

Modular World Models with Competitive Independent Mechanisms

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Abstract

001 Taking inspiration from the Independent Causal Mecha-
 002 nisms principle in the context of world models, we present
 003 Competitive Mechanisms for Efficient Transfer (COMET),
 004 a modular world model which leverages reusable, indepen-
 005 dent mechanisms across different environments. COMET
 006 is trained on multiple environments with varying dynam-
 007 ics via a two-step process: competition and composition.
 008 This enables the model to recognise and learn transfer-
 009 able mechanisms. Specifically, in the competition phase,
 010 COMET is trained with a winner-takes-all gradient allo-
 011 cation, encouraging the emergence of independent mecha-
 012 nisms. These are then re-used in the composition phase,
 013 where COMET learns to re-compose learnt mechanisms in
 014 ways that capture the dynamics of new environments. In so
 015 doing, COMET explicitly reuses prior knowledge, enabling
 016 efficient and interpretable adaptation. In contrast to com-
 017 petitive baselines, we demonstrate that COMET captures
 018 recognisable mechanisms without supervision and is able
 019 to adapt to new environments.

020 1. Introduction

021 To reason about environments as rich and complex as our
 022 physical world requires the ability to learn efficiently and
 023 to flexibly adapt prior knowledge to unseen settings. This
 024 is of particular importance to embodied intelligence, as
 025 robots often need to adapt to changes in the environment.
 026 Whilst humans seem able to generalise knowledge across
 027 myriad tasks and situations effortlessly, building artificial
 028 agents that can do so with minimal training data remains
 029 a significant challenge. At the heart of this challenge
 030 are crucial distinctions between what and how humans
 031 and machines learn. It has been conjectured that humans
 032 represent knowledge internally in a structured and modular
 033 way, i.e., by distilling past experience into general princi-
 034 ples about the world, which can be applied or selectively
 035 updated in novel settings [9, 23, 36, 39]. By contrast,
 036 current learning-based world models are mostly based
 037 on monolithic architectures, and the resulting entangled

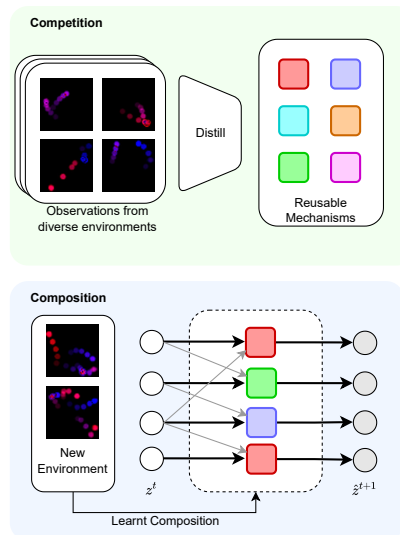


Figure 1. Illustration of training phases. In the first phase, the model learns a set of reusable mechanisms. In the second phase, the model applies these in a new environment.

representations of the world limit the selective re-using of
 prior knowledge in new environments. Therefore, learning
 methods that afford modularity are key to world models
 that can adapt efficiently in diverse settings. In this paper,
 we address this challenge by developing a model capable
 of discovering a toolbox of generalisable concepts that can
 be reused across different contexts.

Recent works on object-centric world models [21, 25]
 have made progress towards a compositional understanding
 of the world. By decomposing an observed scene into
 discrete *object slots*, these methods model the interaction
 between entities in the scene. We argue that, just as the state
 representation of the scene can be factorised into object
 slots, the transition dynamics, too, can be factorised into
 discrete and independent *mechanisms*. Our work is moti-
 vated by the observation that, while different environments
 can exhibit different dynamics, we can often explain the
 behaviour of objects by a small set of interaction primitives,

such as "A rests on top of B" and "C collides with D". The goal of this work is to acquire such a set of versatile mechanisms from observations without supervision.

Conceptually, our motivation is closely related to the *Independent Causal Mechanisms* principle (ICM) [36], which posits that the causal generative process of a system is composed of independent modules that do not inform each other. Taking inspiration from the ICM literature, we employ a competition of expert training scheme [33], where, during training, we keep a set of independently parameterised mechanisms and only update the module which best explains the observed interactions. This serves as a natural inductive bias which encourages modules to specialise in specific interaction primitives, and is consequently conducive to the emergence of reusable mechanisms. In the rest of this paper, we give details of our model and provide empirical results. We defer the discussion of related works to the Appendix.

