Evaluating Task-Oriented Dialogue Consistency through Constraint Satisfaction

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Abstract

 Task-oriented dialogues must maintain consis- tency both within the dialogue itself, ensuring logical coherence across turns, and with the conversational domain, accurately reflecting ex- ternal knowledge. We propose to conceptualize dialogue consistency as a Constraint Satisfac- tion Problem (CSP), wherein variables repre- sent segments of the dialogue referencing the conversational domain, and constraints among variables reflect dialogue properties, including linguistic, conversational, and domain-based aspects. To demonstrate the feasibility of the approach, we utilize a CSP solver to detect in- consistencies in dialogues re-lexicalized by an LLM. Our findings indicate that: (i) CSP is ef- fective to detect dialogue inconsistencies; and (ii) consistent dialogue re-lexicalization is chal- lenging for state-of-the-art LLMs, achieving **only a 0.15 accuracy rate when compared to a** CSP solver. Furthermore, through an ablation study, we reveal that constraints derived from domain knowledge pose the greatest difficulty in being respected. We argue that CSP cap- tures core properties of dialogue consistency that have been poorly considered by approaches based on component pipelines.

027 1 Introduction

 Task-oriented dialogue (TOD) systems [\(McTear,](#page-9-0) [2020;](#page-9-0) [Louvan and Magnini,](#page-9-1) [2020;](#page-9-1) [Balaraman et al.,](#page-8-0) [2021\)](#page-8-0) play a crucial role in human-computer in- teraction, facilitating seamless communication be- tween users and machines to accomplish specific tasks. A peculiar characteristic of TODs is that they need to maintain consistency at two levels: (i) internally within the dialogue itself, ensuring that information in a turn is consistent with informa- tion in other turns, and (ii) consistency with the content of the conversational domain of the dia- logue system. Internal consistency is responsible for the coherence of the dialogue, making it pos-sible to maintain a meaningful exchange between

R1: N=Taberna A=centre F=spanish P=cheap

R2: N=Espana A=centre F=spanish P=moderate

R3: N=Beirut A=centre F=lebanese P=cheap

U1: I am looking for a restaurant serving **Spanish** food. S1: There are three restaurants serving Spanish food, one is cheap and the other is moderate price range. Which price range would you prefer? U2: I am looking for a cheap restaurant in any area that serves Spanish food. S2: Beirut is cheap and serves Lebanese food. Would you like the location information?

Figure 1: An inconsistent task-oriented dialogue with a Knowledge Base. Red values indicate internal inconsistencies, purple values indicate external inconsistencies.

the participants. External consistency, on the other **042** hand, allows the dialogue to correctly reflect do- **043** main knowledge. In this paper, we investigate how **044** dialogue consistency in TOD can be effectively **045** modeled such that possible violations (i.e., incon- **046** sistencies) can be automatically detected. 047

Figure [1,](#page-0-0) shows a fragment of a Knowledge Base **048** (three restaurants in a city) and a short dialogue in **049** which a user expresses preferences for restaurants 050 serving Spanish food, and the system responds pro- **051** viding information about available options. There **052** are two inconsistencies in this dialogue: first, at **053** turn S1, the system mentions three restaurants serv- **054** ing Spanish food, which is not consistent with **055** the domain knowledge, where there are two such **056** restaurants (domain inconsistency). Second, at turn **057** S2, the system introduces a Lebanese restaurant, **058** while it would have been expected to mention a 059

 Spanish restaurant (dialogue inconsistency). We assume that a well-formed TOD should not mani- fest any inconsistency of the type reported in our example. However, while relevant work on evalu- ating TODs has focused on single dialogue com- [p](#page-8-1)onents (e.g., dialogue state tracking [\(Henderson](#page-8-1) [et al.,](#page-8-1) [2014\)](#page-8-1)), consistency evaluation has received much less attention. The problem is even more urgent now that end-to-end approaches [\(Bang et al.,](#page-8-2) [2023;](#page-8-2) [Lai et al.,](#page-9-2) [2023\)](#page-9-2) are by-passing component evaluations. Automatic detection of dialogue incon- sistencies is crucial when dialogues are generated by Large Language Models (LLMs), using few- shot or zero-shot approaches. While LLMs have the capacity to generate TODs without being fine- tuned on training data, it is well known that they are prone to hallucinations [\(Ji et al.,](#page-8-3) [2022\)](#page-8-3), which may affect dialogue consistency. Furthermore, in dynamic domains where the conversational context evolves over time [\(Labruna and Magnini,](#page-9-3) [2023,](#page-9-3) [2022\)](#page-9-4), maintaining dialogue consistency becomes even more challenging. The possible presence of inconsistencies in TODs [\(Qin et al.,](#page-9-5) [2021\)](#page-9-5) raises the problem of detecting them, which is the topic of the paper.

 The novel intuition of the paper is to consider dialogue consistency as a kind of *Constraint Satis- faction Problem* (*CSP*). We investigate how to as- sess the consistency of a TOD under the following working hypothesis: (i) first, dialogue consistency can be modeled with constraints that need to be respected by appropriate linguistic realizations; (ii) such constraints can be well represented to define a CSP, whose allowed solutions can be identified by a CSP solver; (iii) a TOD is consistent if its linguistic realizations belong to the set of solutions allowed by a CSP solver for that dialogue. In the paper, we discuss how dialogue constraints are de- fined, how they can be extracted and modeled as a CSP, and how to set up an experimental setting where we can empirically prove that a CSP solver can detect inconsistencies in a dialogue.

