

000 001 002 003 004 005 SMOOTHIE: SMOOTHING DIFFUSION ON TOKEN EM- 006 BEDDINGS FOR TEXT GENERATION 007 008 009

010 **Anonymous authors**
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ABSTRACT

024 Diffusion models have achieved state-of-the-art performance in generating images,
025 audio, and video, but their adaptation to text remains challenging due to its discrete
026 nature. Prior approaches either apply Gaussian diffusion in continuous latent spaces,
027 which inherits semantic structure but struggles with token decoding, or operate
028 in categorical simplex space, which respect discreteness but disregard semantic
029 relation between tokens. In this paper, we propose Smoothie Diffusion on Token
030 Embeddings (SMOOTHIE), a novel diffusion method that combines the strengths of
031 both approaches by progressively smoothing token embeddings based on semantic
032 similarity. This technique enables gradual information removal while maintaining
033 a natural decoding process. Experimental results on several sequence-to-sequence
034 generation tasks demonstrate that SMOOTHIE outperforms existing diffusion-based
035 models in generation quality. Furthermore, ablation studies show that our proposed
036 diffusion space yields better performance than both the standard embedding space
037 and the categorical simplex.
038

1 INTRODUCTION

039 Diffusion models attracted a lot of attention in recent years as they show very high generation quality
040 in image (Rombach et al., 2022; Podell et al., 2023), audio (Evans et al., 2024) and video (Blattmann
041 et al., 2023) domains surpassing all previous approaches such as GANs (Goodfellow et al., 2014) and
042 Normalizing Flows (Rezende & Mohamed, 2015). Diffusion models work by introducing a forward
043 process that gradually degrades an object by injecting Gaussian noise into it, and then learning the
044 reverse process by denoising the object.

045 Applying diffusion models to text is challenging due to its discrete nature. Nevertheless, several works
046 have explored ways to design suitable diffusion processes. One line of research proposes gradually
047 removing information by replacing tokens with others sampled from a categorical distribution (Austin
048 et al., 2021; He et al., 2023; Lou et al., 2024). Another approach applies Gaussian diffusion to the
049 latent space of token embeddings (Li et al., 2022; Gong et al., 2023a). Additionally, some studies
050 leverage the discreteness of text by performing diffusion directly on the vocabulary probability
051 simplex instead of the embedding space (Karimi Mahabadi et al., 2024; Han et al., 2023).

052 Each of the described methods offers distinct advantages and limitations, as summarized in Table 1.
053 Gaussian diffusion progressively removes semantic information: under the Euclidean semantic space
054 hypothesis (Hashimoto et al., 2016), the distinguishability of noisy tokens depends on their initial
055 distances in the latent space. The addition of Gaussian noise gradually disrupts these distances,
056 making the semantics of a latent representation increasingly difficult to recover. However, Gaussian
057 diffusion does not account for the discrete nature of text, which complicates the mapping of generated
058 latent vectors back to discrete tokens (Li et al., 2022; Shabalin et al., 2025).

059 On the other hand, categorical and simplex-based diffusion methods naturally preserve the dis-
060 creteness of text and eliminate the need for an explicit decoding step. Nevertheless, they disregard
061 semantic relationships between tokens during the noising process, resulting in a more erratic and less
062 meaningful degradation of information.

063 In this paper, we propose SMOOTHIE, a smoothing diffusion framework that satisfies both properties.
064 We represent each token with a vector based on distances between token embeddings. During the
065 forward process, our diffusion mechanism gradually perturbs these distances, progressively dissolving

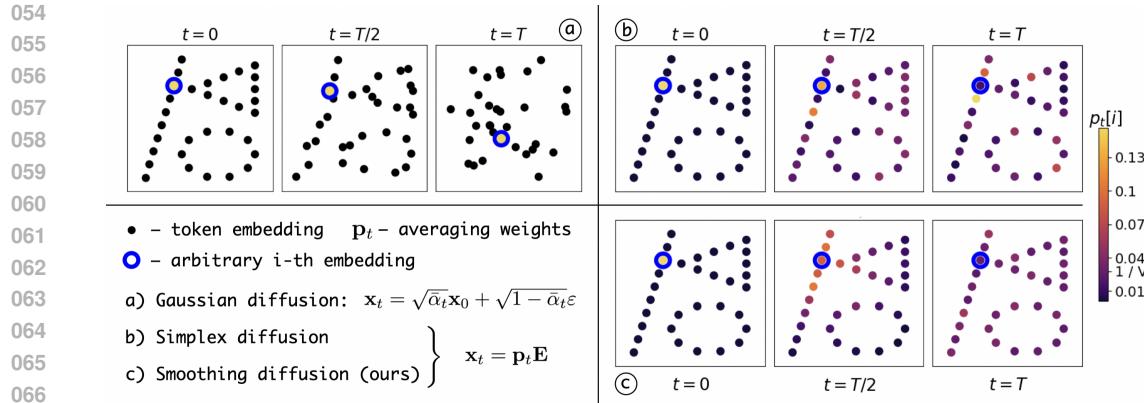


Figure 1: An illustration of the diffusion process for Gaussian, simplex, and smoothing diffusion methods. The key distinction between simplex and smoothing diffusion is that the latter incorporates semantic relationships between tokens during the noise addition process.

Table 1: Comparison of diffusion methods in terms of accounting for text discreteness and semantics.

	Categorical	Gaussian	Simplex	Smoothing (Ours)
Accounting for Discreteness	✓	✗	✓	✓
Accounting for Semantics	✗	✓	✗	✓

semantic information. Like simplex diffusion, our method enables natural decoding from latent representations back to tokens. In theory, SMOOTHIE is applicable not only to text, but to any domain where data comes from a categorical distribution with inherent similarity between categories (e.g. graphs).

We evaluate SMOOTHIE on one unconditional and four sequence-to-sequence generation tasks and show that it outperforms existing diffusion-based approaches. Ablation studies further demonstrate that our method enables effective control over the trade-off between fluency and diversity of the generated text.

The main contributions of our work are as follows:

1. We propose a novel text diffusion framework that simultaneously respects the discrete nature of text and progressively removes semantic information from token representations during the forward process.
2. We show the practical effectiveness of our approach across multiple text generation tasks, providing empirical evidence for the advantages of our diffusion design.

2 PROBLEM STATEMENT AND BACKGROUND

Problem statement In this work, we develop a model for both unconditional and sequence-to-sequence generation tasks. In all cases, the objective is to generate a target sequence $\mathbf{w}^y = w_1^y, \dots, w_m^y$. For sequence-to-sequence generation, the model additionally conditions on a source sequence $\mathbf{w}^x = w_1^x, \dots, w_n^x$. We assume access to parallel datasets, where each source sequence is paired with its corresponding target sequence.

Gaussian diffusion model The diffusion process is defined in terms of a forward (noising) and a reverse (denoising) processes. Given an initial data point sampled from the data distribution, $\mathbf{x}_0 \sim p_{\text{data}}$, the forward process generates a sequence of progressively noisier latent variables $\mathbf{x}_1, \dots, \mathbf{x}_T$. Each step in this sequence is defined by the transition $\mathbf{x}_t \sim q(\mathbf{x}_t \mid \mathbf{x}_{t-1}) = \mathcal{N}(\sqrt{\alpha_t} \mathbf{x}_{t-1}, \sqrt{1 - \alpha_t} \varepsilon)$, where the parameter $\alpha_t \in [0, 1]$ controls the amount of noise injected at timestep t . This formu-

108 lation also supports a direct sampling of \mathbf{x}_t from \mathbf{x}_0 using the marginal distribution $q(\mathbf{x}_t \mid \mathbf{x}_0) =$
 109 $\mathcal{N}(\sqrt{\bar{\alpha}_t} \mathbf{x}_0, \sqrt{1 - \bar{\alpha}_t}, \varepsilon)$, where $\bar{\alpha}_t = \prod_{s=0}^t \alpha_s$ denotes the cumulative product of noise scales.
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111 After the forward process is complete, a neural network f_θ is trained to reverse it by predicting the
 112 original data point \mathbf{x}_0 from the noisy input \mathbf{x}_t . During generation, the model iteratively denoises an
 113 initial sample $\mathbf{x}_T \sim \mathcal{N}(0, I)$, gradually reconstructing the data through the learned reverse process
 114 until it recovers \mathbf{x}_0 .

