 6.294 6.294 6.295 6.204 6.293 6.256 6.204 6.294 6.295 6.204 6.295 6.204 6.295 6.205	100	.8699	.8675	.8687	.8716	.8725	.8691	.8672	.8717	.8607	.8701	.8685	.8508	.8661	.8663	.8697	.8747	.8740	.8587	.8640	.8513	.8651
1918 9903 9918 9921 9920 9913 9920 9913 9920 9914 9920 9914 9922 9920 9915 9915 9915 9915 9915 9916 9912 9918 9918 9921 9920 9913 9920 9914 9920 9904 9922 9920 9915 9915 9915 9915 9916 9912 9918 9910 9918 9921 9918 9921 9918 9921 9918 9921 9918 9921 9918 9921 9918 9921 9918 9921 9918 9921 9918 9921 9920 9904 9922 9920 9915 9915 9915 9918 9912 9912 9913 9910 9918 9921 9938 9330 7403 7391 7398 7398 7382 7391 7399 7383 7308 7234 7236 7330																						
104 9918 9903 9918 9921 9920 9913 9920 9911 9890 9920 9904 9922 9920 9915 9905 9913 9912 9912 9913 9912 9913 9913 9912 9913 9910 7017 7392 7387 7399 7390 7382 7391 7390 7383 7308 7234 7236 7330 7330 7330 7330 7330 7330 7330 73																						
107 .73927387 .7399 .7390 .7403 .7391 .7401 .7397 .7398 .7390 .7382 .7391 .7390 .7383 .7308 .7234 .7236 .7330 .7311 .9456 .9370 .9418 .9557 .9517 .9162 .9519 .9196 .9129 .9250 .9320 .9231 .9225 .9172 .9337 .9399 .9544 .8756 .8951 .8865 .931 .8365 .814 .4549 .3177 .3531 .4659 .4164 .4755 .1709 .43794530 .2291 .3875 .4215 .3399 .3458 .1795 .4103 .3055 .34 .115 .6280 .6235 .6236 .6144 .6250 .6301 .6310 .6258 .6505 .62336258 .6271 .6309 .6277 .6286 .6293 .6098 .6387 .6143 .65 .117 .9843 .9817 .9872 .9883 .9879 .9885 .9849 .9851 .9461 .9863 .9857 .9846 .9858 .9825 .9869 .9869 .9836 .9665 .9658 .9484 .97 .6297 .6296 .6296 .6226 .6293 .6256 .6203 .6293 .6256 .6306 .6211 .6252 .6169 .6220 .5931 .5945 .5883 .62 .121 .7405 .6646 .7430 .7269 .7238 .7372 .7419 .7405																						
112			-																			
115 6.280 6.285 6.263 6.144 6.250 6.301 6.310 6.258 6.505 6.233 - 6.258 6.271 6.309 6.277 6.286 6.293 6.098 6.387 6.143 6.501 6.147 9.884 9.881 9.887 9.885 9.884 9.8851 9.461 9.863 9.857 9.846 9.885 9.869 9.869 9.869 9.869 9.865 9.865 9.865 9.868 9.865 9.865 9.865 9.868 9.865 9.865 9.868 9.865 9.865 9.868 9.869 9.731 5.945 9.832	111	.9456	.9370	.9418	.9557	.9517	.9162	.9519	.9196	.9129	.9250	.9320	.9231	.9225	.9172	.9337	.9539	.9544	.8756	.8951	.8865	.9173
117 9843 9817 9872 9883 9879 9885 9849 9851 9461 9863 9857 9846 9858 9825 9869 9869 9836 9665 9658 9484 97 120 66297 66296 662																						
120																						
121 .7405 .6646 .7430 .7269 .7238 .7372 .7419 .74057358 .7360 .7377 .7286 .72397321 .7044 .3791 .7301 .5343 .73 122 .8497 .8372 .8483 .8553 .8566 .8434 .8480 .8405 .8275 .8473 .8472 .8407 .8468 .8415 .8439 .8512 .8476 .8361 .8289 .8382 .83 123 .8321 .8351 .8357 .8362 .8451 .8348 .8369 .8325 .8134 .8396 .8387 .8263 .8393 .8356 .8391 .8382 .8454 .8307 .7974 .8278 .83 124 .8367 .8291 .8420 .8501 .8500 .8356 .8483 .8476 .8155 .8333 .8369 .8376 .8313 .8413 .8405 .8442 .8483 .8150 .8083 .8304 .84 126 .5933 .5957 .5622 .6140 .6288 .5867 .6032 .6097 .5865 .5575 .5913 .5820 .5755 .5842 .6053 .6047 .6120 .6042 .5850 .5665 .61 127 .9696 .9698 .9706 .9794 .9778 .9648 .9709 .9630 .9857 .9732 .9746 .9664 .9668 .9657 .9752 .9780 .9702 .9631 .9642 .9642 .96 128 .9806 .9751 .9751 .9849 .9799 .9709 .973 .9703 .9669 .9782 .9760 .9717 .9679 .9690 .9763 .9856 .9775 .9451 .9748 .9642 .96 129 .9941 .9921 .9886 .9878 .9858 .9870 .9724 .9893 .9799 .8878 .9795 .9862 .9917 .9925 .9913 .9909 .866 .9941 .9822 .9925 .93 134 .9167 .7958 .9038 .8772 .8896 .7810 .8080 .7791 .6077 .9132 .7776 .7036 .6591 .6715 .7299 .8851 .7657 .213 .8332 .4399 .73 136 .5077 .5373 .5280 .6721 .6649 .5144 .6277 .5765 .5104 .5292 .5764 .4991 .5115 .50456663 .5831 .5052 .5160 .4811 .51 137 .3176 .3594 .3697 .3591 .3579 .3330 .3555 .3636 .3473 .3185 .3009 .3200 .3327 .3073 .3421 .3797 .3479 .3500 .3000 .3170 .32 142 .5219 .5302 .5404 .4812 .5185 .5333 .5476 .5435 .5331 .5336 .5362 .5513 .5505 .5450 .5297 .5641 .4732 .5309 .5564 .5388 .5143 .9933 .9336 .9365 .9388 .9284 .9376 .9358 .9164 .9403 .9400 .9214 .9328 .9363 .9291 .9373 .9408 .9590 .9291 .9239 .92 145 .9946 .9931 .9884 .9865 .9923 .9879 .9821 .9798 .75579651 .9882 .9363 .9291 .9373 .9408 .9590 .9291 .9239 .92 146 .9937 .9943 .9856 .9557 .5757 .5450 .4845 .5333 .5476 .5435 .5331 .5336 .5362 .5513 .5505 .5450 .5297 .5614 .4732 .5309 .5564 .5388 .5144 .9933 .9366 .9369 .9386 .9388 .9284 .9376 .9338 .9484 .9403 .9400 .9214 .9328 .9363 .9291 .9373 .9408 .9590 .9291 .9239 .92 145 .9946 .9931 .9934																						
122																						
124		.8497																				
126 .5933 .5957 .5622 .6140 .6288 .5867 .6032 .6097 .5865 .5575 .5913 .5820 .5755 .5842 .6083 .6047 .6020 .6042 .5850 .5665 .617 .9696 .9698 .9706 .9794 .9778 .9648 .9709 .9630 .9587 .9732 .9746 .9664 .9668 .9657 .9752 .9780 .9702 .9613 .9642 .992 128 .9806 .9751 .9751 .9849 .9799 .9709 .9717 .9763 .9856 .9775 .9451 .9748 .9642 .99 129 .9941 .9921 .9886 .9878 .9858 .9799 .9878 .9795 .9862 .9917 .9925 .9913 .9909 .9866 .9941 .9882 .9727 .9777 .9776 .0366 .6991 .7928 .9886 .9811 .9880 .97919 .0077 .932 .77776	123																					
127 9.696 9.698 9.976 9.974 9.978 9.648 9.979 9.630 9.587 9.732 9.746 9.664 9.668 9.657 9.752 9.780 9.702 9.631 9.642																						
128																						
129 9941 9921 9886 9878 9858 9870 9724 9893 9799 9878 9795 9862 9917 9925 9913 9909 9866 9941 9882 9925 97 136 9167 7958 9038 8772 8896 7810 8080 7791 6077 9132 7776 7036 6591 6715 7299 8851 7657 3213 8332 5439 77 136 5507 5373 5280 6721 6649 5144 6277 5765 5104 5292 5764 4991 5115 5045 - 6663 5831 5052 5160 4811 51 137 3176 3594 3697 3591 3579 3330 3555 3636 3473 3185 3009 3200 3327 3073 3421 3797 3479 3500 3000 3170 37 139 9074 9049 9085 9070 9082 9028 9095 9050 9035 9029 9092 9021 8998 9016 9039 9071 9041 8887 8945 8988 9016 5302 5404 4812 5185 5333 5476 5435 5331 5336 5362 5513 5505 5450 5297 5641 4732 5309 5564 5358 551 43 9333 9336 9405 9386 9388 9284 9376 9358 9164 9403 9400 9214 9328 9363 9291 9373 9408 9590 9291 9239 97 145 9946 9931 9884 9865 9923 9879 9821 9798 7557 - 9651 9882 9830 9811 9958 9927 9516 8963 8902 9370 9814 9936 9939 9939 9939 9939 9939 9939 993																						
134 9,167 7,958 9,038 8,772 8,896 7,810 8,080 7,791 6,077 9,132 7,776 7,036 6,591 6,715 7,299 8,851 7,657 3,213 8,332 5,439 7,731 1,030 1,																						
137 3176 3594 3697 3591 3579 3330 3555 3636 3473 3185 3009 3200 3327 3073 3421 3797 3479 3500 3000 3170 32 31 39 9074 9049 9085 9070 9082 9025 9059 9059 9059 9059 9059 9059 905	134	.9167																				
139 .9074 .9049 .9085 .9070 .9082 .9025 .9050 .9035 .9029 .9021 .8998 .9016 .9039 .9071 .9041 .8887 .8945 .8988 .904 142 .5219 .5302 .5404 .4812 .5185 .5333 .5435 .5313 .5306 .5450 .5297 .5641 .4732 .5309 .5564 .5388 .5284 .9876 .9388 .9284 .9376 .9385 .9164 .9403 .9406 .931 .9884 .9865 .9923 .9879 .9821 .9798 .7557 - .9651 .9882 .9830 .9811 .9958 .9927 .9516 .8963 .8902 .9370 .9988 .9889 .9891 .9319 .9880 .9881 .9889 .9881 .9889 .9991 .9889 .9991 .9889 .9991 .9889 .9991 .9889 .9991 .9881 .9989 .9891 .9981 .9889																						
142 .5219 .5302 .5404 .4812 .5185 .5333 .5476 .5435 .5331 .5336 .5362 .5513 .5505 .5450 .5297 .5641 .4732 .5309 .5564 .5358 .55143 .9333 .9336 .936 .9405 .9386 .9388 .9284 .9376 .9358 .9164 .9403 .9400 .9214 .9328 .9363 .9291 .9373 .9408 .9590 .9291 .9239 .927 .9406 .9931 .9884 .9865 .9923 .9879 .9821 .9798 .7557 - 9651 .9882 .9830 .9811 .9958 .9927 .9516 .8963 .8902 .9370 .9931 .9894 .98963 .9902 .9370 .9932 .9425 .9513 .9312 .9263 .9418 .9476 .9550 .9552 .8820 .8970 .8983 .9946 .9936 .																						
