

000 BEYOND BENCHMARKS: UNDERSTANDING 001 002 MIXTURE-OF-EXPERTS MODELS THROUGH INTER- 003 004 NAL MECHANISMS

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006 **Anonymous authors**
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ABSTRACT

013 Mixture-of-Experts (MoE) architectures have emerged as a promising direction,
014 offering efficiency and scalability by activating only a subset of parameters during
015 inference. However, current research remains largely performance-centric, with
016 limited understanding of its internal mechanisms, thereby constraining broader
017 progress. In this work, we use an internal metric to investigate the mechanisms of
018 MoE architecture by explicitly incorporating routing mechanisms and analyzing
019 expert-level behaviors. Through systematic analyses of a wide range of publicly
020 available MoE models, we uncover several findings: (1) neuron utilization de-
021 creases as models evolve, reflecting stronger generalization; (2) training exhibits
022 a dynamic trajectory, where benchmark performance alone provides limited signal
023 while MUI reveals deeper insights; (3) task completion emerges from collabora-
024 tive contributions of multiple experts, with shared experts driving concentration;
025 and (4) activation patterns at the neuron level provide a fine-grained proxy for
026 data diversity. Together, these results demonstrate the potential of MUI as a com-
027 plementary indicator to benchmark performance, offering new insights into the
028 capacity, dynamics, and specialization of MoE models.

029 1 INTRODUCTION

030 With the rapid advancement of Large Language Models (LLMs), an increasing number of Mixture-
031 032 of-Experts (MoE) architectures have been proposed, such as DeepSeek (Liu et al., 2024), GPT-
033 OSS (OpenAI, 2025), and Qwen3 (Yang et al., 2025). Unlike dense models that rely on fixed
034 forward parameters, MoE models employ dynamic routing, selectively activating different subsets
035 of parameters known as experts. This design offers two key advantages: 1) both training and in-
036 ference are more efficient, as only a small fraction of parameters are activated for each input; and
037 2) performance can be improved, one common explanation is that, under the same computational
038 budget, MoE models can be scaled to much larger parameter sizes. However, are these advantages
039 the only reason behind MoE’s success? Our current understanding of MoE architectures remains
040 limited, and this lack of interpretability poses challenges for their further development.

041 From these perspectives, it is essential to investigate the mechanisms of MoE architectures. Current
042 research primarily focuses on benchmark performance for understanding, but benchmark perfor-
043 mance alone is insufficient. As LLMs increasingly saturate widely used benchmarks, the perfor-
044 mance differences across models become marginal, while potential benchmark leakage (Zhou et al.,
045 2023; Ying et al., 2024a) further undermines the reliability of these results. In this work, we use an
046 internal metric to investigate the mechanisms of MoE architectures, extending the Model Utilization
047 Index (MUI) originally proposed on dense models Cao et al. (2025), which measures the proportion
048 of neurons required for task completion. However, unlike dense models, MoE requires explicitly
049 accounting for routing mechanisms when evaluating the degree to which a model utilizes its internal
050 capacity. Moreover, it is equally important to enable fine-grained investigations at the expert level
051 in order to better understand the functional roles and contributions of individual experts. Through
052 systematic analyses of a wide range of publicly available MoE models, and by tracing how internal
053 mechanisms evolve as model capabilities change, we not only demonstrate the applicability of our
adapted indicators but also conduct in-depth analyses at the expert-level. Based on these analyses,
we uncover several findings and provide the following key insights:

054 1. Reduced neuron utilization with model evolution: within the same family, we observe that as
 055 models evolve, their performance improves while requiring fewer neurons to accomplish the
 056 same tasks. We believe this is a reflection of stronger generalization. Notably, GPT-OSS models
 057 exhibit strikingly low MUI, which may explain why GPT-5 achieve superior performance in
 058 real-world applications — strong generalization (Section 3.2).
 059

060 2. Dynamic MUI trajectory during training: by tracking how MUI evolves throughout the training
 061 process, we provide insights beyond performance metrics, showing how MUI can serve as an
 062 indicator for monitoring training dynamics and guiding model development (Section 3.3).
 063

064 3. Collaborative expert contributions: task completion often emerges from the joint collaboration of
 065 multiple experts. Stronger models exhibit a higher proportion of expert cooperation, with GPT-
 066 OSS showing the highest. Interestingly, the presence of shared experts further drives expert con-
 067 centration, potentially diminishing the diversity advantages of distributed experts (Section 3.4).
 068

069 4. Data measurement: activation patterns at both the neuron and expert levels reflect data diversity,
 070 while neuron-level offering a more efficient way (Section 3.5).
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070 2 MOE MODEL UTILIZATION INDEX 071

072 To address limitations in performance-only evaluation, we propose designing internal indicators that
 073 monitor MoE models from the perspective of underlying mechanisms. Building on recent advances
 074 in interpretability, which have shown how model components, such as neurons and layers, interact
 075 to produce overall behavior (Pan et al., 2024; Cao et al., 2025), we extend this line of inquiry to
 076 MoE architectures. Specially, we focus on identifying the proportion of key neurons required for
 077 task completion, and study how this proportion evolves during capability shifts and across training
 078 iterations. These dynamics form the basis of a meaningful measure for model monitoring, which we
 079 term the MoE-MUI (MUI for simple). To this end, we first introduce the neuron importance calcu-
 080 lation method primarily used in our study in the following section. It is important to note that our
 081 proposed metric is not tied to any specific interpretation method. To ensure robustness, we further
 082 consider several alternative formulations, which are detailed in our ablation studies (Section 4).
 083

084 2.1 PRELIMINARY

085 Neuron-level interpretable methods (Dai et al., 2022a; Geva et al., 2021) connect individual neurons
 086 in the feed-forward network (FFN) sub-layer of LLMs to specific semantic meanings. These neurons
 087 can be treated as mediator variables (Meng et al., 2022) for certain model behaviors. In MoE models,
 088 each expert \mathbf{E}_i corresponds to one FFN. Specifically, omitting the layer normalization for brevity,
 089 the MoE layer l can be defined as a function of input hidden state \mathbf{x}^l :

$$091 \text{MoE}^l(\mathbf{x}^l) = \sum_{i \in \mathcal{R}(\mathbf{x}^l)} \mathbf{G}_i^l(\mathbf{x}^l) \mathbf{E}_i^l(\mathbf{x}^l) + \sum_{s \in \mathcal{S}} \mathbf{G}_s^l(\mathbf{x}^l) \mathbf{E}_s^l(\mathbf{x}^l), \quad (1)$$

$$092 \mathbf{E}_i^l(\mathbf{x}^l) = (\mathbf{x}^l \mathbf{W}_{u,i}^l \odot (\mathbf{x}^l \mathbf{W}_{g,i}^l)) \mathbf{W}_{d,i}^l,$$

$$093$$

094 where $\mathcal{R}(\mathbf{x}^l)$ is the routed (top- k) expert set, \mathcal{S} is the shared expert set, $\mathbf{G}_i^l(\mathbf{x}^l)$ are routing weights
 095 (for shared experts, set $\mathbf{G}_s^l(\mathbf{x}^l) \equiv 1$ if they are always active), and $\mathbf{W}_{u,i}^l$, $\mathbf{W}_{g,i}^l$, $\mathbf{W}_{d,i}^l$ are the projec-
 096 tions in SwiGLU. Following (nostalgia, 2020), for j -th neuron in expert i at layer l contributing
 097 to prediction of token \hat{y} when given input sequence x , we define the token-level neuron contribution:
 098

$$100 f_{\text{neuron}}(i, j, l, \hat{y} | x) = \left(\mathbf{G}_i^l(\mathbf{x}^l) \cdot (\mathbf{x}^l \mathbf{W}_{g,i}^l) \cdot \mathbf{W}_{d,i}^l \right) [j] \cdot \mathbf{W}_{\text{head}}[:, \hat{y}], \quad (2)$$

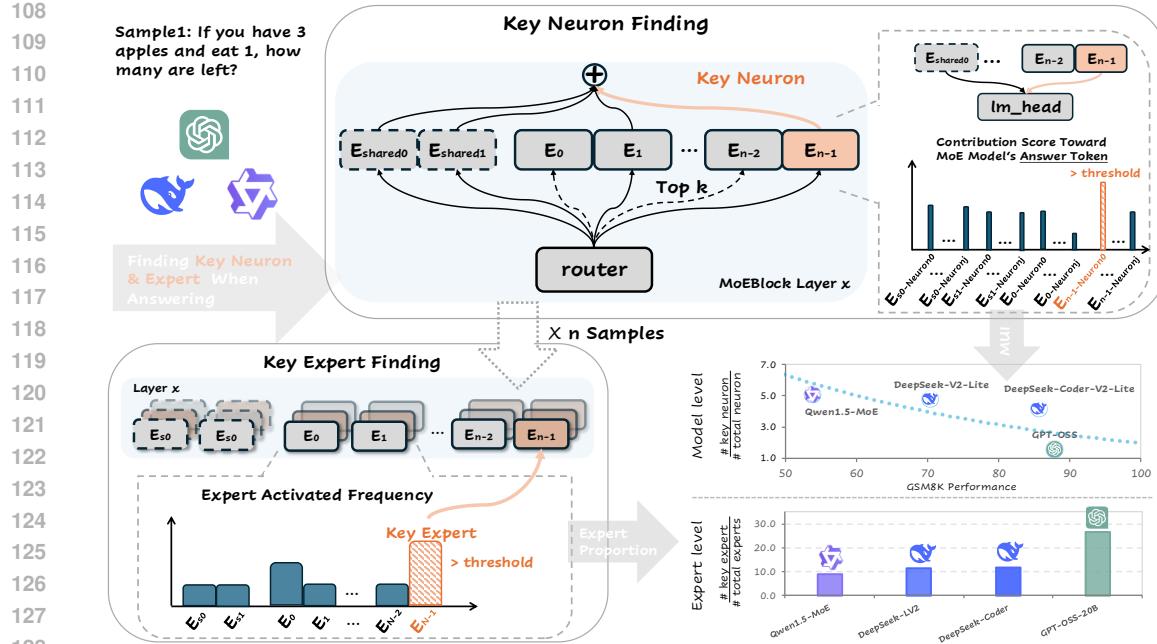
$$101$$

102 where \mathbf{W}_{head} is the unembedding matrix mapping hidden states to vocabulary logits. For a given
 103 threshold η , the key activated neurons for task sample $s = (x, y)$ is defined as:

$$104 N_{\text{activated}}(s) = \left\{ (i, j, l) \mid \exists \hat{y}_t, f_{\text{neuron}}(i, j, l, \hat{y}_t | x \oplus \hat{y}_{<t}) > \eta \right\}, \quad (3)$$

$$105$$

106 where \hat{y}_t denotes the t -th token in y , $\hat{y}_{<t}$ denotes the partial output sequence before the t -th token,
 107 and \oplus represents concatenation with the input sequence.

Figure 1: Illustration of getting key neurons and key experts for given task samples (s_1 to s_n).

2.2 MODEL UTILIZATION INDEX

Given a task set $\mathcal{T} = \{s_1, s_2, \dots, s_k\}$, we first identify the set of key activated neurons for each sample s_i using Equation 2. By accumulating across all samples, we obtain the union of neurons required to complete the task. The neuron-level MUI for MoE is then defined as the proportion of activated neurons relative to the total available neurons in the model:

$$\text{MUI}(\mathcal{T}) = \frac{|\bigcup N_{\text{activated}}(s_i)|}{N \times L \times (|E_s| + |E_r|)}, \quad (4)$$

where N is the number of neurons per expert, L is the number of MoE layers, $|E_s|$ is the number of shared experts, and $|E_r|$ is the number of routed experts per layer. Correspondingly, if we focus only on the expert information contained in the activated neuron set we can identify the experts set $E_{\text{activated}}(s) = \{(i, l) \mid \exists j, (i, j, l) \in N_{\text{activated}}(s)\}$ that are responsible for sample s . Given a frequency threshold η_{expert} , we could find the set of key experts for a task set \mathcal{T} as those experts that consistently contribute across samples:

$$E_{\text{key}}(\mathcal{T}) = \left\{ (i, l) \mid \frac{|\{s \in \mathcal{T} \mid (i, l) \in N_{\text{activated}}(s)\}|}{|\mathcal{T}|} \geq \eta_{\text{expert}} \right\}. \quad (5)$$

Meanwhile, by aggregating the sets of task-responsible experts, we can derive both the overall proportion of key experts within the model as well as the MUI for each individual expert. Formally, the proportion of key experts for a given task \mathcal{T} is defined as:

$$\text{KeyExpertProportion}(\mathcal{T}) = \frac{|\bigcup E_{\text{key}}(\mathcal{T})|}{L \times (|E_s| + |E_r|)} \quad (6)$$

In addition, for a specific expert (i', l') , its MUI with respect to task \mathcal{T} is computed as:

$$\text{MUI}_{(i', l')}(\mathcal{T}) = \frac{|\bigcup \{j \mid (i', j, l') \in N_{\text{activated}}(s)\}|}{N} \quad (7)$$

Figure 1 provides an illustration of our methodology. Starting from a given sample (e.g., sample 1), we identify the key neurons that contribute to the model's response during inference. By aggregating results from multiple samples, we can identify the corresponding task-level experts (shown in red).

162 **3 EXPERIMENTS**
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164 In this section, we present our empirical study on a broad set of open-source MoE models. Specifi-
 165 cally, we conduct interpretability-based analyses on 13 publicly available models ranging from 20B
 166 to 200B parameters, as well as 10 intermediate checkpoints from the OLMoE series. By monitoring
 167 how the MUI changes alongside changes in model capabilities, we aim to reveal the potential of
 168 MUI as an internal indicator of model capacity. Furthermore, we demonstrate how MUI enables
 169 fine-grained expert-level analysis, offering insights into the internal dynamics of MoE architectures.
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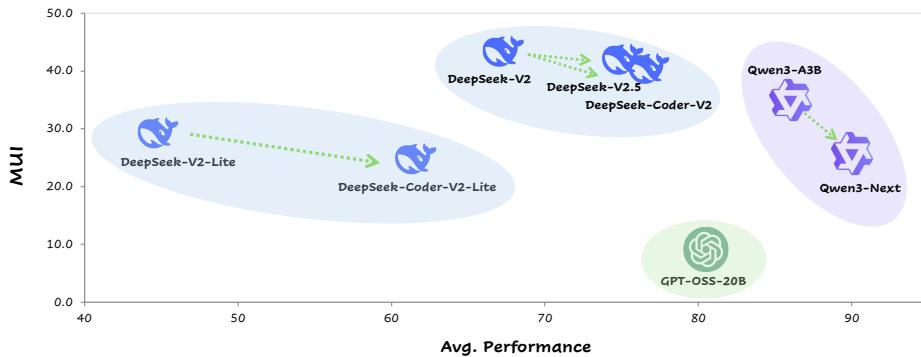
171 **3.1 SETUP**
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173 **Dataset Selection.** To ensure reliable conclusions, we adopt a diverse set of widely used bench-
 174 marks. Following (Cao et al., 2025; Ying et al., 2024b), our evaluation covers three categories: 1)
 175 GSM8K (Cobbe et al., 2021), MATH (Hendrycks et al., 2021), and ARC-Challenge (Clark et al.,
 176 2018) for math reasoning, 2) HumaEval (Chen et al., 2021) and MBPP (Austin et al., 2021) for
 177 coding, 3) BIG-bench Hard (BBH) (bench authors, 2023) and MMLU (Hendrycks et al., 2020) to
 178 cover general tasks. Statistical result for the selected benchmarks is shown in Table 2.

179 **Model Selection.** To maximize the applicability of MUI and ensure fairness in evaluation, we
 180 select four widely used series of open-source LLMs: 1) GPT Series: GPT-OSS-20B and GPT-OSS-
 181 120B (OpenAI, 2025). 2) Qwen Series: Qwen1.5-MoE (Team, 2024), Qwen3-30B, Qwen3-Coder-
 182 30B, Qwen3-235B-Thinking (Yang et al., 2025), and Qwen3-Next. 3) DeepSeek Series: DeepSeek-
 183 MoE (Dai et al., 2024), DeepSeek-V2-Lite (abbreviated as DeepSeek-LV2), DeepSeek-Coder-V2-
 184 Lite, DeepSeek-V2, and DeepSeek-Coder-V2 (et al., 2024). 4) OLMoE Series: several checkpoints
 185 from OLMoE-7B (et al., 2025); detailed checkpoint information is provided in Appendix A.2.

186 **Implementation.** Details of the response generation parameters for each model are provided in the
 187 Appendix. For the threshold η in Equation 3, we set it to the top 1% of total neurons, applied at the
 188 layer level (additional implementation details are reported in the Appendix A.3). Furthermore, we
 189 discuss the neuron selection strategy and justify the choice of threshold in our Section 4.

