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# Sparse Feature Coactivation Reveals Composable Semantic Modules in Large Language Models

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## Abstract

1 We identify semantically coherent, context-consistent network components in large  
2 language models (LLMs) using coactivation of sparse autoencoder (SAE) features  
3 collected from just a handful of prompts. Focusing on country-relation tasks,  
4 we show that ablating semantic components for countries and relations changes  
5 model outputs in predictable ways, while amplifying these components induces  
6 counterfactual responses. Notably, composing relation and country components  
7 yields compound counterfactual outputs (Figure 1). We find that, whereas most  
8 country components emerge from the very first layer, the more abstract relation  
9 components are concentrated in later layers; within relation components themselves,  
10 nodes from later layers tend to have a stronger causal impact on model outputs.  
11 Overall, these findings suggest a modular organization of knowledge within LLMs  
12 and advance methods for efficient, targeted model manipulation.

## 1 Introduction

14 Sparse autoencoders (SAEs) have emerged as a powerful tool for extracting interpretable features  
15 from large language models (LLMs), but it remains unclear how these features integrate across layers  
16 to produce coherent responses. In this work, we uncover modular semantic structures in the form  
17 of networks of coactivating SAE features. Compared to Ameisen et al. [1], our approach does not  
18 require manual grouping of features. We also provide a more granular, feature-level view of the  
19 mechanism identified by Merullo et al. [25]. For a full discussion of related work, see Appendix A.  
20 We focus our analyses on Gemma 2 2B [34], with additional results for Gemma 2 9B in Appendix D.  
21 For each prompt, we collect activations from pre-trained SAEs [21, 3] and select the set of features  
22 that appear in the top-5 activations at any token position for each layer. Second, we construct a  
23 directed graph where nodes are the selected features and an edge connects features in adjacent layers  
24 if their activation patterns have a Pearson correlation over 0.9. Third, to filter out overly generic  
25 features, we prune this graph by removing any feature with an activation density greater than 0.01  
26 according to Neuronpedia [22]. Finally, we identify the resulting weakly connected components  
27 using a standard BFS algorithm [15] and validate their causal role by ablating or amplifying their  
28 activations [27] and measuring the model’s output distribution shift.

## 2 Experimental Results

30 We focused on country-capital, country-currency, and country-language tasks for China, France,  
31 Germany, Japan, Nigeria, Poland, Russia, Spain, the United Kingdom, and the United States. To  
32 collect model activations for each country-capital pair, we used the following prompt template with  
33 in-context examples: “The capital city of Peru is Lima. The capital city of South Korea is Seoul. The

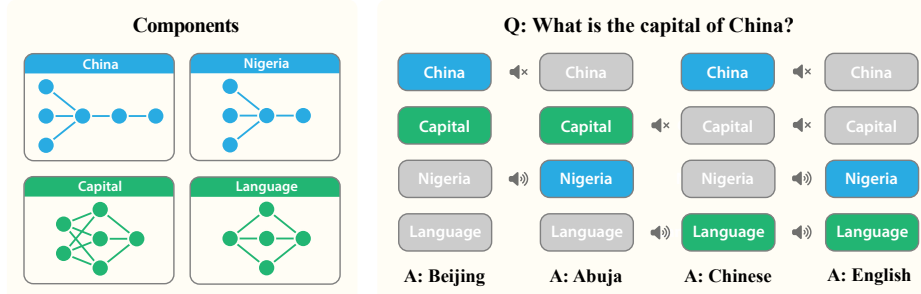


Figure 1: Selective component ablation and amplification steers model toward counterfactual outputs.

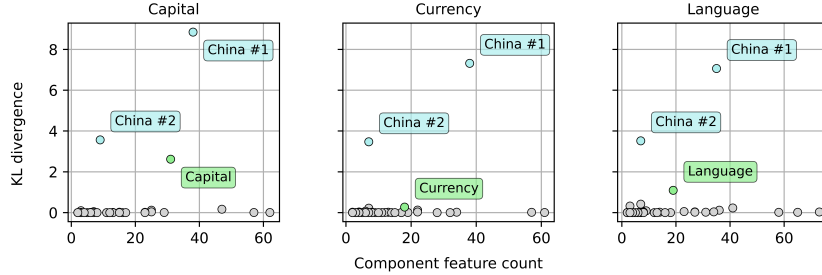


Figure 2: Component feature count ( $x$ -axis) vs. causal effect (KL divergence) when ablated ( $y$ -axis).