2. COMET

In this section, we present COMET: COMpetitive Mechanisms for Efficient Transfer. The main idea of the method is to learn a set of generalisable and composable modules which encode the different modes of interaction between objects. Intuitively, while dynamics can vary across environments, the ways in which objects or entities interact with each other can be explained by a small number of independent rules. For example, in a traffic setting, whilst the behaviour of vehicles can differ across different locations, the act of stopping at a red light (the interaction between cars and traffic lights), can be used to explain behaviours in a wide range of environments. We argue that the ability to *selectively* update the modules during learning, i.e., to recognise parts of the model that are relevant to the data and perform modular updates, is instrumental to the emergence of such discrete independent mechanisms. To this end, we employ the competition of expert training procedure which only updates modules that best explains the interaction. In this scheme, modules that successfully captures reusable interactions automatically 'wins' more relevant training data and further specialises, which encourages a set of diverse modules that partitions the training data.

COMET learns from a dataset of observed sequences $\{\mathbf{x}^{1:T}\}_N$. Importantly, these sequences are sampled from environments with varying dynamics where objects can exhibit different behaviours. We assume that each observation, \mathbf{x}^t , can be factorised into latent object-slots, $\{\mathbf{z}_0^t, \mathbf{z}_1^t, \dots, \mathbf{z}_K^t\}$, where the subscript denotes the object-id. These object representations can be based on ground-truth masks or obtained from object-centric encoders [5, 8, 29]. COMET consists of two components trained in two phases:

the *mechanisms*, which models the interactions between objects and is trained in phase 1, and the *composition module*, which composes the mechanisms to explain a given environment and is trained in phase 2.

Mechanisms contains M independently parameterised feedforward networks, $f_{mech}^m : \mathbb{R}^{2d} \rightarrow \mathbb{R}^d$, with parameters θ_m , where d is the dimension of the object representations. Each mechanism predicts updates to all objects at every timestep, given the state of the object itself and another context object:

$$\Delta \mathbf{z}_i^t(m, j) = f_{mech}^m([\mathbf{z}_i^t \oplus \mathbf{z}_j^t]), \quad (1)$$

where \oplus denotes concatenation, i is the index of the object to be predicted and j is the index of the *context* object, i.e. the object with which object i interacts. The mechanisms are trained during the *competition* phase where each mechanism learns to specialise to cover a particular mode of interaction between objects. Concretely, for each object, the model makes predictions using all possible mechanism-context pairs in parallel. Comparing the predictions, we update the mechanism-context pair with the most accurate prediction for a given object. Given a state transition pair, $(\mathbf{z}_{1:K}^t, \mathbf{z}_{1:K}^{t+1})$, the loss function can be written as:

$$\mathcal{L}(\theta_{1:M}) = \sum_{i=0}^K \min_{m,j} [d(\mathbf{z}_i^t + \Delta \mathbf{z}_i^t(m, j), \mathbf{z}_i^{t+1})], \quad (2)$$

where d is a function that measures the prediction error. In this work, we use the Euclidean distance. Importantly, when performing back-propagation on this loss function, only the parameters of the competition winner are updated.

In order to predict transitions for objects using the trained mechanisms, the *composition module* picks the relevant context object and the active mechanism. The composition module acts as a classifier which picks the optimal mechanism-context pair for each object in the scene. Given the state of object i , for each mechanism-context pair, we compute the confidence score:

$$c_i^t(m, j) = f_{conf}^m([\mathbf{z}_i^t \oplus \mathbf{z}_j^t]), \quad (3)$$

where f_{conf}^m is an independently parameterised MLP for mechanism m , i.e. each mechanism has a corresponding f_{conf}^m . We predict a categorical distribution over all mechanism-context pairs by taking the softmax over the confidence scores for object i at time step t . Given a small number of observation sequences in a new environment, we obtain the best performing mechanism-context pair $(m^*, j^*)_i^t$ for each object at each time step by investigating which pair minimises the loss function of the competition scheme in Eq. 2. The composition module is then trained using the negative log-likelihood loss.