115 **Embedding diffusion** The most popular continuous text diffusion approaches create a latent space
 116 by mapping tokens to their embeddings (Li et al., 2022; Gong et al., 2023a; Yuan et al., 2022). Then
 117 the Gaussian diffusion process is used to corrupt a latent. The decoding is usually performed by
 118 mapping a generated embedding to the token corresponding to the closest embedding.
 119

120 **Simplex diffusion** SSD-LM (Han et al., 2023) and TESS (Karimi Mahabadi et al., 2024) propose a
 121 simplex diffusion model. They map each token w to a k -logit simplex $\mathbf{s}^w \in \{\pm k\}^V$, where V is the
 122 size of the vocabulary and
 123

$$\mathbf{s}_{(i)}^w = \begin{cases} +k, & i = w \\ -k, & \text{otherwise} \end{cases} \quad (1)$$

124 Then the latent is represented as a sequence $\mathbf{S}_0 = (\mathbf{s}^{w_1^y}, \dots, \mathbf{s}^{w_m^y})$. Corruption is performed with
 125 the Gaussian diffusion process with noise variance multiplied by k^2 ($k = 5$ by default), $\mathbf{S}_t =$
 126 $\sqrt{\bar{\alpha}_t} \mathbf{S}_0 + k\sqrt{1 - \bar{\alpha}_t} \varepsilon$. The model input is calculated by first producing a probability simplex over
 127 vocabulary, $\mathbf{p}_t = \text{softmax}(\mathbf{S}_t)$, and then averaging token embeddings with obtained weights, $\mathbf{p}_t \mathbf{E}$,
 128 where \mathbf{E} is a matrix of token embeddings.
 129

3 RELATED WORK

130 Since the initial attempt to apply diffusion models to text generation (Hoogeboom et al., 2021),
 131 numerous studies have explored ways to better align the diffusion process with the specifics of textual
 132 data. D3PM (Austin et al., 2021) tried exploiting the semantic property of tokens by applying a
 133 discrete diffusion process that replaces tokens with semantically similar alternatives with higher
 134 probability. However, their experiments showed that simple token masking approach produces better
 135 empirical results.
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137 Diffusion-LM (Li et al., 2022) proposed applying Gaussian diffusion in the continuous latent space of
 138 token embeddings, while TECDM (Shabalin et al., 2025) further demonstrated that context-dependent
 139 embeddings provide a more suitable latent space for continuous diffusion. Despite achieving strong
 140 generation quality, the downside of these methods is the requirement of an additional latent decoding
 141 step.
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143 DiffuSeq-v2 (Gong et al., 2023b) attempted to bridge the gap between discrete and continuous
 144 diffusion models by combining masking with Gaussian noise during the noising process. Another
 145 research direction (Han et al., 2023; Karimi Mahabadi et al., 2024) focuses on mapping tokens to
 146 almost-one-hot simplex representations over the vocabulary and introducing Gaussian noise directly
 147 into this space. While this approach does not account for token semantics during noising, it preserves
 148 the discrete structure of text.
 149

150 Our work is inspired by a different line of research developed in the image domain (Rissanen
 151 et al., 2023; Hoogeboom & Salimans, 2023), where semantic information is gradually removed by
 152 smoothing pixel values according to the heat dissipation principle. However, while being effective for
 153 continuous signals such as images, this strategy can not be directly applied to text due to its inherently
 154 discrete nature.
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4 SMOOTHING DIFFUSION

156 In this section, we introduce SMOOTHIE, a smoothing text diffusion model that incorporates both the
 157 discrete nature of text and the semantic relationships between tokens into the diffusion process. We
 158 will first derive the diffusion process for unconditional generation and then extend it to conditional
 159

162 generation. We provide an intuitive illustration of our approach, along with pseudo-code for the
 163 training and sampling procedures, in Fig. 1, Alg. 1, and Alg. 2, respectively.
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165 **4.1 FORWARD DIFFUSION PROCESS**

166 Let V denote the vocabulary size, and let $\mathbf{E} \in \mathbb{R}^{V \times d}$ be a fixed embedding matrix, where each row
 167 corresponds to a d -dimensional token embedding. To construct a latent space suitable for diffusion,
 168 we represent each token w_i^y in a target sequence \mathbf{w}^y with a vector of negative squared Euclidean
 169 distances between an embedding of token w_i^y and embeddings of all tokens in the vocabulary:
 170

$$172 \quad \mathbf{D}_0 = \mathbf{D}_0(\mathbf{E}_{\mathbf{w}^y}) = \left\{ -\frac{\|\mathbf{E}_{w_i^y} - \mathbf{E}_j\|^2}{2} \right\}_{i,j=1}^{m,V} \quad (2)$$

173 Here, $\mathbf{E}_{w_i^y}$ is the embedding of the i -th token in the sequence, and \mathbf{E}_j is the embedding of the j -th
 174 vocabulary token. To generate a trajectory of progressively noisier latents, we define a non-Markovian
 175 forward, or noising process:

$$176 \quad \text{Forward process} \quad q(\mathbf{D}_{1:T} | \mathbf{D}_0) = \prod_{t=1}^T q(\mathbf{D}_t | \mathbf{D}_0) = \prod_{t=1}^T \mathcal{N} \left(\mathbf{D}_t \middle| \frac{1}{\sigma_t^2} \mathbf{D}_0, \delta^2 I \right) \quad (3)$$

177 The noise scheduler σ_t ($1 < \sigma_1 < \dots < \sigma_T$) controls the amount of noise added at each timestep. The
 178 hyperparameter δ controls the stochasticity of the diffusion process and makes it non-deterministic.
 179 Following Rissanen et al. (2023), we keep δ independent of the timestep t .

180 To construct the model input, we convert \mathbf{D}_t into a probability distribution over the vocabulary using
 181 the softmax function: $\mathbf{p}_t = \text{softmax}(\mathbf{D}_t)$. In this formulation, each token is represented by the
 182 weights of Nadaraya-Watson kernel estimator applied over all embeddings in the vocabulary with
 183 Gaussian kernel whose bandwidth is defined by σ_t . The choice of a Gaussian kernel is motivated
 184 by the Euclidean semantic space hypothesis (Hashimoto et al., 2016), which assumes that semantic
 185 similarity correlates with Euclidean proximity in embedding space. As a result, as σ_t increases, the
 186 probability mass—initially centered in a single token—gradually distributes between all other tokens,
 187 starting from the most semantically similar and ending with the most distant ones (see Fig. 1 (c)).

188 Note that our approach can be viewed as a generalization of a simplex-based diffusion (Han et al.,
 189 2023; Karimi Mahabadi et al., 2024). In particular, by replacing our Euclidean distance with trivial
 190 metric, we get the latent space formulation defined in Eq. 1, which ignores the semantic relationships
 191 between tokens. We prove this statement in Appendix C. In Section 5 we show that incorporating
 192 semantic similarity into the diffusion process is crucial for achieving better performance.

