000 001 002 003 MEMSIM: A BAYESIAN SIMULATOR FOR EVALUATING MEMORY OF LLM-BASED PERSONAL ASSISTANTS

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Paper under double-blind review

ABSTRACT

LLM-based agents have been widely applied as personal assistants, capable of memorizing information from user messages and responding to personal queries. However, there still lacks an objective and automatic evaluation on their memory capability, largely due to the challenges in constructing reliable questions and answers (QAs) according to user messages. In this paper, we propose MemSim, a Bayesian simulator designed to automatically construct reliable QAs from generated user messages, simultaneously keeping their diversity and scalability. Specifically, we introduce the Bayesian Relation Network (BRNet) and a causal generation mechanism to mitigate the impact of LLM hallucinations on factual information, facilitating the automatic creation of an evaluation dataset. Based on MemSim, we generate a dataset in the daily-life scenario, named MemDaily, and conduct extensive experiments to assess the effectiveness of our approach. We also provide a benchmark for evaluating different memory mechanisms in LLM-based agents with the MemDaily dataset. To benefit the research community, we have released our project at <https://anonymous.4open.science/r/MemSim>.

1 INTRODUCTION

029 030 031 032 033 034 035 036 037 038 039 In recent years, large language model (LLM) based agents have been extensively deployed across various fields [\(Guo et al., 2024;](#page-10-0) [Wang et al., 2024;](#page-11-0) [Xi et al., 2023;](#page-11-1) [Ge et al., 2023;](#page-10-1) [Wang et al., 2023;](#page-11-2) [Wu et al., 2023\)](#page-11-3). One of their most significant applications is serving as personal assistants [\(Li](#page-10-2) [et al., 2024\)](#page-10-2), where they engage in long-term interactions with users to address a wide range of issues [\(Lu et al., 2023;](#page-11-4) [Lee et al., 2023\)](#page-10-3). For LLM-based personal assistants, memory is one of the most significant capability [\(Zhang et al., 2024\)](#page-12-0). To perform personal tasks effectively, these agents must be capable of storing factual information from previous messages and recalling relevant details to generate appropriate responses. For example, a user Alice might tell the agent, "*I will watch a movie at City Cinema this Friday in Hall 3, Row 2, Seat 9.*" When Friday arrives, she might ask the agent, "*Where is my movie seat?*" Then, the agent should recall the relevant information (i.e., the seat number) to generate an appropriate response to Alice.

040 041 042 043 044 045 046 047 048 049 050 051 052 053 Previous research has proposed methods for constructing the memory of LLM-based agents [\(Zhong](#page-12-1) [et al., 2024;](#page-12-1) [Modarressi et al., 2023;](#page-11-5) [Lu et al., 2023;](#page-11-4) [Packer et al., 2023;](#page-11-6) [Shinn et al., 2024\)](#page-11-7). However, there remains a lack of objective and automatic methods to evaluate how well personal assistants can memorize and utilize factual information from previous messages, which is crucial for developing memory mechanisms. One conventional solution is to collect messages from real-world users, and manually annotate answers to human-designed questions based on these messages. However, it requires substantial human labor that lacks **scalability**. Another solution is to generate user messages and question-answers (QAs) with LLMs. However, the hallucination of LLMs can severely undermine the reliability of generated datasets, particularly in complex scenarios [\(Huang et al., 2023\)](#page-10-4). Here, we refer to the reliability of a dataset as the correctness of its ground truths to factual questions given the corresponding user messages. Our research shows that due to the hallucination of LLMs, the correctness of ground truths generated by vanilla LLMs is less than 90% in most scenarios and can fall below 40% in some complex scenarios (see Section [5.2\)](#page-8-0). For instance, when posing aggregative questions like "*How many people are under the age of 35?*," they often provide incorrect answers due to hallucinations. Moreover, generating diverse user profiles through LLMs is also challenging, as they tend to produce the most plausible profiles that lack **diversity**.

054 055 056 057 058 059 060 061 062 063 064 065 066 To address these challenges, we propose MemSim, a Bayesian simulator designed to construct reliable QAs from generated user messages, simultaneously keeping their diversity and scalability, which can be utilized to evaluate the memory capability of LLM-based personal assistants. Specifically, we introduce the Bayesian Relation Network (BRNet) to generate the simulated users that are represented by their hierarchical profiles. Then, we propose a causal generation mechanism to produce various types of user messages and QAs for the comprehensive evaluation on memory mechanisms. By using BRNet, we improve the diversity and scalability of generated datasets, and our framework can effectively mitigate the impact of LLM hallucinations on factual information, which makes the constructed QAs more reliable. Based on MemSim, we create a dataset in the daily-life scenario, named MemDaily, and perform extensive experiments in multiple aspects to assess the quality of MemDaily. Finally, we construct a benchmark to evaluate different memory mechanisms of LLMbased agents with MemDaily. Our work is the first one that evaluates memory of LLM-based personal assistants in an objective and automatic way. Our contributions are summarized as follows:

067 068 • We analyze the challenges of constructing datasets for objective evaluation on the memory capability of LLM-based personal assistants, focusing on the aspects of reliability, diversity, and scalability.

069 070 071 • We propose MemSim, a Bayesian simulator designed to generate reliable, diverse and scalable datasets for evaluating the memory of LLM-based personal assistants. We design BRNet to generate the simulated users, and propose a causal generation mechanism to construct user messages and QAs.

072 073 074 075 076 • We create a dataset in the daily-life scenario based on our framework, named MemDaily, which can be used to evaluate the memory capability of LLM-based personal assistants. We perform extensive experiments to assess the quality of MemDaily in multiple aspects, and provide a benchmark for different memory mechanisms of LLM-based agents. To support the research community, we have made our project available at <https://anonymous.4open.science/r/MemSim>.

077 078 079 080 081 The rest of our paper is organized as follows. In Section [2,](#page-1-0) we review the related works on the evaluation of memory in LLM-based agents and personal assistants. In Section [3,](#page-2-0) we introduce the details of MemSim, and the generation process of MemDaily. In Section [4,](#page-6-0) we assess the quality of MemDaily. Section [5](#page-7-0) provides a benchmark for evaluating different memory mechanisms of LLM-based agents. Finally, in Section [6,](#page-9-0) we discuss the limitations of our work and draw conclusions.

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2 RELATED WORKS

085 086 087 088 089 090 091 092 LLM-based agents have been extensively utilized across various domains, marking a new era for artificial personal assistants [\(Li et al., 2024\)](#page-10-2). For LLM-based personal assistants, memory is a critical component that enables agents to deliver personalized services. This includes storing, managing, and utilizing users' personal and historical data [\(Zhang et al., 2024;](#page-12-0) [Zhong et al., 2024;](#page-12-1) [Shinn et al.,](#page-11-7) [2024;](#page-11-7) [Yao et al., 2023\)](#page-11-8). For instance, MPC [\(Lee et al., 2023\)](#page-10-3) suggests storing essential factual information in a memory pool with a summarizer for retrieval as needed. MemoryBank [\(Zhong et al.,](#page-12-1) [2024\)](#page-12-1) converts daily events into high-level summaries and organizes them into a hierarchical memory structure for future retrieval. These approaches primarily aim to enhance agents' memory capability.

