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# Wavelet Scattering Transform and Fourier Representation for Offline Detection of Malicious Clients in Federated Learning

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## Abstract

1 Federated Learning (FL) enables the training of machine learning models across de-  
2 centralized clients while preserving data privacy. However, the presence of anomalous  
3 or corrupted clients—such as those with faulty sensors or non-representative  
4 data distributions—can significantly degrade model performance. Detecting such  
5 clients without accessing raw data remains a key challenge. We propose **Waffle**  
6 (**W**avelet and **F**ourier representations for **F**ederated **L**earning) a detection algorithm  
7 that labels malicious clients *before training*, using locally computed compressed  
8 representations derived from either the Wavelet Scattering Transform (WST) or  
9 the Fourier Transform. Both approaches provide low-dimensional, task-agnostic  
10 embeddings suitable for unsupervised client separation. A lightweight detector,  
11 trained on a distilled public dataset, performs the labeling with minimal com-  
12 munication and computational overhead. While both transforms enable effective  
13 detection, WST offers theoretical advantages, such as non-invertibility and stability  
14 to local deformations, that make it particularly well-suited to federated scenarios.  
15 Experiments on benchmark datasets show that our method improves detection accu-  
16 racy and downstream classification performance compared to existing FL anomaly  
17 detection algorithms, validating its effectiveness as a pre-training alternative to  
18 online detection strategies.

19 

## 1 Introduction

20 Federated Learning (FL) is a distributed learning framework that enables multiple clients to train  
21 a global model without sharing raw data [1], making it a promising approach for privacy-sensitive  
22 decentralized domains [2, 3, 4]. As deployments scale, a central challenge is data heterogeneity,  
23 where non-IID client data can hinder model convergence and degrade performance [5, 6].  
24 Beyond natural data heterogeneity, FL systems are also vulnerable to malicious or faulty clients  
25 [7, 8]. Consider a scenario in a large-scale sensor network FL deployment (e.g., environmental  
26 monitoring [9] or industrial IoT [10]). Some sensors might be physically damaged, miscalibrated,  
27 or even deliberately tampered with, causing them to report highly perturbed, noisy, or statistically  
28 anomalous data streams. Being able to quickly detect them and remove them for training or fixing  
29 them without accessing raw data is beneficial for monitoring the network, and guaranteeing its correct  
30 functioning [11]. Defenses against malicious clients in FL often rely on robust aggregation methods  
31 [12, 7] to reduce the influence of outlier updates, particularly in the presence of Byzantine attacks  
32 [13]. However, these methods assume most clients are benign and target model-level anomalies,  
33 not data-level perturbations that subtly alter local objectives [14, 15]. Online detectors that monitor  
34 client behavior during training offer an alternative but add overhead and may act too late. Crucially,  
35 neither class of defenses is well-suited to detecting clients with malicious data prior to training, as in

36 compromised sensor networks.  
 37 In this work, we propose **Waffle** (Wavelet and Fourier representations for Federated Learning), an  
 38 offline detector designed to identify clients with malicious data before FL training begins. Performing  
 39 detection offline [16] and in a privacy-preserving manner is particularly desirable, as it limits  
 40 computational overhead on both the server and client sides, making the approach lightweight and  
 41 scalable. **Waffle** trains a classifier on spectral features – extracted via Fourier Transform (FT) and  
 42 Wavelet Scattering Transform (WST) [17] – which offer stable, invariant representations robust to  
 43 data perturbations. Detection is performed using a model pre-trained on a distilled public dataset,  
 44 ensuring efficiency and privacy. Clients locally compute low-dimensional statistics via Principal  
 45 Component Analysis (PCA) and spectral embeddings, sending an aggregated, secure, and non-  
 46 invertible information to the server which classifies them as benign or malicious. Malicious clients  
 47 are excluded prior to training. Unlike many existing methods, **Waffle** does not assume a benign  
 48 majority and can be combined with robust aggregation to strengthen FL security.  
 49 The structure of the paper is the following: Section 2 defines the FL setting, the data attacks considered,  
 50 and the spectral representations (FT and WST). Section 3 details **Waffle**’s training and detection.  
 51 Theoretical guarantees are provided in Section 4 showing the benefits of removing malicious clients.  
 52 Section 5 reports experimental results validating **Waffle** on benchmark datasets.

53 **Related Works and Contributions.**

54 **Malicious Client Detection in FL.** Detection-based approaches classify clients as benign or malicious  
 55 based on anomalies in their updates or data distribution [4]. **FLDetector** [18] identifies malicious  
 56 clients by analyzing the consistency of their updates over time—benign updates follow predictable  
 57 patterns, while malicious ones are erratic. **MuDHog** [19] leverages historical update trajectories with  
 58 model-agnostic meta-learning to detect temporal inconsistencies, though it assumes long-term client  
 59 participation, which is unrealistic in cross-device settings. **VAE** [20] uses a variational autoencoder  
 60 to model the benign update distribution and flags deviations, assuming malicious clients are rare  
 61 and the VAE is well-trained. These methods rely on multi-round update access, limiting early-stage  
 62 applicability, and focus on gradients or parameters, making them vulnerable to indirect attacks.