190 **3.2 REDUCED NEURON UTILIZATION WITH MODEL EVOLUTION**
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204 Figure 2: Overall weighted-average performance (%) and MUI (%) across selected benchmarks.
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206 By comparing earlier and later versions within the same model families, we examine how MUI
 207 reflects the impact of model iteration or evolution. Specifically, within the DeepSeek family, we
 208 compare DeepSeek-V2 and DeepSeek-V2-Lite with their enhanced counterparts, DeepSeek-Coder-
 209 V2/DeepSeek-V2.5 and DeepSeek-Coder-V2-Lite. Although labeled as “Coder” versions, model
 210 reports (Zhu et al., 2024) and benchmark results indicate that these are a comprehensive evolution
 211 of the V2 series (MUI changes under specific capabilities improvement will be discussed in Sec-
 212 tion 3.3). Similarly, in the Qwen family, we compare Qwen3-30B-A3B with its iterative successor,
 213 Qwen3-Next. The performance and corresponding MUI values (Equation 4) for these models are
 214 shown in Figure 2. Analyzing all neurons jointly, we observe that later-released models consistently
 215 achieve stronger performance on the same datasets while exhibiting lower MUI. If we assume that
 these newer models indeed possess higher true capability and stronger generalization (i.e., the ability

216 to handle a broader range of tasks beyond the specific evaluation sets), then MUI may serve as an
 217 indicator of intrinsic capacity and generalization rather than benchmark-specific performance. This
 218 interpretation is supported by two pieces of evidence. First, prior work on dense models Cao et al.
 219 (2025) reached a similar conclusion, showing that lower MUI correlates with stronger generaliza-
 220 tion (Cao et al., 2025). Second, Team (2023) found that with increased training data, parameters
 221 become more specialized even in a single ReLU output model, while generalization simultaneously
 222 improves. Notably, GPT-OSS exhibits strikingly low MUI, which may explain why the GPT series
 223 provides consistently strong user experience in real-world — superior generalization capability.

MUI as an Indicator

Combining performance with MUI offers an indicator of a model’s underlying generalization capability, mitigating the risks of misleading evaluations caused by leakage.

3.3 DYNAMIC MUI TRAJECTORY DURING TRAINING

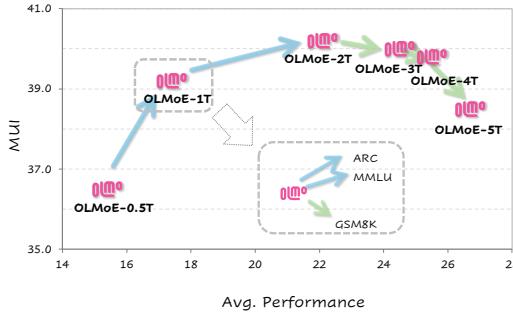


Figure 3: MUI (%) and Performance (%) change across OLMoE checkpoints trained with 0.5T, 1T, 2T, 3T, 4T and 5T tokens on the select 7 benchmarks.

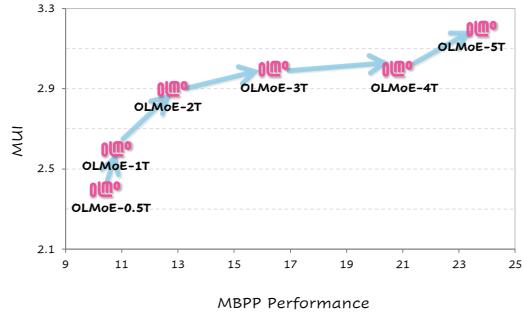


Figure 4: MUI (%) and Performance (%) change across OLMoE checkpoints trained with 0.5T, 1T, 2T, 3T, 4T and 5T tokens on the benchmark MBPP.

Previous results indicate that later-stage models achieve lower MUI alongside improved performance. However, an important question remains: does MUI decrease monotonically throughout training, or do different phases exhibit distinct trajectories? To address this, we monitor MUI for the fully open-source OLMoE models across the entire training process, with the goal of deriving insights that can inform training strategies and model development. Figure 3 plots the overall performance across seven selected tasks alongside the corresponding MUI values for each checkpoint, with more detailed statistics reported in Table 5. The results reveal a two-phase trajectory in training. At earlier stages, performance improvements are accompanied by an increase in MUI, which we refer to as the “**Accumulating**” phase. In this phase, the model appears to recruit a larger set of neurons for memorization and learning (Team, 2023). This trend also emerges when models undergo capability-specific improvements. For example, compared to DeepSeek-V2, DeepSeek-Coder-V2 places greater emphasis on coding ability. As a result (Table 4), its MUI increases on coding tasks such as MBPP (from 4.9 to 6.3) and HumanEval (from 2.7 to 3.3).

At later stages, however, further performance gains occur together with a decrease in MUI, which we call the “**Evolving**” phase. This suggests that with continued exposure to more data, the model transitions toward more efficient utilization. As indicated by our earlier analysis in Section 3.2, such efficiency is closely associated with improved generalization. Importantly, this dynamic learning trajectory is not uniform across all capabilities but results from a mixture of ability-specific trends. For instance, as shown in Figure 3, after training on 1T tokens, OLMoE-1T exhibits an Evolving trend on GSM8K, whereas ARC and MMLU continue to follow the Accumulating trajectory. These heterogeneous ability-specific patterns collectively determine whether the model’s overall trajectory appears Accumulating or Evolving at the aggregate level. Thus, we summarize our takeaway as:

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271**Takeaway: MUI Moniting MoE Training**272
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Monitoring performance alone is insufficient; MUI provides a complementary perspective for performance for detecting divergent trajectories and adjusting training accordingly. For example, as shown in Figure 4, in coding tasks such as MBPP, OLMoE consistently remains in the **Accumulating** phase without entering the **Evolving** phase. This suggests that additional coding data, or a higher proportion of coding tasks during earlier training stages, may be required to help the model further improve its generalization ability.

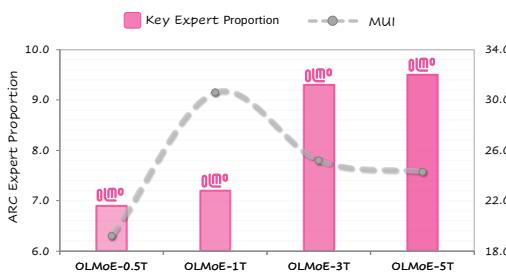
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282**3.4 COLLABORATIVE EXPERT CONTRIBUTIONS**283
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Figure 5: Proportion of key experts for the ARC task and the corresponding MUI within those key experts across the OLMoE series.

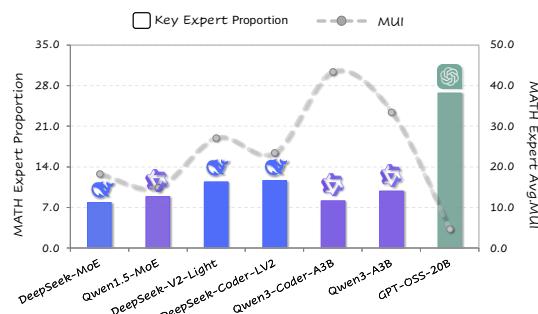


Figure 6: Proportion of key experts for the Task task and the corresponding MUI within those key experts across the selected MoE models.

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After establishing the potential of neuron-level activation as an indicator of model capacity, we now extend our analysis to the expert level. Specifically, following Equation 5, we examine how experts contribute to completing the task. For a given task, the distribution of activated experts can be viewed as a probability distribution over the expert set. To quantify expert contributions, we adopt a frequency threshold of $\eta_{\text{expert}} = 0.6$ to identify key experts that only with consistently involved. While detailed activation distributions for each benchmark are presented in Figures 12 through 16. Considering that different architectures employ varying numbers of experts, we focus here on models within the same architecture family for comparison. As shown in Figure 5, 1). OLMoE exhibits an increasing proportion of key experts (Equation 6) as training progresses (solid bar), with more consistent results reported in Table 6 through Table 9. With GPT-OSS consistently demonstrates the highest proportion of key experts among the models studied. 2). At the same time, the MUI within these key experts (Equation 7) shows a trajectory that first rises and then falls. That is, during early training, the model recruits a large number of neurons (reflected by increasing MUI). As training progresses, specialization emerges, potentially consolidated within experts, leading to a compression phase where MUI decreases. At the same time, having a broader set of experts in “Collaboration”, results in stronger overall performance and improved generalization. This suggests that for MoE models, **activating a larger number of experts while requiring fewer neurons within each expert is often associated with stronger true capability and better generalization**. This observation is consistent with the pattern shown in Figure 6, where GPT-OSS exhibits a markedly different trajectory from other models — aligning well with our hypothesis above.

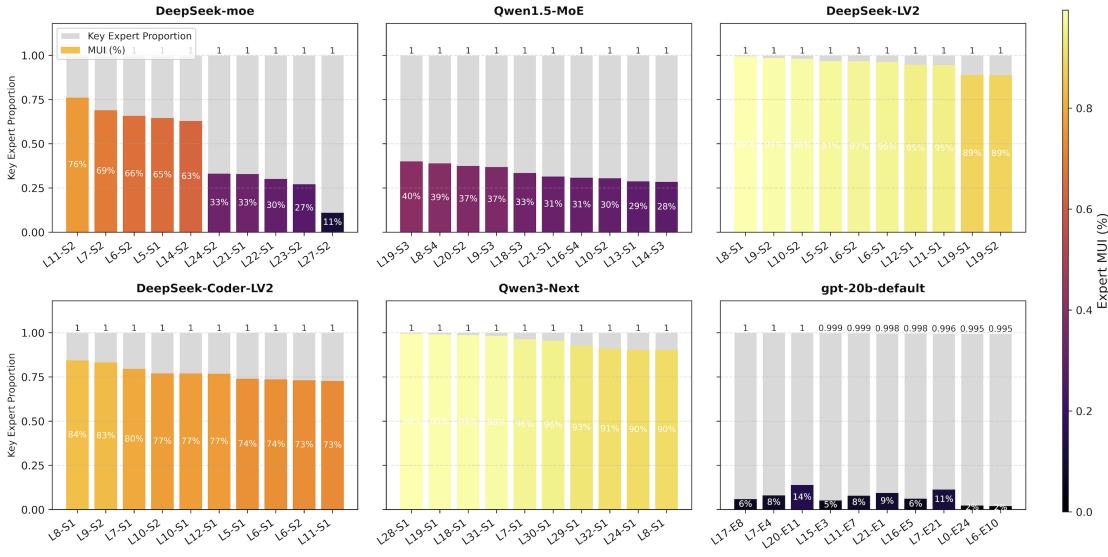
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After analyzing the overall trend of expert utilization, we further analyze the distribution of key experts, particularly in light of architectural differences between shared and routed experts. As shown in Figure 7, we present the results on the MMLU dataset, with additional results provided in Appendix B.3. For MoE architectures that include shared experts, the findings reveal that the top-10 most frequently activated experts are exclusively shared experts. Moreover, the utilization rate of these shared experts is extremely high; for instance, in Qwen3-Next, each shared expert is activated in more than 90% of the cases. By contrast, in GPT-OSS, a routed-only MoE, the activation rate is extremely low. Considering the training dynamics of the two types of experts — shared experts

324 being persistently active versus routed experts only being activated when selected by the router —
 325 this implicates how experts emerge differently across MoE architectures:
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327 Expert “Collaboration” in MoE

329 Though exhibiting an increasing trend of expert “collaborative” during training. In models
 330 having shared experts, their persistent activation leads to concentrated responsibility within
 331 the shared pool, whereas in routed-only architectures, the influence of load-balancing losses
 332 drives a more dispersed “many-hands” collaboration among a broader set of experts.



353 Figure 7: Top-10 experts (ranked by activation frequency in Equation 5) for the selected MoE models
 354 with shared-expert structures (the exception GPT-OSS-20B model is included for comparison) on
 355 MMLU. The corresponding MUI for each expert is reported. Shared experts are denoted as S_i .

356 Given that the proportion of shared experts is relatively small, **task-responsible experts tend to**
 357 **be disproportionately concentrated within the shared pool.** To test this hypothesis, we examine
 358 whether shared experts are enriched in the intersection of per-task key experts. Specifically, we
 359 evaluate three benchmarks from different domains and report in Table 1. Fisher’s exact tests reveal
 360 highly significant enrichment, with odds ratios ranging over 54.6 and two-sided p -values from 10^{-29}
 361 to 10^{-57} . This indicates that shared experts are not only frequently activated within individual
 362 tasks but also disproportionately dominate the set of experts consistently activated across multiple
 363 tasks. In other words, shared experts act as common capacity hubs that concentrate responsibility
 364 across tasks, confirming our hypothesis that training tends to centralize task responsibility within this
 365 subset. Notably, Qwen3-Next shows the lowest proportion of key experts, which can be attributed to
 366 its architecture containing the smallest shared-expert ratio (1 out of 513 experts). This concentration
 367 has a dual implication. On the one hand, shared experts provide “capacity hubs” that can enable
 368 efficient cross-task knowledge transfer. On the other hand, such reliance risks over-centralization,
 369 potentially limiting expert specialization and reducing the effective diversity of the expert pool.

| Task | DeepSeek-MoE | Qwen1.5-MoE | DeepSeek-V2-Lite | DeepSeek-Coder-LV2 | Qwen3-Next |
|---------------------|--------------|-------------|------------------|--------------------|------------|
| GSM8K | 8.3 / 35.6 | 10.2 / 57.1 | 11.9 / 25.4 | 14.1 / 21.5 | 2.8 / 7.0 |
| GSM8K + MBPP | 4.8 / 61.4 | 6.6 / 82.3 | 5.9 / 51.5 | 7.9 / 38.5 | 0.6 / 31.3 |
| GSM8K + MBPP + MMLU | 3.5 / 84.4 | 6.0 / 90.3 | 3.3 / 91.2 | 5.8 / 52.0 | 0.4 / 49.0 |

374 Table 1: Key experts proportion(%) / proportion of shared experts among key experts(%).

375
 376 In summary, although the feed-forward networks in MoE architectures are referred to as “Experts,”
 377 it is difficult in practice to interpret them as independent task-specific units, whether in routed-
 378 only designs or in ones that also include shared experts. In routed-only architectures, the presence

of load-balancing losses prevents learning from consistently concentrating on specific experts, and continued training instead yields experts with sparse and diffuse specialization. As a result, it is difficult to establish a stable union of task-responsible experts that could facilitate further analysis. In architectures with shared experts, task responsibility tends to converge largely within the shared pool, leading to substantial overlap in the experts activated across different tasks. In some sense, this behavior resembles that of dense models, but it also risks undermining the diversity benefits that multiple experts are expected to provide.

3.5 DATA MEASUREMENT

Since the activation of different neurons or experts corresponds to engaging distinct regions of the model’s internal capacity, these activation patterns can be leveraged as an internal proxy for measuring the diversity of input data. To illustrate this, we conduct experiments by randomly sampling data from the three selected domains. In addition, considering the potential influence of reasoning length, we divide each domain into two subsets: the top 50% longest samples (denoted as long) and the remaining shorter samples (denoted as short). The results in Figure 8 and Figure 25 indicate: 1) both the neuron-level MUI and the proportion of activated experts ($\eta_{expert} = 0$) are positively correlated with data diversity, and this correlation remains robust regardless of input length.

This confirms the validity of our case-level, rather than token-level, measurement strategy, as MUI is not artificially inflated by longer reasoning chains; 2) compared to neurons, expert-level activation yields much higher ratios (typically above 90%) due to the larger parameter scale. As a result, the expert-level activation rate saturates and is less suitable for measuring diversity across datasets. In contrast, neuron-level MUI offers finer granularity and efficiency: 600 samples spanning from three domains have comparable MUI to 900 samples from a single domain.

4 ABLATION STUDY

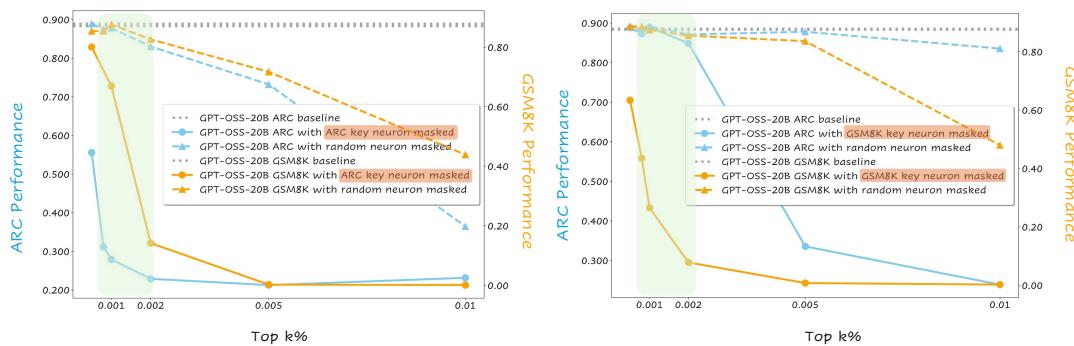


Figure 9: Performance (ACC%) of the Llama-3-8B-Instruction model on the **ARC** and **GSM8K** datasets, with key neurons masked specifically for ARC and GSM8K. Key neurons are identified using Equation 3 and a layer-level top-k threshold function (detailed in Appendix A.3). The threshold value used for our MUI analysis —1%, is visually indicated by a green box.