34 *capital city of Saudi Arabia is Riyadh. The capital city of {country} is*". Similar templates were used  
 35 for country-currency and country-language pairs.

## 36 2.1 Component Identification

37 For each country-relation pair, we obtained around 70 connected components using the methods  
 38 outlined in Section 1. Typically, two to three of the extracted components exert a markedly higher  
 39 causal effect on the model output than the others (Figure 2).

40 **Semantic coherence.** To evaluate the roles of these top components, we began by inspecting  
 41 their associated feature descriptions from Neuronpedia. In most cases, the features within a given  
 42 component had thematically coherent descriptions, often referring to a common country or relation  
 43 (Appendix C). However, there are exceptions—for instance, none of the high-impact components  
 44 obtained from Spain-related prompts explicitly mention Spain in their feature descriptions. Given  
 45 that feature descriptions are not always reliable, we performed component ablations and observed  
 46 the resulting changes in the model’s top predicted tokens. Table 1 presents results from ablation  
 47 experiments using components obtained from China and Nigeria-related prompts. Promisingly, when  
 48 country components were ablated, the model’s top predicted tokens shifted predictably to the capitals,  
 49 currencies, or languages of other countries. When relation components were ablated, the model  
 50 assigned higher probabilities to country names.

Capital						Currency						Language					
Original		Ctry. Abl.		Rel. Abl.		Original		Ctry. Abl.		Rel. Abl.		Original		Ctry. Abl.		Rel. Abl.	
Beijing	97.	Madrid	39.	the	12.	Yuan	80.	Euro	64.	Yuan	59.	Mandarin	59.	Spanish	49.	Chinese	24.
Be	.38	Warsaw	10.	China	6.7	Ren	14.	Lira	20.	Ren	14.	Chinese	37.	English	22.	China	18.
Peking	.35	Rome	9.5	Beijing	6.4	RMB	1.8	Krone	3.1	Yen	1.9	English	.69	French	6.7	Mandarin	11.
Shanghai	.23	Paris	6.1	Shanghai	5.0	Yen	.98	Franc	2.4	P	1.7	also	.43	German	4.0	also	3.5
Xi	.11	Berlin	5.0	a	2.7	yuan	.53	Peso	1.2	Ba	1.5	Put	.22	Italian	2.7	a	2.9
Abuja	85.	New	7.7	Lagos	17.	Naira	93.	Franc	16.	Naira	62.	English	72.	English	50.	Nigeria	40.
Lagos	11.	Islamabad	7.3	the	12.	N	2.9	Euro	9.1	Dollar	6.0	Ha	11.	French	31.	English	14.
...	.38	Kathmandu	6.0	Nigeria	7.1	Nai	2.5	D	7.4	Niger	4.3	Yoruba	4.7	Spanish	2.1	Nigerian	9.8
Nigeria	.29	Delhi	5.7	called	5.1	naira	.36	Pound	5.1	Currency	2.4	Igbo	2.4	Arabic	2.0	...	2.9
...	.27	Tehran	4.9	Abuja	3.4	K	.23	Krone	4.8	Nai	1.4	Nigerian	1.6	Dutch	1.1	also	2.3

Table 1: Top five output tokens and their likelihoods for China (top) and Nigeria (bottom) across all three relations, before and after ablating the relevant country or relation component.

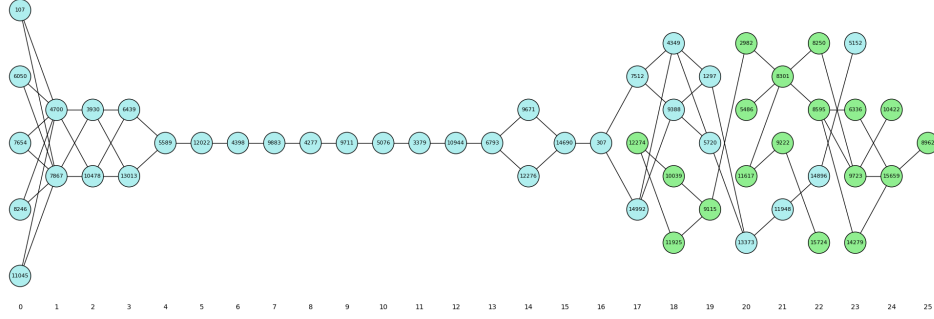


Figure 3: China (blue) and language (green) components.