143 .9336 .9405 .9386 .9388 .9284 .9376 .9403 .9400 .9214 .9328 .9291 .9373 .9408 .9990 .9291 .9284 .9376 .9538 .9164 .9400 .9214 .9328 .9291 .9333 .9429 .9291 .9291 .9294 .9506 .9806 .9802 .9370 .9821 .9828 .9830 .9811 .9958 .9927 .9516 .8903 .8902 .9700 .8839 .9821 .9788 .9839 .9821 .9788 .9582 .9830 .9811 .9946 .9959 .9516 .8907 .9801 .8983 .981 .9869 .9863 .9821 .9798 .9870 .8983 .9883 .981 .9869 .9863 .9818 .9476 .9550 .9552 .8820 .8970 .8983 .981 .9984 .9983 .9883 .9883 .9883 .9883 .9883 .9883 .9883 .9883 .9883 .988																						
145 .9946 .9931 .9884 .9865 .9923 .9879 .9821 .9798 .7557 - .9651 .9882 .9830 .9811 .9958 .9927 .9516 .8963 .8902 .9370 .9514 .9958 .9927 .9516 .8963 .8902 .9370 .9514 .9550 .9552 .8820 .8970 .8983 .9928 .9362 .9418 .9476 .9550 .9552 .8820 .8970 .8983 .9948 .9560 .9564 .9569 .9563 .9418 .9476 .9550 .9552 .8820 .8970 .8983 .9488 .9569 .9681 .9659 .9681 .9659 .9681 .9659 .9681 .9659 .9681 .9659 .9681 .9659 .9681 .9659 .9681 .9659 .9681 .9659 .9681 .9659 .9681 .9681 .9659																						
146 .9527 .9430 .9565 .9575 .9345 .9634 .9479 .9332 .9425 .9513 .9312 .9263 .9418 .9476 .9550 .9552 .8820 .8970 .8983 .94 147 .5690 .5487 .5819 .5575 .5702 .5503 .5672 .5729 .5503 .5627 .5727 .5614 .5505 .5555 .5623 .5837 .5862 .5837 .5862 .5214 .5186 .5225 .56 150 .9659 .96635 .9647 .9678 .9688 .9699 .9680 .9681 - .9713 .9700 .9679 .9678 .96 151 .8517 .8309 .8800 .7675 .7637 .7248 .7664 .7359 .6981 .7429 .7090 .7008 - .7422 .7380 .6812 .7447 .6869 .73 154 .5718 .5930 .5661 .6043 .6016 .5688 .4750 .5953 .6106 .5910 .5681 .5609 .5909																						
150 .9659 .9635 .9647 .9675 .9689 .9687 .9665 .9684 .9709 .9648 .9688 .9699 .9680 .9681 - .9713 .9700 .9679 .9677 .9678 .967 .9671 .9678 .967 151 .8517 .8309 .8800 .7675 .7637 .7248 .7664 .7359 .6981 .7448 .7208 .7239 .7090 .7008 - .7422 .7380 .6812 .7447 .6869 .735 154 .5718 .5930 .5661 .6043 .6016 .5688 .4750 .5953 .6106 .5910 .5681 .5609 .5901 .5749 .5706 .5824 .5853 .5211 .5390 .5503 .543		.9527																				
151 .8517 .8309 .8800 .7675 .7637 .7248 .7664 .7359 .6981 .7448 .7208 .7239 .7090 .70087422 .7380 .6812 .7447 .6869 .7518 .5718 .5930 .5661 .6043 .6016 .5688 .4750 .5953 .6106 .5910 .5681 .5609 .5901 .5749 .5706 .5824 .5853 .5211 .5390 .5503 .54																						
154 .5718 .5930 .5661 .6043 .6016 .5688 .4750 .5953 .6106 .5910 .5681 .5609 .5901 .5749 .5706 .5824 .5853 .5211 .5390 .5503 .5-																						
	131	.,,+1	.1370	.,,55	.,01/	.,,,00	.,,560	.,,,,,,,	.,550	.0223	.,,23	. 1003	., 554	.,,,,,,,	.1501	.1311	.,,62	.,,,,	. 1020	.0,07	., 517	., 550

```
1026
                                 159 .9617
                                                              .9611 .9596 .9631 .9606 .9628 .9582 .9557 .9607
                                                                                                                                             .9584 .9586 .9578 .9584 .9603 .9421 .8288 .9343 .9390 .9577
                                                               .9011 9390 9031 9009 9052 9382 9337 9007 - .9384 9388 9378 9384 
6265 6436 6462 6277 6387 6410 6391 6039 6379 6242 6215 6312 
.8237 .8260 .8244 .8241 .8255 .8253 .8249 .8254 .8251 .8259 .8238 .8236 -
1027
                                 160
                                         .6396
                                                      .6385
                                                                                                                                                                                .6426\ .6334\ .6091\ .6128\ .6152\ .6419
                                 163
                                         .8243
                                                      8239
                                                                                                                                                                                .8270 .8236 .8140 .8068 .8157 .8249
                                                               .9482 .9502 .9482 .9449 .9471 .9467 .9444 .9469 .9460 .9469 .9460 .9448 .9455 .9485 .9489 .9431 .9467 .9408 .9461
                                  164
                                         .9493
                                 166
                                         .9868
                                                      .9837
                                                               .9885.9864.9866.9848.9876.9839.9841.9856.9858.9858.9858.9849.9830.9854.9906.9841.9841.9841.9841.9832.9841
                                                                                                                                            .9439 .9603 .9531 -
                                                      .9557
                                                               .9459 .9677 .9652 .9448 .9350 .9502 .9079 -
                                                                                                                                                                              .9669 .9488 .9624 .8934 .9344 .9130
                                 167
                                         .9565
                                                                .3926 .3859 .3844 .3851 .3986 .3692 .4027 .3779 .3945 .3590 .3726 .3920 .3912 .3949 .3935 .3926 .4058 .3972 .3880
                                  168
                                         .3915
                                                              .9274 .9210 .9218 .9246 .9253 .9249 .9107 .9242 .9241 .9224 .9249 .9249 .9246 .9229 .9129 .9114 .9148 .8999 .9233 .9819 .9449 .9568 .9569 .9535 .9564 .8195 .9542 .9367 .9456 .9522 .9500 .9465 .9460 .8841 .6248 .9222 .6516 .9208
                                 169
                                         .9327
                                                      .9285
1031
                                 170
                                         .9911
                                                      .9847
                                 171
                                         .9612
                                                      9125
                                                               .9652 .9246 .9169 .8550 .8751 .8555 .8318 .8680 .8744 .8518 .8465 .8325 -
                                                                                                                                                                                .9238 .8577 .7527 .8433 .7804 .8554
                                                               9776 9474 9469 9494 9713 9519 7543 9719 9683 9537 9395 9586 9505 9533 936 7634 9013 7879 9504 9815 7220 7188 6122 7159 6287 6082 7372 5958 5930 5981 6201 7246 6449 4977 5782 5392 6015
                                 173
                                         .9828
                                                      .9696
                                  174
1033
                                         .9941
                                                     .6140
                                                               .6595 .6325 .6152 .5708 .5945 .5741 .5611 .6330 - .5745 .5760 .5706 .596 .5891 .6123 .6111 .5763 .5751 .5712 .4357 .5648 .5524 .5710 .5822 .5635 - .9948 .9942 .9949 .9941 .9920 .9940 .9880 .9957 .9924 .9935 .9941 .9915 -
                                 175
                                         .9088
                                                                                                                                             .5745 .5760 .5706 .5965 .6393 .6057 .5558 .5802 .5582 .5745