The previous experiments have demonstrated both the effectiveness and the insightfulness of our proposed methodology. However, one potential concern is the validity of the identified neurons, particularly regarding the choice of thresholds in Equation 3. To address this, we employ neuron masking, a widely used intervention technique in mechanistic interpretability, to verify whether the selected neurons bear a causal relationship to the model’s output. Here, we mask the neurons identified on ARC and GSM8K under different threshold values (to eliminate the confounding effect of

432 varying model shape, we adopt percentage-based thresholds rather than absolute counts). Ideally,
 433 the more task-relevant key neurons are masked, the more pronounced the resulting performance
 434 degradation should be. The result for GPT-OSS in Figure 9 (other shown in Figure 26) confirms
 435 our selection: The results, shown for GPT-OSS in Figure 9 (with additional results in Figure 26),
 436 confirm this expectation. First, masking neurons identified by either ARC or GSM8K produce a
 437 steady decline in performance as more neurons are removed, with a much sharper drop than under
 438 random masking. This effect is especially pronounced when k lies in the range of 0.1% — 0.2% of
 439 neurons. Second, masking neurons derived from ARC using k in the same interval significantly re-
 440 duces performance on both ARC and GSM8K. In contrast, masking neurons derived from GSM8K
 441 has little impact on ARC performance. This arises because ARC spans a broader set of abilities
 442 beyond mathematical reasoning, whereas GSM8K primarily focuses on arithmetic reasoning. These
 443 findings further demonstrate the validity of our neuron selection approach, and our chosen thresh-
 444 old evidently falls within this interval, enabling us to identify task-critical neurons in a principled
 445 manner. In addition to the 0.1% threshold reported in the main paper, we also experiment with alter-
 446 native thresholds, which have consistent results (Appendix C). For completeness, we further evaluate
 447 alternative importance scoring methods, and due to space constraints, we report in Appendix C.
 448

5 RELATED WORK

450 Recent years have seen a resurgence of MoE (Cai et al., 2025; Dai et al., 2024; Jiang et al., 2024),
 451 whose core idea is to activate only a few experts per token. To stabilize training and improve spe-
 452 cialization, DeepSeekMoE introduces always-on shared experts (Dai et al., 2024), a design later
 453 integrated into DeepSeek-V2 (et al., 2024) and DeepSeek-V3 (Liu et al., 2024) and adopted in sub-
 454 sequent systems such as Qwen3-Next (Yang et al., 2025). Meanwhile, a line of work analyzes and
 455 improves expert specialization and load balancing. StableMoE proposes a two-stage training strat-
 456 egy with router distillation to reduce routing volatility and stabilize convergence (Dai et al., 2022b).
 457 Expert-Choice Routing instead lets experts select tokens rather than tokens selecting experts, which
 458 leads to better load balancing (Zhou et al., 2022). To address the issue of experts collapsing into sim-
 459 ilar behaviors, OLMoE introduces orthogonalization and diversity-promoting regularization (et al.,
 460 2025). On the balancing side, new approaches remove the dependence on auxiliary losses (Wang
 461 et al., 2024). Beyond optimization, some works (Xue et al., 2024) conduct token-level analyses of
 462 expert. However, there is still a lack of comprehensive and in-depth analysis of MoE models.
 463

6 DISCUSSION

464 This work represents an attempt to employ interpretability methods as tools for MoE model un-
 465 derstanding and evaluation. Through extensive experiments, we demonstrate the promise and the
 466 practical utility of the MUI. Nonetheless, interpretability remains an evolving field, and several
 467 limitations of our study should be acknowledged. 1) while we observe clear internal transitions to-
 468 ward the Evolving phase across model iterations, establishing a direct and quantitative link between
 469 MUI & performance and generalization remains challenging. 2) our implementation is grounded
 470 in neuron-based interpretability techniques. Though we tested alternative formulations, the broader
 471 interpretability community continues to debate best practices and methodologies. As interpretability
 472 tools evolve, MUI itself should be revisited and refined.
 473

7 CONCLUSION

474 In this work, we move beyond benchmark-centric evaluations and provide a deep analysis of MoE
 475 models through the lens of internal utilization patterns. Our systematic investigations further high-
 476 light that stronger models not only achieve higher performance but also have reduced neuron utili-
 477 zation, and more collaborative expert behaviors. These findings indicate MUI with performance
 478 serves as an indicator of both training progress and generalization strength, providing a new diagno-
 479 stic tool for model development. Expert-level analyses demonstrate that MoE functionality emerges
 480 from collective expert interactions rather than isolated contributions. Further analysis shared experts
 481 showing how their dominance centralizes task responsibility. We hope these results will encourage
 482 future work to build on internal utilization analyses as a complementary perspective for understand-
 483 ing, improving, and controlling MoE architectures.
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648 **A EXPERIMENT DETAILS**
649650 **A.1 DATASET STATISTICAL RESULT**
651652 Following (Cao et al., 2025; Ying et al., 2024b), we focus on three representative abilities: Mathe-
653 matical and Reasoning, Coding, and General Capability. For each ability, we select a set of publicly
654 available datasets to evaluate. To balance computational cost and coverage, we sample from large-
655 scale benchmarks such as BBH (bench authors, 2023) and MMLU (Hendrycks et al., 2020), while
656 ensuring evaluation quality by following the sampling protocol in (Wang et al., 2025). A detailed
657 summary of the statistical characteristics of the selected datasets is provided in Table 2.
658

| Model | GSM8K (Math & Reasoning) | MATH (Math & Reasoning) | ARC _c (Math & Reasoning) | HumanEval (Code) | MBPP (Code) | BBH (General) | MMLU (General) | Totally |
|-------------------|-----------------------------|----------------------------|--|---------------------|----------------|------------------|-------------------|---------|
| # Testing Samples | 1,319 | 5,000 | 1,172 | 164 | 500 | 2,000 | 4,000 | 14,155 |

662 Table 2: The statistical detail of the selected benchmarks.
663664 **A.2 OLMOE SERIES MODEL SELECTION**
665666 For OLMoE (et al., 2025) series model, we include eight checkpoints detailed in Table 3.
667

| Custom Checkpoint Name | Original Checkpoint Name | Training Steps | Training Tokens |
|------------------------|--------------------------|----------------|-----------------|
| OLMoE-0.5T | step120000-tokens503B | 120,000 | 503B |
| OLMoE-1T | step245000-tokens1027B | 245,000 | 1,027B |
| OLMoE-1.5T | step365000-tokens1530B | 365,000 | 1,530B |
| OLMoE-2T | step490000-tokens2055B | 490,000 | 2,055B |
| OLMoE-2.5T | step610000-tokens2558B | 610,000 | 2,558B |
| OLMoE-3T | step735000-tokens3082B | 735,000 | 3,082B |
| OLMoE-3.5T | step855000-tokens3586B | 855,000 | 3,586B |
| OLMoE-4T | step975000-tokens4089B | 975,000 | 4,089B |
| OLMoE-4.5T | step1100000-tokens4613B | 1,100,000 | 4,613B |
| OLMoE-5T | step1200000-tokens5033B | 1,200,000 | 5,033B |

679 Table 3: Summary of the checkpoints of OLMoE used in the study. “Custom Checkpoint Name”
680 represents simplified names defined in this paper for clarity.
681682 **A.3 MECHANISTIC INTERPRETABILITY TECHNIQUES**
683684 For the neuron contribution score, we primarily adopt one of the most commonly used methods, as
685 described in Section 2, for time and computational cost considerations. Nevertheless, our approach
686 is not confined to a single interpretation technique. Our objective is to explore MUI under multiple
687 perspectives to ensure comprehensive conclusions. As detailed in our ablation study (Section 4), we
688 also experiment with alternative neuron analysis methods to further validate our findings.
689690 When applying the method defined in Section 2, the response y_t in Equation 3 is generated under
691 benchmark-specific conditions. For BBH, we use the original 3-shot setting. For all other benchmarks,
692 instruction-tuned models are evaluated in a zero-shot setting, while OLMoE models, being
693 base models, are evaluated with a one-shot prompt. Detailed configurations of model generation,
694 along with the few-shot examples, are provided in Appendix A.5.
695696 The threshold η in Equation 3 is set to the top 1% of neurons per layer (corresponding to the top
697 1% of N), thereby selecting the most salient neurons at each layer level. This threshold function is
698 detailed as follows:
699

700
$$N_{\text{activated}}(s) = \left\{ (i, j, l) \mid \exists \hat{y}_t, f_{\text{neuron}}(i, j, l, \hat{y}_t \mid x \oplus \hat{y}_{<t}) \geq V_l^{\text{top1\%}} \right\}, \quad (8)$$

701

702 where $V_l = [f_{\text{neuron}}(i, j, l, \hat{y}_t \mid x \oplus \hat{y}_{<t}) \mid i \in \{1, 2, \dots, n\}, j \in \{1, 2, \dots, |E|\}, i \in \{1, 2, \dots, N\}]$,
703 with N representing the number of neurons in the tested model, n representing the length for
704 response y , and $|E|$ representing the number total experts.
705

702 A.4 IMPLEMENTATION FOR ALTERNATIVE NEURON IMPORTANCE DEFINITIONS
703

704 In addition to the contribution-based method described in the main text, we also explored several
705 alternative definitions of neuron importance. These implementations include threshold-based func-
706 tions as well as other heuristic approaches for quantifying neuron contribution. Here we are also
707 considering directly using the activation score (Marked as activate):

$$709 f_{\text{neuron}_{\text{activate}}}(i, j, l, \hat{y} | x) = \left(\mathbf{G}_i^l(\mathbf{x}^l) \cdot (\mathbf{W}_{u,i}^l \odot (\mathbf{x}^l \mathbf{W}_{g,i}^l)) \right) [j], \quad (9)$$

710 where $\mathbf{G}_i^l(\mathbf{x}^l)$ are routing weights (for shared experts, set $\mathbf{G}_s^l(\mathbf{x}^l) \equiv 1$ if they are always active),
711 and $\mathbf{W}_{u,i}^l, \mathbf{W}_{g,i}^l, \mathbf{W}_{d,i}^l$ are the projections in SwiGLU. Moreover, in architectures that only employ
712 a single up-projection and down-projection without a gating mechanism, the output directly maps to
713 the vocabulary space (nostalgia, 2020). We adapt this formulation to the MoE setting:

$$716 f_{\text{neuron}_{\text{glu}}}(i, j, l, \hat{y} | x) = \left(\mathbf{G}_i^l(\mathbf{x}^l) \cdot (\mathbf{W}_{u,i}^l \odot (\mathbf{x}^l \mathbf{W}_{g,i}^l)) \cdot \mathbf{W}_{d,i}^l \right) [j] \cdot \mathbf{W}_{\text{head}}[:, \hat{y}], \quad (10)$$

718 A.5 MODEL PARAMETER SETTING
719

720
721 **Response Generation.** All models are evaluated with a fixed decoding temperature of 0.0. For non-
722 reasoning models, the maximum output length is set to 1,024 tokens, while for reasoning-oriented
723 models we follow their default maximum lengths: 16,384 tokens for Qwen3-235B and 131,072
724 tokens for the GPT series. For computational efficiency, we use the default reasoning effort setting,
725 which we found to perform comparably, or in some cases, better than the “high” setting.

726 **Benchmark Conditions.** Generation settings vary depending on the benchmark. For BBH, we
727 adopt the standard 3-shot prompts provided in the benchmark. For all other benchmarks, responses
728 are generated in a zero-shot manner for instruction-tuned models, while OLMoE series models are
729 evaluated under a human-crafted one-shot setting, following Cao et al. (2025).

730 All experiments are conducted on 32 NVIDIA H2000 GPUs, totaling approximately 1,536 GPU
731 hours for the interpretation experiment.

734 B MORE EXPERIMENT RESULTS
735736 B.1 MODEL PERFORMANCE AND MUI
737

| 739 Model | GSM8K (Math & Reasoning) | MATH (Math & Reasoning) | ARC _c (Math & Reasoning) | HumanEval (Code) | MBPP (Code) | BBH (General) | MMLU (General) |
|------------------------------|-----------------------------|----------------------------|--|---------------------|----------------|------------------|-------------------|
| 740 DeepSeek-MoE-A2.8 | 59.6 / 1.6 | 13.2 / 3.7 | 52.4 / 6.9 | 46.9 / 1.3 | 47.3 / 2.0 | 42.3 / 3.6 | 44.8 / 14.7 |
| 741 Qwen1.5-MoE-A2.7B | 53.8 / 5.1 | 17.4 / 7.1 | 70.0 / 10.3 | 46.3 / 1.4 | 42.7 / 2.2 | 35.5 / 5.8 | 54.9 / 23.1 |
| 742 DeepSeek-LV2-A2.4B | 70.4 / 4.8 | 23.1 / 7.7 | 69.2 / 10.5 | 50.0 / 1.7 | 48.3 / 2.9 | 49.4 / 5.5 | 53.4 / 23.1 |
| 743 DeepSeek-Coder-LV2-A2.4B | 85.7 / 4.2 | 56.4 / 8.3 | 69.5 / 8.5 | 72.6 / 1.8 | 64.9 / 3.4 | 63.8 / 6.0 | 55.9 / 18.5 |
| 744 Qwen3-Coder-A3B | 86.4 / 7.5 | 81.2 / 10.4 | 90.7 / 10.8 | 92.7 / 3.3 | 72.9 / 5.7 | 87.5 / 11.0 | 77.5 / 23.7 |
| 745 Qwen3-A3B | 90.0 / 7.2 | 90.7 / 11.5 | 93.3 / 12.0 | 92.7 / 3.4 | 74.9 / 5.7 | 90.5 / 10.5 | 81.6 / 26.1 |
| 746 Qwen3-Next | 93.6 / 5.6 | 92.0 / 9.1 | 92.5 / 10.3 | 94.5 / 2.0 | 80.8 / 3.6 | 93.3 / 7.8 | 84.7 / 25.7 |
| 747 GPT-OSS-A3.6B | 87.9 / 1.6 | 74.2 / 2.5 | 88.3 / 3.2 | 84.7 / 0.8 | 70.5 / 1.3 | 80.0 / 2.4 | 80.1 / 6.8 |
| 748 DeepSeek-V2-A21B | 91.2 / 6.3 | 43.5 / 13.2 | 90.8 / 15.9 | 76.8 / 2.7 | 64.3 / 5.3 | 80.7 / 8.7 | 75.4 / 35.4 |
| 749 DeepSeek-Coder-V2-A21B | 95.0 / 5.9 | 67.2 / 13.7 | 91.1 / 14.4 | 82.9 / 3.3 | 70.0 / 6.3 | 84.5 / 9.6 | 75.5 / 29.8 |
| 750 DeepSeek-V2.5-A21B | 91.4 / 6.6 | 64.5 / 12.2 | 88.4 / 15.4 | 84.8 / 2.6 | 67.1 / 4.9 | 85.6 / 8.9 | 75.2 / 33.8 |
| 751 Qwen3-A22B | 91.4 / 6.3 | 89.2 / 9.0 | 89.3 / 11.3 | 87.8 / 2.6 | 82.2 / 4.6 | 79.8 / 7.9 | 83.1 / 24.2 |
| 752 GPT-OSS-A5.1B | 85.7 / 4.4 | 75.9 / 6.6 | 88.9 / 8.0 | 81.1 / 1.7 | 70.1 / 2.8 | 78.0 / 6.0 | 84.5 / 17.2 |

753 Table 4: Performance (accuracy %) and MUI (%), as determined by neuron analysis (Equation 4)
754 with threshold top $k = 0.1\%$

| 756 | Model | GSM8K (Math & Reasoning) | MATH (Math & Reasoning) | ARC _c (Math & Reasoning) | HumanEval (Code) | MBPP (Code) | BBH (General) | MMLU (General) |
|-----|------------|-----------------------------|----------------------------|--|---------------------|----------------|------------------|-------------------|
| 758 | OLMoE-0.5T | 2.8 / 7.4 | 3.3 / 11.9 | 25.7 / 10.8 | 8.5 / 1.6 | 10.4 / 2.4 | 25.7 / 8.1 | 27.2 / 25.0 |
| 759 | OLMoE-1T | 3.6 / 10.5 | 3.2 / 12.9 | 33.6 / 15.3 | 6.1 / 1.6 | 10.8 / 2.6 | 25.3 / 8.3 | 32.2 / 26.3 |
| 760 | OLMoE-1.5T | 3.8 / 10.4 | 3.8 / 10.9 | 42.2 / 17.3 | 8.0 / 1.7 | 10.6 / 2.6 | 25.6 / 8.7 | 41.3 / 28.0 |
| 761 | OLMoE-2T | 4.4 / 7.9 | 4.1 / 12.5 | 47.7 / 15.9 | 8.0 / 1.8 | 12.8 / 2.9 | 27.7 / 9.2 | 42.1 / 27.9 |
| 762 | OLMoE-2.5T | 4.7 / 9.5 | 4.0 / 11.9 | 50.8 / 15.9 | 11.6 / 1.9 | 17.4 / 3.1 | 26.2 / 8.3 | 44.0 / 26.4 |
| 763 | OLMoE-3T | 6.4 / 10.1 | 4.2 / 10.6 | 53.8 / 15.9 | 8.0 / 1.8 | 16.4 / 3.0 | 29.5 / 8.6 | 46.3 / 28.1 |
| 764 | OLMoE-3.5T | 6.4 / 10.0 | 4.5 / 13.1 | 54.5 / 15.6 | 9.1 / 1.8 | 16.0 / 2.9 | 20.0 / 9.0 | 46.7 / 27.4 |
| 765 | OLMoE-4T | 5.0 / 9.2 | 4.6 / 11.8 | 57.6 / 16.0 | 11.0 / 1.9 | 20.8 / 3.0 | 30.7 / 8.6 | 47.5 / 28.2 |
| 766 | OLMoE-4.5T | 4.4 / 6.5 | 4.7 / 10.5 | 56.7 / 15.3 | 11.6 / 1.8 | 18.0 / 3.0 | 31.8 / 8.5 | 48.5 / 28.0 |
| 767 | OLMoE-5T | 6.0 / 6.2 | 4.9 / 10.7 | 60.5 / 15.2 | 14.6 / 2.0 | 23.8 / 3.2 | 30.2 / 8.5 | 50.1 / 28.0 |

Table 5: Performance (accuracy %) and MUI (%), as determined by neuron analysis (Equation 2) with top $k = 0.1\%$

