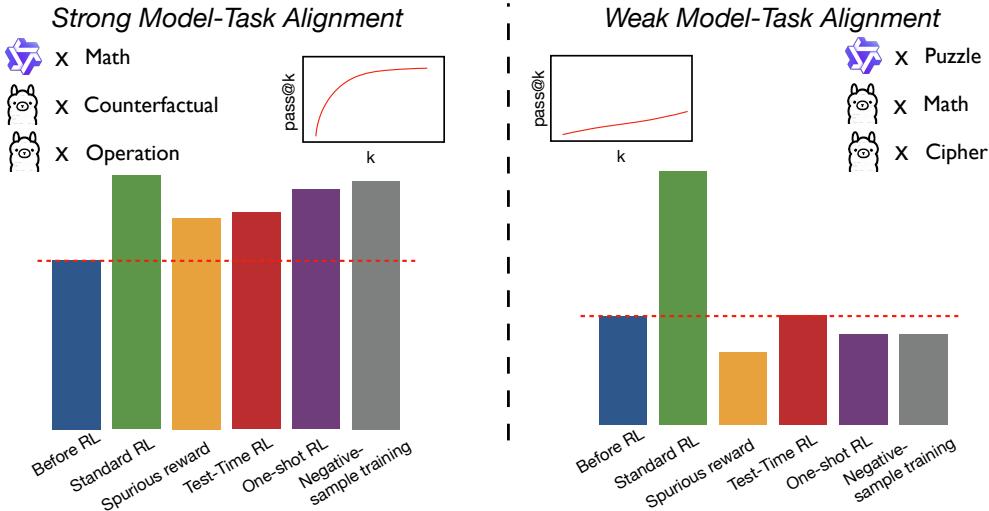


000 001 002 003 004 005 MIRAGE OR METHOD? HOW MODEL-TASK ALIGN- 006 MENT INDUCES DIVERGENT RL CONCLUSIONS 007 008 009

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ABSTRACT

011 Recent advances in applying reinforcement learning (RL) to large language models
012 (LLMs) have led to substantial progress. In particular, a series of remarkable yet
013 often counterintuitive phenomena have been reported in LLMs, exhibiting patterns
014 not typically observed in traditional RL settings. For example, notable claims
015 include that a single training example can match the performance achieved with
016 an entire dataset, that the reward signal does not need to be very accurate, and
017 that training solely with negative samples can match or even surpass sophisticated
018 reward-based methods. However, the precise conditions under which these obser-
019 vations hold—and, critically, when they fail—remain unclear. In this work, we
020 identify a key factor that differentiates RL observations: whether the pretrained
021 model already exhibits strong *Model-Task Alignment*, as measured by $\text{pass}@k$ accu-
022 racy on the evaluated task. Through a systematic and comprehensive examination
023 of a series of counterintuitive claims, supported by rigorous experimental validation
024 across different model architectures and task domains, our findings show that while
025 standard RL training remains consistently robust across settings, many of these
026 counterintuitive results arise only when the model and task already exhibit strong
027 model-task alignment. In contrast, these techniques fail to drive substantial learning
in more challenging regimes, where standard RL methods remain effective.



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045 Figure 1: Model-task alignment, which is measured by $\text{pass}@k$ accuracy on the evaluated task, drives
046 distinct outcomes from the same series of RL approaches.

1 INTRODUCTION

047 Reinforcement Learning (RL) (Sutton et al., 1998) has emerged as a transformative post-training
048 technique for Large Language Models (LLMs), enabling them to follow instructions (Ouyang et al.,
049 2022) and align with human preferences (Ziegler et al., 2019; Rafailov et al., 2024). A particularly
050 prominent application focuses on enhancing reasoning capabilities, as exemplified by breakthrough
051 models such as OpenAI-o1 (Jaech et al., 2024), DeepSeek-R1 (Guo et al., 2025), QwQ (Team,
052 2025), and Kimi-1.5 (Team et al., 2025). These systems demonstrate remarkable performance across
053

054 reasoning-intensive domains including coding (Jain et al., 2024), mathematics (Lewkowycz et al.,
 055 2022; He et al., 2024), and logical reasoning (Liu et al., 2025; Chen et al., 2025).

056 While RL yields significant performance improvements in LLM reasoning—mirroring the success of
 057 RL in traditional domains such as games (Silver et al., 2017a;b)—we also observe several remarkable
 058 yet often counterintuitive empirical phenomena. These effects appear to be unique to LLMs and
 059 would be considered unexpected in traditional RL settings. For instance, single training examples
 060 can match or rival full-dataset training performance (Wang et al., 2025), ground-truth reward may
 061 be surprisingly dispensable (Shao et al., 2025), and training with negative samples alone can match
 062 sophisticated reward-based methods (Agarwal et al., 2025).

063 Although these findings have generated considerable enthusiasm, the precise conditions under
 064 which they hold, and when they break down, remain insufficiently explored. Given that these
 065 observations may have important implications for RL practices, it is concerning that the conclusions
 066 are largely based on limited experimental settings, where Qwen models (Qwen et al., 2025) trained
 067 on mathematical tasks dominate the landscape.

068 To this end, we carry out a systematic empirical investigation of several notable RL claims, supported
 069 by rigorous experimental validation across diverse model architectures and task domains. Concretely,
 070 we experiment with both Qwen and non-Qwen models on math and other tasks. Our controlled
 071 experiments reveal that *model-task alignment*, defined as the degree to which model capabilities match
 072 task requirements, is a critical indicator for categorizing RL observations. Specifically, models benefit
 073 from noisy rewards, test-time RL (Zuo et al., 2025), minimal training, and negative-sample training
 074 primarily within their domains of expertise, where these techniques fail for unfamiliar tasks even
 075 though standard RL training can succeed. Interestingly, we also observe that certain meta-patterns
 076 hold consistently across different settings. For instance, one-shot RL training is generally effective for
 077 the specific task to which the training example belongs, and negative-sample training helps stabilize
 078 model entropy, even though it does not always lead to overall improvements in accuracy.

079 We evaluate the “alignment” between model capabilities and task requirements using $\text{pass}@k$ accuracy,
 080 which we find to be a reliable indicator for distinguishing these counterintuitive RL phenomena.
 081 Our hypothesis is that strong, inherent model capabilities can be readily activated through minimal
 082 training, even when guided by incorrect reward signals, whereas unfamiliar tasks demand substantially
 083 more effort—cases that we argue dominate when scaling up RL compute. Concurrent work (Wu
 084 et al., 2025) investigates the mechanism behind spurious rewards and attributes their effectiveness
 085 primarily to data leakage in Qwen models on the test set. However, our results suggest otherwise: we
 086 find that spurious rewards remain effective even in the absence of contamination, provided the model
 087 already exhibits strong alignment on the evaluated task.

088 Our study reveals that, unlike traditional RL training, distinct RL mechanisms emerge in the context
 089 of LLMs, depending on whether the pretrained model is already familiar with the target tasks. On the
 090 one hand, this suggests that RL phenomena should be interpreted with extra caution, as they may only
 091 reflect one of these two mechanisms. On the other hand, it also opens up opportunities for jointly
 092 optimizing base model pretraining (or mid-training) and RL post-training. For example, one might
 093 enhance the domain-specific capabilities of the base model during mid-training, enabling effective
 094 RL with limited training data and potentially inaccurate reward signals, or alternatively, allocate most
 095 compute resources to the RL stage using carefully curated training data and precise reward signals.

096 2 ON UNIQUE PHENOMENA OF RL TRAINING IN LLM REASONING

097 Reinforcement Learning from Verifiable Rewards (RLVR) has achieved significant success in im-
 098 proving language model reasoning. While similar gains in accuracy from standard training have
 099 also been observed in traditional RL domains such as games, we have noticed several phenomena
 100 that appear unique to LLMs and would not typically be expected in conventional settings. For
 101 example, we highlight several remarkable, and at times counterintuitive, observations below: **(a)**
 102 **Unexpected robustness to unreliable or absent rewards:** Shao et al. (2025) demonstrate that
 103 random and incorrect reward signals can improve model performance, while Agarwal et al. (2025)
 104 show that reward-free, entropy-minimization objectives can rival reward-based approaches. Test-
 105 Time Reinforcement Learning (TTRL) proposed by Zuo et al. (2025) further reinforces this trend by
 106 generating reward signals through aggregating majority-vote outcomes, thereby guiding the model
 107 to evolve itself on the test set. Together, these suggest surprising fault tolerance in RL training that
 challenges standard assumptions about the critical role of accurate reward signals. **(b) One-shot**

108 **training sufficiency:** Wang et al. (2025) report that training on a single carefully selected example
 109 can match or exceed performance from full dataset training, challenging assumptions about data
 110 volume requirements. **(c) Negative-only signal effectiveness:** Zhu et al. (2025) demonstrate that
 111 using exclusively negative reward signals achieves comparable results to standard RL training while
 112 maintaining beneficial entropy properties.

113 These findings carry significant implications. If broadly confirmed, they would necessitate shifts in
 114 resource allocation—such as prioritizing data selection algorithms over dataset scale, questioning the
 115 necessity of highly accurate reward modeling, and potentially introducing new research directions.
 116 Therefore, we believe it is important to assess whether these conclusions hold in general, and if
 117 not, under what conditions they succeed or fail. Clarifying these patterns would not only help
 118 us understand the limitations of the current findings but also, in the opposite direction, reveal
 119 new opportunities for modifying models so that these findings become valid, thereby making RL
 120 training substantially easier. In this work, we will investigate these observations through controlled
 121 experiments comprehensively.

122 2.1 CENTRAL HYPOTHESIS: MODEL-TASK ALIGNMENT DEPENDENCY

124 As most of the findings discussed above are based on mathematical reasoning tasks using Qwen
 125 models (Qwen et al., 2025; Yang et al., 2025), a natural question arises: do these results generalize to
 126 other settings? For instance, Shao et al. (2025) reported that spurious rewards were ineffective with
 127 Llama (Meta, 2024) models on mathematical tasks. However, we argue that treating Qwen+math
 128 as merely a special case is an overly superficial categorization. It remains unclear what specifically
 129 makes Qwen+math unique, and what the deeper, more essential factors might be. We propose a
 130 guiding hypothesis for designing and categorizing experimental settings, which we call **Model-Task**
 131 **Alignment Dependency:** *the effectiveness of these unique RL findings fundamentally depend on the*
 132 *degree of alignment between a model’s inherent capabilities and the requirements of the task domain.*
 133 In other words, they depend on the model’s proficiency on the evaluated task. This hypothesis may
 134 or may not hold, but we will use it as a framework to categorize experimental settings in terms of
 135 whether the model–task combination is aligned or misaligned.

