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Fairness-aware Prompt Tuning for Graph Neural Networks

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Abstract

Graph prompt tuning has achieved significant success for its ability to effectively adapt pre-trained graph neural networks to various downstream tasks. However, the pre-trained models may learn discriminatory representation due to the inherent prejudice in graph-structured data. Existing graph prompt tuning overlooks such unfairness, leading to biased outputs towards certain demographic groups determined by sensitive attributes such as gender, age, and political ideology. To overcome this limitation, we propose a fairness-aware graph prompt tuning method to promote fairness while enhancing the generality of any pre-trained GNNs (named FPrompt). FPrompt introduces hybrid graph prompts to augment counterfactual data while aligning the pre-training and downstream tasks. It also applies edge modification to increase sensitivity heterophily. We provide a two-fold theoretical analysis: first, we demonstrate that FPrompt possesses universal capabilities in handling pre-trained GNN models across various pre-training strategies, ensuring its adaptability in different scenarios. Second, we show that FPrompt effectively reduces the upper bound of generalized statistical parity, thereby mitigating the bias of pre-trained models. Extensive experiments demonstrate that FPrompt outperforms baseline models in both accuracy and fairness (~33%) on benchmark datasets. Additionally, we introduce a new benchmark for transferable evaluation, showing that FPrompt achieves stateof-the-art generalization performance.

1 Introduction

Graph Neural Networks (GNNs) have been successfully applied across a wide range of domains, including social network analysis [5], anomaly detection [11, 12], and recommendation systems [16]. However, traditional GNNs often rely on large amounts of labeled data, which can be scarce in real-world applications [43]. Furthermore, these models frequently struggle with poor generalization when faced with out-of-distribution data [34]. To address these limitations, researchers have increasingly explored pre-training and fine-tuning strategies for GNNs [22], inspired by the success of similar approaches in natural language processing [24]. In this paradigm, a GNN is pre-trained on a massive corpus of graph datasets, then fine-tuned for specific downstream tasks, leveraging the knowledge acquired during pre-training.

While pre-training and fine-tuning on graphs have shown promising results, there are still several challenges. One significant issue is the gap between pre-training objectives, such as edge prediction in self-supervised tasks [14] and the goals of downstream tasks like node or graph classification [22]. This misalignment often leads to sub-optimal performance during fine-tuning [19]. Additionally, pretrained models are prone to catastrophic forgetting when adapted to new tasks, where the model forgets previously learned knowledge during the fine-tuning process [42].

In response to these challenges, prompt tuning has recently emerged as a compelling alternative for tuning pre-trained GNNs [9, 20, 27, 38]. Rather than fine-tuning model parameters, prompt tuning modifies the input data to better align with the downstream task, leaving the parameters of the pre-trained GNNs unchanged. For instance, GraphPrompt [20] pre-trains GNNs on link prediction tasks and adapts downstream node or graph classification tasks to this pre-training task format by introducing prompt-specific parameters such as class prototypes. This approach allows for efficient adaptation while preserving the integrity of the pre-trained model.

Despite its success, current graph prompt tuning techniques neglect the issue of bias present in pre-trained models. Bias can arise from the graph-structured data used during pre-training, as numerous studies have demonstrated that historical data often contains patterns of discrimination related to sensitive attributes like age, gender, race, and region [6, 23, 33]. Additionally, commonly used pre-trained GNN models such as GCN [17] and GAT [31] do not inherently address fairness, and their message-passing mechanisms may even amplify existing biases [26]. Our experiments in Table 2 further indicate that existing graph prompt tuning tends to exacerbate biases in pre-trained models. This largely limits the real-world applicability of graph prompt tuning in fairness-aware domains.

Therefore, a natural question is raised: can we develop fairnessaware graph prompt tuning that retains the benefits of efficient adaptation while ensuring fairness? Nevertheless, answering the above question is technically challenging: (i) Existing fairness approaches are often tailored to specific datasets, while in practice, the same pre-trained GNNs are expected to be adapted to various datasets without the need for further parameter tuning. Therefore, it is highly non-trivial to directly apply existing fairness methods to eliminate bias in pre-trained GNNs; and (ii) most existing fairness methods lack theoretical analysis [29], meaning they do not provide a practical guarantee, i.e., provable upper bounds on common fairness metrics such as statistical parity.

To address these issues, in this paper, we propose a fairnessaware graph prompt tuning method named FPrompt, that could alleviate bias in any pre-trained GNNs and enhance their adaptability at the same time. Specifically, FPrompt introduces hybrid graph prompts, which include both fixed and learnable prompts. The fixed prompts are designed to represent sensitive group embeddings, and their interaction with the original graph can be viewed as counterfactual data augmentation to mitigate bias. The learnable graph prompts, which adopt the token as graph prompt, effectively adapt the pre-trained model to different datasets. Additionally, FPrompt predicts the sensitive attributes of nodes and applies heterophilyenhanced edge modification based on the assignments. This process enhances information flow between nodes in different sensitive groups, thereby reducing the representational disparity across these groups. We provide a two-part theoretical analysis: (i) we establish that FPrompt exhibits a high degree of versatility in handling pretrained GNN models, regardless of the specific pre-training strategy employed. This flexibility ensures that FPrompt can be seamlessly

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integrated into a wide range of applications and use cases, adapt-117 ing to different scenarios with ease; and (ii) we demonstrate that 118 119 FPrompt can reduce the upper bound of generalized statistical parity, effectively addressing and mitigating the inherent biases present 120 in pre-trained models. To validate the cross-dataset fairness per-121 formance of different fine-tuning strategies, we construct a new 123 benchmark consisting of four real-world datasets. These datasets 124 share the same feature dimensions, which eliminates the potential 125 fairness impact caused by traditional cross-dataset generalization 126 experiments involving singular value decomposition operations. In summary, our main contributions are as follows: 127

- To the best of our knowledge, we are the first to propose a fairness-aware graph prompt tuning method that can mitigate bias in any pre-trained models and enhance their generalization ability at the same time;
- We provide theoretical analysis of standard fairness metrics for
 the pre-training and fine-tuning paradigm, establishing a solid
 theoretical foundation for FPrompt's performance; and
- We construct a new benchmark to evaluate the cross-dataset fairness performance of fine-tuning strategies. Extensive experiments on different scenarios demonstrate that FPrompt achieves state-of-the-art performance in both accuracy and fairness.

2 Related Work

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2.1 Graph Neural Networks

Graph Neural Networks (GNNs) have become the predominant 143 framework for learning on graph-structured data. They can be 144 broadly categorized as spectral- and spatial-based GNNs. Spectral-145 based GNNs rely on the graph Fourier transform, which operates 146 in the spectral domain of the graph Laplacian. The pioneering 147 work by Bruna et al. [2] introduced the concept of using graph 148 149 convolution in the spectral domain. This was later simplified in GCN [17], which approximates the spectral convolution opera-150 151 tion using 1-order Chebyshev polynomials to improve computa-152 tional efficiency. However, spectral methods typically depend on the eigen-decomposition of the graph Laplacian, making them less scal-153 able and limited to transductive learning. In contrast, spatial-based 154 155 GNNs define convolutions in the graph's spatial domain by aggregating features from a node's local neighborhood [8, 14, 31, 37]. 156 These models support inductive learning and offer better scalability 157 to large-scale graphs. 158

159 Traditional GNNs are typically trained in a supervised manner, requiring a substantial amount of labeled data. However, this re-160 161 liance on labeled data presents challenges in real-world applications, 162 where labels may be sparse or costly to obtain, and models often face poor transferability to new domains. Recently, unsupervised 163 graph representation learning has gained a lot of attraction. Early 164 attempts like DeepWalk [25] and node2vec [13], employ random 165 walks to transform graph learning into a sequence learning prob-166 lem. While these methods are scalable, they largely focus on local 167 168 neighborhoods, overlooking broader graph structures. To overcome these limitations, more recent approaches [32, 36, 39, 40] apply 169 contrastive learning techniques to maximize mutual information 170 between local and global node representations. This allows the mod-171 172 els to generate more meaningful, transferable embeddings without 173 labeled data, achieving competitive performance on tasks such as

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node classification and graph classification [3]. For example, GCL designs four types of graph augmentations to incorporate various priors [40]. GRACE takes the original graph as input and GNN model with its perturbed version as two encoders to obtain two correlated views for contrast [35].

2.2 Graph Prompt Tuning

Graph prompt tuning has gained significant attention due to its effectiveness in bridging the gap between pre-training and downstream objectives. Due to its parameter-efficient nature, graph prompt tuning has quickly become popular as an alternative to finetuning large pre-trained models, particularly in scenarios with limited downstream task labels [38]. For instance, GraphPrompt [20] presents a unified framework that relies on subgraph similarity and link prediction, utilizing a learnable prompt to guide downstream tasks by incorporating task-specific aggregation in the readout function. Additionally, it computes class prototype vectors through supervised prototypical contrastive learning. GPF [9] extends node embeddings by integrating task-specific prompt parameters, making it adaptable to any pre-trained GNN model, regardless of the pre-training strategy. All-in-one [28] reformulates node-level and edge-level tasks into graph-level tasks and introduces meta-learning techniques into graph prompt tuning. For a more comprehensive summary of graph prompt tuning methods, we refer readers to [29]. However, these approaches largely overlook the inherent bias in pre-trained models, which significantly limits the real-world applicability of graph prompt tuning in fairness-sensitive domains.

2.3 Fairness in Graph Representation Learning

Recently, with the rapid advancements and widespread adoption of Graph Neural Networks (GNNs), concerns about fairness within these models are attracting increasing attention. Algorithmic fairness in GNNs can be broadly categorized into two main types: individual fairness and group fairness. On the one hand, individual fairness requires that similar individuals (or nodes) in the graph receive similar treatment or outcomes. On the other hand, group fairness focuses on ensuring that specific disadvantaged or protected groups are not unfairly treated in comparison to other groups, addressing concerns like bias against minorities or marginalized communities. For example, FairGNN [4] enhances fairness by reducing the identifiability of sensitive attributes within node embeddings through adversarial training. FairVGNN [33] introduces a feature masking strategy to prevent sensitive information leakage during the feature propagation process in GNNs. NIFTY [1] aims to maximize the agreement between the original graph and its counterfactual augmented views to promote fairness. However, these fairness-aware models require optimizing a fair GNN for each specific dataset and cannot be directly applied to mitigate bias in pre-trained models, where a single pre-trained model is expected to be adapted across different downstream datasets.