093 094 095 096 097 098 099 Previous studies have also attempted to evaluate the memory capability of LLM-based agents, but there still exist limitations. Some studies use subjective methods, employing human evaluators to score the effectiveness of retrieved memory [\(Lee et al., 2023;](#page-10-3) [Zhong et al., 2024;](#page-12-1) [Liu et al., 2023\)](#page-10-5). However, this approach can be costly due to the need for evaluators and may introduce biases from varying annotators. Other studies use objective evaluations by constructing dialogues and questionanswer pairs [\(Packer et al., 2023;](#page-11-6) [Hu et al., 2023;](#page-10-6) [Maharana et al., 2024\)](#page-11-9), but these methods still require human involvement for creating or editing the QAs. Therefore, how to construct reliable QAs according to user messages automatically is significant for the objective evaluation.

100 101 102 103 104 105 106 107 Some previous studies construct knowledge-based question-answering (KBQA) datasets to assess Retrieval-Augmented Generation (RAG) [\(Lan et al., 2021;](#page-10-7) [Peng et al., 2024\)](#page-11-10), which is relative to the data generation for memory evaluation. These studies typically either use knowledge graphs to generate QAs through templates or manually annotate QAs with human input [\(Zhang et al., 2023;](#page-12-2) [Cao et al., 2020;](#page-10-8) [Jin et al., 2024;](#page-10-9) [Huang et al., 2024;](#page-10-10) [Kwiatkowski et al., 2019;](#page-10-11) [Yang et al., 2024\)](#page-11-11). However, most of these efforts focus on common-sense questions rather than personal questions whose answers are only determined by the user messages in the same trajectory. They do not include textual user messages and target indexes for retrieval evaluation [\(Cao et al., 2020;](#page-10-8) [Jin et al., 2024;](#page-10-9)

Figure 1: Overview of MemSim and MemDaily.

129 130 131 132 [Huang et al., 2024;](#page-10-10) [Yih et al., 2016;](#page-12-3) [Talmor & Berant, 2018\)](#page-11-12). Additionally, they are highly dependent on the entities extracted from the given corpus, which limits their scalability [\(Cao et al., 2020;](#page-10-8) [Yih](#page-12-3) [et al., 2016\)](#page-12-3). Our work is the first one that evaluate memory of LLM-based personal assistants in an objective and automatic way, which can generate user messages and QAs without human annotators, keeping reliability, diversity and scalability.

3 METHODS

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136 137 138 139 140 141 142 Our final goal is to evaluate memory mechanisms of LLM-based personal assistants in an objective and automatic way. The whole pipeline is demonstrated in Figure [1.](#page-2-1) First of all, we propose MemSim that can simulate users and generate evaluation datasets, mainly including the Bayesian Relation Network and a causal generation mechanism. Then, we employ MemSim to create a dataset in the daily-life scenario, named MemDaily. Finally, we construct a benchmark that evaluates different memory mechanisms of LLM-based agents based on MemDaily. In this section, we will deliver the details of MemSim and MemDaily, while the evaluation benchmark will be presented in Section [5.](#page-7-0)

143 3.1 OVERVIEW OF MEMSIM

144 145 146 147 148 149 150 151 152 153 In order to construct reliable QAs from generated user messages, we propose a Bayesian simulator named MemSim, which includes two primary components. First, we develop the Bayesian Relation Network to model the probability distribution of users' relevant entities and attributes, enabling the sampling of diverse hierarchical user profiles. Then, we introduce a causal mechanism to generate user messages and construct reliable QAs based on these sampled profiles. We design various types of QAs for comprehensive memory evaluation, including single-hop, multi-hop, comparative, aggregative, and post-processing QAs, incorporating different noises to simulate real-world environments. Based on the constructed QAs and generated user messages, researchers can objectively and automatically evaluate the memory capability of LLM-based personal assistants on factual information from previous messages, which can be helpful in developing advanced memory mechanisms.

154 155 3.2 BAYESIAN RELATION NETWORK

156 157 158 159 160 161 We introduce Bayesian Relation Network (BRNet) to model the probability distribution of users' relevant entities and attributes, where we sample hierarchical profiles to represent simulated users (see Figure [1\(](#page-2-1)a)). Specifically, we define a two-level structure in BRNet, including the entity level and the attribute level. The entity level represents user-related entities, such as relevant persons, involved events, and the user itself. At the attribute level, each entity comprises several attributes, such as age, gender, and occupation. Here, BRNet actually serves as a predefined meta-user. Formally, let A^1, \ldots, A^N represent different entities, and each entity A^i comprises several attributes

162 163 164 165 $\{A_1^i, A_2^i, \ldots, A_{N^i}^i\}$, where N is the number of entities, and Nⁱ is the number of attributes belonging to the entity \mathcal{A}^i . Each attribute A^i_j corresponds to a random variable X^i_j , which can be sampled in a value space. For example, the *college's* (entity \mathcal{A}^i) *age* (attribute A^i_j) is 28 years old (value $x^i_j \sim X^i_j$).

166 167 168 169 170 171 172 173 174 175 We denote BRNet as a directed graph $G = \langle V, E \rangle$ at the attribute level, where the vertex set V includes all attributes, i.e., $V = \bigcup_{i=1}^{N} \{A_1^i, A_2^i, \dots, A_{N^i}^i\}$. The edge set E captures all the direct causal relations among these attributes, defined as $E = \{ \langle A_j^i, A_l^k \rangle \mid \forall X_j^i, X_l^k \in \mathcal{X}, X_j^i \to X_l^k \},$ where $\mathcal{X} = \bigcup_{i=1}^N \{X_1^i, X_2^i, \dots, X_{N^i}^i\}$. For better demonstration, in this subsection, we simplify the subscripts of the variables in X as $1, 2, ..., \sum_{i=1}^{N} N_i$. The conditional probability distribution among them can either be explicitly predefined or implicitly represented by LLM's generation with conditional prompts. It is important to note that we assume the causal structure is loop-free, ensuring that BRNet forms a directed acyclic graph (DAG), which is typical in most scenarios [\(Heinze-Deml](#page-10-12) [et al., 2018\)](#page-10-12). Additionally, the vertices (i.e., attributes), edges (i.e., causal relations), and conditional probability distributions (i.e., prior knowledge) can be easily scaled to different scenarios.

176 177 178 179 180 So far, we have constructed the BRNet, where the joint probability distribution $P(X_1, X_2, \ldots, X_{|\mathcal{X}|})$ over all attributes can represent the user distribution in the given scenario. Then, we can sample different values of attributes on entities from BRNet to represent various user profiles. One straightforward approach is to compute the joint probability distribution and sample from it.

181 Assumption 1 (Local Markov Property). *BRNet satisfies the local Markov property, which states that*

 $X_t \perp \!\!\! \perp X_{\overline{des}(X_t)} | par(X_t), \forall X_t \in \mathcal{X},$

183 184 185 *where* $des(X_t)$ *denotes the non-descendant set of* X_t *,* $par(X_t)$ *denotes the parent set of* X_t *, and the notation* · ⊥⊥ ·|· *indicates the variables are conditionally independent.*

186 187 188 Because the parents of an attribute can be extended to any non-descendant attributes of it by adding a new edge if they have a direct causal relation. Therefore, given these parent attributes, other non-descendent attributes are conditionally independent of that attribute.

Theorem 1 (Factorization). *The joint probability distribution of BRNet can be expressed as*

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P(X_1, X_2, ..., X_{|\mathcal{X}|}) = \prod_{X_t \in \mathcal{X}} P(X_t | par(X_t)),
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where $par(X_t)$ *denotes the set of parent attributes of* X_t *.*

194 195 196 197 198 199 The proof of Theorem [1](#page-3-0) is provided in Appendix [A.1.](#page-13-0) However, calculating the joint probability distribution and sampling from it may be impractical in our scenarios. First, the joint probability distribution is often high-dimensional, making its calculation and sampling costly. Second, some conditional probability distributions are difficult to represent in explicit forms, particularly when using LLMs for value generation through conditional prompts. To address these issues, we introduce the ancestral sampling process to obtain the values of attributes.