Capital, China				Currency, China				Language, China			
·, Nigeria	Currency, ·	Language, ·	·, Nigeria	Capital, ·	Language, ·	·, Nigeria	Capital, ·	Currency, ·	·, Nigeria	Capital, ·	Currency, ·
_Abuja 87.	_Yuan 15.	_Mandarin 32.	_Naira 75.	_Beijing 98.	_Chinese .35	_English 71.	_Beijing 96.	_Yuan 15.			
_Nigeria 4.6	_yuan 12.	_Chinese 27.	_naira 8.3	_Be .75	_Mandarin .33	_Yoruba 5.6	_Be 1.5	_Ren 10.			
_Lagos 3.9	_RMB 11.	_English 25.	_Nai 3.7	_BE .34	_English .28	_Ha 4.8	_Peking .83	_RMB 6.8			
-.58	_Ren 5.6	_Spanish 2.2	_Nigeria 3.3	_Peking .27	_Simplified .82	_Nigeria 4.4	Beijing .42	_yuan 6.3			
-.57	_China 5.4	_mandarin 2.1	_Nigerian 2.4	Beijing .25	_Spanish .79	_Igbo 3.4	_BE .30	_The 5.3			

Table 2: Top five output tokens and likelihoods for prompts about China after ablating an in-prompt component and amplifying a target country or relation.

51 **Context consistency.** We found that country and relation components are remarkably consistent  
52 across different contexts. Therefore, in subsequent experiments, we define each country component  
53 as the intersection of all the components for that country across relations; similarly, each relation  
54 component is defined as the intersection of all the components for that relation across countries.  
55 Figure 3 shows the resulting China and Language components.

## 56 2.2 Component Steering

57 Having identified distinct graph components for each country and relation, we next investigate  
58 whether these components can be used to steer model outputs individually and in combination. To test  
59 whether components generalize across different contexts, we applied a test prompt template different  
60 from the one used to collect the initial activations: “*Q: What is the {capital city of / currency of /*  
61 *main language in} {country}? Answer directly (two words max). A:*”.

62 **Country steering.** By ablating an *in-prompt country* component and amplifying a *target country*  
63 component, we successfully directed the LLM to respond to questions about the capital, currency, and  
64 language of the in-prompt country with *counterfactual answers*, i.e., the capital, currency, or language  
65 for the target country, which is not actually queried in the prompt. As shown in Table 2, when we  
66 ablated the China component and amplified the Nigeria component, the model consistently responded  
67 with the desired counterfactual answers “*Abuja*”, “*Naira*”, and “*English*” for capital, currency, and  
68 language questions, respectively—disregarding the prompt’s reference to China. Overall, country  
69 steering successfully produced the desired counterfactual answers 96% of the time (Table 3). This  
70 confirms that our identified country components encode country-specific information that causally  
71 determines model outputs.

72 **Relation steering.** Similarly, by ablating an *in-prompt relation* while amplifying a *target relation*,  
73 we successfully directed the model to respond to queries about the *in-prompt relation* as though they  
74 concerned the *target relation*. As shown in Table 2, with the capital component ablated, the model  
75 answered a question about China’s capital with “*Yuan*” and “*Mandarin*” when currency and language  
76 components were respectively amplified. We observed similar results for currency and language  
77 prompts. The average success rate for relation steering is 92% (Table 3).

CN	FR	DE	JP	NG	PL	RU	ES	UK	US	Avg.	Cap.	Curr.	Lang.	Avg.
1.00	1.00	1.00	1.00	1.00	0.78	1.00	0.78	1.00	1.00	0.96	0.95	0.90	0.90	0.92

Table 3: Steering success rates for each target country and relation.

Capital, China				Currency, China				Language, China			
Currency, Nigeria		Language, Nigeria		Capital, Nigeria		Language, Nigeria		Capital, Nigeria		Currency, Nigeria	
_Naira	34.	_English	71.	_Abuja	70.	_English	93.	_Abuja	49.	_Naira	40.
_Nigeria	28.	_French	5.1	_Lagos	26.	_French	1.7	_Lagos	46.	_Nigeria	18.
_naira	13.	_Yoruba	4.1	-	2.3	_Yoruba	1.5	-	1.7	_Dollar	6.2
_N	4.1	_Spanish	3.8	_Nigeria	.41	_Spanish	1.1	_Nigeria	.78	_naira	4.7
-	3.2	_Igbo	3.0	...	.30	_Igbo	.55	...	.36	-	3.7

Table 4: Top five output tokens and likelihoods for prompts about China after ablating both in-prompt components (row 1) and amplifying a target country-relation pair (row 2).