136 **Quantifying Model-Task Alignment with pass@k.** To systematically evaluate the degree of
 137 alignment between a model’s inherent capabilities and the requirements of specific task domains, we
 138 employ the pass@k metric as our primary measure of model-task proficiency. Pass@k represents the
 139 probability that at least one correct solution appears among k independent samples generated by the
 140 model for a given problem. This metric effectively captures how well a model’s existing knowledge
 141 and reasoning patterns align with the demands of a particular task.

142 Formally, for a problem x_i from evaluation dataset \mathcal{D} , we generate n samples ($n \geq k$) and count
 143 the number of correct samples as c_i , then the unbiased estimator of pass@k over the dataset is:

$$144 \text{pass@k} := \mathbb{E}_{x_i \sim \mathcal{D}} [1 - \binom{n-c_i}{k} / \binom{n}{k}].$$

145 2.2 STRATEGIC MODEL AND TASK SELECTION

146 Building on our *Model-Task Alignment Dependency* hypothesis outlined in Section 2.1, we strategi-
 147 cally design model-task combinations that test the boundaries of current claims in RL for language
 148 model reasoning. Our experimental design is motivated by the critical need to distinguish between
 149 findings that represent universal RL properties versus those that emerge from specific model-task
 150 capability alignments. We evaluate two representative language models from different families:
 151 Qwen2.5-7B-Base (Qwen et al., 2025) and Llama-3.1-8B-Instruct (Meta, 2024), enabling system-
 152 atic comparison across model architectures with varying baseline capabilities while controlling for
 153 architectural differences at comparable parameter scales.

154 Our evaluation encompasses mathematical and logical reasoning domains. For mathematical reason-
 155 ing, we employ AIME24 (AIME, 2024), MATH500 (Hendrycks et al., 2021) and AMC23 (AMC,
 156 2023). For logical reasoning, we utilize SynLogic (Liu et al., 2025) (synthetic puzzles with 35
 157 task types, we use the validation split), BBH (Suzgun et al., 2022) (multi-step reasoning tasks),
 158 BBEH Kazemi et al. (2025) (extended-difficulty version), and KOR-Bench (Ma et al., 2024)
 159 (knowledge-orthogonal reasoning across five categories).

160 To operationalize our hypothesis, we systematically measure alignment strength using pass@k metrics
 161 across all model-task combinations. As demonstrated in Figure 2, models exhibit markedly different

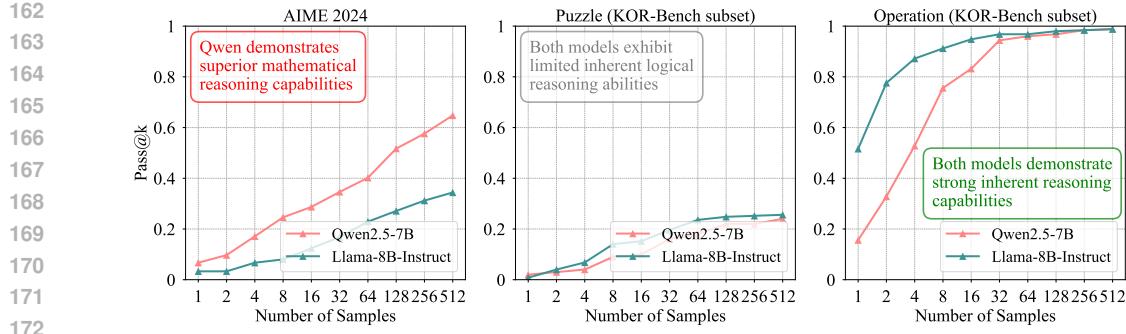


Figure 2: Pass@k for different tasks. Different LLMs have significantly different abilities on different tasks, which will affect how the RL techniques perform across model-task combinations.

inherent capabilities across domains. Based on comprehensive evaluation (full results in Appendix C), we identify cases of strong model-task alignment, such as Qwen2.5 on mathematical domains and both models on Operation and Counterfactual subsets of KOR-Bench, as well as weak model-task alignment cases, such as Llama3.1 on mathematical domains and both models on other logical reasoning tasks. This categorization enables us to test whether counterintuitive RL phenomena are artifacts of specific model-task alignments or represent fundamental properties of reinforcement learning in language model reasoning.

2.3 THE CONTAMINATION HYPOTHESIS

Concurrent work from Wu et al. (2025) proposed an alternative hypothesis, where they specifically focus on the spurious reward pattern and suggest that it stems primarily from dataset contamination during pre-training. They further confirmed the presence of data leakage in the Qwen models on several mathematical benchmarks. While we acknowledge contamination as a valid concern, our hypothesis diverges by emphasizing the distinction between contamination and inherent task proficiency. In particular, models may demonstrate strong task performance without direct contamination of the test data. In what follows, we categorize different experimental settings based on their contamination and inherent model-task alignment status. Later, in our experiments, we will empirically show that contamination is not the underlying cause; instead, model-task alignment serves as a more reliable differentiator.

Model	Portion	AMC 23		MATH500		Puzzle		Operation	
		ROUGE	EM	ROUGE	EM	ROUGE	EM	ROUGE	EM
Qwen2.5-7B	0.4	63.78	23.91	50.36	8.20	19.56	0.00	21.37	0.00
	0.6	64.42	33.73	60.98	21.20	19.62	0.00	24.25	0.00
	0.8	73.23	49.39	66.42	40.20	19.24	0.00	20.18	0.00
Llama-3.1-8B	0.4	27.18	0.00	23.09	0.60	18.27	0.00	21.83	0.00
	0.6	30.64	0.00	40.56	3.80	17.31	0.00	18.34	0.00
	0.8	44.54	4.81	48.33	17.8	15.85	0.00	16.75	0.00

Table 1: Contamination Analysis across model-task combinations. Portion refers to the truncation ratio of the prompt used to test whether models can complete the remaining content. **Red** indicates potential contamination with strong model-task alignment; **Gray** indicates no contamination with weak model-task alignment; **Green** indicates no contamination with strong model-task alignment.

To verify our hypothesis, we extend contamination analysis beyond Qwen-Math combinations. Following Wu et al. (2025), we evaluate model generation given partial prompts while preserving word boundaries (more details are provided in Appendix D). We employ greedy decoding and calculate both exact match (EM) rates and ROUGE-L scores, where ROUGE-L scores of 1.0 indicate perfect reconstruction. Table 1 alongside Appendix D show that Operation and Counterfactual subsets have no contamination, yet both models demonstrate strong inherent reasoning capabilities with high pass@k scores (see Appendix C). As we will show in our experiments, contamination is not the necessary condition for the effectiveness of these RL phenomena. Based on our contamination analysis and pass@k measurements, we categorize experimental settings into three groups: **Red (Potential Contamination + Strong Model-Task Alignment)**: Qwen2.5 on mathematical domains. **Gray**

216 (No Contamination + Weak Model-Task Alignment): Llama3.1 on mathematical domains; both
 217 models on SynLogic, BBH, BBEH, and Logic, Cipher, Puzzle subsets of KOR-Bench. **Green (No**
 218 **Contamination + Strong Model-Task Alignment):** Both models on Operation and Counterfactual
 219 subsets of KOR-Bench.

221 3 EXPERIMENTAL SETUP

223 **Training Datasets and Evaluation.** Except for the experiments on Test-Time RL (Section 4.2),
 224 we use DeepScaleR (Luo et al., 2025) as the training set for mathematical tasks and the training
 225 split of SynLogic-Easy (Liu et al., 2025) for logical tasks. Evaluation datasets are as described in
 226 Section 2.2. Following SynLogic (Liu et al., 2025), all evaluations are conducted in a zero-shot
 227 setting, with avg@8 metrics computed for AIME 2024 and SynLogic to mitigate variance.

228 **Training Configuration.** Our experiments default to using the DAPO algorithm with a group
 229 size of 16. Its effectiveness has been demonstrated on math (Yu et al., 2025) and logic tasks (Liu
 230 et al., 2025). We set $\epsilon_{low} = 0.2$, $\epsilon_{high} = 0.28$, max prompt length = 2048, max generation length =
 231 8192. We use dynamic sampling, which is crucial for improving the reward on SynLogic, and set
 232 max_num_gen_batches = 2. For logical tasks, each sampled batch often contains very few samples
 233 with non-zero reward variance. We apply two strategies: (1) if neither generated batch contains
 234 samples with non-zero reward variance, the second batch is used for training; (2) if the number of
 235 available samples is smaller than the batch size, samples are duplicated. We do not use a length penalty.
 236 In most experiments, we set $lr = 1e^{-6}$, batch size = 128, mini batch size = 64, temperature = 1.0.
 237 We fix all key hyperparameters across experiments to ensure that observed differences primarily
 238 reflect model-task alignment rather than tuning effort.

239 4 RQ1 – REWARD SIGNAL: HOW CRITICAL IS IT?

241 This section investigates the role of reward signal quality and its impact on RL performance for LLMs.
 242 Previous work in Reinforcement Learning with Human Feedback has shown that more accurate
 243 reward models do not always lead to better downstream performance (Chen et al., 2024). In the
 244 specific context of LLM reasoning, initial studies found that models with strong inherent reasoning
 245 abilities exhibit surprising robustness to noisy reward signals, whereas weaker models show poor
 246 noise tolerance (Lv et al., 2025; Shao et al., 2025). Building on these findings, we extend the analysis
 247 by considering diverse reward signals across different model-task combinations. Hyperparameters
 248 follow Section 3, and training runs for 300 steps (see Appendix B for more details).