 The contributions of the paper are the following: (i) we model TOD consistency as CSP: to the best of our knowledge, this is a fully original approach; (ii) we set up a reusable experimental setting where TOD consistency can be automatically evaluated 07 against a CSP solver;¹ (iii) we show that current state-of-the-art LLMs still struggle to solve simple

dialogue consistency tasks, which opens to further **109** research in dialogue consistency. **110**

2 Dialogue Consistency as a Constraint **¹¹¹ Satisfaction Problem** 112

In this section, we explore the conceptualization of **113** dialogue consistency in the CSP framework. We **114** first describe the fundamental component of a con- **115** versational domain (Section [2.1\)](#page-1-1), then we elucidate **116** the various constraints that contribute to dialogue **117** coherence (Section [2.2\)](#page-1-2), encompassing linguistic, **118** dialogic, and domain-based considerations. We fi- **119** nally expound upon the formalization of dialogue **120** constraints as CSPs (Section [2.3\)](#page-2-0), delineating the **121** process of modeling dialogue coherence as a con- **122** straint satisfaction task. **123**

2.1 Conversational Domain **124**

A conversational domain for a TOD refers to the **125** specific topic that the dialogue revolves around, 126 encompassing all the knowledge that is pertinent **127** to the conversation. In this context, the conversa- **128** tional domain is typically represented by a domain **129** ontology providing a schema of the concepts (e.g., **130** RESTAURANT, HOTEL, MOVIE), a set of slots S **131** (e.g., FOOD, AREA, PRICE) for the concepts, and **132** the set of values that each slot can assume (e.g., EX- **133** PENSIVE, MODERATE, and CHEAP for the PRICE **134** slot). Then, a domain KB comprises a collection 135 of instances for the ontology concepts, each con- **136** sisting of [slot,slot-value] pairs, adhering to the 137 domain ontology schema. **138**

2.2 Dialogue Consistency **139**

A TOD can be conceptualized as a sequence of **140** conversational turns between a user and a system **141** aimed at achieving a specific goal. Within this **142** framework, ensuring the consistency of the dia- **143** logue is crucial for effective communication be- **144** tween the user and the system. We consider three **145** types of constraints, which need to be respected for **146** a dialogue to be consistent: linguistic, dialogic and **147** domain-based constraints. **148**

Linguistic Constraints. They are necessary to **149** respect general linguistic rules of language, includ- **150** ing morpho-syntactic rules (e.g., genre and number **151** agreement) and syntax-based rules (e.g., the correct **152** use of a preposition). For instance, if we are given **153** with the following masked utterance: 154

U: I am looking for a restaurant in <MASK>. **155**

¹All resources are publicly available at https://github.com/mwozgpt/tod-csp

 the choice of *center* as substitute to the mask token is valid, while *expensive* would not be suitable, be- cause the preposition *in* is rarely used to introduce a price in English.

 Dialogic Constraints. They maintain the seman- tic coherence across successive turns of the dia- logue, ensuring that each utterance logically aligns with the preceding context, thereby facilitating a seamless flow of information. As an example, sup-pose the following masked dialogue turns:

- **166** U: I would like an Italian restaurant.
- **167** S: There is no <MASK> restaurant in the **168** center.

 Here both *Italian* and *cheap* would be eligible choices from a linguistic point of view, but only *Italian* would maintain the coherence with the pre-vious turn in the dialogue.

 Domain Constraints. They ensure alignment be- tween the dialogue content and the domain knowl- edge, thereby maintaining the dialogue's alignment with relevant factual information. Consider, for **instance, a KB** with the following restaurants:

178 R1: N=Mario A=east F=italian P=expensive **179** R1: N=Napoli A=centre F=italian P=moderate

180 And the following piece of masked dialogue:

- **181** U: I am looking for an Italian restaurant **182** in the centre.
- **183** S: We have <MASK> restaurants available for **184** your preferences.

 Then, the only admissible choice for the masked token would be *one*, as selecting any other number would introduce an inconsistency with the informa-tion provided in the KB.

189 2.3 Dialogue Consistency as CSP

 A CSP [\(Kumar,](#page-9-6) [1992\)](#page-9-6) imposes certain conditions on a finite set of variables through constraints. Each variable has a finite set of possible values, known as its domain, and constraints define which combi- nations of values are allowed for specific subsets of the variables. A constraint can be given either explicitly, by enumerating the tuples allowed, or implicitly, e.g., by an algebraic expression. The solution of a CSP is an instantiation of all the vari- ables for which all the constraints are satisfied. A CSP is solvable if it has at least one solution, other-wise it is unsolvable or overconstrained.

202 The hypothesis of this paper is that the dialogue **203** constraints outlined in Section [2.2](#page-1-2) can be modeled as CSPs. Intuitively, variables are the portions of **204** the dialogue that need to be constrained (i.e., the **205** <MASK> tokens in our examples), while the range **206** of possible values for the variables are expressed, **207** either explicitly or implicitly, in a domain KB for 208 that dialogue. The CSP task consists of select- **209** ing variable assignments that adhere to linguistic, **210** dialogic, and domain constraints. To formalize **211** this notion, consider a dialogue d_i for which $n \t 212$ variables (i.e., masked tokens) x_1, x_2, \ldots, x_n have 213 been defined. Let D_i denote the domain of pos- 214 sible values for variable x_i ; let C be the set of 215 constraints (i.e., linguistic, dialogic, and domain **216** constraints) over the dialogue d_i , and let c rep- 217 resent a single constraint in C. The CSP task is **218** to determine if there exists an assignment $A = 219$ $\{(x_1, a_1), (x_2, a_2), \ldots, (x_n, a_n)\}\$ with $a_i \in D_i$ 220 for $1 \leq i \leq n$, such that A satisfies all constraints 221 in C. This problem can be formulated as follows: **222**

Satisfies(
$$
\{(x_1, a_1), (x_2, a_2), \ldots, (x_n, a_n)\}
$$
, C_j) 223

$$
\forall C_j \in \mathcal{C} \tag{225}
$$

224

where *Satisfies* (A, C_i) denotes the binary relation- 226 ship between an assignment A and a constraint **227** C_j , indicating whether the assignment satisfies the 228 constraint. **229**