63 **Robust Aggregation in FL.** Robust aggregation methods aim to mitigate the influence of malicious  
 64 clients without explicitly identifying them [21, 7]. **KRUM** [12] selects the most central update in  $\ell_2$   
 65 distance, but requires fewer than half of the clients to be malicious. **TrimmedMean** [7] discards  
 66 extreme values per coordinate, improving robustness to outliers, though it overlooks dependencies  
 67 across dimensions. **FLTrust** [8] uses a trusted server-side dataset to normalize and rescale client  
 68 updates, enhancing robustness but breaking strict decentralization. Secure aggregation protocols  
 69 like **RFLPA** [22] and **RoFL** [23] ensure client privacy via cryptographic techniques, but do not address  
 70 adversarial robustness. These approaches, unlike detection-based ones, do not label clients, limiting  
 71 their use when malicious participants must be explicitly excluded.

72 **Spectral Analysis and Frequency-based Defenses.** Spectral methods aim to identify or mitigate  
 73 malicious behavior by analyzing updates in the frequency domain [24, 25, 26]. **FreqFeD** [27] applies  
 74 the Discrete Fourier Transform to client updates, filtering high-frequency components assumed to  
 75 contain adversarial noise, though this may remove relevant information under data heterogeneity.  
 76 **FedSSP** [28] targets backdoor attacks by smoothing and pruning suspicious spectral patterns in model  
 77 weights, but depends on specific architectures and requires access to full model parameters. Unlike  
 78 these methods, our approach extracts frequency-based embeddings directly from client-side data  
 79 before training, enabling model-agnostic detection.

80 Our *main contributions* are summarized as follows:

- 81 • We propose **Waffle**, a novel offline detector for identifying clients with data attacks, introducing  
 82 the use of WST for anomaly detection in FL.
- 83 • We provide a theoretical framework motivating WST and FT as robust data representations, and  
 84 mathematically demonstrate that removing malicious clients improves global model estimation.
- 85 • We present experiments on benchmark datasets showing that **Waffle** significantly improves model  
 86 performance and robustness compared to training with contaminated data or using only robust  
 87 aggregation.



Figure 1: Examples of attacked data. Two images downloaded from [link1](#) and [link2](#). For each image: *left*: clean client, *center*: noisy attack with magnitude  $\sigma = 0.2$ , *right*: blur attack with spread  $\beta = 11$

## 88 2 Theoretical Framework

89 In this section, we introduce the mathematical framework that provides the foundation for our  
90 algorithm. Section 2.1 presents the Federated Learning (FL) setting and defines the class of attacks  
91 considered on clients’ data. Section 2.2 introduces the WST and the Fourier Transform FT, recalling  
92 their basic properties that are relevant for anomaly detection.

### 93 2.1 Problem Formulation

94 Consider a standard FL scenario 1 with  $K \in \mathbb{N}$  clients and a central server. Each client  $k$  possesses  
95  $n_k$  data samples  $(x_k^i, y_k^i)_{i=1}^{n_k} \sim \mathcal{D}_k$  supported in  $\mathcal{X} \times \mathcal{Y}$ . The objective of FL is to learn a shared  
96 global model  $\theta$  that generalizes across all clients, by solving the following optimization problem:

$$\theta^* \in \arg \min_{\theta \in \Theta} \frac{1}{N} \sum_{k=1}^K n_k \mathcal{L}_k(\theta) \quad (1)$$

97 where  $\Theta$  denotes the model’s parameter space,  $N = \sum_{k=1}^K n_k$  is the total number of data samples,  
98 and  $\mathcal{L}_k$  represents the empirical loss function for client  $k$  with respect to its local data distribution  
99  $\mathcal{D}_k$ . In each communication round  $t \in \{1, \dots, T\}$ , a subset of clients  $\mathcal{P}_t$  is randomly selected to  
100 participate in training. Each participating client  $k \in \mathcal{P}_t$  performs  $S \in \mathbb{N}$  local iterations of a stochastic  
101 optimizer. Subsequently, clients send their updated parameters to the server, which aggregates these  
102 updates to derive a new global model.

103 A critical challenge in realistic FL deployments is the *non-i.i.d.* nature of client data, which can  
104 hinder the convergence and performance of the global model. In this work, we specifically address  
105 non-i.i.d. settings where the data distribution discrepancies are caused by malicious clients perturbing  
106 their original data samples. This differs from typical attack detection scenarios focusing on model  
107 poisoning during training.

108 **Type of Attacks** We define two types of feature-level attacks that our algorithms aim to address:  
109 noisy and blur attackers. Examples of the effect of these attacks are displayed in Figure 1. This  
110 focus is motivated by the fact that noise and blur are common consequences of real-world faults  
111 [29, 30] –such as sensor degradation, miscalibration, or environmental interference – that can subtly  
112 compromise data quality and model performance without exhibiting overtly malicious behavior.

113 **Definition 1.** Let  $k \in [K]$  and  $\sigma_k > 0$ . Client  $k$  is a **noisy attacker** if its data samples are perturbed  
114 as  $\tilde{x}_k^i = x_k^i + \sigma_k \epsilon_k^i$ , where  $x_k^i$  is the clean sample, and,  $(\epsilon_k^i)_{i=1}^{n_k}$  is a family of independent Wiener  
115 processes supported in  $\mathcal{X}$ .