201 **4.2 REVERSE DIFFUSION PROCESS**

202 The reverse, or denoising process, starts with a sample from prior distribution $p(\mathbf{D}_T)$ and ends with
 203 the denoised data sample $\tilde{\mathbf{D}}_0$. We define it as a Markov chain with Gaussian distributions:

$$204 \quad \text{Reverse process} \quad p_\theta(\mathbf{D}_{0:T}) = p(\mathbf{D}_T) \prod_{t=1}^T p_\theta(\mathbf{D}_{t-1} | \mathbf{D}_t) = p(\mathbf{D}_T) \prod_{t=1}^T \mathcal{N}(\mathbf{D}_{t-1} | \mu_\theta(\mathbf{p}_t, t), \tilde{\delta}^2 I), \quad (4)$$

205 where θ are trainable model parameters and $\tilde{\delta}^2$ is a noise variance used in the reverse process.
 206 Inspired by Rissanen et al. (2023), we allow noise variance to change between the forward and reverse
 207 processes. That permits us to explicitly control the stochasticity of the generation trajectory, which
 208 significantly affects the model performance (see Section 5.1).

209 Our goal is to find such parameters θ , that minimize the marginal negative likelihood of data samples
 $p_\theta(\mathbf{D}_0) = \int p_\theta(\mathbf{D}_{0:T}) d\mathbf{D}_{1:T}$. We optimize the negative log-likelihood by minimizing its variational

216 upper bound:
 217

$$218 -\log p_\theta(\mathbf{D}_0) = -\log \int \frac{p_\theta(\mathbf{D}_{0:T})q(\mathbf{D}_{1:T}|\mathbf{D}_0)}{q(\mathbf{D}_{1:T}|\mathbf{D}_0)} d\mathbf{D}_{1:T} \leq -\mathbb{E}_q \log \frac{p_\theta(\mathbf{D}_{0:T})}{q(\mathbf{D}_{1:T}|\mathbf{D}_0)} \quad (5)$$

$$221 = -\mathbb{E}_q \left[\log \frac{p_\theta(\mathbf{D}_T)}{q(\mathbf{D}_T|\mathbf{D}_0)} + \sum_{t=2}^T \log \frac{p_\theta(\mathbf{D}_{t-1}|\mathbf{D}_t)}{q(\mathbf{D}_{t-1}|\mathbf{D}_0)} + \log p_\theta(\mathbf{D}_0|\mathbf{D}_1) \right] \quad (6)$$

$$224 = \mathbb{E}_q \left[\underbrace{\text{D}_{\text{KL}}[q(\mathbf{D}_T|\mathbf{D}_0)\|p(\mathbf{D}_T)]}_{L_T} + \sum_{t=2}^T \underbrace{\text{D}_{\text{KL}}[q(\mathbf{D}_{t-1}|\mathbf{D}_0)\|p_\theta(\mathbf{D}_{t-1}|\mathbf{D}_t)]}_{L_{t-1}} - \underbrace{\log p_\theta(\mathbf{D}_0|\mathbf{D}_1)}_{L_0} \right] \quad (7)$$

228 In this formula, L_T is constant during the training, as it does not depend on any learnable parameters.
 229 Both forward and reverse processes are defined by Gaussian distributions, which allows us to compute
 230 the terms L_0 and L_{t-1} in closed form:
 231

$$232 L_0 = \mathbb{E}_q \left[\frac{1}{2\tilde{\delta}^2} \|\mathbf{D}_0 - \mu_\theta(\mathbf{p}_1, 1)\|^2 \right] + C_0; L_{t-1} = \mathbb{E}_q \left[\frac{1}{2\tilde{\delta}^2} \left\| \frac{1}{\sigma_t^2} \mathbf{D}_0 - \mu_\theta(\mathbf{p}_t, t) \right\|^2 \right] + C_{t-1}, \quad (8)$$

237 where C_0 and C_{t-1} are constants that do not depend on parameters θ . This implies that the most
 238 direct parameterization of μ_θ is a model that predicts \mathbf{D}_0/σ_t^2 , corresponding to the posterior mean
 239 of the forward process. However, for practical reasons, we instead parameterize μ_θ as g_θ/σ_t^2 which
 240 ensures that all model outputs are scaled to have the same variance across timesteps.

$$241 L_{t-1} = \mathbb{E}_q \left[\frac{1}{2\tilde{\delta}^2\sigma_t^4} \|\mathbf{D}_0 - g_\theta(\mathbf{p}_t, t)\|^2 \right] + C_{t-1}, \quad (9)$$

244 Following Ho et al. (2020), we replace L_{t-1} with its simplified version by removing the scaling
 245 coefficient $2\tilde{\delta}^2\sigma_t^4$, resulting in the following loss function:
 246

$$247 L_{\mathbf{D}}(\theta) = \mathbb{E}_{\mathbf{w}^y, t, \mathbf{p}_t} [\|\mathbf{D}_0(\mathbf{E}_{\mathbf{w}^y}) - g_\theta(\mathbf{p}_t, t)\|^2] \quad (10)$$

249 However, this loss function is challenging to optimize due to the high variance and dimensionality of
 250 \mathbf{D}_0 . To address this issue, we introduce the following theorem:
 251

252 **Theorem 4.1.** *Let $g^*(\mathbf{p}_t, t)$ be an optimal prediction for Eq. 10. Then $g^*(\mathbf{p}_t, t) = \mathbf{D}_0(f^*(\mathbf{p}_t, t)) + C$,
 253 where C is a constant that does not depend on $f^*(\mathbf{p}_t, t)$ and $f^*(\mathbf{p}_t, t)$ is an optimal prediction for
 254 Eq. 11*

$$255 L_{\mathbf{E}}(\theta) = \mathbb{E}_{\mathbf{w}^y, t, \mathbf{p}_t} [\|\mathbf{E}_{\mathbf{w}^y} - f_\theta(\mathbf{p}_t, t)\|^2] \quad (11)$$

257 We train the model f_θ by minimizing Eq. 11. During the sampling, we initialize from $\mathbf{D}_T \sim$
 258 $\mathcal{N}(0, \tilde{\delta}^2 I)$ and iteratively update it over 200 steps using the following scheme:
 259

$$260 \mathbf{D}_{t-1} = \frac{1}{\sigma_{t-1}^2} \mathbf{D}_0(f_\theta(\mathbf{p}_t, t)) + \tilde{\delta}\varepsilon, \quad (12)$$

263 Note that by Th. 4.1, this procedure is equivalent to updating \mathbf{D}_{t-1} as $\mathbf{D}_{t-1} = g_\theta(\mathbf{p}_t, t)/\sigma_{t-1}^2 + \tilde{\delta}\varepsilon$,
 264 where g_θ is optimized with Eq. 10, because models take $\mathbf{p}_t = \text{softmax}(\mathbf{D}_t)$ as input, which is
 265 invariant to shifts of \mathbf{D}_t . The proof of Th. 4.1 is provided in Appendix D.

267 In contrast, related methods such as SSD-LM (Han et al., 2023) and TESS (Karimi Mahabadi et al.,
 268 2024) employ cross-entropy loss during training. While our method is also compatible with this loss,
 269 in our experiments it led to inferior performance and faster overfitting. Therefore, we chose to rely
 on the MSE objective.

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Algorithm 1 Training

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Input: $\mathbf{w}^x, \mathbf{w}^y, \delta, t \sim \mathcal{U}(1, T), \varepsilon \sim \mathcal{N}(0, I)$
 Compute \mathbf{D}_0 with Eq. 2
 Compute $\mathbf{D}_t = \mathbf{D}_t / \sigma_t^2 + \delta \varepsilon$
 Compute $\mathbf{p}_t = \text{softmax}(\mathbf{D}_t)$
 Minimize $\|\mathbf{E}_{\mathbf{w}^y} - f_\theta(\mathbf{p}_t, t, \mathbf{w}^x)\|^2$

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4.3 NOISE SCHEDULER

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The noise scheduler plays a crucial role in the diffusion process by controlling the rate at which the signal decays over time. Following the observation that text diffusion models benefit from adding more noise at the early stages of the forward process (Shabalin et al., 2025), we define our noise schedule as follows:

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$$\sigma_t = (\sigma_{\max} - \sigma_{\min}) \frac{2}{\pi} \arctan \left(\frac{1}{d} \sqrt{\frac{t}{T-t+\epsilon}} \right) + \sigma_{\min}, \quad \forall t \in [0, T] \quad (13)$$

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Here, σ_{\min} and σ_{\max} sets the minimum and maximum bandwidth respectively, d controls the rate of noise accumulation, and ϵ is a small constant added to prevent division by zero. Throughout our experiments, we use $\sigma_{\min} = 1.5$, $\sigma_{\max} = 200$ and $d \in \{5, 7\}$ to achieve a linear increase in model entropy with increasing t (Dieleman et al., 2022). Also, we set $\delta = 1$ during training. We discuss the noise scheduler ablation in Appendix I.