3 Methodology **²³⁰**

This section outlines the process of modeling a **231** TOD as a CSP, and then to assess the dialogue **232** consistency using a CSP solver. The assessment **233** involves three key steps for a $[d, kb]$ pair, where **234** d is a dialogue and kb is a Knowledge Base: (1) **235** identification of variables within the dialogue d 236 (Section [3.1\)](#page-2-1); (2) extraction of dialogue constraints **237** and construction of a CSP solver for the [d, kb] pair **238** (Section [3.2\)](#page-3-0); and (3) application of the CSP solver **239** to determine if the dialogue d represents a feasi- **240** ble solution with respect to the defined constraints **241** (Section [3.3\)](#page-4-0). These phases of the methodology are **242** illustrated in Figure [2.](#page-3-1) **243**

3.1 Identifying Dialogue Variables **244**

At step 1 (see Figure [2\)](#page-3-1), we consider a TOD d and 245 a kb (i.e., a set of entities described by slot-value **246** pairs) related to the conversational domain of the **247** dialogue. We do not assume any particular depen- **248** dency between d and kb: d could be either fully **249** covered by kb (i.e., all mentions of slot values in **250** d are present in kb), only partially covered, or not **251**

Figure 2: Overview of the CSP-based methodology applied to TOD consistency.

 covered at all. We consider text portions in d refer- ring to the conversational domain as potential CSP variables: a text portion referring to a slot value or mentioning amounts of instances in kb. The ratio- nale is that both slot values and instance amounts are elements that better characterize a TOD and are responsible for its consistency. In our example in Figure [1,](#page-0-0) we will obtain the following variables with their assignments:

261 $[x_1 = Spanish], [x_2 = three], [x_3 =$ 262 **Spanish**, $[x_4 = cheap] ... [x_{10} = Lebanese]$.

263 3.2 Extracting Dialogue Constraints

264 We have now established a set X of variables $x_1, x_2, ..., x_n$, where each variable x_i can assume a value either from the slot values or from instance amounts described in kb. Moving to step 2 in Figure [2,](#page-3-1) we now extract the set of constraints C 269 over the values that can be assigned to X variables. We consider the three categories of constraints in- troduced in Section [2.2:](#page-1-2) linguistic, dialogic, and domain-based constraints.

 Extracting linguistic constraints. We model lin- guistic constraints as the need for a variable derived from a slot value to match the semantic type of its slot type. For instance, given the utterance *I am looking for a restaurant at* x_1 , the value of the 278 variable x_1 must belong to the AREA type. More precisely, C1 is defined as follows:

$$
C1: x_1 \in V
$$

 where V is the set of values belonging to the same slot type as the original value. Constraint C1, is meant to avoid that a variable can assume values that are semantically non valid. For instance, avoid-285 ing that x_1 =NORTH can be assigned to a FOOD, as in *I am looking for a restaurant at* INDIAN, which is ungrammatical in English.

Extracting dialogic constraints. There are two **288** dialogic constraints that we currently consider. C2 **289** for ensuring that variables mentioning the same **290** slot value in d are assigned to the same value. $C3$ 291 for ensuring that variables with the same semantic **292** type occurring in the same utterance are assigned **293** to different values. Given the turn *U: I want an* x_1 294 *restaurant. S: There are 3 restaurant that serve* x_2 , x_3 , 295 we define C₂ as follows: ²⁹⁶

$$
C_2: x_1 = x_2 \tag{297}
$$

where the aim is to keep internal coherence across 298 the dialogue turns. Given the utterance *We have* x_1 , 299 x_2 , or x_3 *restaurants.*, we define $C3$ as: 300

$$
C_3: x_1 \neq x_2, \quad x_1 \neq x_3, \quad x_2 \neq x_3 \tag{301}
$$

which captures non redundancy at the utterance 302 **level.** 303

Extracting domain-based constraints. There **304** are three domain-based constraints that we cur- **305** rently consider. All of them are meant to guar- **306** antee consistency between the number of instances **307** mentioned in d and the actual number of instances 308 present in kb. We distinguish three cases: C4 cov- **309** ers the cases when an utterance in d states that there **310** are no instances in kb; C5 covers the cases where **311** it is stated that there is at least one instance; and **312** $C6$ the cases where there are exactly *n* instances. 313

As for C4, consider an utterance indicating no results for a search: *There are no restaurants serv-* **315** *ing* x_1 *food*, assuming that there are no restaurants with $[FOOD=x_1]$ in kb. For this utterance, $C4$ is defined as:

$$
C4: \neg \exists i \in KB \text{ with values } x_1
$$

implying that the variable x_1 can not assume a 320 value that is present in an instance of the KB. **321**

-
-
-
-

 As for C5, consider the utterance: *We have many* x_1 *restaurants at* x_2 , where at least one restaurant 324 with $[FOOD=x_1]$ and $[AREA=x_2]$ is supposed to exist in kb. For this utterance, C5 is defined as:

$$
C5: \exists i \in KB \text{ with values } x_1, x_2
$$

327 imposing the existence of at least one instance with 328 values x_1 and x_2 .

329 Finally, for C6, consider the utterance *There are* 330 x_1 *restaurants at* x_2 . We define the constraint as:

$$
331 \tC6: |\{i \in KB \text{ with value } x_2\}| = x_1
$$

332 to check that the number of instances with value 333 x_2 is exactly equal to x_1 .