Ctry. / Rel.	CN	FR	DE	JP	NG	PL	RU	ES	UK	US	Avg.
Capital	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
Currency	1.00	0.94	1.00	0.72	0.61	0.50	0.11	0.94	1.00	1.00	0.78
Language	0.50	1.00	1.00	1.00	1.00	0.78	1.00	1.00	1.00	1.00	0.93
Average	0.83	0.98	1.00	0.91	0.87	0.76	0.70	0.98	1.00	1.00	0.90

Table 5: Composite steering success rates for each target country-relation pair.

**Composite steering.** We conducted composite steering experiments where both country and relation components were manipulated at once. By ablating both the *in-prompt country* and *in-prompt relation* components while amplifying the *target country* and *target relation* components, it is indeed possible to steer the model to ignore both the *in-prompt country* and *in-prompt relation* and answer about a different country-relation pair. Table 4 provides specific examples of composite steering success. As shown in the first column, when we ablated both the China and capital components while amplifying the Nigeria and currency components, the model correctly answered “Naira” despite being asked about China’s capital. The average steering success rate for composite steering is 90% (Table 5).

## 2.3 Component Organization

Having established the causal role and composability of country and relation components, we next analyze their distribution across network layers and the relative importance of individual nodes within these components. To quantify the causal importance of an individual country node, we compute the average post-ablation KL divergence from the original output distribution across all relations. For a relation node, we compute the same average across all countries. Country and relation components show distinct distribution patterns across model layers. Eight out of the ten country components tested begin in the first layer of the network; some (e.g., China) span nearly all layers, while others (e.g., Nigeria) concentrate in early to middle layers. In contrast, all three relation components appear only in later layers of the network (Figure 4). This suggests that representations of concrete entities are established earlier in processing, while those of abstract relational concepts emerge later. Not only do all three relation components concentrate in later layers, but we find that, even within each relation component, nodes from later layers tend to have a stronger causal impact on model outputs. This is not the case for country nodes, which exhibit variable relationships between layer depth and KL divergence ranging from positive to negative.

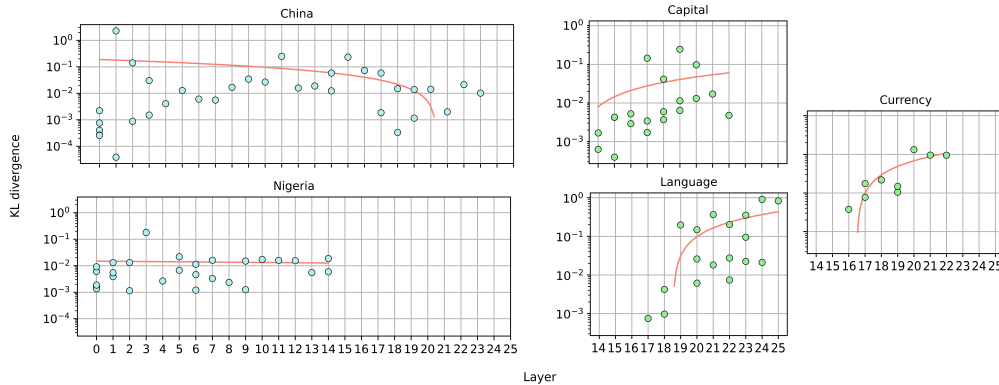


Figure 4: Node-wise KL divergence between pre- and post-ablation output token distributions.

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## A Related Work

Mechanistic interpretability aims to reverse-engineer neural networks into human-interpretable algorithms. Central to this field is the hypothesis that large networks can be understood as compositions of subnetworks, known as circuits, that perform specific functions [11, 28, 33]. Early efforts involved manual identification of circuits for specific tasks such as numerical comparison [16] and indirect object recognition [35]. Work on in-context learning revealed specialized mechanisms like induction heads, which detect repeated subsequences and predict their completion [29]. To improve scalability, automated circuit discovery methods were developed, including path patching [14], ACDC [6], CD-T [18], and edge pruning [2]. However, these approaches are often computationally expensive and can yield circuits that are difficult for humans to interpret.

