Label Privacy in Split Learning for Large Models with Parameter-Efficient Training

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Abstract

 As deep learning models become larger and more expensive, many practitioners turn to fine-tuning APIs. These web services allow fine-tuning a model between two parties: the client that provides the data, and the server that hosts the model. While convenient, these APIs raise a new concern: the data of the client is at risk of privacy breach during the training procedure. This challenge presents an important practical case of vertical federated learning, where the two parties perform parameter-efficient fine-tuning (PEFT) of a large model. In this study, we systematically search for a way to fine-tune models over an API *while keeping the labels private*. We analyze the privacy of LoRA, a popular approach for parameter- efficient fine-tuning when training over an API. Using this analysis, we propose ¹¹ P³EFT, a multi-party split learning algorithm that takes advantage of existing PEFT properties to maintain privacy at a lower performance overhead. To validate our algorithm, we fine-tune DeBERTa-v2-XXLarge, Flan-T5 Large and LLaMA-2 7B using LoRA adapters on a range of NLP tasks. We find that $\overline{P}{}^3EFT$ is competitive with existing privacy-preserving methods in multi-party and two-party setups while having higher accuracy.

1 Introduction

 One of the main reasons behind deep learning success is its ability to transfer knowledge between tasks [\[34\]](#page-11-0). When training a model for any particular problem, it is common to reuse previously trained models from other, related problems. In the past, this was typically done by downloading pre-trained model weights from public hubs, then fine-tuning the said models on the downstream task. However, as models grow larger and more compute-intensive, fine-tuning them locally becomes an increasingly difficult task. Furthermore, many recent models are not released, but instead made available as proprietary services.

 When a model cannot be fine-tuned locally, many practitioners opt instead for the so-called fine-tuning APIs [\[27,](#page-10-0) [16,](#page-10-1) [6,](#page-9-0) [26\]](#page-10-2). These APIs are web services that host one or several pre-trained models and allow clients to perform limited fine-tuning. More specifically, APIs usually allow their clients to run parameter-efficient fine-tuning (PEFT), such as LoRA [\[15\]](#page-10-3) or Prefix-tuning [\[21\]](#page-10-4). These techniques allow adapting a model to a dataset while training a relatively small number of additional weights, which is particularly important for large language or image generation models that have billions of parameters.

 Although the fine-tuning APIs can be convenient, they also introduce new risk in terms of data privacy. When a client uses such API to train on sensitive data, they need to ensure that their data will stay private [\[7\]](#page-9-1). This is particularly important when dealing with patient's medical records, personal user data or trade secrets [\[24,](#page-10-5) [19\]](#page-10-6). The two main threats to data privacy are that the API provider obtains the private data and that a third party intercepts data in transit. Therefore, data privacy is

 not guaranteed even if the API provider is trusted. Several recent works propose LLM fine-tuning protocols that establish a certain level of privacy for multi-party fine-tuning [\[42,](#page-11-1) [7,](#page-9-1) [22\]](#page-10-7). Unfortunately, these algorithms work for a narrow class of fine-tuning algorithms or assume that a client can run LLM training locally using an obfuscated version of the model, provided by a remote server [\[42\]](#page-11-1). As a result, these algorithms are impractical for our use case of fine-tuning over an API. The few algorithms that are suitable for API fine-tuning guarantee the privacy of input tokens [\[22\]](#page-10-7), meaning that the attacker can infer private training *labels*. In this work, we seek to alleviate this problem by designing a two-party fine-tuning protocol that

 performs standard parameter-efficient fine-tuning with privacy guarantees. We formulate our protocol 46 as a **special case of split learning** (or vertical federated learning), where one side (server) holds the 47 pre-trained model and the other (client) has private training data. More specifically, we focus on the **privacy of client's training labels**. While input privacy is often crucial, there are scenarios where input data is publicly available, such as social media user pages. In these cases, labels could include ad clicks (known to the social network) or financial information (known to a bank that matches social profiles to its internal records). This example further justifies the use of LLMs, as social media pages often contain substantial amounts of text, and LLMs excel at processing long-context data.

 Instead of developing a specific privacy-preserving architecture, we seek algorithms that can work with popular existing models and PEFT algorithms. Furthermore, our approach relies on the properties of parameter-efficient fine-tuning. Notably, since the adapters are compact, both parties can maintain multiple sets of adapters and swap between them with relative ease. This allows us to design a PEFT-specific algorithm that can solve its task more effectively than general split learning strategies [\[18\]](#page-10-8).

We summarize our main contributions as follows:

- We analyze Low-Rank Adaptation, a common parameter-efficient fine-tuning algorithm, from the perspective of label privacy in the split learning setup. We observe that, despite fine-tuning less than 0.1% of model parameters, PEFT algorithms leak client's training labels against simple attacks that work for modern pretrained transformers.
- Based on our analysis, we formulate a framework for privacy-preserving parameter-efficient 65 fine-tuning (P³EFT). This framework leverages the properties of PEFT to obfuscate the gradients and parameters communicated during fine-tuning with little impact on the fine-tuned model quality.
- \bullet To verify the practical viability of P³EFT, we conduct experiments on popular real-world 69 PEFT workloads^{[1](#page-1-0)}. Specifically, we fine-tune DeBERTa-v2-XXL [\[13\]](#page-9-2), Flan-T5-Large [\[4\]](#page-9-3) and LLaMA-2 7B [\[35\]](#page-11-2) on a set of standard language understanding problems. We find that, μ ₇₁ compared to prior split learning algorithms, P^3EFT can maintain label privacy throughout training with a significantly smaller accuracy drop.