116 Let us observe that the severity of the attack is determined by the magnitude of  $\sigma_k$ . Smaller values  
117 of  $\sigma_k$  might represent natural noise inherent in data collection or random transformations, requiring  
118 careful consideration of what constitutes a ‘malicious’ level of perturbation.

119 Another feature-wise attack we formally define is the **blur attacker**. This attack is particularly  
120 relevant for image or signal data where  $x_k^i$  can be treated as a function over  $\mathcal{X}$ .

121 **Definition 2.** Let  $k \in [K]$  and  $\beta_k > 0$ . Client  $k$  is a **blurred attacker** if it provides samples perturbed  
122 according to a convolution operation:

$$\tilde{x}_k^i = x_k^i \star \zeta_k = \int_{\mathcal{X}} x_k^i(u') \zeta_k(u - u') du' \quad i = 1, \dots, n_k \quad (2)$$

123 where  $\star$  denotes the convolution operation. Typically,  $\zeta_k$  is a smooth kernel, and the parameter  $\beta_k$   
 124 controls its spread or blur radius.

125 A common choice for the kernel  $\zeta_k$  falls on Gaussian kernels, and the scalar  $\beta_k$  has a role of  
 126 controlling the spread of the kernel. Similarly to noisy attacks, in blur attacks the magnitude of the  
 127 perturbation is controlled by the parameter  $\beta_k$ , the larger it is the higher it perturbs the data.

## 128 2.2 Representation Operators: Wavelet Scattering Transform and Fourier Transform

129 In this section we recall the notion of a representation operator  $\Phi$ , which maps a signal  $x$  (e.g., an  
 130 image or a time-series) onto a transformed space. This transformation induces a metric  $d(x, x') =$   
 131  $\|\Phi[x] - \Phi[x']\|$  in the new space [31]. The core idea is that an effective representation operator  
 132  $\Phi$  should possess properties instrumental for accurately detecting and differentiating between data  
 133 samples. Specifically, for the purpose of identifying perturbed data,  $\Phi$  should be able to separate  
 134 distinct data characteristics while exhibiting robustness to common variations like slight translations  
 135 or small, non-malicious perturbations. We propose two variants for the representation layer of our  
 136 detection algorithm: one based on the Fourier Transform (FT) and the other on the Wavelet Scattering  
 137 Transform (WST) [17, 31]. The Fourier Transform is by far the most widely used tool for spectral  
 138 analysis in signal processing and data science due to its simplicity and interpretability. However, it  
 139 has been surprisingly underutilized in the context of Federated Learning (FL). We therefore include it  
 140 as an internal baseline in our study, allowing us to contrast its performance against the more structured  
 141 and hierarchical Wavelet Scattering Transform.

142 **Fourier Representation** We first formally define the Fourier Transform.

143 **Definition 3.** Let  $x \in L^1(\mathcal{X}, du)$ , the **Fourier Transform** of  $x$ , denoted by  $\mathcal{F}[x]$  is a complex valued  
 144 function defined as

$$\mathcal{F}[x](\omega) = \int_{\mathcal{X}} x(u) e^{-2\pi i(u \cdot \omega)} du \quad (3)$$

145 FT can be efficiently computed using the FFT algorithm [32]. Beyond its computational efficiency,  
 146 the Fourier Transform offers several critical advantages for feature extraction, particularly in the  
 147 context of analyzing data perturbations. As a linear operator ( $\mathcal{F}[ax + bx'] = a\mathcal{F}[x] + b\mathcal{F}[x']$  for  
 148 scalars  $a, b$  and integrable signals  $x, x'$ ), the FT maps additive perturbations directly to additive  
 149 components in the frequency domain. For instance, in the case of a *noisy attacker* where  $\tilde{x} = x + \epsilon$ ,  
 150 we have  $\mathcal{F}[\tilde{x}] = \mathcal{F}[x] + \mathcal{F}[\epsilon]$ . This linearity simplifies the analysis of such perturbations. Moreover,  
 151 the convolution theorem [33] states that convolution in the spatial domain corresponds to point-  
 152 wise multiplication in the frequency domain ( $\mathcal{F}[x \star \delta] = \mathcal{F}[x] \cdot \mathcal{F}[\delta]$ ). This property is highly  
 153 advantageous for detecting *blur attacker* perturbations, which are defined as convolutions. By  
 154 examining the frequency spectrum, different types of data manipulations, like blurring (attenuating  
 155 high frequencies) or specific noise patterns, reveal distinct signatures. However, FT is an invertible  
 156 operator: on one side it preserves all information present in the original signal, on the other hand it is  
 157 possible to reconstruct the original data from the FT.

158 **Wavelet Scattering Transform.** WST is a non-linear operator that, alternatively to Fourier based  
 159 representation, has been designed to be stable to additive perturbations, locally translation invariant  
 160 and to small continuous deformation. Moreover, the fact that WST is not invertible makes it  
 161 particularly attractive for privacy-enhancing applications in FL, as reconstructing the original input  
 162 data from the scattering coefficients is a challenging task. Following the construction in [17, 31] we  
 163 define the WST and discuss its most relevant properties.