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4.4 SELF-CONDITIONING

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Following previous works (Dieleman et al., 2022; Shabalin et al., 2025; Karimi Mahabadi et al., 2024), we employ *self-conditioning* (Chen et al., 2023) to our model. During training, with 50% probability the model is fed with self-condition set to zero: $\hat{\mathbf{x}}_0^t = f_\theta(\mathbf{p}_t, \mathbf{0}, t)$. Otherwise the model receives its previous prediction as an input: $\hat{\mathbf{x}}_0^t = f_\theta(\mathbf{p}_t, \text{SG}(\bar{\mathbf{x}}_0^t), t)$, where $\bar{\mathbf{x}}_0^t = f_\theta(\mathbf{p}_t, \mathbf{0}, t)$ and SG is the stop-gradient function that prevent gradients from flowing through $\bar{\mathbf{x}}_0^t$. During the generation stage, the first prediction is made with self-condition set to zero and at all subsequent steps the predictions are performed as $\hat{\mathbf{x}}_0^t = f_\theta(\mathbf{p}_t, \hat{\mathbf{x}}_0^{t+1}, t)$. We demonstrate the impact of self-conditioning in Appendix G.

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4.5 SEQUENCE LENGTH

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Because diffusion models operate over fixed-length sequences, we pad all shorter sequences using a special padding token, which the model is trained to predict. To limit computational overhead, we set the maximum sequence length for each dataset to approximately the 99th percentile of training set sequence lengths. The exact values used for each dataset are provided in the Appendix E.

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5 EXPERIMENTS

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Implementation details In all experiments, we use a pre-trained embedding matrix, \mathbf{E} , from the BERT (Devlin et al., 2019) model¹. We normalize this matrix to have a zero mean and a unit variance and keep it fixed throughout training. Although the model receives the soft token distribution \mathbf{p}_t as input, it does not operate directly on this distribution. Instead, we compute a weighted average of the token embeddings, $\mathbf{p}_t \mathbf{E}$, which yields a lower-dimensional, more tractable representation for the model to process.

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Our model architecture is based on the design proposed in Shabalin et al. (2025), consisting of Transformer decoder layers (Vaswani et al., 2017) augmented with UNet-style skip connections.

¹We discuss the ablation of other embedding types in Appendix H

324 Specifically, the output of the first layer is added to the input of the last, the second to the second-last,
 325 and so on. The full model has 12 layers and approximately 100M parameters. For conditional
 326 generation, we modify the model to accept an input sequence w^x , which is processed by an additional
 327 6-layer Transformer encoder. The encoder output is integrated into the decoder through cross-
 328 attention mechanisms. For timestep conditioning, we adopt the approach from Gong et al. (2023a),
 329 plugging learned timestep embeddings into each Transformer block akin to positional embeddings.
 330 The complete set of hyperparameters used for training and evaluation is provided in Appendix E.

332 5.1 THE IMPORTANCE OF $\tilde{\delta}$

334 Before presenting results on seq-to-seq generation tasks,
 335 we highlight the importance of the hyperparameter $\tilde{\delta}$,
 336 which controls the stochasticity of the denoising process.
 337 To illustrate its impact, we evaluate generation quality on
 338 an *unconditional* generation task using different values of
 339 $\tilde{\delta}$. Specifically, we use the **ROCStories** dataset and assess
 340 performance using three metrics: generative **perplexity**
 341 (to estimate average text quality), **diversity** (to measure
 342 lexical variety) (Su et al., 2022), and the **MAUVE Score**
 343 (Pillutla et al., 2021) (to evaluate the overall similarity of
 344 generated texts to the reference distribution). When cal-
 345 culating MAUVE, we generate 1,000 texts five times with
 346 different seeds and compare them with 1,000 randomly
 347 sampled reference texts. We then average the results.

348 Figure 2 shows the results for a model trained with $\delta = 1$.
 349 We observe that lower values of $\tilde{\delta}$ lead to better perplex-
 350 ity scores but lower diversity. In other words, reduced
 351 stochasticity improves the quality of individual texts but decreases their uniqueness. This trade-off is
 352 actually desirable for sequence-to-sequence tasks, where diversity typically arises naturally from the
 353 varying input conditions. In Appendix F, we justify this insight by grid-searching the best $\tilde{\delta}$ value.
 354 As a result, we set $\tilde{\delta} = 0.1$ for all sequence-to-sequence experiments.

355 In contrast, for unconditional generation, the optimal value of $\tilde{\delta}$ is slightly higher than the one used
 356 during training, as indicated by the MAUVE Score. At this point, the generated texts exhibit sufficient
 357 diversity while maintaining acceptable perplexity. These findings show that $\tilde{\delta}$ has a strong influence
 358 on the generation process and should be tuned carefully depending on the target task.

359 **Datasets** In addition to the unconditional generation on **ROCStories** dataset, we evaluate
 360 SMOOTHIE on four sequence-to-sequence datasets of varying difficulty. For *paraphrase generation*,
 361 we use the Quora Question Pairs (**QQP**) dataset (Chen et al., 2017), which contains 147K
 362 pairs of semantically equivalent questions. For *question generation*, we adopt the **Quasar-T** dataset
 363 (Dhingra et al., 2017), processed by Gong et al. (2023a), resulting in 119K document-question pairs.
 364 For *summarization*, we use the **XSum** dataset (Narayan et al., 2018), comprising 204K BBC articles
 365 and their corresponding summaries. For *detoxification*, we use **ParaDetox** (Logacheva et al., 2022)
 366 dataset with 19,766 pairs of toxic and neutral comments. More detailed information about each
 367 dataset is provided in the Appendix L.

368 **Metrics** Following the evaluation protocol from Gong et al. (2023a); Karimi Mahabadi et al. (2024),
 369 we employ a combination of n-gram-based, diversity and semantic similarity metrics. Specifically,
 370 we report **BLEU** (Papineni et al., 2002) and **ROUGE-1/2/L** (Lin, 2004) scores to measure lexical
 371 overlap between generated and reference texts, and **BERTScore (BS)** (Zhang et al., 2020) to assess
 372 semantic similarity. For BERTScore, we use the `microsoft/deberta-xlarge-mnli` model
 373 to ensure consistency with previous studies (Yuan et al., 2022; Karimi Mahabadi et al., 2024).

374 To evaluate the diversity of generated texts, we compute n-gram diversity (Deshpande et al., 2019),
 375 which reports the fraction of unique unigrams (**Div-1**) and 4-grams (**Div-4**) in a text. Additionally, for
 376 the text detoxification task, we measure **J-Score**, which comprises text fluency, style accuracy, and
 377 content preservation.

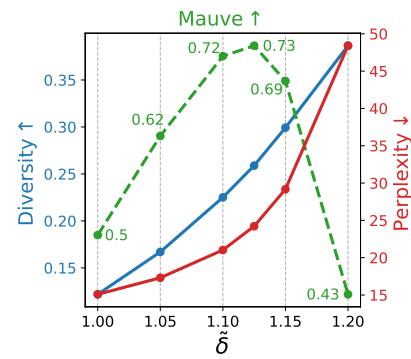


Figure 2: Unconditional generation quality for $\delta = 1$ and varying $\tilde{\delta}$.