334 3.3 Assessing Dialogue Consistency

 Once all variables and constraints for a dialogue d are identified, a CSP solver computes possible solutions for the variables in d given kb (step 3 in Figure [2\)](#page-3-1). If one of these solutions matches the variable assignments in d, we consider d consis- tent with respect to kb (step 4 in Figure [2\)](#page-3-1). For example, in the dialogue and kb illustrated in Fig- ure [1,](#page-0-0) the variable assignments do not match any CSP admissible solution. Specifically, variable as-344 signment $[x_2 = three]$ violates C6, referring to an incorrect number of Spanish instances in kb, and 346 variable $[x_{10} = \text{Lebanese}]$ violates C2, as it does not maintain coherence with the previous turns. If the CSP solver finds at least one solution, the vari- able assignments in the dialogue must match one of those solutions, ensuring all constraints are fol- lowed. On the other hand, if no solution is found with respect to kb, the variable assignments should be empty or contain values not in kb to ensure con- sistency. These aspects will be further explored in the experiments discussed in Section [4.](#page-4-1)

³⁵⁶ 4 Experimental Setting

 In this section, we present the experimental setup used to assess dialogue consistency through a CSP solver. We describe the general setting and the purposes of the experiments (Section [4.1\)](#page-4-2), the dataset utilized (Section [4.2\)](#page-5-0), the KBs associated to each dialogue (Section [4.3\)](#page-5-1), the tools employed for constraint satisfaction (Section [4.4\)](#page-5-2), the language model used for dialogue generation (Section [4.5\)](#page-5-3), the baselines against which we compare our results (Section [4.6\)](#page-5-4) and finally, the evaluation metrics that have been used (Section [4.7\)](#page-5-5).

Table 1: Dialogue distribution based on the number of solutions provided by the CSP solver.

4.1 Purposes and General Setting **368**

The purpose of the experiments is to check the **369** feasibility of the CSP-based approach described **370** in Section [3](#page-2-2) for detecting dialogue inconsistencies. **371** Our focus is not on optimizing the performance of **372** the CSP solver but rather on investigating critical **373** aspects of the process in a realistic setting. Several **374** steps are involved in this process: 375

- 1. Initially, we require dialogue-knowledge base **376** $(d-kb)$ pairs. As for dialogues d , we uti- 377 lize MultiWoz [\(Han et al.,](#page-8-4) [2020\)](#page-8-4) dialogues, **378** which are already annotated for dialogue state **379** tracking, enabling precise identification of **380** variables within the dialogue. From an an- **381** notated MultiWoz dialogue d, we derive a **382** de-lexicalized version d_{delex} , where dialogue 383 content is replaced with CSP variables. **384**
- 2. Additionally, for each dialogue, we derive a **385** knowledge base (kb) from the MultiWoz on- **386** tology, allowing variation in both the size and **387** type of instances. **388**
- 3. With d_{delex} and kb established, the next step 389 involves generating variable assignments that **390** can be assessed via a CSP solver. To pro- **391** duce dialogues with potential realistic in- **392** consistencies, we employ a large language **393** model (LLM). The LLM is tasked with re- **394** lexicalizing the variables (i.e., substituting **395** slot-values to CSP variables) in d_{delex} , consid- 396 ering the provided kb. The LLM prompt is il- **397** lustrated in Appendix [A.](#page-9-7) This re-lexicalization **398** process aims to maximize correctness while **399** adhering to all implicit dialogue constraints. **400**
- 4. Finally, the re-lexicalized dialogue d_{relex} pro- 401 duced by the LLM serves as a variable assign- **402** ment and is compared with the solutions of the **403**

	Constraint # variables	% coverage
C1	768	1.00
C ₂	686	0.89
C ₃	108	0.14
C ₄	9	0.01
C ₅	394	0.51
C ₆	197	0.25

Table 2: Number of dialogue variables affected by constraints and their proportion.

404 CSP solver on the same d-kb pair to produce **405** a consistency score.

406 4.2 MultiWOZ Dataset

 The experimental data was sourced from the Multi- WOZ 2.3 dataset [\(Han et al.,](#page-8-4) [2020\)](#page-8-4), a widely used benchmark for TOD systems comprising more than ten thousand conversations between a user and a system, covering various domains such as restau- rants, hotels, or attractions. For our experiments, we focus on restaurant-related dialogues from the MultiWOZ dataset. In total we consider 131 dia- logues with 768 total de-lexicalizations (i.e., CSP variables), as shown in the first row of Table [1.](#page-4-3) In addition, Table [1](#page-4-3) categorizes the dataset into groups based on the number of solutions identified by MiniZinc (see Section [4.4\)](#page-5-2) for each dialogue.

420 4.3 Knowledge Base

 The kb employed in the experiments are sourced from the MultiWOZ database. Specifically, for each dialogue d in MultiWOZ, we selected a perti- nent instance from the global MultiWOZ KB that aligns with the content of the dialogue. This en- sures both relevance and coherence between the dialogue and the associated domain information. Additionally, to introduce variability in the compo- sition of the dialogue kb, we randomly sampled a set of n instances from the global MultiWOZ KB, where n is a randomly generated number between 0 and 8. This approach ensures a diverse range of instances in the dialogue kb while constraining the total number of instances to a maximum of 9, facilitating efficient prompting of the kb to the **436** LLM.

