

Reservoir Computing in R: a Tutorial for Using reservoirnet to Predict Complex Time-Series

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Abstract

Reservoir Computing (RC) is a machine learning method based on neural networks that efficiently process information generated by dynamical systems. It has been successful in solving various tasks including time series forecasting, language processing or voice processing. RC is implemented in Python and Julia but not in R. This article introduces reservoirnet, an R package providing access to the Python API ReservoirPy, allowing R users to harness the power of reservoir computing. This article provides an introduction to the fundamentals of RC and showcases its real-world applicability through three distinct sections. First, we cover the foundational concepts of RC, setting the stage for understanding its capabilities. Next, we delve into the practical usage of reservoirnet through two illustrative examples. These examples demonstrate how it can be applied to real-world problems, specifically, regression of COVID-19 hospitalizations and classification of Japanese vowels. Finally, we present a comprehensive analysis of a real-world application of reservoirnet, where it was used to forecast COVID-19 hospitalizations at Bordeaux University Hospital using public data and electronic health records.

Keywords: Reservoir Computing, Covid-19, Electronic Health Records, Time series

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32 1 Introduction

Reservoir Computing (RC) is a prominent machine learning method, proposed by Jaeger (2001), Maass, 33 Natschläger, and Markram (2002) and Lukoševičius and Jaeger (2009) that has gained significant 34 attention in recent years for its ability to efficiently process information generated by dynamical 35 systems. This innovative approach leverages the dynamics of a high-dimensional "reservoir" (we 36 define it below) to perform complex computations and solve various tasks based on the response 37 of this dynamical system to input signals. RC has demonstrated its efficacy in tackling various 38 challenges, encompassing pattern classification and time series forecasting in applications ranging 39 from electrocardiogram analysis to bird calls (Trouvain and Hinaut 2021), language processing 40 (Hinaut and Dominey 2013), power plants, internet traffic, stock prices, and beyond (Lukoševičius 41

⁴² and Jaeger 2009; Tanaka et al. 2019).

Originally, the RC paradigm was implemented in artificial firing-rate neurons ("Echo State Networks", 43 Jaeger (2001)) and spiking neurons ("Liquid State Machine", Maass, Natschläger, and Markram (2002)) 44 as a recurrent neural network (RNN) where the internal recurrent connections, denoted as the 45 reservoir, are randomly generated and only the output layer (named "read-out") is trained. The 46 reservoir projects temporal input signals onto a high-dimensional feature space, facilitating the 47 learning of non-linear and temporal interactions. Thus, this recurrent layer contains high-dimensional 48 non-linear recombination of the inputs and past states: it is a "reservoir of computations" from 49 which useful information can be linearly extracted (or "read-out") to provide the desired outputs. 50 This offers the advantage of decreasing the computing time compared to conventional RNNs while 51 consistently maintaining performance (Vlachas et al. 2020). Besides, this RC paradigm fostered 52 increasing interest thanks to its ability to be implemented on classical computers, as the hidden 53 recurrent layer can be kept untrained. A wide range of physical media can be also used to replace 54 it and Tanaka et al. (2019) recently reviewed this prolific field: from FPGA hardware (Penkovsky, 55 Larger, and Brunner 2018), to spin waves using magnetic properties (Nakane, Tanaka, and Hirose 56 2018), skrymions (Prychynenko et al. 2018) or optical implementations (Rafayelyan et al. 2020). 57 This provides interesting and potentially more efficient alternative to traditional machine learning 58 computing and might play an important role in the coming years (Yan et al. 2024). 50

RC leverages various hyperparameters to introduce prior knowledge about the relationship between 60 input variables and output targets. But because the connections within the reservoir are randomly 61 initialized, the same set of hyperparameters may exhibit diverse behaviors across different instances 62 of the reservoir connections. This unpredictability makes it challenging to anticipate the performance 63 of a particular hyperparameter setting, as identical settings may produce varying outcomes when 64 applied to distinct instances of the reservoir. Moreover, selecting the most suitable hyperparameters 65 often requires researchers to experiment with multiple combinations on a training dataset and 66 evaluate their performance on a separate test set². Although this approach can be resource-intensive 67 and time-consuming, it is a compromise that is acceptable considering the rapid simulation capabilities 68 offered by RC. Furthermore, there is a current absence of implementation in R, rendering the method 69 challenging for users unfamiliar with Python (Trouvain and Hinaut 2022) or Julia (Martinuzzi et al. 70 2022). 71

Here, we offer comprehensive guidance to assist new users in maximizing the benefits of RC. Initially, 72 a broad introduction to reservoir computing is presented in Section 2, followed in Section 3 by a 73 tutorial on its application using reservoirnet, an R package built upon the ReservoirPy Python 74 module (Trouvain, Rougier, and Hinaut 2022; Trouvain and Hinaut 2022; Trouvain et al. 2020). 75 Section 3 then introduces the workflow usage on reservoirnet for RC with two basic use-cases, 76 and finally, in Section 4 we investigate the various challenges associated with an advanced case-77 study leveraging RC for forecasting COVID-19 hospitalizations. This case-study exploration includes 78 detailed guidance on the modeling strategy, the selection of hyperparameters, and the implementation 79 process. 80

81 2 RC presentation

⁸² RC is a machine learning paradigm which is most often implemented as Echo State Networks (ESNs), ⁸³ i.e. the firing-rate neuron version (Jaeger 2001). An ESN is described by three matrices of connectivity: ⁸⁴ an input layer W_{in} , a recurrent layer W and an output layer W_{out} . At each time step, the input vector

u_t is projected into the reservoir which is also combined with reservoir past state x(t - 1) through

²In this article, we employ the term "train set" to refer to the combined dataset consisting of both the training and validation sets, which are cycled through in a cross-validation manner.

the recurrent connections. The output y(t) is linearly read-out from the reservoir. Input W_{in} and

⁸⁷ recurrent *W* matrices are kept random; only the output matrix W_{out} is trained in an offline or online

method. Often a ridge regression (i.e. a regularized linear regression) is used to obtain the desired

⁸⁹ outputs y(t) from the reservoir states x(t). Figure 1 depicts the architecture. For simplicity, we will

⁹⁰ use the term "reservoir computing" for "Echo State Network" in the remainder of the paper.

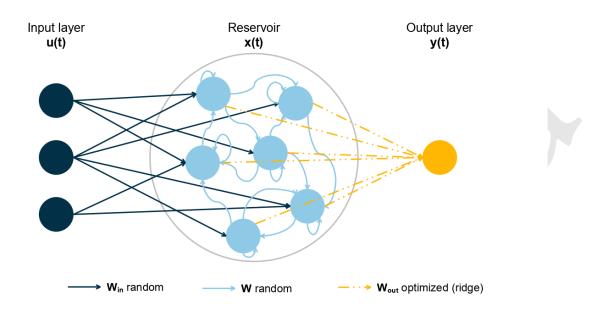


Figure 1: Reservoir computing is composed of an input layer, a reservoir and an output layer. Connection between input layer and reservoir and inside reservoir are random. Only the output layer is optimized based on a ridge regression. Adapted from Trouvain et al. (2020)

⁹¹ The input layer u(t) is an *M*-dimension vector, where *M* is the number of input time series, which

⁹² corresponds to the values of the input time series at time *t* where t = 1, ..., T. The reservoir layer x(t)

is an N_{res} -dimensional vector where N_{res} is the number of nodes in the reservoir. The value x(t) is

94 defined as follow:

$$x(t+1) = (1-\alpha)x(t) + \alpha \tanh(Wx(t) + W_{in}u(t+1)).$$
(1)

⁹⁵ The leaking rate $\alpha \in [0, 1]$ defines the update rate of the nodes. The closer α is to 1, the more the ⁹⁶ reservoir is sensitive to new inputs u(t). Therefore, the reservoir state at time t + 1 denoted x(t + 1)⁹⁷ depends on the reservoir state at the previous time x(t) and the new inputs u(t + 1). The function ⁹⁸ *tanh*() represents the activation function, applied element-wise to each component of the vector, ⁹⁹ ensuring that each node's activation is scaled between -1 and 1. Both W_{in} and W are random matrices ¹⁰⁰ of size $N_{res} \times M$ and $N_{res} \times N_{res}$ respectively.

The input-reservoir connection matrix (W_{in}) and the intra-reservoir connection matrix (W) are 101 generated in three steps. Win is generated using a Bernoulli (bimodal) distribution where each value 102 can be either $-I_{scale}(m)$ or $I_{scale}(m)$ with an equal probability where m = 1, ..., M corresponds to a 103 given feature in the input layer. The input scaling, denoted Iscale, is a hyperparameter coefficient 104 common to all features from the input layer or specific to each feature m. In that case, the more 105 important the feature is, the greater should be its input scaling. W is generated from a Gaussian 106 distribution $\mathcal{N}(0, 1)$. Both W_{in} and W then undergo sparsification, where a connectivity mask is 107 applied to retain only 10% of the connections, enforcing sparsity. In a third step, the W matrix is 108

scaled according to the defined spectral radius, a hyperparameter defining the highest eigen value of W.