3 Preliminaries

3.1 Pre-training, Prompt, and Fine-tuning

We use $\mathcal{G} = (\mathbf{A}, \mathbf{X})$ to denote a graph, where \mathcal{V} and \mathcal{E} denotes the node and edge sets, respectively. $\mathbf{A} \in \mathbb{R}^{N \times N}$ is the adjacency matrix, where N is the number of nodes. $\mathbf{X} \in \mathbb{R}^{N \times F}$ is the node feature

matrix, where each node v_i is associated with a *F*-dimensional attribute vector $\mathbf{x}_i \in \mathbb{R}^F$. Furthermore, each node v_i has a binary sensitive attribute $s_i \in \{0, 1\}$. The sensitive group is defined as $\mathcal{S}_k = \{v_i | s_i = k\}, k = \{0, 1\}.$

In general, the pre-training, prompting and fine-tuning paradigm of a graph model consists of three main components: a GNN back-bone $\Psi : (\mathbf{X}, \mathbf{A}) \to \mathbf{H} \in \mathbb{R}^{N \times P}$, a prompting function $\Phi : (\mathbf{X}, \mathbf{A}) \to (\mathbf{X}', \mathbf{A}')$, and an adapter $\Xi : \mathbf{H} \to \mathbf{Z} \in \mathbb{R}^{N \times C}$. In the pre-training phase, the goal is to optimize the parameters of the GNN backbone Ψ through self-supervised learning, enabling it to capture useful information from the graph structure [35, 40]. In the prompting phase, the original graph is transformed into a prompted graph via the prompting function Φ . Commonly used graph transformations in-clude generating the new feature matrix, adding or removing edges, and adding or removing sub-graphs [9, 28]. In the fine-tuning phase, the parameters of the GNN backbone are frozen, and only the parameters in the prompting function Φ and the adapter Ξ need to be optimized for different downstream tasks. In this paper, we consider the node classification task where each node v_i belongs to only one class y_i . After pre-training, prompting, and fine-tuning, the output can be written as $Z = \Xi \circ \Psi \circ \Phi(X, A) \in \mathbb{R}^{N \times C}$, where *C* is the class number. The predicted label \hat{y}_i of node v_i can be obtained from the *i*-th row z_i of Z.

3.2 Fairness Measurement

Fairness ensures that no individual or group faces unjust treatment based on sensitive attributes such as race and gender. Our paper focuses on group fairness [4, 33], which asserts that a model's outcomes should treat groups with differing sensitive attributes equitably. Nonetheless, in many instances, models may exhibit a bias that disproportionately benefits one group over another, leading to unfair outcomes [6]. Various fairness metrics have been proposed to evaluate how models perform across different demographic groups. These metrics are commonly formulated within the context of binary classification, where $y_i \in \{0, 1\}$.

Definition 3.1 (Statistical Parity [7]). Statistical parity requires the predictions to be independent with the sensitive attribute *s*, i.e.,

$$\mathbb{P}(\hat{y}_i \mid s_i = 0) = \mathbb{P}(\hat{y}_i \mid s_i = 1).$$
(1)

Definition 3.2 (Equal Opportunity [15]). Equal opportunity requires the probability of an instance in a positive class being assigned to a positive outcome should be equal for both subgroup members. The property of equal opportunity is defined as:

$$\mathbb{P}(\hat{y}_i = 1 \mid y_i = 1, s_i = 0) = \mathbb{P}(\hat{y}_i = 1 \mid y_i = 1, s_i = 1).$$
(2)

Following [4], we apply the following metrics to quantitatively evaluate statistical parity and equal opportunity:

$$\Delta_{SP} = |\mathbb{P}(\hat{y}_i = 1 \mid s_i = 0) - \mathbb{P}(\hat{y}_i = 1 \mid s_i = 1)|,$$

$$\Delta_{EO} = |\mathbb{P}(\hat{y}_i = 1 \mid y_i = 1, s_i = 0) - \mathbb{P}(\hat{y}_i = 1 \mid y_i = 1, s_i = 1)|,$$
(3)

where the probabilities are evaluated on the test set. For both metrics, smaller values indicate better fairness. Finally, we define the node-level fairness homophily. Definition 3.3 (Fairness Homophily [33]). For node v_i in a graph \mathcal{G} , we define its fairness homophily ratio h_i as:

$$h_i = \frac{\left|\left\{\left(v_i, v_j\right) : v_j \in \mathcal{N}_i \land s_i = s_j\right)\right\}\right|}{|\mathcal{N}_i|}.$$
(4)

The fairness homophily of the graph is defined as $h_{\mathcal{G}} = \sum_{i=1}^{N} h_i / N$.

It is important to note that, unlike the traditional definition of homophily [3], where homophily is typically defined based on node labels y_i , in this context, h_i depends on the sensitive attribute s_i . This means that instead of measuring how nodes with the same labels tend to connect, we focus on how nodes with similar sensitive attributes (such as gender) tend to interact with each other.

3.3 **Problem Formulation**

Following existing models [4, 6], we focus on the binary class and binary sensitive attribute setting, i.e., both y_i and s_i can either be 0 or 1 for each node v_i . Given a subset of nodes with labels \mathcal{V}^L and sensitive attributes \mathcal{S}^L , our goal is to design a tuning method that can be applied to any pre-trained GNNs without modifying the pre-trained model's parameters. The output of the pre-trained and fine-tuning graph model should maintain high accuracy while satisfying the fairness criteria such as statistical parity.

4 Methodology

In this section, we propose a fairness-aware prompt tuning method for GNNs named FPrompt. The key ingredient of FPrompt is a novel prompting function that applies graph transformation to both the features and adjacency matrix:

$$\Phi^{(FPrompt)}: (\mathbf{X}, \mathbf{A}) \to \left(\mathbf{X}^{(FPrompt)}, \mathbf{A}^{(FPrompt)}\right).$$
(5)

where $\mathbf{X}^{(FPrompt)} \in \mathbb{R}^{N \times F}$, $\mathbf{A}^{(FPrompt)} \in \mathbb{R}^{N \times N}$ represent the transformed graph features and adjacency matrix, respectively. To this end, the prompting function consists of two essential components: (i) *hybrid graph prompts* that promote fairness through generating counterfactual features $\mathbf{X}^{(FPrompt)}$, while narrowing the gap between pre-training and downstream tasks via learnable tokens (Section 4.1); (ii) *heterophily-enhanced edge modification* that mitigates bias by modifying the graph structure to $\mathbf{A}^{(FPrompt)}$ to increasing message passing between different sensitive groups (Section 4.2). Through these designs, FPrompt can alleviate bias in any pre-trained GNNs by merely fine-tuning the parameters in the prompt function and the adapter without altering the parameters of the pre-trained models. We introduce the detailed fine-tuning strategy of FPrompt in Section 4.3. We summarize the framework of FPrompt in 1.

4.1 Hybrid Graph Prompts

Graph prompts are designed to bridge the gap between the pretraining task and the downstream task. They allow for efficient learning by adapting the model through learnable prompts rather than full-scale retraining, achieving high-quality outcomes while keeping computational costs low. However, existing graph prompts overlook potential biases in pre-trained graph models, leading to unfair outputs. To address this issue, we propose hybrid graph prompts that consist of fixed graph prompts and learnable graph prompts. 

Figure 1: The framework of FPrompt.

Both types of graph prompts are added to the original features to generate new features $X^{(FPrompt)}$. The fixed graph prompts are designed to enhance fair representation learning through counterfactual data augmentation. Meanwhile, the learnable graph prompts aim to narrow the gap between pre-training and downstream tasks (*e.g.* node classification).

4.1.1 Fixed graph prompts. The purpose of fixed graph prompts is to create counterfactual features. Specifically, the fixed graph prompts contain two sensitivity-group-aware prompt tokens $\mathcal{P} = \{p_0, p_1\}$, where each token $p_s \in \mathcal{P}$ can be represented by a token vector $\mathbf{p}_s \in \mathbb{R}^F$. We obtain \mathbf{p}_s by calculating the average feature of the nodes with sensitive attribute *s* as

$$\mathbf{p}_s = \mathrm{mean}(\mathbf{x}_i \mid v_i \in \mathcal{S}_k^L) \tag{6}$$

The token \mathbf{p}_s captures the general feature patterns of nodes within the sensitive group S_s , serving as a proxy of the group's characteristics. By incorporating these tokens, we can infuse information from different sensitive groups, allowing for the generation of counterfactual representations that promote fairness. Next, we obtain the generated prompted feature $\mathbf{X}^{(\mathcal{P})} \in \mathbb{R}^{N \times F}$ as

$$\mathbf{x}_{i}^{\mathcal{P}} = \mathbf{x}_{i} + \sum_{s \in \{0,1\}} \alpha_{1,s} \mathbf{p}_{s}, \quad , i = 1, \dots, N,$$
 (7)

where the coefficients are defined as

$$\alpha_{i,s} = \frac{\exp \widetilde{\alpha}_{i,s}}{\exp \widetilde{\alpha}_{i,0} + \exp \widetilde{\alpha}_{i,1}}, \quad \widetilde{\alpha}_{i,s} = -\operatorname{Tanh}\left(\operatorname{Sim}\left(\mathbf{x}_{j}, \mathbf{p}_{k}\right)\right). \quad (8)$$

That is to say, node v_i is more inclined to aggregate feature from different sensitive group while simultaneously disperse the feature of the same sensitive group.

To better understand our design, consider an example where the sensitive attribute of the central node v_i is 0. According to the proposed generation mechanism, after message passing between v_i and the fixed tokens, v_i will exhibit sensitive characteristic of nodes with the different sensitive attribute. In other words, we obtain a new feature **x'** from **x**, where **x'**_i carries sensitive information from the opposite sensitive group S_1 . This process is similar to counterfactual data augmentation (CAD), which involves generating new data by making changes to the sensitive attributes of existing data. However, our approach has a key difference from traditional CAD. In practice, it is unrealistic to perform CAD for all nodes, as we often only have access to the sensitive attribute for a limited number of them. To overcome this, we take an alternative approach: instead of changing the node's sensitive attribute directly, we adjust its sensitive representation to align with the opposite sensitive group. This allows us to generate counterfactual data without needing to know each node's sensitive attribute.