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 379 Table 2: Results on XSum (left) and Quasar-T (right) datasets. \dagger denotes autoregressive models,
 380 \triangle denotes the results reproduced with original code, $*$ denotes our implementations. The best-
 381 performing *diffusion* results are highlighted in **bold**, the second-best are underlined.

XSum			Quasar-T				
Method	BS \uparrow	R-1/2/L \uparrow	Method	BS \uparrow	BLEU \uparrow	R-L \uparrow	D-1/4
GPT-2 $\dagger\triangle$	69.0	28.3/8.2/21.8	GPT-2 \dagger	60.5	7.4	27.2	96.0/92.2
Transformer \dagger	—	30.5/10.4/24.2	GPVAE-T5 \dagger	63.1	12.5	33.9	93.8/72.8
FLAN-T5 \dagger	72.7	34.6/12.9/27.2	BART \dagger	66.2	17.4	38.8	98.2/61.7
MDLM \triangle	62.1	27.9/7.7/21.1	MDLM \triangle	60.7	17.5	33.6	91.0/ 64.2
DiffuSeq	46.8	18.9/1.3/13.6	DiffuSeq	59.4	15.8	—	91.1/—
SeqDiffuSeq \triangle	61.8	28.6/6.7/21.3	SeqDiffuSeq	61.4	17.2	—	92.7/—
AR-Diffusion	—	31.7/10.1/24.7	SSD-LM	62.8	14.1	38.5	94.5/56.9
GENIE	—	29.3/8.3/21.9	TESS (random)	60.8	19.0	36.1	96.1 /62.4
Embedding*	<u>68.2</u>	<u>32.1</u> /10.1/24.6	Embedding*	62.0	18.9	35.2	92.4/61.2
Simplex*	63.8	29.6/8.5/23.0	Simplex*	<u>63.0</u>	<u>19.3</u>	<u>36.9</u>	93.0/63.8
SMOOTHIE* (ours)	68.8	33.7 / <u>11.1</u> / 26.0	SMOOTHIE* (ours)	63.1	19.9	36.5	92.8/63.3

394
 395 **Baselines** We compare SMOOTHIE against several diffusion-based and autoregressive baselines, all
 396 with approximately 100M parameters and trained from scratch on each dataset. The diffusion-based
 397 baselines include DiffuSeq (Gong et al., 2023a), SeqDiffuSeq (Yuan et al., 2022), SSD-LM (Han
 398 et al., 2023), TESS (Karimi Mahabadi et al., 2024), AR-Diffusion (Wu et al., 2023), and GENIE (Lin
 399 et al., 2023). We also compare against MDLM (Sahoo et al., 2024), an established masked diffusion
 400 model that we trained for sequence-to-sequence tasks using the provided code. For autoregressive
 401 baselines, we evaluate BART (Lewis et al., 2020), GPT-2 (Radford et al., 2019), GPVAE-T5 (Du
 402 et al., 2022), FLAN-T5 (Chung et al., 2024), and a standard Transformer (Vaswani et al., 2017).
 403 TESS approach uses pre-trained RoBERTa (Liu et al., 2019) to initialize its diffusion model. For a
 404 fair comparison, we only compare to the model trained from random initialization.

405 Additionally, we conduct a rigorous comparison of our proposed distance-based latent space with
 406 two previously explored alternatives: the embedding space (Gong et al., 2023a; Yuan et al., 2022)
 407 (Embedding* in experiments) and the simplex space (Han et al., 2023; Karimi Mahabadi et al., 2024)
 408 (Simplex* in experiments). To ensure a fair evaluation, we train all diffusion models under identical
 409 conditions, keeping the architecture, training hyperparameters, and decoding strategy fixed. The only
 410 variables are the latent space and its associated noise schedule. For embedding-based diffusion, we
 411 use the noise scheduler from Shabalin et al. (2025), while for simplex-based diffusion, we adopt
 412 the scheduler from Han et al. (2023). In all three cases, sampling is performed using a procedure
 413 defined in the respective latent space, following the formulation in Eq. 12. SMOOTHIE and the
 414 embedding-based diffusion model are trained using MSE loss, while the simplex-based diffusion is
 415 trained using cross-entropy loss because it is not suitable for predicting continuous embeddings.

416 5.2 RESULTS

417 We now present a quantitative comparison of SMOOTHIE against a range of generative models.
 418 Wherever possible, we adopt reported results from prior work (Karimi Mahabadi et al., 2024; Lovelace
 419 et al., 2023; Wu et al., 2023; Meshchaninov et al., 2025). When certain metrics are unavailable,
 420 we reproduce the corresponding methods using the original implementations. For consistency, we
 421 re-implement and train the embedding- and simplex-based diffusion baselines within our framework.

422 We show the results on XSum and Quasar-T dataset in Table 2, and on QQP, ParaDetox, and
 423 ROCStories in Table 3. Overall, SMOOTHIE consistently outperforms other text diffusion approaches,
 424 as well as diffusion methods based on embedding- and simplex-based latent spaces, across all tasks,
 425 achieving quality comparable to that of autoregressive models.

426 Notably, embedding-based diffusion yields higher quality than simplex-based diffusion on all datasets
 427 except Quasar-T. This difference can be attributed to the fact that simplex-based diffusion does
 428 not incorporate semantic information into the noising process, making it inherently more chaotic.
 429 Nevertheless, when combined with our proposed architecture, simplex-based diffusion surpasses the
 430 TESS approach, which employs the same diffusion process and a training pipeline, differing only in

432
 433 Table 3: Text generation results on ROCStories, QQP and ParaDetox datasets. \dagger denotes autoregres-
 434 sive models, \triangle denotes the results reproduced with original code, \star denotes our implementa-
 435 tions. The best-performing *diffusion* results are highlighted in **bold**, the second-best are underlined.

Method	ROCStories			QQP			ParaDetox		
	MAUVE \uparrow	PPL \downarrow	Div \uparrow	BS \uparrow	BLEU \uparrow	R-L \uparrow	D-1/4 \uparrow	BLEU \uparrow	J-Score \uparrow
GPT-2 \dagger	78.9	20.5	25.2	82.5	19.8	52.1	98.0/62.5	67.7	60.4
GPVAE-T5 \dagger	—	—	—	84.7	24.1	58.9	96.9/61.7	—	—
BART \dagger	—	—	—	85.7	30.4	61.4	98.8/61.0	—	—
MDLM \triangle	<u>63.9</u>	58.1	35.1	76.3	21.5	46.2	96.2/64.4	61.5	41.4
DiffuSeq	8.6	50.5	12.4	79.5	18.5	—	97.6/—	67.9	47.5
SeqDiffuSeq	10.3	29.3	13.7	82.9	23.3	—	98.1/—	<u>68.8</u>	48.6
AR-Diffusion \triangle	6.6	41.8	10.1	80.1	19.2	54.9	—	64.7	46.5
SSD-LM	—	—	—	83.8	22.9	58.3	98.8/57.3	—	—
Embedding \star	23.4	18.6	13.6	83.4	31.3	59.4	97.7/64.5	67.6	49.1
Simplex \star	15.2	25.3	12.4	80.6	26.8	54.9	96.8/ 64.8	65.1	47.7
SMOOTHIE \star (ours)	73.5	<u>24.2</u>	<u>25.9</u>	83.9	<u>30.8</u>	60.9	98.4/60.5	69.2	51.7

448
 449 the architecture design. This highlights that selecting an appropriate model architecture is as critical
 450 as choosing the diffusion space.

451
 452 The most pronounced improvement in generation quality is observed on the ROCStories dataset.
 453 By tuning the δ parameter (Section 5.1), SMOOTHIE effectively balances diversity and coherence,
 454 achieving the highest MAUVE score and nearly matching the quality of GPT-2. Note that embedding-
 455 based diffusion exhibits lower perplexity, primarily due to reduced diversity—a well-known limitation
 456 of the generative perplexity metric Holtzman et al. (2020).