200 201 Assumption 2 (Conditional Sampling). *In BRNet, an attribute can be sampled from the conditional probability distribution given its parent attributes. Specifically, we have*

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\tilde{x}_t \sim P\left(X_t|par\left(X_t\right)\right), \forall X_t \in \mathcal{X},
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203 *where the conditional probability distribution can be expressed in either explicit or implicit forms.*

205 206 207 208 209 210 211 The ancestral sampling algorithm is outlined as follows. First, we obtain the topological ordering of BRNet using Kahn's algorithm [\(Kahn, 1962\)](#page-10-13). Next, we sample all attributes according to this ordering. For top-level attributes without parents, the sampling is performed based on their marginal probability distributions. For other variables like X_t , we sample their values using the conditional probability distribution $\tilde{x}_t \sim P(X_t|par(X_t))$ as specified in Assumption [2.](#page-3-1) Finally, we consider each sampling result $\{\tilde{x}_1, \tilde{x}_2, \ldots, \tilde{x}_{|\mathcal{X}|}\}$ as the attribute-level profiles of a user, which constitute different entities as the entity-level profiles of the user. These two levels represent the user in different grains, which are important to generate user messages and QAs subsequently.

212 213 Theorem 2 (Ancestral Sampling). *For BRNet, the result of ancestral sampling is equivalent to that of sampling from the joint probability distribution. Specifically, we have*

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P(\tilde{x}_1, \tilde{x}_2, ..., \tilde{x}_{|\mathcal{X}|}) = P(x_1, x_2, ..., x_{|\mathcal{X}|}),
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where $x_1, x_2, ..., x_{|\mathcal{X}|} \sim P(X_1, X_2, ..., X_{|\mathcal{X}|})$ *are sampled from the joint probability distribution.*

Types	Descriptions	Examples	Causal Hints	Retrieval Target
Single-hop	Rely on one message to an- swer the question directly.	O: When is Alice's birthday? A: June 1st.	$({\cal A}_{(i)}, K_{(i)}, v_{(i)})$	${m_{(i)}\}$
Multi-hop	Require multiple messages to answer the question jointly.	Q: Where is the meeting that I will attend next week? A: Victoria Conference Center.	$({\cal A}^t, K_{(j)}, x_{(j)}),$ $(\mathcal{A}^t, K_{(k)}, x_{(k)})$	${m_{(i)}, m_{(k)}}$
	Comparative Compare two entities on a shared attribute with multi- ple messages.	Q: Who is younger between Alice and Bob? A: Bob.	$(\mathcal{A}_{(i)}, K, v_{(i)}),$ $(\mathcal{A}_{(k)}, K, v_{(k)})$	${m_{(i)}, m_{(k)}}$
Aggregative	Aggregate messages about more than two entities on a common attribute.	Q: How many people are under 35 years old? A: Three.	$\{(\mathcal{A}_{(i_k)}, K, v_{(i_k)})\}_{k=1}^d \{m_{(i_k)}\}_{k=1}^d$	
Post- processing	Involve extra reasoning steps to answer with multi- ple messages.	O: What season was the teacher that I know born in? A: Spring.	$({\cal A}^t, K_{(j)}, v_{(j)}),$ $(\mathcal{A}^t, K_{(k)}, v_{(k)})$	${m_{(i)}, m_{(k)}}$

Table 1: Overview of comprehensive questions and answers.

The proof can be found in Appendix [A.2.](#page-13-1) By employing ancestral sampling, we eliminate the need to compute the joint probability distribution, making the sampling process more efficient and practical. By utilizing BRNet, we introduce prior knowledge of the specific scenario into the graphical structure and sampling process, which can improve the diversity and scalability of user profiles, thereby enhancing the diversity and scalability of whole datasets.

238 3.3 CAUSAL GENERATION MECHANISM

239 240 241 242 243 244 245 Based on hierarchical user profiles, we propose a causal generation mechanism to generate user messages, and construct reliable QAs corresponding to them. Here, *causal* indicates that the generation of user messages and the construction of QAs are causally dependent on the same informative *hints* that are also causally derived from hierarchical user profiles. Specifically, we define a piece of hint as a triple (A^i, A^i_j, x^i_j) that provides factual information in a structural format. In other words, the hierarchical user profiles provide a structural foundation to get different hints, which then provide a set of relevant information as the causation of both user messages and QAs, shown in Figure [1\(](#page-2-1)b).

246 247 248 249 250 251 252 253 Construction of Informative Hints. We construct the hints of factual information based on hierarchical user profiles before creating the user messages and QAs. We select a target entity \mathcal{A}^t at the entity-level, and choose l^t attributes $\{K_1^t, K_2^t, \ldots, K_{l^t}^t\} \subseteq \mathcal{A}^t$ along with their corresponding values $\{v_1^t, v_2^t, \ldots, v_{l^t}^t\}$ from the attribute-level profiles. Then, we reformulate them into a list of triple hints $H^t = [(\mathcal{A}^t, K_i^t, v_i^t)]_{i=1}^t$. For some complex types of QAs, we choose more than one target entities, and concatenate their lists of hints. For better demonstration, we re-index the final list of hints as $H = [(\mathcal{A}_{(j)}, K_{(j)}, v_{(j)})]_{j=1}^l$, where l is the number of hints in the final list.

254 255 256 257 258 259 260 Construction of User Messages. Based on the j-th hint $(A_{(j)}, K_{(j)}, v_{(j)}) \in H$, we construct the corresponding user message $m_{(j)}$ with LLM, where we have $m_{(j)} = LLM(\mathcal{A}_{(j)}, K_{(j)}, v_{(j)})$. Here, the LLM only serves the purpose of rewriting structural hints, without any reasoning process. For example, if the hint is (*my uncle Bob*, *occupation*, *driver*), the generated user message might be "*The occupation of my uncle Bob is a driver*". We generate user messages for all the hints in H, and we finally get the list of user messages $M = [m_{(j)}]_{j=1}^{l}$.

261 262 263 264 265 266 Construction of Questions and Answers. In order to evaluate the memory capability of LLM-based personal assistants more comprehensively, we propose to construct five representative types of QAs to cover various complexities in real-world scenarios, as detailed in Table [1.](#page-4-0) For each question q , we provide three forms of ground truths: (1) the textual answer a that can correctly respond to q , (2) the correct choice a among confusing choices a' (generated by LLM) as a single-choice format, and (3) the correct retrieval target $h \subseteq M$ that contains the required factual information to the question.

267 268 269 *(i.) Single-hop QA.* Single-hop QA is the most basic type of QAs, relying on a single piece message to directly answer the question. In constructing QA, we randomly select the j-th hint $(A_{(j)}, K_{(j)}, v_{(j)})$ and generate the question $q = LLM(\mathcal{A}_{(j)}, K_{(j)})$ through LLM rewriting, where the answer is $a = v_{(j)}$. Correspondingly, the retrieval target is $h = \{m_{(j)}\}.$

Table 2: Summary of the MemDaily dataset.