¹¹¹ The final layer is a linear regression with ridge penalization where the explanatory features are the

reservoir state and the variable to be explained is the outcome to predict such that:

$$W_{out} = YX^T(XX^T + \lambda I)^{-1}$$

¹¹³ Where x(t) and y(t) are accumulated in X and Y respectively such that:

$$X = \begin{bmatrix} x(1) \\ x(2) \\ \dots \\ x(T) \end{bmatrix} \text{ and } Y = \begin{bmatrix} y(1) \\ y(2) \\ \dots \\ y(T) \end{bmatrix}.$$

The parameter λ is the ridge penalization which aims to prevent overfitting. Additionally, one can also connect the input layer to the output layer to the reservoir nodes. In that case, *X* is the accumulation

¹¹⁶ of both such that :

$$X = \begin{bmatrix} x(1), u(1) \\ x(2), u(2) \\ \dots \\ x(T), u(T) \end{bmatrix} \text{ and } Y = \begin{bmatrix} y(1) \\ y(2) \\ \dots \\ y(T) \end{bmatrix}$$

Overall, there are four main hyperparameters to be chosen by the user: i) the leaking rate which defines the memory of the RC, ii) the input scaling which defines the relative importance of the features, iii) the spectral radius which defines the connections of the neurons inside the reservoir which in turn defines the degree of non-linear combination of features, and iv) the ridge penalization which controls the degree of overfitting. The choice of hyperparameters often requires the user to evaluate the performance of different combinations of hyperparameters on a validation set before selecting the optimal combination to forecast on the test set.

124 **3** Usage workflow

¹²⁵ In this section, we will cover the basics of reservoirnet use including installation, classification and ¹²⁶ regression. A more in depth description is provided in Section 4 with the covid-19 forecast use case.

127 **3.1 Installation**

¹²⁸ reservoirnet is an R package making the Python module ReservoirPy easily callable from R using

reticulate R package Ushey, Allaire, and Tang (2024). It is available on CRAN (see https://cran.r project.org/package=reservoirnet) and can be installed using:

```
# Install reservoirnet package from CRAN
install.packages("reservoirnet")
```

Alternatively, it can also be installed from GitHub:

Install reservoirnet package from GitHub
devtools::install_github(repo = "reservoirpy/reservoirR")

- ¹³² For reservoirnet to work, it will require Python version 3.8 or higher, along with the reservoirpy
- ¹³³ module which can be installed with the install_reservoirpy() function:

reservoirnet::install_reservoirpy()

¹³⁴ Reservoir Computing (RC) is well suited to both regression and classification tasks. We will introduce

a simple example for both task.

3.2 Package workflow overview

The workflow of reservoirnet is described in Figure 2. A reservoir model is created by the association of an input layer (a matrix), a reservoir, and an output layer. Both the reservoir and the output layer are created using the function reservoirnet::createNode() by specifying the node type (i.e., either Reservoir or Ridge).

This function accepts several arguments to specify the hyperparameters of the reservoir and will be detailed in future sections. After the reservoir and output layer are created, they can be connected using the %>>% operator, a specific pipe operator dedicated to reservoirnet. The model can then be fitted using reservoirR_fit() and used to make predictions on a new dataset using predict_seq().

145 **3.3 Basic regression use-case**

146 **3.3.1 Covid-19 data**

In this first use-case, we will introduce the fundamental usage of the reservoirnet package. This 147 demonstration will be conducted using the COVID-19 dataset that is included within the package. 148 These data encompass hospitalization, positive RT-PCR (Reverse Transcription Polymerase Chain 149 Reaction) results, and overall RT-PCR data sourced from Santé Publique France, which are publicly 150 available on data.gouv.fr (for further details, refer to help(dfCovid)). Our primary objective is to 151 predict the number of hospitalized patients 14 days into the future. To accomplish this, we will 152 initially train our model on data preceding the date of January 1, 2022, and then apply it to forecast 153 values using the following dataset. 154

We can proceed by loading useful packages - namely ggplot2 Wickham, Navarro, and Pedersen
 (2018) and dplyr Wickham et al. (2023), data and define the task:

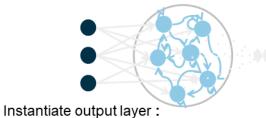
```
# Load usefull packages
library(dplyr)
library(ggplot2)
library(reservoirnet)
# load dfCovid data from the reservoirnet package which contains Covid data
data("dfCovid")
# Set the forecast horizon to 14 days
dist_forecast = 14
# Set the train-test split to 2022-01-01
traintest_date = as.Date("2022-01-01")
```

Due to the substantial fluctuations observed in both RT-PCR metrics, our initial step involves applying a moving average computation over the most recent 7-day periods for these features. Additionally, we augment the dataset by introducing an outcome column and an outcomeDate column, which will serve as valuable inputs for model training. Moreover, we calculate the outcome_deriv as the difference between the outcome and the number of hospitalized patients (hosp), representing the variation in hospitalization in relation to the current count of hospitalized individuals. The resulting smoothed data is visualized in Figure 3.

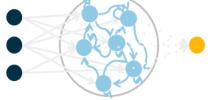


Instantiate reservoir :

reservoir <- createNode(nodeType = "Reservoir")</pre>

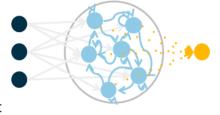


readout <- createNode(nodeType = "Ridge")</pre>



Build model :

model <- reservoir %>>% readout



Fit model :

fit <- reservoirR_fit(node = model, X = X, Y = Y) Forecast: predict_seq(node = fit\$fit, X = X)

Figure 2: Worflow of reservoirnet.

```
outcomeDate = date + dist_forecast,
       # Create a new column 'outcomeDate' which is the current date plus the
       # forecast period (14 days).
       outcome_deriv = outcome - hosp) %>%
       # Create a new column 'outcome_deriv' which is the difference between
       # the predicted outcome and current hospitalizations.
       # This represents the change in hospitalizations over the forecast
       # period.
# rolling average for tested and positive_pcr
mutate_at(.vars = c("Positive", "Tested"),
          .funs = function(x) slider::slide_dbl(.x = x,
                                                  .before = 6,
                                                  .f = mean))
          # Apply a rolling mean (7-day average) to the 'Positive'
                                                                      and
          # 'Tested' columns.
          # The 'slider::slide dbl' function is used to calculate the mean
          # over a window of 7 days (current day + 6 days before). This
          # smooths out daily fluctuations and provides a better trend
          # indicator.
       2000
       1500
                                                                              hosp
       1000
        500
         0
      30000
   value
                                                                              Positive
      20000
      10000
          0
      90000
                                                                             Tested
      60000
      30000
         0
                           2021
                                                 2022
                                                                        2023
                                          date
```

Figure 3: Hospitalizations, number of positive RT-PCR and number of RT-PCR of Bordeaux University Hospital.

164 3.3.2 First reservoir

The objective of this task is to train a RC model using the input features to forecast the number of
 hospitalized patients 14 days ahead, as illustrated in Figure Figure 4.

¹⁶⁷ Setting a reservoir is done with the createNode() function. The important hyperparameters are the ¹⁶⁸ following :

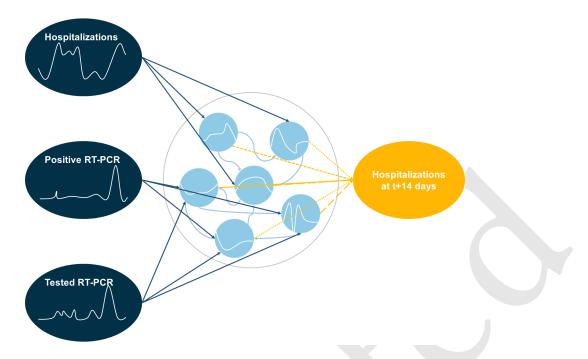


Figure 4: Regression use case: Forecasting the number of hospitalized patients 14 days ahead.

169	• Number of nodes (units) : it corresponds to the number of nodes inside the reservoir. Usually
170	the more the better, but more nodes increases the computation time.
171	• Leaking rate (lr): the leaking rate corresponds to the balance between the new inputs and the
172	previous state. A leaking rate of 1 only consider information from new inputs.
173	• Spectral radius (sr): the spectral radius is the largest eigenvalue in modulus of the reservoir
174	connectivity matrix. A small spectral radius induces stable dynamics inside the reservoir, a
175	high spectral radius induces a chaotic regime inside the reservoir.
176	• Input scaling (input_scaling): the input scaling is a gain applied to the input features of the
177	reservoir.
178	• Warmup (warmup) : it corresponds to the number of time step during which the data are
179	propagating into the reservoir but not used to fit the output layer. This hyperparameter is set
180	in the reservoirR_fit() function.
181 182	In addition, we can set the seed (seed). Because the reservoir connections are set at random, setting the seed is a good approach to ensure reproducibility.
183 184	For this part of the tutorial, we will set the hyperparameter at a given value. Hyperparameter optimization will be detailed at Section 4.
	# Create a reservoir computing node using the 'createNode' function from the
	# reservoirnet package.
	# Arguments:
	# - nodeType = "Reservoir": Specify the type of node to be a reservoir.
	# - seed = 1: Set the seed for reproducibility, ensuring consistent results
	# when the model is run multiple times.
	# - units = 500: Set the number of reservoir units (neurons) to 500.
	# - lr = 0.7: Set the leakage rate (lr) of the reservoir, which controls how

- # quickly the reservoir state decays over time.
- # sr = 1: Set the spectral radius (sr) of the reservoir, which influences the
 # stability and memory capacity of the reservoir.