2 Background

2.1 Federated learning and split learning

 Privacy preservation in machine learning has been a subject of active study within several frameworks. An important branch of privacy-preserving learning methods is federated learning, or FL [\[24\]](#page-10-5), which can be broadly described as an approach allowing several parties to train a model jointly without sharing their private data. In particular, vertical federated learning [\[12,](#page-9-4) [43\]](#page-11-3) targets the scenario where different features (including the label) of each training instance are kept by different parties.

 One of the most popular approaches to vertical FL for neural networks is split learning [\[10,](#page-9-5) [37\]](#page-11-4), where each party stores its part of the overall model. To train the model in such an approach, it is only necessary to transfer the intermediate activations and the gradients between layers, while the data itself is stored at the premises of the participant hosting each layer. In this work, we focus on the two-party formulation of split learning, where one side stores the features for each example and

another one stores the labels.

¹The code is available at github.com/anonymousauthor56/P3EFT

 Recent works have investigated the setting of two-party split learning from the label leakage per- spective [\[38,](#page-11-5) [28\]](#page-11-6): because the label party needs to pass the gradients of the loss function to the non-label party, it is possible for the latter party to deduce the labels by inspecting the gradients or activations or by hijacking the training procedure. Li et al. [\[18\]](#page-10-8) provide a set of attack methods that allow recovering private labels and propose a defense mechanism that injects noise into the gradients; however, they test the approach on pretraining smaller models, and we study finetuning large models on private downstream data.

93 2.2 Parameter-efficient finetuning

 The majority of large neural networks today are not trained with a specific task in mind: instead, they are pretrained on a general objective and then adapted for the downstream problem. Importantly, the growth in the size of foundation models has led to the increased popularity of parameter-efficient finetuning (PEFT) methods that adapt the model to a given task by training a small number of task-specific parameters. There are several prominent approaches to parameter-efficient finetuning, ranging from trainable prompts [\[21,](#page-10-4) [11\]](#page-9-6), to residual adapters [\[14,](#page-10-9) [29\]](#page-11-7). We focus on Low-Rank Adaptation (or LoRA, [15\)](#page-10-3), one of the most popular PEFT methods that adds extra parameters to each weight matrix in the form of a low-rank factorization (see Appendix [C](#page-13-0) for a more detailed description). Such formulation allows LoRA adapters to be merged into the original weights after finetuning; this ability, combined with the simplicity of the method, has made LoRA a broadly popular approach in multiple domains. Still, the approach we propose can be applied to any PEFT method.

 Several recent lines of work explore the problem of fine-tuning LLMs with privacy guarantees [\[44,](#page-12-0) [31\]](#page-11-8). Zhao et al. [\[46\]](#page-12-1) analyze the viability of prompt tuning for federated learning, and Zhang et al. [\[45\]](#page-12-2), Liu et al. [\[23\]](#page-10-10) study PEFT algorithms in the setting of *horizontal* federated learning, that is, where multiple users train a shared model on their local private data. Another, more relevant research direction considers private fine-tuning in a *vertical* federated learning scenario, where participants hold different model layers [\[22,](#page-10-7) [40\]](#page-11-9). Most of these studies leverage the idea of differential privacy to prove an upper bound on how much information is leaked [\[8\]](#page-9-7). Unfortunately, these upper bounds are typically loose and do not match practical observations for real models. Furthermore, the majority of these studies only guarantees privacy of specific parts of the training procedure: for instance, Li et al. [\[22\]](#page-10-7) only protects the input features, and not labels or model parameters. Finally, Xiao et al. [\[42\]](#page-11-1) presents an alternative algorithm that protects client data by running the entire fine-tuning on client side by emulating the server-side model layers. While this approach is more holistic, it assumes that clients can run fine-tuning locally, which makes it impractical for many real-world users of LLM fine-tuning APIs. The primary distinction between our work and these studies is that we investigate parameter-efficient adaptation in the setting of split learning: we aim to finetune a model without disclosing the labels of examples to the model provider.

3 Privacy-preserving parameter-efficient fine-tuning

 In this section, we analyze the privacy of parameter-efficient fine-tuning and propose a protocol for two-party parameter-efficient fine-tuning with the desired privacy guarantees. We begin by analyzing the privacy of API fine-tuning with popular PEFT algorithms in Sections [3.1](#page-2-0) and [3.2.](#page-3-0) Then, in Section [3.3,](#page-4-0) we formulate a protocol for privately computing gradients over fine-tuning APIs. Finally, 126 we formulate the full P^3EFT protocol in Section [3.4.](#page-5-0)

3.1 Setup

 To analyze the privacy of API fine-tuning, we first need to formulate a common framework for this type of APIs and develop private learning protocols. This step is important, because existing fine-tuning APIs greatly vary in what they offer to the client: from closed APIs that require users to submit their full training data [\[27\]](#page-10-0) to more flexible APIs where clients can run individual training steps [\[20,](#page-10-11) [2,](#page-9-8) [30\]](#page-11-10). Similarly to most existing works on split learning, we focus on the latter type of APIs that allows clients to run individual forward and backward passes over a remote model. Thus, a client can use these APIs to obtain the training gradients for their PEFT adapters, then update adapters locally with any optimization method. In our work, we adopt this archetype of fine-tuning API as it offers sufficient flexibility to develop privacy-preserving algorithms.