4.1.2 Learnable Graph Prompts. Inspired by the recently proposed graph prompt literature [9], we introduce learnable graph prompts $Q = \{q_1, \ldots, q_T\}$ to bridge the gap between the pre-training task and the downstream task. Specifically, each prompt q_k is assigned with a learnable vector \mathbf{q}_k and the generated prompted features $\mathbf{X}^{(Q)} \in \mathbb{R}^{N \times F}$ as

$$\mathbf{x}_{i}^{(Q)} = \mathbf{x}_{i} + \sum_{t=1}^{T} \beta_{1,t} \mathbf{q}_{t}, \quad i = 1, \dots, N$$
 (9)

where the coefficients are calculated as

$$\beta_{i,t} = \frac{\exp \widetilde{\beta}_{i,t}}{\sum_{i=1}^{T} \exp \widetilde{\beta}_{i,j}}, \quad \widetilde{\beta}_{i,t} = \exp \left(\mathbf{x}_i^{\top} \eta_t\right).$$
(10)

Here $\eta_t \in \mathbb{R}^F$ is learnable. This design can be effectively adapted to graphs with varying scales (i.e., different node numbers), and it optimizes storage efficiency for large-scale input graphs, having O(T) learnable parameters [9].

4.2 Heterophily-Enhanced Edge Modification

Recent research has shown that GNNs tend to perform worse on fairness homophilic graphs (with high h_G) and better on heterophilic graphs (with low h_G), both in terms of accuracy and fairness metrics [21]. The reason is that, in graphs with high fairness homophily, nodes primarily exchange information with others from the same sensitivity group. This can widen the feature gap between different sensitivity groups, ultimately increasing bias. Therefore, reducing fairness homophily may lead to more equitable representations and better accuracy.

However, a potential issue with the hybrid graph prompts is that we only modify the features without altering the sensitive attributes. This means that the feature generation does not influence whether connected node pairs belong to the same sensitive group, thus not changing fairness homophily. This differs from traditional counterfactual data augmentation, where the sensitive attribute of each node is known and can be directly flipped (e.g., from 0 to 1) to create counterfactual samples. In such cases, if two nodes belong to the same group, changing their sensitive attributes can make them belong to different groups, thus reducing the fairness homophily. However, this approach often requires knowledge of each node's sensitive attribute, which is impractical due to privacy concerns.

To address this challenge, we propose a heterophily-enhanced edge modification strategy that transforms the original graph structure into one with higher heterophily. Specifically, we compute the probability of a node v_i belonging to either of the two sensitive groups S_0 or S_1 by calculating the distance between the node and each sensitive group. This allows us to infer the likely sensitive group of each node. We then modify the graph structure to obtain $A^{(FPrompt)}$, increasing heterophily (i.e., reducing homophily) by modifying edges according to the identified sensitive groups. We provide theoretical analysis of heterophily-enhanced edge modification in Section 5.

4.2.1 Sensitive Group Assignment. Following [10], we define $X_k = [\mathbf{x}_s] \in \mathbb{R}^{|\mathcal{S}_k^L| \times F}$, $s \in |\mathcal{S}_k^L|$ as the representation matrix for sensitive group \mathcal{S}_k^L , where \mathcal{S}_k^L denotes the training set with sensitive attribute k. In this way, the distance between node v_i and \mathcal{S}_k can be calculated as

$$DIS(v_i, S_k) = \mathbf{x}_i - PROG(v_i, S_k)$$
(11)

where $PROG(v_i, S_k)$ denotes the projection of v_i to $Span(X_k)$ and $Span(X_k)$ denotes the space spanned by the row vectors of X_k . We estimate the projection via ridge regression as

$$\operatorname{PROG}(v_i, \mathcal{S}_k) \approx \operatorname{PROG}(v_i, \mathcal{S}_k^L) = \mathbf{x}_i - \gamma \mathbf{X}_k^\top \left(\mathbf{I} + \gamma \mathbf{X}_k \mathbf{X}_k^\top \right)^{-1} \mathbf{X}_k \mathbf{x}_i.$$
(12)

The probability that node v_i belongs to S_k can be obtained by feeding $DIS(v_i, S_k)$ into a softmax function. We assign v_i to the sensitive group with the higher probability, and denote its sensitive attribute as \hat{s}_i accordingly.

4.2.2 Fair Edge Mask. With estimated sensitive attributes, we propose to modify the subgraph \mathcal{G} via a mask matrix as $A^{(FPrompt)} = \mathbf{A} \circ \mathbf{E}$ where recall that \mathbf{A} is the adjacency matrix of \mathcal{G} . Specifically, each entry \mathbf{E}_{ij} of the mask matrix is sampled from a binomial distribution $\mathcal{B}(\epsilon)$ when $\hat{s}_i \neq \hat{s}_j$, and from $\mathcal{B}(1 - \epsilon)$ when $\hat{s}_i = \hat{s}_j$. Here ϵ is the probability of success. If $\epsilon = 0$, the matrix \mathbf{E} retains all connections between nodes from the same sensitive group while removing all connections between nodes from different sensitive groups. Conversely, if $\epsilon = 1$, the opposite occurs. In other words, ϵ controls the retention of homophilic connections. To enhance information exchange between nodes of different sensitive groups, we set $\epsilon > 0.5$.

4.3 Prompt-Based Fine-Tunining

Given a pre-trained GNN model Ψ and graph $\mathcal{G} = (\mathbf{A}, \mathbf{X})$, we apply the proposed prompting function $\Phi^{(FPrompt)}$ to obtained the generated features and adjacency matrix. Specifically, the generated features $\mathbf{X}^{(FPrompt)}$ is calculated according to Section 4.1 as

$$\mathbf{x}_{i}^{(FPrompt)} = \mathbf{x}_{i} + \sum_{s \in \{0,1\}} \alpha_{1,s} \mathbf{p}_{s} + \sum_{t=1}^{T} \beta_{1,t} \mathbf{q}_{t}, \quad , i = 1, \dots, N.$$
(13)

The generated adjacency matrix $\mathbf{A}^{(FPrompt)}$ is obtained according to Section 4.2.2. With the prompted graph $\left(\mathbf{X}^{(FPrompt)}, \mathbf{A}^{(FPrompt)}\right)$, we obtain the output embedding as

$$\mathbf{Z} = \Xi \circ \Psi \left(\mathbf{X}^{(FPrompt)}, \mathbf{A}^{(FPrompt)} \right), \tag{14}$$

where recall that Ξ denotes the adapter. We choose a two layer multilayer perceptron (MLP) as the adapter, and the output dimension equals to the class number. The total loss function is defined as

$$\mathcal{L} = \sum_{v_i \in \mathcal{V}^L} \ell_{CE}(\widetilde{\mathbf{z}}_i, y_i) + \lambda_1 \ell_{CE}(\mathbf{z}_i, y_i) + \lambda_2 \|\widetilde{\mathbf{z}}_i - \mathbf{z}_i\|_2^2.$$
(15)

where ℓ_{CE} represents the cross-entropy loss for node classification and \tilde{z}_i denotes the features without counterfactual data augmentation, i.e.,

$$\widetilde{\mathbf{Z}} = \Xi \circ \Psi \left(\mathbf{X}^{(Q)}, \mathbf{A}^{(FPrompt)} \right), \tag{16}$$

where $X^{(Q)}$ is defined in Section 4.1.2. In the loss function (15), the first and the second terms restrict the outputs to be aligned with

the downstream task. The third term aims to minimize the discrepancy between the representation \tilde{z}_i and its augmented version z_i , ensuring that the fine-tuning process ignores differences caused by varying sensitive attributes, thus promoting fairness. We freeze the parameters in the pre-trained GNN and only fine-tune the adapter and the learnable graph prompts defined in Section 4.1.2.

5 Theoretical Analysis

In this section, we theoretically analyze the effectiveness of FPrompt. Specifically, we show the adaptation ability in Section 5.1 and fairness guarantees in Section 5.2.

5.1 Adaptation Ability

Note that the prompting function of FPrompt is $\Phi^{(FPrompt)}(\mathcal{G}) = (\mathbf{A}^{(FPrompt)}, \mathbf{X}^{(FPrompt)})$. Assume that there exists another prompting function θ , generating a graph template $\mathcal{G}^* = (\mathbf{A}^*, \mathbf{X}^*) = \theta(\mathcal{G})$ for a given downstream task. The candidate space for \mathbf{A}^* and \mathbf{X}^* is denoted as \mathbb{A} and \mathbb{X} , respectively. Then we have the following theorem.

THEOREM 1. Given a pre-trained GNN model Ψ , for any prompted graph $\widehat{\mathcal{G}} = (\widehat{A} \in \mathbb{A}, \widehat{X} \in \mathbb{X})$ in the candidate space of the graph template $\mathcal{G}^* = \theta(\mathcal{G})$, there exists a learnable graph prompt \widehat{Q} in Section 4.1.2 satisfying

$$\Psi\left(\Phi^{(FPrompt)}(\mathcal{G})\right) = \Psi\left(\widehat{\mathcal{G}}\right).$$
(17)

Theorem 1 is a direct extension of [Theorem 1, [9]] and we omit the proof here. Theorem 1 suggests that for any prompting function, FPrompt can attain the theoretical upper bound of performance. This also holds when some prompting function generates an optimal graph template according to the downstream loss, which means that FPrompt can also achieve the same performance theoretically. As a result, FPrompt provides universal adaptability for handling pre-trained GNN models across various pre-training strategies.

5.2 Fairness Guarantee

For binary node classification task, we use the sigmoid function in the adapter to generate the prediction $\mathbf{z} = \Xi \circ \Psi(\mathbf{X}, \mathbf{A}) \in \mathbb{R}^N$, where z_i indicates the probability that v_i is classified as 1. We then introduce a quantitative criterion of fairness:

$$\Delta_{\text{GSP}}(\mathbf{z}) = \|\mathbb{E}\left[z_i \mid i \in \mathcal{S}_0\right] - \mathbb{E}\left[z_i \mid i \in \mathcal{S}_1\right]\|.$$
(18)

It can be viewed as a generalization of the commonly used metric statistical parity (Definition 3.1) [18], considering that

$$\mathbb{E}\left[z_{i} \mid i \in S_{0}\right] = \int z_{i} \mathbb{P}(s_{i} = 0) dz_{i}$$

$$= \int \mathbb{P}(\hat{y}_{i} = 1 \mid z_{i}) \mathbb{P}(z_{i} \mid s_{i} = 0) dz_{i},$$
(19)

where the last term is exactly $\mathbb{P}(\hat{y}_i \mid s_i = 0)$. Note that Δ_{GSP} measures the disparity between the predictions for different sensitive groups, and a smaller Δ_{GSP} indicates less bias in the predictions.

Our goal is to provide an upper bound of Δ_{GSP} . Before that, we make the following assumption:

Assumption 1. The activation functions in both the GNN backbone and the adapter exhibit Lipschitz continuity.