Then we can feed the data to the reservoir and see the activation state of the reservoir x(t). To do so, we first prepare the data and transform it to a matrix.

```
## select explanatory features of the train set and transform it to an array
X <- dfOutcome %>%
  filter(outcomeDate < traintest_date) %>%
  select(hosp, Positive, Tested) %>%
  as.matrix()
```

Then we run the predict_seq() function. It takes as input a node (i.e a reservoir or a reservoir associated with an output layer) and the feature matrix.

```
# Generate the state of the reservoir using the 'predict_seq' function from the
# reservoirnet package.
# Arguments:
# - node = reservoir: The reservoir computing node created earlier.
# - X = X: The input data matrix containing the features 'hosp', 'Positive',
# and 'Tested'.
# The function computes the state of the reservoir for each time step in the
# input sequence, effectively transforming the input data into the reservoir's
# high-dimensional state space.
reservoir_state <- predict_seq(node = reservoir, X = X)</pre>
```

¹⁸⁹ Now we can visualize node activation using the plot() function presented at Figure 5.

Plot the reservoir state activation over time
plot(reservoir_state)

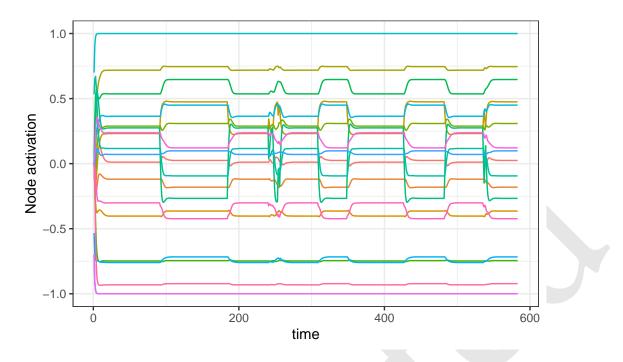


Figure 5: 20 random nodes activation over time.

¹⁹⁰ Numerous nodes within the system exhibit a consistent equilibrium state. The challenge arises when

¹⁹¹ the output layer attempts to extract knowledge from these nodes, as they do not convey meaningful

¹⁹² information. This issue can be attributed to the disparate scales of the features. To address this

¹⁹³ concern, a practical approach involves normalizing the features by dividing each of them by their

respective maximum values, thereby scaling them within the range of -1 to 1 by dividing by the

¹⁹⁵ maximum of the absolute value. Of note, here the features will be scaled between 0 and 1 because all

¹⁹⁶ features are positive.

```
# Standardise features by dividing by the maximum value can improve performance
# After standardisation, all features are on a similar scale which helps RC
stand_max <- function(x) return(x/max(abs(x)))
# scaled features
Xstand <- dfOutcome %>%
filter(date < traintest_date) %>%
select(hosp, Positive, Tested) %>%
mutate_all(.funs = stand_max) %>%
as.matrix() %>%
as.array()
```

¹⁹⁷ We then feed them to the reservoir and plot the node activation again. Compared to Figure 5, the ¹⁹⁸ obtained node activation at Figure 6 shows interesting trend outputs as no node seems saturated.

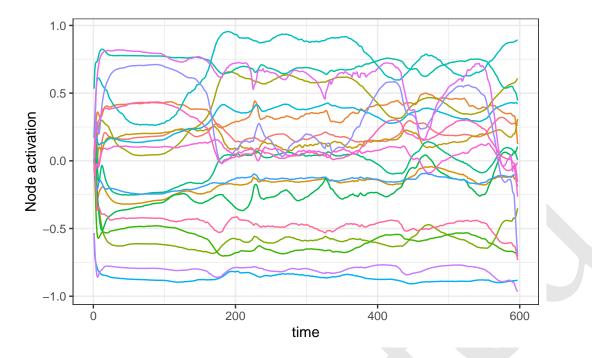


Figure 6: 20 random node activation over time. Scaled features.

199 **3.3.3 Forecast**

In order to train the reservoir, we should train the last layer which linearly combines the neuron's
 output.

202 3.3.3.1 Set the ESN

Initially, we establish the output layer with the createNode() function, incorporating a ridge penalty set at 1e3. It's important to note that this hyperparameter can be subject to optimization, a topic that will be explored in Section 4. This parameter plays a pivotal role in fine-tuning the model's conformity to the data. When set excessively high, the risk of underfitting arises, whereas setting it too low can lead to overfitting. We connect the output layer to the reservoir, with the %>>% operator, making the model ready to be trained.

```
readout <- reservoirnet::createNode(nodeType = "Ridge",</pre>
                                     ridge = 1e3)
# Create a readout node using ridge regression with the 'createNode' function
# from the reservoirnet package.
 Arguments:
#
  - nodeType = "Ridge": Specify the type of node to be a ridge regression
#
#
                        readout.
   ridge = 1e3: Set the regularization parameter (ridge) for the ridge
#
#
                  regression to 1000.
# Ridge regression is used to prevent overfitting by adding a penalty on the
# size of the coefficients.
```

model <- reservoir %>>% readout

Link the reservoir and readout nodes to form a complete reservoir computing
model. The '%>>%' operator connects the high-dimensional state generated by

the reservoir to the readout layer, allowing the model to learn the mapping
from the reservoir states to the target outputs.

209 3.3.3.2 Set the data

²¹⁰ First we separate the train set on which we will learn the ridge coefficients and the test set on which

we will make the forecast. We define the train set to be all the data before 2022-01-01 and the test data to be all the data to have forecast both on train and test sets.

Perform some data management to isolate train and test sets # train set dftrain <- dfOutcome %>% filter(outcomeDate <= traintest_date) yTrain <- dftrain %>% select(outcome) yTrain_variation <- dftrain %>% select(outcome_deriv) xTrain <- dftrain %>% select(hosp, Positive, Tested) # test set xTest <- dfOutcome %>% select(hosp, Positive, Tested)

We standardize with the same formula as seen before. We learn the standardization on the training set and apply it on the test set. Then we convert the dataframe to matrix.

```
# copy train and test sets
xTrainstand <- xTrain
xTeststand <- xTest
# standardise based on training set values
ls_fct_stand <- apply(xTrain,</pre>
                       MARGIN = 2,
                       FUN = function(x) function(feature) feature/(max(x)))
lapply(X = names(ls_fct_stand),
       FUN = function(x){
         xTrainstand[,x] <<- ls_fct_stand[[x]](feature = xTrain[,x])</pre>
         xTeststand[,x] <<- ls_fct_stand[[x]](feature = xTest[,x])</pre>
         return()
       })
# convert to array
lsdf <- lapply(list(yTrain = yTrain,</pre>
                     yTrain_variation = yTrain_variation,
                     xTrain = xTrainstand,
                     xTest = xTeststand),
                function(x) as.matrix(x))
```

215 3.3.3.3 Train the model and predict

²¹⁶ We then feed the reservoir with the train set using the reservoirR_fit() function. To do so, we set

a warmup of 30 days during which the data are propagating into the reservoir but not used to fit the

218 output layer.

²¹⁹ Now that the ridge layer is trained, we can forecast using the predict_seq() function. We set the

²²⁰ parameter reset to TRUE in order to clean the reservoir from the data used by the training set.

```
# Forecast with the trained reservoir on the test data
vec_pred <- reservoirnet::predict_seq(node = fit$fit,</pre>
                                      X = lsdf$xTest,
                                      reset = TRUE)
# Make figure to represent forecast on the train and test sets.
dfOutcome %>%
 mutate(pred = vec_pred) %>%
  na.omit() %>%
  ggplot(mapping = aes(x = outcomeDate)) +
  geom_line(mapping = aes(y = outcome,
                          color = "observed")) +
 geom_line(mapping = aes(y = pred,
                          color = "forecast")) +
  annotate("rect",
           xmin = traintest_date,
           xmax = max(dfOutcome$outcomeDate, na.rm = T),
           ymin = 0,
           ymax = max(dfOutcome$outcome, na.rm = T)*1.1,
           alpha = .2) +
  annotate("text", label = "Test set",
           x = as.Date("2022-08-01"), y = 2200, size = 7)
  annotate("text", label = "Train set",
           x = as.Date("2021-03-01"), y = 2200, size = 7) +
  scale_color_manual(values = c("#3772ff", "#080708")) +
  theme_minimal() +
  labs(color = "", x = "Date", y = "Hospitalizations")
```

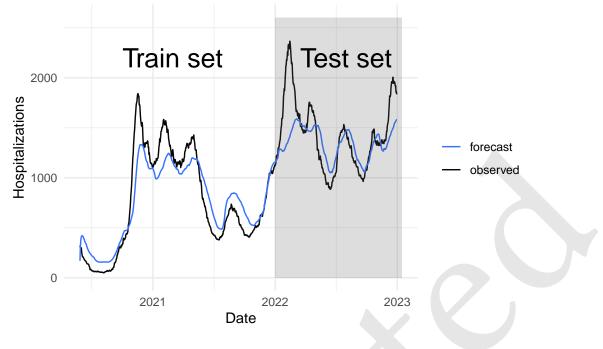


Figure 7: Forecast

We observe that the model forecast at Figure 7 is not fully accurate, both on the test set and the train set. In that case, one option could be to reduce ridge penalization to fit more closely the data,

train set. In that case, one option could be to reduce ridge penalization to fit more closely the data, the optimization of ridge hyperparameter will be discussed at Section 4. Another possibility is to

ease the learning of the algorithm by forecasting the variation of the hospitalization instead of

the number of hospitalized patients. For that step, we will learn on the outcome_deriv contained

in yTrain_variation data which is defined outcome as outcome_deriv = outcome - hosp. As