 We formulate fine-tuning over an API for two or more parties: a client, and one or several servers. 138 The client owns a training dataset with inputs X and labels Y . In turn, each server has the same 139 pre-trained model $h(x_i, \tilde{\theta}) \in \mathcal{R}^d$. Note that the parameters θ denote not the pre-trained model

Figure 1: A visualization of top-2 principal components of gradients (top) and activations (bottom) from different fine-tuning steps (left to right). Color indicates the training labels (binary).

¹⁴⁰ weights, but the trainable adapter weights for a certain PEFT algorithm. A model can encode an input $141 \quad x_i \in X$ and produce a d-dimensional vector of activations that depend on the learned adapter weights 142 θ .

¹⁴³ To allow fine-tuning, a server offers two API methods:

144 1. **forward** $(x, \theta) \rightarrow h(x, \theta)$ that computes model activations on input x using adapter weights 145 θ ;

146 2. **backprop** $(x, \theta, g_h) \rightarrow g_\theta$ that receives gradients of an arbitrary loss function w.r.t. model activations $g_h = \frac{\partial L(h(x, \theta))}{\partial h(x, \theta)}$ activations $g_h = \frac{\partial L(h(x, \theta))}{\partial h(x, \theta)}$ and returns the gradients w.r.t. adapter parameters, g_θ 148 $\frac{\partial L(h(x, \theta))}{\partial \theta}$.

149 We further assume that both forward(\cdot) and backprop(\cdot) APIs are stateless and deterministic, i.e. ¹⁵⁰ calling the same API method multiple times (or on multiple servers) with the same inputs produces ¹⁵¹ identical results. Thus, if the model uses dropout or any other form of non-determinism, we assume 152 that clients provide the random seed as a part of x .

¹⁵³ To fine-tune a model with this API, a client can initialize adapters locally, alongside with a small task-specific head^{[2](#page-3-1)}, then train both adapters and the head. For each training batch $(x, y) \in D$, a client 155 calls forward (x, θ) to compute feature representations, then predicts with local "head" and computes ¹⁵⁶ task-specific loss function L. After that, a client performs backward pass: first, it computes gradients 157 w.r.t. local head inputs $g_h = \frac{\partial L}{\partial h}$, then passes those gradients to a remote server via backprop (x, θ, g_h) 158 API call to compute gradients w.r.t. $\frac{\partial L}{\partial \theta}$. Finally, a client updates both θ and local "head" parameters ¹⁵⁹ using the optimizer of choice.

 Before building more advanced algorithms, let us analyze the privacy of client's labels under standard fine-tuning. We consider an "honest, but curious" attacker model. This means that the server will faithfully run the forward and backprop computations as requested by the client without changing the results. Furthermore, we assume that servers are independent and do not communicate client's data between each other. However, a server can recover client's labels by performing arbitrary computations using any information it receives from the client. When training in this way, a client does not directly communicate training labels to the server. However, it communicates inputs, adapter parameters, and gradients. Furthermore, the server communicates input representations that can be intercepted by a third party.

¹⁶⁹ 3.2 Label Leakage of Standard Split Learning

¹⁷⁰ In Figure [1,](#page-3-2) we train a DeBERTa-v2-XXL model on the SST-2 [\[32\]](#page-11-11) sentiment classification dataset.

171 The top row depicts the gradients g_h communicated by the client when calling backprop(\cdot) at different

172 training stages. In the bottom row, we similarly track activations $h(x, \theta)$ that server may compute

173 based on the specified x, θ . We defer further additional figures and details to Section [4.1.](#page-6-0)

¹⁷⁴ As we can see, both gradients and activations are arranged in such a way that simple k-means ¹⁷⁵ clustering would reveal which objects have the same label. The training activations (bottom row) do

²A linear layer that predicts class logits or regression target.

Figure 2: An intuitive illustration of the proposed fine-tuning protocol.

 not reveal labels right away (at least not against this attack). However, they gradually "leak" private label information during training. Informally, it appears that the training gradients gradually pull apart the feature representations for each label, until eventually they turn into separate clusters. From an information-theoretic perspective, knowing just one vector of gradients *or* trained activations allows the attacker to learn all but one bit^{[3](#page-4-1)} of information about client's private labels.

¹⁸¹ To summarize, leaving any *one* data source unprotected (gradients, activations or parameters) would ¹⁸² already compromise label privacy. However, we found that gradients and activations require different ¹⁸³ means of protection.

¹⁸⁴ 3.3 Privacy-preserving backpropagation

 In this section, we formulate an algorithm for "anonymizing" the gradients communicated over a single training step with arbitrary PEFT type. Several prior works approach this by modifying the training objective or model architecture. However, when dealing with a real-world PEFT workload with optimized hyperparameters, changing the model or loss function often results in reduced model 189 accuracy^{[4](#page-4-2)}. Thus, we seek an algorithm that preserves both model and training objective.

¹⁹⁰ We design our algorithm based on an observation that backpropagation is conditionally lin-191 ear in output gradients, even when the model itself is nonlinear. Formally, if we take a model 192 $h(·, ·)$, a fixed set of trainable parameters θ and input samples x, the backprop function^{[5](#page-4-3)} computes 193 backprop $(x, \theta, \frac{\partial L}{\partial h(x, \theta)}) = \frac{\partial L}{\partial \theta}$. For convenience, we shorten it to backprop $(x, \theta, g_h) = g_\theta$, where 194 $g_h = \frac{\partial L}{\partial h(x,\theta)}$ represents the gradients of some objective function with respect to model activations 195 (outputs), and $g_{\theta} = \frac{\partial L}{\partial \theta}$ are gradients of the same objective function w.r.t. trainable parameters. In 196 this notation, backprop is linear in terms of g_h for any fixed x, θ .