164 Let  $\psi(u) \in L^2(\mathcal{X}, du)$  be a function referred to as the **mother wavelet**, and let  $\{a^j\}_{j \in \mathbb{Z}}$  be a family  
 165 of scale factors defined with respect to a fixed scalar  $a > 1$ . Let  $r \in G$  denote a discrete rotation,  
 166 where  $G$  is the group of discrete rotations acting on the domain  $\mathcal{X}$ . The  $j$ -th **wavelet function** is  
 167 then defined as  $\psi_j(u) = a^{-dj}\psi(a^{-j}r^{-1}u)$ . For a fixed maximal depth  $J \in \mathbb{Z}$ , we define the set of  
 168 admissible scale-rotation operators as  $\Lambda_J = \{\lambda = a^j r : |\lambda| = a^j < 2^J\}$ . In most implementations,  
 169 Morlet wavelets are employed as the mother wavelet, and the scale factor is typically chosen as  
 170  $a = 2^{1/Q}$  for some  $Q \in \mathbb{N}$  [34].

171 To streamline notation, following [17], we introduce the **propagator operator**, which acts on a  
 172 signal  $x \in L^1(\mathcal{X})$  by cascading modulus and convolution operations. Given a path of scale-rotation

173 operators  $p = (\lambda_1, \lambda_2)$ , the propagator applied to  $x$  is defined as:

$$U[p]x = | |x \star \psi_{\lambda_1}| \star \psi_{\lambda_2} | .$$

174 The definition of the WST naturally follows.

175 **Definition 4.** Let  $p = (\lambda_1, \dots, \lambda_m) \subset \Lambda_J$  be a path of length  $m$ . For any signal  $x \in L^1(\mathcal{X})$ , the  
176 WST along  $p$  is defined as:

$$S_J[p]x = U[p]x \star \phi_J, \quad (4)$$

177 where  $\phi_J$  is a low-pass filter rescaled to recover low-frequency content.

178 The WST representation shares structural similarities with convolutional neural networks (CNNs),  
179 with the key distinction that the wavelet filters are fixed rather than learned. The WST defines a norm  
180 with properties desirable for detection and classification. Notably, the operator is **non-expansive**: for  
181 any  $x, x' \in L^2(\mathcal{X}, du)$ , the following inequality holds:

$$\|S_J[p]x - S_J[p]x'\| \leq \|x - x'\|. \quad (5)$$

182 This implies that small, non-adversarial perturbations do not substantially affect the representation.

183 Additionally, WST is **translation invariant** in the limit: for a translated signal  $x_c(u) = x(u - c)$   
184 with  $c \in \mathcal{X}$ , we have

$$\lim_{J \rightarrow \infty} \|S_J[p]x - S_J[p]x_c\| = 0.$$

185 Finally, the WST is **Lipschitz continuous** with respect to small  $C^2$ -diffeomorphisms. That is, if  
186 a signal  $x$  undergoes a smooth deformation with small norm, the resulting change in the WST  
187 representation remains bounded.

### 188 3 Malicious Client Detector: Waffle

189 This section details the architecture and training of our server-side detector, **Waffle** (Wavelet and  
190 Fourier representations for Federated Learning), designed to identify clients contributing potentially  
191 harmful updates based on their data characteristics. **Waffle** is a parametric classification model,  
192 trained offline on a generated auxiliary dataset  $\mathcal{D}^{\text{aux}}$  to distinguish between benign and malicious  
193 clients. It operates by analyzing aggregated, non-privacy-leaking spectral embeddings of client data  
194 distributions.

#### 195 3.1 Offline Detector Training

196 The training of the **Waffle** detector is conducted entirely offline, prior to the federated learning  
197 process. This approach offers several advantages: it avoids interfering with live FL rounds, allows for  
198 controlled generation of diverse malicious scenarios, and ensures the detector is fully trained and  
199 ready when FL begins. Coherently with common practices in FL frameworks utilizing auxiliary data  
200 [35], the server has access to a representative auxiliary dataset  $\mathcal{D}^{\text{aux}}$ . Algorithm 1 summarizes the  
201 procedure.

202 The offline training proceeds over  $E$  epochs. In each epoch  $e \in \{1, \dots, E\}$ , the server simulates a  
203 new FL round by generating a set of  $\tilde{K}$  fictitious clients with synthetic data and associated ground-  
204 truth labels (benign or malicious). This dynamic generation of clients each epoch, similar to methods  
205 used for estimating client relationships [36], increases the diversity of simulated scenarios and  
206 helps prevent overfitting. Each training iteration within an epoch consists of two main steps: *data  
207 simulation/attack* and *feature extraction/labeling*.