                                                                                                                                                                                .6011 .6166 .4845 .5989 .5071 .5718 .9947 .9940 .9896 .9946 .7259 .9927
                                          .5995
                                  177
                                                      .5821
                                  180
                                         .9949
1035
                                 182
183
                                                              . 9295 .9235 .9381 .9012 .8606 .9147 .9131 .8937 - . .8980 .9049 .9154 - . .9361 .9038 .8646 .7853 .8919 .8924 .9172 .9132 .9105 .8938 .9288 .8992 .9184 .9078 .9129 .9205 .9011 .9178 .9294 .9279 .9221 .9041 .8447 .9068 .9169
                                         .9211
                                                      9380
                                         .9129
                                                      .8913
1036
                                                               .7217 .7233 .7230 .7181 .7217 .7087 .7205 .7240 .7245 .7194 .7175 .7171 .7216 .7221 .7198 .7125 .7145 .7188 .7174
                                 185
                                         .7213
1037
                                 186
187
                                         .7811
                                                               .7004 .5778 .5166 .6549 .5081 .5953 .4919 .5344 -
                                                                                                                                            .6126 .6532 .5874 .4925 .6027 .5498 .7868 .5556 .5191 .5339
1038
                                                                9785 .9789 .9794 .9783 .9789 .9786 .9754 .9794 .9793 .9780 .9790 .9789 .9793 .9781 .9803 .9798 .9799 .9780 .9790
                                  193
                                         .9800
                                                              7406 7611 7622 7708 7777 8002 7976 8045 7980 7984 7974 7982 - 9309 9311 7954 9310 7973 7975
                                                      .9766
                                 194
                                         1.000
1039
                                  195
                                         .7590
1040
                                 196
197
                                         .9292
                                                              9309 9298 9308 8012 7973 8002 7976 8045 7980 7984 7974 7982 - 9309 9311 7954 9310 7973 7975 5102 5362 5358 5084 5348 5157 4508 - 4737 4693 4859 5014 5270 4729 4169 4065 4351 3504
                                         .5284
                                                      .5244
1041
                                                               .8165 .8144 .8084 .8125 .8141 .8109 .8131 .8128 .8146 .8078 .8130 .8136 .8114 .8089 .8111 .8129 .8167 .7984 .8110
                                  198
                                         .8090
                                                              .9898 .8610 .8647 .9527 .9761 .9674 .8551 .9907 .9734 .9211 .8722 .8560 .9607 .8659 .8262 .6801 .8814 .7515 .9517 .8474 .8627 .8624 .8581 .8534 .8553 .8502 .8526 .8471 .8540 .8575 .8648 .8616 .8744 .8698 .8507 .8602 .8575 .8494
                                 199
                                         9950
                                                      9248
1042
                                 200
                                         .8551
                                                      .8689
                                                                .8760 .8836 .8774 .8496 .8487 .8507 .8328 .8787 .8504 .8489 .8475 .8464 .8509 .8870 .8827 .8581 .8372 .8420 .8474
                                 201
                                         .8796
1043
                                                              . 9156 .6044 .7900 .8606 .9138 .8889 .5547 .8866 .9089 .8570 .7952 .7808 .8821 .8959 .7083 .2794 .7277 .3841 .8446 .9038 .8579 .8134 .8727 .9106 .9005 .5530 - .8706 .8567 .7966 .7695 .8762 .8770 .7101 .2800 .7153 .3822 .8453 .7360 .7292 .7349 .7343 .7331 .7259 .7349 - .7384 .7267 .7372 .7376 .7350 .7343 .7326 .7328 .7203 .7279 .7159
                                 203
                                         9388
                                                      7733
1044
                                         .9371
                                 204
                                                      .7835
                                 206
                                         .7318
                                                               .7370 .7435 .7431 .6068 .7361 .7348 .7393   - .7344 .7342 .7380 .7312 .7374 .7355 .7450 .7203 .7234 .7332 .7298 .9849 .9643 .9709 .9745 .9759 .9722 .8842 .9739 .9706 .9652 .9724 .9597   - .9650 .9102 .6940 .9508 .8760 .9740 .7240 .8632 .8643 .6152 .6691 .5917 .7645 .6248 .5827 .5856 .5818 .6226   - .8638 .7412 .6035 .6783 .6066 .5729
                                 207
                                         7388
                                                      7361
                                         .9854
                                 208
                                                      .9766
                                 209
                                         .8332
                                                               .9872 .9867 .9883 .9867 .9871 .9865 .9821 .9871 .9864 .9878 .9861 .9850 .9872 .9876 .9852 .9819 .9866 .9707 .9865 .8325 .8213 .8128 .7241 .7123 .6677 .7392 .8125 .7360 .7291 .7097 .7015 .7149 .8332 .8204 .6256 .8276 .6158 .6939
1047
                                 210
                                         9861
                                                      9847
                                 211
                                         .8289
                                                      .7993
                                 213
                                         .9722
                                                      .9713
                                                               .9693\ .9660\ .9680\ .9615\ .9642\ .9577\ .9383\ .9637\ .9643\ .9602\ .9647\ .9660\ \ -\ \ .9688\ .9655\ .9775\ .9625\ .9620\ .9593
                                                               .9653 .9572 .8718 .8445 .8523 .8467 .8330 .8523 .8555 .8407 .8483 .8438 .8578 .8622 .8350 .8650 .8340 .8457 .9557 .9400 .9595 .9563 .9555 .9377 .9575 .9495 .9542 .9610 .9503 .9468 .9502 .9472 .9425 .9600 .9498 .9512
                                 214
                                         .8648
                                                      .8408
                                 215
                                         .9653
                                 216
217
                                                               .7633.7488.7428.7643.7668.7592.6900.7615.7445.7692.7580.7662.7650.7533.7490.7492.7600.6218.7577.9667.9610.9520.9623.9490.9600.9455 - .9588.9642.9592 - .9625.9580.9500.9600.9572.9505
                                         .7553
                                                      7535
1050
                                                                                                                                                                                .9625 .9580 .9500 .9600 .9572 .9505