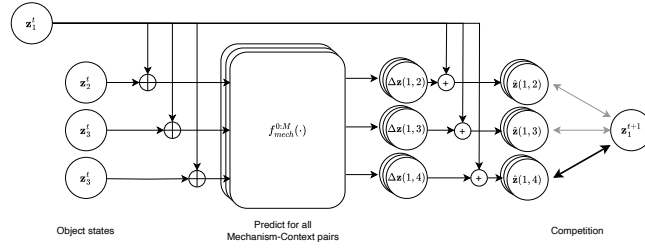


Figure 2. In the *competition* phase, predictions are made using all possible mechanism-context pairs for each object. Gradients are only allocated to the mechanism-context pair with the most accurate prediction. The figure describes the prediction step for a single object.

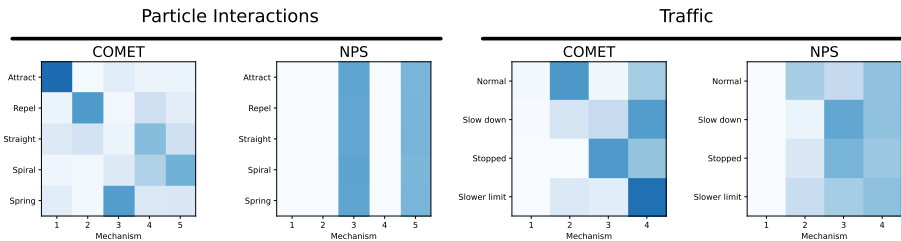


Figure 3. Disentanglement plots showing the correlation between mechanisms chosen by the models and ground-truth interaction modes. In the ideal case, the matrices should look like permutation matrices. Here, COMET is able to learn disentangled mechanisms that correspond to ground-truth behaviours in all three domains, as indicated by the fact that each interaction mode has one main corresponding learnt mechanism. In contrast, NPS does not exhibit the same structure.

157 3. Experiments

158 In this section, we demonstrate that COMET is able to dis-
159 entangle different modes of interaction between objects and
160 can efficiently reuse learnt mechanisms during adaptation.

161 **Baselines.** We evaluate COMET against two competitive
162 baselines, C-SWM [21] and Neural Production Systems
163 (NPS) [11]. C-SWM learns a world model from observa-
164 tion via contrastive learning with a GNN-based dynamics
165 model. Similar to COMET, C-SWM operates on an object-
166 factorised representation and achieves state-of-the-art pre-
167 diction accuracy. COMET further disentangles the inter-
168 actions between objects as independent mechanisms rather
169 than learning a monolithic model that captures all interac-
170 tions. We also compare against NPS, which learns to cap-
171 ture object interactions as independent mechanisms. Archi-
172 tecturally, NPS is similar to COMET, except that the
173 mechanism-context pair is selected using dot-product atten-
174 tion [42] which is trained jointly with the mechanisms. In
175 contrast, COMET deploys a competitive training scheme
176 which allows the model to recognise shared mechanisms
177 across environments. In our experiments, we show that
178 competition serves as a strong inductive bias that enables
179 the emergence of reusable mechanisms.

Datasets. We evaluate COMET on two problem domains: 180
Particle Interactions and *Traffic*. For each of these domains, 181
we define a set of environments where objects can exhibit 182
different behaviours. These environments are designed to 183
test whether COMET can extract meaningful mechanisms and 184
adapt to unseen environments via composition. The 185
Particle Interactions dataset consists of coloured particles 186
that can interact with each other in different ways such as at- 187
traction and repulsion. Environments are defined by a com- 188
bination of rules such as "red particles repel each other". 189
The *Traffic* dataset contains observation sequences of traffic 190
scenarios generated with the CARLA simulator [6]. Here, 191
the environments are defined by traffic rules that apply to 192
different vehicles such as "blue cars do not need to stop at 193
red lights". In both cases, the observations are given as 194
RGB images with ground-truth object masks such that each 195
object can be encoded into an object-slot. 196

Disentanglement of Mechanisms. We investigate the 197
emergence of recognisable mechanisms from competition. 198
Here, both COMET and NPS are trained on a mixture of 199
environments in each domain. We obtain the ground-truth 200
labels for the object interactions and use these to directly 201
investigate whether the learnt mechanisms correspond to 202
actual interactions without any supervision. These labels 203
are not accessible to the models during training. Fig. 3 204