249 4.1 RESULTS

252 We present results in Table 2. From the results, we identify three critical findings regarding the impact
 253 of reward signal quality on model performance (Appendix D.3 provides additional discussion):

254 **Ground Truth Rewards Consistently Outperform All Alternatives.** Across both model families
 255 and all task domains, utilizing ground truth rewards consistently yields the highest performance
 256 improvements. For instance, Qwen2.5-7B achieves substantial gains on AIME24 (14.2 vs. baseline
 257 3.3) and MATH500 (71.0 vs. baseline 40.8) when trained with accurate reward signals. This
 258 establishes ground truth rewards as the gold standard for RL training in reasoning tasks.

259 **Model-Task Alignment Determines Robustness to Noisy Rewards.** The effectiveness of noisy
 260 reward signals depends on model-task alignment strength across our three experimental categories. In
 261 settings with strong alignment (Red and Green categories), models demonstrate surprising robustness
 262 to spurious rewards, with Qwen2.5-7B maintaining reasonable performance on mathematical tasks
 263 and both models showing improvements on Operation and Counterfactual tasks even with random
 264 rewards. Conversely, in weak alignment settings, spurious rewards consistently fail to provide
 265 meaningful improvements, as seen with Llama3.1-8B on mathematical tasks and both models on
 266 challenging logical reasoning benchmarks. This pattern confirms that alignment strength, rather than
 267 contamination alone, determines robustness to noisy rewards.

268 **Limited Effectiveness of Self-Rewarded Methods.** Self-Rewarded Reinforcement Learning
 269 methods, including majority voting and entropy minimization, consistently underperform compared
 to external reward-based approaches. While self-rewarded methods shows some promise on math-

	Math Tasks										Logic Tasks				
						KOR Benchmark									
	AIME24	MATH500	AMC	SynLogic	BBH	BBEH	OP	CF	Puzzle	Logic	OP	CF	Puzzle	Logic	Cipher
Qwen2.5-7B Family															
Base	3.3	40.8	31.0	1.5	45.2	1.2	27.2	17.2	0.8	8.0	4.8				
RLVR (External Reward)															
Correct	14.2 _{+10.9}	71.0 _{+30.2}	62.4 _{+31.4}	42.6 _{+41.1}	62.7 _{+17.5}	6.8 _{+5.6}	82.4 _{+55.2}	79.6 _{+62.4}	16.8 _{+10.0}	46.4 _{+38.4}	20.4 _{+15.6}				
Random	10.0 _{+6.7}	57.5 _{+16.7}	45.7 _{+14.7}	10.2 _{+8.7}	32.7 _{-12.5}	0.0 _{-1.2}	53.6 _{+26.4}	30.8 _{+13.6}	1.2 _{+0.4}	6.8 _{-1.2}	3.6 _{-1.2}				
Incorrect	6.7 _{+3.4}	57.0 _{+16.2}	43.1 _{+12.1}	0.0 _{-1.5}	30.3 _{-14.9}	0.0 _{-1.2}	60.8 _{+33.6}	12.8 _{-4.4}	0.4 _{-0.4}	6.4 _{-1.6}	3.2 _{-1.6}				
Format	6.7 _{+3.4}	55.3 _{+14.5}	48.9 _{+17.9}	1.5 _{0.0}	44.4 _{-0.8}	2.4 _{+1.2}	37.2 _{+10.0}	21.6 _{+4.4}	0.8 _{0.0}	6.8 _{-1.2}	4.4 _{-0.4}				
Self-Rewarded Reinforcement Learning															
Vote	13.3 _{+10.0}	69.4 _{+28.6}	58.2 _{+27.2}	2.8 _{+1.3}	33.6 _{-11.6}	0.0 _{-1.2}	56.4 _{+29.2}	16.3 _{-0.9}	0.8 _{0.0}	6.8 _{-1.2}	3.2 _{-1.6}				
EM	11.6 _{+8.3}	70.8 _{+30.0}	57.8 _{+26.8}	1.5 _{0.0}	37.5 _{-7.7}	0.0 _{-1.2}	67.2 _{+40.0}	27.2 _{+10.0}	0.8 _{0.0}	6.8 _{-1.2}	3.2 _{-1.6}				
Llama3.1-8B-Instruct Family															
Base	3.3	32.5	20.2	0.8	38.6	4.1	60.4	86.4	2.0	28.8	8.4				
RLVR (External Reward)															
Correct	6.7 _{+3.4}	38.6 _{+6.1}	25.1 _{+4.9}	21.0 _{+20.2}	49.1 _{+10.5}	4.3 _{+0.2}	76.0 _{+15.6}	88.8 _{+2.4}	15.6 _{+13.6}	34.4 _{+7.6}	11.6 _{+3.2}				
Random	3.3 _{0.0}	26.8 _{-5.7}	21.3 _{+1.1}	0.0 _{-0.8}	32.1 _{-6.5}	4.1 _{0.0}	69.2 _{+8.8}	87.2 _{+0.8}	0.8 _{-1.2}	23.6 _{-5.2}	4.4 _{-4.0}				
Incorrect	2.1 _{-1.2}	26.4 _{-6.1}	18.7 _{-1.5}	0.8 _{0.0}	30.2 _{-8.4}	3.8 _{-0.3}	70.0 _{+9.6}	83.2 _{-3.2}	0.8 _{-1.2}	19.2 _{-9.6}	4.4 _{-4.0}				
Format	3.1 _{-0.2}	31.5 _{-1.0}	18.7 _{-1.5}	0.8 _{0.0}	36.4 _{-2.2}	4.1 _{0.0}	68.8 _{+8.4}	85.6 _{-0.8}	2.0 _{0.0}	28.0 _{-0.8}	6.4 _{-2.0}				
Self-Rewarded Reinforcement Learning															
Vote	4.6 _{+1.3}	37.7 _{+5.2}	23.0 _{+2.8}	1.5 _{+0.7}	35.9 _{-2.7}	4.3 _{+0.2}	67.2 _{+6.8}	83.2 _{-3.2}	2.0 _{0.0}	28.0 _{-0.8}	8.8 _{+0.4}				
EM	5.1 _{+1.8}	38.3 _{+5.8}	25.0 _{+4.8}	0.8 _{0.0}	34.8 _{-3.8}	4.1 _{0.0}	73.6 _{+13.2}	87.2 _{+0.8}	2.0 _{0.0}	23.6 _{-5.2}	7.6 _{-0.8}				

Table 2: Comprehensive evaluation of different reward signals in RL. ‘‘Vote’’ denotes Majority Voting, ‘‘EM’’ means entropy minimization on self-generated samples only; OP: Operation ; CF: Counterfactual. **Red** indicates potential contamination with strong model-task alignment; **Gray** indicates no contamination with weak model-task alignment; **Green** indicates no contamination with strong model-task alignment.

ematical tasks for Qwen2.5-7B (majority vote achieves 69.4 on MATH500), it fails to match the performance of ground truth external rewards and shows poor generalization to logical reasoning tasks across both model families.

4.2 TEST-TIME RL

Test-Time Reinforcement Learning (TTRL) (Zuo et al., 2025) addresses a fundamental challenge in LLM development: how to improve model performance on unlabeled test data without access to ground-truth labels for reward signals. It prompts the model to generate multiple responses to each test question and use the most frequent answer as the label for reward signals. Although the model is trained on the unlabeled test set, this approach is essentially no different from Self-Rewarded Reinforcement Learning when majority voting is employed. Thus, we are also curious whether TTTRL remains effective for different models and in domains beyond mathematics.

Table 3 shows the results of the Qwen and Llama models on different tasks. Due to the limited scale of the test dataset, we trained for 30 steps on all test datasets. It could be observed that in settings where the model–task alignment is strong, TTTRL yields substantial improvements, as exemplified by Qwen on math tasks and Operation subset. For tasks in which the model lacks initial prior knowledge, TTTRL fails to deliver improvements or yields only marginal gains. As discussed by Zuo et al. (2025), majority voting is the foundation of TTTRL. We also recorded the variation of Maj@16 during the training process; the results are shown in Table 9. We can observe that, in settings where TTTRL yields substantial improvements, Maj@16 consistently rises throughout training. Especially for Qwen on Operation subset, it achieves an absolute gain of 16.4 points. This further underscores that TTTRL’s efficacy hinges on strong model–task alignment, rather than on contamination.

5 RQ2 – Is ONE-SHOT ENOUGH FOR RL TO WORK?

Wang et al. (2025) demonstrated that training on a single carefully selected question can yield performance comparable to full dataset training, challenging conventional assumptions about data volume requirements in RL. Wang et al. (2025) designs a selection algorithm based on the variance of training rewards, and we denote samples selected by this algorithm as $m_{selected}$ for mathematical tasks and $l_{selected}$ for logical tasks. In addition to that, we also randomly selected one or two samples

324	Model	MATH500	SynLogic	OP	Model	MATH500	SynLogic	OP
325	Qwen2.5-7B	40.8	1.5	27.2	Llama-3.1-8B-Instruct	32.5	0.8	60.4
326	+TTRL	62.1 _{+21.3}	1.8 _{+0.3}	55.6 _{+28.4}	+TTRL	41.2 _{+8.7}	0.8 _{0.0}	83.6 _{+23.2}

328 Table 3: Test-Time Reinforcement Learning (TTRL) performance changes. TTRL produces significant
329 gains only when model-task alignment is strong (red and green cells).

330 from the dataset to form (m_{random}, l_{random}) and $(m'_{random}, l'_{random})$ for comparison. The specific
331 examples we used are detailed in Appendix K. The remaining experimental settings are consistent
332 with those described in Section 3, and we train models for 300 steps.