437 4.4 MiniZinc Constraint Solver

438 [A](#page-9-8)s for CSP solver, we use MiniZinc [\(Nethercote](#page-9-8) **439** [et al.,](#page-9-8) [2007\)](#page-9-8), an open-source constraint program-**440** ming language specifically designed for modeling and solving constraint satisfaction problems. We **441** employed MiniZinc to obtain solutions satisfying **442** the dialogue constraints for ourevaluation purposes. **443** MiniZinc provides a high-level modeling language **444** that allows users to express problem constraints **445** and objectives. It supports a wide range of con- **446** straint types, which make it suitable for modeling **447** diverse problem domains. Among MiniZinc's suite **448** of solvers, we leveraged Chuffed [\(Chu et al.,](#page-8-5) [2018\)](#page-8-5), **449** a state-of-the-art solver known for its efficiency **450** in solving CSPs through time optimization, espe- **451** cially advantageous for addressing complex and **452** large-scale optimization problems. **453**

4.5 GPT-3.5-Turbo Language Model **454**

For dialogue re-lexicalization, we employed the **455** GPT-3.5-Turbo language model, a member of the **456** OpenAI GPT family [\(Achiam et al.,](#page-8-6) [2023\)](#page-8-6), specif- **457** ically designed to perform well in conversational **458** contexts. GPT-3.5-Turbo was prompted with both **459** (d_{delex}) and its associated kb. This comprehen- 460 sive input served to guide the model to produce 461 dialogues that adhere to the implicit constraints, 462 thereby ensuring dialogue coherence and adher- **463** ence to the domain. We utilized GPT-3.5 for inference in zero-shot mode (see Appendix [A\)](#page-9-7), without **465** any fine-tuning, leveraging the API version dated **466** "2023-05-15" with a temperature setting of 0.9 to **467** ensure balanced exploration and exploitation dur- **468** ing dialogue generation. **469**

4.6 Baselines 470

We introduce two dialogue re-lexicalization base- **471** lines, for a comparative analysis with GPT. The first **472** baseline (RANDOM), produces a dialogue d_{relex} 473 where variables in d_{delex} are randomly assigned to 474 slot values present in the kb. The second baseline **475** (MOST FREQUENT) produces a dialogue d_{relex} 476 where variables in d_{delex} are assigned to the most 477 frequent value observed in the kb. By contrast- **478** ing our evaluation results with these baselines, we **479** gain insights into the efficacy of our approach in **480** capturing and assessing dialogue consistency. **481**

4.7 Evaluation Metrics **482**

Global Consistency Accuracy (GCA) and Variable **483** Consistency Accuracy (VCA) are the two metrics **484** used to evaluate the adherence of a dialogue to a **485** specific set of constraints. Given a re-lexicalized **486** dialogue d_{relex} where variables are assigned to val- 487 ues, GCA measures the overall accuracy of the **488** assignments for each variable. The average GCA is **489**

Dataset	GCA –	VCA
RANDOM	0.01	0.06
MOST FREQUENT	0.01	0.10
GPT	0.15	0.27

Table 3: Global and variable consistency for dialogues re-lexicalized by GPT compared to the RANDOM and MOST FREQUENT baselines.

490 calculated as the proportion of dialogues that fully **491** comply with all defined constraints:

$$
GCA = \frac{\sum_{i=1}^{N} (\prod_{j=1}^{M} \text{Satisfies}(A_i, C_j))}{N}
$$

 where N is the total number of dialogues, and **Satisfies** (A_i, C_j) is a binary indicator function that returns 1 if and only if all variable assignments in 496 dialogue d_i comply with the constraint j, 0 other- wise. On the other hand, VCA assesses the assign- ment accuracy on individual variables within the dialogue. We compare the dialogue assignment to the solutions of the CSP solver and find the most similar solution; then, we count how many variable assignments coincide with the assignments of the most similar solution. We formally define VCA as **504** follows:

$$
VCA = \frac{\sum_{i=1}^{N} |CorrectAssignments(d_i)|}{M}
$$

 where N is the total number of dialogues, M is the total number of variables in the dialogues, and *CorrectAssignments* (d_i) are the variable as- $\frac{1}{509}$ signments in dialogue d_i that coincide with the assignments of the most similar solution provided by the CSP solver. GCA and VCA provide insights into the ability of the dialogue generation system to maintain coherence and fidelity to the underly- ing domain knowledge while generating responses. Higher values of GCA and VCA indicate better performance in terms of dialogue quality and con-sistency.

⁵¹⁸ 5 Results

 Table [2](#page-5-6) presents the impact of each constraint on the variables in the dataset, detailing the percent- age of variables influenced by each constraint. This shows that C1 (i.e., assigned values need to respect the semantic type of the variable) applies to all vari- ables in the dataset, while C4 (no instances in kb) applies only nine time in total. Table [3](#page-6-0) compares

Dataset	GCA	VCA
0 sol.	0.0	0.0
1 SOL.	0.31	0.48
2-10 SOL.	0.22	0.53
$11 - 100$ sol.	0.22	0.55
$101 +$ SOL.	0.36	0.70

Table 4: Assessment of global and variable consistency for re-lexicalized dialogues across solution groups.

the global and variable consistency in dialogues re- **526** lexicalized by GPT with the RANDOM and MOST **527** FREQUENT baselines. GPT dialogues exhibit sig- **528** nificantly higher global and variable consistency **529** compared to the baseline datasets. Table [4](#page-6-1) assesses **530** GCA and VCA for GPT dialogues across various **531** CSP solution groups. Results show that dialogues **532** with more solutions tend to have higher GCA and 533 VCA scores, while the model is not able to recog- **534** nize and address the 0 solution cases. **535**

Table [5](#page-7-0) presents the results of an ablation study, **536** where we systematically remove each constraint 537 one by one and analyse their impact on GCA and **538** VCA for each configurations. Results show that **539** the most critical constraint is C6 (i.e., exact match **540** with number of kb instances). Additionally, we 541 conducted experiments where groups of constraints **542** were collectively removed to observe their influ- **543** ence on the dialogue generation process, confirm- **544** ing that domain-based constraints are more critical. **545**

6 Discussion **⁵⁴⁶**

The experiment results shed light on several key 547 aspects of consistency assessment for TODs. First, **548** comparing GPT and the two baselines (RANDOM **549** and MOST FREQUENT) on re-lexicalized dialogues, **550** we note the better quality achieved by the GPT 551 model (see Table [3\)](#page-6-0), both in term of GCA and **552** VCA. GPT can effectively re-lexicalize dialogues **553** that more closely adhere to the defined constraints. **554** Furthermore, the assessment of global and vari- **555** able consistency across different solution groups **556** reveals interesting patterns (see Table [4\)](#page-6-1). Dialogues **557** with a higher number of solutions tend to exhibit 558 higher levels of consistency, indicating that the **559** model performs better when presented with more **560** options to fulfill constraints. At the other extreme, **561** the model is not able to address cases where no **562** feasible solution exists, as it always provides an at- **563** tempt of assignment for the variables. This finding **564**