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Table 1: Detailed statistics of the datasets.

Statistic	$ \mathcal{V} $	$ \mathcal{S} $	F	Label	Sensitivity
Credit	30,000	1,436,858	13	Future default	Age
Pokec_z	67,797	882,765	277	Working field	Region
Pokec_n	66,569	729,129	266	Working field	Region
Pokec_TR	11,294	44,884	241	Working field	Region
Pokec_BA	7,949	32,008	241	Working field	Region
Pokec_KO	13,280	55,568	241	Working field	Region
Pokec_PR	41,203	499,304	241	Working field	Region

Assumption 2. The aggregation function in GNN backbone assigns equal weight to each node in the neighbor set.

Assumption 1 is easily satisfied, for instance, by activation functions such as ReLU, LeakyReLU, and Tanh. Assumption 2 encompasses a wide range of GNN models, including GraphSAGE, GIN, and GCN. We consider the adapter to be a MLP, which is widely used in many pre-training and fine-tuning graph model. For simplicity, we assume the both GNN backbone and the adapter have one layer, and our theoretical analysis can be easily extended to multi-layer cases (see Appendix C).

With the conditions established, we are now ready to present the main theorem in the following:

THEOREM 2. For a pre-training and fine-tuning model $\Xi \circ \Psi$: (X, A) $\rightarrow z \in \mathbb{R}^N$, if Assumptions 1 and 2 hold, then we have

$$\Delta_{GSP}(\mathbf{z}) \le \|\mathbf{W}_{\Xi}\| \|\mathbf{W}_{\Psi}\| \left((\overline{\mu}_0 + \overline{\mu}_1 - 1) \Delta_{GSP}(\mathbf{X}) + 2\sqrt{N}\delta \right), \quad (20)$$

where \mathbf{W}_{Ξ} and \mathbf{W}_{Ψ} are the parameters of the adapter and GNN backbone, respectively. $\overline{\mu}_k$ is the average homophily ratio of sensitive group S_k as $\overline{\mu}_k = \sum_{i \in S_k} \mu_i / |S_k|$, and

$$|\delta| \le \max\left(\delta_0, \delta_1\right), \delta_k^{(l+1)} = \max_{i \in \mathcal{S}_{1-k}} \left\| \mathbf{x}_i^{(l+1)} - \overline{\mathbf{c}}_k^{(l+1)} \right\|, \qquad (21)$$

where $\mathbf{\bar{c}}_{k}^{(l+1)} = \sum_{i \in S_{k}} \mathbf{x}_{i}^{(l)} / |S_{k}|, \quad k = 0, 1.$ PROOF. The proof is left to Appendix C.

From Theorem 2, we observe that the upper bound of $\Delta_{GSP}(z)$ is determined by the following key parts.

625 Average homophily ratio. A smaller $\overline{\mu}_k$ plays a critical role in reducing the upper bound of $\Delta_{GSP}(\mathbf{z})$, thereby contributing signif-626 627 icantly to the model fairness. In Section 4.2, we present an edge 628 modification strategy specifically designed to address this by alter-629 ing the structure of the graph. The core idea behind this strategy is to promote connections between nodes belonging to different sen-630 sitive groups while simultaneously reducing the number of edges 631 632 between nodes within the same sensitive group. By increasing cross-group connections and limiting within-group interactions, 633 the modification lowers the expected value of h_i for individual 634 nodes. Since h_i directly impacts $\overline{\mu}_k$, decreasing h_i leads to a reduc-635 636 tion in $\overline{\mu}_k$. Consequently, this effectively restructures the graph such that mitigates the effects of fairness homophily. 637

Representation discrepancy between two sensitive groups. Both Δ_{GSP} (X) and δ are key measures related to the representation discrepancy between two sensitive groups. As highlighted in Section 4.1.1, the introduction of a fixed graph prompt in conjunction with the original graph can be likened to the generation of counterfactual data. As discussed in Section 4.1.1, the introduction of a fixed graph prompt in connection with the original graph is akin to generating counterfactual data, which reduces group discrepancy. Therefore, this approach helps align the representations of different sensitive groups, ultimately shrinking the distance between them and promoting fairness. By introducing this fixed graph prompt, the model essentially reshapes the data space, creating a more balanced representation of the two groups. This alignment process minimizes differences between their respective learned representations. As a result, the distance between the representations of different sensitive groups is significantly diminished, which directly contributes to improved fairness in the model. This approach ensures that both groups are treated more equally by the model, and the overall impact of sensitive attributes on the learned representations is minimized, fostering a more equitable predictive process.

6 Experiments

6.1 Experimental Settings

6.1.1 Datasets. We compare our methods with other approaches on three public datasets as follows: 1) **Credit** [1]: the nodes in the dataset are clients and two nodes are connected if they have a high similarity of the credit accounts. The task is to classify the credit risk level as high or low with the sensitive attribute gender; 2) **Pokec_z** and **Pokec_n** [4]: both datasets are sampled from an anonymized version of the Pokec network of 2012 (a social network from Slovakia), where nodes correspond to users who live in two major regions and the region information is utilized as the sensitive attribute. The working field of the users is binarized and utilized as the labels in node classification. We summarize these datasets in Table 1 and the training/validation/testing split in Appendix A.1.

Furthermore, existing prompt fine-tuning methods often utilize singular value decomposition (SVD) to align the feature dimensions when validating the performance of the same pre-trained model across different datasets [28]. However, applying SVD may distort the sensitive attributes to features that lack actual semantic meaning, potentially influencing fairness research. To better evaluate the cross-dataset performance and fairness of pre-trained models, we construct a new benchmark. The benchmark consists of four datasets, all created by sampling from the Pokec social network data based on geographic regions [30]. We select the regions of Trenciansky, Banskobystricky, Presovsky, and Kosicky, which we refer to as Pokec_TR, Pokec_BA, Pokec_PR, and Pokec_KO, respectively. For more details we refer to Appendix A.2. In all datasets, the sensitive attribute is region, and the label is working field.

6.1.2 Baselines. Compared approaches are from five categories: **1) Vanilla GNNs**: GCN [17] is a widely used spectral GNN; **2) Fairness-aware GNNs**: FairGNN [4] uses adversarial training to achieve fairness on graphs; NIFTY [1] flips the sensitive attributes to get counterfactual data; FairVGNN [33] introduces a feature

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Table 2: Performance comparison of graph representation learning methods with respect to prediction and fairness. The backbone is GCN and pre-training strategy is Infomax. The best results are bold and the second best results are underlined.

Mathad	Credit				Pokec_z			Pokec_n				
Method	ACC (↑)	AUC (†)	DP (↓)	EO (↓)	ACC (†)	AUC (↑)	DP (↓)	EO (↓)	ACC (†)	AUC (†)	$\mathrm{DP}\left(\downarrow ight)$	EO (\downarrow)
GCN	70.92 _{0.44}	$67.58_{0.54}$	14.45 _{4.13}	14.14 _{4.89}	68.79 _{1.11}	69.09 _{1.21}	6.38 _{1.63}	$5.30_{1.35}$	67.91 _{0.71}	68.61 _{0.57}	1.83 _{1.15}	2.28 _{2.11}
FairGNN	$72.85_{0.12}$	$67.78_{0.76}$	$9.44_{1.29}$	$7.98_{7.79}$	67.89 _{0.27}	$69.18_{0.40}$	$2.20_{1.50}$	$1.42_{1.14}$	68.70 _{0.25}	$68.36_{0.25}$	1.330.59	$1.57_{0.76}$
NIFTY	71.943.16	67.470.77	$10.32_{2.71}$	$8.43_{2.58}$	66.720.44	$66.87_{0.48}$	$5.48_{1.75}$	2.90 _{0.59}	68.32 _{0.45}	$68.07_{0.44}$	1.601.16	$1.59_{1.17}$
FairVGNN	$77.19_{0.45}$	$67.61_{0.62}$	$10.28_{1.39}$	$6.87_{2.53}$	68.860.17	$74.17_{0.38}$	$2.99_{1.50}$	$2.77_{1.02}$	66.860.76	$68.76_{0.67}$	$5.62_{1.83}$	4.59 _{1.62}
Infomax	70.77 _{2.06}	67.54 _{2.97}	12.443.30	10.943.00	68.050.61	70.621.16	6.44 _{2.57}	4.612.67	68.220.42	68.12 _{0.60}	6.32 _{2.22}	4.772.43
GPF	74.113.52	$67.10_{1.32}$	$13.92_{3.52}$	$13.34_{2.64}$	70.500.23	76.660.40	$11.30_{0.96}$	$10.92_{2.14}$	68.83 _{0.91}	67.62 _{0.77}	$9.29_{1.34}$	6.202.25
GraphPrompt	$73.19_{1.34}$	$68.37_{0.80}$	$15.95_{3.09}$	$14.13_{3.20}$	68.810.24	$65.55_{1.14}$	9.31 _{0.11}	8.691.05	67.65 _{0.64}	$67.54_{0.14}$	8.181.25	$7.78_{0.25}$
GraphPAR	$74.83_{2.32}$	$\underline{69.46_{0.43}}$	7.532.62	$\underline{6.03_{3.13}}$	66.69 _{1.41}	$73.40_{0.53}$	$\underline{1.84_{0.65}}$	$1.36_{0.56}$	<u>69.01_{0.88}</u>	$74.79_{1.01}$	$1.61_{0.31}$	$1.52_{1.05}$
FPrompt	77.422.07	70.260.85	4.342.04	3.05 _{2.30}	68.940.57	76.70 _{1.28}	1.56 _{1.04}	0.86 _{0.54}	69.54 _{0.47}	74.63 _{1.05}	0.780.24	1.28 _{1.11}

masking strategy to prevent sensitive information leakage during the feature propagation; **3**) **Pre-training with fine-tuning**: Infomax [32] maximizes the mutual information between node and graph representations; GRACE [35] perturbs the graph model parameter spaces and narrow down the gap between different perturbations for the same graph; **4**) **Pre-training with prompt finetuning**: GPF [9] adds soft prompts to all node features of the input graph; GraphPrompt [20] inserts the prompt vector into the graph pooling by element-wise multiplication;; **5**) **Fairness-aware pretraining with fine-tuning**: GraphPAR [41] introduces a sensitive semantic augmenter that incorporates varying sensitive attribute semantics for each node. For all pre-training with and without prompt fine-tuning models, we choose the same adapter as FPrompt, which is a 2-layer MLP with output dimension equal to the class number.