                                         .9650
                                                      .9623
                                                               .8727 .7807 .7855 .8477 .8333 .8298 .6793 .8218 .7977 .8347 .8397 .8385 .8180 .7945 .7603 .8238 .8050 .8257 .8332
                                 218
                                         .7902
                                 219
220
                                         .9809
.6308
                                                               .9988 .9630 .9907 .9923 .9802 .9948 .9880 .9812 .9793 .9914 .9991 .9935 .9926 .9861 .9796 .9861 1.000 .9772 .9864 .6328 .6203 .6189 .6300 .6276 .6290 .6116 .6277 .6259 .6220 .6190 .6284 - .6192 .6112 .5680 .5863 .5964 .6263
                                                      9917
1052
                                                      .6162
                                 221
222
                                         .9843
                                                                .9893 .9805 .9803 .9832 .9817 .9826 .9613 .9833 .9814 .9807 .9786 .9767
                                                                                                                                                                                 .9795 .9701 .8369 .9668 .9034 .9798
1053
                                         .9428
                                                              .9426 .9459 .9466 .9194 .9276 .9250 .9273 .9386 .9279 .9148 .8991 .9252 .9325 .9458 .9456 .7785 .9112 .8502 .9185 .9699 .9695 .9695 .9697 .9691 .9681 .9619 - .9625 .9694 .9697 .9699 - .9694 .9638 .9583 .9656 .9635 .9682
                                                      .9124
1054
                                 224
                                         .9690
                                                      .9704
                                                               9969 1.000 1.000 .9809 .9965 .9845 .9979 .9998 .9773 .9829 .9730 .9893 .9893 1.000 1.000 .9964 .8788 .9504 .9822 .7312 .7514 .7508 .7338 .7500 .7481 .7309 .7312 .7407 .7323 .7335 .7328 - .7464 .7407 .7237 .7249 .7295 .7459
                                 225
226
                                         .9989
.7475
1055
                                                      .7472
                                 227
                                                               .7898 .7715 .8533 .8240 .8115 .8060 .7035 .8125 .7360 .7717 .8038 .7850 .7804 .7640 .7804 .6531 .7781 .7379 .7167
                                          .8408
                                                      .7850
1056
                                 228
229
                                          .7054
                                                      .7215
                                                              .7294 .5958 .6510 .6981 .6921 .6938 .2073 .7077 .6335 .6310 .6606 .6769 .6927 .5781 .6269 .4640 .6250 .3869 .6348 .8583 .8033 .8896 .8717 .8473 .8531 .7575 .8740 .8140 .8123 .8388 .8550 .8260 .8125 .7952 .8125 .8312 .7979 .7917
                                         .8752
1057
                                                      .8456
                                                               .8964 .8995 .9063 .8939 .9019 .9032 .8875 .8894 .8998 .8958 .8958 .8916 .9016 .9012 .9038 .8824 .8739 .8905 .8989
                                 230
                                         .9053
                                                      .8898
1058
                                 231
232
                                                              9871 9824 9825 9779 9835 9571 9785 9698 9805 9868 9811 - 9831 9801 9582 9795 9810 9807 9442 9479 9440 9374 9483 9431 9369 9337 9452 9303 9474 9466 9408 9481 9500 9408 9507 9439 9446
                                         .9913
                                                      9867
                                         .9466
                                                      .9437
1059
                                 234
                                         .9668
                                                               .9677 .9745 .9667 .9669 .9671 .9663 .9295 .9685 .9632 .9694 .9679 .9646 .9707 .9712 .9703 .9565 .9616 .8715 .9661
                                 235
                                         .9330
                                                      .9291
                                                              .9336 .9381 .9351 .9273 .9309 .9183 .9324 .9339 .9183 .9336 .9363 .9291 .9381 .9375 .9357 .9324 .9369 .9258 .9318 .8846 .8856 .8880 .8820 .8978 .8867 .8978 .8824 .8969 .8907 .8920 .8999 .8912 .8773 .8941 .8871 .8914 .8835 .8909
1060
                                 236
                                         .8937
                                                      .8816
                                 237
                                         .8943
                                                               .8989\ .9151\ .9016\ .8989\ .8959\ .8975\ .8779\ .8986\ .8945\ .9005\ .8989\ .9021\ .8957\ .9110\ .8913\ .9027\ .8904\ .8854\ .8995
                                 238
239
                                         .9940
                                                      .9938
                                                              .9943 .9414 .9913 .9950 .9935 .9942 .9807 .9929 .9937 .9929 .9947 .9937 .9943 .9509 .9879 .9281 .9909 .9854 .9927 .8892 .8766 .8797 .8684 .8809 .8710 .8538 .8698 .8654 .8610 .8583 .8480 .8744 .8807 .8852 .7294 .8686 .7987 .8632
                                         .8860
                                                      .8771
                                 240
243
                                                              .9887 .9824 .9860 .9854 .9914 .9882 .9808 .9904 .9853 .9853 .9845 .9881 .9878 .9818 .9732 .8815 .9534 .9569 .9841 .7452 .7556 .7782 .7291 .7547 .7585 .7492 .7205 .7532 .7305 .7333 .7436 .7401 .7587 .7628 .6973 .7006 .7217 .7473
                                         .9885
                                         .7345
                                                      .8043
                                                               .8632 .8645 .8613 .8932 .8537 .8720 .6768 .8537 .7953 .8926 .8970 .8831 .8645 .8616 .8515 .8711 .8673 .8657 .8720
                                 246
                                         .8635
                                                      .8294
1064
                                 249
250
                                         .9268
                                                              9216 9189 9223 9179 9204 9192 9191 9175 9192 9163 9203 9198 9179 9234 9218 9213 9239 9178 7902 9795 9715 9711 9741 9765 9696 9688 9779 9774 8180 9726 9735 9625 9741 9367 7705 7757 9221 9746
                                                      .9283
1065
                                         .9802
                                 251
                                         .8375
.9104
                                                               .8824 .7922 .7858 .6600 .7196 .6488 .6475 .7416 .7168 .6581 .6596 .6601 .6840 .7983 .7490 .5718 .6640 .6227 .6429
                                                              .9131 .9142 .9135 .8993 .8959 .9045 .8612 .9040 .8947 .8979 .8923 .8868 .9125 .9162 .9086 .8367 .9075 .8654 .8953 .9190 .9149 .9202 .9199 .9137 .9188 .7957 .8986 .9059 .9185 .9130 .9130 .9110 .9177 .9196 .8297 .8896 .8420 .9052
                                 253
