

000 001 002 003 004 005 006 007 008 009 010 011 012 013 014 015 016 017 018 019 020 021 022 023 024 025 026 027 028 029 030 031 032 033 034 035 036 037 038 039 040 041 042 043 044 045 046 047 048 049 050 051 052 053 PRIVACY *Déjà Vu* EFFECT: RESURFACING SENSITIVE SAMPLES IN CONTINUAL FINE-TUNING

005 **Anonymous authors**

006 Paper under double-blind review

ABSTRACT

011 Continual fine-tuning of large pre-trained models is now ubiquitous in industry
012 for adapting a model to freshly collected user data. Existing privacy protection
013 practices assume earlier training data is less sensitive and thus focus on the latest ar-
014 riving samples. We challenge this assumption by tracking per-sample membership-
015 inference risk across sequential fine-tuning rounds of popular transformer-based
016 models, ViT for image data, and BERT for text data. Our experiments reveal the
017 *Privacy Déjà Vu Effect*: new data can *remind* the model of semantically similar
018 legacy samples, possibly elevating their privacy risk significantly. We further
019 demonstrate that this resurgence is closely correlated with the latent-feature-space
020 similarity between old and new examples. These findings underscore the need
021 for a more comprehensive privacy protection mechanism in continual fine-tuning.
022 We have published our code at [https://anonymous.4open.science/r/](https://anonymous.4open.science/r/Privacy-Déja-vu-Effect-F006/README.md)
023 *Privacy-Déja-vu-Effect-F006/README.md*.

1 INTRODUCTION

027 As machine learning models continue to grow in size, training them from scratch becomes pro-
028 hibitively expensive. Many companies, such as Reddit (Reddit, Inc.) and IBM (Stapleton), instead opt
029 to fine-tune pre-trained base models using newly arriving data samples incrementally. Such continual
030 fine-tuning (Wang et al., 2024) is a common strategy employed in sectors such as customer support,
031 recommendation systems, and autonomous vehicles, where new user data is constantly integrated to
032 enhance the model performance and freshness.

033 However, privacy concerns arise in this practice. A widely held assumption is that the most recent
034 training data predominantly influence the model’s behavior, and the old data likely suffers from
035 catastrophic forgetting, resulting in a largely reduced ability to capture the utility of old samples
036 (Wang et al., 2024). Thus, the common belief is to prioritize privacy safeguards for new samples while
037 progressively neglecting older ones to reduce the protection expenses (Chathoth et al., 2022a; Desai
038 et al., 2021; Chathoth et al., 2022b). Correspondingly, industry parties start to adopt this strategy.
039 IBM Watsonx, for instance, implements robust privacy measures on the latest fine-tuning samples
040 (IBM Cloud, 2023). Regulatory documents, e.g., EDPB Opinion 28/2024 (European Data Protection
041 Board, 2024) also stress that newer data in continual fine-tuning should be protected primarily.

042 Yet, our research reveals a counterintuitive phenomenon which we call ‘‘Privacy Déjà Vu Effect’’:
043 While the standard continual fine-tuning is applied to make models more likely to forget the old
044 distribution (Bafghi et al., 2024), some old samples, initially exhibiting low privacy sensitivity,
045 become more vulnerable during model fine-tuning. It seems new samples remind the model of its old
046 memory.

047 **Scope of Our Research.** In this paper, we show that such Privacy Déjà Vu Effect exists in the
048 fine-tuning processes on two typical transformer-based models, ViT and BERT, covering image- and
049 text-based applications, respectively. To detect the change of samples’ privacy risks, we consider a
050 canonical family of privacy attacks called membership inference attacks (Shokri et al., 2017), which
051 predict whether or not a given example is contained in the model’s training set. Privacy risk measures
052 derived from membership inference attacks, such as the per-sample $\frac{\text{TPR}}{\text{FPR}}$ ratio, an empirical measure
053 conceptually similar to the privacy budget ϵ^c in (ϵ, δ) -differential privacy, have been widely accepted
054 as indicators of practical privacy risks (Aerni et al., 2024; Jagielski et al., 2020; Nasr et al., 2023;
055 Steinke et al., 2024). By using this privacy risk measurement in consecutive fine-tuning ViT models

054 on Tiny-ImageNet-200 and BERT models on IMDb, we observed that the largest increase in privacy
 055 risk for sensitive samples exhibits an astonishing jump.
 056

057 We perform several experiments to understand the root causes of the Privacy Déjà Vu Effect. This
 058 effect can be partially explained by the level of distribution shifting between neighboring fine-tuning
 059 rounds - if the new samples focus on a few classes (not randomly sparsely distributed), the privacy
 060 risk of the old samples in similar classes gets boosted more than other samples. An in-depth analysis
 061 of the similarity between consecutive steps of fine-tuning confirms that old samples similar to the
 062 newcomers are more prone to a privacy risk surge. Thus, the name Privacy Déjà Vu precisely captures
 063 how the new samples revive the model’s memory about similar old ones.
 064