197 This becomes self-evident if we view backprop as multiplying g_h by the Jacobian of model outputs 198 w.r.t. trainable parameters, $\frac{\partial h(x,\theta)}{\partial \theta}$. If x, θ are constant, the Jacobian is also constant, and backprop ¹⁹⁹ is a linear operator:

$$
\text{backprop}(x,\theta,\frac{\partial L}{\partial h(x,\theta)}) = \frac{\partial L}{\partial \theta} = \frac{\partial L}{\partial h(x,\theta)} \times \frac{\partial h(x,\theta)}{\partial \theta}.
$$
 (1)

²⁰⁰ This observation allows us to design a private backpropagation protocol. To illustrate ²⁰¹ this protocol, let us first consider a distributed API with two identical independent servers 202 that offer backprop API. Then, for arbitrary vector z, we can rewrite backprop (x, θ, g_h) as 203 backprop (x, θ, g_h+z) +backprop (x, θ, g_h-z) .

204 During API fine-tuning, we obtain backprop $(x, \theta, g_h + z)$ using an API call to server 1, whereas the 205 second term backprop $(x, \theta, g_h - z)$ translates to an API call to server 2. Note that neither of two 206 servers has access to the true gradient g_h : they only receive the sum $[g_h + z]$. If we sample a large 207 noise vector $z(\text{Var}(z)) \gg ||g_h||_2^2$, this sum also becomes dominated by noise. However, when both ²⁰⁸ API calls finish, a client can sum the results to recover the true gradient of the loss with respect to ²⁰⁹ parameters.

210 If both requests are processed by the same server, it can obviously recover g_h by adding up gradients ²¹¹ from both calls, which leads us to the final step. Instead of generating a single noise vector, a client

 3 The missing bit corresponds to attacker not knowing which cluster corresponds to label "1".

⁴We validate this empirically in [4.2.](#page-7-0)

⁵This is the same as the backprop API defined in Section [3.1.](#page-2-0)

212 needs to generate (privately) a set of $m > 1$ random vectors $\hat{g}_h^1, \dots, \hat{g}_h^m$ and scalars $\alpha_1, \dots, \alpha_m$ such ²¹³ that

$$
g_h = \sum_{i=1}^m \alpha_i \cdot \hat{g}_h^i.
$$
 (2)

214 Then, for each \hat{g}_h^i , client computes backprop (x, θ, \hat{g}_h^i) as m parallel API calls. Once this is done, ²¹⁵ client recovers

$$
g_{\theta} = \sum_{i=1}^{m} \alpha_i \cdot \text{backprop}(x, \theta, \hat{g}_h^i).
$$
 (3)

216 Note that the client does not reveal $\alpha_1, \ldots, \alpha_m$ to anyone.

 The resulting procedure is formulated in Algorithm [1.](#page-5-1) This algorithm is conceptually similar to the secure aggregation protocol for conventional (horizontal) federated learning [\[1\]](#page-9-9). This protocol allows clients to average their local vector with peers while keeping each individual vector provably private. Similarly to our scheme, clients perturb the vector in such a way that the average of perturbed vectors remains the same. Unlike Bonawitz et al. [\[1\]](#page-9-9), our protocol privately backpropagates through a server-hosted model by leveraging the conditional linearity of the backpropagation operator.

1: **Input:** x inputs, θ adapter weights, g_h gradients w.r.t. activations, $m > 1$ - number of passes
2: $\hat{a}_h^1, \ldots, \hat{a}_k^m, \alpha_1, \ldots, \alpha_m = \text{obfuscate}(a_h, m)$ [2](#page-5-2): $\hat{g}_h^1, \ldots, \hat{g}_h^m, \alpha_1, \ldots, \alpha_m = \text{obfuscate}(g_h, m)$ \triangleright 2 3: for $j = 1, \ldots, m$ do 4: $\hat{g}_{\theta}^{j} = \text{backprop}(x, \theta, \hat{g}_{h}^{j})$
5: **end for**) ▷ computed by server 6: $g_{\theta} = \sum_{j=1}^{m} \alpha_j \cdot \hat{g}_{\theta}^j$ 7: **Return:** g_{θ}

²²³ The private backpropagation algorithm can allow client to safely compute gradients *once*, but, in ²²⁴ practice, client usually needs to run many consecutive steps. This creates an additional vector of 225 attack: if the same server receives two sets of parameters θ_t , θ_{t+1} , they could potentially recover g_θ

²²⁶ by inverting the optimizer.

227 In the simplest case, if the server somehow knows that the client computes $\theta_{t+1} = \theta_t - \eta \cdot g_\theta$, then 228 they can compute $g_{\theta} = (\theta_t - \theta_{t+1})/\eta$. While g_{θ} does not necessarily leak private labels, a server 229 could, in some cases, use g_{θ} to recover g_h , either fully (e.g. if Jacobian is invertible), or partially.

 The client has two ways to prevent this attack. The first one is to ensure that no single server runs backprop on two consecutive steps. This is easy to do in decentralized systems where there are many potential servers. However, even when there is a single server, they could be required to set up multiple trusted execution environments [\[25\]](#page-10-12). A more risky alternative is to ensure that the gradients cannot be reversed from consecutive parameters: randomize initial optimizer statistics or add noise to parameters. This solution is easier, but it can slow down training in some cases.