                                                      .9051
                                 254
                                         .9277
                                                      .9042
1067
                                 255
                                                               .9262 .9313 .9293 .9277 .9280 .9250 .9340 .9219 .9282 .9215 .9251 .9333 .9224 .9295 .9340 .9295 .9246 .9280 .9297
                                         .9304
                                                               .9168 .9131 .9204 .9168 .9080 .9250 .8729 .8978 .9080 .9166 .9285 .9289 - .9994 .9998 .9997 .9991 .9996 .9989 .9997 .9995 .9993 .9988 .9992 -
                                                                                                                                                                               .9166 .9154 .8621 .9028 .8966 .9066 .8539 .9997 .9268 .9991 .9750 .9990
                                 256
                                         .9220
                                                      .9457
                                 260
                                         .9996
                                                      .9992
                                                               9388 9523 9467 9386 9393 9383 9399 9304 9346 9374 9397 9373 9407 9461 9330 9191 9175 9301 9389 8310 9558 9529 8735 9493 9456 7730 - 8410 8787 9078 9475 9591 9428 7972 8480 8504 9354
                                 263
                                         .9320
                                                      .9404
                                 264
265
                                         .9437
                                                      .9329
1070
                                                               .8360 .8407 .8340 .8303 .8330 .8223 .7017 .8163 .8053 .8347 .8317 .8353 .8187 .8440 .8247 .8360 .8250 .8217 .8350
                                         .8377
                                                      .8313
                                         .7250
.7512
.9588
                                 266
                                                               .7297 .7467 .7430 .7250 .7123 .7123 .7227 .7187 .7303 .7273 .7307 .7087 .7130 .7433 .7450 .7350 .7250 .7250 .7230 .7113 .7558 .7794 .7911 .7536 .7632 .6769 .5748 .7606 .7539 .7326 .7465 .7477 .7741 .7805 .7654 .7253 .7532 .4896 .7424
1071
                                                      .7200
                                 268
273
                                                      .7482
1072
                                                                .9638 .9454 .9524 .9309 .9471 .9357 .9154 .9463 .9330 .9329 .9287 .9337 .9410 .9424 .9316 .9161 .8820 .9112 .9315
                                 274
275
                                                               .9678 .9702 .9718 .9685 .9674 .9662 .9678 .9662 .9705 .9686 .9689 .9672 - .9712 .9717 .9677 .9714 .9522 .9670 .7973 .7962 .8057 .7925 .8005 .8002 .7988 .7931 .8005 .7913 .7914 .7906 .7917 .8031 .7968 .7944 .7793 .7840 .7977 .9981 .9784 .9900 .9964 .9962 .9967 .8820 .9962 .9927 .9953 .9985 .9968 .9967 .9081 .9675 .9982 .9855 .9800 .9932
                                         .9674
                                                      .9695
                                                                                                                                                                                .9712\ .9717\ .9677\ .9714\ .9522\ .9670
1073
                                         .7969
.9974
                                                      .7976
                                 276
1074
                                 277
278
                                                               .9896 .9952 .9949 .9867 .9894 .9840 .9756 .9910 .9915 .9842 .9840 .9876 .9883 .9953 .9964 .9382 .9500 .9745 .9811 .9861 .9915 .9952 .9842 .9858 .9807 .9353 .9871 .9858 .9814 .9830 .9814 .9847 .9974 .9929 .9571 .9563 .9727 .9759
                                         9921
                                                      9815
1075
                                         .9873
                                                      .9783
                                 279
                                                               .6814 .6921 .6924 .6956 .6932 .6924 .6350 .6870 .6938 .6952 .6904 .6921 .6852 .6858 .6929 .6971 .6607 .6836 .6927
                                         .6692
1076
                                 282
283
                                                               .5102\ .5103\ .5170\ .5026\ .5153\ .5070\ .4751\ .4803\ .5033\ .4988\ .4934\ .5023\ .5151\ .5147\ .5090\ .4357\ .4777\ .4660\ .5139\ .9762\ .9763\ .9774\ .9773\ .9782\ .9676\ .9791\ .9782\ .9740\ .9783\ .9748\ .9796\ .9715\ .9757\ .9745\ .9791\ .9797\ .9728\ .9762
                                         5243
                                                      4937
                                         .9778
                                                      .9799
1077
                                 284
                                         .8024
                                                               .8576\ .7604\ .7529\ .8235\ .7824\ .8439\ .7820\ .8133\ .7784\ .8043\ .7945\ .7757\ .8024\ .7812\ .7278\ .7596\ .7294\ .7165\ .7976
                                                              - . .6974 .7088 .6985 .7184 .7005 .6393 - - . .6870 .6910 .6869 - .6960 .6271 .5742 .6741 .6341 .6992 .6713 .6519 .6617 .6434 .6537 .6457 - .6500 .6519 .6412 .6169 .6143 - .6519 .6159 .2455 .6310 .3154 .6433
                                 285
                                         .7718
                                                      .7384
1078
                                 287
                                         .6774
1079
                                                     .9349 .9773 .9958 .9965 .9341 .9797 .9282 .9096 .9889 .9839 .9274 .9189 .9253 .9606 .9982 .9930 .6868 .9249 .8440 .9205 .8931 .9050 .9025 .8998 .9078 .9013 .9056 .9006 .9072 .8978 .9072 .9049 .8998 .9088 .9041 .9001 .8950 .9056 .9032 .9040
                                         .9877
                                         .8990
```

```
      290
      .8624
      .8659
      .8664 .8541 .8596 .8557 .8611 .8588 .8625 .8624 .8609 .8602 .8613 .8609 .8498 .8495 .8510 .8628 .8510 .8637 .8119

      291
      .3283
      .3435 .3329 .3392 .3391 .3351 .3330 .3355 .3346 .3311 .3326 .3349 .3390 .3384 .3374 .3481 .3372 .3367 .3560 .3377 .3338

      292
      .8752 .8762 .8522 .8626 .8369 .8438 .8587 .8642 .8561 .8569 .8551 .8504 .8569 .8555 .8564 .8499 .8173 .8291 .8620 .8410 .8590 .8587

      294
      .8753 .8745 .8745 .8972 .8878 .9043 .8954 .9014 .9087 .8962 - - .8859 .8728 .8836 .8819 .8898 .8802 .8450 .8708 .8578 .8145

      296
      .7448 .7435 .7393 .7500 .7534 .7268 .7234 .7211 .7517 .7298 .7220 .7190 .7280 .7198 .7260 .7339 .7386 .7045 .7710 .6881 .7212

      298
      .6363 .6119 .6127 .6362 .6073 .5867 .5819 .5617 .5823 .6065 .5515 .5327 .5498 .5552 .5746 .5550 .6360 .6329 .5481 .6562 .4879 .5648

      299
      .6327 .5924 .6265 .6242 .6315 .5779 .5517 .5586 .3430 .5942 .5327 .5498 .5752 .5395 .5498 .6295 .6335 .5306 .6337 .5336 .5337 .5235 .5331

      300
      .6034 .6305 .5984 .5984 .6083 .6031 .5982 .5928 .5957 .5987 .5672 .5912 .5591 .55915 .6002 .5138 .5825 .6247 .5859 .5960 .5437 .5908
```