065 This Privacy Déjà Vu Effect challenges the currently adopted practice for economical privacy protection:
 066 *protecting mainly the newest samples in fine-tuning* is not sufficient. Our work shows that such
 067 biased protection may introduce significant privacy leakage to the related old samples.
 068

069 **Contributions.** (1), We reveal the Privacy Déjà Vu Effect: new data in continual fine-tuning
 070 can increase the privacy risk of previously safe samples. (2), Experiments on two representative
 071 foundation models and two benchmark datasets show that the effect might commonly exist. (3), We
 072 have also experimentally studied the reasons behind this effect and identified the significant factors.
 073

074 2 RELATED WORK

075 **Continual Fine-tuning and Catastrophic Forgetting.** Unlike conventional machine-learning
 076 pipelines that assume a static data distribution, continual learning adapts to non-stationary streams
 077 of data (Wang et al., 2024). Its central challenge is *catastrophic forgetting*: updating on new
 078 data degrades performance on previously learned tasks (McClelland et al., 1995; McCloskey &
 079 Cohen, 1989). Gido et al. show that the same problem arises during continual fine-tuning of neural
 080 networks (Van de Ven & Tolias, 2019). To curb forgetting, Hadsell et al. propose preserving weights
 081 that are critical for early-stage data (Hadsell et al., 2020). Industry systems adopt additional heuristics
 082 such as hard attention to historical samples (Serra et al., 2018). The REMIND approach rehearses
 083 compressed representations of past data (Hayes et al., 2020). Focusing on transformer models,
 084 Bafghi et al. report that full-parameter continual fine-tuning suffers the most severe forgetting (Bafghi
 085 et al., 2024).

086 **Privacy Risks in Continual Fine-tuning.** Because catastrophic forgetting appears to reduce the
 087 model’s memory of earlier data, some studies argue that it can reduce the privacy risk of old data, and
 088 therefore we should concentrate protection on newly ingested samples (Wang et al., 2025; Chathoth
 089 et al., 2022a; Desai et al., 2021; Chathoth et al., 2022b). For instance, Hassanpour et al. assign
 090 smaller differential-privacy budgets to successive training rounds (Hassanpour et al., 2022). However,
 091 other work demonstrates that legacy data can remain susceptible to extraction attacks even after
 092 multiple fine-tuning rounds on both vision and language models (Jagielski et al., 2023; Chen et al.,
 093 2024; Borkar et al., 2025). These findings challenge the assumption that older data can be neglected
 094 in privacy analyses for continual fine-tuning systems.
 095

096 3 PRELIMINARIES

097 In this section, we introduce a typical continual fine-tuning method on foundation models. We also
 098 describe the process of measuring privacy risks using a membership inference attack, specifically the
 099 Offline Likelihood Ratio Attack (LiRA).
 100

101 **Continual Fine-tuning on Foundation Models.** Let \mathcal{D}_k denote a data distribution and $S_k =$
 102 $\{(x_{i,k}, y_{i,k}) | (x_{i,k}, y_{i,k}) \in \mathcal{D}_k, i = 1 \dots N_k\}$ denote a training dataset of k -th round fine-tuning,
 103 and $f_k \leftarrow \mathcal{T}(S_k)$ denote the model we obtain by fine-tuning the previous model f_{k-1} . Continual
 104 fine-tuning can be categorized into various types according to the difference among \mathcal{D}_k (Wang et al.,
 105 2024). In this paper, we consider domain-incremental fine-tuning, where each \mathcal{D}_k has the same label
 106 space but possibly different distributions, as considered by previous works (Jagielski et al., 2023;
 107 Carlini et al., 2022b). This setting also facilitates the in-depth study of causes of the Privacy Déjà Vu
 108 Effect, which will be introduced in Section 4.

108 As shown in Figure 7 in Appendix 1, the k -th round model f_k is given by fine-tuning f_0 sequentially
 109 with $\{S_1, \dots, S_k\}$, where S_0 is the dataset to train a foundation model f_0 , e.g., a ViT model pre-trained
 110 on the ImageNet (Dosovitskiy et al., 2021). Furthermore, we adopted the setting that fine-tunes all
 111 parameters (Bafghi et al., 2024). This strategy is most likely to catastrophically forget old distribution
 112 and thus considered to benefit the privacy protection of old data (Wang et al., 2025).

113 **Per-sample Privacy Risk Metric.** There are several metrics to estimate the per-sample privacy risk,
 114 e.g., per-sample attack success rate of Membership Inference Attacks (MIAs) (Carlini et al., 2022c)
 115 and the Fisher information of samples (Farokhi & Sandberg, 2017). We adopt the per-sample $\frac{\text{TPR}}{\text{FPR}}$ of
 116 an MIA as the privacy risk metric because it intrinsically relates to differential privacy (Aerni et al.,
 117 2024; Tramer et al., 2022) as follows.