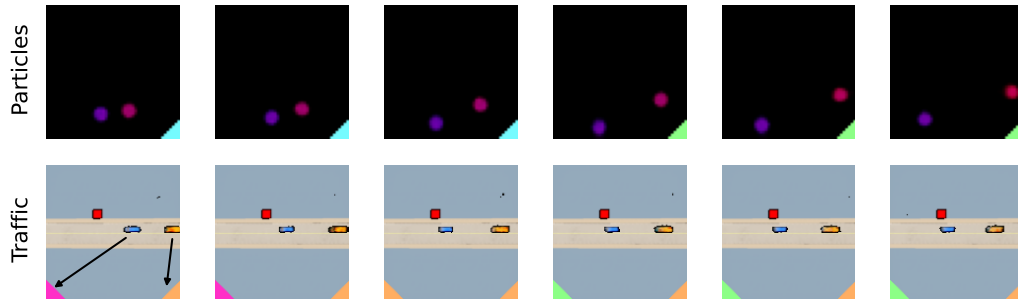


Figure 4. Qualitative rollouts. The colour of the tabs on the bottom of each frame indicates the 'winning' mechanism at each time step. Across all environments, the competition winner changes as the underlying interaction mode changes. **Top:** The particles repel each other when they are close (blue) and moves independently when they are apart (green). **Bottom:** In this traffic environment, the orange car obeys a slower speed limit and always pick the slow mechanism (orange). The blue car approaches the red light with normal driving (pink) → slow down (orange) → stop (green). Note that the orange mechanism is used as slow driving for both cars.

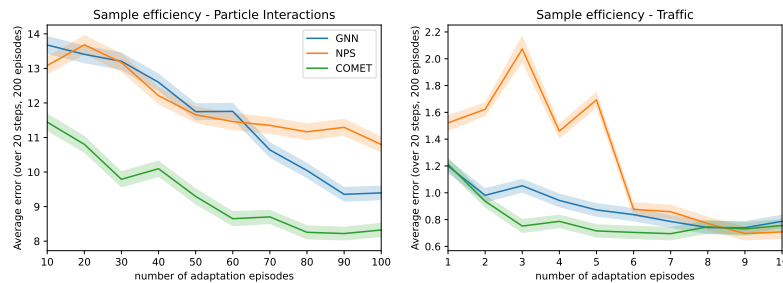


Figure 5. The average rollout error in an unseen environment with different amount of observed data in the new environment (lower is better). Shaded areas represent the standard errors of the mean. All models eventually converge to similar errors given enough data. However, COMET is able to achieve lower errors with few adaptation episodes. This means that COMET can learn to use the correct mechanisms with a small amount of data, thus corroborates our hypothesis that composing learnt mechanisms enables efficient transfer.

205 shows the correlation between the ground-truth interactions
 206 and the winning mechanisms in the competition process.
 207 COMET achieves successful disentanglement and learns
 208 mechanisms that corresponds to the ground-truth interac-
 209 tions, COMET recovering the ground-truth mode of interac-
 210 tions such as stopping before a red light. In contrast, the
 211 mechanisms learnt by NPS show no correspondence with
 212 the ground-truth interactions. This is likely because NPS
 213 cannot learn from a mixture of environments with varying
 214 dynamics as it employs a simple dot-product attention for
 215 picking mechanisms during training. To this end, COMET's
 216 ability to learn from diverse environments is uniquely af-
 217 forded by the competition scheme which assigns relevant
 218 data to update each mechanism. Fig. 4 qualitatively illus-
 219 trate that the 'winning' mechanisms switches as the under-
 220 lying interaction type changes.

221 **Adaptation Efficiency** One of our main hypotheses is
 222 that learning to compose learnt mechanisms leads to data-
 223 efficient adaptation. For each domain, we train all of the
 224 models on a mixture of environments and adapt the models
 225 to unseen environments. COMET adapts via the composi-

tion module, whereas the baselines adapt by finetuning the
 226 entire model on new data. Fig. 5 shows the performance
 227 of the models when trained on different amounts of data in
 228 the new environment. COMET outperforms the baselines
 229 in the low-data regime, illustrating that reusing mechanisms
 230 improves sample efficiency compared to finetuning.
 231

4. Conclusion 232

In this paper, we introduce COMET, a structured world
 233 model which encodes discrete abstract mechanisms explic-
 234 itly from observations. Our model performs *selective*
 235 updates during the training phase, a central capability
 236 which facilitates the emergence of recognisable and
 237 reusable mechanisms. We show experimentally that the
 238 proposed method is indeed able to disentangle shared me-
 239 chanisms across different environments from image observa-
 240 tions, and thus enables sample-efficient and interpretable
 241 adaptation to novel situations. Looking forward, we believe
 242 that the method developed here opens up several promising
 243 avenues of research, such as designing agents that learn a
 244 growing repertoire of re-usable interaction behaviours and
 245 agents that explore the world through the lens of mechanism
 246 discovery.
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Supplementary Material