Statistics	Simp.	Cond.	Comp.	Aggr.	Post.	Noisy	Total
Trajectories	500	500	492	462	500	500	2.954
Messages	4215	4195	3144	5536	4438	4475	26,003
Ouestions	500	500	492	462	500	500	2,954
TPM	15.48	15.49	14.66	14.65	17.07	16.14	15.59

279 280 281 282 283 284 *(ii.) Multi-hop QA.* Multi-hop QA necessitates the use of multiple messages to determine the correct answer, making it more complex than single-hop QA. In constructing Multi-hop QA, we first sample two hints $(A_{(j)}, K_{(j)}, v_{(j)})$ and $(A_{(k)}, K_{(k)}, v_{(k)})$ from the same bridge entity A^t (i.e., $A^t = A_{(j)}$ = $\mathcal{A}_{(k)}$). We then mask this bridge entity and generate the question $q = LLM(K_{(j)}, v_{(j)}, K_{(k)})$ through LLM rewriting, where the answer is $a = v_{(k)}$. The target message set is $h = \{m_{(j)}, m_{(k)}\}.$ By incorporating additional entities, the questions can be easily extended to more hops.

285 286 287 288 289 290 *(iii.) Comparative QA.* Comparative QA is an extensive type of multi-hop QA, which involves comparing two entities based on a shared attribute. We first select two hints $(A_{(j)}, K_{(j)}, v_{(j)})$ and $(\mathcal{A}_{(k)}, K_{(k)}, v_{(k)})$ from different entities with the same meaning attribute K (i.e., $\mathcal{A}_{j} \neq \mathcal{A}_{k}$ and $K \cong$ $K_{(j)} \cong K_{(k)}$). We then rewrite the question $q = LLM(\mathcal{A}_{(j)}, \mathcal{A}_{(k)}, K)$ by LLM, where the answer $a = f(K, v_{(j)}, v_{(k)})$ is derived from the function $f(\cdot)$. The retrieval target is $h = \{m_{(j)}, m_{(k)}\}.$

291 292 293 294 295 *(iv.) Aggregative QA.* Aggregative QA is a general type of comparative QA, which requires aggregating messages from more than two entities on a shared attribute. For construction, we choose d hints $\{(\mathcal{A}_{(j_k)}, \mathcal{K}, v_{(j_k)})\}_{k=1}^d$ from different entities with the same meaning attribute K. Then, we construct the question $q = LLM(\{\mathcal{A}_{(j_k)}\}_{j=1}^d, K)$, where we obtain the answer $a = f(K, \{v_{(j_k)}\}_{k=1}^d)$. The target message set should include all these related references, that is, $h = \{m_{(j_k)}\}_{k=1}^d$.

296 297 298 299 300 301 *(v.) Post-processing QA.* Post-processing QA addresses situations where personal questions require additional reasoning steps for agents to answer, based on the retrieved messages. We first select two hints $(A_{(j)}, K_{(j)}, v_{(j)})$ and $(\mathcal{A}_{(k)}, K_{(k)}, v_{(k)})$ from the same bridge entity \mathcal{A}^t . We then design a reasoning factor ψ to generate the question $q = LLM(K_{(j)}, v_{(j)}, K_{(k)}, \psi)$, and derive the answer $a = f(K_{(k)}, v_{(k)}, \psi)$, where ψ specifies the reasoning process. For example, it could be "*the sum of the last five digits of the phone number* $v_{(k)}$ ". Similarly, the retrieval target will be $h = \{m_{(j)}, m_{(k)}\}$.

302 303 304 305 306 Infusion of Noise in User Messages. We integrate two types of noise in user messages by concatenation, in order to simulate real-world circumstances. The first type is entity-side noise, which refers to noisy messages that contain the selected attributes from unselected entities. The second type is attribute-side noise, which involves noisy messages that describe unselected attributes of the selected entities. Both types of noise can impact agents' ability to retrieve messages and generate answers.

307 308 309 310 311 312 313 314 315 316 317 Eventually, we formulate the trajectory $\xi = (M, q, a, a', h)$ by discarding all hints, where each trajectory serves as a test instance for evaluating the memory capability of LLM-based personal assistants. There are two insights into the causal generation mechanism. First, the factual information of messages and QAs are causally constructed from the shared hints that are sampled from user profiles, where LLMs are only responsible for rewriting based on the given information, rather than imagining or reasoning. This pipeline mitigates the impact of LLM hallucination on the factual information, keeping the reliability of QAs. It can also prevent contradictions among user messages from the same trajectory, because their hints are derived from the same user profile. Second, our method focuses on designing the asymmetric difficulty between constructing QAs (i.e., profiles→hints→messages, question and answer) and solving QAs (i.e., messages|question→answer), which is critical for the automatic generation of evaluation datasets.

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319 3.4 MEMDAILY: A DATASET IN THE DAILY-LIFE SCENARIO

320 321 322 323 Based on MemSim, we create a dataset in the daily-life scenario, named MemDaily, which can be used to evaluate the memory capability of LLM-based personal assistants, shown in Figure [1\(](#page-2-1)c). Specifically, MemDaily incorporates 11 entities and 73 attributes (see details in Appendix [E.1\)](#page-18-0), all of which are representative and closely related to users' daily lives. We create 6 sub-datasets of different QA types mentioned previously: (1) Simple (Simp*.*): single-hop QAs. (2) Conditional (Cond.):

Methods	R-Human	R-GPT	SWI-R	SWI-O	SWI-A
IndePL	1.35 ± 0.53	4.32	0.464	0.231	0.347
SeqPL	1.64 ± 0.73	4.40	1.471	1.416	1.443
JointPL	3.02 ± 1.14	4.80	1.425	0.462	0.943
MemSim	4.91 ± 0.30	4.68	3.206	2.895	3.050

Table 3: Results of the evaluation on user profiles.

333 334 335 336 337 multi-hop QAs with conditions. (3) **Comparative (Comp.**): comparative QAs. (4) **Aggregative** (Aggr.): aggregative QAs. (5) Post-processing (Post.): post-processing QAs. (6) Noisy: multi-hop QAs with additional irrelevant noisy texts inside questions. The summary of MemDaily is shown in Table [2,](#page-5-0) where we present the number of trajectories, user messages, questions, and TPM (tokens per message). More details and examples can be found in Appendix [E.](#page-18-1)

4 EVALUATIONS

In this section, we evaluate the quality of MemDaily, which can reflect the effectiveness of MemSim. Specifically, the evaluations are conducted in three parts: the user profiles, the user messages, and the constructed QAs. Besides, we also conduct comprehensive case studies in Appendix [E.](#page-18-1)

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4.1 EVALUATION ON USER PROFILES

346 347 348 349 350 The generated user profiles are supposed to express both rationality and diversity, which also directly influence the creation of user messages and QAs. Therefore, we evaluate these two aspects to reflect their quality. Rationality means that the user profiles should possibly exist in the real world, with no internal contradictions in their descriptions. Diversity indicates that the descriptions among users are distinct, covering a wide range of user types.

351 352 353 354 Metrics. For rationality, we recruit six human evaluators to score the generated user profiles on a scale from [1](#page-6-1) to 5. Additionally, we use GPT-40 $¹$ as a reference for scoring. These two metrics are</sup> denoted as R-Human and R-GPT. For diversity, we calculate the average Shannon-Wiener Index (SWI) [\(Morris et al., 2014\)](#page-11-13) on key attributes, using the following formula:

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 $SWI-W = -\frac{1}{114}$ $|\mathcal{W}|$ \sum $X_k \in \mathcal{W}$ \sum $x_i \in X_k$ $p(x_i) \ln p(x_i),$

358 359 where $W \subseteq \mathcal{X}$ is the subset of attribute variables. Therefore, we calculate SWI-R, SWI-O, and SWI-A, corresponding to role-relevant attributes, role-irrelevant attributes, and all attributes, respectively.