²²⁷ depicted at Figure 8, this strategy improved the model forecast.

```
## Fit reservoir on outcome variation instead of raw outcome
fit2 <- reservoirnet::reservoirR_fit(node = model,</pre>
                                       X = lsdf$xTrain,
                                      Y = lsdf$yTrain_variation,
                                       warmup = 30,
                                       reset = TRUE)
## Get the forecast on the test set
vec_pred2_variation <- reservoirnet::predict_seq(node = fit2$fit,</pre>
                                                   X = lsdf$xTest,
                                                   reset = TRUE)
## Transform the outcome variation forecast into hospitalization forecast
vec_pred2 <- vec_pred2_variation + xTest$hosp</pre>
## Plot the results
dfOutcome %>%
  mutate(Raw = vec_pred,
         Variation = vec_pred2) %>%
  tidyr::pivot_longer(cols = c(Raw, Variation),
                      names_to = "Outcome_type",
                       values_to = "Forecast") %>%
  na.omit() %>%
```

```
ggplot(mapping = aes(x = outcomeDate)) +
geom_line(mapping = aes(y = outcome,
                        color = "observed")) +
geom_line(mapping = aes(y = Forecast,
                        color = "Forecast")) +
annotate("rect",
         xmin = traintest_date,
         xmax = max(dfOutcome$outcomeDate, na.rm = T),
         ymin = 0,
        ymax = max(dfOutcome$outcome, na.rm = T)*1.1,
         alpha = .2) +
annotate("text", label = "Test set",
         x = as.Date("2022-08-01"), y = 2200, size = 5) +
annotate("text", label = "Train set",
         x = as.Date("2021-03-01"), y = 2200, size = 5) +
facet_wrap(Outcome_type ~ .,
           labeller = label_bquote(cols = "Outcome" : .(Outcome_type))) +
scale_color_manual(values = c("#3772ff", "#080708"))
theme_minimal() +
theme(legend.position = "bottom") +
labs(color = "", x = "Date", y = "Hospitalizations")
```

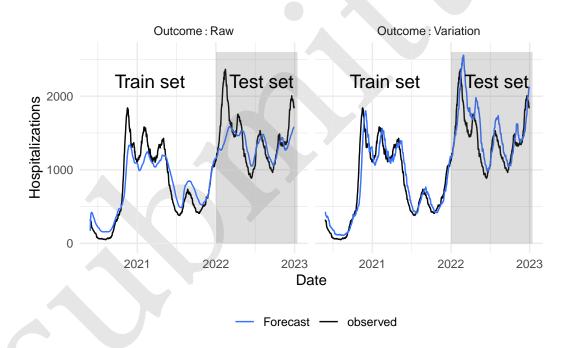


Figure 8: Covid-19 hospitalizations forecast. The model is either trained to forecast the number of hospitalizations (denoted Raw) or the variation of the hospitalizations compared to current level of hospitalisation (denoted Variation)

228 3.4 Classification

229 3.4.1 The Japanese vowel dataset

²³⁰ This example is largely inspired from the classification tutorial of reservoirpy. To illustrate the

classification task, we will use the Japanese vowel dataset (Kudo, Toyama, and Shimbo (1999)). The

232 data can be loaded from reservoirnet as follow :

```
# Get the Japanese vowels dataset using the 'generate_data' function from the
# reservoirnet package.
# The dataset contains preprocessed features and labels for classification.
# Then we isolate train and test sets
japanese_vowels <- reservoirnet::generate_data(dataset = "japanese_vowels")[[1]]
X_train <- japanese_vowels$X_train
Y_train <- japanese_vowels$Y_train
X_test <- japanese_vowels$X_test
Y_test <- japanese_vowels$Y_test</pre>
```

²³³ The dataset comprises 640 vocalizations of the Japanese vowel æ, contributed by nine distinct

speakers. Each vocalization represents a time series spanning between 7 and 29 time steps, encoded
 as a 12-dimensional vector denoting the Linear Prediction Coefficients (LPC). A visual representation

- of six distinct utterances from the test set, originating from three different speakers, is depicted in
- ²³⁷ Figure 9.

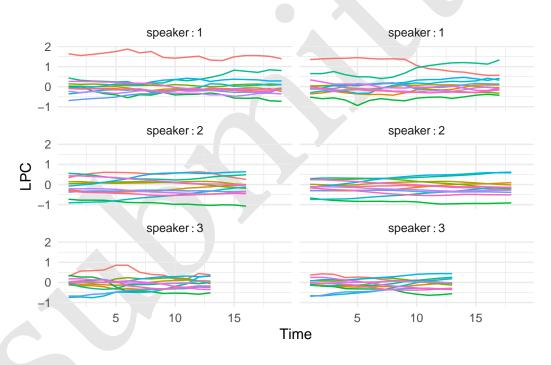


Figure 9: Vowel dataset, sample with 3 speakers and 2 utterance each.

The primary objective involves the attribution of each utterance to its respective speaker, this is denoted as classification or sequence-to-vector encoding. The secondary objective involves the attribution of each time step of each utterance to its speaker, this is denoted as transduction or sequence-to-sequence encoding. While this second approach may seem somewhat superfluous in this context, it could be useful, for example, in cases where multiple speakers take turns speaking, allowing us to identify which sequence belongs to each individual speaker. Figure Figure 4 illustrates

²⁴⁴ this task.

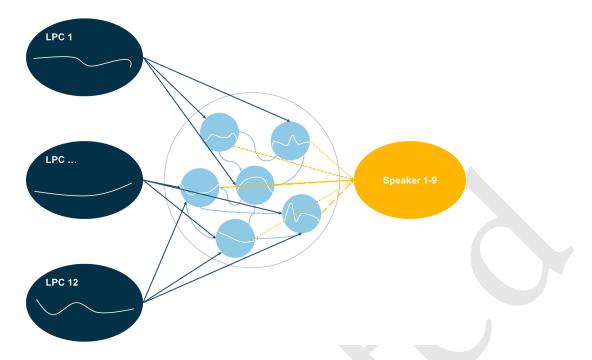


Figure 10: Classification use-case, identifying the speaker from an utterance.

245 3.4.2 Classification (sequence-to-vector model)

The first approach is the sequence-to-vector encoding. For this task we aim to predict the speaker of

the whole utterance (i.e the label is assigned to the whole sequence). We first start by creating the
reservoir and the output layer using createNode() function.

```
reservoir <- reservoirnet::createNode("Reservoir", units = 500,</pre>
                                      lr=0.1, sr=0.9,
                                      seed = 1)
# Create a reservoir computing node with 500 units using the 'createNode'
# function from the reservoirnet package.
# Arguments:
# - units = 500: Set the number of reservoir units (neurons) to 500.
# - lr = 0.1: Set the leakage rate (lr) of the reservoir to 0.1, controlling
#
              how quickly the reservoir state decays over time.
# - sr = 0.9: Set the spectral radius (sr) of the reservoir to 0.9, influencing
              the stability and memory capacity of the reservoir.
#
# - seed = 1: Set the seed for reproducibility, ensuring consistent results
             when the model is run multiple times.
#
readout <- reservoirnet::createNode("Ridge",ridge=1e-6)</pre>
# Create a readout node using ridge regression with the 'createNode' function
# from the reservoirnet package.
# Arguments:
# - ridge = 1e-6: Set the regularization parameter (ridge) for the ridge
#
                  regression to 1e-6.
# Ridge regression is used to prevent overfitting by adding a penalty on the
# size of the coefficients.
```

To perform this task, we need to modify the training and testing processes. Leveraging the inherent inertia of the reservoir, information from preceding time steps is preserved, effectively endowing the

- ²⁵¹ RC with a form of memory. Consequently, the final state vector encapsulates insights gathered from
- ²⁵² all antecedent states. In the context of the sequence-to-vector encoding task, only the final state is
- used. To simplify this process, we introduce the last_reservoir_state() function, which extracts
- the final reservoir state. This process is executed as follows:

```
states_train <- reservoirnet::last_reservoir_state(node = reservoir, X = X_train)</pre>
```

Then, we use only the final state for prediction. We first extract the final state using the last_reservoir_state() function and then use the trained readout to predict the vowel using the predict_seq() function with the seq_to_vec parameter set to TRUE:

```
# Fit the reservoir using the last state vector (each observation is the whole
# vowel sequence)
res <- reservoirnet::reservoirR_fit(node = readout, X = states_train, Y = Y_train)</pre>
```

²⁵⁸ Then we can perform the prediction using only the final state. We first get the final state using

- ²⁵⁹ the last_reservoir_state() function and use the trained readout to predict the vowel using the
- ²⁶⁰ predict_seq() function with the seq_to_vec parameter set to TRUE.

```
# The operation is repeated for the test set :
states_test <- reservoirnet::last_reservoir_state(node = reservoir, X = X_test)
Y_pred <- reservoirnet::predict_seq(node = readout, X = states_test, seq_to_vec = TRUE)</pre>
```

Figure 11 shows the prediction for the 6 utterances depicted at Figure 9 where the model correctly identifies the speaker.

bind_rows()

}) %>%

theme_minimal() +
theme(legend.position = "none") +
labs(y = 'Score',
 x = "Speaker")

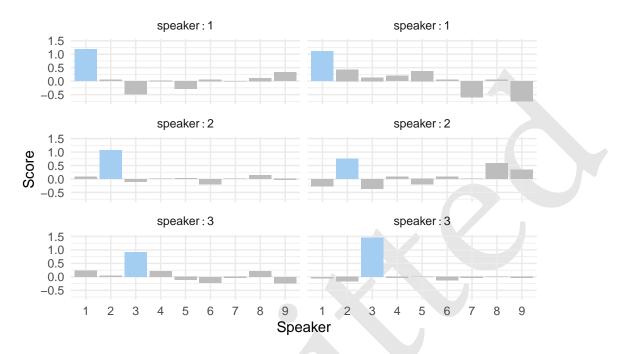


Figure 11: Prediction in a sequence-to-sequence approach 6 samples with 3 speakers and 2 utterance each. The speaker to predict is depicted in blue. For each of the 6 utterance, the model correctly identifies the speaker.