457 5.3 AMOUNT OF DENOISING STEPS

460 Table 4 presents the relationship between the
 461 number of denoising steps and the generation
 462 quality of SMOOTHIE in terms of J-Score for Pa-
 463 radox and BERTScore for other datasets. We
 464 observe that for all datasets except ParaDetox,
 465 the quality does not change much regardless of
 466 the number of steps. Nevertheless, for XSum the
 467 performance improves as the number of steps
 468 increases until we reach 200 steps, after which
 469 the performance drops. This can be explained
 470 by the impact of self-conditioning, which lead to a mismatch between train and generation trajectory
 471 for larger amount of steps Shabalin et al. (2025). Overall, the results align with the observation
 472 made in the TESS paper (Karimi Mahabadi et al., 2024), which suggests that the optimal number of
 473 denoising steps correlates with the complexity of the task.

474 6 CONCLUSION

477 In this work, we introduce SMOOTHIE, a text diffusion method that constructs its diffusion process
 478 with consideration of the discrete nature of text and the semantic relationships between tokens.
 479 To capture these properties, each token is mapped to a vector of Euclidean distances between its
 480 embedding and the embeddings of all tokens in the vocabulary. Our choice of the Euclidean distance
 481 is based on the Euclidean semantic space hypothesis (Hashimoto et al., 2016), which posits that
 482 semantic similarity correlates with Euclidean proximity in embedding space.

483 Our method also can be applicable to other categorical domains where semantic relationships exist
 484 between categories (e.g. graphs, protein sequences). However, in such cases, a different distance
 485 metric more suited to the domain’s properties may be required. We leave the exploration of this
 486 direction to future work.

457 Table 4: The impact of changing the number of
 458 steps on generation quality. We show J-score for
 459 ParaDetox and BERTScore for the other datasets.

Steps	XSum	Quasar-T	QQP	ParaDetox
25	67.7	63.1	83.9	51.1
50	68.5	63.1	83.8	51.4
100	68.7	63.1	83.7	51.7
200	68.8	63.1	83.6	51.0
500	68.4	63.1	83.5	50.8

486 Empirical results on four sequence-to-sequence tasks demonstrate that SMOOTHIE outperforms
 487 existing text diffusion methods, as well as our diffusion model framework with alternative diffusion
 488 latent spaces that do not rely on additional encoders.
 489

490 REPRODUCIBILITY STATEMENT 491

492 To facilitate reproducibility, we release the source code used to train SMOOTHIE, as well as the
 493 embedding- and simplex-based diffusion models. A complete set of hyperparameter configurations is
 494 provided in Appendix E. All experiments are conducted exclusively on publicly available datasets,
 495 whose details are described in Appendix L.
 496

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732 A LIMITATIONS

733 734 **Pre-trained Embeddings** Our proposed method relies on a pre-trained embedding matrix \mathbf{E} from
 735 the BERT model. While this choice simplifies the training process and improves its stability, it limits
 736 the model’s scalability and may cap its generation quality, because finetuning embeddings for a
 737 specific task should offer better results. An end-to-end training approach, as used in Li et al. (2022);
 738 Gong et al. (2023a); Karimi Mahabadi et al. (2024), could be applied to our method as well. We leave
 739 the exploration of this approach for future work.

740 741 **Fixed Sequence Length** As with most text diffusion models, our method operates with a fixed
 742 sequence length. Variable-length outputs are emulated by discarding tokens past the end-of-sequence
 743 (EOS) token. This strategy introduces inefficiencies during training and generation, as the model
 744 must predict padding tokens regardless of actual sequence length. To the best of our knowledge,
 745 dynamically varying sequence lengths during the denoising stage remains an underexplored area.
 746 SeqDiffuSeq (Yuan et al., 2022) addresses this by truncating sequences early, based on the observation
 747 that the EOS token position often stabilizes early in denoising. However, this is an ad hoc solution,
 748 and more advanced approaches need to be developed.

749 B SOCIETAL IMPACT

750 751 Language models have been shown to produce harmful outputs (Weidinger et al., 2022), spread
 752 disinformation (Shao et al., 2018), hallucinate (Huang et al., 2025), and potentially violate user
 753 privacy (Carlini et al., 2021). Although our study focuses on tasks that differ from those typically
 754 used in prior harmfulness evaluations, future scaling of our approach could lead to similar negative
 755 outcomes. Research on methods for mitigating model harmfulness is actively developing, and we

believe that insights from this work may also inform improvements in the reliability and safety of text diffusion models.

C RELATIONSHIP BETWEEN DISTANCE-BASED AND SIMPLEX-BASED LATENT SPACES

In this section, we demonstrate that our proposed *distance-based latent space* generalizes the *simplex-based latent space*. Specifically, we show that the simplex-based latent space corresponds to a special case of a distance-based latent space when equipped with a trivial metric.

SMOOTHIE maps each token w to a latent vector \mathbf{d}^w , where each component is given by:

$$\mathbf{d}_{(i)}^w = -\frac{1}{2} \|\mathbf{E}_w - \mathbf{E}_i\|^2. \quad (14)$$

For other categorical domains, the Euclidean distance can be replaced with a more suitable metric $\rho(w, i)$, leading to:

$$\mathbf{d}_{(i)}^w = -\rho(w, i). \quad (15)$$

To relate this to simplex-based representations, consider the case where ρ is the *trivial metric*:

$$\rho(w, i) = [w \neq i], \quad (16)$$

i.e., 0 when $w = i$ and 1 otherwise. Under this choice, the latent vector becomes:

$$\mathbf{d}_{(i)}^w = \begin{cases} 0, & i = w, \\ -1, & \text{otherwise.} \end{cases} \quad (17)$$

In comparison, the simplex-based latent space maps each token w to a vector \mathbf{s}^w in the k -logit simplex:

$$\mathbf{s}_{(i)}^w = \begin{cases} +k, & i = w, \\ -k, & \text{otherwise.} \end{cases} \quad (18)$$

Both SMOOTHIE and simplex diffusion apply a Gaussian diffusion process to corrupt the latent vector:

$$\mathbf{z}_t = \phi_t \mathbf{z}_0 + \gamma_t \varepsilon, \quad (19)$$

where $\mathbf{z}_0 \in \{\mathbf{d}^w, \mathbf{s}^w\}$ and $\varepsilon \sim \mathcal{N}(0, I)$. To form a model input, the corrupted vector is then transformed into a probability distribution using the softmax function:

$$p_t = \text{softmax}(\mathbf{z}_t). \quad (20)$$

Since the softmax function is invariant to uniform additive shifts, we have:

$$\text{softmax}(\phi_t \mathbf{s}^w + \gamma_t \varepsilon) = \text{softmax}(\phi_t (\mathbf{s}^w - k) + \gamma_t \varepsilon) = \text{softmax}(2k\phi_t \mathbf{d}^w + \gamma_t \varepsilon), \quad (21)$$

where the final equality follows from observing that $\mathbf{s}^w - k = 2k\mathbf{d}^w$.

This confirms that the simplex-based latent space is equivalent, up to scaling, to the distance-based latent space under the trivial metric. Hence, the simplex-based representation is a special case within the more general distance-based latent space framework.

D PROOF OF THEOREM 4.1

Proof. We begin by recalling a standard result:

Lemma. The minimum value of the function $\mathbb{E}_{\mathbf{y}} [\|\mathbf{y} - \mathbf{z}\|^2]$ is achieved when $\mathbf{z} = \mathbb{E}[\mathbf{y}]$.