 To summarize, we formulated a procedure that allows a client to compute gradients privately for any given model and PEFT type. Furthermore, since Equation [3](#page-5-3) recovers true gradients, this obfuscation method does not affect the training dynamics. However, as we have shown in Section [3.1,](#page-2-0) gradients are not the only source of privacy leakage.

²⁴⁰ 3.4 Full fine-tuning

 The other major attack vector are training activations. As the model fits to training data, it's 242 intermediate activations $h(x, \theta)$ allow attackers to recover labels, e.g. by clustering (see Figure [1\)](#page-3-2). To combat this issue, we take advantage of the fact that PEFT has few trainable parameters. Instead 244 of learning just one set of trainable parameters, a client creates n independent adapter sets $\theta_1, ..., \theta_n$. 245 Note that this does not require n unique servers: a single server can run multiple sets of adapters. Furthermore, a client can alternate between using different servers for the same adapters. During forward pass, the outputs of different adapters are mixed together using randomized mixing weights $W \in \mathcal{R}^{\tilde{n},d}$:

$$
h'(x, \theta_1, \dots, \theta_n) = \sum_{i=1}^n W_i \odot h(x, \theta_i)
$$
 (4)

²⁴⁹ Overall, we design this model in such a way the combined model h' can predict the labels, but the 251 adapters $h(x, \theta_i)$ do not allow predicting these labels without knowing the mixing weights W. The 252 mixing weights are generated such that initial activations $h'(x, \ldots)$ are equal to mean $h(x, \cdot)$ for all 253 x. To achieve this, we generate W as follows: first, we generate $n \cdot (n-1)/2$ d-dimensional random 254 vectors $\xi_{i,j} \in \mathcal{R}^d \forall i \in [1, n], j \in [i + 1, n]$. Then, we add them up in the following way:

$$
W = \begin{pmatrix} \frac{1}{n}e + \xi_{1,2} + \xi_{1,3} + \dots + \xi_{1,n} \\ -\xi_{1,2} + \frac{1}{n}e + \xi_{2,3} + \dots + \xi_{2,n} \\ \dots \\ -\xi_{1,n} - \xi_{2,n} - \xi_{3,n} - \dots + \frac{1}{n}e \end{pmatrix}
$$
(5)

²⁵⁵ Here, e stands for a vector of all ones. The purpose of these mixing weights is to ensure that the 256 gradients w.r.t. individual $h(x, \theta_i)$ are obfuscated, but the averaged model behaves the same as 257 regular PEFT adapter. To illustrate this, consider $n=2$ identical LoRA adapters θ_1, θ_2 . During the 258 first training step $h(x, \theta_1) = h(x, \theta_2)$. Therefore,

$$
h'(x, \theta_1, \dots, \theta_n) = (1/2e + \xi_{1,2}) \odot h(x, \theta_1) + (1/2e - \xi_{1,2}) \odot h(x, \theta_2) = h(x, \theta_1) \tag{6}
$$

²⁵⁹ However, the two adapters will learn different functions as they receive different gradients. From the 260 first update on, h' will be equal to an average of adapter predictions.

261 Finally, to ensure that individual adapters $h(x, \theta)$ do not accidentally "learn to leak" labels, we ²⁶² maintain this over the course of training with a privacy regularizer inspired by [\[9\]](#page-9-10). This ensures that 263 it is impossible to predict labels from individual adapters $h(x, \theta_i)$. Intuitively, on each training step, 264 client fits n linear "heads" that learn to predict labels y from $h(x, \theta_i)$, then performs an adversarial 265 update of θ_i to prevent the "head" from predicting y. Formally, each of n "heads" minimize the same ²⁶⁶ objective function as the full model. For instance, if the full model solves multi-class classification, ²⁶⁷ each head is trained to minimize cross-entropy:

$$
\eta_i^* = \underset{\eta_i}{\text{arg min}} \sum_{x, y \in D} -y \cdot \log \frac{e^{\langle \eta_{ij}, h(x, \theta_i) \rangle}}{\sum_k e^{\langle \eta_{ik}, h(x, \theta_i) \rangle}}, \tag{7}
$$

268

²⁶⁹ where y is one-hot encoding of the correct class.

270 The whole adversarial update takes place locally on client's side, using the same $h(x, \theta)$ it uses for the ²⁷¹ main training objective. The resulting procedure appears complicated but it typically takes negligible 272 time compared to running the large pre-trainied model $h(x, \theta)$. Furthermore, since adversarial "heads" ²⁷³ are linear, minimizing the objective above is done with standard logistic regression solver.

 To summarize, our approach combines the two proposed ideas: we use the private backpropagation algorithm from Section [3.3](#page-4-0) to protect the gradients, then trains a mixture of adapters in such a way that obfuscates learned activatons leaking labels. The resulting procedure is described in Algorithm [2.](#page-13-1) In the next section, we will evaluate the efficacy of $P³EFT$ on popular NLP benchmarks.

²⁷⁸ 4 Experiments

 The main goal of our study is to find a practical method of private fine-tuning that would scale to large models. Because our approach leverages parameter-efficient fine-tuning techniques, we evaluate P³ EFT with fine-tuning Transformer models on popular NLP benchmarks that these techniques were designed for.