²⁶³ Then, we can also compute the overall accuracy :

3.4.3 Transduction (sequence-to-sequence model)

264

For this task, the goal is to predict the speaker for each time step of each utterance. The first step is to get the data where the label is repeated for each time step. This is easily done with the repeat_targets argument as follow :

²⁶⁹ Then we can train a simple Echo State Network to solve this task. For this example, we will connect

²⁷⁰ both the input layer and the reservoir layer to the readout layer, which is performed by the %>>%

operator. This direct connection between the input layer and the output layer can be particularly

useful when the relationship between the input sequences and the output is partially linear, potentially

²⁷³ improving performance. Section 4 will explore this aspect in more detail through the SARS-CoV-2

```
<sup>274</sup> prediction task.
```

```
# Create an input, a reservoir and an output layers
source <- createNode("Input")
readout <- createNode("Ridge",ridge=1e-6)
reservoir <- createNode("Reservoir",units = 500,lr=0.1, sr=0.9, seed = 1)
# Connect the input layer to the reservoir and connect both the input layer and
# the reservoir to the output layer
model <- list(source %>>% reservoir, source) %>>% readout
```

²⁷⁵ We can then fit the model and predict the labels for the test data. The reset parameter is set to TRUE

²⁷⁶ to remove information from the reservoir from the training process.

From the Y_pred and Y_test we represent at Figure 12 the predictions for the same patients as in Figure 9.

```
pattern = "V", ""),
                            speaker = speaker,
                            uterrance = i,
                            .before = 1) %>%
                     return()
                 }) %>%
  bind_rows()
ggplot(dfplotseqtoseq, mapping = aes(x = Time,
                                     y = pred_speaker,
                                     fill = prediction)) +
  geom_tile() +
  facet_wrap(uterrance ~ speaker,
            labeller = label_bquote(cols = "speaker" : .(speaker)),
            ncol = 2) +
  scale_fill_gradient2(low = "#8ECAE6", high = "#FB8500", mid = "#023047",
                       midpoint = 0) +
  theme_minimal() +
  labs(y = 'Predicted speaker',
      fill = "Prediction score")
```

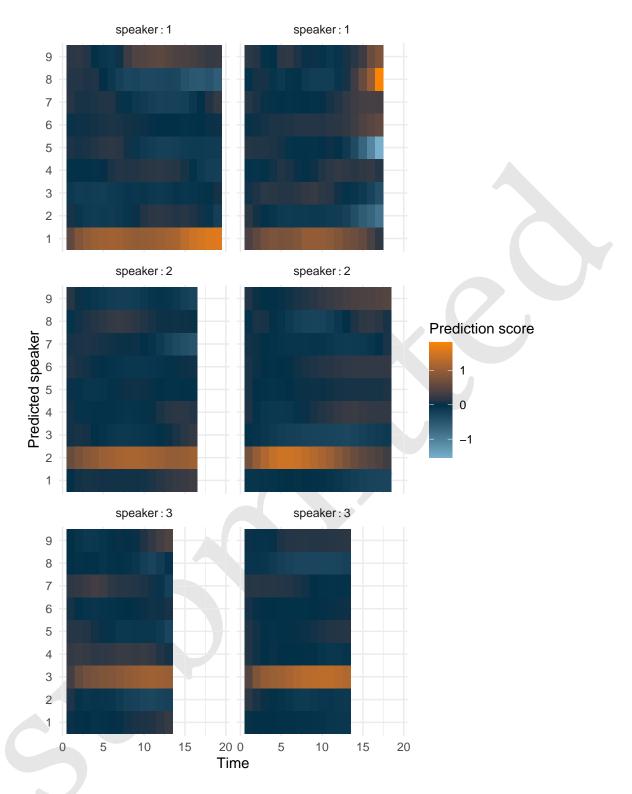


Figure 12: Prediction in a sequence-to-sequence approach 6 samples with 3 speakers and 2 utterance each. The higher the score of the speaker, the lighter the color.

For those 6 utterances, the model correctly identify the speaker for most of the time steps. We can then evaluate the overall accuracy of the model :

Compute the accuracy

281 [1] "Accuracy: 92.456%"

4 Avanced case-study: Covid-19 hospitalizations forecast

283 4.1 Introduction

Since late 2020, millions of cases of SARS-CoV-2 infection have been documented across the globe 284 (World Health Organisation 2020; COVID-19 Cumulative Infection Collaborators 2022; Carrat et al. 285 2021). This ongoing pandemic has exerted significant strain on healthcare systems, resulting in a surge 286 in hospitalizations. This surge, in turn, necessitated modifications to the healthcare infrastructure and 287 gave rise to population-wide lockdown measures aimed at preventing the saturation of healthcare 288 facilities (Simões et al. 2021; Hübner et al. 2020; Kim et al. 2020). The capacity to predict the 280 trajectory of the epidemic on a regional scale is of paramount importance for effective healthcare 290 system management. 291

Numerous COVID-19 forecasting algorithms have been proposed using different methods (e.g en-292 semble, deep learning, mechanistic), yet none has proven entirely satisfactory (Cramer et al. 2022; 293 Rahimi, Chen, and Gandomi 2021). In France, short-term forecasts with different methods have 294 been evaluated with similar results (Paireau et al. 2022; Carvalho et al. 2021; Mohimont et al. 2021; 295 Pottier 2021). In this context a machine learning algorithm based on linear regression with elastic-net 296 penalization, leveraging both Electronic Health Records (EHRs) and public data, was implemented at 297 Bordeaux University Hospital (Ferté et al. 2022). This model, which aimed at forecasting the number 298 of hospitalized patients at 14 days, showed good performance but struggled to accurately anticipate 290 dynamic shifts of the epidemic. 300

RC has been used in the context of covid-19 epidemic forecast (Kmet and Kmetova 2019; Liu et 301 al. 2023; Ray, Chakraborty, and Ghosh 2021; Zhang et al. 2023; Ghosh et al. 2021). Among them, 302 Ghosh et al. (2021), Liu et al. (2023) and Ray, Chakraborty, and Ghosh (2021) used it to forecast 303 epidemic, Zhang et al. (2023) performed sentiment analysis and Kmet and Kmetova (2019) used 304 it to solve optimal control related to vaccine. The evaluation of RC for epidemic forecast showed 305 promising results in all approaches, being competitive with Long-Short Term Memory (LSTM) and 306 Feed-Forward Neural Network (FFNN) in Ray, Chakraborty, and Ghosh (2021). However, the test 307 period was short for Ghosh et al. (2021) (21 and 14 days) and Ray, Chakraborty, and Ghosh (2021) 308 (86 days) making it difficult to evaluate the behavior of the methods during epidemic dynamic shift. 309 This was not the case for Liu et al. (2023) (6 months) but they implemented daily ahead forecast 310 which would be difficult to use to manage a hospital. Finally, all three implementations used only 311 one time series as input whereas it has been shown that using different data sources could improve 312 forecast Ferté et al. (2022). Therefore, it is still difficult to assess the usefulness of RC over a large 313 period and using many time series as inputs. 314

RC can be viewed as an extension of penalized linear regression, where inputs undergo processing by a
 reservoir, introducing the capacity for memory and non-linear combinations. Given the effectiveness

of penalized linear regression in COVID-19 forecasting, as highlighted in Ferté et al. (2022), and the

promising results exhibited by RC in epidemic forecasting, as demonstrated in studies such as Ghosh

et al. (2021), Liu et al. (2023), and Ray, Chakraborty, and Ghosh (2021), we have opted to employ RC

³²⁰ for the prediction of hospitalizations at 14 days at the University Hospital of Bordeaux.

The aim of this study is to showcase the use of reservoirnet for an advanced use case in forecasting the SARS-CoV-2 pandemic in R. Several architectural choices will be evaluated, such as the connection

between the input layer and the output layer, and the use of either individual input scaling per feature

³²⁴ or a common input scaling. The performance of Reservoir Computing (RC) will be compared with

elastic-net penalized regression (identified as the optimal model in Ferté et al. (2022)), while a more

in-depth comparison of performance against other methods can be found in Ferté, Dutartre, Hejblum,

³²⁷ Griffier, Jouhet, Thiébaut, Legrand, et al. (2024).