B.2 EXPERT LEVEL ANALYZE RESULT

| 772 | Model | GSM8K (Math & Reasoning) | MATH (Math & Reasoning) | ARC _c (Math & Reasoning) | HumanEval (Code) | MBPP (Code) | BBH (General) | MMLU (General) |
|-----|--------------------------|-----------------------------|----------------------------|--|---------------------|----------------|------------------|-------------------|
| 774 | DeepSeek-MoE-A2.8 | 59.6 / 8.2 | 13.2 / 7.8 | 52.4 / 9.1 | 46.9 / 9.9 | 47.3 / 9.3 | 42.3 / 5.7 | 44.8 / 7.6 |
| 775 | Qwen1.5-MoE-A2.7B | 53.8 / 10.2 | 17.4 / 8.9 | 70.0 / 9.2 | 46.3 / 11.3 | 42.7 / 9.4 | 35.5 / 6.7 | 54.9 / 8.0 |
| 776 | DeepSeek-LV2-A2.4B | 70.4 / 11.9 | 23.1 / 11.4 | 69.2 / 6.4 | 50.0 / 14.5 | 48.3 / 13.5 | 49.4 / 6.4 | 53.4 / 4.7 |
| 777 | DeepSeek-Coder-LV2-A2.4B | 85.7 / 14.1 | 56.4 / 11.7 | 69.5 / 15.2 | 72.6 / 13.9 | 64.9 / 13.6 | 63.8 / 5.2 | 55.9 / 13.3 |
| 778 | Qwen3-Coder-A3B | 86.4 / 10.3 | 81.2 / 8.1 | 90.7 / 11.1 | 92.7 / 12.4 | 72.9 / 11.0 | 87.5 / 8.1 | 77.5 / 9.8 |
| 779 | Qwen3-A3B | 90.0 / 11.3 | 90.7 / 9.8 | 93.3 / 12.1 | 92.7 / 9.9 | 74.9 / 7.8 | 90.5 / 8.8 | 81.6 / 10.5 |
| 780 | Qwen3-Next | 93.6 / 2.8 | 92.0 / 2.2 | 92.5 / 2.6 | 94.5 / 2.4 | 80.8 / 2.0 | 93.3 / 1.5 | 84.7 / 1.9 |
| 781 | GPT-OSS-A3.6B | 87.9 / 31.4 | 74.2 / 26.7 | 88.3 / 33.2 | 84.7 / 39.6 | 70.5 / 37.8 | 80.0 / 29.4 | 80.1 / 28.5 |
| 782 | DeepSeek-V2-A21B | 91.2 / 5.9 | 43.5 / 6.9 | 90.8 / 5.3 | 76.8 / 9.8 | 64.3 / 8.9 | 80.7 / 4.3 | 75.4 / 4.9 |
| 783 | DeepSeek-Coder-V2-A21B | 95.0 / 10.2 | 67.2 / 8.0 | 91.1 / 2.8 | 82.9 / 9.2 | 70.0 / 8.7 | 84.5 / 4.0 | 75.5 / 2.7 |
| 784 | DeepSeek-V2.5-A21B | 91.4 / 8.4 | 64.5 / 7.8 | 88.4 / 5.7 | 84.8 / 11.5 | 67.1 / 10.8 | 85.6 / 4.2 | 75.2 / 5.0 |
| 785 | Qwen3-A22B | 91.4 / 16.9 | 89.2 / 16.4 | 89.3 / 15.6 | 87.8 / 17.4 | 82.2 / 17.1 | 79.8 / 15.5 | 83.1 / 14.3 |
| 786 | GPT-OSS-A5.1B | 85.7 / 24.2 | 75.9 / 21.5 | 88.9 / 25.2 | 81.1 / 34.2 | 70.1 / 33.4 | 78.0 / 22.7 | 84.5 / 22.8 |

Table 6: Performance (%) and corresponding task Expert proportion(%), with $\eta_{expert} = 0.6$.

| 787 | Model | GSM8K (Math & Reasoning) | MATH (Math & Reasoning) | ARC _c (Math & Reasoning) | HumanEval (Code) | MBPP (Code) | BBH (General) | MMLU (General) |
|-----|--------------------------|-----------------------------|----------------------------|--|---------------------|----------------|------------------|-------------------|
| 788 | DeepSeek-MoE-A2.8 | 59.6 / 8.9 | 13.2 / 18.3 | 52.4 / 21.9 | 46.9 / 6.8 | 47.3 / 9.5 | 42.3 / 18.9 | 44.8 / 31.9 |
| 789 | Qwen1.5-MoE-A2.7B | 53.8 / 11.2 | 17.4 / 15.0 | 70.0 / 21.8 | 46.3 / 4.3 | 42.7 / 5.5 | 35.5 / 12.6 | 54.9 / 36.5 |
| 790 | DeepSeek-LV2-A2.4B | 70.4 / 17.9 | 23.1 / 27.1 | 69.2 / 42.8 | 50.0 / 6.9 | 48.3 / 11.0 | 49.4 / 24.0 | 53.4 / 64.3 |
| 791 | DeepSeek-Coder-LV2-A2.4B | 85.7 / 12.5 | 56.4 / 23.6 | 69.5 / 25.8 | 72.6 / 6.6 | 64.9 / 10.1 | 63.8 / 29.3 | 55.9 / 38.6 |
| 792 | Qwen3-Coder-A3B | 86.4 / 29.9 | 81.2 / 43.6 | 90.7 / 36.8 | 92.7 / 13.3 | 72.9 / 20.2 | 87.5 / 34.4 | 77.5 / 50.8 |
| 793 | Qwen3-A3B | 90.0 / 22.4 | 90.7 / 33.6 | 93.3 / 31.3 | 92.7 / 15.1 | 74.9 / 22.4 | 90.5 / 27.0 | 81.6 / 44.4 |
| 794 | Qwen3-Next | 93.6 / 35.4 | 92.0 / 50.4 | 92.5 / 40.4 | 94.5 / 20.3 | 80.8 / 28.6 | 93.3 / 41.5 | 84.7 / 55.4 |
| 795 | GPT-OSS-A3.6B | 87.9 / 3.1 | 74.2 / 4.7 | 88.3 / 5.8 | 84.7 / 1.5 | 70.5 / 2.1 | 80.0 / 4.4 | 80.1 / 9.2 |
| 796 | DeepSeek-V2-A21B | 91.2 / 22.1 | 43.5 / 37.2 | 90.8 / 39.0 | 76.8 / 9.8 | 64.3 / 16.0 | 80.7 / 24.8 | 75.4 / 57.2 |
| 797 | DeepSeek-Coder-V2-A21B | 95.0 / 14.8 | 67.2 / 32.5 | 91.1 / 53.6 | 82.9 / 10.5 | 70.0 / 15.8 | 84.5 / 26.7 | 75.5 / 65.7 |
| 798 | DeepSeek-V2.5-A21B | 91.4 / 19.2 | 64.5 / 29.4 | 88.4 / 34.4 | 84.8 / 7.8 | 67.1 / 12.1 | 85.6 / 24.3 | 75.2 / 52.1 |
| 799 | Qwen3-A22B | 91.4 / 19.6 | 89.2 / 28.3 | 89.3 / 30.1 | 87.8 / 10.0 | 82.2 / 16.1 | 79.8 / 24.2 | 83.1 / 43.7 |
| 800 | GPT-OSS-A5.1B | 85.7 / 10.5 | 75.9 / 15.3 | 88.9 / 16.4 | 81.1 / 3.6 | 70.1 / 5.7 | 78.0 / 12.7 | 84.5 / 27.4 |

Table 7: Performance (accuracy %) and corresponding task Expert MUI(%) with $\eta_{expert} = 0.6$.

| 810 | Model | GSM8K (Math & Reasoning) | MATH (Math & Reasoning) | ARC _c (Math & Reasoning) | HumanEval (Code) | MBPP (Code) | BBH (General) | MMLU (General) |
|-----|------------|-----------------------------|----------------------------|--|---------------------|----------------|------------------|-------------------|
| 811 | OLMoE-0.5T | 2.8 / 6.9 | 3.3 / 8.2 | 25.7 / 14.2 | 8.5 / 10.7 | 10.4 / 11.6 | 25.7 / 11.5 | 27.2 / 11.2 |
| 812 | OLMoE-1T | 3.6 / 7.2 | 3.2 / 6.0 | 33.6 / 16.9 | 6.1 / 11.6 | 10.8 / 11.0 | 25.3 / 10.6 | 32.2 / 12.6 |
| 813 | OLMoE-1.5T | 3.8 / 8.5 | 3.8 / 7.0 | 42.2 / 12.1 | 8.0 / 11.0 | 10.6 / 10.9 | 25.6 / 11.5 | 41.3 / 11.4 |
| 814 | OLMoE-2T | 4.4 / 6.8 | 4.1 / 8.6 | 47.7 / 16.2 | 8.0 / 12.4 | 12.8 / 14.7 | 27.7 / 10.0 | 42.1 / 12.6 |
| 815 | OLMoE-2.5T | 4.7 / 7.4 | 4.0 / 8.0 | 50.8 / 14.6 | 11.6 / 12.1 | 17.4 / 13.5 | 26.2 / 11.9 | 44.0 / 11.5 |
| 816 | OLMoE-3T | 6.4 / 9.3 | 4.2 / 9.5 | 53.8 / 16.6 | 8.0 / 13.6 | 16.4 / 13.4 | 29.5 / 11.8 | 46.3 / 13.6 |
| 817 | OLMoE-3.5T | 6.4 / 9.3 | 4.5 / 6.3 | 54.5 / 17.0 | 9.1 / 13.9 | 16.0 / 14.6 | 20.0 / 7.5 | 46.7 / 14.2 |
| 818 | OLMoE-4T | 5.0 / 9.1 | 4.6 / 8.4 | 57.6 / 17.0 | 11.0 / 11.6 | 20.8 / 11.3 | 30.7 / 11.8 | 47.5 / 12.3 |
| 819 | OLMoE-4.5T | 4.4 / 9.7 | 4.7 / 8.2 | 56.7 / 15.7 | 11.6 / 13.5 | 18.0 / 12.8 | 31.8 / 11.0 | 48.5 / 12.0 |
| | OLMoE-5T | 6.0 / 9.5 | 4.9 / 7.8 | 60.5 / 16.2 | 14.6 / 13.2 | 23.8 / 14.2 | 30.2 / 10.4 | 50.1 / 13.4 |

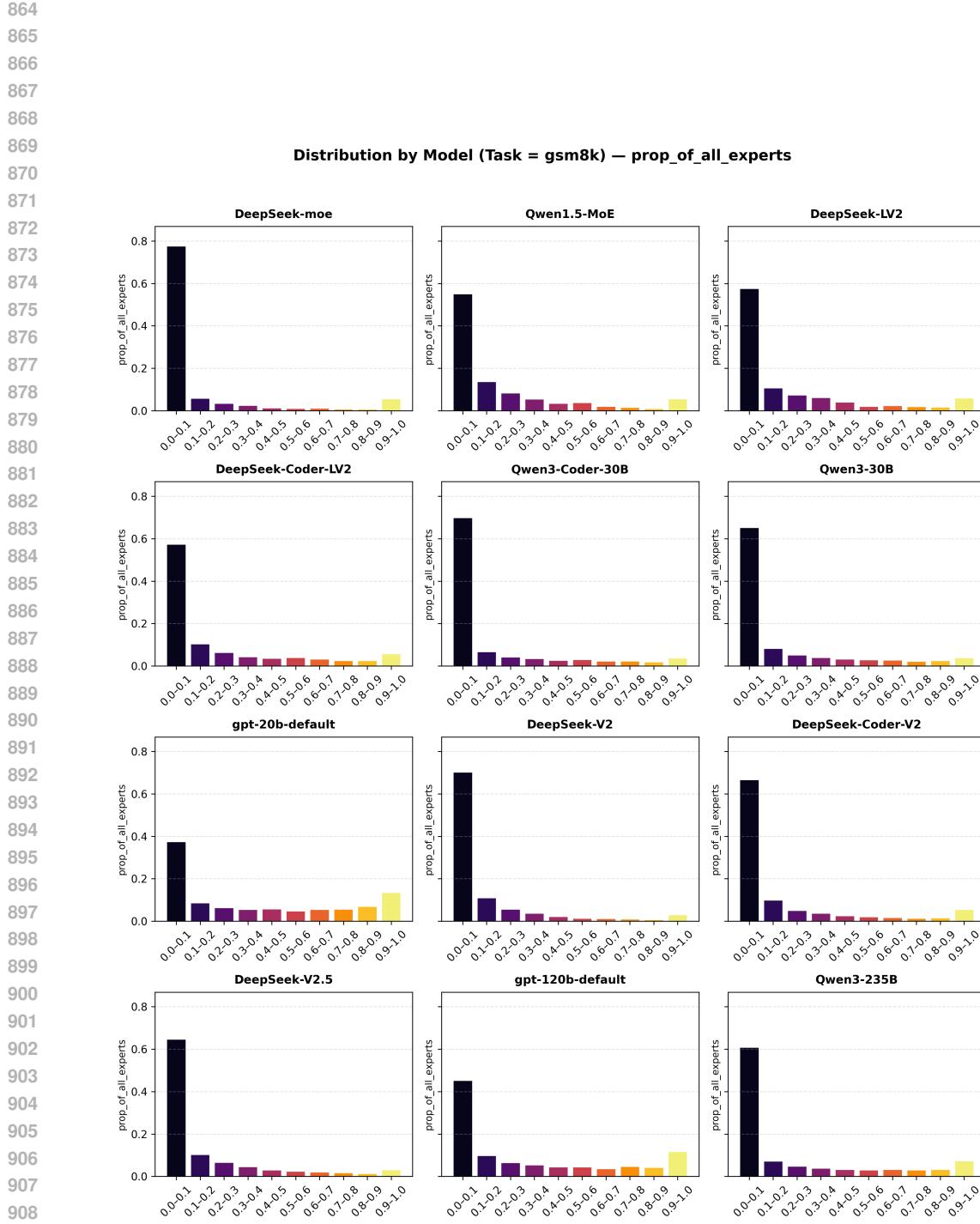
Table 8: Performance (%) and corresponding task Expert proportion(%), with $\eta_{expert} = 0.6$.

| 820 | Model | GSM8K (Math & Reasoning) | MATH (Math & Reasoning) | ARC _c (Math & Reasoning) | HumanEval (Code) | MBPP (Code) | BBH (General) | MMLU (General) |
|-----|------------|-----------------------------|----------------------------|--|---------------------|----------------|------------------|-------------------|
| 821 | OLMoE-0.5T | 2.8 / 20.4 | 3.3 / 38.8 | 25.7 / 19.0 | 8.5 / 7.2 | 10.4 / 9.6 | 25.7 / 13.7 | 27.2 / 26.1 |
| 822 | OLMoE-1T | 3.6 / 24.5 | 3.2 / 42.1 | 33.6 / 25.3 | 6.1 / 7.0 | 10.8 / 10.8 | 25.3 / 14.5 | 32.2 / 27.8 |
| 823 | OLMoE-1.5T | 3.8 / 25.3 | 3.8 / 36.6 | 42.2 / 30.6 | 8.0 / 7.8 | 10.6 / 11.1 | 25.6 / 14.8 | 41.3 / 28.5 |
| 824 | OLMoE-2T | 4.4 / 21.7 | 4.1 / 36.2 | 47.7 / 26.8 | 8.0 / 7.3 | 12.8 / 9.1 | 27.7 / 17.5 | 42.1 / 29.1 |
| 825 | OLMoE-2.5T | 4.7 / 25.3 | 4.0 / 36.0 | 50.8 / 27.7 | 11.6 / 8.0 | 17.4 / 10.9 | 26.2 / 14.0 | 44.0 / 27.7 |
| 826 | OLMoE-3T | 6.4 / 24.8 | 4.2 / 31.8 | 53.8 / 25.2 | 8.0 / 6.7 | 16.4 / 10.0 | 29.5 / 15.4 | 46.3 / 28.7 |
| 827 | OLMoE-3.5T | 6.4 / 24.2 | 4.5 / 45.1 | 54.5 / 25.0 | 9.1 / 6.6 | 16.0 / 9.2 | 20.0 / 22.6 | 46.7 / 28.4 |
| 828 | OLMoE-4T | 5.0 / 23.9 | 4.6 / 35.6 | 57.6 / 25.7 | 11.0 / 8.2 | 20.8 / 11.8 | 30.7 / 14.9 | 47.5 / 28.1 |
| 829 | OLMoE-4.5T | 4.4 / 19.3 | 4.7 / 34.3 | 56.7 / 24.7 | 11.6 / 6.7 | 18.0 / 10.5 | 31.8 / 14.8 | 48.5 / 28.8 |
| 830 | OLMoE-5T | 6.0 / 19.6 | 4.9 / 36.8 | 60.5 / 24.3 | 14.6 / 7.6 | 23.8 / 10.3 | 30.2 / 15.1 | 50.1 / 29.0 |
| 831 | | | | | | | | |

Table 9: Performance (accuracy %) and corresponding task Expert MUI(%) with $\eta_{expert} = 0.6$.

B.3 EXPERT DISTRIBUTION

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Figure 10: Frequency distribution of activated experts across all task instances for the selected
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models evaluated on the GSM8K benchmark.