208 **Step 1: Data Simulation and Attack** For each sample  $x \in \mathcal{D}^{\text{aux}}$ , the server decides whether  
209 to simulate an attack on that sample or keep it clean. This decision is made by drawing from a  
210 Bernoulli distribution with probability  $p = 1/2$  of being attacked. If selected for attack, the server  
211 randomly chooses between two types of data perturbations with equal probability: blur or noise. If a  
212 sample is selected for blurring, the server samples a blur severity parameter  $\beta \sim \text{Unif}(\beta_0, \beta_1)$  and  
213 applies a blurring operation according to Definition 2. This simulates clients whose data might be of  
214 lower quality or intentionally blurred to impair model training or target specific vulnerabilities. If a  
215 sample is selected for adding noise, the server samples a noise variance  $\sigma \sim \text{Unif}(\sigma_0, \sigma_1)$  and applies  
216 additive noise according to Definition 1. This simulates clients whose data might be corrupted by

217 sensor noise or intentionally perturbed with adversarial noise patterns. After processing all samples  
 218 in  $\mathcal{D}^{\text{aux}}$  in this manner, the server possesses a modified dataset where each sample is either clean,  
 219 blurred, or noisy, with the attack type and parameters recorded.

220 **Step 2: Fictitious Client Creation and Feature Extraction** The modified dataset from Step 1 is  
 221 then partitioned to create the data for  $\tilde{K}$  fictitious clients. These clients are equally divided into two  
 222 groups:  $\tilde{K}/2$  benign and  $\tilde{K}/2$  malicious. Clean data samples are assigned to benign clients, while  
 223 attacked data samples (either blurred or noisy) are assigned to malicious clients. Let  $\{x_k^i\}_{i=1}^{n_k}$  denote  
 224 the data points assigned to the  $k$ -th fictitious client, where  $n_k$  is the number of samples for client  $k$ .

225 **Principal Component Analysis** For each simulated client  $k$ , PCA [37] is applied to their local  
 226 dataset  $\{x_k^i\}_{i=1}^{n_k}$  to analyze the covariance structure and extract the top  $r$  principal components  $v_k^i$   
 227 with eigenvalues  $\lambda_k^i$ , capturing dominant directions of variance. A compact representation vector is  
 228 defined as:

$$\hat{x}_k = \sum_{i=1}^r \alpha_k^i v_k^i, \quad \text{with } \alpha_k^i = \frac{\lambda_k^i}{\sum_{j=1}^r \lambda_k^j} \quad (6)$$

229 This PCA-derived vector  $\hat{x}_k$  summarizes the client data's intrinsic structure by weighting principal  
 230 directions by their explained variance. The PCA step supports dimensionality reduction and noise  
 231 filtering, extracting features sensitive to structural perturbations such as blur or noise. Notably, it  
 232 is performed offline on simulated data at the server: in real FL deployments, clients neither share  
 233 raw data nor PCA results. Instead, this offline PCA informs training, while clients transmit only the  
 234 privacy-preserving spectral embedding  $\varphi_k$ , discussed next.

235 **Spectral Embedding** Following this PCA step, the spectral representation  $\varphi_k$  is computed for  
 236 each fictitious client  $k$ . This is achieved by applying a spectral operator  $\Phi$  (either the WST or FT) to  
 237 statistics derived from the client's data distribution, such as the PCA-derived representation vector  $\hat{x}_k$   
 238 or the set of principal eigenvalues  $\lambda_k^i$ . Spectral transforms are particularly sensitive to frequency and  
 239 texture information, making them effective at capturing the systematic changes introduced by attacks  
 240 like blur and noise. The output  $\varphi_k = |\Phi[\hat{x}_k]|$ , where the modulus is taken element-wise, results in a  
 241 fixed-size vector representation for each client. This  $\varphi_k$  is designed to be an aggregate statistic that  
 242 captures characteristics of the data distribution without revealing individual data points, making it  
 243 suitable as a non-privacy-leaking feature for the detector in a live FL setting.

244 Finally, for each epoch, we obtain a dataset of client representations and their corresponding labels:  
 245  $\{(\varphi_k, \mu_k)\}_{k=1}^{\tilde{K}}$ , where  $\mu_k \in \{\text{B (Benign), A (Attacker)}\}$ . The detector weights  $w$  are updated using  
 246 a stochastic optimizer (e.g., SGD, Adam) to minimize a binary classification loss, such as Binary  
 247 Cross-Entropy (BCE) [38], between the detector's prediction based on  $\varphi_k$  and the ground-truth label  
 248  $\mu_k$ .

### 249 3.2 Offline Detection and Filtering

250 Once the **Waffle** detector model  $w$  has been trained offline on the simulated auxiliary dataset  $\mathcal{D}^{\text{aux}}$   
 251 and prior to the first FL communication round, each client  $k \in \{1, \dots, K\}$  in the federation processes  
 252 its local training data  $\{x_k^i\}_{i=1}^{n_k}$  privately on their device. This processing involves a sequence of  
 253 steps performed locally. First, each client computes the PCA of their local training samples to  
 254 derive the representation vector  $\hat{x}_k$ , as defined in Equation (6). Then, each client computes its spectral  
 255 embedding  $\varphi_k = \Phi[\hat{x}_k]$ , by applying the spectral operator  $\Phi$  (WST or FT).

256 After completing these local computations and obtaining  $\varphi_k$ , each client  $k$  securely transmits only  
 257 this resulting spectral embedding vector to the server. The server, upon receiving  $\varphi_k$  from each  
 258 participating client, inputs it into the pre-trained **Waffle** detector  $w$ . Clients that are classified as  
 259 malicious by the detector are then excluded from participating in the federated training process for  
 260 the global model  $\theta$ . This preemptive filtering step enhances the stability and reliability of the global  
 261 model training process, leading to potentially faster and more robust convergence by ensuring that  
 262 aggregation occurs over updates from predominantly benign sources.