360 361 362 363 364 Baselines. We design several baselines to generate user profiles: (1) **JointPL**: prompting an LLM to generate attributes jointly. (2) **SeqPL**: prompting an LLM to generate attributes sequentially, conditioned on previous attributes in linear order. (3) **IndePL**: prompting an LLM to generate attributes independently. We compare our method with these baselines on generating user profiles.

365 366 367 368 Results. As shown in Table [3,](#page-6-2) MemSim outperforms other baselines on R-Human, demonstrating the effectiveness of BRNet as an ablation study. However, we also observe an inconsistency between R-Human and R-GPT, which may be due to the inaccuracy of the LLM's scoring [\(Chu et al., 2024\)](#page-10-14). Furthermore, our method achieves the highest diversity compared to the other baselines.

369 4.2 EVALUATION ON USER MESSAGES

371 372 373 We evaluate the quality of generated user messages in multiple aspects, including fluency, rationality, naturalness, informativeness, and diversity. The first four aspects are designed to assess the quality inside a trajectory, while the final one targets the variety across trajectories.

374 375 376 Metrics. For the inside-trajectory aspects, human evaluators score user messages on a scale from 1 to 5, denoted as F-Human (fluency), R-Human (rationality), N-Human (naturalness), and I-Human (informativeness). GPT-4o scores are also available and detailed in Appendix [C.](#page-14-0) To assess the

¹<https://openai.com/index/hello-gpt-4o/>

Methods	F-Human	R-Human	N-Human	L-Human	SWIP
ZeroCons	$4.94 + 0.24$	4.94 ± 0.24	4.85 ± 0.35	2.82 ± 1.15	2.712
PartCons	4.98 ± 0.14	$4.94 + 0.37$	4.97 ± 0.18	$4.01 + 1.18$	6.047
SoftCons	4.93 ± 0.30	4.80 ± 0.77	$4.91 + 0.42$	4.37 ± 0.98	5.868
MemSim	$4.93 + 0.30$	4.93 ± 0.39	$4.90 + 0.41$	3.61 ± 1.19	6.125

Table 4: Results of the evaluation on user messages.

Table 5: Results of the evaluation on questions and answers.

399 400 diversity across trajectories, we extract all entities and calculate their average Shannon-Wiener Index per 10,000 tokens of user messages, referred to as SWIP.

401 402 403 404 405 406 407 408 Baselines. We implement several baselines that generate messages under different constraints regarding user profiles and tasks: (1) **ZeroCons**: no constraints on attributes when prompting LLMs. (2) PartCons: partial attributes of user profiles are constrained in prompts for LLMs. (3) SoftCons: full attributes of user profiles are constrained in prompts but they are not forcibly for generation. Our MemSim method imposes the most strict constraints, requiring both the integration of specific attributes into user messages and ensuring that questions are answerable with established ground truths based on the shared hints. Generally, higher constraint commonly means sacrifice of fluency and naturalness, because it compulsively imposes certain information to benefit QA constructions.

409 410 411 412 Results. As shown in Table [4,](#page-7-1) our method maintains relatively high scores despite the rigorous constraints on constructing reliable QAs. Additionally, MemSim exhibits the highest diversity index, attributed to the BRNet and the causal generation mechanism that produces a wider variety of user messages based on the provided hierarchical user profiles.

413 414 4.3 EVALUATION ON QUESTIONS AND ANSWERS

415 416 417 418 419 The primary challenge for constructing a reliable dataset is ensuring the accuracy of ground truths for the constructed questions. To assess the reliability of MemDaily, we sample approximately 20% of all the trajectories in MemDaily and employ human evaluators to verify the correctness of their ground truths. Specifically, the evaluators are required to examine three parts of the ground truths: textual answers, single-choice answers, and retrieval targets, and report their accuracy.

420 421 422 423 424 Metrics. The accuracy of textual answers assesses whether an answer correctly responds to the question based on the user messages within the same trajectory. The accuracy of single-choice answers indicates whether the ground truth choice is the sole correct answer for the question, given the user messages, while other choices are incorrect. The accuracy of retrieval targets evaluates whether the messages of the retrieval target are sufficient and necessary to answer the question.

425 426 427 428 429 430 431 Results. As shown in Table [5,](#page-7-2) MemDaily significantly ensures the accuracy of the answers provided for constructed questions. In the few instances where accuracy is compromised, it is attributed to the rewriting process by LLMs, which occasionally leads to information deviation. The results also demonstrate that MemSim can effectively mitigate the impact of LLM hallucinations on factual information, addressing a critical challenge in generating reliable questions and answers for memory evaluation. Another baseline method that directly generates answers through LLMs based on targeted user messages and questions performs much lower reliability. We implement this method and present the results as *OracleMem* in our constructed benchmarks in Section [5.2.](#page-8-0)

432 433 5 BENCHMARK

434 435 436 In this section, we create a benchmark based on the MemDaily dataset, in order to evaluate the memory capability of LLM-based personal assistants. Our benchmark sets various levels of difficulty by introducing different proportions of question-irrelevant daily-life posts.

437 438 5.1 EXPERIMENTAL SETTINGS

439 440 441 442 443 444 445 446 Levels of Difficulty. We utilize the MemDaily dataset as the basis of our benchmark. In order to set different levels of difficulty, we collect question-irrelevant posts from social media platforms, and randomly incorporate them into user messages by controlling their proportions. Specifically, we denote MemDaily-vanilla as the vanilla and easiest one without extra additions, and create a series of MemDaily- η , where we use η to represent the inverse percentage of original user messages. Larger η indicates a higher level of difficulty in the benchmark. We primarily focus on MemDaily-vanilla and MemDaily-100 as representatives. We also conduct evaluations on MemDaily-10, MemDaily-50, and MemDaily-200, putting their experimental results in Appendix [D.](#page-15-0)

447 448 449 450 451 452 453 454 455 456 457 458 459 Baselines. We implement several common memory mechanisms for LLM-based agents according to previous studies [\(Zhang et al., 2024\)](#page-12-0), including (1) Full Memory (FullMem): saves all previous messages and concatenates them into the prompt for LLM inference. (2) **Recent Memory (ReceMem)**: maintains the most recent k messages and concatenates them into the prompt for LLM inference, also known as short-term memory. (3) Retrieved Memory (RetrMem): stores all previous messages using FAISS [\(Johnson et al., 2019\)](#page-10-15) and retrieves the top- k relevant messages for inclusion in the prompt for LLM inference, which is commonly used to construct long-term memory. Specifically, we use Llama-160m [\(Miao et al., 2023\)](#page-11-14) to transform a message into a 768-dimensional embedding and compute relevance scores using cosine similarity [\(Singhal et al., 2001\)](#page-11-15). (4) **None Memory (Non-**Mem): does not use memory for LLM inference. Additionally, we include two special baselines for reference: (5) Noisy Memory (NoisyMem): receives only untargeted messages. (6) Oracle Memory (OracleMem): receives only targeted messages. Here, the targeted messages indicate the messages in the ground truth retrieval target. For all methods, we use the open-source GLM-4-9B [\(Team et al.,](#page-11-16) [2024\)](#page-11-16) as the foundational model for its excellent ability in long-context scenarios.

460 461 462 463 464 465 466 467 468 Metrics. We propose to evaluate the memory of LLM-based agents from two perspectives: effectiveness and efficiency. Effectiveness refers to the agent's ability to store and utilize factual information. The metrics for effectiveness include: (1) **Accuracy**: The correctness of agents' responses, measured by their ability to answer personal questions based on the factual information from historical user messages. (2) **Recall** \circ **5**: The percentage of messages in retrieval target successfully retrieved within the top-5 relevant messages. Efficiency mainly assesses the time cost associated with storing and utilizing information from memory. We use two metrics to evaluate efficiency: (1) **Response Time**: The time taken for an agent to respond after receiving a query, covering the retrieval and utilization processes. (2) Adaptation Time: The time required for an agent to store a new message.