Table 11: Detailed results (average RMSE) for all regression datasets over all methods. Due to space constraints, dataset IDs from Ye et al. (2024a) are used in place of dataset names. "XGB", "RF", "LG", "RN", "ND", "ST", "TG", "DAN", "FTT", "DCN", "TT", "PT", "EF", and "TR" denote "XGBoost", "Random Forest", "LightGBM", "ResNet", "NODE", "SwitchTab", "TANGOS", "DANets", "FT-T", "DCNv2", "PTaRL", "Excelformer" and "TabR", respectively.

ID	M-NCA	L-NCA	TR	XGB	CGB	MLP	FTT	DCN	ND	MP	EF	DAN	TG	ST	LG	RF	SVM	KNN	SW	PT
1 (×10 ³)	.6383	.4786																		
$2(\times 10)$.1002											.4977					.2380			
$3(\times 10^{-5})$	0.000	437.8												5003.				0.000		
$4(\times 10^{-5})$	0.000			111.0													Inf			Inf
$6(\times 10)$ $7(\times 10^{-3})$.2106 .1576	.2123										.3206					.1696			
$9(\times 10^3)$.7892	.7739																		
13×10^2	.1143	.1152																		
14×10^3	.4549	.4593																		.4572
15 (×10)	.4574	.4622																		
$16 (\times 10)$.2892	.3072																		.3006
20	.6006	.6404																		
21	.5555											2.496								
22×10^{-1} 24×10^{3}	.4420 .4618	.1828 .4782																		
24×10^{-1} 25×10^{4}	.1245	.1317																		
26×10^{3}	.3655	.3678																		
30	.2011	.2293																		
31	.2342	.2259	.2262	.2691	.2592	.2228	.2625	.2171	.3034	.2243	.2603	2.297	.2100	.2587	.2711	.2856	.3459	.3148	.5101	.2129
32	.2445	.2198																		
33	.2449																			.2514
34 35 (×10)	.2483 .1487																			.2456
38×10^{5}	.4922											.6108								
41×10^3	.5250											4.049								.6726
54×10^2	.1735											.3016								
57 (×10)	.7280											.9422								
62	.4688	.4866																		
64	.2510	.2598																		
66 (×10 ⁻¹)	.2629	.4044																		
69 70	.4293 .2011	.4292 .2007																		
71	.3148																			.3138
73 (×10)	1.063																			1.322
74	.7224	-	.9062	.7055	.7070	.9059	.7158	.8344	.7371	.8890	.7193	1.140	.8121	.8318	.7078	.7168	.8272	.8311	1.036	.7902
76×10^2	.7057	.7131																		
$77 (\times 10^3)$.4135	.4026																		
$78 (\times 10^5)$.1563											3.268					.3027			
$79 (\times 10^4)$.6636	.6932												-			1.384			
80×10^{5}	.2513	.4257															.3290			
81 (×10 ⁴)	.3750	.6091															1.465			
82×10^{-1}	.9290	.8924																		
86×10^5 87×10^3	.8508 .7965	.9156 .8100																		.7946
89×10^2	.4025	.4025															.4488			
$90 (\times 10^2)$.1642	.1651																		
$90(\times 10^{-1})$ $92(\times 10^{2})$.1552	.1561																		
93 (×10)	.5423											.3286								
94	.4283	.4273										.6890								
96 (×10)	.3083	.3320																		.3474
105	.4245											.5468								
106×10^2 108×10	.2903 .4414											.2923								
108 (×10) 109 (×10)	.1923											.4692								
110 (×10)	1.038											3.713					1.838			
$113 (\times 10)$.5990	.8794	-	1.047	.9139	.9958	1.265	1.929	.8625	.6186	-	12.59	.9678	-			3.120			
$114 (\times 10^{-1})$		1.076																		
116	.4668											.9514								
118	.6260	.5809																		
119 125 (×10)	.6110 .1613	.6137 .6764										.9056								
130×10^{-1}		.9082																		
$131 (\times 10^3)$.3510	.3949										.4632								
132 (×10)	.4463	.4237										.4712								
133 (×10)	.3099	.2584																		

```
1134
                                                   135 (\times 10^3)
                                                                                                        5.419 \;\; 9.373 \;.6753 \;.7938 \;\, 10.16 \;\, 10.15 \;\, 10.12 \;\, 9.828 \;\, 10.35 \;\, 10.01 \;\, 2.725 \;\, 9.682 \;\, 9.970 \;\, .5332 \;\, 1.041 \;\, 8.391 \;\, 4.593 \;\, 5.198 \;\, 3.016 \;\, 10.12 \;\, 9.828 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12 \;\, 10.12
1135
                                                 138 \times 10^{-1}
                                                                                                         1.205 .9079 1.147 1.028 1.788 1.100 1.253 2.356 1.352 1.131 3.963 2.026 1.159 1.172 1.478 2.956 2.405 3.885 1.358
                                                 140 (\times 10^{-1})
                                                                                      .7825
                                                                                                                         .7819\ .8101\ .7921\ .7892\ .7908\ .7857\ .7856\ .7883\ .7928\ 1.330\ .7862\ .8258\ .8097\ .8325\ .8596\ .9688\ 1.241\ .7782
1136
                                                 141 \times 10^{-1}
                                                                                      .2915
                                                                                                         .2944 .2925 .3009 .2878 .2973 .2863 .2876 - .2833 .2856 1.589 .2942 .2902 .3029 .3195 .4088 .4932 1.549 .2848
1137
                                                   144 (\times 10^2)
                                                                                                                        .2241 .2076 .2044 .2383 .2321 .2399 .2287 .2197 .2109 .5529 .2381 - .2043 .2023 .3030 .2264 .3482 .2328
                                                     148 (×10)
149
                                                                                                          3744
1138
                                                                                                         .1364 .1437 .1325 .1336 .1338 .1369 .1361 .1363 .1360 .1333 .3889 .1355 .1378 .1363 .1337 .1380 .1348 .2294 .1414
                                                                                       .1390
                                                                                                                          .3554 .3924 .3903 .4795 .4468 .4714 .4417 .4361 .3846 1.065 .4332
                                                             152
                                                                                                                                                                                                                                                                                               .4094 .4249 .4606 .4146 .5252 .4326
1139
                                                                                                                        . 35534 .3924 .3903 .4795 .4406 .4714 .4417 .4361 .3846 1.005 .4552 - .4094 .429 .4006 .4146 .322 .4326 .1573 .4826 .4380 1.609 1.626 1.619 1.624 1.634 1.636 .1618 1.630 1.628 .4658 .6438 1.000 .9348 1.007 .5151 .2334 .2404 .2365 .2492 .2331 .2475 .2503 .2441 .2396 1.746 .2539 .2463 .2298 .2526 1.011 .4781 1.711 .2494
                                                     153 (×10)
155 (×10)
                                                                                       .8053
                                                                                                         .9441
1140
                                                                                       .2416
                                                                                                         .2455
                                                     156 (×10)
                                                                                                                         .2779 .2777 .2713 .2911 .2846 .2944 .3058 .2942 .2900 1.742 .2941 .2919 .2743 .2934 1.021 .3635 1.727 .2920
1141