263 Moreover, due to its modular nature, **Waffle** operates as an initial defense layer. The set of clients  
 264 validated as benign by **Waffle** can proceed with any federated learning aggregation methods, allowing  
 265 **Waffle** to be easily combined with other online robust aggregation techniques to further strengthen  
 266 the overall defense strategy.

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**Algorithm 1** Waffle Offline Training

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**Require:** Auxiliary dataset  $\mathcal{D}^{\text{aux}}$ , Number of epochs  $E$ , Number of fictitious clients  $\tilde{K}$ , Number of top PCs  $r$ , Spectral operator  $\Phi$ , Learning rate  $\eta$   
**Ensure:** Trained detector weights  $w$

```
1: Initialize detector weights  $w$ 
2: for  $e = 1 \dots E$  do
3:   // Simulate Data and Clients for Epoch  $e$ 
4:    $\mathcal{D}_e^{\text{simulated}} \leftarrow \text{SimulateAttackedData}(\mathcal{D}^{\text{aux}})$                                  $\triangleright$  Applies random attacks to  $\mathcal{D}^{\text{aux}}$ 
5:    $\{(\mathcal{D}_k, \mu_k)\}_{k=1}^{\tilde{K}} \leftarrow \text{PartitionData}(\mathcal{D}_e^{\text{simulated}}, \tilde{K})$            $\triangleright$  Creates  $\tilde{K}$  clients with labels
6:   // Extract Features for Each Simulated Client
7:   Initialize epoch dataset  $\mathcal{S}_e = \emptyset$                                                $\triangleright$  Stores  $(\varphi_k, \mu_k)$  pairs
8:   for  $k = 1 \dots \tilde{K}$  do
9:      $\{x_k^i\}_{i=1}^{n_k} \leftarrow \mathcal{D}_k$ 
10:    Compute PCA-derived representation  $\hat{x}_k$  from  $\{x_k^i\}$                                  $\triangleright$  Eq. (6)
11:    Compute spectral embedding  $\varphi_k \leftarrow |\Phi[\hat{x}_k]|$                            $\triangleright$  Apply FT or WST to  $\hat{x}_k$ 
12:    Add  $(\varphi_k, \mu_k)$  to  $\mathcal{S}_e$ 
13:   end for
14:   // Update Detector Model
15:    $w \leftarrow \text{Opt}(\mathcal{L}_{\text{BCE}}(w; \mathcal{S}_e))$                                       $\triangleright$  Optimization step
16: end for
17: return  $w$ 
```

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267 **4 Theoretical Guarantees**

268 In this section, we establish a theoretical foundation for our proposed algorithm, which we refer  
269 to as **Waffle**. Our primary focus is to demonstrate the benefits of removing adversarial clients in  
270 FL scenarios. We show that by filtering out malicious updates, **Waffle** provides a more accurate  
271 estimate of the true global model compared to standard FedAvg [1], which is susceptible to adversarial  
272 poisoning. We provide general error bounds with detailed proofs presented in Appendix [A].

273 Let  $\mathcal{B} \subset \{1, \dots, K\}$  denote the set of benign clients and  $\mathcal{M} \subset \{1, \dots, K\}$  the set of malicious  
274 clients in a federated system with  $K$  total clients. We assume these sets are disjoint and their union  
275 covers all clients, i.e.,  $\mathcal{B} \cap \mathcal{M} = \emptyset$  and  $\mathcal{B} \cup \mathcal{M} = \{1, \dots, K\}$ . To model the heterogeneity and  
276 potential adversarial influence in client updates, we adopt the following statistical framework:

277 **Assumption 1.** For each benign client  $k \in \mathcal{B}$ , the local model update  $\theta_k$  is an independent random  
278 variable drawn from a distribution  $\rho_k(\bar{\theta}^b, \sigma^b)$ . This distribution is centered around a common benign  
279 mean  $\bar{\theta}^b$  with variance  $(\sigma^b)^2$ , i.e.,  $\mathbb{E}[\theta_k] = \bar{\theta}^b$  and  $\text{Var}[\theta_k] = (\sigma^b)^2$ . Similarly, for malicious clients  
280  $k \in \mathcal{M}$ , the local updates  $\theta_k$  are independent random variables drawn from  $\rho_k(\bar{\theta}^m, \sigma^m)$  with  
281  $\mathbb{E}[\theta_k] = \bar{\theta}^m$  and  $\text{Var}[\theta_k] = (\sigma^m)^2$ .

282 **Assumption 2.** We posit that malicious clients exhibit significantly higher update variance com-  
283 pared to benign clients, reflecting a diverse range of attack strategies and the potential for large,  
284 destabilizing updates. Formally, we assume  $\sigma^m \gg \sigma^b$ .

285 The standard federated averaging estimator is defined as a weighted average of client updates:  
286  $\theta_{\text{avg}} = 1/K \sum_{k=1}^K \theta_k$ . Our objective is to obtain an estimator that is unbiased with respect to the  
287 benign client distribution, meaning  $\mathbb{E}[\theta_{\text{avg}}] = \bar{\theta}^b$ . We demonstrate that removing malicious clients  
288 is crucial for achieving this goal. We analyze two scenarios: one where the benign and malicious  
289 updates have different means (Lemma [1]) and one where they share the same mean but differ in  
290 variance (Lemma [2]).