334	Dataset	Math Tasks					Logic Tasks					
		AIME24	MATH500	AMC	SynLogic	BBH	BBEH	KOR Benchmark				
								OP	CF	Puzzle	Logic	Cipher
Qwen2.5-7B												
339	\emptyset	3.3	40.8	31.0	1.5	45.2	1.2	27.2	17.2	0.8	8.0	4.8
340	full set	14.2 _{+10.9}	71.0 _{+30.2}	62.4 _{+31.4}	42.6 _{+41.1}	62.7 _{+17.5}	6.8 _{+5.6}	82.4 _{+55.2}	79.6 _{+62.4}	16.8 _{+10.0}	46.4 _{+38.4}	20.4 _{+15.6}
341	random-1	10.7 _{+7.4}	58.7 _{+17.9}	53.1 _{+22.1}	0.8 _{-0.7}	40.2 _{-5.0}	0.0 _{-1.2}	60.4 _{+33.2}	36.8 _{+19.6}	0.8 _{0.0}	6.4 _{-1.6}	4.4 _{-0.4}
342	random-2	12.5 _{+9.2}	63.0 _{+22.2}	55.7 _{+22.7}	2.4 _{+0.9}	43.1 _{-2.1}	1.2 _{0.0}	67.2 _{+40.0}	56.8 _{+39.6}	2.0 _{+1.2}	3.2 _{-4.8}	4.8 _{0.0}
343	selected-1	12.3 _{+9.0}	65.2 _{+24.4}	55.2 _{+24.2}	0.8 _{-0.7}	39.9 _{-5.3}	0.0 _{-1.2}	69.2 _{+42.0}	38.4 _{+21.2}	0.8 _{0.0}	8.0 _{0.0}	6.4 _{+1.6}
Llama3.1-8B-Instruct												
345	\emptyset	3.3	32.5	20.2	0.8	38.6	4.1	60.4	86.4	2.0	28.8	8.4
346	full set	6.7 _{+3.4}	38.6 _{+6.1}	25.1 _{+4.9}	21.0 _{+20.2}	49.1 _{+10.5}	4.3 _{+0.2}	76.0 _{+15.6}	88.8 _{+2.4}	15.6 _{+13.6}	34.4 _{+7.6}	11.6 _{+3.2}
347	random-1	3.8 _{+0.5}	30.5 _{-2.0}	21.1 _{+0.9}	0.8 _{0.0}	35.1 _{-3.5}	3.8 _{-0.3}	73.6 _{+13.2}	85.6 _{-0.8}	1.2 _{-0.8}	28.0 _{-0.8}	8.8 _{+0.4}
348	random-2	2.7 _{-0.6}	33.1 _{+0.6}	21.1 _{+0.9}	0.8 _{0.0}	36.7 _{-1.9}	4.1 _{0.0}	70.0 _{+9.6}	86.4 _{0.0}	2.8 _{+0.8}	27.2 _{-1.6}	8.4 _{0.0}
	selected-1	3.7 _{+0.4}	30.3 _{-2.2}	22.3 _{+2.1}	0.8 _{0.0}	34.4 _{-4.2}	3.8 _{-0.3}	69.2 _{+8.8}	88.8 _{+2.4}	2.0 _{0.0}	19.2 _{-9.6}	6.8 _{-1.6}

349 Table 4: One-shot RL Results. OP: Operation; CF: Counterfactual. We only observe the effectiveness
350 of one-shot reinforcement learning in settings with strong model-task alignment (red and green).

351 5.1 RESULTS

353 We present results in Table 4. Based on the experimental results, we identify two critical findings
354 regarding the effectiveness of one-shot reinforcement learning:

355 **One-shot RL Success Depends on Model-Task Alignment.** The effectiveness of one-shot re-
356inforcement learning is highly contingent on the alignment between model capabilities and task
357 domain requirements. In strong alignment settings (Red and Green categories), both models demon-
358strate remarkable ability to generalize from single examples: Qwen2.5-7B achieves performance
359 comparable to full dataset training on mathematical tasks (MATH500: 65.2 vs. full training 71.0),
360 while both Qwen2.5-7B and Llama3.1-8B-Instruct show substantial improvements on Operation
361 and Counterfactual tasks (e.g., Llama on Operation: 69.2 vs. baseline 60.4). However, this success
362 does not extend to weak alignment settings, where both models show minimal improvements across
363 challenging logical reasoning benchmarks. This suggests that one-shot RL serves as an effective
364 fine-tuning mechanism only when models already possess strong foundational capabilities.

365 **Sample Selection Strategy Shows Limited Impact.** Contrary to expectations, the sophisticated
366 sample selection algorithm proposed by Wang et al. (2025). does not consistently outperform
367 random sample selection. For Qwen2.5-7B on mathematical tasks, both selected and random samples
368 achieve similar performance levels (MATH500: selected 65.2 vs. random 58.7 and 63.0), while for
369 Llama3.1-8B-Instruct, the differences are negligible across all benchmarks. This finding challenges
370 the assumption that reward variance-based selection provides substantial advantages over simpler
371 random sampling approaches.

372 5.2 DISCUSSION

373 Wang et al. (2025) showed that training on a single sample for mathematical tasks can quickly improve
374 the accuracy of that sample and also lead to improvements on the test set. We attempt to verify this
375 conclusion on logical tasks. Considering that the initial rollout accuracy of the model on $l_{selected}$ is 0,
376 we additionally sample two examples whose initial rollout accuracies on Qwen2.5-7B are 5/16 and
377 1/16 (on Llama-3.1-8B-Instruct are 3/16 and 1/16), denoted as l_{simple} and l_{mid} . During training,
378 we track three metrics: the rollout accuracy of these examples acc_{1-shot} , the accuracy of the subtask

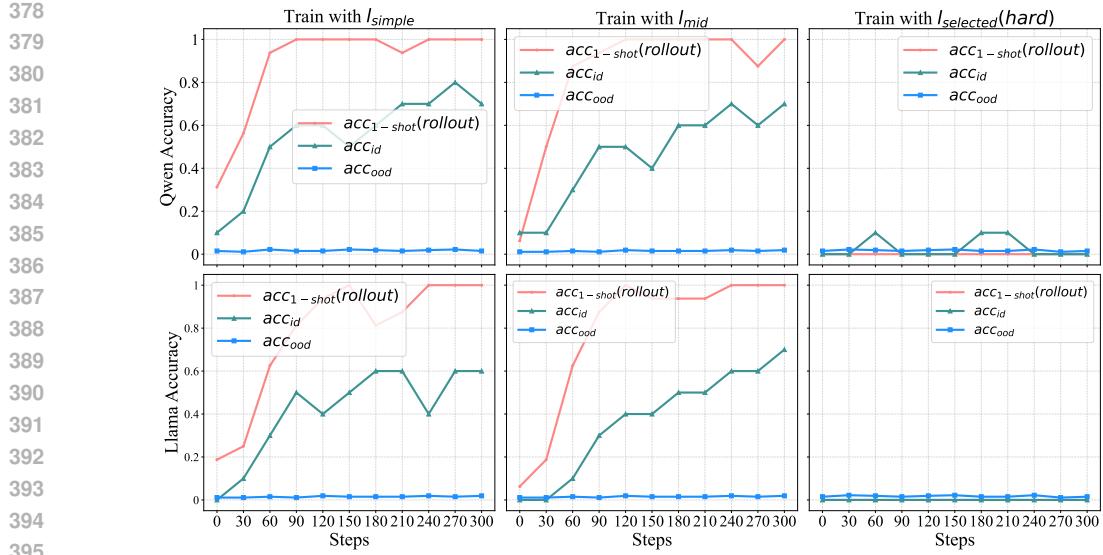


Figure 3: The changes in two models’ accuracy during the training. If the initial rollout accuracy is non-zero, both models rapidly fit the employed samples (l_{simple} , l_{mid}) and exhibit generalization within the same subtask; however, we observe no generalization to puzzles of other types.

to which this example belongs (in-distribution) acc_{id} , and the accuracy of other subtasks in SynLogic (out-of-distribution) acc_{ood} . The results are shown in Figure 3.

One-shot RL possesses the ability to generalize within the distribution. When the problem is relatively simple (with an initial rollout accuracy that is not zero), the model’s rollout accuracy on that sample quickly increases. Although the initial rollout accuracy of l_{mid} on Qwen is only one-fifth that of l_{simple} (on Llama is one-third), it still attains a high rollout accuracy within a few dozen steps. Since GRPO and DAPO compute advantages via intra-group normalization, the model is unable to derive any informative feedback from samples whose initial rollout accuracy is zero. Moreover, we observe that the test accuracy for the same subtask also continues to improve, demonstrating effective within-distribution generalization.

One-shot RL struggles to generalize to other types of logic puzzles. We find that while models can improve on tasks similar to their training example, they fail to transfer learning to different puzzle types. This suggests that one-shot learning primarily exploits existing model capabilities rather than developing new reasoning skills.

6 RQ3 — DOES RL WORK WITH ONLY NEGATIVE SAMPLES?

Recent work (Zhu et al., 2025) has demonstrated that training exclusively on negative samples can be surprisingly effective for model reasoning. However, these findings are primarily observed in scenarios with strong model-task alignment. We investigate whether negative-only training generalizes to weak model-task alignment scenarios, where models lack strong foundational capabilities.