6.1.3 Implements. We use the library PygDebias¹ to implement GCN, FairGNN, NIFTY, and FairVGNN. We apply the library ProG² for pre-training with (prompt) fine-tuning models including Infomax, GRACE, GPF, and GraphPrompt. For GraphPAR, we use the source code at Github³. For our model FPrompt, we search hyperparameters by the grid search method and we refer to Appendix A.3 for detailed explanation.

6.2 Prediction Performance and Fairness

We present the results across different datasets in Fig. 2. Our obser-vations reveal that while vanilla GNNs, as well as those utilizing pre-training with fine-tuning and pre-training with prompt fine-tuning, achieve commendable accuracy performance, they exhibit significant shortcomings when it comes to fairness metrics. This in-dicates that although these models can classify or predict outcomes accurately, they often do so at the expense of equitable treatment across different demographic groups. In contrast, fairness-aware GNNs demonstrate strong fairness performance. However, a notable drawback of these fairness-focused models is their requirement for separate training of GNNs on each dataset. This separation can lead to inefficiencies in practical applications. FPrompt achieves

⁷⁵² ²https://github.com/sheldonresearch/ProG

753 ³https://github.com/BUPT-GAMMA/GraphPAR

Table 3: Performance comparison with respect to prediction and fairness. The backbone is GCN and pre-training strategy is GRACE. The best results are bold and the second best results are underlined.

Mathad		Credit							
Method	ACC (†)	AUC (†)	DP (↓)	EO (↓)					
GRACE	$71.57_{2.50}$	68.12 _{3.58}	9.03 _{2.21}	7.61 _{2.49}					
GPF	$74.25_{2.71}$	67.963.32	$11.72_{4.26}$	9.353.24					
GraphPrompt	$74.70_{2.68}$	67.89 _{2.98}	9.91 _{3.17}	$9.04_{2.58}$					
GraphPAR	$75.52_{2.15}$	$\underline{68.23_{2.44}}$	$5.62_{1.64}$	$4.25_{1.58}$					
FPrompt	76.35 _{2.68}	69.35 _{3.68}	5.01 _{2.68}	4.551.56					

Table 4: Performance comparison with respect to prediction and fairness. The pre-training strategy is Infomax. The best results are bold and the second best results are underlined.

Method			Cre	dit	
ľ	letilou	ACC (↑)	AUC (†)	DP (↓)	EO (↓)
	Infomax	70.55 _{3.81}	67.45 _{1.24}	12.064.21	11.424.35
CAT	GPF	$75.26_{2.95}$	68.89 _{1.85}	$12.81_{4.53}$	$12.20_{3.56}$
GAI	GraphPAR	$75.21_{2.18}$	$69.54_{0.24}$	$7.75_{1.86}$	6.352.39
	FPrompt	$76.18_{1.74}$	<u>69.53_{1.49}</u>	$5.94_{3.02}$	$4.77_{2.50}$
	Infomax	70.29 _{3.66}	65.92 _{3.20}	10.662.27	10.883.40
CIN	GPF	$74.71_{2.99}$	69.81 _{3.24}	$11.57_{3.62}$	$8.81_{2.71}$
OIN	GraphPAR	$74.94_{5.19}$	$68.86_{2.87}$	$6.07_{2.33}$	$4.42_{2.12}$
	FPrompt	76.06 _{1.15}	$69.71_{3.35}$	$4.90_{1.80}$	$3.78_{1.31}$

both strong accuracy and fairness performance simultaneously. For example, FPrompt significantly enhances fairness performance on the Credit, Pokec_z, and Pokec_n datasets, with improvements of 42%, 15%, and 41%, respectively, in terms of demographic parity.

^{751 &}lt;sup>1</sup>https://github.com/yushundong/PyGDebias

Table 5: Performance comparison of graph representation learning methods with respect to prediction and fairness. The backbone is GCN and pre-training strategy is Infomax. The best results are bold and the second best results are underlined.

Mathad	Р	okec_TR —	→ Pokec_B	A	Pc	$kec_TR \rightarrow$	Pokec_K	0	Р	okec_TR –	→ Pokec_P	R
Method	ACC (↑)	AUC (↑)	DP (↓)	EO (↓)	ACC (↑)	AUC (↑)	DP (↓)	EO (↓)	ACC (↑)	AUC (↑)	$\mathrm{DP}\left(\downarrow\right)$	EO (↓)
Infomax	71.99 _{0.63}	75.11 _{0.22}	7.603.63	5.29 _{1.81}	65.271.49	66.70 _{2.36}	3.462.47	5.58 _{2.22}	66.340.24	68.94 _{0.58}	24.97 _{2.08}	25.89 _{2.38}
GPF	72.630.71	$76.70_{0.44}$	9.09 _{3.62}	$10.46_{2.75}$	67.361.52	68.34 _{1.32}	$4.56_{1.62}$	6.64 _{1.83}	66.17 _{0.18}	67.93 _{0.92}	$28.73_{4.87}$	27.56 _{5.28}
GraphPrompt	72.121.67	76.98 _{1.56}	8.824.58	8.562.91	65.99 _{1.29}	66.142.58	$4.98_{1.18}$	$6.54_{2.15}$	65.62 _{0.51}	67.79 _{1.18}	$25.32_{2.53}$	$25.78_{2.57}$
GraphPAR	$71.00_{2.54}$	$76.45_{1.21}$	$4.97_{2.85}$	$4.65_{1.87}$	65.301.71	$66.26_{1.54}$	$\underline{3.45_{2.12}}$	$2.55_{2.06}$	66.540.51	69.06 _{0.79}	$\underline{15.70_{3.94}}$	14.103.86
FPrompt	72.810.86	76.91 _{1.68}	4.572.90	3.242.46	66.482.81	69.03 _{1.87}	1.700.62	2.10 _{1.50}	66.625.58	67.95 _{0.55}	8.93 _{3.67}	6.523.36

To further demonstrate FPrompt's ability to enhance different pre-trained strategies, we experiment with the pre-training method GRACE.The results, as outlined in Table 3, clearly illustrate that FPrompt effectively reduces bias in the pre-trained model, leading to more balanced outcomes across different demographic groups. Moreover, we extend our evaluation to include different GNN architectures, as presented in Table 4. The results indicate that FPrompt adapts well to various GNN architectures, including GIN (which satisfies Assumption 2) and GAT (which does not). This adaptability underscores the versatility of FPrompt. For more experimental results, please refer to Appendix B.

6.3 Transferability Analysis

To assess the transferability of our model, we compare it against both the fine-tuning method Infomax and various prompt-based fine-tuning methods. We intentionally exclude fairness-aware GNNs from this comparison, as these models require retraining the GNN on each new dataset, which limits their adaptability in transfer learning scenarios. Our evaluation is conducted using our newly proposed benchmark, where we pre-train the GNN model on the Pokec_TR dataset and subsequently fine-tune it on different downstream datasets, applying different fine-tuning strategies. The results of this comparison are summarized in Table 5. We observe that while prompt-based fine-tuning methods tend to achieve high accuracy, they generally perform poorly in terms of fairness metrics. In contrast, FPrompt not only maintains competitive accuracy but also significantly improves fairness outcomes across datasets, demonstrating its ability to in transfer learning tasks.

6.4 Model Analysis

To further verify the theoretical effectiveness of our method as discussed in Section 5.2, we present a detailed comparison of the representation discrepancies between two sensitive groups (i.e., Δ_{GSP} (X) and δ). These discrepancies are evaluated both for the raw features and after applying our proposed FPrompt method. In particular, we observe in Figure 2 that the use of a fixed graph prompt within FPrompt significantly reduces both Δ_{GSP} (X) and δ . This reduction in discrepancies between sensitive groups indi-cates that the representations of individuals from different sensitive categories become more aligned, thereby reducing bias. This re-sult aligns closely with our theoretical analysis, which suggests that FPrompt's ability to reduce the discrepancy between sensitive groups can directly contribute to enhancing fairness in graph-based



Figure 2: The representation discrepancy between the two sensitive groups. (a): The generalized SP; (b): The maximum feature distance of the raw features (denoted as Original) and prompted features $X^{\mathcal{P}}$ (denoted as FPrompt). We unify the scale for better presentation.

predictions. By narrowing the gap between group representations of different sensitive groups, FPrompt ensures that individuals are treated more equitably in downstream tasks.

7 Conclusion

In this work, we proposed FPrompt, a fairness-aware graph prompt tuning method designed to mitigate the inherent bias present in pre-trained graph neural networks (GNNs) while retaining their generalization capabilities. By introducing hybrid graph prompts for counterfactual data augmentation and applying edge modification to increase sensitivity heterophily, FPrompt successfully aligns pre-training and downstream tasks, addressing bias introduced by sensitive attributes. Theoretical analysis demonstrate two key aspects of FPrompt: (1) it has universal capabilities to effectively adapt to various pre-training strategies, and (2) it reduces the upper bound of generalized statistical parity, significantly mitigating bias in pre-trained models. Extensive experiments confirm that FPrompt outperforms existing methods in both fairness and accuracy on standard benchmarks.

The present work also opens up promising future directions. One notable opportunity arises from the success of prompt tuning in adapting pre-trained GNN models to tasks beyond node classification (e.g., link prediction). However, bias can arise in link prediction due to factors such as imbalanced data, where certain types of links (e.g., between nodes from different sensitive groups) are underrepresented. Therefore, a potential next step would be to explore the application of FPrompt to reduce bias of pre-trained models in link prediction tasks.