810 Using this lemma, we obtain:
 811

$$812 \quad g^*(\mathbf{p}_t, t) = \mathbb{E}_{\mathbf{w}^y} [\mathbf{D}_0(\mathbf{E}_{\mathbf{w}^y})] = \mathbb{E}_{\mathbf{w}^y} \left[-\frac{1}{2} \left\{ \|\mathbf{E}_{w_i^y} - \mathbf{E}_j\|^2 \right\}_{i,j=1}^{m,V} \right] \quad \text{and} \quad f^*(\mathbf{p}_t, t) = \mathbb{E}_{\mathbf{w}^y} [\mathbf{E}_{\mathbf{w}^y}], \\ 813 \quad 814 \quad (22)$$

815 where $\mathbf{w}^y \sim p(\mathbf{w}^y \mid \mathbf{p}_t)$. Since both $g^*(\mathbf{p}_t, t)$ and $f^*(\mathbf{p}_t, t)$ are matrices, without loss of generality
 816 we will prove this statement for an arbitrary row i and column j . For brevity, we will define $u = \mathbf{E}_{w_i^y}$
 817 and $v = \mathbf{E}_j$. Then, we need to show that
 818

$$820 \quad \mathbb{E}_u \left[-\frac{1}{2} \|u - v\|^2 \right] = -\frac{1}{2} \|\mathbb{E}[u] - v\|^2 + C \quad (23) \\ 821 \\ 822$$

823 Expanding both sides:
 824

$$825 \quad \mathbb{E}_u [\|u - v\|^2] = \mathbb{E}[\|u\|^2] - 2v^\top \mathbb{E}[u] + \|v\|^2 \\ 826 \quad \|\mathbb{E}[u] - v\|^2 = \|\mathbb{E}[u]\|^2 - 2v^\top \mathbb{E}[u] + \|v\|^2$$

827 Subtracting:
 828

$$829 \quad \mathbb{E}[\|u\|^2] - \|\mathbb{E}[u]\|^2 = \sum_{k=1}^d \text{Var}(u_k) =: C \\ 830 \\ 831$$

832 Thus,
 833

$$834 \quad \mathbb{E}_u \left[-\frac{1}{2} \|u - v\|^2 \right] = -\frac{1}{2} \|\mathbb{E}[u] - v\|^2 + \underbrace{-\frac{1}{2} C}_{\text{constant}}$$

835 where C is a constant independent of $\mathbb{E}[u]$.
 836

837 Since this holds for all (i, j) , the matrix identity holds:
 838

$$839 \quad g^*(\mathbf{p}_t, t) = \mathbf{D}_0(f^*(\mathbf{p}_t, t)) + \mathbf{C} \\ 840 \\ 841$$

□

843 E IMPLEMENTATION DETAILS

844 The hyperparameters for training and inference of the models across all datasets are presented in
 845 Table 5. We trained our models using two 80 GB NVIDIA A100 GPUs for 15 hours on average. For
 846 all the tasks, we save checkpoints every 25,000 steps. We select the best checkpoint by the quality on
 847 the development set. During generation we do not apply the clamping trick (Li et al., 2022), since
 848 it does not improve quality in our experiments. We do not use the classifier-free guidance (Ho &
 849 Salimans, 2021) for the same reason.
 850

851 F AN IMPACT OF $\tilde{\delta}$ ON SEQ2SEQ TASKS

852 In this section, we measure how the quality of
 853 sequence-to-sequence generation changes when the
 854 value of $\tilde{\delta}$ varies. For this experiment, we consider
 855 values in the range of $\tilde{\delta} \in \{0.1, 0.25, 0.5, 0.75, 1\}$
 856 and set the number of generation steps to 100. Table
 857 6 reports J-Score for ParaDetox and BERTScore for
 858 all other datasets. Although the difference in quality
 859 for different $\tilde{\delta}$ is not as significant as for the uncon-
 860 ditional generation, it can be seen that lower values
 861 of $\tilde{\delta}$ produce better quality overall. Following these
 862 results, we set $\tilde{\delta} = 0.1$ for all datasets.
 863

864 Table 6: The impact of $\tilde{\delta}$ value on generation
 865 quality. We show J-Score for ParaDetox and
 866 BERTScore for the other datasets.

$\tilde{\delta}$	XSum	Quasar-T	QQP	ParaDetox
0.1	68.8	63.1	83.7	51.7
0.25	68.7	63.1	83.7	51.4
0.5	68.7	63.1	83.7	51.3
0.75	68.6	63.1	83.6	50.9
1	68.2	63.1	83.4	50.9

Table 5: Complete hyperparameter configurations for all datasets.

Hyperparameter	ROCStories	XSum	Quasar-T	QQP	ParaDetox
Tokenizer		bert-base-cased			
Transformer Layers		12			
Transformer Dim		768			
Self-Attention Heads		12			
Optimizer		AdamW			
Learning Rate		$2 \cdot 10^{-4}$			
β_1, β_2		0.9, 0.98			
Warmup steps		5000			
LR scheduler		Constant			
Weight decay		0.01			
Gradient clipping		1			
EMA decay		0.9999			
Batch size	256	256	512	256	256
Training steps	1M	225k	150k	50k	150k
Max input length	—	512	100	50	40
Max target length	80	64	50	50	40
Generation steps	350	200	100	25	100
d	5	5	7	5	7
$\delta, \sigma_{\min}, \sigma_{\max}$		1, 1.5, 200			
$\tilde{\delta}$	1.125	0.1	0.1	0.1	0.1

Table 7: Impact of self-conditioning on the generation performance on XSum, Quasar-T and QQP datasets.

Method	XSum		Quasar-T			QQP		
	BS \uparrow	R-L \uparrow	BS \uparrow	BLEU \uparrow	R-L \uparrow	BS \uparrow	BLEU \uparrow	R-L \uparrow
Embedding	68.2	24.6	62.0	18.9	35.2	83.5	31.6	59.6
w/o SC	65.2	23.6	62.9	19.5	36.0	81.7	27.7	57.4
Simplex	63.8	23.0	63.0	19.3	36.9	81.2	27.3	55.0
w/o SC	61.2	21.5	62.5	19.4	36.4	80.0	25.9	54.1
SMOOTHIE	68.8	26.0	63.0	19.0	35.8	83.9	30.8	60.9
w/o SC	67.5	25.4	61.9	19.0	35.7	83.2	29.4	59.9

G SELF-CONDITIONING

Previous studies have shown that self-conditioning significantly improves the quality of text diffusion models (Yuan et al., 2022; Shabalin et al., 2025; Karimi Mahabadi et al., 2024; Dieleman et al., 2022). In this section, we compare the performance of SMOOTHIE, as well as of embedding- and simplex-based diffusion models, with and without self-conditioning. The results on the XSum, Quasar-T, and QQP datasets are reported in Table 7. Although performance gains vary across models and datasets, self-conditioning generally improves quality, which confirms the previous observations.

H EMBEDDINGS ABLATION

Throughout this work, we utilize BERT embedding matrix to represent text tokens without additional comments. We find it important to evaluate the robustness of SMOOTHIE to other choices of embeddings. Therefore, we demonstrate how model performance changes on the ROCStories dataset when embeddings are changed. We choose two alternatives with the same hidden size: GPT-2 (Radford et al., 2019) embeddings with the vocabulary size of 50k

Table 8: The generation quality of SMOOTHIE trained with different embedding types on ROCStories dataset.