The theory of superposition proposes that networks represent more features than dimensions by encoding sparse features across polysemantic neurons [10]. Dictionary learning techniques such as SAEs promise greater interpretability by extracting monosemantic features from polysemantic neurons [5, 19]. However, standard SAEs face challenges such as inconsistent feature quality, poor reconstruction, and weak functional alignment—issues that recent work has sought to address through architectural and training improvements [4, 31, 32]. SAEs have also allowed circuit discovery to operate on interpretable features instead of neurons [23]. Circuit tracing efforts by Anthropic [1] utilized transcoders [9], an alternative approach for extracting human-interpretable features from LLMs. Despite these advances, high computational costs remain a significant barrier. More recently, coactivation patterns have been explored for understanding SAE feature organization. Li et al. [20] analyzed the geometry of SAE features, finding spatial clustering of related concepts. Building on this approach, we construct directed graphs based on feature coactivation and introduce node pruning based on activation density. This allows us to discover semantically coherent, context-consistent connected components that can influence model outputs individually or in combination. Our approach offers a computationally efficient framework for analyzing and controlling LLM behavior without exhaustive circuit tracing.

Factual knowledge is believed to reside in the feedforward layers of transformer-based LLMs. Geva et al. [13] characterized these layers as key-value memories mapping textual patterns to vocabulary distributions. Dai et al. [7] identified “knowledge neurons” whose activations correlate with specific facts. These insights have informed approaches for editing factual knowledge stored in LLMs [8, 26, 24]. Geva et al. [12] described the recall of factual associations as a three-step process involving subject enrichment, relation propagation, and attribute extraction. Hernandez et al. [17] demonstrated that relation decoding in transformers can be approximated by simple linear transformations. Merullo et al. [25] showed that LLMs implement Word2Vec-style vector arithmetic to solve some relational tasks. Recent work on “knowledge circuits” has begun tracing causal pathways underlying factual recall [36, 30]. Leveraging SAEs, our method offers a more human-interpretable analysis of LLMs’ knowledge organization by identifying emergent connected components that correspond to task-related concepts.

## B Model and Hyperparameter Selection

Our choice of LLMs was constrained to those with pretrained SAEs available via Neuronpedia. We did not use smaller models like GPT-2, as they demonstrated a weaker grasp of the factual concepts under investigation (e.g., confusing Lagos, Nigeria’s largest city, with its capital) and an inability to follow in-context instructions to shorten their answers.

For individual country and relation steering, we selected steering strengths  $\alpha_c, \alpha_r$  from  $\{k \cdot 0.05 : k \in \mathbb{Z}\} \cap (0, 1]$  that achieved the highest respective success rates. For composite steering, we selected the  $(\alpha'_c, \alpha'_r)$  pair from  $\{\alpha_c - 0.05, \alpha_c, \alpha_c + 0.05\} \times \{\alpha_r - 0.05, \alpha_r, \alpha_r + 0.05\}$  that achieved the highest success rate. This procedure yielded parameters  $\alpha_c = 0.1, \alpha_r = 0.45, \alpha'_c = 0.15$ , and  $\alpha'_r = 0.45$ .

## C Component Feature Visualizations

Figure 5 shows word clouds for LLM-generated descriptions [22] of SAE features within the China, capital, currency, and language components.