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- Chirag Agarwal, Himabindu Lakkaraju, and Marinka Zitnik. 2021. Towards a unified framework for fair and stable graph representation learning. In Uncertainty in Artificial Intelligence. 2114–2124.
- [2] Joan Bruna, Wojciech Zaremba, Arthur Szlam, and Yann LeCun. 2014. Spectral networks and deep locally connected networks on graphs. In 2nd International Conference on Learning Representations.
- [3] Jingyu Chen, Runlin Lei, and Zhewei Wei. 2024. POLYGCL: Graph contrastive learning via learnable spectral polynomial filters. In 12th International Conference on Learning Representations.
- [4] Enyan Dai and Suhang Wang. 2021. Say no to the discrimination: Learning fair graph neural networks with limited sensitive attribute information. In Proceedings of the 14th ACM International Conference on Web Search and Data Mining. 680– 688.
- [5] Enyan Dai, Tianxiang Zhao, Huaisheng Zhu, Junjie Xu, Zhimeng Guo, Hui Liu, Jiliang Tang, and Suhang Wang. 2024. A comprehensive survey on trustworthy graph neural networks: Privacy, robustness, fairness, and explainability. *Machine Intelligence Research* (2024), 1–51.
- [6] Yushun Dong, Jing Ma, Song Wang, Chen Chen, and Jundong Li. 2023. Fairness in graph mining: A survey. *IEEE Transactions on Knowledge and Data Engineering* 35, 10 (2023), 10583–10602.
- [7] Cynthia Dwork, Moritz Hardt, Toniann Pitassi, Omer Reingold, and Richard Zemel. 2012. Fairness through awareness. In Proceedings of the 3rd Innovations in Theoretical Computer Science Conference. 214–226.
- [8] Moshe Eliasof, Lars Ruthotto, and Eran Treister. 2023. Improving graph neural networks with learnable propagation operators. In Proceedings of the 40th International Conference on Machine Learning. 9224-9245.
- [9] Taoran Fang, Yunchao Zhang, Yang Yang, Chunping Wang, and Lei Chen. 2023. Universal prompt tuning for graph neural networks. In Proceedings of the 37th International Conference on Neural Information Processing Systems. 52464–52489.
- [10] Qizhang Feng, Zhimeng Jiang, Ruiquan Li, Yicheng Wang, Na Zou, Jiang Bian, and Xia Hu. 2023. Fair graph distillation. In Proceedings of the 37th International Conference on Neural Information Processing Systems. 80644–80660.
- [11] Yuan Gao, Junfeng Fang, Yongduo Sui, Yangyang Li, Xiang Wang, Huamin Feng, and Yongdong Zhang. 2024. Graph anomaly detection with bi-level optimization. In Proceedings of the ACM on Web Conference 2024. 4383–4394.
- [12] Yuan Gao, Xiang Wang, Xiangnan He, Zhenguang Liu, Huamin Feng, and Yongdong Zhang. 2023. Addressing heterophily in graph anomaly detection: A perspective of graph spectrum. In *Proceedings of the ACM Web Conference 2023*. 1528–1538.
- [13] Aditya Grover and Jure Leskovec. 2016. node2vec: Scalable feature learning for networks. In Proceedings of the 22nd ACM SIGKDD International Conference on Knowledge Discovery and Data Mining. 855–864.
- [14] Will Hamilton, Zhitao Ying, and Jure Leskovec. 2017. Inductive representation learning on large graphs. In Proceedings of 31st International Conference on Neural Information Processing Systems. 1025–1035.
- [15] Moritz Hardt, Eric Price, and Nathan Srebro. 2016. Equality of opportunity in supervised learning. In Proceedings of the 30th International Conference on Neural Information Processing Systems. 3323–3331.
- [16] Xiangnan He, Kuan Deng, Xiang Wang, Yan Li, Yongdong Zhang, and Meng Wang. 2020. Lightgcn: Simplifying and powering graph convolution network for recommendation. In Proceedings of the 43rd International ACM SIGIR conference on research and development in Information Retrieval. 639–648.
- [17] Thomas N. Kipf and Max Welling. 2017. In 5th International Conference on Learning Representation.
- [18] O Deniz Kose and Yanning Shen. 2024. FairGAT: Fairness-aware graph attention networks. ACM Transactions on Knowledge Discovery from Data 18, 7 (2024), 1–20.
- [19] Pengfei Liu, Weizhe Yuan, Jinlan Fu, Zhengbao Jiang, Hiroaki Hayashi, and Graham Neubig. 2023. Pre-train, prompt, and predict: A systematic survey of prompting methods in natural language processing. *Comput. Surveys* 55, 9 (2023), 1–35.
- [20] Zemin Liu, Xingtong Yu, Yuan Fang, and Xinming Zhang. 2023. Graphprompt: Unifying pre-training and downstream tasks for graph neural networks. In Proceedings of the ACM Web Conference 2023. 417–428.
- [21] Donald Loveland, Jiong Zhu, Mark Heimann, Ben Fish, Michael T Schaub, and Danai Koutra. 2023. On graph neural network fairness in the presence of heterophilous neighborhoods. In SIGKDD 2023 Deep Learning on Graphs Workshop.
- [22] Yuanfu Lu, Xunqiang Jiang, Yuan Fang, and Chuan Shi. 2021. Learning to pretrain graph neural networks. In Proceedings of the AAAI Conference on Artificial Intelligence, Vol. 35. 4276–4284.
- [23] Jing Ma, Ruocheng Guo, Mengting Wan, Longqi Yang, Aidong Zhang, and Jundong Li. 2022. Learning fair node representations with graph counterfactual fairness. In Proceedings of the 15th ACM International Conference on Web Search and Data Mining. 695–703.
- [24] OpenAI. 2023. Gpt-4 technical report. arXiv preprint arXiv:2303.08774 (2023).

- [25] Bryan Perozzi, Rami Al-Rfou, and Steven Skiena. 2014. Deepwalk: Online learning of social representations. In Proceedings of the 20th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining. 701–710.
- [26] Tahleen Rahman, Bartlomiej Surma, Michael Backes, and Yang Zhang. 2019. Fairwalk: Towards fair graph embedding. In Proceedings of the 28th International Joint Conference on Artificial Intelligence. 3289–3295.
- [27] Mingchen Sun, Kaixiong Zhou, Xin He, Ying Wang, and Xin Wang. 2022. Gppt: Graph pre-training and prompt tuning to generalize graph neural networks. In Proceedings of the 28th ACM SIGKDD Conference on Knowledge Discovery and Data Mining. 1717–1727.
- [28] Xiangguo Sun, Hong Cheng, Jia Li, Bo Liu, and Jihong Guan. 2023. All in one: Multi-task prompting for graph neural networks. In Proceedings of the 29th ACM SIGKDD Conference on Knowledge Discovery and Data Mining. 2120–2131.
- [29] Xiangguo Sun, Jiawen Zhang, Xixi Wu, Hong Cheng, Yun Xiong, and Jia Li. 2023. Graph prompt learning: A comprehensive survey and beyond. arXiv preprint arXiv:2311.16534 (2023).
- [30] Lubos Takac and Michal Zabovsky. 2012. Data analysis in public social networks. In International scientific conference and international workshop present day trends of innovations, Vol. 1.
- [31] Petar Veličković, Guillem Cucurull, Arantxa Casanova, Adriana Romero, Pietro Liò, and Yoshua Bengio. 2018. Graph attention networks. In 6th International Conference on Learning Representations.
- [32] Petar Veličković, William Fedus, William L Hamilton, Pietro Liò, Yoshua Bengio, and R Devon Hjelm. 2018. Deep graph infomax. In 6th International Conference on Learning Representations.
- [33] Yu Wang, Yuying Zhao, Yushun Dong, Huiyuan Chen, Jundong Li, and Tyler Derr. 2022. Improving fairness in graph neural networks via mitigating sensitive attribute leakage. In Proceedings of the 28th ACM SIGKDD Conference on Knowledge Discovery and Data Mining. 1938–1948.
- [34] Qitian Wu, Fan Nie, Chenxiao Yang, Tianyi Bao, and Junchi Yan. 2024. Graph out-of-distribution generalization via causal intervention. In Proceedings of the ACM on Web Conference 2024. 850–860.
- [35] Jun Xia, Lirong Wu, Jintao Chen, Bozhen Hu, and Stan Z Li. 2022. Simgrace: A simple framework for graph contrastive learning without data augmentation. In Proceedings of the ACM Web Conference 2022. 1070–1079.
- [36] Teng Xiao, Huaisheng Zhu, Zhengyu Chen, and Suhang Wang. 2023. Simple and asymmetric graph contrastive learning without augmentations. In Proceedings of the 37th International Conference on Neural Information Processing Systems. 16129–16152.
- [37] Keyulu Xu, Weihua Hu, Jure Leskovec, and Stefanie Jegelka. 2018. How powerful are graph neural networks?. In 6th International Conference on Learning Representations.
- [38] Yuhao Yang, Lianghao Xia, Da Luo, Kangyi Lin, and Chao Huang. 2024. GraphPro: Graph pre-training and prompt learning for recommendation. In Proceedings of the ACM on Web Conference 2024. 3690–3699.
- [39] Yuning You, Tianlong Chen, Yang Shen, and Zhangyang Wang. 2021. Graph contrastive learning automated. In Proceedings of the 38th International Conference on Machine Learning. 12121–12132.
- [40] Yuning You, Tianlong Chen, Yongduo Sui, Ting Chen, Zhangyang Wang, and Yang Shen. 2020. Graph contrastive learning with augmentations. In Proceedings of the 34th International Conference on Neural Information Processing Systems. 5812–5823.
- [41] Zhongjian Zhang, Mengmei Zhang, Yue Yu, Cheng Yang, Jiawei Liu, and Chuan Shi. 2024. Endowing pre-trained graph models with provable fairness. In Proceedings of the ACM on Web Conference 2024. 1045–1056.
- [42] Fan Zhou and Chengtai Cao. 2021. Overcoming catastrophic forgetting in graph neural networks with experience replay. In *Proceedings of the AAAI Conference* on Artificial Intelligence, Vol. 35. 4714–4722.
- [43] Marinka Zitnik, Rok Sosič, and Jure Leskovec. 2018. Prioritizing network communities. Nature Communications 9, 1 (2018), 2544.

A Experimental Details 1045

A.1 Datasets Split

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In our experiments, we adhere to standard dataset splits and employ random seeds for re-producibility. Note that for all datasets, the node labels are binary (i.e., 0 and 1). Denote the node set with label 0 and 1 as \mathcal{V}_0 and \mathcal{V}_1 , respectively. Then we randomly split the nodes into validation/testing sets with ratio $0.25|\mathcal{V}_0|+0.25|\mathcal{V}_1|/0.25|\mathcal{V}_0|+$ $0.25|\mathcal{V}_1|$. The training ratio is set to

$$\min(T, 0.25|\mathcal{V}_0|) + \min(T, 0.25|\mathcal{V}_1|), \tag{22}$$

where we choose T = 3000 for all datasets. We also summarize other statistical details in Table 6.