505

Constraint	GCA	VCA
ALL EXCEPT C1	0.15	0.31
ALL EXCEPT C ₂	0.15	0.27
ALL EXCEPT C3	0.15	0.29
ALL EXCEPT C4	0 16	0.30
ALL EXCEPT C5	0.15	0.32
ALL EXCEPT C6	0.21	0.48
ALL EXCEPT	0.15	0.30
DIALOGIC		
ALL EXCEPT	0.23	0.56
DOMAIN		

Table 5: Ablation study: global and variable consistency under different constraint configurations.

 emphasizes the importance of considering the rich- ness and diversity of CSP solutions, as they have a strong impact on the quality and consistency of re- lexicalized dialogues. Additionally, analysing the distribution of constraints on the dialogue variables, reveals significant variations (see Table [2\)](#page-5-6), with cer- tain constraints exerting a stronger influence than others. The ablation study provides valuable in- sights into the impact of the different constraints on dialogue re-lexicalization. Excluding domain con- straints, in particular, leads to significantly higher GCA and VCA scores, indicating the critical role of domain-specific knowledge in shaping dialogue coherence and relevance (see Table [5\)](#page-7-0). This sug- gests that recent LLMs may not effectively leverage the provided kb, highlighting an area for potential improvement in future iterations of language model training and dialogue re-lexicalization techniques. Our experiments have shown that modeling and as- sessing dialogue consistency through CSP is both feasible and challenging. We were able to high- lights both strengths and weaknesses of dialogue generation and to discern which constraints are met and which are not, gaining insight into the specific features and challenges inherent in this process.

⁵⁹⁰ 7 Related Work

 TOD systems have been extensively investigated in NLP. [\(Allen et al.,](#page-8-7) [2001\)](#page-8-7). Recent research has explored the use of neural network architectures for dialogue state tracking [\(Wu et al.,](#page-9-9) [2020;](#page-9-9) [Zhao et al.,](#page-9-10) [2021\)](#page-9-10) and policy learning [\(Su et al.,](#page-9-11) [2016;](#page-9-11) [Liu and](#page-9-12) [Lane,](#page-9-12) [2017\)](#page-9-12). Several metrics have been proposed to assess the performance of TOD systems, including task completion rates, user satisfaction scores, and objective measures for system components, such as **599** precision, recall, and F1-score [\(Chen et al.,](#page-8-8) [2017;](#page-8-8) 600 [Santhanam and Shaikh,](#page-9-13) [2019;](#page-9-13) [Deriu et al.,](#page-8-9) [2021\)](#page-8-9). **601** Recent studies have emphasized the importance of **602** holistic evaluation frameworks that consider multi- **603** ple aspects of dialogue quality [\(Zhang et al.,](#page-9-14) [2021\)](#page-9-14). **604**

Maintaining consistency and coherence in di- **605** alogues is essential for effective communication **606** between users and dialogue systems. Previous **607** research has investigated various approaches to **608** ensure dialogue coherence, including coherence **609** modeling [\(Cervone et al.,](#page-8-10) [2018\)](#page-8-10), and coherence- **610** based response generation [\(Cervone and Riccardi,](#page-8-11) **611** [2020\)](#page-8-11), aiming to enhance the naturalness and flu- **612** ency of generated dialogues. Finally, several stud- **613** ies have explored the application of CSPs to lan- **614** guage. These include early attempts to ensure co- **615** herence in generated text [\(Kibble and Power,](#page-8-12) [2004\)](#page-8-12), 616 model preposition lexicalization using constraints **617** [\(Moriceau and Saint-Dizier,](#page-9-15) [2004\)](#page-9-15), guide lexi- **618** cal choices through constraints [\(McKeown et al.,](#page-9-16) **619** [1997\)](#page-9-16), and treat context-sensitive utterance genera- **620** tion as a CSP [\(Popescu et al.,](#page-9-17) [2009\)](#page-9-17). **621**

8 Conclusion **⁶²²**

In this paper, we have introduced a novel ap- **623** proach to assess dialogue consistency in the con- **624** text of TODs using a metric based on Constraint **625** Satisfaction. In our approach, variables repre- **626** sent de-lexicalized segments of the dialogue and **627** constraints reflect linguistic, conversational, and **628** domain-based properties of TODs. Our experi- **629** ments have demonstrated the feasibility of this ap- **630** proach, enabling us to effectively identify and quan- **631** tify inconsistencies present in the dialogues. An **632** interesting side-effect of our investigation is the **633** observation that state-of-the-art LLMs often intro- **634** duce numerous inconsistencies when tasked with **635** re-lexicalizing dialogues. These inconsistencies **636** primarily concern domain knowledge adherence, **637** resulting in an overall accuracy of only 0.15 at the **638** dialogue level. Our study highlights the potential of **639** CSP-based methodologies in evaluating dialogue **640** consistency and identifying areas for improvement **641** in automated dialogue generation systems. Fu- **642** ture research should further explore the application **643** of CSP in this domain and investigate strategies **644** to enhance the coherence of LLM-generated di- **645** alogues, particularly in applications with strong **646** domain knowledge requirements. **647**

⁶⁴⁸ 9 Limitations

 Our study is subject to several limitations that war- rant consideration. Firstly, the process of defining constraints for dialogue consistency assessment is complex and multifaceted. While we have delin- eated several constraints in this study, the TOD landscape is vast, and additional constraints may need to be identified and incorporated to capture a broader range of dialogue scenarios accurately. Each constraint is formulated based on our current understanding of the phenomena, acknowledging that further investigations may uncover additional constraints. Additionally, we also consider imple- mentation feasibility, as certain constraints may require more extensive implementation efforts to detect. Moreover, the selection and prioritization of constraints inherently involve subjective judgment, and achieving consensus on the most relevant con- straints for a given dialogue domain may pose a challenge.