328 4.2 Methods

329 4.2.1 Data

The study utilized aggregated data spanning from May 16, 2020, to January 17, 2022, regarding 330 the COVID-19 epidemic in France, drawing from various sources to enhance forecasting accuracy. 331 These sources encompassed epidemiological statistics from Santé Publique France, weather data 332 from the National Oceanic and Atmospheric Administration (NOAA), both providing department-333 level data (Smith, Lott, and Vose 2011; Etalab 2020) and Electronic Health Record (EHR) data from 334 the Bordeaux Hospital providing hospital-level data. All data were daily updated. Santé Publique 335 France data included information on hospitalizations, RT-PCR tests, positive RT-PCR results, variant 336 prevalence, and vaccination data, categorized by age groups. NOAA data contributed temperature, 337 wind speed, humidity, and dew point data, allowing for the computation of the COVID-19 Climate 338 Transmissibility Predict Index (Roumagnac et al. 2021). EHRs data included hospitalizations, ICU 339 admissions, ambulance service records, and emergency unit notes, with relevant COVID-19-related 340 concepts extracted from the notes. Data are discussed more in depth in Ferté et al. (2022). 341

First derivative over the last 7 days were computed to enrich model information. To take into account measurement error and daily noise variation, data were smoothed using a local polynomial regression with a span of 21 days. As previously described, input features were scaled between -1 and 1 by dividing the observed value by the maximum of the absolute value of the given input feature.

All data are publicly available. Weather data can be obtained from Smith, Lott, and Vose (2011) using R package worldmet (Carslaw 2023). Vaccine data can be downloaded from Etalab (2020). EHRs data can be downloaded on dryad (Ferté et al. 2023). For privacy issues, publicly available EHRs data below 10 patients were obfuscated to 0. For convenience, all data were downloaded, merged and provided as replication material.

4.2.2 Evaluation framework

The task was to forecast 14 days ahead the number of hospitalized patients. As seen at Section 3.3, we will train the model to predict the variation of hospitalization, denoted as *hosp*, defined as *outcome*_{t+14} = $hosp_{t+14} - hosp_t$ with t = 1, ..., T. Metrics computation and visualizations will be performed on the predicted number of hospitalizations denoted as $hosp_{t+14} = outcome_{t+14} + hosp_t$.

The dataset was separated into two periods. First period from May 16, 2020 to March 1, 2021 served to identify relevant hyperparameters. Remaining data was used to evaluate the model performance.

³⁵⁸ The performance of the model was evaluated according to several metrics:

• the mean absolute error : MAE =
$$\frac{1}{T}\sum_{t=1}^{T} |\hat{hosp}_{t+14} - hosp_{t+14}|$$
.

• the median relative error : MRE = median $\left(\left| \frac{\hat{hosp}_{t+14} - hosp_{t+14}}{hosp_{t+14}} \right| \right)$

• the mean absolute error to baseline : MAEB =
$$\frac{1}{T}\sum_{t=1}^{T} \left(\left| hos p_{t+14} - hos p_{t+14} \right| - \left| hos p_t - hos p_{t+14} \right| \right)$$

• the median relative error to baseline : MREB = median $\left(\left| \frac{hos p_{t+14} - hos p_{t+14}}{hos p_t - hos p_{t+14}} \right| \right)$

Median was chosen over mean for *MRE* and *MREB* because those metrics tend to have extremely high values when the denominator is close to 0 (i.e when the number of hospitalized patients is close to 0 or the number of patients hospitalized at 14 days is close to the current number of hospitalized patients respectively). *MAEB* and *MREB* compare model performance to a baseline model which predicts the current number of hospitalized patients at 14 days. Those metrics help to determine the information added by the model and is a good baseline as covid-19 forecast model do not always outperform this basic forecast (Cramer et al. (2022)).

Because the outcome is obfuscated below 10 hospitalizations for privacy reason, we set both the

outcome and the forecast to 10 when the observed value was 0 or the forecasted value was below 10 when evaluating the model performance.

373 4.2.3 Models

We compared RC to elastic-net penalized regression (denoted as Enet). Furthermore we evaluated RC based on several architectures. First we compared RC with a single input scaling common to all features and a RC with a specific input scaling per feature. Second we compared RC where the input layer is connected to the output layer in addition to the connection between reservoir and output layer. Therefore, five models were evaluated :

- Elastic-net penalized regression denoted *Enet*
- RC with a single input scaling and no connection between input and ouput layers denoted
 Common IS R %»% O
- RC with a single input scaling and connection between input and ouput layers denoted *Common* IS I+R %»% O
- RC with multiple input scaling and no connection between input and ouput layers denoted Multiple IS R %»% O
- RC with multiple input scaling and connection between input and ouput layers denoted *Multiple* IS I+R %»% O

Because of the randomness of the reservoir, we took the median forecast of 10 reservoir on the train set to evaluate the performance of a given hyperparameter set. On the test set we aggregated the forecast of 40 reservoirs, each of them having one of the 40 best hyperparameter sets found on the train set. In addition, because covid-19 hospitalization is a non-stationary process, models were re-trained everyday using all previous days. To ease computation burden, only one day over two was used to find hyperparameters on the training set.

394 4.2.4 Hyperparameter optimisation using random search

RC relies mainly on 4 hyperparameters including the leaking rate (i.e "memory" parameter), spectral
 radius (i.e "chaoticity" parameter), input scaling (i.e "feature gain" parameter) and ridge (i.e penalization parameter). Input scaling can be either, common to all features or specific to each feature which
 increases the number of hyperparameter by the number of features.

- ³⁹⁹ Following the notation from glmnet package (Friedman, Hastie, and Tibshirani 2010), elastic-net
- ⁴⁰⁰ penalized linear regression relies on two hyperparameters, lambda (i.e the penalization parameter)
- and alpha (i.e the compromise between lasso and ridge penalty)

Hyperparameter were selected in the training set (i.e before March 1, 2021) using a wrapper approach
 and a random search sampler using 2000 samples for each model. The sampling distribution were
 defined as follow :

- (RC) ridge and (Enet) lambda : log-uniform law defined between 1e-10 and 1e5
 - (RC) input scaling and spectral radius : log-uniform law defined between 1e-5 and 1e5
- (RC) leaking rate : log-uniform law defined between 1e-3 and 1
- (Enet) alpha : uniform defined between 0 and 1

We provided large search space for all hyper-parameters. Search space was slightly reduced for leaking rate based on previous results and because a leaking rate of 1e-3 already imply that new inputs make the reservoir change really slowly which is not inline with the dynamic of covid-19 but would be appropriate for an application where the phenomena to forecast has a slow dynamic.

Finally, we provided an additional Enet model similar to the one in Ferté et al. (2022) where alpha was set to 0.5 and lambda was re-evaluated everyday in the test set based on previous data using the cross-validation procedure provided by glmnet.

416 4.3 Results

The goal of this task is to predict 14 days ahead the hospitalization. Figure 13 shows both the training 417 set (i.e before 2021-03-01) and the test set where the blue curve correspond to the input features (first 418 derivatives are not shown) and the orange curves correspond to the outcome the model is trained 419 on (i.e the hospitalization variation) and the hospitalizations at 14 days on which the performance 420 metrics are computed. The figures outline that the relation between the input features and the 421 outcome evolve over time and that the time series is not stationary. For instance IPTCC (Index 422 PREDICT de Transmissivité Climatique de la COVID-19) seems correlated to the outcome except that 423 it completely miss the summer 2021 increase. 424

425 4.3.1 Hyperparameter selection

Figure 14 shows the hyperparameter optimisation using random search for the different RC architectures. We observe that model with multiple input scaling achieved better performance on the train set compared to model with single input scaling which is expected as they can adapt more closely to the data thanks to specific input scaling for each feature.

As expected, we observe that the optimal leaking rate is above 1e-2 for all RC which is coherent with the short term dynamic of covid-19 epidemic. Trends for other hyperparameters are less clear even though best hyperparameters sets were close for RC with common input scaling and for RC with multiple input scaling.

Figure 15 shows the hyperparameter search for RC with multiple input scaling and connected input layer. We observe that the random search tends to favor high importance given to derivative of positive RT-PCR (including the elderly) and the derivative of IPTCC. The remaining features do not exhibit a clear pattern.

438 4.3.2 Forecast performance

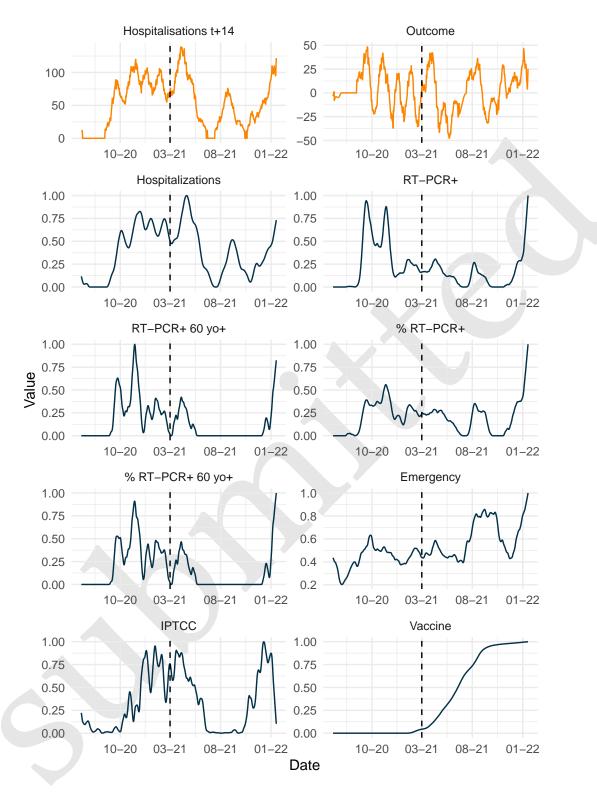


Figure 13: Covid-19 epidemic at BUH. Outcome of interest is presented in orange. Model is trained to forecast Outcome curve which corresonds to the difference between Hospitalisations at 14 days and current hospitalisations. Other features are scaled (divide by the maximum of the feature) represented in darkblue.