A.2 **Benchmark Construction**

We introduce the construction details of Pokec_PR as an example, 1060 and the remaining datasets follow the same process. We first filter 1061 out nodes where the region starts with "presovsky kraj" and select 1062 the following columns: user id, public, completion percentage, gen-1063 der, region, AGE, I am working in field, spoken languages, hobbies, 1064 *I_most_enjoy_good_food, body_type, eye_color, hair_color, hair_type,* 1065 completed_level_of_education, favourite_color, relation_to_smoking, 1066 relation_to_alcohol, on_pokec_i_am_looking_for, love_is_for_me, rel 1067 ation_to_casual_sex, my_partner_should_be, marital_status, relatio 1068 n to children, I like movies, I like watching movie, I like music, 1069 I mostlv_like_listening_to_music, the_idea_of_good_evening, I_like_ 1070 specialties_from_kitchen, I_am_going_to_concerts, my_active_sports, 1071 my passive sports, and I like books. For the features from spoken l 1072 anguages onwards, we generate columns where the column names 1073 correspond to the values of those features. If an element has that 1074 value for the feature, the corresponding element is 1; otherwise, it is 1075 1076 0. Note that a feature can have multiple values for a single element. 1077 Then, following the existing data, we map I am working in field to 0, 1, and -1 (where -1 indicates missing data). Next, we select the 1078 two most frequent regions and filter the corresponding data as the 1079 final dataset (presovsky kraj, poprad and presovsky kraj, bardejov). 1080 Finally, we extract the connection relationships based on user_id. 1081 The source data can be found from [30]. 1082

A.3 Implements

We conduct all the experiments on a machine with an NVIDIA A100 80GB PCIe, Intel Xeon CPU (2.20 GHz) with 6 cores, and 150 GB of RAM. Our code is built on pytorch==2.1.1, pyg==2.4.0, cuda==12.1, and dgl==2.1.0. We choose learning rate=0.001, weight decay=1e-5, and num_layer=2 for all datasets. For Credit, we set hidden_dim=16 and for the remaining datasets, we let hidden_dim=24. The optimal hyperparameters such as regularization term λ_1 , λ_2 , edge modifictaion ratio ϵ , and learnable token number T are tuned for each dataset separately. We will release the source code after the review process.

Additional Experimental Results B

B.1 Results of GNN Backbones

We conduct experiments on Pokec_z with different GNN backbones in Table 7. It can be observed that FPrompt outperforms baseline models in terms of classification performance and fairness.

B.2 Results on Pokec TR

We provide the results where we first pre-train a GNN model on Pokec_TR and fine-tune the model on the same dataset. Results in Table. 8 demonstrate the state-of-the-art performance of FPrompt.

C Proof of Theorem 2

To prove Theorem 2, we first derive the upper bound of Δ_{GSP} for both the GNN backbone (Theorem 3) and the adapter (Theorem 4) separately. Afterward, the overall upper bound for the pre-training and fine-tuning graph model can be directly derived by combining these results.

C.1 Δ_{GSP} for the GNN Backbone

For a GNN model that outputs a feature matrix rather than a prediction vector as Eq. (18), the fairness criterion is defined as

$$\Delta_{\text{GSP}}(\mathbf{H}) = \|\mathbb{E}\left[\mathbf{h}_{i} \mid i \in \mathcal{S}_{0}\right] - \mathbb{E}\left[\mathbf{h}_{i} \mid i \in \mathcal{S}_{1}\right]\|, \quad (23)$$

where \mathbf{h}_i is the *i*-th row of **H**. We have the following result.

THEOREM 3. For a GNN model $\Psi : (\mathbf{X}, \mathbf{A}) \to \mathbf{H}$, if Assumptions 1 and 2 hold, then we have

$$\Delta_{GSP}\left(\mathbf{H}^{(l+1)}\right) \leq \left((\overline{\mu}_{0} + \overline{\mu}_{1} - 1)\Delta_{GSP}\left(\mathbf{H}^{(l)}\right) + 2\sqrt{N}\delta^{(l+1)}\right) \left\|\mathbf{W}_{\Psi}^{(l)}\right\|,$$
(24)

where $\mathbf{W}_{\Psi}^{(l)}$ is the parameter at the *l*-th layer of GNN, $\overline{\mu}_k$ is the average homophily ratio of sensitive group S_k as $\overline{\mu}_k = \sum_{i \in S_k} \mu_i / |S_k|$, and

$$|\delta^{(l+1)}| \le \max\left(\delta_0^{(l+1)}, \delta_1^{(l+1)}\right), \delta_k^{(l+1)} = \max_{i \in \mathcal{S}_{1-k}} \left\| \mathbf{c}_i^{(l+1)} - \overline{\mathbf{c}}_k^{(l+1)} \right\|,$$
(25)

where $\overline{\mathbf{c}}_{k}^{(l+1)} = \sum_{i \in \mathcal{S}_{k}} \mathbf{h}_{i}^{(l)} / |\mathcal{S}_{k}|, \quad k = 0, 1.$

PROOF OF THEOREM 3. Estimating the expected distribution with empirical distribution, we have

$$\Delta_{\text{GSP}}(\mathbf{H}^{(l+1)}) = \left\| \mathbb{E} \left[\mathbf{h}_i^{(l+1)} \mid i \in \mathcal{S}_0 \right] - \mathbb{E} \left[\mathbf{h}_i^{(l+1)} \mid i \in \mathcal{S}_1 \right] \right\|$$
$$= \left\| \frac{1}{1} \sum_{i=1}^{n} \mathbf{h}_i^{(l+1)} - \frac{1}{1} \sum_{i=1}^{n} \mathbf{h}_i^{(l+1)} \right\|$$

$$\left\| \frac{|\mathcal{S}_0|}{|\mathcal{S}_0|} \sum_{i \in \mathcal{S}_0} \mathbf{h}_i^{i} \right\| \leq -\frac{|\mathcal{S}_1|}{|\mathcal{S}_1|} \sum_{i \in \mathcal{S}_1} \mathbf{h}_i^{i} \leq \| \frac{1}{|\mathcal{S}_0|} \sum_{i \in \mathcal{S}_0} \sigma\left(\mathbf{r}_i^{(l+1)}\right) - \frac{1}{|\mathcal{S}_1|} \sum_{i \in \mathcal{S}_0} \sigma\left(\mathbf{r}_i^{(l+1)}\right) \right\|$$

$$(26)$$

$$\| \frac{1}{|S_0|} \sum_{i \in S_0} \mathbf{r}_i^{(l+1)} - \frac{1}{|S_1|} \sum_{i \in S_1} \mathbf{r}_i^{(l+1)} \|,$$

where (a) is due to the Lipschitz continuity of the activation functions (Assumption 1). Here, $\sigma(\cdot)$ denotes the activation function and $\mathbf{r}_{i}^{(l+1)}$ is the representation of node v_{i} after aggregation. The first term can be rewritten as

$$\frac{1}{|\mathcal{S}_0|} \sum_{i \in \mathcal{S}_0} \mathbf{r}_i^{(l+1)}$$

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$$= \frac{1}{|S_0|} \sum_{i \in S_0} \frac{1}{|N_i|} \left(\sum_{j \in N_i \cap S_0} \mathbf{c}_j^{(l+1)} + \sum_{j \in N_i \cap S_1} \mathbf{c}_j^{(l+1)} \right)$$

$$1 = \frac{1}{|S_0|} \left(\sum_{j \in N_i \cap S_0} \mathbf{c}_j^{(l+1)} + \sum_{j \in N_i \cap S_1} \mathbf{c}_j^{(l+1)} \right)$$
(27)

$$= \frac{1}{|S_0|} \sum_{i \in S_0} \frac{1}{|N_i|} \left(\sum_{j \in N_i \cap S_0} \overline{c}_1^{(l+1)} + \sum_{j \in N_i \cap S_1} \overline{c}_0^{(l+1)} \right) + \delta^{(l+1)}$$

$$= \frac{1}{|\mathcal{S}_0|} \sum_{i \in \mathcal{S}_0} \left(\mu_i \bar{\mathbf{c}}_1^{(l+1)} + (1 - \mu_i) \bar{\mathbf{c}}_0^{(l+1)} \right) + \delta^{(l+1)}$$

$$\overline{\mu}_0 \overline{\mathbf{c}}_1^{(l+1)} + (1 - \overline{\mu}_0) \overline{\mathbf{c}}_0^{(l+1)} + \delta^{\prime(l+1)},$$
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Statistic	Training Size	Label Ratio	Label Distribution ($ \mathcal{V}_0 / \mathcal{V}_1 $)	Sensitivity Distribution ($ \mathcal{S}_0 / \mathcal{S}_1 $)
Credit	6,000	1.00	0.28	10.17
Pokec_z	5,131	0.15	0.86	1.84
Pokec_n	4,398	0.13	1.05	2.46
Pokec_TR	3,746	0.66	0.97	1.08
Pokec_BA	2,314	0.58	1.41	1.00
Pokec_KO	4,002	0.60	1.67	1.41
Pokec_PR	3,780	0.18	1.15	1.68

Table 6: Experimental detail of the datasets.

Table 7: Performance comparison of graph representation learning methods with respect to prediction and fairness. The pre-training strategy is Infomax. The best results are bold and the second best results are underlined.

	Method	Pokec_z							
1	vietnou	ACC (↑)	AUC (†)	DP (↓)	EO (↓)				
	Infomax	66.39 _{0.52}	70.871.20	6.51 _{2.22}	5.272.30				
CAT	GPF	67.430.36	$72.10_{0.74}$	$10.36_{1.52}$	8.282.66				
GAI	GraphPAR	67.20 _{0.69}	73.380.95	$1.55_{0.90}$	$1.50_{1.14}$				
	FPrompt	$67.97_{0.73}$	$73.91_{0.54}$	$1.42_{1.17}$	$1.29_{0.74}$				
	Infomax	64.90 _{0.65}	71.23 _{0.94}	4.223.15	4.062.23				
GIN	GPF	66.72 _{1.28}	73.25 _{0.98}	$10.25_{2.34}$	$9.28_{3.51}$				
OIN	GraphPAR	$65.49_{1.77}$	$73.03_{1.32}$	$3.74_{2.06}$	$3.04_{1.52}$				
	FPrompt	$68.43_{0.72}$	$74.59_{0.72}$	$2.52_{1.14}$	$1.13_{0.92}$				

Table 8: Performance comparison of graph representation learning methods with respect to prediction and fairness. The backbone is GCN and pre-training strategy is Infomax. The best results are bold and the second best results are underlined.