Embeddings	MAUVE \uparrow	PPL \downarrow	Div \uparrow
BERT (default)	73.5	24.2	25.9
GPT-2	64.4	23.1	25.0
GloVe	36.8	36.4	24.6

918 and GloVe (Pennington et al., 2014) embeddings trained manually on Wikipedia dataset for BPE
 919 tokens with the vocabulary size of 10k. In the Table 8 we show the results of the ablation.
 920

921 In terms of perplexity and diversity, GPT-2 embeddings perform similarly to BERT, with the exception
 922 of MAUVE. However, these results are still better than of other methods (see Table 3). Interestingly,
 923 we found out that the optimal value of $\tilde{\delta}$ for GPT2 embeddings is lower than for BERT embeddings
 924 (1.03 vs 1.125). Most probably, this is because diversity increases naturally with the increase of the
 925 vocabulary size and the need to increase it artificially disappears. GloVe embeddings are worse than
 926 the ones extracted from a language model. Therefore, a significant drop in quality is not surprising.
 927 We can conclude that embeddings is an important component of the framework and the quality of the
 928 model does depend on the quality of embeddings. However, the method allows freedom in the choice
 929 of embeddings, which should help in applicability.
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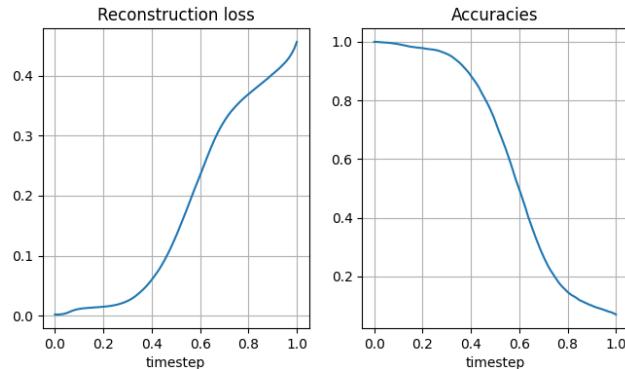
I NOISE SCHEDULER ABLATION

931 In this work, we use a special *arctan* noise scheduler
 932 for SMOOTHIE to make sure that the model entropy
 933 grows linearly with t (Dieleman et al., 2022). In this
 934 section, we perform an ablation study for the pro-
 935 posed noise scheduler by evaluating different values
 936 of d . In Table 9, we show the numerical performance
 937 on the ROCStories dataset. For each d we chose the
 938 best $\tilde{\delta}$ based on MAUVE. Smaller d values corre-
 939 spond to more aggressive corruption. The results sug-
 940 gest that while the difference is marginal, SMOOTHIE
 941 is sensitive to the choice of the noise scheduler.
 942

943 Figure 3 illustrates how the reconstruction loss and the accuracy of the predicted tokens depend
 944 on the timestep t for our noise scheduler. In other words, we evaluate how closely the prediction
 945 $\hat{x}_0 = f_\theta(p_t, 0, t)$ matches the original x_0 . Accuracy is calculated only for non-padding tokens.
 946

Table 9: An impact of the parameter d in
 947 noise scheduler on the generation quality on
 948 the ROCStories dataset.

	MAUVE \uparrow	PPL \downarrow	Div \uparrow
$d = 4$	66.2	24.4	24.5
$d = 5$	73.5	24.2	25.9
$d = 6$	66.5	26.7	27.7
$d = 7$	64.9	24.6	26.7



947 Figure 3: Reconstruction loss (left) and reconstruction accuracy (right) w.r.t. timestep for SMOOTHIE,
 948 trained with *arctan* noise scheduler with $d = 5$.
 949

J COMPUTATIONAL COMPLEXITY

950 In Table 10, we show the empirical comparison of runtime and GPU memory consumption for
 951 Smoothie, simplex- and embedding-based diffusions. We report the training time in hours for one
 952 million iterations on the ROCStories dataset. For generation, we perform 100 steps with a batch
 953 size of 32 and a sequence length of 80 and report the total generation time and the peak memory
 954 consumption.
 955

956 We observe that our approach is slower than embedding-based diffusion, because we must compute
 957 pair-wise distances between sequence embeddings and vocabulary embedding on each iteration,
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Table 10: The comparison of methods in terms of computational complexity.

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Method	Train time (h)	Generation time (s)	Memory (MB)
Embedding	37.89	1.642	593.3
Simplex	51.91	2.897	678.4
SMOOTHIE	49.71	2.897	593.3

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which have a complexity of $\mathcal{O}(\text{batch size} \times \text{seq len} \times d \times V)$. The generation is about $1.75 \times$ slower, while training is $1.3 \times$ slower. The difference in training speed is smaller because both methods involve gradient computation and parameter update with the same complexity. Simplex diffusion has approximately the same speed because it predicts tokens on each step instead of embeddings, which requires an application of a linear head with complexity $\mathcal{O}(\text{batch size} \times \text{seq len} \times d \times V)$ (same as SMOOTHIE). In terms of memory consumption all methods are the same, except simplex diffusion adds memory for storing the linear head. We also would like to note that several diffusion methods have the same exact complexity, because some of them utilize clamping trick (Li et al., 2022) and some predict tokens instead on embeddings, which requires an application of a large linear head (Han et al., 2023; Karimi Mahabadi et al., 2024; Dieleman et al., 2022).

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K TRAINING DYNAMICS

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In this section, we examine the differences in the training dynamics of SMOOTHIE, embedding and simplex diffusions. Figure 4 shows how training loss and Mauve change with respect to training time. For the embedding diffusion, we perform 1.75 times more generation steps (175 vs. 100) than for the other diffusion types, in order to match the generation time. The results suggest that, although SMOOTHIE trains and generates more slowly, it converges more quickly and produces higher-quality results than models trained for the same amount of time. We do not report loss for simplex diffusion, as it is trained with the cross-entropy loss, while other diffusions utilize MSE.

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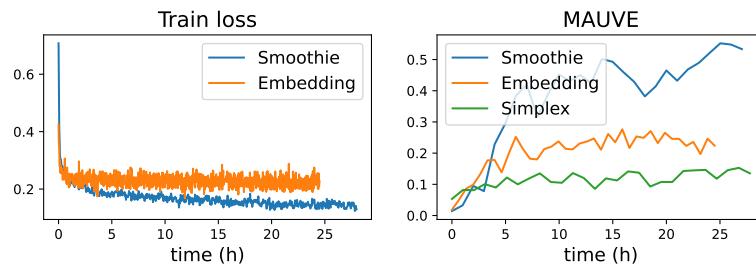


Figure 4: Training dynamics of SMOOTHIE, embedding and simplex diffusions on the ROCStories dataset.

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L DATASET STATISTICS

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ROCStories The ROCStories dataset (Mostafazadeh et al., 2016) contains 98,161 five-sentence commonsense fictional stories that capture causal and temporal relations between everyday events. It is a widely used small-scale benchmark for unconditional text generation. The dataset is split into 93,161 training instances, 4,000 validation instances, and 1,000 test instances. Url: <https://cs.rochester.edu/nlp/rocstories/>

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XSum The XSum dataset (Narayan et al., 2018) is used for extreme summarization of BBC news articles. Each article covers a diverse range of topics (e.g., sports, politics) and is paired with a single-sentence summary. The dataset is divided into 204,045 training, 11,332 validation, and 11,334 test instances. Url: <https://huggingface.co/datasets/EdinburghNLP/xsum>

1026 **Quasar-T** Quasar-T (Dhingra et al., 2017) is a large-scale dataset for the question generation
1027 task. It requires models to comprehend natural language queries and extract answers from a large
1028 corpus. The dataset consists of open-domain trivia questions and their corresponding answers,
1029 collected from various internet sources. We use the version preprocessed by Gong et al. (2023a),
1030 which includes 116,953 training instances, 2,048 validation instances, and 10,000 test instances. Url:
1031 <https://github.com/Shark-NLP/DiffuSeq/tree/main>

1032
1033 **QQP** The Quora Question Pairs (QQP) dataset (Chen et al., 2017) consists of over 400,000 question
1034 pairs from the Quora platform, each annotated with a binary label indicating whether the two questions
1035 are paraphrases. For the paraphrase generation task, we use the subset containing 149,263 positively
1036 labeled pairs, split into 119,410 training instances, 14,926 validation instances, and 14,927 test
1037 instances. Url: <https://huggingface.co/datasets/nyu-mll/glue/viewer/qqp>

1038 **ParaDetox** We use ParaDetox dataset (Logacheva et al., 2022) for small-scale conditional genera-
1039 tion. It comprises 19,766 pairs of toxic and neutral comments and is intended for the text detoxification
1040 task. Url: <https://huggingface.co/datasets/s-nlp/paradetox>

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