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5.2 EFFECTIVENESS OF MEMORY MECHANISMS

471 472 473 474 475 476 477 478 479 480 481 482 Accuracy of factual question-answering. The results of accuracy are presented in Table [6.](#page-9-1) FullMem and RetrMem demonstrate superior performance compared to other memory mechanisms, achieving high accuracy across both datasets. ReceMem tends to underperform when a large volume of noisy messages is present, as target messages may fall outside the memory window. We observe that agents excel with simple, conditional, post-processing, and noisy questions but struggle with comparative and aggregative questions. By comparing with OracleMem, we find the primary difficulty possibly lies in retrieving target messages. Even with accurate retrieval, aggregative questions remain challenging, indicating a potential bottleneck in textual memory. An interesting phenomenon we notice is that NoisyMem shows higher accuracy than NonMem in MemDaily-vanilla but lower accuracy in MemDaily-100. Similarly, FullMem unexpectedly outperforms OracleMem on simple questions in MemDaily. We suspect that LLMs may perform better with memory prompts of medium length, suggesting a potential limitation of textual memory mechanisms for LLM-based agents.

483 484 485 Recall of target message retrieval. We implement three retrieval methods to obtain the most relevant messages and compare them with target messages to calculate Recall @5. **Embedding** refers to the retrieval process used in RetrMem. **Recency** considers the most recent k messages as the result. LLM directly uses the LLM to respond with the top-k relevant messages. The results are presented

Table 6: Results of accuracy for factual question-answering.

Table 7: Results of recall@5 for target message retrieval.

in Table [7.](#page-9-2) We find that LLM performs best in short-context scenarios, while Embedding achieves higher recall scores in longer contexts. Additionally, we notice that separating the retrieval and inference stages may exhibit different performances compared with integrating them.

5.3 EFFICIENCY OF MEMORY MECHANISMS

We put the results in Appendix [B](#page-14-1) due to the page limitation. We find that RetrMem consumes the most response time in short-context scenarios, and FullMem also requires more time for inference due to longer memory prompts. However, the response time of FullMem increases significantly faster than that of other methods as the context lengthens. Regarding adaptation time, we observe that RetrMem requires substantially more time because it needs to build indexes in the FAISS system.

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6 LIMITATIONS AND CONCLUSIONS

531 532 533 534 535 536 537 538 539 In this paper, we propose MemSim, a Bayesian simulator designed to generate reliable datasets for evaluating the memory capability of LLM-based agents. MemSim comprises two primary components: The bayesian Relation Network and the causal generation mechanism. Utilizing MemSim, we generate MemDaily as a dataset in the daily-life scenario, and conduct extensive evaluations to assess its quality. Additionally, we provide a benchmark on different memory mechanisms of LLM-based agents and provide further analysis. However, as the very initial study, there are several limitations. Firstly, our work focuses on evaluating the memory capability of LLM-based agents on factual information, but does not address higher-level and abstract information, such as users' hidden preferences. Additionally, our evaluation does not include dialogue forms, which are more complex and challenging to ensure reliability. In future works, we aim to address these two issues.

540 541 REFERENCES

542 543 544 545 546 547 548 549 550 551 552 553 554 555 556 557 558 559 560 561 562 563 564 565 566 567 568 569 570 571 572 573 574 575 576 577 578 579 580 581 582 583 584 585 586 587 588 589 590 591 592 593 Shulin Cao, Jiaxin Shi, Liangming Pan, Lunyiu Nie, Yutong Xiang, Lei Hou, Juanzi Li, Bin He, and Hanwang Zhang. Kqa pro: A dataset with explicit compositional programs for complex question answering over knowledge base. arXiv preprint arXiv:2007.03875, 2020. KuanChao Chu, Yi-Pei Chen, and Hideki Nakayama. A better llm evaluator for text generation: The impact of prompt output sequencing and optimization. arXiv preprint arXiv:2406.09972, 2024. Yingqiang Ge, Yujie Ren, Wenyue Hua, Shuyuan Xu, Juntao Tan, and Yongfeng Zhang. Llm as os (llmao), agents as apps: Envisioning aios, agents and the aios-agent ecosystem. arXiv preprint arXiv:2312.03815, 2023. Taicheng Guo, Xiuying Chen, Yaqi Wang, Ruidi Chang, Shichao Pei, Nitesh V Chawla, Olaf Wiest, and Xiangliang Zhang. Large language model based multi-agents: A survey of progress and challenges. arXiv preprint arXiv:2402.01680, 2024. Christina Heinze-Deml, Marloes H Maathuis, and Nicolai Meinshausen. Causal structure learning. Annual Review of Statistics and Its Application, 5(1):371–391, 2018. Chenxu Hu, Jie Fu, Chenzhuang Du, Simian Luo, Junbo Zhao, and Hang Zhao. Chatdb: Augmenting llms with databases as their symbolic memory. arXiv preprint arXiv:2306.03901, 2023. Lei Huang, Weijiang Yu, Weitao Ma, Weihong Zhong, Zhangyin Feng, Haotian Wang, Qianglong Chen, Weihua Peng, Xiaocheng Feng, Bing Qin, et al. A survey on hallucination in large language models: Principles, taxonomy, challenges, and open questions. arXiv preprint arXiv:2311.05232, 2023. Wenyu Huang, Guancheng Zhou, Mirella Lapata, Pavlos Vougiouklis, Sebastien Montella, and Jeff Z Pan. Prompting large language models with knowledge graphs for question answering involving long-tail facts. arXiv preprint arXiv:2405.06524, 2024. Bowen Jin, Chulin Xie, Jiawei Zhang, Kashob Kumar Roy, Yu Zhang, Suhang Wang, Yu Meng, and Jiawei Han. Graph chain-of-thought: Augmenting large language models by reasoning on graphs. arXiv preprint arXiv:2404.07103, 2024. Jeff Johnson, Matthijs Douze, and Hervé Jégou. Billion-scale similarity search with gpus. IEEE Transactions on Big Data, 7(3):535–547, 2019. Arthur B Kahn. Topological sorting of large networks. Communications of the ACM, 5(11):558–562, 1962. Tom Kwiatkowski, Jennimaria Palomaki, Olivia Redfield, Michael Collins, Ankur Parikh, Chris Alberti, Danielle Epstein, Illia Polosukhin, Jacob Devlin, Kenton Lee, et al. Natural questions: a benchmark for question answering research. Transactions of the Association for Computational Linguistics, 7:453–466, 2019. Yunshi Lan, Gaole He, Jinhao Jiang, Jing Jiang, Wayne Xin Zhao, and Ji-Rong Wen. A survey on complex knowledge base question answering: Methods, challenges and solutions. arXiv preprint arXiv:2105.11644, 2021. Gibbeum Lee, Volker Hartmann, Jongho Park, Dimitris Papailiopoulos, and Kangwook Lee. Prompted llms as chatbot modules for long open-domain conversation. arXiv preprint arXiv:2305.04533, 2023. Yuanchun Li, Hao Wen, Weijun Wang, Xiangyu Li, Yizhen Yuan, Guohong Liu, Jiacheng Liu, Wenxing Xu, Xiang Wang, Yi Sun, et al. Personal llm agents: Insights and survey about the capability, efficiency and security. arXiv preprint arXiv:2401.05459, 2024. Lei Liu, Xiaoyan Yang, Yue Shen, Binbin Hu, Zhiqiang Zhang, Jinjie Gu, and Guannan Zhang. Think-in-memory: Recalling and post-thinking enable llms with long-term memory. arXiv preprint arXiv:2311.08719, 2023.