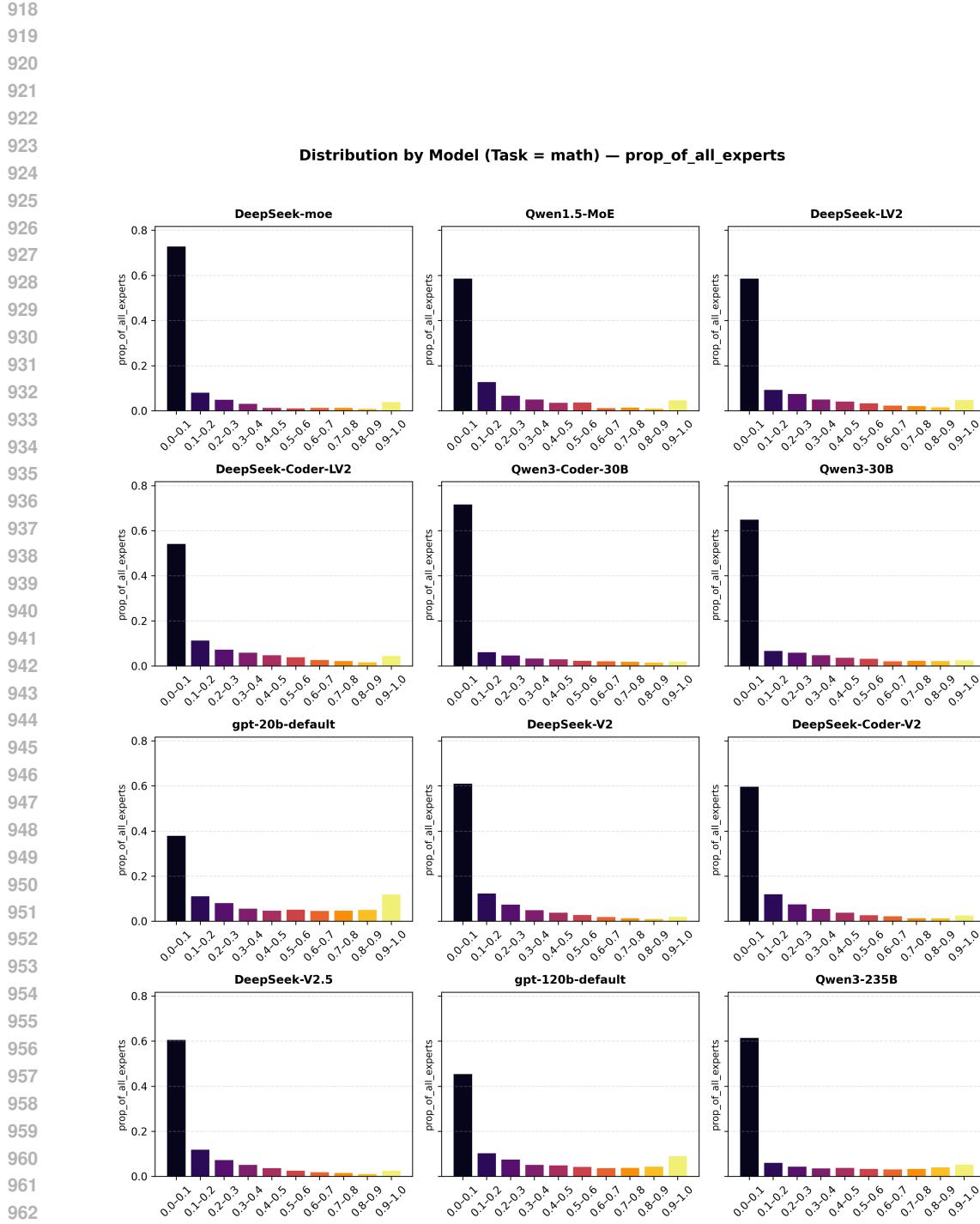


Figure 11: Frequency distribution of activated experts across all task instances for the selected models evaluated on the MATH benchmark.

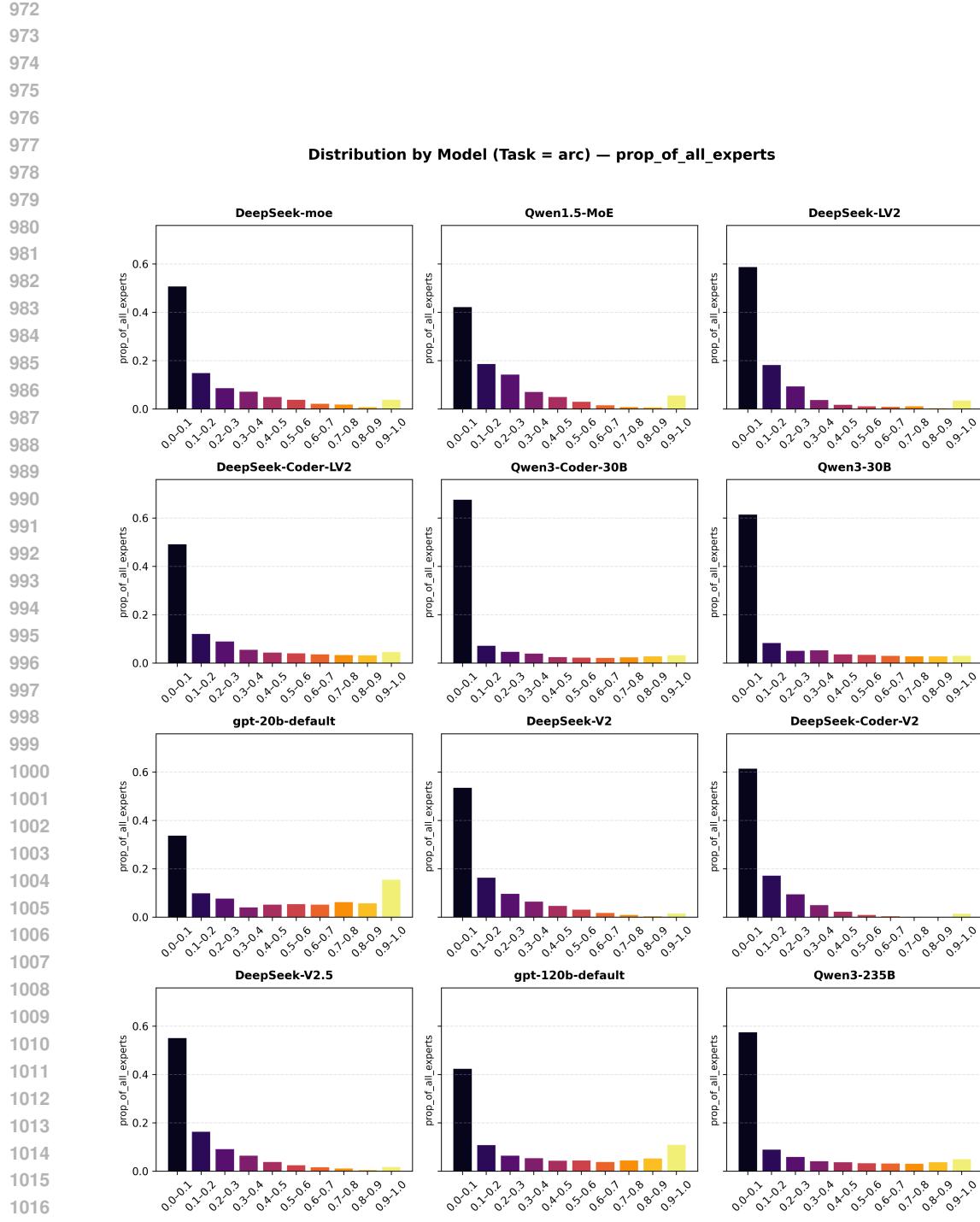


Figure 12: Frequency distribution of activated experts across all task instances for the selected models evaluated on the ARC benchmark.

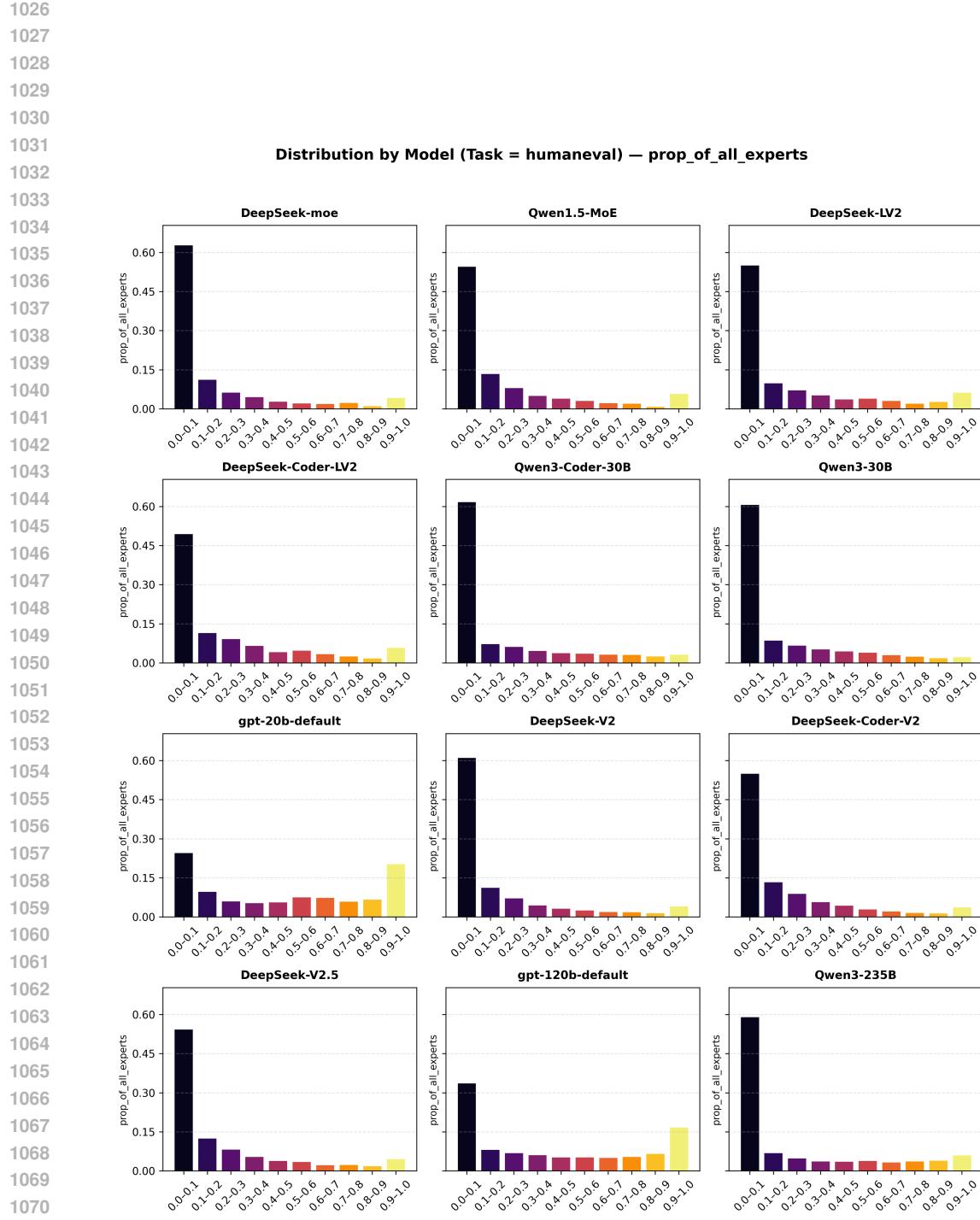
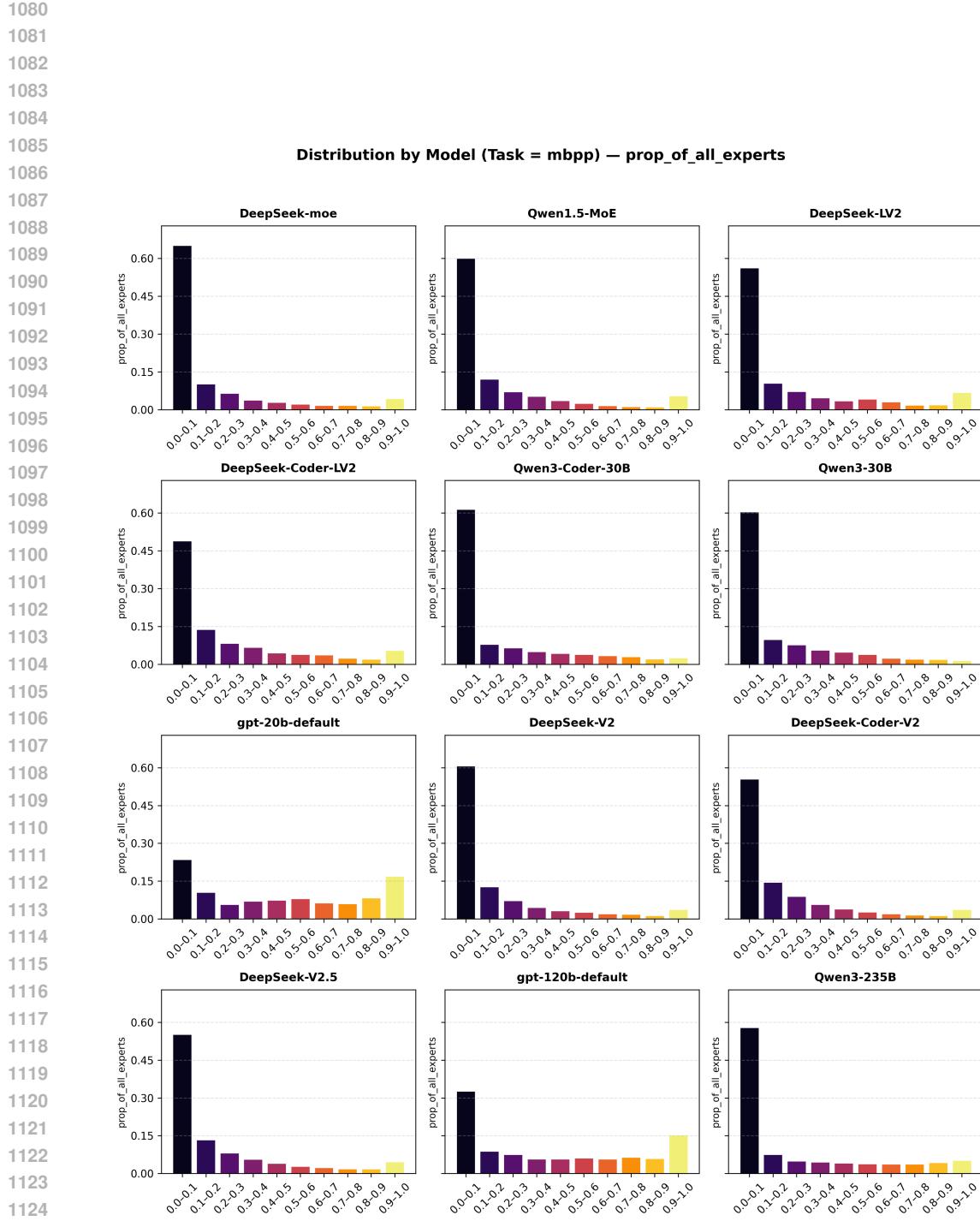
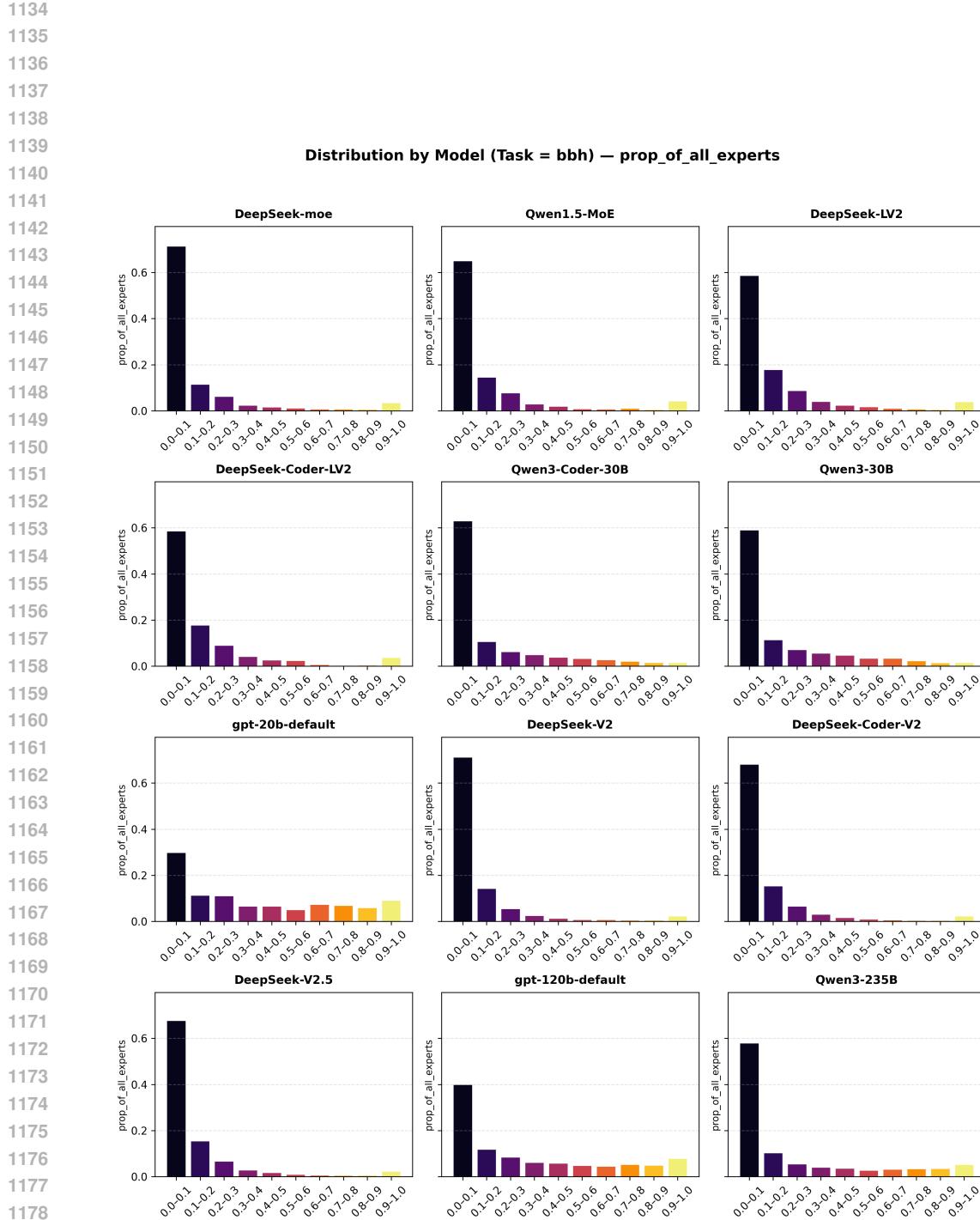


Figure 13: Frequency distribution of activated experts across all task instances for the selected models evaluated on the HumanEval benchmark.