 Secondly, while we employed a state-of-the-art Large Language Model (LLM) for dialogue gener- ation and consistency assessment, the performance of alternative language models remains unexplored. Investigating the effectiveness of various LLM ar- chitectures, pre-training strategies, or fine-tuning approaches could provide valuable insights into their suitability for TOD tasks.

 Furthermore, while our methodology endeavors to be as generalizable as possible, it is important to acknowledge that nuances in dialogue structures and domain-specific knowledge may exist across different datasets, and there may still be aspects of dialogue consistency that our approach may not fully capture. Exploring additional datasets span- ning diverse domains and languages could offer a more comprehensive understanding of dialogue consistency challenges and the efficacy of our pro-posed methodology.

⁶⁸⁷ References

- **688** Josh Achiam, Steven Adler, Sandhini Agarwal, Lama **689** Ahmad, Ilge Akkaya, Florencia Leoni Aleman, **690** Diogo Almeida, Janko Altenschmidt, Sam Altman, **691** Shyamal Anadkat, et al. 2023. Gpt-4 technical report. **692** arXiv preprint arXiv:2303.08774.
- **693** James Allen, George Ferguson, and Amanda Stent. **694** 2001. An architecture for more realistic con-**695** versational systems. In Proceedings of the 696 6th international conference on Intelligent user **697** interfaces, pages 1–8.
- Vevake Balaraman, Seyedmostafa Sheikhalishahi, and **698** Bernardo Magnini. 2021. [Recent neural methods on](https://aclanthology.org/2021.sigdial-1.25) **699** [dialogue state tracking for task-oriented dialogue sys-](https://aclanthology.org/2021.sigdial-1.25) **700** [tems: A survey.](https://aclanthology.org/2021.sigdial-1.25) In Proceedings of the 22nd Annual **701** Meeting of the Special Interest Group on Discourse **702** and Dialogue, SIGdial 2021, Singapore and Online, **703** July 29-31, 2021, pages 239–251. Association for **704** Computational Linguistics. **705**
- Yejin Bang, Samuel Cahyawijaya, Nayeon Lee, Wen- **706** liang Dai, Dan Su, Bryan Wilie, Holy Lovenia, Ziwei **707** Ji, Tiezheng Yu, Willy Chung, et al. 2023. A multi- **708** task, multilingual, multimodal evaluation of chatgpt **709** on reasoning, hallucination, and interactivity. arXiv **710** preprint arXiv:2302.04023. **711**
- Alessandra Cervone and Giuseppe Riccardi. 2020. Is **712** this dialogue coherent? learning from dialogue acts **713** and entities. arXiv preprint arXiv:2006.10157. **714**
- Alessandra Cervone, Evgeny Stepanov, and Giuseppe **715** Riccardi. 2018. Coherence models for dialogue. **716** arXiv preprint arXiv:1806.08044. **717**
- Hongshen Chen, Xiaorui Liu, Dawei Yin, and Jil- **718** iang Tang. 2017. A survey on dialogue systems: **719** Recent advances and new frontiers. Acm Sigkdd **720** Explorations Newsletter, 19(2):25–35. **721**
- Geoffrey Chu, Peter J. Stuckey, Anthony Schutt, **722** Thorsten Ehlers, Graeme Gange, and Keith Fran- **723** cis. 2018. Chuffed, a lazy clause generation solver. **724** <https://github.com/chuffed/chuffed>. **725**
- Jan Deriu, Alvaro Rodrigo, Arantxa Otegi, Guillermo **726** Echegoyen, Sophie Rosset, Eneko Agirre, and Mark **727** Cieliebak. 2021. Survey on evaluation methods for **728** dialogue systems. Artificial Intelligence Review, **729** 54:755–810. **730**
- Ting Han, Ximing Liu, Ryuichi Takanobu, Yixin **731** Lian, Chongxuan Huang, Wei Peng, and Minlie **732** Huang. 2020. Multiwoz 2.3: A multi-domain task- **733** oriented dataset enhanced with annotation correc- **734** tions and co-reference annotation. arXiv preprint **735** arXiv:2010.05594. **736**
- Matthew Henderson, Blaise Thomson, and Jason D. **737** Williams. 2014. [The second dialog state track-](https://doi.org/10.3115/v1/W14-4337) **738** [ing challenge.](https://doi.org/10.3115/v1/W14-4337) In Proceedings of the 15th Annual **739** Meeting of the Special Interest Group on Discourse **740** and Dialogue (SIGDIAL), pages 263–272, Philadel- **741** phia, PA, U.S.A. Association for Computational Lin- **742** guistics. **743**
- Ziwei Ji, Nayeon Lee, Rita Frieske, Tiezheng Yu, **744** Dan Su, Yan Xu, Etsuko Ishii, Yejin Bang, Andrea **745** Madotto, and Pascale Fung. 2022. Survey of hal- **746** lucination in natural language generation. ACM **747** Computing Surveys. **748**
- Rodger Kibble and Richard Power. 2004. Opti- **749** mizing referential coherence in text generation. **750** Computational Linguistics, 30(4):401–416. **751**