Mathad	Pokec_TR						
Method	ACC (↑)	AUC (†)	DP (↓)	EO (↓)			
Infomax	76.23 _{0.76}	80.96 _{0.44}	3.68 _{2.61}	4.702.20			
GraphPAR	$74.26_{0.56}$	$79.13_{0.42}$	2.891.39	$2.64_{1.38}$			
FPrompt	75.82 _{2.29}	79.88 _{0.45}	1.45 _{1.40}	2.00 _{0.92}			

where $\mathbf{c}_{i}^{(l+1)} = \mathbf{W}_{\Psi}^{(l)} \mathbf{h}_{i}^{(l)}, \overline{\mu}_{0}$ is the average homophily ratio of sensitive group $S_{0}. \overline{\mathbf{c}}_{1}^{(l+1)}$ denotes the average representation of sensitive group S_{k} at the *l*-th layer as

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$$\overline{\mathbf{c}}_{k}^{(l+1)} = \frac{1}{|\mathcal{S}_{k}|} \sum_{i \in \mathcal{S}_{k}} \mathbf{h}_{i}^{(l)}, \quad k = 0, 1.$$
 (28)

The error term $\delta'^{(l+1)}$ is upper-bounded by

$$|\delta'^{(l+1)}| \le \max\left(\delta_0^{(l+1)}, \delta_1^{(l+1)}\right),$$
 (29)

with $\delta_k^{(l+1)} = \max_{i \in S_{1-k}} \left\| \mathbf{c}_i^{(l+1)} - \overline{\mathbf{c}}_k^{(l+1)} \right\|$ denoting the maximum feature distance between node v_i and the average representation of the opposite sensitive class. Similarly, the second term can be rewritten as

$$\frac{1}{|\mathcal{S}_1|} \sum_{i \in \mathcal{S}_1} \mathbf{r}_i^{(l+1)}$$

$$= \frac{1}{|S_1|} \sum_{i \in S_1} \frac{1}{|N_i|} \left(\sum_{j \in N_i \cap S_0} \mathbf{c}_j^{(l+1)} + \sum_{j \in N_i \cap S_1} \mathbf{c}_j^{(l+1)} \right)$$
(30)
= $(1 - \overline{\mu}_1) \overline{\mathbf{c}}_1^{(l+1)} + \overline{\mu}_1 \overline{\mathbf{c}}_0^{(l+1)} + \delta^{\prime\prime(l+1)},$

where $\delta^{\prime\prime(l+1)}$ has the same upper bound with $\delta^{\prime(l+1)}.$ As a result, we have

$$\left\| \frac{1}{|\mathcal{S}_0|} \sum_{i \in \mathcal{S}_0} \mathbf{r}_i^{(l+1)} - \frac{1}{|\mathcal{S}_1|} \sum_{i \in \mathcal{S}_1} \mathbf{r}_i^{(l+1)} \right\|$$
(31)

$$= (\overline{\mu}_0 + \overline{\mu}_1 - 1) \left\| \overline{\mathbf{c}}_0^{(l+1)} - \overline{\mathbf{c}}_1^{(l+1)} \right\| + 2\sqrt{N} \delta^{\prime\prime\prime\prime(l+1)},$$

where $\delta^{\prime\prime\prime}(l+1)$ is also upper-bounded as in Eq. (29). Notice that

$$\left\| \mathbf{\bar{c}}_{0}^{(l+1)} - \mathbf{\bar{c}}_{1}^{(l+1)} \right\|$$
$$= \left\| \mathbf{W}_{\Psi}^{(l)} \right\| \left\| \frac{1}{|\mathcal{S}_{0}|} \sum_{i \in \mathcal{S}_{0}} \mathbf{h}_{i}^{(l)} - \frac{1}{|\mathcal{S}_{1}|} \sum_{i \in \mathcal{S}_{1}} \mathbf{h}_{i}^{(l)} \right\|$$
(32)

$$= \left\| \mathbf{W}_{\Psi}^{(I)} \right\| \Delta_{\mathrm{GSP}} \left(\mathbf{H}^{(I)} \right).$$

Combining Eq. (26), Eq. (27), and Eq. (32), we arrive that

$$\Delta_{\text{GSP}}\left(\mathbf{H}^{(l+1)}\right) \le \left((\overline{\mu}_{0} + \overline{\mu}_{1} - 1)\Delta_{\text{GSP}}\left(\mathbf{H}^{(l)}\right) + 2\sqrt{N}\delta^{(l+1)}\right) \left\|\mathbf{W}_{\Psi}^{(l)}\right\|,\tag{33}$$

where

$$\begin{split} |\delta'^{(l+1)}| &\leq \max\left(\delta_0^{(l+1)}, \delta_1^{(l+1)}\right), \delta_k^{(l+1)} = \max_{i \in \mathcal{S}_{1-k}} \left\| \mathbf{c}_i^{(l+1)} - \overline{\mathbf{c}}_k^{(l+1)} \right\|. \end{split}$$
Proof finished.

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C.2 \triangle_{GSP} for the Adapter

THEOREM 4. For a L-layer MLP adapter $\Xi : \mathbf{H} \to \mathbf{z} \in \mathbb{R}^N$, if Assumption 1 holds, we have

$$\Delta_{GSP}(\mathbf{z}) \leq \prod_{l=0,\dots,L-1} \left\| \mathbf{W}_{\Xi}^{(l)} \right\| \Delta_{GSP}(\mathbf{H}),$$
(35)

where $\mathbf{W}_{\Xi}^{(l)}$ is the parameter at the l-th layer of the adapter.

PROOF OF THEOREM 4. Denote the representation at the l-th layer as $\mathbf{Z}^{(l)}$ and $\mathbf{Z}^{(0)} = \mathbf{H}$. Notice that F (1.1) ъ.

$$\begin{split} \begin{array}{l} {}^{1287} & \Delta_{\text{GSP}}\left(\mathbf{Z}^{(l+1)}\right) = \left\| \mathbb{E}\left[\mathbf{z}_{i}^{(l+1)} \mid i \in \mathcal{S}_{0}\right] - \mathbb{E}\left[\mathbf{z}_{i}^{(l+1)} \mid i \in \mathcal{S}_{1}\right] \right\| \\ {}^{1289} & = \left\| \frac{1}{|\mathcal{S}_{0}|} \sum_{i \in \mathcal{S}_{0}} \mathbf{z}_{i}^{(l+1)} - \frac{1}{|\mathcal{S}_{1}|} \sum_{i \in \mathcal{S}_{1}} \mathbf{z}_{i}^{(l+1)} \right\| \\ {}^{1291} & = \left\| \frac{1}{|\mathcal{S}_{0}|} \sum_{i \in \mathcal{S}_{0}} \sigma\left(\mathbf{t}_{i}^{(l+1)}\right) - \frac{1}{|\mathcal{S}_{1}|} \sum_{i \in \mathcal{S}_{1}} \sigma\left(\mathbf{t}_{i}^{(l+1)}\right) \right\| \\ {}^{1292} & = \left\| \frac{1}{|\mathcal{S}_{0}|} \sum_{i \in \mathcal{S}_{0}} \sigma\left(\mathbf{t}_{i}^{(l+1)}\right) - \frac{1}{|\mathcal{S}_{1}|} \sum_{i \in \mathcal{S}_{1}} \sigma\left(\mathbf{t}_{i}^{(l+1)}\right) \right\| \\ {}^{1293} & = \left\| \frac{1}{|\mathcal{S}_{0}|} \sum_{i \in \mathcal{S}_{0}} \sigma\left(\mathbf{t}_{i}^{(l+1)}\right) - \frac{1}{|\mathcal{S}_{1}|} \sum_{i \in \mathcal{S}_{1}} \sigma\left(\mathbf{t}_{i}^{(l+1)}\right) \right\| \\ {}^{1294} & = \left\| \frac{1}{|\mathcal{S}_{0}|} \sum_{i \in \mathcal{S}_{0}} \mathbf{t}_{i}^{(l+1)} - \frac{1}{|\mathcal{S}_{1}|} \sum_{i \in \mathcal{S}_{1}} \mathbf{t}_{i}^{(l+1)} \right\|, \\ {}^{1298} & (36) \\ {}^{1300} & \text{where } \mathbf{t}_{i}^{(l+1)} = \mathbf{W}_{i}^{(l)} \mathbf{z}_{i}^{(l)}, \sigma(\cdot) \text{ denotes the activation function, and} \end{split}$$

where $\mathbf{t}_i^{(l+1)} = \mathbf{W}_{\Xi}^{(l)} \mathbf{z}_i^{(l)}$, $\sigma(\cdot)$ denotes the activation function, and (*a*) is due to the Lipschitz continuity of the activation functions

(Assumption 1). Because

$$\left\| \mathbf{t}_{0}^{(l+1)} - \mathbf{t}_{1}^{(l+1)} \right\|$$
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$$= \left\| \mathbf{W}_{\Xi}^{(l)} \right\| \left\| \frac{1}{|\mathcal{S}_0|} \sum_{i \in \mathcal{S}_0} \mathbf{z}_i^{(l)} - \frac{1}{|\mathcal{S}_1|} \sum_{i \in \mathcal{S}_1} \mathbf{z}_i^{(l)} \right\|$$
(37)
$$= \left\| \mathbf{W}_{\Xi}^{(l)} \right\| \Delta_{\text{GSP}} \left(\mathbf{Z}^{(l)} \right).$$

Thus we have

$$\Delta_{\rm GSP}(\mathbf{H}^{(l+1)}) \le \left\| \mathbf{W}_{\Xi}^{(l)} \right\| \Delta_{\rm GSP}(\mathbf{H}^{(l)}).$$
(38)

Proof finished.

C.3 Δ_{GSP} for the Pre-Training and Fine-Tuning **Graph Model**

PROOF OF THEOREM 2. For simplicity, we assume the both GNN backbone and the adapter have one layer. Thus we have

$$\begin{split} \Delta_{\text{GSP}}(\mathbf{z}) &\leq \|\mathbf{W}_{\Xi}\| \, \Delta_{\text{GSP}}(\mathbf{H}) \\ &\leq \|\mathbf{W}_{\Xi}\| \, \|\mathbf{W}_{\Psi}\| \left((\overline{\mu}_0 + \overline{\mu}_1 - 1) \Delta_{\text{GSP}} \left(\mathbf{X} \right) + 2\sqrt{N} \delta \right), \end{split}$$
(39)

where

$$|\delta| \le \max(\delta_0, \delta_1), \delta_k^{(l+1)} = \max_{i \in S_{1-k}} \left\| \mathbf{x}_i^{(l+1)} - \bar{\mathbf{c}}_k^{(l+1)} \right\|,$$
(40)

where
$$\overline{\mathbf{c}}_{k}^{(l+1)} = \sum_{i \in S_{k}} \mathbf{x}_{i}^{(l)} / |S_{k}|, \quad k = 0, 1.$$
 Proof finished. \Box

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