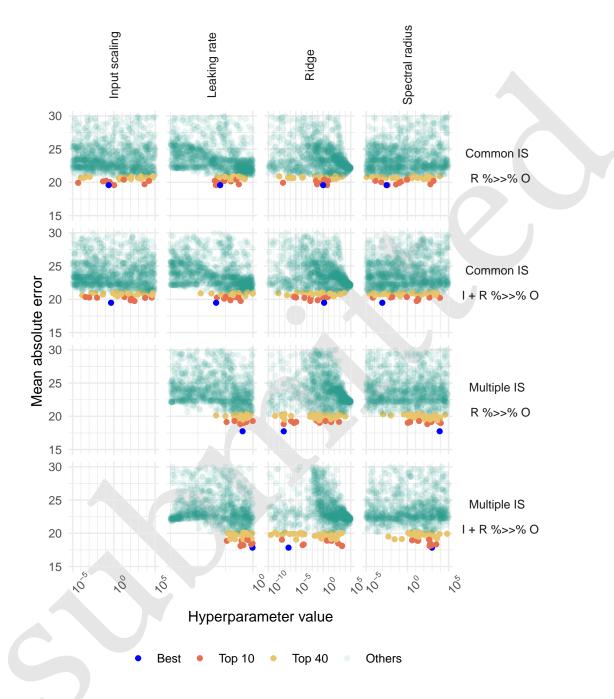


Figure 14: Hyperparameter evaluation on training set by random search. Hp sets with MAE above 30 were removed for clarity of visualisation.

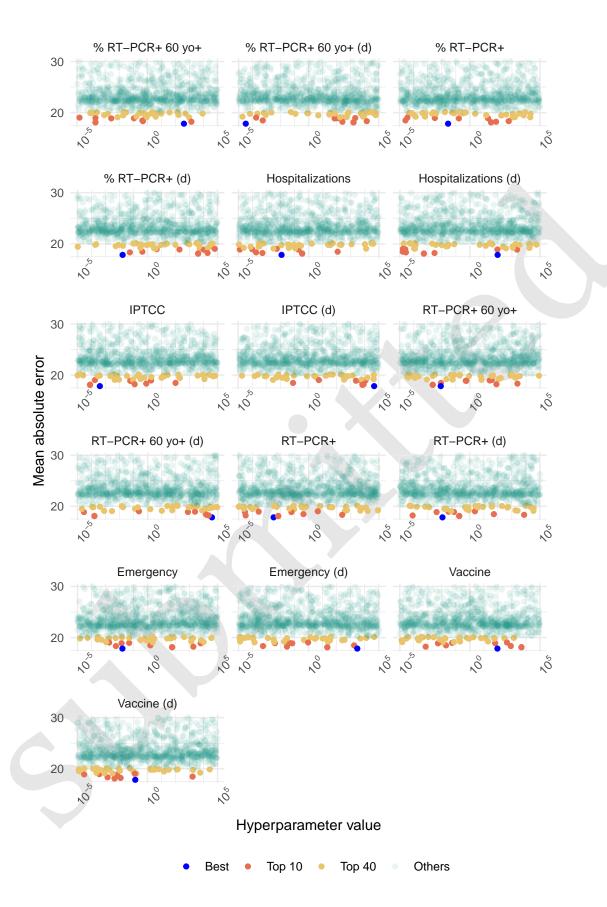


Figure 15: Hyperparameter evaluation on training set by random search of the model with multiple input scaling and no connection between input layer and output layer. Hp sets with MAE above 30 were removed for clarity of visualisation.

Table 1: Model performance with several reservoir configuration. For each setting, 40 reservoirs are computed and the forecast is the median of the 40 forecasts. Results show the performance metrics : MAE = Mean Absolute Error, MRE = Median Relative Error, MAEB = Mean Absolute Error to Baseline, MREB = Median Relative Error to Baseline.

Table 1: Model Performance						
Model	MAE	MRE	MAEB	MREB		
Common IS: R %»% O	15.23	0.26	-3.50	0.85		
Common IS: I + R %»% O	14.84	0.26	-3.89	0.83		
Multiple IS: R %»% O	15.38	0.28	-3.35	0.82		
Multiple IS: I + R %»% O	15.25	0.28	-3.49	0.83		
Elastic-net	16.40	0.29	-2.34	0.93		

Table 1 shows the performance on the test set. Best model according to all metrics was RC with common input scaling and connection between input and output layers. Having one input scaling per

feature did not improve the model which might be due to low generalisability of the hyperparameter of the training set to the test set due to non-stationarity. Additionally, connecting input layer to output layer improved the model forecast. All PC models performed better than the electic performed

output layer improved the model forecast. All RC models performed better than the elastic-netmodel.

Figure 16 shows the forecast of the different models. We note that models struggle to accurately
forecast slope shifts. For instance, summer 2021 initial increase is partially predicted by all models
but its decrease is not well predicted. Winter 2021 increase is anticipated by all models but they tend
to overestimate it because of the rise of vaccine effect.

449 4.3.3 Number of model to aggregate

Figure 17 show the individual forecast for the 40 best sets of hyperparameters of each RC architecture. Due to the internal random connection of the reservoir, we observe forecast stochasticity and relying on only one forecast is unreliable. We explored the number of model needed at Figure 18 which shows that after 10 models, forecast is stable and even 5 models for the simpler model with common input scaling which rely on less hyperparamters.

455 4.3.4 Input feature importance

We compared the coefficients of the output layer estimated for the input layer and the reservoir nodes. Additionally, we compared the coefficient given to the input layer by the output layer in the reservoir and the coefficient estimated by the elastic-net model.

Figure 19 illustrates the ranking of input layer compared to all connections to the output layer, including the 500 reservoir nodes and the 16 features of the input layer (excluding bias). The figure shows that the model with common input scaling tends to assign less weight to input layer compared to the model with multiple input scaling. This suggests that the reservoir with common input scaling provides more information than the reservoir with multiple input scaling, which aligns with its better performance, as shown in Table Table 1.

⁴⁶⁵ Furthermore, Figure 20 compares the coefficients assigned to input features by the elastic-net model

and the RC models. While the coefficients are generally consistent across RC models, there are

some notable differences with elastic-net. Specifically, certain features deemed important by the

elastic-net model, such as the derivative of RT-PCR, and the derivative of Vaccine, are less important

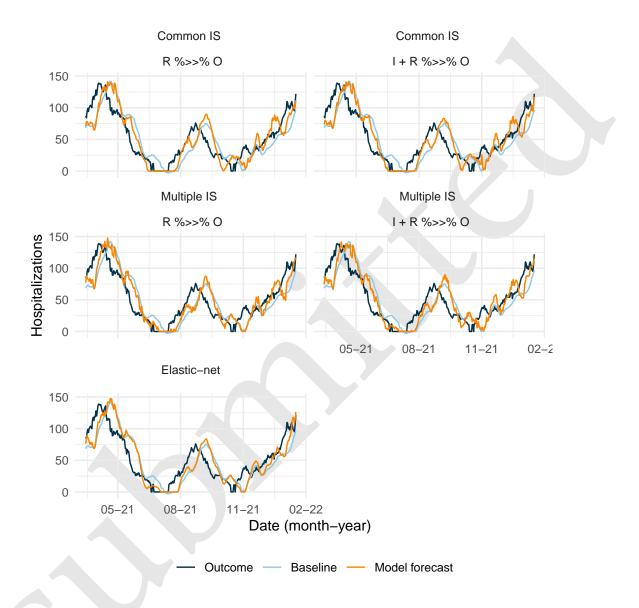


Figure 16: Reservoir computing forecast depending on the setting with and without monthly update. Red line is the median forecast of 40 reservoirs. Grey lines are individual forecast of each of the 40 reservoirs.

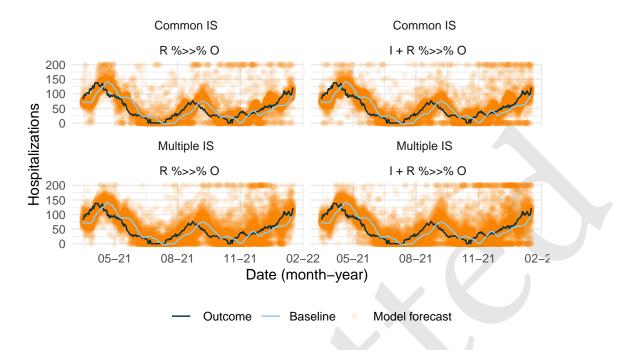


Figure 17: Individual forecast the 40 best hyperparameter sets for the different RC configuration. Forecast value above 200 were set to 200 for clarity.