1182 Figure 15: Frequency distribution of activated experts across all task instances for the selected
1183 models evaluated on the BBH benchmark.

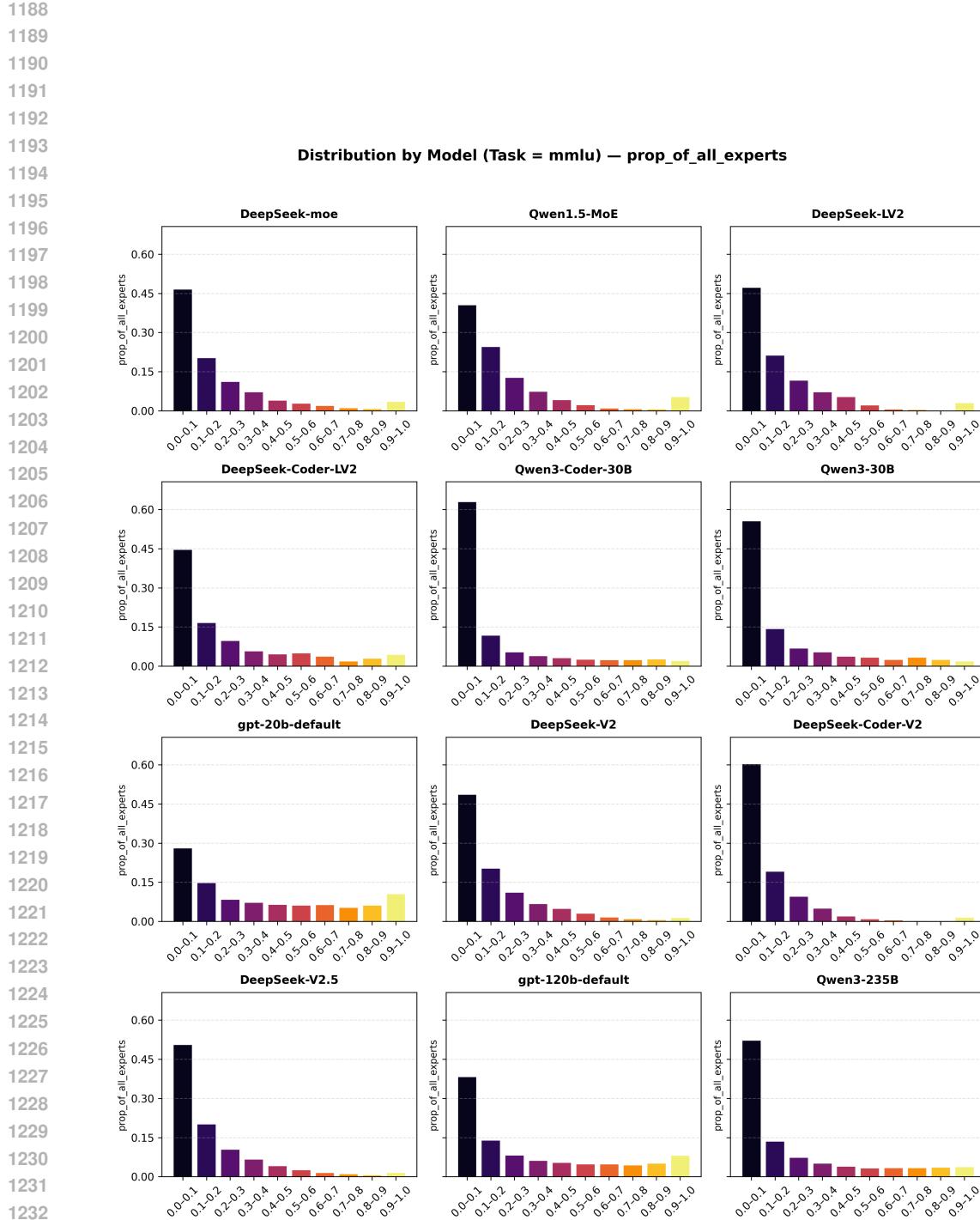


Figure 16: Frequency distribution of activated experts across all task instances for the selected models evaluated on the MMLU benchmark.

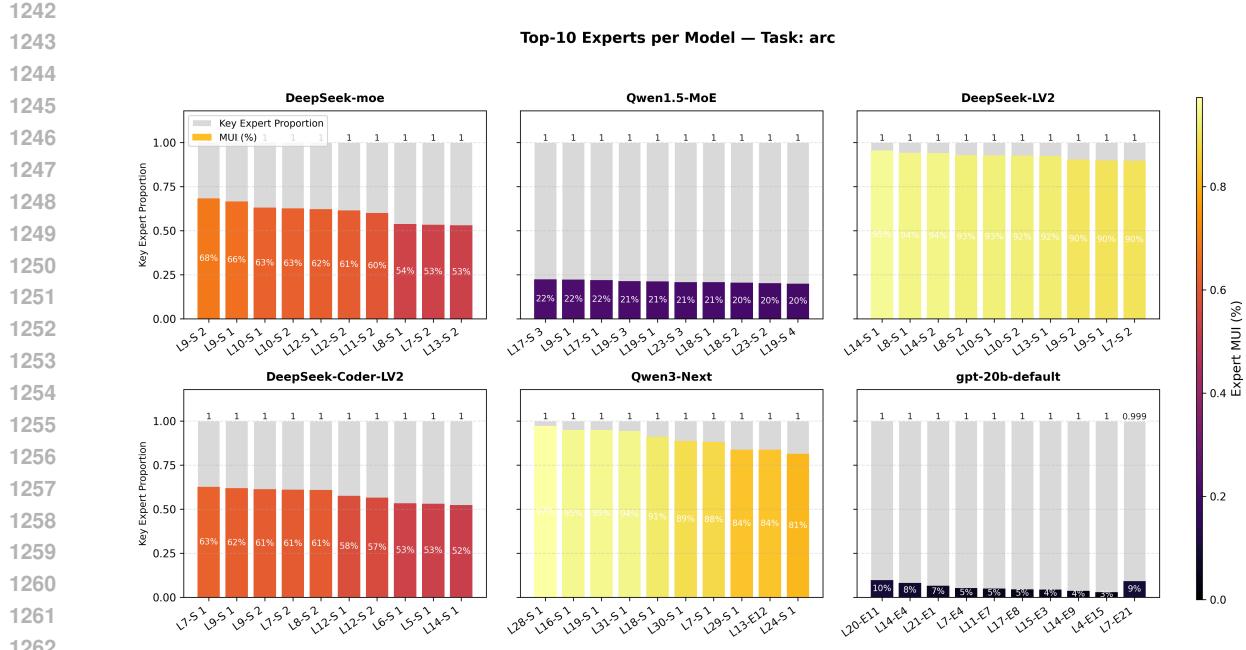


Figure 17: Top-10 experts (ranked by activation frequency Equation 5) for the selected MoE models with shared-expert structures (the exception GPT-OSS-20B model is included for comparison) on ARC. The corresponding MUI for each expert are also reported. Shared experts are denoted as S_i .

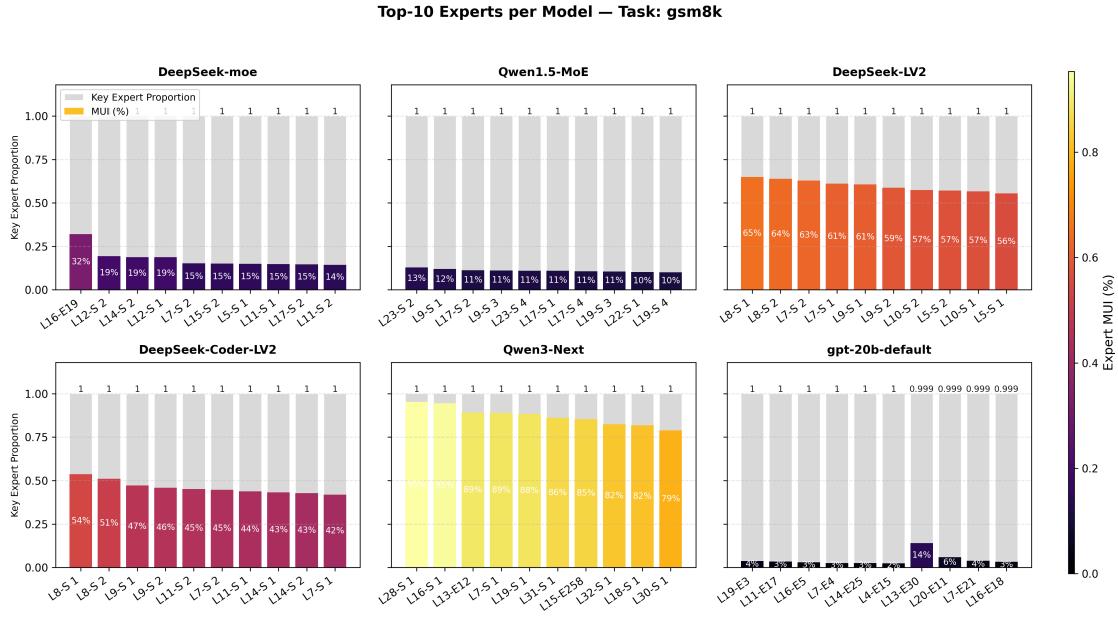


Figure 18: Top-10 experts (ranked by activation frequency Equation 5) for the selected MoE models with shared-expert structures (the exception GPT-OSS-20B model is included for comparison) on GSM8K. The corresponding MUI for each expert are also reported. Shared experts are denoted as S_i .

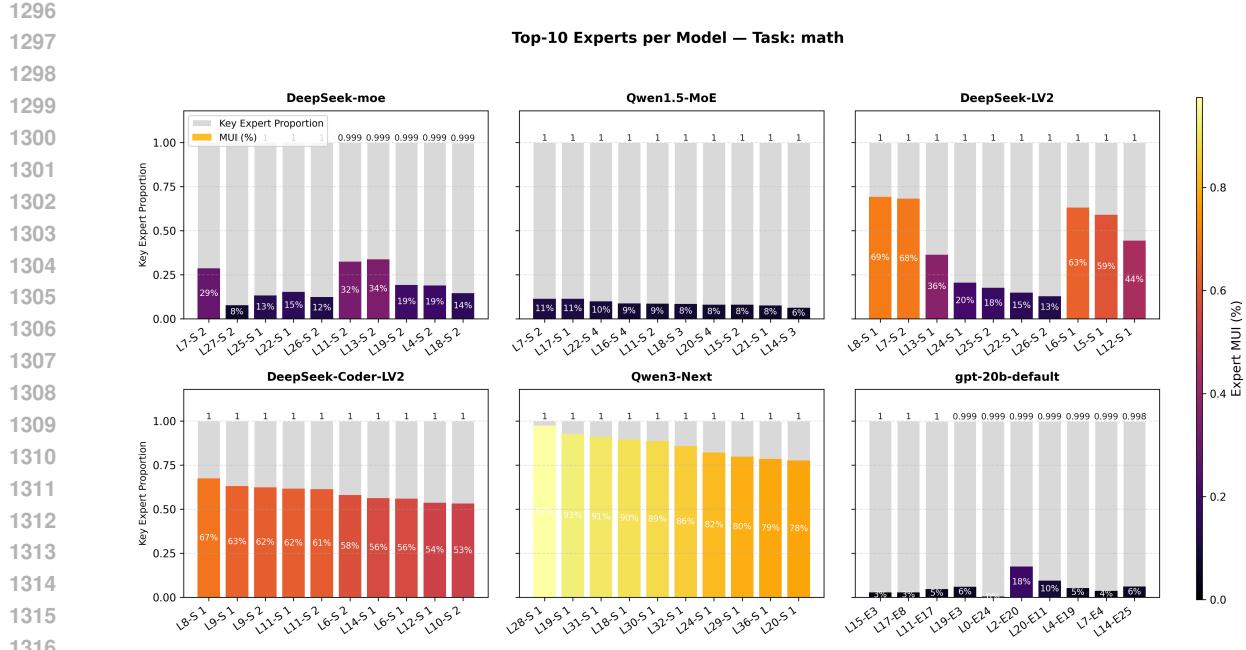


Figure 19: Top-10 experts (ranked by activation frequency Equation 5) for the selected MoE models with shared-expert structures (the exception GPT-OSS-20B model is included for comparison) on MATH. The corresponding MUI for each expert are also reported. Shared experts are denoted as S_i .

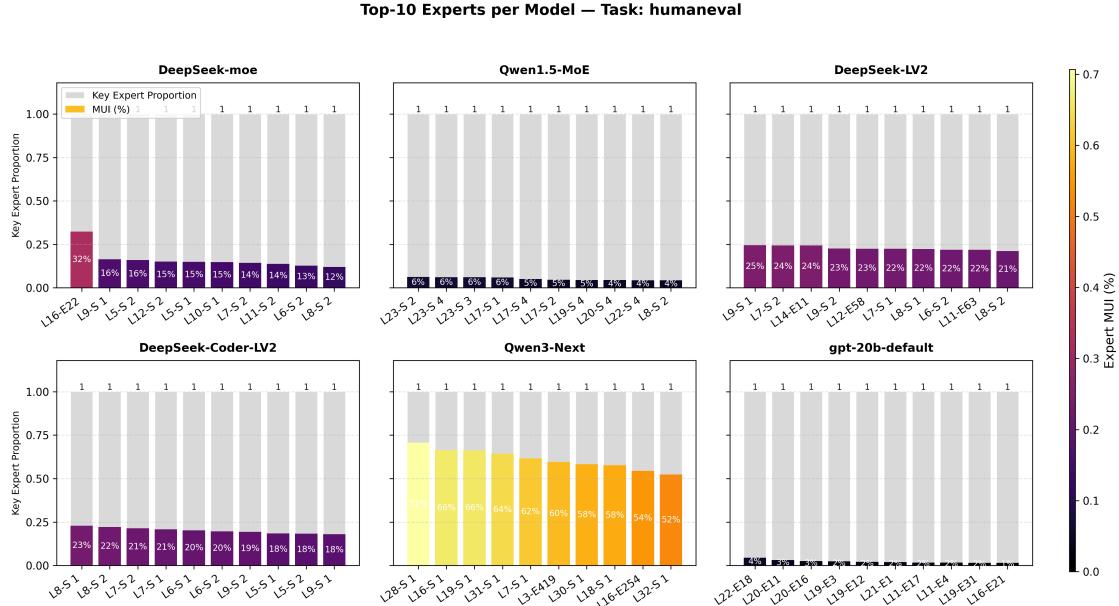


Figure 20: Top-10 experts (ranked by activation frequency Equation 5) for the selected MoE models with shared-expert structures (the exception GPT-OSS-20B model is included for comparison) on HumanEval. The corresponding MUI for each expert are also reported. Shared experts are denoted as S_i .

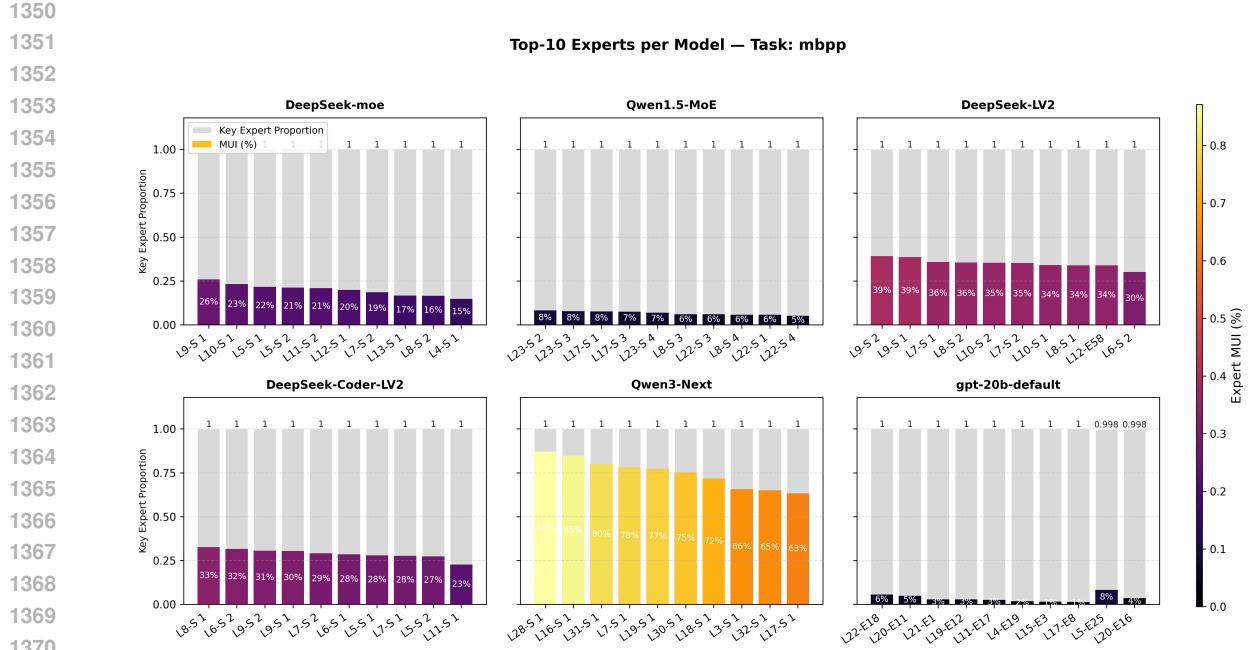


Figure 21: Top-10 experts (ranked by activation frequency Equation 5) for the selected MoE models with shared-expert structures (the exception GPT-OSS-20B model is included for comparison) on MBPP. The corresponding MUI for each expert are also reported. Shared experts are denoted as S_i .