²⁸³ To that end, we chose three pre-trained models: DeBERTa-XXLarge [\[13\]](#page-9-2), Flan-T5-Large [\[4\]](#page-9-3) and ²⁸⁴ LLaMA-2 7B [\[35\]](#page-11-2). We train these models on several datasets from the GLUE benchmark [\[39\]](#page-11-12): ²⁸⁵ SST-2 [\[32\]](#page-11-11), MNLI [\[41\]](#page-11-13) and QNLI.

²⁸⁶ 4.1 Privacy of gradients and activations

²⁸⁷ For this experiment, we train DeBERTa-XXLarge on SST-2 dataset using LoRA adapters with ²⁸⁸ hyperparameters from [\[15\]](#page-10-3). First, we train the model locally and track model activations h and ²⁸⁹ gradients w.r.t. those activations. We apply principal component analysis to them and plot the first

Figure 3: Gradients of cross-entropy w.r.t. LoRA parameters for DeBERTa-v2-XXLarge. The top row corresponds to normal backpropagation and the bottom row uses privacy-preserving backprop.

2 dimensions in Figure [1.](#page-3-2) Similarly, we visualize gradients of individual per-sample loss functions

291 w.r.t. LoRA parameters θ in Figure [3](#page-7-1) (top row). The results suggest that a hypothetical attacker could easily recover private labels by performing K-Means clustering over any data source: activations, gradients with respect to activations, or individual gradients with respect to parameters.

 Next, we run the same experiment using privacy-preserving backpropagation as defined in Section [3.3.](#page-4-0) 295 We use $n = 2$ with the noise variance set to 1000. As expected, we observed the same learning curve as with normal training. However, instead of sending gradients w.r.t. activations to the server, a client uses specially crafted random noise vectors that are not informative. In Figure [3](#page-7-1) (bottom) we plot the same kind of individual gradients as in the top row, except that we visualize the gradients computed by the first of the two servers. Finally, we train XGBoost [\[3\]](#page-9-11) with default hyperparameters to predict labels given the noisy gradients (pre-PCA): the resulting classifier is able to fit the training data perfectly, but has at most 50.4% accuracy on a balanced test set.

4.2 Main fine-tuning experiments

 Next, we evaluated the entire P3EFT algorithm. To control tasks and model type, we examined DeBERTa and Flan-T5 across all four datasets mentioned above, in addition to evaluating LLaMA on SST2 and QNLI datasets. For each setup, we compare against three baselines:

306 • Without LoRAs. In this baseline, the client gathers h activations at the beginning (with no adapters), then proceeds to train local "head" layers using these activations. This method cannot leak information about training labels except for what is stored in X.

- 309 Regular fine-tuning (Regular FT) refers to training a single LoRA adapter normally. This baseline represents an upper bound on model accuracy, but lacks privacy.
- 311 Distance Correlation (DC). Our re-implementation of the distance correlation defense formulated in [\[33\]](#page-11-14) for Transformer models.
- For each algorithm, we evaluated a task-specific metric (accuracy or F1), as well as the privacy leakage value for the 3 following measures:
- 315 Spectral attack AUC a measure of vulnerability to an attack proposed in [\[33\]](#page-11-14), measured as classifier ROC AUC: lower value corresponds to better privacy.
- $317 \cdot \text{Norm}$ attack AUC vulnerability to a variant of attack proposed in [\[18\]](#page-10-8), measured as classifier ROC AUC (lower is better). Despite the initial proposal of this approach for attacking gradients, we observed that it is also well-suited for attacking activations.
- **K-means accuracy** vulnerability to clusterization attack, measured in the percentage of correctly clustered activations, lower is better.

 For all setups, we report the worst (least private) value among these metrics throughout the entire training period as a measure of privacy leakage, because it is the worst possible scenario that matters from the client's perspective. For DC and $P³$ EFT, we specify the values for the best configuration in terms of the utility-privacy trade-off. See details in Appendix [A.](#page-12-3) We also report adjusted standard 326 deviations for the two privacy aware algorithms: $P^3E\overrightarrow{FT}$ and DC. To do so, we run the full training procedure from scratch with 3 random seeds.

DeBERTa XXLarge.					Flan-T5-Large.					
Dataset		Without Regular DC LoRAs FT DC		P^3EFT	Dataset			Without Regular LoRAs FT DC		P^3EFT
SST2 $_{leak}^{acc}$ 82.9		96.9 99.1		$96.6_{\pm 0.4}$ $96.5_{\pm 0.2}$ $93.3_{+6.8}$ 62.6 _{+2.6}	$SST2$ $\begin{matrix} acc & 92.8 \\ leak & 55.8 \end{matrix}$			96.1 98.3		$95.0_{\pm 0.1}$ $96.1_{\pm 0.1}$ $68.1_{+5.0}$ 74.1 _{+3.0}
QNLI $_{leak}^{acc}$ 72.6		96.0 99.1		$95.8_{\pm 0.3}$ $95.6_{\pm 0.5}$ $85.0_{\pm 11.6}$ 74.6 \pm 11.1	QNLI $_{leak}^{acc}$ 83.2			95.3 98.9	$67.0_{+1.2}$ $63.0_{+0.8}$	$95.2_{\pm 0.1}$ $94.7_{\pm 0.0}$
MNLI $_{leak}^{acc}$ 49.2		91.9 91.5	$\overline{}$	$86.9{\scriptstyle \pm 0.5}$ 37.4 ${\scriptstyle \pm 0.7}$	MNLI acc 73.9 leak 34.6			90.5 85.9	89.8 \pm 0.1 90.1 \pm 0.1 $45.6_{+0.8}$ $40.0_{+1.1}$	

Table 1: Accuracy and privacy metrics.