Implementation Details. In our implementation, negative Sample Reinforcement (NSR) masks out all trajectories with reward 1 (correct answers) when computing the policy gradient, leaving only negative-rewarded samples to drive updates. Conversely, Positive Sample Reinforcement (PSR) ignores trajectories with reward 0 and optimizes only on positively rewarded samples. **All other hyperparameters remain identical to the DAPO baseline described in Section 3.**

6.1 RESULTS

Table 5 summarizes the performance of NSR and PSR relative to the full-signal DAPO baseline across our three experimental categories. It reveals distinct patterns based on model-task alignment:

Strong Model-Task Alignment Enables Effective Negative-Sample Learning. In settings with strong model-task alignment (Red and Green categories), both NSR and PSR show comparable effectiveness, recovering most of the performance gains achieved by full-signal DAPO. For Qwen2.5-

	Math Tasks						Logic Tasks					
	AIME24			SynLogic		BBH		BBEH		KOR Benchmark		
	AIME24	MATH500	AMC	SynLogic	BBH	BBEH	OP	CF	Puzzle	Logic	Cipher	
Qwen2.5-7B	3.3	40.8	31.0	1.5	45.2	1.2	27.2	17.2	0.8	8.0	4.8	
DAPO	14.2 _{+10.9}	71.0 _{+30.2}	62.4 _{+31.4}	42.6 _{+41.1}	62.7 _{+17.5}	6.8 _{+5.6}	82.4 _{+55.2}	79.6 _{+62.4}	16.8 _{+10.0}	46.4 _{+38.4}	20.4 _{+15.6}	
NSR	13.9 _{+10.6}	68.7 _{+27.9}	63.5 _{+32.5}	1.5 _{0.0}	41.2 _{-4.0}	1.6 _{+0.4}	60.4 _{+33.2}	36.8 _{+19.6}	2.0 _{+1.2}	6.8 _{-1.2}	4.8 _{0.0}	
PSR	14.0 _{+10.7}	70.3 _{+29.5}	63.1 _{+32.1}	24.8 _{+23.3}	57.1 _{+11.9}	4.3 _{+3.1}	73.6 _{+46.4}	38.4 _{+21.2}	9.2 _{+8.4}	31.2 _{+23.2}	11.2 _{+6.4}	
Llama3.1-8B	3.3	32.5	20.2	0.8	38.6	4.1	60.4	86.4	2.0	28.8	8.4	
DAPO	6.7 _{+3.4}	38.6 _{+6.1}	25.1 _{+4.9}	21.0 _{+20.2}	49.1 _{+10.5}	4.3 _{+0.2}	76.0 _{+15.6}	88.8 _{+2.4}	15.6 _{+13.6}	34.4 _{+7.6}	11.6 _{+3.2}	
NSR	7.9 _{+4.6}	36.9 _{+4.4}	24.7 _{+4.5}	0.0 _{-0.8}	34.2 _{-4.4}	4.3 _{+0.2}	67.2 _{+6.8}	86.4 _{0.0}	2.0 _{0.0}	28.0 _{-0.8}	5.2 _{-3.2}	
PSR	7.9 _{+4.6}	35.7 _{+4.2}	23.6 _{+3.4}	13.0 _{+11.5}	43.3 _{+4.7}	4.1 _{0.0}	69.2 _{+8.8}	89.6 _{+3.2}	12.0 _{+11.2}	34.4 _{+7.6}	10.8 _{+2.4}	

Table 5: Results of NSR and PSR under different settings. When Model-Task alignment is strong, both NSR and PSR yield pronounced performance gains for all models (Red and Green). Conversely, under weak alignment, NSR-trained models exhibit no noticeable improvement (Gray).

7B on mathematical tasks, both approaches achieve ~95% of the DAPO improvement (MATH500: NSR 68.7 and PSR 70.3 vs. DAPO 71.0). This demonstrates that when models already possess strong domain capabilities, either positive-only or negative-only signals can effectively drive learning.

Weak Model-Task Alignment Reveals Superior Performance of Positive-Only Signals. In weak alignment settings (Gray category), PSR consistently outperforms NSR across logical reasoning tasks. For instance, on SynLogic, PSR enables meaningful improvements (Qwen2.5-7B: 1.5 vs. 24.8, Llama3.1-8B: 0.8 vs. 13.0), while NSR shows minimal gains. Overall, while PSR and NSR demonstrate comparable effectiveness in strong alignment settings, PSR emerges as the more robust approach in challenging domains where models lack expertise.

6.2 DISCUSSION

The relationship between positive and negative samples in reinforcement learning is fundamentally connected to the exploration-exploitation trade-off, with entropy serving as a key mediator. To elucidate these dynamics in our experimental context, we examine how different sample types affect the exploration-exploitation balance through their impact on training entropy.

Negative Signals Help

Maintain Exploration. Figure 4 plots token-level entropy throughout training. Consistent with Zhu et al. (2025), NSR slows entropy collapse, especially on mathematical tasks—suggesting that penalising only erroneous trajectories can preserve output diversity. However, the flatter entropy curve on logical tasks corresponds to poorer final accuracy.

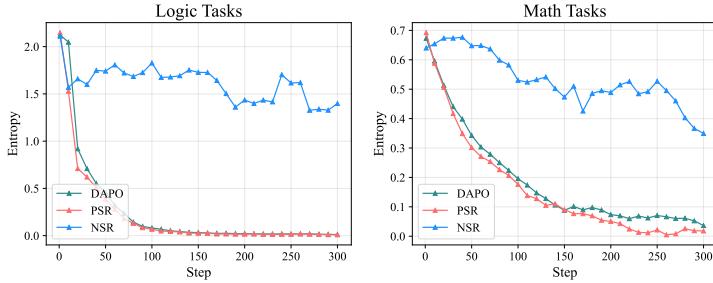


Figure 4: Entropy Dynamics of Qwen2.5-7B during Training. NSR can maintain the exploration space of RL, but a larger exploration space is not always favorable, as in logical tasks.

7 CONCLUSION

This work reveals that *Model-Task Alignment* strength, measured by pass@k accuracy, serves as the fundamental determinant of when counterintuitive RL phenomena emerge in language model reasoning. We demonstrate that remarkable behaviors—including robustness to spurious rewards, one-shot training effectiveness, and negative-only signal sufficiency—manifest primarily when models already possess strong foundational capabilities in the target domain, functioning more as capability elicitation mechanisms rather than genuine learning drivers for unfamiliar tasks.

486 REPRODUCIBILITY STATEMENT
487488 To ensure full reproducibility of our results, we conduct all experiments using publicly available mod-
489 els and datasets. We provide complete implementation code, detailed hyperparameter configurations,
490 and step-by-step reproduction instructions in the supplementary material.
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648 **A LLM USAGE STATEMENT**
649

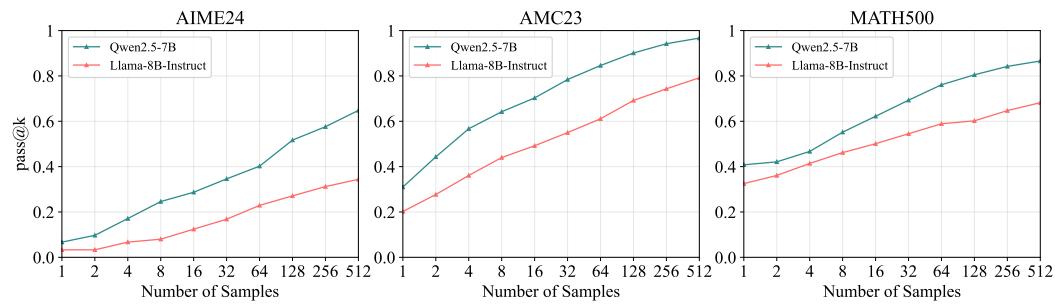
650 As non-native English speakers, we used LLMs solely to assist with grammatical correction and
651 linguistic polishing of the manuscript. The LLM was not involved in any aspect of conceptual
652 development, experimental design, data analysis, or interpretation of results. All scientific content,
653 including hypotheses, methodology, figures, and conclusions, was generated independently by the
654 authors. The use of the LLM was strictly limited to improving clarity and fluency of expression in
655 English, ensuring that language barriers do not impede the accurate communication of our research
656 contributions.

658 **B IMPLEMENTATION DETAILS**
659

660 Following the setting described in Section 3, we train with different rewards for 300 steps on
661 mathematical and logical reasoning tasks, respectively. The format reward is different from that of
662 Shao et al. (2025), we use the same format as SynLogic:

663 `<think>thinking process</think><answer>final answer</answer>`
664

665 We set $\gamma = 0.5$ for the random reward. For incorrect rewards, we reward rollouts that produce
666 incorrect answers during training for logic and code tasks. Apart from these changes, the definition
667 of the reward functions remains consistent with spurious reward (Shao et al., 2025).

669 **C MORE PASS@K RESULTS**
670

681 Figure 5: Pass@k for math tasks. Qwen demonstrates strong capabilities across all three mathematical
682 evaluation datasets.
683

685 **D CONTAMINATION EVALUATION**
686687 **D.1 IMPLEMENTATION DETAILS**

689 Our contamination analysis follows a systematic prompt truncation methodology to evaluate potential
690 data leakage across model-task combinations. Original prompts are truncated at varying ratios (0.4,
691 0.6, and 0.8) while preserving word boundaries, and models are asked to complete the remaining
692 content using greedy decoding for deterministic outputs. We measure contamination using ROUGE-L
693 scores between model completions and the actual remaining prompt content, where a perfect score of
694 1.0 indicates complete reconstruction and potential contamination. The evaluation pipeline employs
695 distributed processing to handle complex mathematical expressions and prevent evaluation timeouts,
696 with results aggregated across multiple rollouts to ensure statistical reliability.

697 **D.2 MORE RESULTS**
698699 **D.3 DISCUSSION ABOUT RQ1**
700

701 **How Different Reward Signals Affect the Behavior of LLMs.** Shao et al. (2025) observed that
in mathematical tasks, employing ground truth rewards decreases the frequency of code usage in

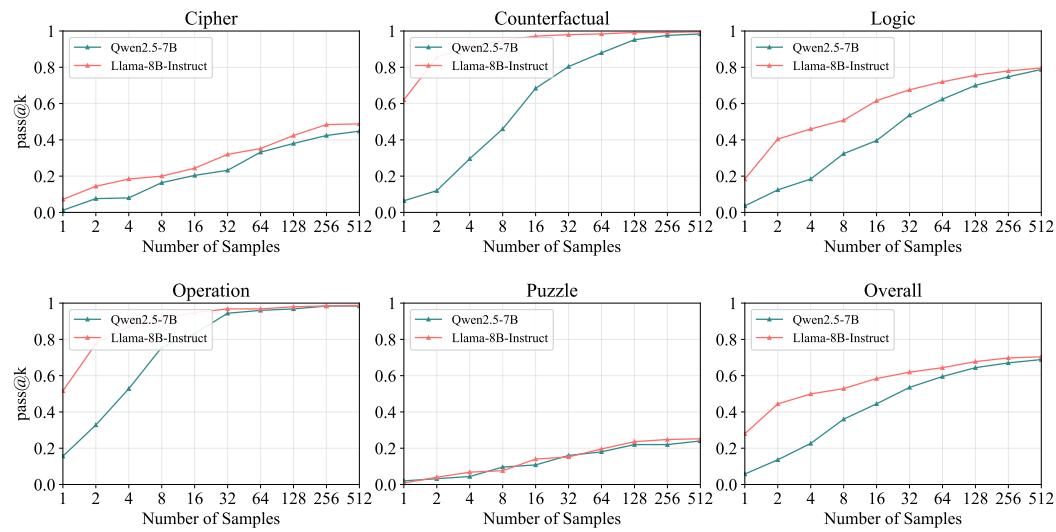


Figure 6: Pass@k for KOR-Bench. Both models demonstrate strong inherent reasoning capabilities in Operation and Counterfactual subtasks, but exhibit limited inherent logical reasoning abilities in Cipher, Puzzle and Logic.