291 **Lemma 1.** If the benign and malicious client updates have different mean parameter values, i.e.,  
292  $\bar{\theta}^m \neq \bar{\theta}^b$ , then the standard federated averaging estimator  $\theta_{\text{avg}}$  is a **biased estimator** of  $\bar{\theta}^b$ , meaning  
293  $\mathbb{E}[\theta_{\text{avg}}] \neq \bar{\theta}^b$ .

294 **Lemma 2.** Let  $\theta_{avg}^{\mathcal{B}} = \frac{1}{|\mathcal{B}|} \sum_{k \in \mathcal{B}} \theta_k$  be the federated averaging estimator computed using only  
 295 benign client updates. Under Assumption 2 if  $(\sigma^m)^2 > \left(2 + \frac{|\mathcal{M}|}{|\mathcal{B}|}\right) (\sigma^b)^2$ , then the variance of the  
 296 standard federated averaging estimator is higher than that of our estimator:  $\text{Var}[\theta_{avg}] \geq \text{Var}[\theta_{avg}^{\mathcal{B}}]$ .

297 Lemmas 1 and 2 provide the foundation for the following proposition, which formally establishes the  
 298 advantage of removing malicious clients from the federated aggregation process.

299 **Proposition 1.** Under Assumptions 1 and 2, removing malicious clients (those in  $\mathcal{M}$ ) from the  
 300 federation yields a superior estimator of the global model. Specifically, the resulting estimator is  
 301 unbiased (in the sense of Lemma 1) and exhibits a reduced variance (as shown in Lemma 2), leading  
 302 to improved model accuracy and robustness.

## 303 5 Experiments

304 In this section, we present experimental results on widely used federated learning benchmark  
 305 datasets [39, 40, 41], comparing the performance of Waffle in its two variants—one using the  
 306 WST representation and the other using FT—with established baselines from the Byzantine-resilient  
 307 FL literature. Details on implementation settings, datasets, and models are provided in Appendix B.  
 308 Section 5.1 evaluates the detection performance of the two variants of Waffle, highlighting the  
 309 differences between the WST and FT representations. In Section 5.2, we compare Waffle against  
 310 standard Byzantine-resilient FL baselines, including FedAvg [1], Krum and mKrum [12], GeoMed [42],  
 311 and TrimmedMean [7]. Additionally, we demonstrate that Waffle can be applied on top of any  
 312 aggregation algorithm, improving their performance. Further experiments, comparisons and code  
 313 release details are reported in Appendix B and the metrics used for evaluation—both for detection  
 and classification—are detailed in Appendix C.

Table 1: **Client Detection.** Comparison between variants of Waffle using WST and FT representations, under two attack scenarios (40% top, 90% bottom). Metrics (F1 score, Precision, Recall, Accuracy [43]) refer to the detection of malicious clients.

Method	FashionMNIST				CIFAR-10				CIFAR-100				
	F1	Prec.	Rec.	Acc.	F1	Prec.	Rec.	Acc.	F1	Prec.	Rec.	Acc.	
40%	Waffle - FT	65.11	60.9	<b>70.0</b>	70.0	79.75	68.42	<b>95.59</b>	67.0	56.69	41.38	<b>90.0</b>	
	Waffle - WST	<b>71.88</b>	<b>95.83</b>	57.5	<b>82.0</b>	<b>94.87</b>	<b>97.36</b>	92.5	<b>96.0</b>	<b>83.33</b>	<b>93.75</b>	75.0	<b>88.0</b>
90%	Waffle - FT	<b>81.81</b>	95.45	<b>71.59</b>	<b>72.0</b>	<b>93.05</b>	89.69	<b>96.67</b>	<b>87.0</b>	88.1	88.1	<b>88.1</b>	<b>80.0</b>
	Waffle - WST	65.65	<b>100.0</b>	48.86	55.0	90.91	<b>100.0</b>	83.33	86.0	<b>88.85</b>	<b>100.0</b>	67.86	73.0

314

### 315 5.1 Waffle : WST vs Fourier

316 We compare the detection performance of Waffle to assess the differences between the WST  
 317 and FT representations. As illustrated in Figure 2, both representations yield a clear separation  
 318 between benign and malicious clients. The visualizations—obtained via two-dimensional PCA  
 319 embeddings—show that the method effectively distinguishes between the different attacker groups  
 320 and benign clients, regardless of the chosen representation. However, as shown in Table 1, the  
 321 quantitative results at the client level differ between the two variants. We report standard detection  
 322 metrics: precision, F1 score, recall, and accuracy [43], setting 40% and 90% of attackers. The WST  
 323 variant consistently achieves higher precision and F1 scores, while the FT variant tends to yield  
 324 higher recall. In the context of malicious client detection, higher recall is often desirable, as it reduces  
 325 the likelihood of overlooking faulty clients. Table 1 highlights the robustness of Waffle : unlike  
 326 most Byzantine-resilient FL methods, it maintains strong predictive performance even when the vast  
 327 majority of clients are malicious. Notably, in the extreme case with 90% adversarial clients, Waffle  
 328 with WST achieves 100% precision across all datasets.