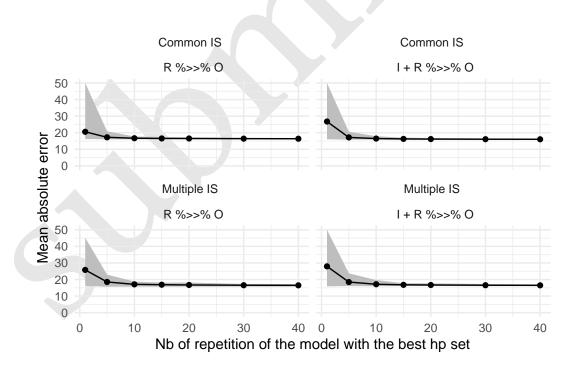


Figure 18: Mean absolute error depending on the number of aggregated reservoir.

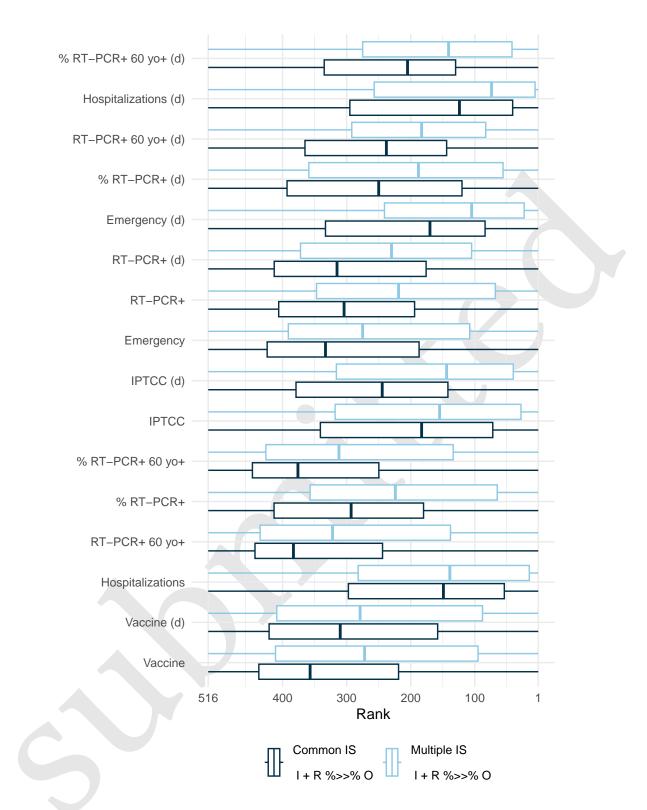


Figure 19: Mean feature importance of the 40 best hyperparameter sets by model, focus on the connection between the input and output layers. Models with direct connection between input and output layer are included. The rank is obtained by comparing the feature input layer and all other connection coefficients (both input and reservoir corresponding coefficients) attributed by the output layer at each date for each hyperparameter set. The higher the output layer's coefficient for the input layer, the closer its rank will be to 1 and the more important the feature is.

for the reservoir computing model. This may indicate that these features predictive ability is better conveyed by their relationship with other features, which is captured by the reservoir computing model but might not be by the elastic-net model. Conversely, emergency, IPTCC, proportion of positive RT-PCR, and hospitalizations are more important for the reservoir computing model than for the elastic-net model.

474 4.4 Discussion

In this specific application, we have demonstrated that RC exhibits commendable performance in
comparison to Elastic-net, which serves as the reference model. Furthermore, we highlight the
inherent challenges in forecasting within this context, primarily stemming from the non-stationarity
of the time series.

All computations in this study were conducted using the reservoirnet package, and the entire codebase is accessible on Zenodo (Ferté, Ba, et al. 2024). This R package demonstrates its efficacy in implementing various reservoir architectures, including connection between the input layer and the output layer, as well as the utilization of several input scaling, all within the context of a real-world use case.

Given the substantial number of hyperparameters involved, we acknowledge that random search may not be the most efficient optimization algorithm. We have retained this approach for the sake of simplicity in this tutorial paper; however, meta-heuristic approaches, particularly those utilizing evolutionary algorithms, may prove more efficient, especially when employing multiple input scaling (Data et al. 2018). Fortá Dutactor, Uniform Lenhet Thidbart Uncert et al. 2024)

(Bala et al. 2018; Ferté, Dutartre, Hejblum, Griffier, Jouhet, Thiébaut, Hinaut, et al. 2024).

This study represents a novel contribution to epidemic forecasting utilizing RC. Notably, previous literature predominantly focused on simpler problems characterized by fewer input features or shorter evaluation periods (Liu et al. 2023; Ray, Chakraborty, and Ghosh 2021; Ghosh et al. 2021). Our findings underscore the potential of this approach for future epidemics, suggesting its potential to surpass more traditional epidemiological tools while maintaining a lightweight model structure compared to other RNNs.

It is worth noting that all models, including those presented in Ferté et al. (2022), face challenges in accurately predicting slope shifts, highlighting the need for further investigation. Specifically, additional work is required to extend the application of Reservoir Computing (RC) to high-dimensional settings, building upon insights gained from models that use a more extensive feature set. While RC has demonstrated promising performance for epidemic forecasting in high-dimensional settings, this task remains challenging (Ferté, Dutartre, Hejblum, Griffier, Jouhet, Thiébaut, Legrand, et al. 2024).

501 5 Discussion and conclusion

In this paper, we introduce the R package reservoirnet, which serves as a versatile tool for implementing reservoir computing based on ReservoirPy's Python library. It offers flexibility in defining the reservoir architecture, including options for specifying connections between the input layer and the output layer, as well as variations in input scaling as demonstrated on a real-world use case.

We provided a comprehensive overview of the basic usage of the reservoirnet package through illustrative examples in regression and classification tasks. This introductory section serves as a foundation for R users, offering step-by-step guidance on constructing and training reservoir computing models using the package. By demonstrating the application of RC in both regression and classification scenarios, we aim to equip users with the essential knowledge and skills needed to harness the capabilities of reservoir computing for diverse tasks.

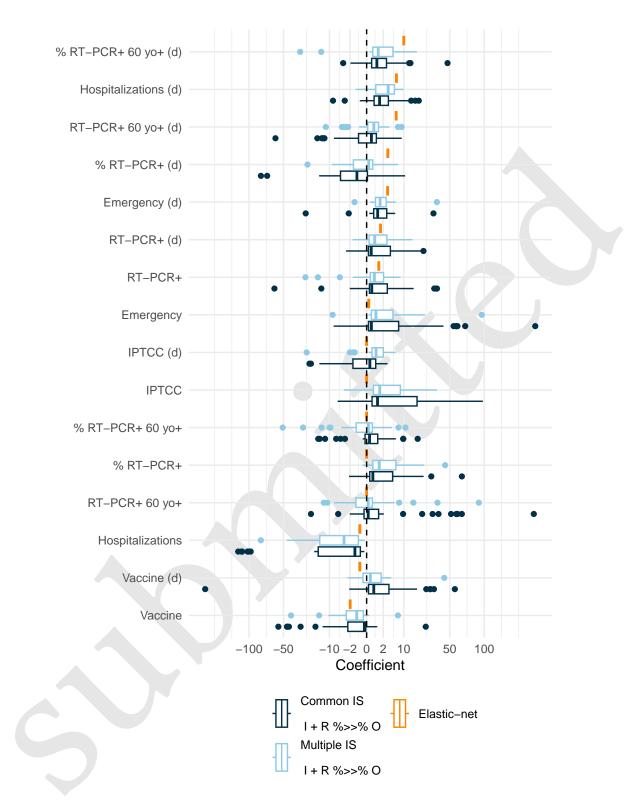


Figure 20: Mean feature coefficient of the 40 best hyperparameter sets by model and the elasticnet model. Only models with direct connection between input and output layer are included. The coefficients were calculated as the average value across all dates for each feature, model and hyperparamet set.

⁵¹² Drawing on the robust foundation of the ReservoirPy structure, a well-maintained Python library,

this package inherits its reliability and longevity. We have focused on providing access to the

⁵¹⁴ fundamental features, building upon the strong base provided by ReservoirPy. Therefore, this initial

version of reservoirnet must evolve in tandem with the growing understanding and adoption of

⁵¹⁶ RC within the R community.

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 d'Aquitaine (see https://www.plafrim.fr), as well as by the MCIA (Mésocentre de Calcul Intensif

522 Aquitain).

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687 Session information

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sessionInfo()
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689
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   Running under: Ubuntu 24.04.2 LTS
690
691
   Matrix products: default
692
            /usr/lib/x86_64-linux-gnu/blas/libblas.so.3.12.0
   BLAS:
693
   LAPACK: /usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.12.0
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   locale:
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     [1] LC_CTYPE=C.UTF-8
                                  LC_NUMERIC=C
                                                           LC_TIME=C.UTF-8
697
     [4] LC_COLLATE=C.UTF-8
                                  LC_MONETARY=C.UTF-8
                                                           LC_MESSAGES=C.UTF-8
698
     [7] LC PAPER=C.UTF-8
                                  LC NAME=C
                                                           LC ADDRESS=C
699
    [10] LC_TELEPHONE=C
                                  LC_MEASUREMENT=C.UTF-8 LC_IDENTIFICATION=C
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```

```
time zone: Etc/UTC
702
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704
   attached base packages:
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                  graphics grDevices datasets utils
   [1] stats
                                                             methods
                                                                        base
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   other attached packages:
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                                                dplyr_1.1.4
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                                                                   renv_1.0.11
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                                                                   xfun_0.49
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                                               knitr_1.49
                                                                   farver_2.1.2
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                                                                   carData_3.0-5
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                            compiler_4.4.1
727
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