647 Zeyuan Chen, Jianguo Zhang, Devansh Arpit, et al. Retroformer: Retrospective large language agents with policy gradient optimization. arXiv preprint arXiv:2308.02151, 2023.

A PROOF IN BAYESIAN RELATION NETWORK

A.1 PROOF OF THEOREM [1](#page-3-0)

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Theorem 1 (Factorization). *The joint probability distribution of BRNet can be expressed as*

$$
P(X_1, X_2, ..., X_{|X|}) = \prod_{X_t \in \mathcal{X}} P(X_t | par(X_t)),
$$

710 *where* $par(X_t)$ *denotes the set of parent attributes of* X_t *.*

712 Proof. *Because BRNet is DAG, we can certainly find a topological ordering*

 $O = [o_1, o_2, ..., o_{|\mathcal{X}|}]$.

Then, we inverse the sequence to get a reversed topologically ordering

$$
\tilde{O} = \begin{bmatrix} \tilde{o}_1, \tilde{o}_2, ..., \tilde{o}_{|\mathcal{X}|} \end{bmatrix}
$$

.

Then, we utilize the theorem of conditional probability according to the order \tilde{O} *, and we have*

$$
P(X_1, X_2, ..., X_{|\mathcal{X}|}) = P(X_{\tilde{o}_1}|X_{\tilde{o}_2}, ..., X_{\tilde{o}_{|\mathcal{X}|}}) \cdot P(X_{\tilde{o}_2}|X_{\tilde{o}_3}, ..., X_{\tilde{o}_{|\mathcal{X}|}}) \dots P(X_{\tilde{o}_{|\mathcal{X}|}}).
$$

=
$$
\prod_{i=1}^{|\mathcal{X}|} P(X_{\tilde{o}_i} | \mathbf{X} [\tilde{o}_{i+1} : \tilde{o}_{|\mathcal{X}|}]),
$$

where $\mathbf{X}\left[\tilde{o}_{i+1}:\tilde{o}_{|{\cal X}|}\right]$ means all the variables after \tilde{o}_{i+1} in the reversed topologically ordering, and *there are no descendant variables inside. According to Assumption [1,](#page-3-2) we have*

$$
P(X_{\tilde{o}_i}|\mathbf{X}\left[\tilde{o}_{i+1}:\tilde{o}_{|\mathcal{X}|}\right]) = P(X_{\tilde{o}_i}|par(X_{\tilde{o}_i})).
$$

Finally, we rewrite it and obtain

$$
P(X_1, X_2, ..., X_{|\mathcal{X}|}) = \prod_{X_t \in \mathcal{X}} P(X_t | par(X_t)).
$$

A.2 PROOF OF THEOREM [2](#page-3-3)

Theorem 2 (Ancestral Sampling). *For BRNet, the result of ancestral sampling is equivalent to that of sampling from the joint probability distribution. Specifically, we have*

 $P(\tilde{x}_1, \tilde{x}_2, ..., \tilde{x}_{|\mathcal{X}|}) = P(x_1, x_2, ..., x_{|\mathcal{X}|}),$

where $x_1, x_2, ..., x_{|\mathcal{X}|} \sim P(X_1, X_2, ..., X_{|\mathcal{X}|})$ *are sampled from the joint probability distribution.* Proof. *We first calculate the reversed topologically ordering*

$$
\tilde{O} = [\tilde{o}_1, \tilde{o}_2, ..., \tilde{o}_{|\mathcal{X}|}].
$$

Then, we have

$$
P(\tilde{x}_1, \tilde{x}_2, ..., \tilde{x}_{|\mathcal{X}|}) = \prod_{i=1}^{|\mathcal{X}|} P(\tilde{x}_{\tilde{o}_i} | \tilde{\mathbf{x}} \left[\tilde{o}_{i+1} : \tilde{o}_{|\mathcal{X}|} \right])
$$

$$
= \prod_{i=1}^{|\mathcal{X}|} P(\tilde{x}_{\tilde{o}_i} | par(\tilde{x}_{\tilde{o}_i})).
$$

where $\tilde{\bf x}\left[\tilde{o}_{i+1}:\tilde{o}_{|{\cal X}|}\right]$ means the values of all the variables after \tilde{o}_{i+1} in the reversed topologically *ordering. According to Assumption [2,](#page-3-1) we have*

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$$
P(\tilde{x}_1, \tilde{x}_2, ..., \tilde{x}_{|\mathcal{X}|}) = \prod_{i=1}^{|\mathcal{X}|} P(x_{\tilde{o}_i}|par(x_{\tilde{o}_i}))
$$

$$
= P(x_1, x_2, ..., x_{|\mathcal{X}|}).
$$

B BENCHMARK ON THE EFFICIENCY OF MEMORY MECHANISMS

The results of efficiency are presented in Table [8](#page-14-2) and Table [9.](#page-14-3)

Table 8: Results of response time for generating answers (seconds per query).

Table 9: Results of adaptation time for storing messages (seconds per message).

C EXTENSIVE EVALUATION ON USER MESSAGES BY GPT-4O

We also let GPT-4o score on user messages as a reference, and the results are shown in Table [10.](#page-14-4)

Table 10: Results of evaluation on user messages by GPT-4o.

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D EXTENSIVE BENCHMARK ON MORE COMPOSITE DATASETS

D.1 RESULTS ON MEMDAILY-10

The results of accuracy are shown in Table [11.](#page-15-1) The results of recall@5 are shown in Table [12.](#page-15-2) The results of response time are shown in Table [13.](#page-15-3) The results of adaptation time are shown in Table [14.](#page-15-4)

Table 11: Results of accuracy on MemDaily-10.

Table 12: Results of recall@5 on MemDaily-10.

Methods	Simp.	Cond.	Comp.	Aggr.	Post.	Noisy
I.M				0.794 ± 0.035 0.872 ± 0.019 0.518 ± 0.027 0.732 ± 0.036 0.756 ± 0.038 0.846 ± 0.036		
Embedding				0.704 ± 0.039 0.833 ± 0.026 0.506 ± 0.052 0.643 ± 0.043	0.609 ± 0.027	0.648+0.018
Recency	0.032 ± 0.017		0.011 ± 0.010 0.013 ± 0.011 0.030 ± 0.012		$0.009 + 0.007$	0.504+0.047

Table 13: Results of response time on MemDaily-10 (seconds per query).

Methods	Simp.	Cond.	Comp.	Aggr.	Post.	Noisy
FullMem	0.243 ± 0.008	0.243 ± 0.008	$0.208 + 0.003$	0.306 ± 0.008	0.263 ± 0.006	0.262 ± 0.010
RetrMem	$0.213 + 0.002$	0.230 ± 0.005	0.246 ± 0.008	0.212 ± 0.002	0.240 ± 0.004	0.292 ± 0.014
ReceMem	$0.120 + 0.000$	$0.121 + 0.000$	$0.120 + 0.000$	$0.119 + 0.002$	$0.126 + 0.001$	0.124 ± 0.001
NonMem	$0.119 + 0.000$	$0.119 + 0.001$	$0.119 + 0.000$	$0.117 + 0.002$	0.122 ± 0.000	0.119 ± 0.002
NoisyMem	0.205 ± 0.005	0.207 ± 0.007	0.181 ± 0.004	0.253 ± 0.010	0.223 ± 0.005	0.222 ± 0.006
OracleMem	$0.121 + 0.001$	0.123 ± 0.001	0.122 ± 0.000	$0.131 + 0.001$	0.130 ± 0.001	0.128 ± 0.001

Table 14: Results of adaptation time on MemDaily-10 (seconds per message).