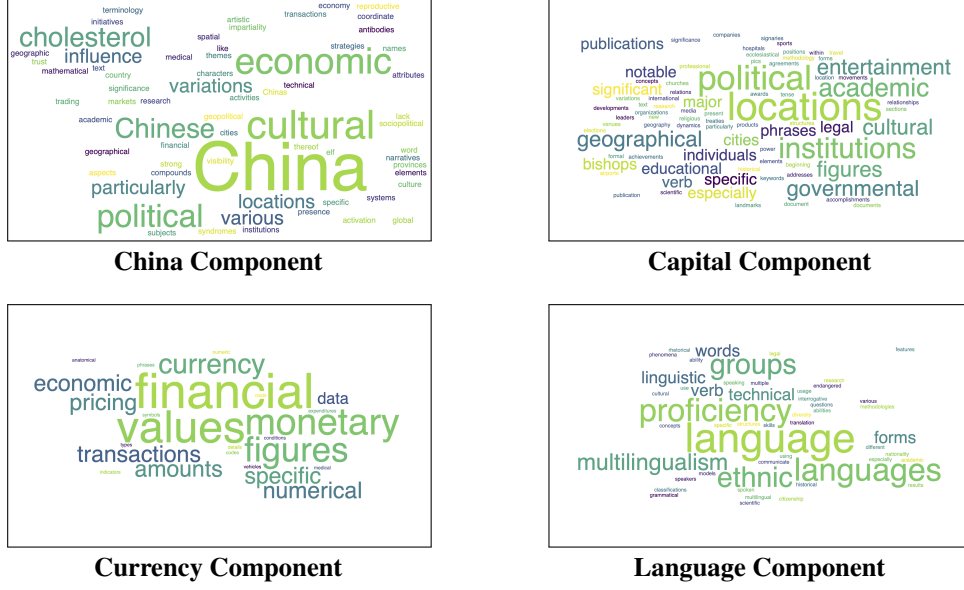


Figure 5: Component word clouds.

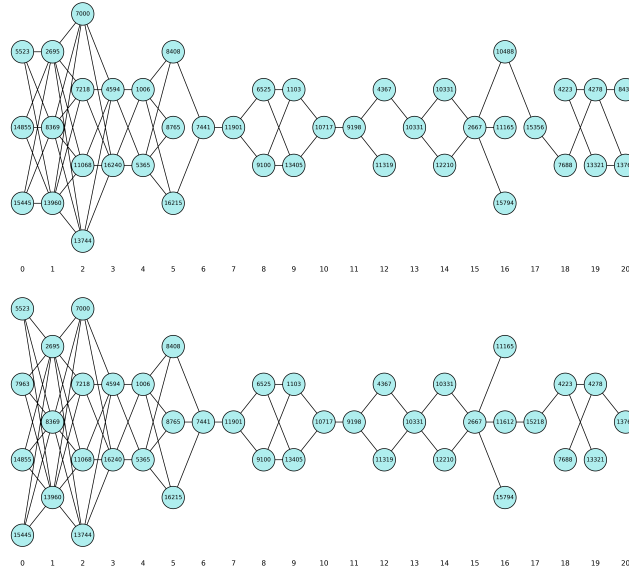


Figure 6: China components extracted from capital and currency prompts (Gemma 2 9B).

## 307 D Gemma 2 9B Results

308 We replicated all experiments using Gemma 2 9B. Results closely mirrored those observed with  
 309 Gemma 2 2B. The model showed context consistency, with similar country components across  
 310 relations (Figure 6) and similar relation components across countries (Figure 7). High success rates  
 311 were achieved for country (93%), relation (97%), and composite (92%) steering (see Tables 6-7).

CN	FR	DE	JP	NG	PL	RU	ES	UK	US	Avg.	Cap.	Curr.	Lang.	Avg.
1.00	0.78	0.85	1.00	0.89	0.81	1.00	0.96	1.00	0.96	0.93	0.90	1.00	1.00	0.97

Table 6: Steering success rates for each target country and relation (Gemma 2 9B).

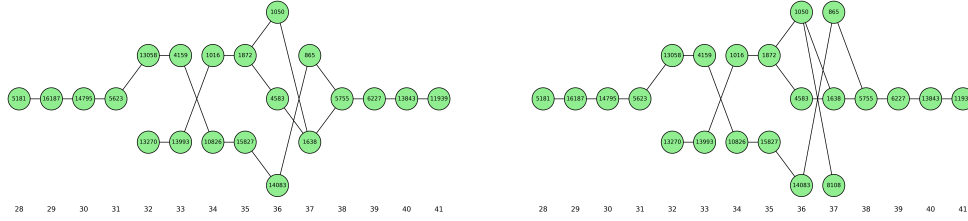


Figure 7: Language components extracted from China and Nigeria prompts (Gemma 2 9B).

<i>Ctry. / Rel.</i>	CN	FR	DE	JP	NG	PL	RU	ES	UK	US	Avg.
<i>Capital</i>	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
<i>Currency</i>	1.00	1.00	1.00	0.72	1.00	0.50	0.11	0.94	1.00	1.00	0.83
<i>Language</i>	0.50	1.00	1.00	1.00	1.00	0.78	1.00	1.00	1.00	1.00	0.93
<i>Average</i>	0.83	1.00	1.00	0.91	1.00	0.76	0.70	0.98	1.00	1.00	0.92

Table 7: Composite steering success rates for each target country-relation pair (Gemma 2 9B).

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