                                                                                                                        4341 3920 3895 4231 4097 4150 4212 4605 3981 5203 4152 4026 3911 3915 4851 4573 5010 3962 4243 3967 3959 3977 4081 4043 4156 4334 4186 6509 4012 4181 4044 4070 4426 4393 6487 3931
                                                             158
                                                                                       .3936
                                                                                                          3940
                                                     161 (×10)
                                                                                       .3971
1142
                                                 162 \times 10^{-1}
                                                                                      .6253
                                                                                                                         .7242\ .7196\ .6435\ .6504\ .6356\ .6548\ 1.192\ .6746\ .6881\ 1.492\ .6949\ .6425\ .6409\ .8302\ 1.393\ .6633\ 1.501\ .6776
                                                 165 \times 10^{-2}
1143
                                                                                     .1366
                                                                                                         .1372 \quad .1386 \quad .1388 \quad .1383 \quad .1381 \quad .1378 \quad .1389 \quad .1371 \quad .1389 \quad .1376 \quad .2338 \quad .1375 \quad .1374 \quad .1395 \quad .1399 \quad .1423 \quad .1410 \quad .2290 \quad .1379 \quad .1423 \quad .1410 \quad .2290 \quad .1379 \quad .1410 \quad .2290 \quad .1423 \quad .1410 \quad .2290 \quad .1410 \quad .2290 \quad .1410 \quad .2290 \quad .1423 \quad .1410 \quad .2290 \quad .1410 \quad .1410 \quad .2290 \quad .229
                                                172 \times 10^{-2}
                                                                                      .1862
                                                                                                                         .1844 .2340 .2030 .1868 .1827 .1850 .2230 .1844 .1868 .6717 .1898
                                                                                                                                                                                                                                                                                               .2310 .2815 .2899 .3703 .6556 .1867
1144
                                                                                                                        7884 7721 7728 8141 7978 8070 7958 7991 8034 1.402 8151 8033 7698 7872 1.091 9369 1.312 8044 1.017 1.079 1.010 1.022 1.009 1.010 1.007 1.007 1.006 4.949 1.041 - 1.063 1.395 2.643 1.854 4.945 1.026
                                                             176
                                                                                        .7874
                                                    178 (×10)
1145
                                                                                      .1011
                                                                                                         .1093
                                                                                                                          .1758 .1281 .1315 .1821 .1763 .1765 .1761 .1761 .1762 .1376 .1779 .1763 .1281 .1299 .1570 .1441 .1534 .1542
                                                             179
1146
                                                             181
                                                                                                                         15.39 .5704 .5220 15.39 15.48 16.33 15.54 15.61 15.15 .6482 15.62
                                                                                                                                                                                                                                                                                               .5932 .7295 .9492 1.014 2.165 .5564
                                                                                       1.304
                                                                                                         1.411
                                                   184 \, (\times 10^4)
                                                                                       4699
                                                                                                         4492
                                                                                                                         .4650 .4650 .4736 .4798 .4616 .4874 .4677 .5330 .5255 1.310 .4869 .4605 .4696 .4535 .6506 .5315 1.284 .4763
1147
                                                   188 \, (\times 10^5)
                                                                                       .3102
                                                                                                         .3452 .3054 .3136 .2994 .3175 .3067 .3133 .3483 .3138 .3216 .5458 .3187 - .3098 .3278 .4819 .3623 .5397 .3158
1148
                                                   189 (\times 10^5)
                                                                                       2954
                                                                                                         .3130 .2922 .2871 .2847 .2971 .2907 .2979 .2996 .2901 .2860 1.004 .2981 .2926 .2846 .2891 .4797 .3154 .5345 .2968
                                                   190 \, (\times 10^6)
                                                                                       .1255
                                                                                                         .1490 .1423 .1396 .1177 .1382 .1193 .1309 .1376 .1272 .1368 .4149 .1413 - .1359 .1485 .2406 .1714 .3928 .1394
1149
                                                                                                                        .4214 .4797 .4546 .5200 .4796 .5019 .5426 .5016 .4838 1.167 .5205 .5117 .4665 .5247 .7140 .6000 1.148 .5128
                                                   191 (\times 10^5)
                                                                                       4291
                                                                                                         4469
1150
                                                   192 (\times 10^7)
                                                                                       .1225
                                                                                                         .1373 .1108 .1020 .1117 .1113 .1081 .1176 .1045 .1083 .1079 .1510 .1138 .1098 .1027 .1141 .1120 .1121 .1598 .1148
                                                202 (×10<sup>-1</sup>)
                                                                                      .6968
                                                                                                         .8805 .6639 1.321 .9017 .6877 .6736 .6677 .9350 .6559 .6924 4.072 .7158 .6857 1.215 1.492 2.054 1.205 2.620 .6781
1151
                                                205 (×10<sup>-5</sup>)
212
                                                                                                         87.82 22.92 1453. 1.618 751.2 24.46 63.69 63.91 92.98 81.79 Inf 414.3 83.63 .0015 0.000 Inf Inf Inf 205.1
                                                                                      1830.