Table 2: Accuracy and privacy metrics.

 The results for DeBERTa are presented in Table [1.](#page-8-0) To improve reproducibility, we reuse the hyperpa- rameters from original paper, with the exception of the LoRA dropout value. We disable dropout because it interferes with the mixing weights [\(5\)](#page-6-1). In preliminary experiments, we observed that with dropout enabled, both our algorithm and DC begin to perform significantly worse.

332 We use $n = 2$ adapter sets for P³EFT for all datasets and adhered to the same approach for the 333 other models as well. Overall, P³FT achieves nearly the same accuracy as traditional (non-private) fine-tuning, outperforming the DC-based algorithm in terms of accuracy given the same privacy level. On the MNLI dataset, we could not find the hyperparameters for DC that ensure stable training while maintaining privacy. Meanwhile, $P³EFT$ maintains consistent performance on this task with a slight drop in quality.

³³⁸ Table [2](#page-8-0) a reports evaluation for the Flan-T5 base model[\[4\]](#page-9-3). For this model, we adapt the exact same

³³⁹ hyperparameters as in the previous evaluation with DeBERTa-XXLarge. Compared to DeBERTa, ³⁴⁰ these results are more closely matched. Both both our algorothm and DC consistently solve all three

 1341 tasks, but P³EFT slightly outperforms DC in terms of privacy.

Dataset		Without Regular LoRAs FT		DC	P^3EFT	
SST ₂	acc	94.6	97.4	97.1 $_{\pm 0.1}$	$95.8_{\pm 0.1}$	
	leak	59.1	99.3	$83.6{\scriptstyle \pm10.6}$	$68.9{\scriptstyle \pm2.6}$	
QNLI	acc	77.0	95.0	$95.2_{+0.1}$	$94.7_{\pm 0.2}$	
	leak	53.3	85.5	$66.6 + 4.1$	$62.9_{+0.8}$	

Table 3: Accuracy and privacy metrics for LLaMA-2 7B.

 To evaluate how our algorithm scales to larger models, we also fine-tune Llama-2 7B [\[35\]](#page-11-2) on SST2 [\[32\]](#page-11-11) and QNLI [\[39\]](#page-11-12) datasets. For these evaluations, we use LoRA hyperparameters that Hu et al. [\[15\]](#page-10-3) used when fine-tuning GPT-3, with several changes inspired by Dettmers et al. [\[5\]](#page-9-12). Namely, we use the NF4 weight format, apply LoRA to both attention and MLP layers with rank 16. We fine-tune both tasks with maximum context length of 512 and weight decay 0.01. Table [3](#page-8-1) summarizes 347 our results: for QNLI, P³EFT achieves somewhat better privacy-accuracy trade-off. On SST2, P³EFT shows similarly favorable trade-offs while DC struggles to preserve privacy.

³⁴⁹ 5 Conclusion and Discussion

 In this work, we analyze privacy-preserving fine-tuning of large neural networks in the context of parameter-efficient fine-tuning and the two-party split learning setting. We show that while standard fine-tuning suffers from label leakage even in the parameter-efficient case, it is possible to leverage the efficiency of PEFT to alter the procedure without any significant performance drawbacks. We test the resulting method, named $P³EFT$, on a range of pretrained language models and multiple datasets, showing that it is competitive with a strong baseline in terms of label privacy while having higher task performance.

 In future work, it is natural to explore how this approach can be extended to establish holistic privacy in both labels and inputs. This problem can be approached from two directions: either adapt the 359 ideas of P³EFT for input privacy, or combine it with an existing work like [\[22\]](#page-10-7). Another important direction for future research is exploring the privacy of the long-term client-provider interaction. In a typical real-world use case of API fine-tuning, a client performs multiple training runs on overlapping data and hyperparameters. This could open additional attacks vectors that combine information from multiple training runs.

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A Hyperparameters search

In P³EFT and Distance Correlation methods resulting loss L function can be viewed in the form

$$
L = L_m + \alpha \cdot L_r,
$$

525 where L_m - main task loss, L_r - regularizer and α is a coefficient that controls the tradeoff between these two losses. The selection of this coefficient affects the final performance of the model. Therefore, to find the best configurations for both methods, we iterated through this hyperparameter using a grid search.

529 We started with $\alpha = 1$ and then altered it with a multiplicative step of $10^{\frac{1}{2}}$. Values were discarded if the quality did not exceed that achieved by solely training the classifier without LoRA. This criterion was adopted because such outcomes would suggest the method's inability to outperform training scenarios in which the server does not engage with the labels whatsoever. Additionally, we excluded values that led to unstable training. By this, we mean instances where, although the model initially trained on the primary task, at some point, the regularizer began contributing significantly more, and the utility value dropped to the starting value. We observed this issue for the DC method with DeBERTa on the MNLI. From the remaining values, we aimed to choose the one that offered the 537 lowest privacy leakage. The final hyperparameter values for P³EFT can be found in the Table [4](#page-12-4) and for DC in the Table [5.](#page-12-5)

Table 4: Regularization parameter α for the P³EFT method. The values in the table represent powers of the $10^{\frac{1}{2}}$.

Table 5: Regularization parameter α for the DC method. The values in the table represent powers of the $10^{\frac{1}{2}}$.