Task Type	Benchmark	Model	Portion=0.4		Portion=0.6		Portion=0.8	
			ROUGE	EM	ROUGE	EM	ROUGE	EM
Math Tasks	AMC 23	Qwen2.5-7B	63.78	23.91	64.42	33.73	73.23	49.39
		Llama-3.1-8B	27.18	0.00	30.64	0.00	44.54	4.81
	MATH500	Qwen2.5-7B	50.36	8.20	60.98	21.20	66.42	40.20
		Llama-3.1-8B	23.09	0.60	40.56	3.80	48.33	17.8
Logic Tasks	AIME24	Qwen2.5-7B	44.64	10.00	48.69	13.33	60.08	30.00
		Llama-3.1-8B	26.08	0.00	30.80	0.00	50.50	13.33
	Puzzle	Qwen2.5-7B	19.56	0.00	19.62	0.00	19.24	0.00
		Llama-3.1-8B	18.27	0.00	17.31	0.00	15.85	0.00
	Operation	Qwen2.5-7B	21.37	0.00	24.25	0.00	20.18	0.00
		Llama-3.1-8B	21.83	0.00	18.34	0.00	16.75	0.00
	Counterfactual	Qwen2.5-7B	18.88	0.00	19.96	0.00	18.66	0.00
		Llama-3.1-8B	19.02	0.00	19.39	0.00	18.94	0.00
	Logic	Qwen2.5-7B	22.08	0.00	27.28	0.00	28.23	0.00
		Llama-3.1-8B	21.38	0.00	28.37	0.00	28.42	0.00
	Cipher	Qwen2.5-7B	34.61	0.00	41.03	0.00	44.77	0.00
		Llama-3.1-8B	29.59	0.00	36.95	0.00	42.93	0.00

Table 6: Extended Contamination Analysis across model-task combinations. **Red** indicates potential contamination with strong baseline performance; **Gray** indicates no contamination with weak baseline performance; **Green** indicates no contamination with strong baseline performance.

model responses. Their study also revealed that, in contrast to Qwen2.5-Math (Yang et al., 2024), the accuracy improvement of the Qwen2.5 Base model was primarily attributed to a shift from code-based reasoning to language-based reasoning. As shown in Table 7, we identify analogous trends in mathematical tasks. Specifically, for logic puzzles, the application of ground truth rewards similarly reduces the incidence of code in responses. However, other types of rewards, particularly

format and random rewards, do not demonstrate a significant impact on diminishing code usage frequency. We speculate that, throughout the RL training process, ground truth rewards can steer the model away from its old reasoning pattern (i.e., producing reasoning responses with code) and toward a more natural, language-based reasoning pattern.

Reward Type	MATH500		SynLogic	
	Before RL	After RL	Before RL	After RL
Correct		12.4		21.7
Random	89.1	94.2	57.3	48.2
Format		96.7		50.7
Incorrect		28.1		28.3

Table 7: Code Usage Count of Qwen2.5-7B before and after RL training with different rewards.

As shown in Table 2, spurious rewards are effective only on the Operation and Counterfactual for the Llama model; consequently, we also report the frequency of code-based reasoning before and after training on these two tasks. As shown in Table 8, we observe that, both before and after RL training, Llama almost never invokes code during the reasoning process. We attribute the sporadic use of code (0.8) to the fact that some SynLogic tasks explicitly require outputs to be presented as code blocks. This indicates that Llama and Qwen exhibit distinct reasoning patterns even though they both benefit from noisy reward signals in these settings.

Reward Type	Operation		Counterfactual	
	Before RL	After RL	Before RL	After RL
Correct		0.8		0.0
Random	0.0	0.0	0.0	0.0
Format		0.0		0.0
Incorrect		0.0		0.0

Table 8: Code Usage Count of Llama-3.1-8B-Instruct before and after RL training on two tasks.

E MORE TTRL RESULTS

	Step 0	Step 5	Step 10	Step 15	Step 20	Step 25	Step 30
Qwen+Math500	54.2	60.6	64.3	68.2	67.1	69.3	70.5+16.3
Qwen+SynLogic	2.2	3.0	3.7	4.4	4.4	4.4	5.2+3.0
Qwen+OP	46.0	53.6	55.6	57.2	58.8	60.0	60.0+16.4
Llama+Math500	46.3	48.6	51.3	53.2	53.9	55.0	54.7+8.4
Llama+SynLogic	1.5	1.5	2.2	1.5	2.2	2.2	2.2+0.7
Llama+OP	73.6	78.0	79.6	84.0	83.6	86.8	88.4+14.8

Table 9: The variation of Maj@16 as training progresses. In tasks where TTRL brings significant improvements (red and green), Maj@16 continues to improve with training.

F MORE DISCUSSION ABOUT DIFFICULT EXAMPLE IN ONE-SHOT RL

During training with $l_{selected}$, apart from the rollout accuracy (reward) remaining consistently at 0, metrics such as entropy and response length also exhibit almost no changes. As shown in Figure 7, after 300 training steps, the model still maintains a large reinforcement learning exploration space.

G RESULTS ON CODE GENERATION TASKS

We additionally include code-generation tasks to further validate the generality of our findings. Specifically, we evaluate on HumanEval (Chen et al., 2021) and LiveCodeBench (2024.8–2025.1) (Jain

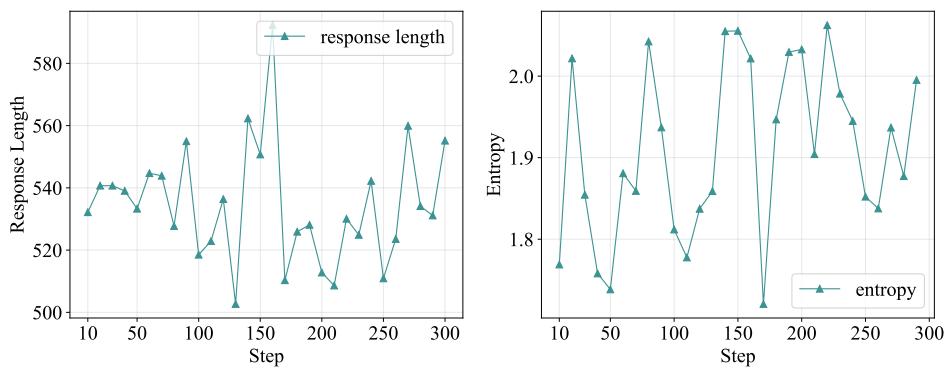


Figure 7: Training Dynamics of Qwen2.5-7B when trained with $l_{selected}$. Entropy and response length exhibit almost no changes.

et al., 2024). The live nature of LiveCodeBench ensures that data contamination is almost impossible. However, both models achieve relatively high Pass@1 scores on HumanEval. To assess whether these high scores may result from contamination, we conduct an analysis analogous to that in Table 1. The results are shown in Table 10. Similar to the math tasks, we observe a higher risk of data contamination in Qwen. Accordingly, we categorize Qwen/HumanEval as red and Llama/HumanEval as green. And we show the Pass@K curves for LiveCodeBench in Figure 8. Neither model exhibits sufficiently strong capability on this benchmark; as K increases, their performance does not rise as sharply as it does on tasks such as Operation (shown in Figure 6). Consequently, we categorize Qwen/LiveCode and Llama/LiveCode as gray.

Model	Portion	ROUGE	EM	Model	Portion	ROUGE	EM
Qwen2.5-7B	0.4	56.32	9.7	LLama3.1-8B	0.4	23.42	0.0
	0.6	60.89	14.3		0.6	32.13	1.2
	0.8	66.81	36.7		0.8	47.32	8.4

Table 10: Contamination Analysis on HumanEval.

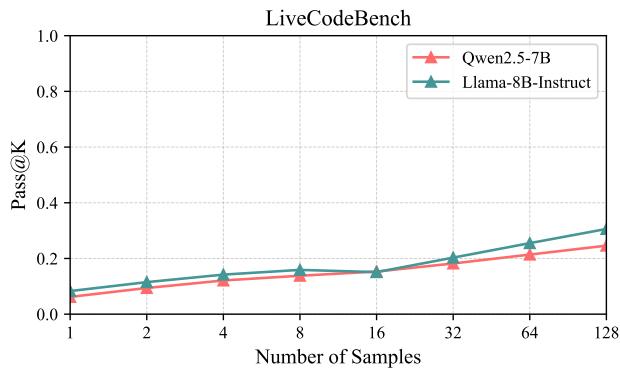


Figure 8: Pass@K curves for LiveCodeBench.

For training, we use code-r1-12k (Liu, 2025) as the training data. Importantly, to keep the setup consistent with the math and logic tasks, we assign a correctness reward of 1 only when the generated code passes all test cases; otherwise, the model receives no correctness reward at all. Because code outputs are difficult to aggregate via majority voting, we do not evaluate the Vote setting in this task. To reduce variance, we report avg@8, following the same protocol as SynLogic and AIME24.