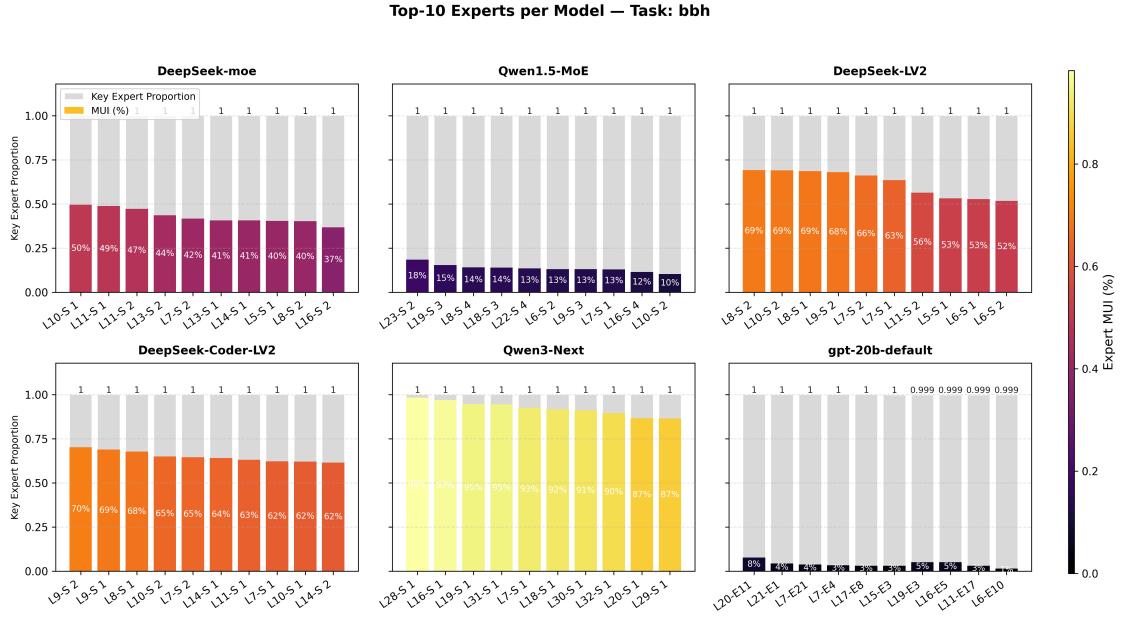
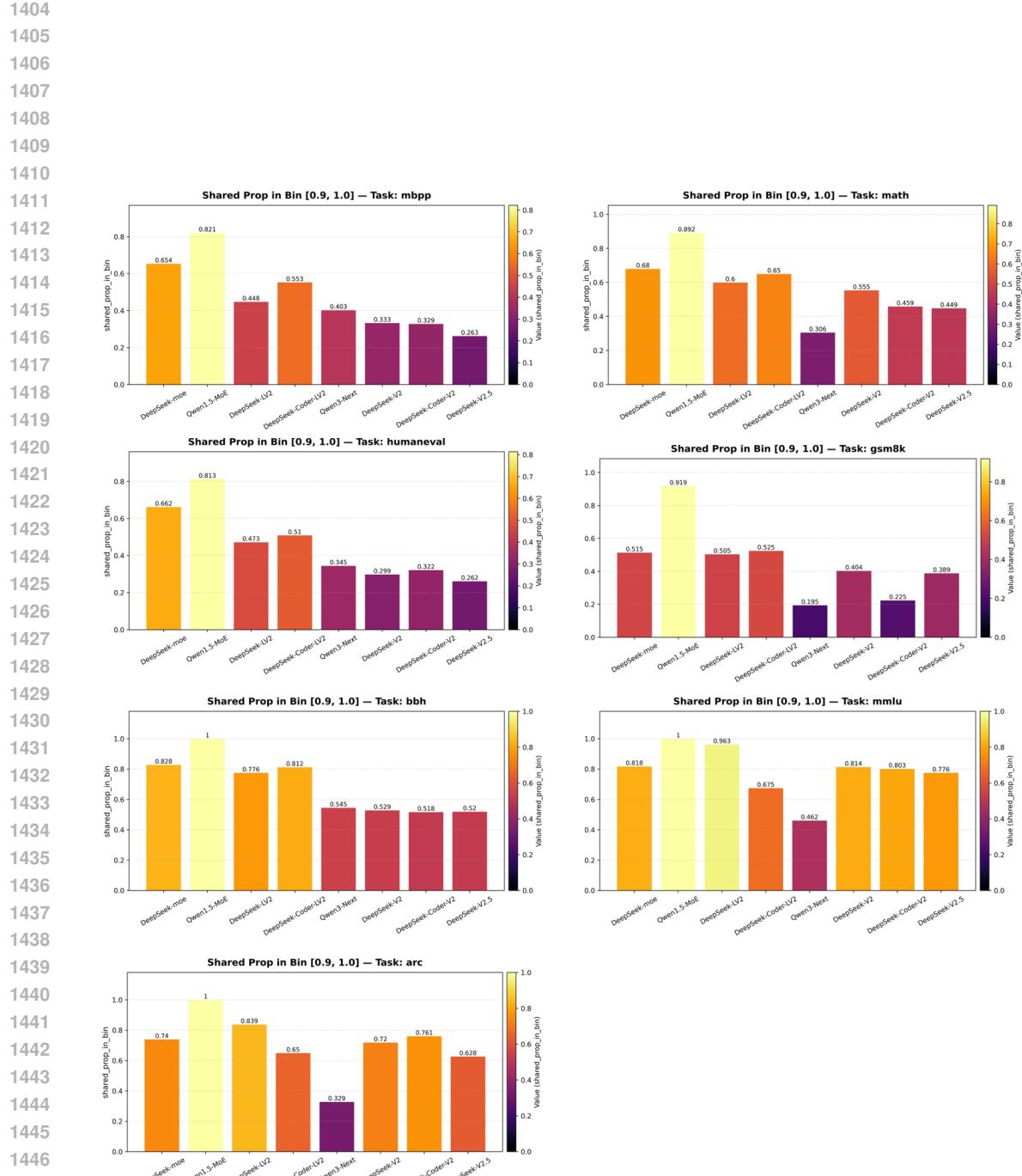
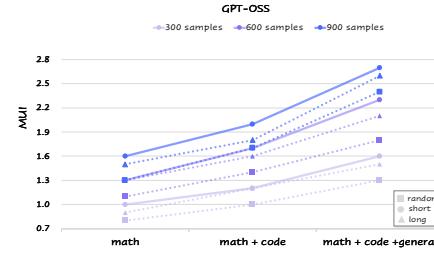
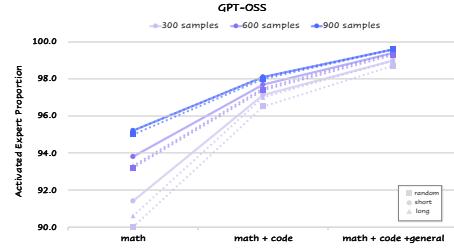


Figure 22: Top-10 experts (ranked by activation frequency Equation 5) for the selected MoE models with shared-expert structures (the exception GPT-OSS-20B model is included for comparison) on BBH. The corresponding MUI for each expert are also reported. Shared experts are denoted as S_i .



1450 Figure 23: Proportion of shared experts among task experts with occurrence frequency greater than
1451 0.9, showing a notably high level of overlap.

1458 B.4 MUI AND ACTIVATED EXPERT PROPORTION FOR DATA MEASUREMENT
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14681469 Figure 24: MUI across different data diversity.
14701471 Figure 25: Proportion of key experts across different data diversity.
14721473 C ABLATION STUDY
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1475 In the main experiments, we primarily adopt a threshold of 0.1% for identifying key neurons. To test
1476 the robustness of this choice, we additionally evaluate smaller thresholds of 0.08% and 0.2% when
1477 computing MUI. The results, shown in Table 10 and Table 11, indicate extremely high consistency
1478 with the 0.1% setting: Pearson correlation = 0.9958 and Spearman correlation = 0.9965. These
1479 results demonstrate that our findings are stable across threshold variations.
1480

| Model | GSM8K (Math & Reasoning) | MATH (Math & Reasoning) | ARC _c (Math & Reasoning) | HumanEval (Code) | MBPP (Code) | BBH (General) | MMLU (General) |
|--------------------------|-----------------------------|----------------------------|--|---------------------|----------------|------------------|-------------------|
| DeepSeek-MoE-A2.8 | 59.6 / 1.4 | 13.2 / 3.2 | 52.4 / 5.9 | 46.9 / 1.1 | 47.3 / 1.7 | 42.3 / 3.0 | 44.8 / 12.6 |
| Qwen1.5-MoE-A2.7B | 53.8 / 4.2 | 17.4 / 5.9 | 70.0 / 8.4 | 46.3 / 1.1 | 42.7 / 1.8 | 35.5 / 4.7 | 54.9 / 19.4 |
| DeepSeek-V2L-A2.4B | 70.4 / 4.1 | 23.1 / 6.6 | 69.2 / 9.0 | 50.0 / 1.4 | 48.3 / 2.5 | 49.4 / 4.7 | 53.4 / 20.3 |
| DeepSeek-Coder-V2L-A2.4B | 85.7 / 3.6 | 56.4 / 7.2 | 69.5 / 7.3 | 72.6 / 1.5 | 64.9 / 2.8 | 63.8 / 5.1 | 55.9 / 16.2 |
| Qwen3-Coder-A3B | 86.4 / 6.5 | 81.2 / 9.2 | 90.7 / 9.5 | 92.7 / 2.8 | 72.9 / 4.9 | 87.5 / 9.5 | 77.5 / 21.4 |
| Qwen3-A3B | 90.0 / 6.2 | 90.7 / 10.1 | 93.3 / 10.5 | 92.7 / 2.9 | 74.9 / 4.9 | 90.5 / 9.1 | 81.6 / 23.4 |
| Qwen3-Next | 93.6 / 4.6 | 92.0 / 7.7 | 92.5 / 8.6 | 94.5 / 1.7 | 80.8 / 3.0 | 93.3 / 6.5 | 84.7 / 22.1 |
| GPT-OSS-A3.6B | 87.9 / 1.4 | 74.2 / 2.2 | 88.3 / 2.7 | 84.7 / 0.7 | 70.5 / 1.1 | 80.0 / 2.0 | 80.1 / 5.8 |
| DeepSeek-V2-A21B | 91.2 / 5.4 | 43.5 / 11.3 | 90.8 / 13.7 | 76.8 / 2.2 | 64.3 / 4.4 | 80.7 / 7.4 | 75.4 / 31.5 |
| DeepSeek-Coder-V2-A21B | 95.0 / 5.0 | 67.2 / 11.7 | 91.1 / 12.3 | 82.9 / 2.8 | 70.0 / 5.3 | 84.5 / 8.1 | 75.5 / 26.2 |
| DeepSeek-V2.5-A21B | 91.4 / 5.6 | 64.5 / 10.4 | 88.4 / 13.2 | 84.8 / 2.1 | 67.1 / 4.1 | 85.6 / 7.6 | 75.2 / 30.0 |
| Qwen3-A22B | 91.4 / 5.4 | 89.2 / 7.8 | 89.3 / 9.7 | 87.8 / 2.2 | 82.2 / 3.9 | 79.8 / 6.8 | 83.1 / 21.4 |
| GPT-OSS-A5.1B | 85.7 / 3.7 | 75.9 / 5.6 | 88.9 / 6.7 | 81.1 / 1.4 | 70.1 / 2.3 | 78.0 / 5.0 | 84.5 / 14.8 |

1493 Table 10: Performance and MUI, as determined by Equation 2 with threshold top $k = 0.08\%$.
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| Model | GSM8K (Math & Reasoning) | MATH (Math & Reasoning) | ARC _c (Math & Reasoning) | HumanEval (Code) | MBPP (Code) | BBH (General) | MMLU (General) |
|--------------------------|-----------------------------|----------------------------|--|---------------------|----------------|------------------|-------------------|
| DeepSeek-MoE-A2.8 | 59.6 / 2.7 | 13.2 / 5.8 | 52.4 / 11.1 | 46.9 / 2.1 | 47.3 / 3.3 | 42.3 / 6.0 | 44.8 / 22.4 |
| Qwen1.5-MoE-A2.7B | 53.8 / 9.7 | 17.4 / 12.7 | 70.0 / 18.6 | 46.3 / 2.8 | 42.7 / 4.4 | 35.5 / 10.9 | 54.9 / 37.9 |
| DeepSeek-V2L-A2.4B | 70.4 / 7.6 | 23.1 / 11.8 | 69.2 / 16.3 | 50.0 / 3.0 | 48.3 / 5.0 | 49.4 / 9.0 | 53.4 / 33.1 |
| DeepSeek-Coder-V2L-A2.4B | 85.7 / 6.5 | 56.4 / 12.7 | 69.5 / 13.1 | 72.6 / 3.2 | 64.9 / 5.7 | 63.8 / 9.4 | 55.9 / 26.9 |
| Qwen3-Coder-A3B | 86.4 / 11.5 | 81.2 / 14.8 | 90.7 / 15.9 | 92.7 / 5.5 | 72.9 / 9.0 | 87.5 / 16.7 | 77.5 / 32.1 |
| Qwen3-A3B | 90.0 / 11.4 | 90.7 / 16.8 | 93.3 / 18.1 | 92.7 / 5.7 | 74.9 / 9.2 | 90.5 / 16.2 | 81.6 / 36.1 |
| Qwen3-Next | 93.6 / 9.7 | 92.0 / 15.0 | 92.5 / 16.7 | 94.5 / 3.7 | 80.8 / 6.5 | 93.3 / 13.3 | 84.7 / 38.3 |
| GPT-OSS-A3.6B | 87.9 / 2.9 | 74.2 / 4.1 | 88.3 / 5.8 | 84.7 / 1.4 | 70.5 / 2.2 | 80.0 / 4.3 | 80.1 / 11.6 |
| DeepSeek-V2-A21B | 91.2 / 10.2 | 43.5 / 20.2 | 90.8 / 24.4 | 76.8 / 4.7 | 64.3 / 8.8 | 80.7 / 14.0 | 75.4 / 48.0 |
| DeepSeek-Coder-V2-A21B | 95.0 / 9.7 | 67.2 / 21.1 | 91.1 / 22.5 | 82.9 / 5.9 | 70.0 / 10.7 | 84.5 / 15.2 | 75.5 / 42.3 |
| DeepSeek-V2.5-A21B | 91.4 / 11.0 | 64.5 / 19.0 | 88.4 / 23.8 | 84.8 / 4.6 | 67.1 / 8.5 | 85.6 / 14.2 | 75.2 / 46.4 |
| Qwen3-A22B | 91.4 / 9.9 | 89.2 / 13.5 | 89.3 / 17.1 | 87.8 / 4.5 | 82.2 / 7.5 | 79.8 / 12.4 | 83.1 / 33.7 |
| GPT-OSS-A5.1B | 85.7 / 7.6 | 75.9 / 10.8 | 88.9 / 13.2 | 81.1 / 3.0 | 70.1 / 4.9 | 78.0 / 10.1 | 84.5 / 26.5 |

1507 Table 11: Performance and MUI, as determined by Equation 2 with threshold top $k = 0.2\%$.
1508

1509 In addition, we also experimented with alternative methods for computing neuron importance.
1510 Specifically, besides the default projection-based method, we tested using raw activations and pro-
1511 jecting the entire upsampled outputs (details are provided in the Appendix A.4). We further con-
ducted threshold ablations (Figure 27 and Figure 28) under these alternative formulations. After

evaluating different settings, we selected a threshold of 0.1% as the most appropriate and carried out experiments accordingly. For efficiency reasons, we restricted this analysis to four representative benchmarks: ARC, GSM8K, MBPP, and BBH. The resulting MUI values are shown in Table 12 and Table 13. We further compute similarity with Table 4, obtaining the following results: Cosine similarity: 0.9665, Pearson correlation: 0.8511, Spearman correlation: 0.7442; Cosine similarity: 0.9835, Pearson correlation: 0.9317, Spearman correlation: 0.9236. These results demonstrate that the overall trends remain highly consistent across different methods. Furthermore, within the same model scale, the ranking of models is stable, with GPT-OSS consistently exhibiting the lowest MUI.

| Model | GSM8K | ARC _c | MBPP | BBH |
|--------------------------|------------|------------------|------------|------------|
| DeepSeek-LV2-A2.4B | 70.4 / 3.4 | 69.2 / 8.1 | 50.0 / 2.3 | 49.4 / 4.4 |
| DeepSeek-Coder-LV2-A2.4B | 85.7 / 2.9 | 69.5 / 7.8 | 72.6 / 2.4 | 63.8 / 4.9 |
| Qwen3-A3B | 90.0 / 5.6 | 93.3 / 10.5 | 92.7 / 4.5 | 90.5 / 8.9 |
| GPT-OSS-A3.6B | 87.9 / 4.7 | 88.3 / 8.7 | 84.7 / 3.6 | 80.0 / 6.7 |
| DeepSeek-V2-A21B | 91.2 / 5.1 | 90.8 / 14.4 | 64.3 / 4.6 | 80.7 / 7.9 |
| DeepSeek-Coder-V2-A21B | 95.0 / 4.3 | 91.1 / 12.3 | 70.0 / 5.7 | 84.5 / 8.5 |

Table 12: Performance and MUI, as determined by Equation 9 with threshold top $k = 0.1\%$.

| Model | GSM8K | ARC _c | MBPP | BBH |
|--------------------------|------------|------------------|------------|-------------|
| DeepSeek-LV2-A2.4B | 70.4 / 6.3 | 69.2 / 16.0 | 50.0 / 3.7 | 49.4 / 9.4 |
| DeepSeek-Coder-LV2-A2.4B | 85.7 / 5.4 | 69.5 / 12.0 | 72.6 / 4.5 | 63.8 / 9.7 |
| Qwen3-A3B | 90.0 / 8.3 | 93.3 / 14.0 | 92.7 / 6.3 | 90.5 / 12.3 |
| GPT-OSS-A3.6B | 87.9 / 1.4 | 88.3 / 3.1 | 84.7 / 1.3 | 80.0 / 2.2 |
| DeepSeek-V2-A21B | 91.2 / 6.3 | 90.8 / 16.1 | 64.3 / 4.8 | 80.7 / 9.3 |
| DeepSeek-Coder-V2-A21B | 95.0 / 5.0 | 91.1 / 14.2 | 70.0 / 5.4 | 84.5 / 9.4 |

Table 13: Performance and MUI as determined by Equation 10 with threshold top $k = 0.1\%$.