D.2 RESULTS OF MEMDAILY-50

The results of accuracy are shown in Table [15.](#page-16-0) The results of recall@5 are shown in Table [16.](#page-16-1) The results of response time are shown in Table [17.](#page-16-2) The results of adaptation time are shown in Table [18.](#page-16-3)

Methods	Simp.	Cond.	Comp.	Aggr.	Post.	Noisy
FullMem	$0.962 + 0.027$	$0.948 + 0.020$	$0.602 + 0.065$	$0.296 + 0.072$	$0.802 + 0.046$	0.880 ± 0.041
RetrMem	$0.886 + 0.035$	$0.864 + 0.037$	$0.724 + 0.062$	0.320 ± 0.071	0.780 ± 0.059	0.748 ± 0.049
ReceMem	$0.508 + 0.042$	$0.434 + 0.052$	$0.108 + 0.044$	$0.237 + 0.054$	0.588 ± 0.066	0.376 ± 0.099
NonMem	$0.510+0.061$	$0.452 + 0.055$	$0.159 + 0.039$	$0.254 + 0.066$	$0.594 + 0.078$	0.380 ± 0.055
NoisyMem	0.454 ± 0.040	0.416 ± 0.083	$0.229 + 0.071$	$0.272 + 0.073$	0.568 ± 0.078	0.360 ± 0.084
OracleMem	$0.966 + 0.025$	$0.988 + 0.010$	$0.910 + 0.053$	$0.376 + 0.042$	$0.888 + 0.032$	0.984 ± 0.012

Table 15: Results of accuracy on MemDaily-50.

Table 16: Results of recall@5 on MemDaily-50.

Table 17: Results of response time on MemDaily-50 (seconds per query).

Methods	Simp.	Cond.	Comp.	Aggr.	Post.	Noisy
FullMem	$0.776 + 0.031$	$0.783 + 0.067$	0.596 ± 0.021	$1.134 + 0.054$	0.841 ± 0.032	0.847 ± 0.062
RetrMem	$0.203 + 0.003$	0.206 ± 0.004	0.215 ± 0.004	0.204 ± 0.003	0.229 ± 0.005	0.324 ± 0.020
ReceMem	$0.120 + 0.001$	$0.121 + 0.002$	$0.118 + 0.000$	$0.118 + 0.001$	$0.123 + 0.002$	0.123 ± 0.001
NonMem	$0.118 + 0.001$	$0.118 + 0.002$	0.117 ± 0.002	$0.118 + 0.001$	0.121 ± 0.001	$0.119 + 0.001$
NoisyMem	0.728 ± 0.037	0.737 ± 0.041	0.562 ± 0.027	1.060 ± 0.055	$0.787 + 0.028$	0.794 ± 0.058
OracleMem	$0.121 + 0.001$	$0.122 + 0.001$	$0.121 + 0.001$	$0.131 + 0.001$	$0.129 + 0.001$	0.128 ± 0.001

Table 18: Results of adaptation time on MemDaily-50 (seconds per message).

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D.3 RESULTS OF MEMDAILY-200

 The results of accuracy are shown in Table [19.](#page-17-0) The results of recall@5 are shown in Table [20.](#page-17-1) The results of response time are shown in Table [21.](#page-17-2) The results of adaptation time are shown in Table [22.](#page-17-3)

Table 20: Results of recall@5 on MemDaily-200.

Methods	Simp.	Cond.	Comp.	Aggr.	Post.	Noisy
LLM.			0.457 ± 0.066 0.356 ± 0.051 0.556 ± 0.035 0.176 ± 0.022		$0.342+0.048$ $0.322+0.043$	
Embedding			0.674 ± 0.052 0.641 ± 0.044 0.753 ± 0.036 0.484 ± 0.050		$0.544 + 0.054$ $0.508 + 0.052$	
Recency	0.001 ± 0.003		0.001 ± 0.002 0.001 ± 0.002 0.000 ± 0.001		0.001+0.003	$0.000 + 0.000$

Table 21: Results of response time on MemDaily-200 (seconds per query).

Methods	Simp.	Cond.	Comp.	Aggr.	Post.	Noisy
FullMem	$4.028 + 0.161$	$3.914 + 0.213$	2.697 ± 0.100	6.365 ± 0.374	4.252 ± 0.328	4.307 ± 0.283
RetrMem	0.236 ± 0.023	0.241 ± 0.018	0.238 ± 0.024	0.585 ± 0.230	1.012 ± 0.690	1.252 ± 0.427
ReceMem	0.130 ± 0.002	$0.120 + 0.002$	$0.118 + 0.001$	$0.119 + 0.001$	$0.124 + 0.001$	0.123 ± 0.001
NonMem	$0.139 + 0.006$	$0.119 + 0.001$	0.119 ± 0.001	$0.117 + 0.001$	0.121 ± 0.001	0.121 ± 0.001
NoisyMem	3.947 ± 0.209	3.832 ± 0.203	2.637 ± 0.118	6.221 ± 0.325	4.158 ± 0.226	$4.214 + 0.288$
OracleMem	$0.141 + 0.003$	0.122 ± 0.001	$0.121 + 0.001$	$0.131 + 0.002$	$0.128 + 0.002$	$0.128 + 0.001$

Table 22: Results of adaptation time on MemDaily-200 (seconds per message).

972 973 E CASE STUDIES

974 975 976 977 In this section, we present several case studies to illustrate the effectiveness of the data generated by MemDaily. First, we will display the hierarchical user profiles generated from BRNet. Next, we will present examples of user messages created by our method. Finally, we will provide examples of questions and answers for each type.

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988 989 990 E.1 CASE STUDY ON GENERATED USER PROFILES

980 981 In MemDaily, we incorporate 11 entities that cover 7 types, with 73 attributes of them. The summary of entities and attributes of MemDaily are provided in Table [23.](#page-20-0)

982 983 984 985 986 987 We introduce prior knowledge as several rules according to our scenarios to constrain among attributes. For example, a relative role is highly possible to share the same hometown with the user, because they are likely to come from the same place. All of these constraints are expressed in BRNet with causal relations. We generate 50 graphical user profiles and conduct observations, finding that most profiles align well with real-world users without contradictions.

Here is a case of user profiles, and we translate them into English for better demonstration:

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E.2 CASE STUDY ON USER MESSAGES

 Based on the generated user profiles, we further generate user messages without inside contradictory according to Section [3.3.](#page-4-1) Here is a case of message list (translated into English) in Table [24.](#page-21-0)

 By utilizing our mechanisms, we can ensure that there is no contradiction among user messages. We further demonstrate the list of hints that correspond to the above messages in Table [25.](#page-22-0)

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1242 1243 E.3 CASE STUDY ON QUESTIONS AND ANSWERS

1244 1245 1246 In this section, we will show the cases of questions and answers of different types. We leave out the time and place of each message in this section, where they do not influence the QA in these cases. We have translated all texts into English for better demonstration.

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Simple *(Simp.)* Simple QAs in single-hop.

Conditional *(Cond.)* Conditional QAs in multi-hop.

Aggregative *(Aggr.)* Aggregative QAs in multi-hop.

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- **1345 1346**
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Noisy *(Nois.)* Multi-hop QAs that add extra noise in questions.