### 329 5.2 Comparison with Baselines and Orthogonality of Waffle

330 In this section, we compare Waffle with established Byzantine-resilient FL methods, highlighting its  
 331 advantages in two complementary settings: (1) we evaluate the impact of applying the two Waffle

Table 2: Comparison between baselines for detecting malicious clients and **Waffle** (with both WST and FT). **Waffle** -WST combined with FedAvg achieves the highest test accuracy across all datasets, outperforming baselines designed to mitigate Byzantine attacks. Results also highlight the orthogonality of **Waffle** to aggregation methods, consistently improving their performance. For reference, the test accuracy of FedAvg without malicious clients is: FashionMNIST 75.08%, CIFAR-10 50.24%, CIFAR-100 17.72%.

Dataset	Setting	FedAvg	Krum	mKrum	GeoMed	TrimmedMean
FashionMNIST	w/o detector	73.33	73.85	70.56	72.75	74.84
	<b>Waffle</b> - WST	<b>76.18</b>	70.26	74.75	74.18	75.21
	<b>Waffle</b> - FT	73.38	72.10	74.40	75.35	74.98
CIFAR-10	w/o detector	48.75	45.2	47.4	48.51	48.22
	<b>Waffle</b> - WST	<b>49.70</b>	46.28	49.08	49.41	49.0
	<b>Waffle</b> - FT	46.95	44.13	47.58	47.14	46.86
CIFAR-100	w/o detector	16.35	9.61	14.73	16.83	16.85
	<b>Waffle</b> - WST	<b>17.12</b>	8.50	14.85	16.32	15.89
	<b>Waffle</b> - FT	11.58	7.24	10.15	12.25	10.29

332 variants to FedAvg, compared to using different aggregation rules without detection; and (2) we  
 333 assess the effect of applying **Waffle** on top of robust aggregation algorithms. As shown in Table 2  
 334 the WST variant of **Waffle** combined with FedAvg consistently outperforms all baselines across all  
 335 datasets. Furthermore, **Waffle** improves the performance of each aggregation method it is applied to,  
 336 demonstrating its orthogonality to the choice of aggregator. These results indicate that **Waffle** is  
 337 effective in identifying and removing malicious clients without compromising benign contributions.  
 338 In contrast, the FT variant exhibits more variable performance, further confirming the suitability of  
 339 WST representations for this detection task. For reference, we also report the test accuracy of FedAvg  
 340 trained on a clean federation (i.e., without malicious clients, corresponding to  $\theta_{avg}^B$  in the notation  
 341 of Lemma 2): FashionMNIST 75.08%, CIFAR-10 50.24%, CIFAR-100 17.72%. These values  
 342 demonstrate that **Waffle** enables recovery of near-optimal performance, effectively neutralizing the  
 343 impact of adversarial clients.

## 344 6 Conclusion

345 We propose **Waffle**, a novel offline algorithm to detect malicious client data in Federated Learning  
 346 (FL) before training. Exploiting stable spectral features extracted via the Wavelet Scattering Transform  
 347 (WST) and Fourier Transform (FT), it enables robust anomaly detection from private, low-dimensional  
 348 client-side summaries built on publicly distilled data. By filtering out compromised clients prior to  
 349 training, **Waffle** significantly improves convergence speed, final model accuracy, and robustness to  
 350 data contamination. It achieves near-perfect precision (100% in our benchmarks) even in extreme  
 351 scenarios with up to 90% malicious clients, outperforming strategies that rely solely on robust  
 352 aggregation. This early detection mechanism also reduces training time, communication overhead,  
 353 and energy consumption—factors crucial in large-scale deployments. Furthermore, **Waffle** is model-  
 354 agnostic and can be seamlessly integrated with existing FL defenses to enhance overall system  
 355 security.

356 Future work will focus on extending **Waffle** to defend against more sophisticated threats, including  
 357 backdoor attacks, model poisoning, and sybil-based infiltration. In parallel, we plan to adapt  
 358 the approach to support wider neural architectures capable of handling more complex and high-  
 359 dimensional datasets, such as CIFAR-100 or even ImageNet-scale benchmarks. These directions aim  
 360 to broaden the applicability of **Waffle** to realistic FL scenarios in vision, healthcare, and IoT.

361 **Limitations.** **Waffle** targets data-level attacks altering client input features, not model-level attacks  
 362 (e.g., gradient manipulation, backdoors), which necessitate different defense strategies. However,  
 363 combining **Waffle** with robust aggregation can help mitigate such hybrid threats.

364 **Broader Impact.** Our method enhances FL robustness and trustworthiness, crucial for deployments in  
 365 sensitive domains (e.g., healthcare, finance), and reduces resource consumption. Potential misuse (e.g.,  
 366 unfairly excluding outlier populations) warrants careful auditing and fairness-aware deployments,  
 367 though **Waffle** itself introduces no new privacy or fairness risks beyond those inherent in existing  
 368 FL pipelines.

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621 results?

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623 Justification: All implementation details on splits, hyperparameters, optimizers and architectures are detailed in Appendix B.

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634 Justification: Appendix B contains the results obtained from experiments conducted with  
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