The results of the two code evaluation tasks are shown in Table 11. From the table, we can see that under the standard RL setting, the model shows clear improvements on both HumanEval and LiveCodeBench. Under non-standard settings, only the red-category case—Qwen/HumanEval and the green-category case Llama/HumanEval—exhibit small gains, while no consistent improvement is

	HumanEval	LiveCodeBench		HumanEval	LiveCodeBench
Qwen2.5-7B	52.4	6.2	Llama3.1-8B	68.4	8.3
Correct	65.2 _{+12.8}	15.4 _{+9.2}	Correct	75.1 _{+6.7}	12.0 _{+3.7}
Format	58.5 _{+6.1}	5.2 _{-1.0}	Format	69.2 _{+0.8}	8.9 _{+0.6}
Random	56.1 _{+3.7}	5.0 _{-1.2}	Random	67.4 _{-1.0}	7.3 _{-1.0}
Incorrect	53.0 _{+0.6}	4.2 _{-2.0}	Incorrect	68.8 _{+0.4}	6.0 _{-2.3}
EM	58.1 _{+5.7}	6.2 _{+0.0}	EM	70.4 _{+2.0}	8.0 _{-0.3}
1-shot	51.5 _{-0.9}	6.0 _{-0.2}	1-shot	69.0 _{+0.6}	6.5 _{-1.8}
NSR	55.1 _{+2.7}	7.4 _{+1.2}	NSR	70.4 _{+2.0}	6.8 _{-1.5}

Table 11: Code-generation results on HumanEval and LiveCodeBench. The 1-shot samples are selected based on Wang et al. 2025’s method.

observed in the weak-alignment setting. This is consistent with our observations on math and logic tasks.

H RESULTS OF A MORE WEAKLY ALIGNED MODEL: MISTRAL-7B-v0.1

We additionally include Mistral-7B-v0.1 (Jiang et al., 2023) in the weak-alignment setting. Its performance on math and logic tasks is worse than that of Llama-3.1-8B-Instruct, which allows us to provide more weakly aligned settings. Results are shown in Table 12. We can see that Mistral shows stable improvements on math and logic tasks only under the standard RL setting. This further reinforces the validity of our conclusions under the weak-alignment setting.

	Math Tasks						Logic Tasks					
	AIME24	MATH500	AMC	SynLogic	BBH	BBEH	KOR Benchmark					Cipher
							OP	CF	Puzzle	Logic	Cipher	
Mistral-7B-v0.1 (Weakly Aligned)												
Base	0.0	6.8	3.4	0.0	27.1	0.4	11.2	22.8	2.4	28.4	2.4	
RLVR (External Reward)												
GroundTruth	3.3 _{+3.3}	17.6 _{+10.8}	12.5 _{+9.1}	14.6 _{+14.6}	38.9 _{+11.8}	3.2 _{+2.8}	26.8 _{+15.6}	43.4 _{+20.6}	9.8 _{+7.4}	46.2 _{+17.8}	8.8 _{+6.4}	
Format	0.0 _{+0.0}	6.4 _{-0.4}	2.0 _{-1.4}	0.0 _{+0.0}	24.3 _{-2.8}	0.0 _{-0.4}	14.6 _{+3.4}	26.2 _{+3.4}	2.0 _{-0.4}	26.8 _{-1.6}	3.2 _{+0.8}	
Random	0.0 _{+0.0}	6.4 _{-0.4}	3.2 _{-0.2}	0.4 _{+0.4}	21.2 _{-5.9}	0.4 _{+0.0}	9.2 _{-2.0}	19.4 _{-3.4}	2.0 _{-0.4}	22.4 _{-6.0}	2.0 _{-0.4}	
Incorrect	0.0 _{+0.0}	5.6 _{-1.2}	1.0 _{-2.4}	0.0 _{+0.0}	13.4 _{-13.7}	0.0 _{-0.4}	9.0 _{-2.2}	19.2 _{-3.6}	1.8 _{-0.6}	21.0 _{-7.4}	1.8 _{-0.6}	
Self-Rewarded Reinforcement Learning												
Vote	0.4 _{+0.4}	5.8 _{-1.0}	3.2 _{-0.2}	0.0 _{+0.0}	14.2 _{-12.9}	0.4 _{+0.0}	12.8 _{+1.6}	28.6 _{+5.8}	1.2 _{-1.2}	18.8 _{-9.6}	3.6 _{+1.2}	
EM	0.0 _{+0.0}	7.8 _{+1.0}	2.4 _{-1.0}	0.8 _{+0.8}	23.4 _{-3.7}	0.4 _{+0.0}	10.4 _{-0.8}	19.2 _{-3.6}	1.4 _{-1.0}	24.4 _{-4.0}	2.0 _{-0.4}	
Few-shot Reinforcement Learning												
1-shot (selected)	0.4 _{+0.4}	8.4 _{+1.6}	2.8 _{-0.6}	0.0 _{+0.0}	22.4 _{-4.7}	0.0 _{-0.4}	8.8 _{-2.4}	19.8 _{-3.0}	2.4 _{+0.0}	29.6 _{+1.2}	2.0 _{-0.4}	
Negative Sampling Reinforcement Learning												
NSR	0.8 _{+0.8}	6.4 _{-0.4}	3.0 _{-0.4}	0.0 _{+0.0}	24.2 _{-2.9}	0.4 _{+0.0}	12.4 _{+1.2}	23.2 _{+0.4}	2.8 _{+0.4}	24.0 _{-4.4}	2.0 _{-0.4}	

Table 12: Results of Mistral-7B-v0.1.

H.1 DISCUSSION

In Tables 2 and 5, although Llama-Math is a weakly aligned model-task pair, both self-rewarded methods and NSR consistently lead to performance improvements. Here we provide an explanation for this phenomenon: Although we categorize Llama-Math as a weakly aligned model-task pair, its alignment is still noticeably stronger than that of Llama-Logic. We see two reasons for this:

1. As shown in Table 1, although we do not observe the severe contamination found in Qwen, the Llama-Math combination exhibits a higher risk of data contamination compared with Llama-Logic (EM = 0)
2. As shown in Figure 5, while the model’s performance does not increase rapidly as K grows, its curve is still significantly sharper than that of tasks such as Puzzle in Figure 6

918 That being said, model–task alignment strength may be more continuous rather than falling into
 919 just three discrete categories. When the alignment is slightly stronger, as in the case of LLama
 920 on math tasks, some RL methods may begin to take effect. The results on Mistral further support
 921 our conclusion: due to its weaker alignment, neither NSR nor the self-reward method achieves
 922 consistent performance gains on the math tasks. Identifying such an “emergence boundary” in terms
 923 of model–task alignment strength is an interesting direction for future work.

925 I KL DIVERGENCE BETWEEN THE INITIAL AND TRAINED POLICIES

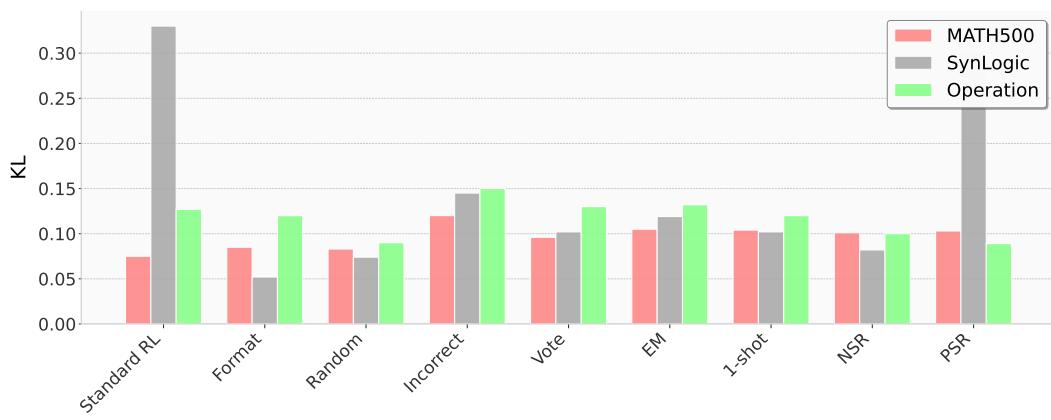
928 During training, consistent with DAPO (Yu et al., 2025), we removed the KL regularization term
 929 from the loss function. This enables us to fairly compare the impact of different training methods on
 930 the output distribution under varying levels of alignment.

931 We explore it in three representative settings: Qwen on MATH500 (red), Qwen on Operation (green),
 932 and Qwen on SynLogic (gray). Specifically, we use trained policies to generate trajectories via
 933 greedy decoding. Then, we feed these trajectories into the untrained reference model to obtain the
 934 log-probabilities for each token. We follow the approach used in DeepSeek-R1 (Guo et al., 2025) for
 935 computing KL divergence:

$$937 \text{KL}(\pi_\theta || \pi_{ref}) = \frac{\pi_{ref}(o_i|q, o_{<i})}{\pi_\theta(o_i|q, o_{<i})} - \log \frac{\pi_{ref}(o_i|q, o_{<i})}{\pi_\theta(o_i|q, o_{<i})} - 1 \quad (1)$$

940 and compute the average KL over all tokens. We present the results in the Figure 9. From the results,
 941 we can observe that:

- 943 • In the standard RL setting, weaker model–task alignment leads to a larger divergence
 944 between the pre- and post-training output distributions (the gray is substantially higher than
 945 the green and red ones).
- 946 • In the weak-alignment setting (gray), only standard RL and PSR can drive the model away
 947 from the reference model and achieve substantial performance improvements (+41.1 and
 948 +23.3 on SynLogic).
- 949 • In the strong-alignment setting (green and red), neither the reward choices nor the sampling
 950 methods substantially amplify the divergence between the pre- and post-training output
 951 distributions.



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 Figure 9: KL divergence between the initial and trained policies under different settings.

Based on these results, we hypothesize that in the strong-alignment setting, large deviations from the initial policy are unnecessary; small updates are sufficient to improve performance. This also helps explain why spurious-reward methods can still be effective, as the initial policy is already close to the correct solution. In contrast, in the weak-alignment setting, merely oscillating around the initial policy does not yield meaningful gains—substantial improvement requires moving further away under the guidance of correct rewards to form a stable and effective reasoning pattern.