453 5. Related Works

454 Learning internal models of the world enables decision-
455 making agents to plan, predict and reason about the world
456 [14, 15, 21]. As such, latent world models have attracted
457 significant interest in recent years. These methods [e.g.
458 21, 31, 44] in general involve learning latent representations
459 of the state and forward prediction models. Our work situ-
460 ates in this broad context of world model learning and we
461 focus our contribution on learning dynamics models which
462 are factorised into composable mechanisms. We take recent
463 works form object-centric state representations as a starting
464 point.

465 **Object-Centric Representations** There has been a grow-
466 ing interest in models that reflect the compositional nature
467 of real-world scenarios and aim to use object-centric rep-
468 resentations to leverage recurring features in scenes. Prior
469 works have investigated unsupervised object-centric repre-
470 sentation learning from static images [5, 8, 13, 26, 29]. Mo-
471 tivated by the assumption that dynamics tend to manifest
472 themselves at the object-level [3, 16], subsequent works
473 extend this capability to video data via factorised dynam-
474 ics models which operate on object-centric latent spaces.
475 While most of these object-centric world models (OCWMs)
476 are geared towards using temporal inputs to generate future
477 video rollouts [7, 19, 21, 22, 25, 30], some more explic-
478 itly consider their use in model-based reinforcement learn-
479 ing and planning [38, 43, 46, 47]. In particular, graph
480 neural networks (GNNs) are often used as a natural way
481 to predict future states of objects and enable the mod-
482 elling of interactions between objects via message passing
483 [21, 25, 34, 38, 40, 41, 43]. We build on these approaches
484 by further factorising the dynamics into reusable interaction
485 primitives.

486 **Mechanism-based Models** Our work is motivated by the
487 conjecture that the organisation of knowledge into high-
488 level abstract concepts is crucial to systematic generalisa-
489 tion [9]. This idea is similar in spirit to the *Independent*
490 *Causal Mechanisms* principle [35] and the *Sparse Mecha-*
491 *nism Shift* hypothesis [36] in the causality literature, which
492 respectively posit that data-generating causal mechanisms
493 operate independently from one another, and that changes
494 in the environment can be attributed to sparse changes to
495 such mechanisms. Several works [17, 24, 27] have lever-
496 aged causal discovery techniques, e.g., sparsity regularisa-
497 tion, to learn dynamics models that are factorised into struc-
498 tural causal models.

Similar to our approach is a class of models which represents
the learned dynamics in OCWMs not as a monolithic
module, but rather as a collection of independently acting
mechanisms – each focusing on a different aspect of the en-
vironment’s dynamics. Becker-Ehmck et al. [4] use a vari-
ational approach to learn to pick different transition models
conditioned on the state, but is limited to linear transitions.
RIMs [12] constitute an approach where parts of the state
space are represented by independent and sparsely interact-
ing recurrent units. Building on this, [10] use a GNN to
model environment dynamics but reflect the concept of in-
dependent mechanisms by using different sets of GNN pa-
rameters depending on an object’s current state. Another
approach that follows this line of work is VIM [2] which
considers the disentanglement of mechanisms and objects
in the setting where object move independently to each
other. Closer to our method are Neural Production Systems
(NPS) [11], another descendant of RIMs, learning a set of
independent mechanisms capturing the interaction between
objects. Our method differs from NPS in the application of
competition training which, as we demonstrate empirically
in Sec. 3, is instrumental to the emergence of composable
mechanisms. Furthermore, we propose a novel method for
adapting to changes in the environment.

Competition of Experts The backbone of our learning
algorithm draws from mixture of experts methods [18, 20,
37] and in particular from the algorithm of Parascandolo
et al. [33]. In the context of learning independent causal
mechanisms, Parascandolo et al. [33] demonstrate that the
competition of experts algorithm induces the emergence of
mechanisms that explain transformations in the data. The
idea of utilising a competitive training scheme on modu-
lar model architectures has been applied on diverse settings
such as lifelong learning [1, 32], generative models [28] and
object-centric scene composition [45]. Taking inspiration
from this line of work, COMET uses a similar competi-
tive training scheme as an inductive bias for disentangling
modes of interaction in the setting of world model learning.