⁵³⁹ B Formal algorithm definition

540 Below, we define the full P³EFT algorithm. In Algorithm [2,](#page-13-1) main_loss is the task-specific objective ⁵⁴¹ e.g. cross-entropy; reg_loss is the adversarial regularizer described in Section [3.4.](#page-5-0) We denote 542 client-side model "head" as $f(h, \psi^t)$, where ψ represent trainable head parameters. Finally, opt_step ⁵⁴³ function performs a single gradient descent step with a task-specific optimizer, typically Adam [\[17\]](#page-10-13).

Algorithm $2P^3EFT$ - full training algorithm

1: **Input:** dataset $D = \{X, Y\}$, $n > 1$ number of adapters, $\alpha \ge 0$ - regularizing weight, $m > 1$ number of obfuscated gradients 2: Initialize head ψ^0 , mixing weights W_i and adapters θ_i^0 , $i = \overline{1,n}$ 3: for $t = 0, 1, \ldots, T - 1$ do 4: Sample batch $\{x^t, y^t\}$ 5: **for** $i = 1, ..., n$ **do** 6: $h_i^t = h(x^t, \theta_i^t)$) ▷ by server 7: $l_i = \text{reg_loss}(h_i^t, y^t)$ 8: end for \triangleright by client 9: $h' = \sum_{i=1}^{n} W_i \odot h_i^t$
10: $l = \text{main_loss}(f(h', \psi^t), y^t)$ 11: $L = l + \alpha \cdot \sum_{i=1}^{n} l_i$ 12: **for** $i = 1, ..., n$ **do** 13: $g_h = \frac{\partial L}{\partial h_i^t}$

14: $g_i^t = \text{private_backprop}(x, \theta_i^t, g_h, m)$

15: $\theta_i^{t+1} = \text{opt_step}(\theta_i^t, g_i^t, t)$ ▷ Client performs partial backprop $14:$ $15:$ 16: end for $17:$ $t+1 = \text{opt_step}(\psi^t, \partial l / \partial \psi^t, t)$ 18: end for 19: **Return:** $\psi^T, \theta_1^T, \ldots, \theta_M^T$

⁵⁴⁴ C Informal description of LoRA fine-tuning

 For convenience, we provide a brief summary of fine-tuning with LoRA [\[15\]](#page-10-3). This PEFT method was originally designed for fine-tuning large pre-trained language models on downstream NLP tasks. These language models are typically based on the Transformer architecture [\[36\]](#page-11-15), where most trainable parameters are allocated to linear layers in multi-head self-attention and feedforward blocks.

⁵⁴⁹ In the first stage of LoRA fine-tuning, user augments the model with adapters. To do so, a user goes ⁵⁵⁰ over linear layers in transformer blocks and adds two trainable matrices, A and B that affect this 551 layer's forward pass. Let $W_i \times x + b_i$ be the original layer with n inputs and m hidden units. Here, 552 $W_i \in \mathcal{R}^{m \times n}$ is a pre-trained weight matrix, $b_i \in \mathcal{R}^m$ is a pre-trained intercept vector and $x \in \mathcal{R}^n$ ⁵⁵³ represents a vector of inputs to this particular layer. During the forward pass, a layer with LoRA 554 adapter computes $W_i \times x + b_i + B_i \times A_i \times x$, or equivalently, $(W_i + B \times A) \times x + b_i$. Here, A_i 555 and B_i are two newly added matrices that constitute a LoRA adapter.

556 The adapter matrices $A \in \mathbb{R}^{r \times n}$ and $B \in \mathbb{R}^{m \times r}$ have a very small intermediate dimension r. For 557 instance, when training GPT-3 with LoRA adapters, authors use $1 \le r \le 64$, whereas the main 558 weight dimensions are $m = n = 12288$. The first matrix A is initialized with small random normal 559 values, and the second matrix B is initialized at zeros. That way, initial A and B do not affect the ⁵⁶⁰ model predictions.

561 Once all adapters are initilized, the user trains all A_i and B_i matrices of the model, while keeping ⁵⁶² the rest of the weights frozen. This way, only a small faction (less than 1%) of model weights are 563 updated. Once the training is over, the learned adapters A_i and B_i can be merged into the main 564 weights $(W_i := W_i + A_i \times B_i)$ or used separately.

⁵⁶⁵ LoRA adapters are designed with two objectives in mind: i) to allow fine-tuning models in limited ⁵⁶⁶ GPU memory and ii) to allow inferencing many fine-tuned models using one inference server. When ⁵⁶⁷ fine-tuning, LoRA achieves small memory footprint due to the fact that user does not need to compute gradients (or optimizer statistics) for billions of main model parameters. During inference, a server can keep a library of several adapters for different tasks and swap between them on demand.

D Informal description of LoRA fine-tuning

We used NVIDIA A100 GPUs for all the experiments. Experiments with DeBERTA [\[13\]](#page-9-2) and Flan-T5

[\[4\]](#page-9-3) on SST2 [\[32\]](#page-11-11) were conducted on the single GPU, while experiments on MNLI [\[41\]](#page-11-13) and QNLI

require 4 A100. LLaMA-2 [\[35\]](#page-11-2) expetiments were carried out on the node of 8 A100.

All the experiments last 12-24 hours. However, it is possible to speed up some of them using more

 GPUs, as well as conduct them on a smaller number of GPUs using technics to save GPU memory (see parameters in our code).

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Answer: [NA]