972 I.1 POTENTIAL CHANGES INTRODUCED BY ADDING KL REGULARIZATION
973

974 A natural question is whether introducing KL regularization during training would affect our con-
975 clusions. Considering that the difference between the pre- and post-training output distributions is
976 small in the strong-alignment setting, we believe that introducing KL regularization does not affect
977 the overall trend of performance changes, although it may influence convergence speed (Yu et al.,
978 2025). To assess the impact under the weak-alignment setting, particularly for standard RL and PSR,
979 we set the KL penalty coefficient to 0.001 and retrain Qwen on the logic tasks. The experimental
980 results are shown in Table 13. Introducing KL regularization leads to a slight drop in performance.
981 However, the overall trend remains the same as in the setting without regularization, indicating that
982 the presence or absence of KL regularization does not affect our conclusions.
983

	SynLogic	BBH	BBEH
Pretrain	1.5	45.2	1.2
Standard	42.6 _{+41.1}	62.7 _{+17.5}	6.8 _{+5.6}
Standard + KL	33.6 _{+32.1}	52.1 _{+6.9}	6.8 _{+5.6}
PSR	24.8 _{+23.3}	57.1 _{+11.9}	4.3 _{+3.1}
PSR + KL	17.3 _{+15.8}	49.1 _{+3.9}	3.8 _{+2.6}

991 Table 13: Performance of different training methods with and without KL regularization under the
992 weak-alignment setting.
993

994 I.2 DISCUSSION
995

996 From Figure 9, we believe that the divergence between the pre- and post-training output distributions
997 in a successful standard RL run (without collapse) can serve as a complementary indicator of
998 model–task alignment strength. This is also consistent with our intuition: in the strong-alignment
999 setting, the model does not need to extensively explore regions far from the initial policy to achieve
1000 performance gains. In contrast, in the weak-alignment setting, a successful training process must
1001 sufficiently explore regions farther away from the initial policy in order to discover an effective
1002 reasoning pattern. Moreover, the consistency between KL divergence and Pass@K further reinforces
1003 that Pass@K can be viewed as a reliable proxy for model–task alignment.
1004

1005 J CORRELATION BETWEEN PASS@K AND RL GAINS
1006

1007 In Figure 10, we present the relationship between RL gains and Pass@K. Each data point in the figure
1008 is derived from the results reported in Tables 2, 3, 4, and 5. And each point represents a task, with
1009 points in the first column averaged over different reward signals. We can find that across different
1010 K values (32, 128, 512) and across the various RL phenomena we study, we consistently observe
1011 that performance improvements grow as Pass@K increases. This further strengthens the connection
1012 between model–task alignment strength and performance gains.
1013

1014 K FEW-SHOT RL EXAMPLE DETAILS
1015

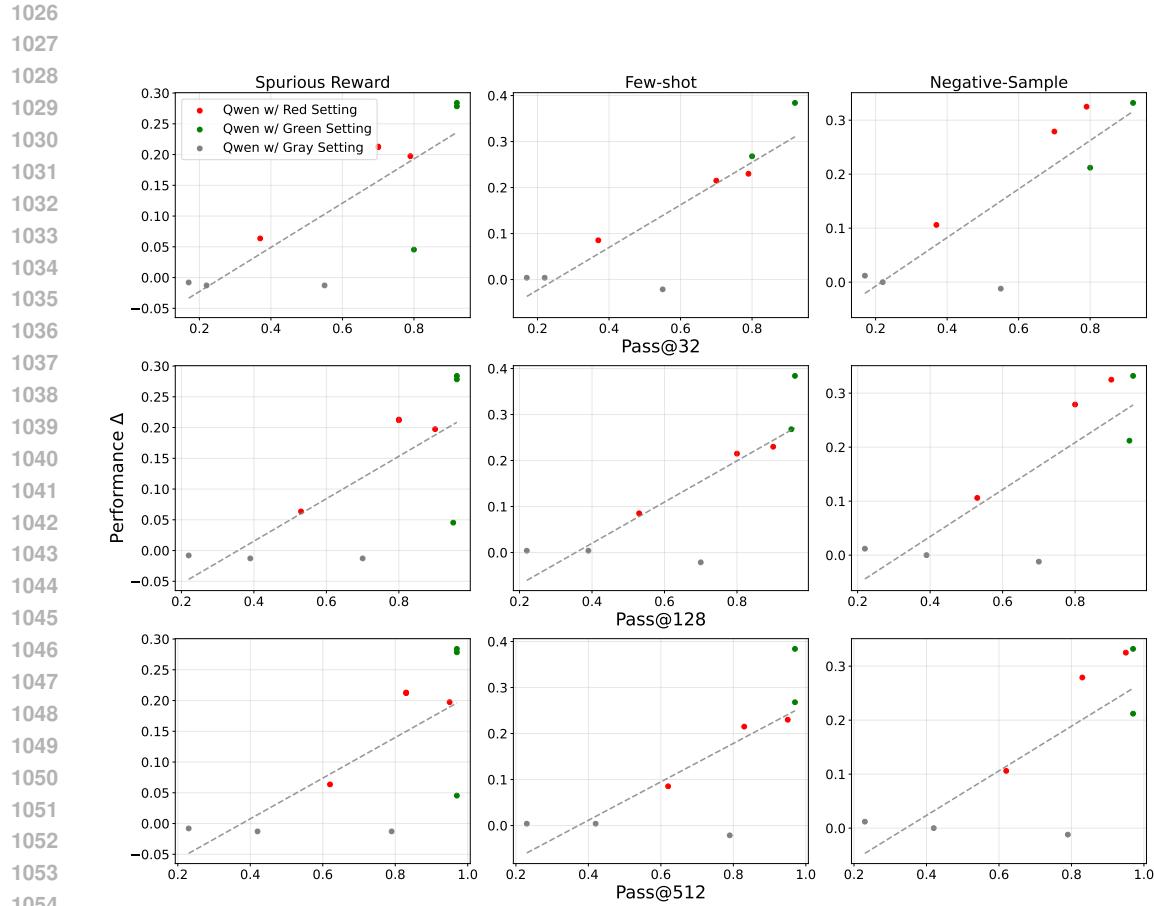


Figure 10: Pass@K versus performance gains across tasks and RL settings.

Details of example $m_{selected}$

How many positive divisors do 9240 and 13860 have in common?

Details of example m_{random}

The angles of quadrilateral $PQRS$ satisfy $\angle P = 3\angle Q = 4\angle R = 6\angle S$. What is the degree measure of $\angle P$?

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Details of example m'_{random}

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Given a finite sequence $S = (a_1, a_2, \dots, a_n)$ of n real numbers, let $A(S)$ be the sequence $\left(\frac{a_1+a_2}{2}, \frac{a_2+a_3}{2}, \dots, \frac{a_{n-1}+a_n}{2}\right)$ of $n-1$ real numbers. Define $A^1(S) = A(S)$ and, for each integer m , $2 \leq m \leq n-1$, define $A^m(S) = A(A^{m-1}(S))$. Suppose $x > 0$, and let $S = (1, x, x^2, \dots, x^{100})$. If $A^{100}(S) = \left(\frac{1}{2^{50}}\right)$, then what is x ? **AND** If $x, 2x+2, 3x+3, \dots$ are in geometric progression, the fourth term is:

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Details of example $l_{selected}$

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Here's a mathematical expression: $?-?+(6\%5)*2-?+?/?/?/4/2 = 2$. The digits on the left side of the equation have been replaced with question marks. Each question mark corresponds to a digit between 0 and 9. You need to try replacing the question marks with the correct digits to restore the expression. Please put the complete expression with the filled - in digits between [[and]] at the end of your response, with no other content, like this: [[2 + 4 * 3 - 4 = 10]]

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Details of example l_{random}

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Solve this cryptarithm: RRYUU + UYR + U = RYUUU (where RRYUU is a 5-digit number, UYR is a 3-digit number, U is a 1-digit number, and RYUUU is a 5-digit number). Each letter represents a unique digit. Find the digit substitution that makes the equation true.

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Details of example l'_{random}

1140 In this Number Wall puzzle, add walls (marked as 'A') to
 1141 divide the grid into islands. Each island must contain
 1142 exactly one number, and its size must equal that number.
 1143

Grid:

```
1144 +---+---+---+
1145 | X | 3 | X |
1146 +---+---+---+
1147 | X | X | X |
1148 +---+---+---+
1149 | X | X | X |
1150 +---+---+---+
```

Rules:

- Each island must contain exactly one number.
- The total number of cells in an island (including the number cell) must equal the value of that number.
- All cells within an island must be connected horizontally or vertically.
- Walls (marked as 'A') cannot form 2×2 or larger continuous rectangles.
- All islands must be separated by walls.

AND

In the cryptarithm: MMII + MIXIMM = MMXIIIX, each letter stands for a different digit (MMII is 4 digits, MIXIMM is 6 digits, and MMXIIIX is 6 digits). Determine what each letter represents to make the equation true.

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Details of example l_{simple}

1176 In this word sorting challenge, you need to rearrange
 1177 words in increasing based on a modified alphabet
 1178 where l, z and a are the first letters. Words to sort:
 1179 yachted, coelomic, harateen. Write your final answer inside:
 1180 \boxed{, like this: \boxed{word1, word2, word3}}.
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1200 **Details of example l_{mid}**

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 1202 You are an expert proficient in Dyck language, where you must
 1203 complete all types of unclosed brackets (e.g., [], , <>) in
 1204 language sequences. You need to analyze the steps of bracket
 1205 pairing according to Dyck language rules. Given an initial
 1206 Dyck language sequence and steps for deriving the closed
 1207 bracket sequence (presented in a thinking process format),
 1208 your task is to identify locations with incorrect reasoning
 1209 in the Dyck language, and there may be multiple errors. This
 1210 could be forgetting to close a bracket, using the wrong
 1211 closing bracket, or incorrectly copying a subsequence of
 1212 closing brackets in the next step. Task: Check the sequence
 1213 to ensure brackets are properly closed. Input: [[(){}]]{}
 1214 Thought 1: We should process the input one by one and track
 1215 the stack configuration.
 1216 Thought 2: Stack: Empty
 1217 Thought 3: [; Stack: Empty
 1218 Thought 4: [; Stack: [[
 1219 Thought 5: (; Stack: [[(
 1220 Thought 6:) ; Stack: [[
 1221 Thought 7: { ; Stack: [[{
 1222 Thought 8: } ; Stack: [[
 1223 Thought 9:] ; Stack: [
 1224 Thought 10:] ; Stack: Empty
 1225 Thought 11: { ; Stack: {
 1226 Thought 12: } ; Stack: Empty
 1227 Thought 13: Now, we have reached the end. The final stack
 1228 is empty.
 1229 Question: Are there any reasoning errors in this sequence?

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