835 847 853

- **752** Vipin Kumar. 1992. Algorithms for constraint-**753** satisfaction problems: A survey. AI magazine, **754** 13(1):32–32.
- **755** Tiziano Labruna and Bernardo Magnini. 2022. Fine-**756** tuning bert for generative dialogue domain adapta-**757** tion. In Text, Speech, and Dialogue, pages 490–501.
- **758** Tiziano Labruna and Bernardo Magnini. 2023. Address-**759** ing domain changes in task-oriented conversational **760** agents through dialogue adaptation. In Proceedings **761** of the 17th Conference of the European Chapter **762** of the Association for Computational Linguistics: **763** Student Research Workshop, pages 149–158.
- **764** Tuan M Lai, Giuseppe Castellucci, Saar Kuzi, Heng Ji, **765** and Oleg Rokhlenko. 2023. External knowledge ac-**766** quisition for end-to-end document-oriented dialog **767** systems. In Proceedings of the 17th Conference **768** of the European Chapter of the Association for **769** Computational Linguistics, pages 3633–3647.
- **770** Bing Liu and Ian Lane. 2017. Iterative policy learning in **771** end-to-end trainable task-oriented neural dialog mod-**772** els. In 2017 IEEE Automatic Speech Recognition **773** and Understanding Workshop (ASRU), pages 482– **774** 489. IEEE.
- **775** [S](https://doi.org/10.18653/v1/2020.coling-main.42)amuel Louvan and Bernardo Magnini. 2020. [Re-](https://doi.org/10.18653/v1/2020.coling-main.42)**776** [cent neural methods on slot filling and intent clas-](https://doi.org/10.18653/v1/2020.coling-main.42)**777** [sification for task-oriented dialogue systems: A](https://doi.org/10.18653/v1/2020.coling-main.42) **778** [survey.](https://doi.org/10.18653/v1/2020.coling-main.42) In Proceedings of the 28th International **779** Conference on Computational Linguistics, pages **780** 480–496, Barcelona, Spain (Online). International **781** Committee on Computational Linguistics.
- **782** Kathleen McKeown, Michael Elhadad, and Jacques **783** Robin. 1997. Floating constraints in lexical choice.
- **784** Michael McTear. 2020. Conversational ai: Dia-**785** logue systems, conversational agents, and chat-**786** bots. Synthesis Lectures on Human Language **787** Technologies, 13(3):1–251.
- **788** Véronique Moriceau and Patrick Saint-Dizier. 2004. A **789** constraint-based model for preposition choice in nat-**790** ural language generation. Constraint Solving and **791** Language Processing, page 124.
- **792** Nicholas Nethercote, Peter J. Stuckey, Rowan Becket, **793** Simon Brand, Greg J. Duck, and Guido Tack. 2007. **794** [Minizinc: Towards a standard cp modelling language.](http://www.minizinc.org/) **795** In CP 2007, volume 4741 of LNCS, pages 529–543. **796** Springer.
- **797** Vladimir Popescu, Jean Caelen, and Corneliu Burileanu. **798** 2009. A constraint satisfaction approach to context-**799** sensitive utterance generation in multi-party dia-**800** logue systems. International Journal of Speech **801** Technology, 12:95–112.
- **802** Libo Qin, Tianbao Xie, Shijue Huang, Qiguang Chen, **803** Xiao Xu, and Wanxiang Che. 2021. Don't be contra-**804** dicted with anything! ci-tod: Towards benchmarking **805** consistency for task-oriented dialogue system. arXiv **806** preprint arXiv:2109.11292.
- Sashank Santhanam and Samira Shaikh. 2019. Towards **807** best experiment design for evaluating dialogue sys- **808** tem output. arXiv preprint arXiv:1909.10122. **809**
- Pei-Hao Su, Milica Gasic, Nikola Mrksic, Lina Rojas- **810** Barahona, Stefan Ultes, David Vandyke, Tsung- **811** Hsien Wen, and Steve Young. 2016. On-line active **812** reward learning for policy optimisation in spoken **813** dialogue systems. arXiv preprint arXiv:1605.07669. **814**
- Peng Wu, Bowei Zou, Ridong Jiang, and AiTi Aw. 2020. **815** Gcdst: A graph-based and copy-augmented multi- **816** domain dialogue state tracking. In Findings of the **817** Association for Computational Linguistics: EMNLP **818** 2020, pages 1063–1073. **819**
- Chen Zhang, Grandee Lee, Luis Fernando D'Haro, and **820** Haizhou Li. 2021. D-score: Holistic dialogue evalua- **821** tion without reference. IEEE/ACM Transactions on **822** Audio, Speech, and Language Processing, 29:2502– **823** 2516. **824**
- Jeffrey Zhao, Mahdis Mahdieh, Ye Zhang, Yuan Cao, **825** and Yonghui Wu. 2021. Effective sequence-to- **826** sequence dialogue state tracking. arXiv preprint **827** arXiv:2108.13990. **828**

A Appendix A: GPT prompt **⁸²⁹**

Below is an instruction that outlines a task, along **830** with a Knowledge Base containing domain-specific **831** information to be utilized, and a dialogue for you **832** to work on. Return a response that effectively **833** fulfills the task. **834**

Instruction: **836**

Fill in the [MASK] placeholders in the dialogue 837 based on the information provided in the Knowl- **838** edge Base. Provide the updated dialogue exactly as **839** it was given, but with the placeholders replaced by **840** the appropriate values for each turn in the dialogue. **841** If a turn does not contain any placeholders, leave **842** the sentence unchanged. Turns should start with **843** either User or System. Be aware of leaving blank **844** spaces before punctuation as in the original (e.g. 845 Hi, instead of Hi, 846

Knowledge Base: **848**

Restaurant #1 - Area: centre, Food: british, Price: **849** moderate **850**

Restaurant #2 - Area: west, Food: european, Price: **851** expensive **852**

Dialogue: **854**

- USER: I'm looking for a restaurant serving 855 [MASK] food in any area . **856** SYSTEM: There are no [MASK] restaurants **857**
	- in the area . **858**