                                                                                                                         .4440 .5918 .4109 .6367 .5507 .5745 .4221 .4719 .5490 22.68 .6340 .7251 .4351 .6579 2.353 2.487 16.72 .6655
                                                                                       .4331
1152
                                                223 (\times 10^{-2})
                                                                                     2.739
                                                                                                                         2.797 19.28 8.548 2.867 3.095 1.624 .9159 2.650 3.633 1181. 23.81
                                                                                                                                                                                                                                                                                             11.38 9.087 497.5 147.8 1037. 9.693
1153
                                                                                                                         . 1341 .1423 .1397 .1393 .1330 .1395 .1321 - - . 1329 .1369 .1331 .1412 .1350 .1317 .1416 .1332 .1464 .2236 .4775 .4189 .2436 .2158 .2208 .4421 .2249 .6091 4.051 .2533 - .5038 .5424 3.057 .8922 4.170 .2520
                                                             233
                                                                                       .1537
                                                                                                          1537
                                                    241 (×10)
                                                                                       .2328
                                                                                                          3402
1154
                                                     242 (×10)
                                                                                                                         .2322 .4383 .3669 .2578 .2216 .2306 .4418 .2365 .2560 5.338 .2561
                                                                                                                                                                                                                                                                                             .4576 .4984 3.095 .9333 4.170 .4549
                                                244 (\times 10^{-2})
                                                                                                                         .5905\ .7873\ .6453\ .8170\ .7535\ .6531\ .8634\ .6826\ .7819\ 2.941\ .8971
                                                                                                                                                                                                                                                                                               .7804 .7914 2.608 2.567 2.939 .7009
1155
                                                                                                                         .3308 .3304 .3281 .3341 .3285 .3321 - . .3306 .3273 .5563 .3366 .3331 .3279 .3272 .4440 .3768 .5517 .3300 .1172 .1136 .1062 .1162 .1239 .1172 .1122 .1210 .1179 .1731 .1169 .1211 .1244 .1154 .1427 .1112 .1711 .1126
                                                     245 (\times 10)
                                                                                       3258
                                                                                                          3263
1156
                                                    247 (\times 10)
                                                                                       .1381
                                                                                                          .1417
                                                                                                                           .9483 .9030 .8619 .8886 .9068 1.029 .8567 .8900 .9064 1.310 .8802 .9175 .8791 .8597 .9821 .9643 1.256 .9469
                                                                                       1.027
1157
                                                                                                                         .7274 .7033 .6682 .6889 .7274 .6992 .8339 .6688 .6973 3.361 .6850 .6870 .6900 .7221 1.226 .7109 2.170 .7165 .7812 .7245 .7331 .7747 .7234 .7457 .7300 - .8272 .8312 .8148 .7634 .7037 .7073 .8879 .7962 .8328 .7344
                                                             252
                                                                                       6112
                                                                                                          6935
                                                             257
                                                                                       .7146
1158
                                                                                                                           .2974 .2658 .2637 .2658 .2760 .2642 .2622 .2820 .2628 .3244 .2616 .2665 .2639 .2707 .3041 .2641 .3109 .2608
                                                             258
                                                                                       .2607
1159
                                                             259
                                                                                       3147
                                                                                                          3168
                                                                                                                         .3185 .3161 .3127 .3526 .3222 .3452 .3173 .3397 .3197 .3980 .3233 .3329 .3150 .3188 .3882 .3344 .4023 .3197
                                                   261 \, (\times 10^2)
                                                                                                                         .1982 .2389 .2463 .2802 .1346 .2227 .2754 .2576 .1697 9.860 .2097 .1370 .2337 .2501 .1935 .2360 .4149 .1107
                                                                                      .1695
                                                                                                         .1429
1160
                                                262 (×10<sup>-1</sup>)
                                                                                                                         .9945\ 1.138\ 1.091\ .9784\ 1.017\ 1.057\ 1.319\ 1.078\ 1.032\ 2.037\ 1.028\ 1.035\ 1.109\ 1.191\ 1.400\ 1.269\ 1.983\ .9885
                                                                                      1.066
                                                                                                         1.084
                                                                                                                         .4005 1.081 .7602 .7415 .5087 .5442 .3696 .9050 .5609 35.41 1.629
                                                             267
                                                                                       .6202
                                                                                                                                                                                                                                                                                               1.067 1.353 4.958 2.945 33.25 .8614
1161
                                                                                                                         .6899\ .8361\ .7969\ .7572\ .7649\ .8194\ .6973\ .7282\ .7382\ 11.82\ .7656\ .7821\ .9136\ .9651\ 2.132\ .7345\ 6.730\ .9068
                                                             269
                                                                                       .6791
                                                                                                          .6675
1162
                                                   270 \, (\times 10^2)
                                                                                                                         .1694\ .2236\ .1835\ .1986\ .1887\ .1873\ .1868\ .1779\ .1955\ .1996\ .2058\ .2042\ .1843\ .1802\ .2187\ .1911\ .2000\ .2180
                                                                                       .2059
                                                                                                          1941
                                                271 \times 10^{-1}
                                                                                                                         .1794\ .2185\ .2166\ .2102\ .2127\ .2234\ .3405\ .1659\ .2046\ .5677\ .2164\ .1766\ .2438\ .2471\ .4945\ .2065\ .5669\ .2371\ .7410\ .6877\ .6704\ .7739\ .7379\ .7452\ .7066\ .7262\ .7229\ .9334\ .6994\ .7920\ .6829\ .6827\ .8137\ .7717\ .8920\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ .7042\ 
                                                                                       .1986
1163
                                                             272
                                                                                       .7032
                                                                                                          .7452
1164
                                                280 (\times 10^{-1})
                                                                                                                         .3579 .3484 .3468 .3505 .3549 .6941 .3497 .3562 .3542 .3578 .3520
                                                                                                                                                                                                                                                                                               .3484 .3476 .3531 .3522 .3589 .3473
                                                                                      3491
                                                                                                          3496
                                                                                                                         .2772 .2857 .2816 .2126 .3062 .2185 .3295 .2608 .2692 15.71 .2141 .2738 .3103 .3163 .2884 .2989 4.244 .2395
1165
                                                   286 \, (\times 10^2)
                                                                                                                          .4162 .3802 .3821 .4796 .4212 .5103 .4293 .3904 .4253 .6248 .4703 .4547 .3851 .3898 .5630 .5163 .6112 .4748
                                                                                       .4147
                                                                                                         .1228 .1254 .1182 .1254 .1182 .1167 .1170 .1144 1.040 .1206 .1173 1.438 .1212 .1177 .1329 .1357 .1327 .2006 1.303 .1209 .2952 .2913 .2998 .2923 .2884 .2938 .2917 .3477 .2919 .2998 1.472 .2933 .2975 .3007 .3084 .3163 .3348 .6349 .2903
                                                     293 (\times 10)
                                                                                       1202
1166
                                                    295 (×10)
                                                                                       .2943
1167
                                                                                                          .6361 .6895 .6613 .6569 .7314 .7287 .7441
                                                                                                                                                                                                                          .7061 .7240 .9099 .7470 .7361 .6751 .6758 .7690 .6793 .9149 .7192
1168
```