On the other hand, we also perform expert-level analyses using the same threshold of $\eta_{expert} = 0.6$ to define key experts. We compute results based on Equation 9 and Equation 10, reported in Table 14 and Table 15, and then compare them with the main results (Table 6). The similarities are as follows: Cosine similarity: 0.9947, Pearson correlation: 0.9863, Spearman correlation: 0.9533; Cosine similarity: 0.9794, Pearson correlation: 0.9503, Spearman correlation: 0.9030. These results demonstrate that expert-level measurements yield highly consistent trends and results. Moreover, GPT consistently exhibits the highest proportion of key experts, further confirming our findings.

| Model | GSM8K | ARC _c | MBPP | BBH |
|--------------------------|-------------|------------------|-------------|-------------|
| DeepSeek-LV2-A2.4B | 70.4 / 9.6 | 69.2 / 6.8 | 50.0 / 11.7 | 49.4 / 6.2 |
| DeepSeek-Coder-LV2-A2.4B | 85.7 / 12.7 | 69.5 / 13.0 | 72.6 / 10.9 | 63.8 / 6.0 |
| Qwen3-A3B | 90.0 / 10.2 | 93.3 / 10.8 | 92.7 / 7.4 | 90.5 / 6.6 |
| GPT-OSS-A3.6B | 87.9 / 30.1 | 88.3 / 36.5 | 84.7 / 40.9 | 80.0 / 28.9 |
| DeepSeek-V2-A21B | 91.2 / 7.1 | 90.8 / 5.9 | 64.3 / 10.0 | 80.7 / 4.7 |
| DeepSeek-Coder-V2-A21B | 95.0 / 12.8 | 91.1 / 3.3 | 70.0 / 10.3 | 84.5 / 5.2 |

Table 14: Performance and corresponding task Expert proportion (the neuron is finding using Equation 9), with $\eta_{expert} = 0.6$.

| Model | GSM8K | ARC _c | MBPP | BBH |
|--------------------------|-------------|------------------|-------------|-------------|
| DeepSeek-LV2-A2.4B | 70.4 / 16.8 | 69.2 / 9.0 | 50.0 / 20.6 | 49.4 / 14.0 |
| DeepSeek-Coder-LV2-A2.4B | 85.7 / 23.7 | 69.5 / 23.0 | 72.6 / 23.7 | 63.8 / 13.6 |
| Qwen3-A3B | 90.0 / 12.0 | 93.3 / 12.4 | 92.7 / 8.4 | 90.5 / 8.9 |
| GPT-OSS-A3.6B | 87.9 / 33.1 | 88.3 / 35.9 | 84.7 / 40.5 | 80.0 / 29.0 |
| DeepSeek-V2-A21B | 91.2 / 8.3 | 90.8 / 8.2 | 64.3 / 11.7 | 80.7 / 5.9 |
| DeepSeek-Coder-V2-A21B | 95.0 / 13.5 | 91.1 / 3.3 | 70.0 / 11.6 | 84.5 / 6.1 |

Table 15: Performance and corresponding task Expert proportion (the neuron is finding using Equation 10), with $\eta_{expert} = 0.6$.

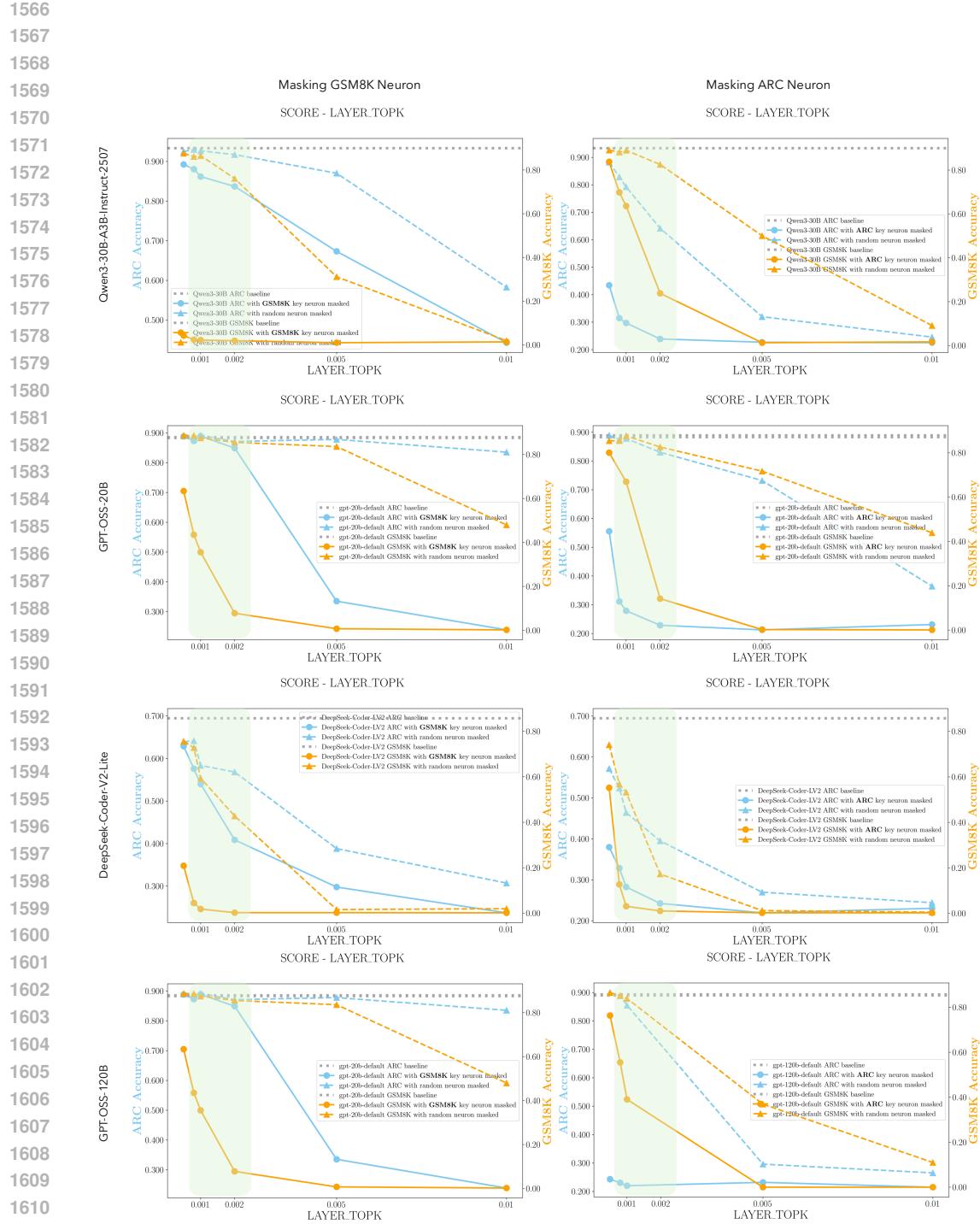


Figure 26: Performance accuracy (ACC) of the on the [ARC](#) and [GSM8K](#) datasets, with key neurons masked specifically for the [ARC](#) dataset or the [GSM8K](#) dataset. Key neurons are identified using Equation 2 and a pre-defined threshold function (Detailed in Appendix A.3). The threshold value used for our MUI analysis —0.1% to 0.2%, is visually indicated by a green box. The performance impact of masking an equivalent number of key neurons as in the [ARC](#) / [GSM8K](#) dataset on the corresponding model is represented with a dashed line.

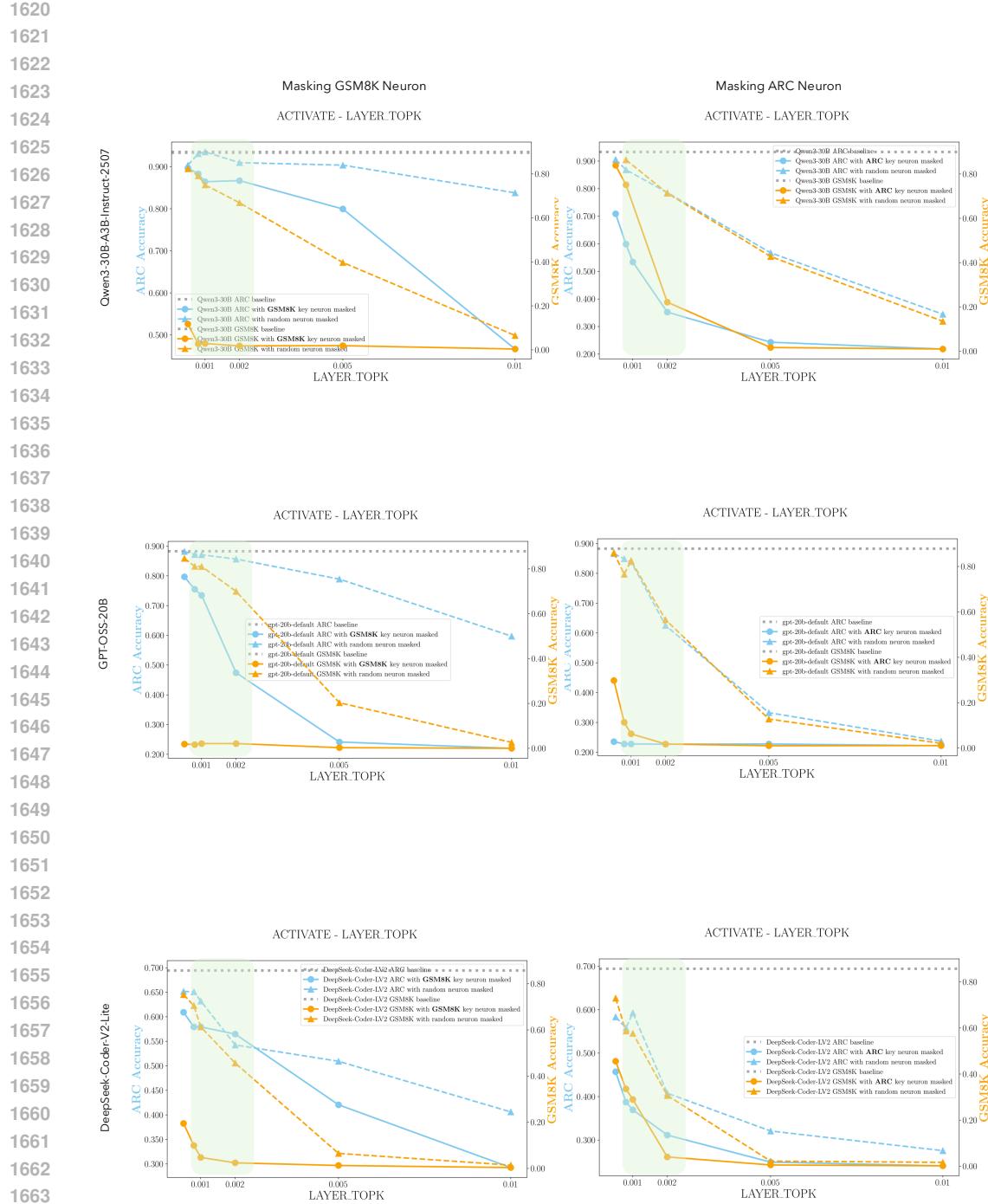
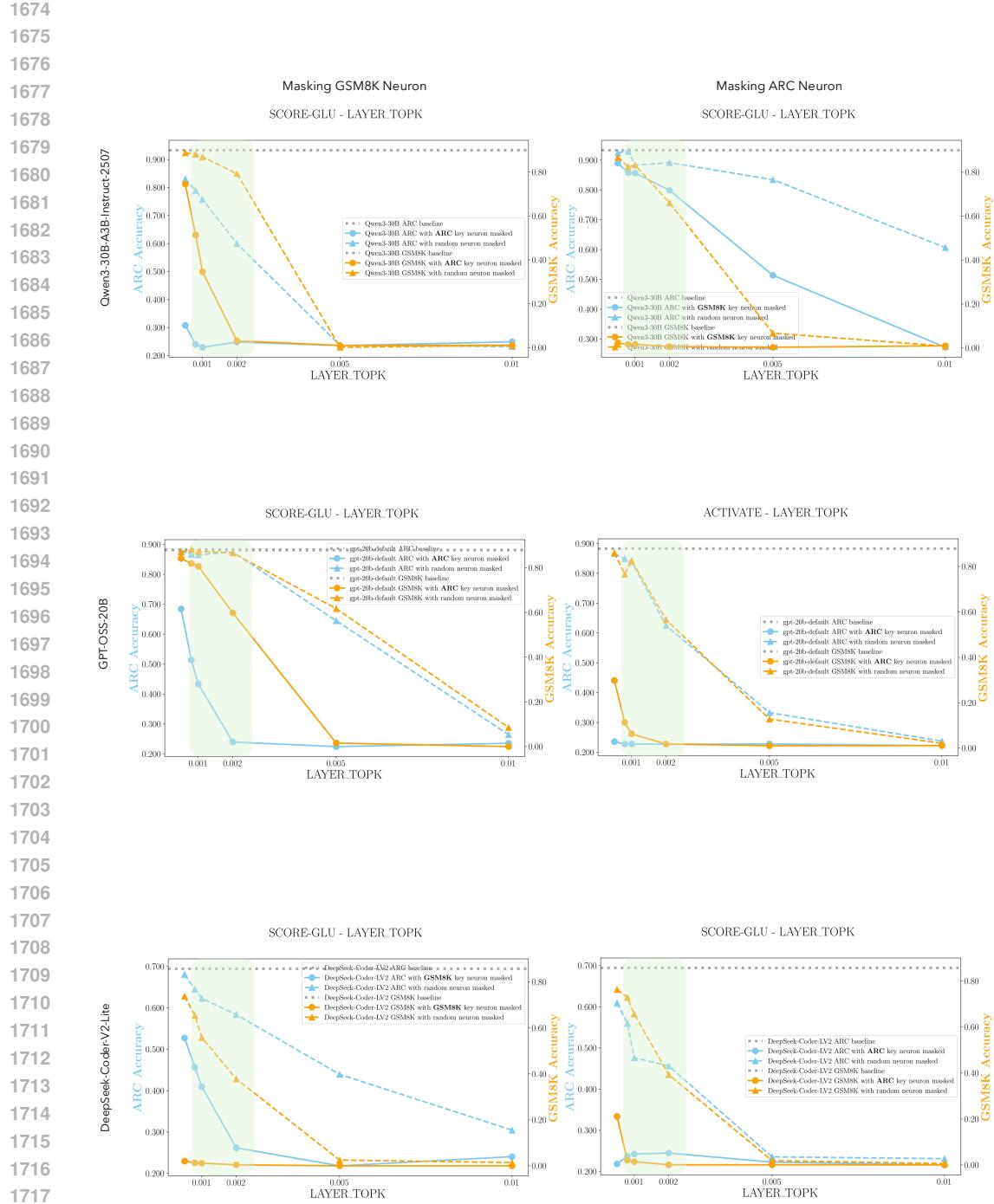


Figure 27: Performance accuracy (ACC) of the on the **ARC** and **GSM8K** datasets, with key neurons masked specifically for the **ARC** dataset or the **GSM8K** dataset. Key neurons are identified using Equation 9 and a pre-defined threshold function (Detailed in Appendix A.3). The threshold value used for our MUI analysis —0.1% to 0.2%, is visually indicated by a green box. The performance impact of masking an equivalent number of key neurons as in the **ARC** / **GSM8K** dataset on the corresponding model is represented with a dashed line.



1720 Figure 28: Performance accuracy (ACC) of the on the [ARC](#) and [GSM8K](#) datasets, with key neurons
1721 masked specifically for the [ARC](#) dataset or the [GSM8K](#) dataset. Key neurons are identified using
1722 Equation 10 and a pre-defined threshold function (Detailed in Appendix A.3). The threshold value
1723 used for our MUI analysis —0.1% to 0.2%, is visually indicated by a green box. The performance
1724 impact of masking an equivalent number of key neurons as in the [ARC](#) / [GSM8K](#) dataset on the
1725 corresponding model is represented with a dashed line.