118 Recall the definition of (ϵ, δ) -differential privacy (DP) (Dwork, 2006) for a randomized mechanism
 119 \mathcal{M} acting on adjacent datasets D, D' . Assuming $\forall \mathcal{O} \subseteq \text{Range}(\mathcal{M})$:

$$\Pr[\mathcal{M}(D) \in \mathcal{O}] \leq e^\epsilon \Pr[\mathcal{M}(D') \in \mathcal{O}] + \delta.$$

120 When $\delta \approx 0$ (δ is always very small in practice), the DP guarantee in the *hypothesis-testing* form
 121 ensures no sample's MIA result $\frac{\text{TPR}}{\text{FPR}}$ exceeds the privacy budget (Kairouz et al., 2015; Dong et al.,
 122 2022):

$$\frac{\text{TPR}}{\text{FPR}} \leq e^\epsilon$$

123 where TPR and FPR denote, respectively, the true and false positive rates of any distinguishing attack
 124 that decides whether the output $\mathcal{M}(\cdot)$ came from D or D' . Due to the statistical nature of machine
 125 learning, even without a DP randomization mechanism, an MIA on a non-DP model still gives a
 126 measure $\frac{\text{TPR}}{\text{FPR}}$ for each sample, which we consider the sample's "inherent privacy risk". While an
 127 ideal attack can precisely estimate this risk measure, in practice, we can only use the best MIA so far
 128 to get the maximum $\frac{\text{TPR}}{\text{FPR}}$ estimate. We choose to use one of the most powerful MIAs, LiRA (Carlini
 129 et al., 2022a), in the experiments. Samples with larger $\frac{\text{TPR}}{\text{FPR}}$ values are considered more risky.

130 **The Likelihood Ratio Attack (LiRA).** LiRA is considered one of the most powerful MIAs. Thus, we
 131 use LiRA as the backbone attack of our privacy risk estimator. There are online and offline versions
 132 of LiRA, which are based on two-sided and one-sided hypothesis testing, respectively. Offline LiRA
 133 is more efficient because it only needs to estimate the "out" distribution by sacrificing some marginal
 134 effectiveness. For simplicity, we use the term "LiRA" to represent the offline version of LiRA in this
 135 paper. The details of LiRA are as follows.

136 1. Estimate distribution of "out" logits. Given a machine learning model g and the training strategy
 137 $\mathcal{G}(\cdot)$, LiRA first train multiple "shadow models" $\{g_j \leftarrow \mathcal{G}(X_j)\}$ on random subsets $\{X_j | X_j \subset$
 138 $\mathcal{D}, j = 1..m\}$ drawn from the known training data distribution \mathcal{D} . For any non-member sample
 139 (x, y) , e.g., for g_j , LiRA computes the logits of the confidence of the target class y , $p = g_j(x)_y$:
 140 $\log \frac{p}{1-p}$. This computation will be applied to a sufficient number of randomly selected non-members
 141 for $\{g_j\}$, respectively. The distribution of the logits values is approximately a univariate Gaussian
 142 distribution, the parameters of which can be estimated with these samples. We train 256 shadow
 143 models to estimate the distribution parameters, as suggested by (Carlini et al., 2022a).

144 2. Attack target sample (x_i, y_i) . To predict whether a target sample (x_i, y_i) is a member of X_j , LiRA
 145 computes the logit transformation of the prediction of g_j , and computes the likelihood of the sample
 146 drawn from the "out" Gaussian distribution, denoted as q . In practice, there is a threshold τ for the
 147 adversary to classify the sample as an "in" or "out" sample. If $q < \tau$, then the prediction is "member",
 148 and "non-member" otherwise. Choice of τ will be introduced in the next subsection.

149 **Estimation of Per-sample $\frac{\text{TPR}}{\text{FPR}}$.** To estimate privacy risk $\frac{\text{TPR}_i}{\text{FPR}_i}$ of each sample $(x_i, y_i) \in X$, we
 150 conduct a random sampling of the training data X to generate m sample sets, where each sample
 151 set X_j is generated by selecting each sample x_i in X with probability of 0.5. Each of the sample
 152 set is used to train a model g_j . Thus, x_i is used by about $m/2$ models in training, which forms
 153 the ground-truth of the x_i 's membership in the m models. We then use LiRA to compute $q_{i,j}$, the
 154 probability of sample x_i is drawn from "out" Gaussian distribution. In our estimation, each threshold
 155 τ will give a pair of TPR and FPR by comparing the attacking results and the ground truths, and we
 156 choose the τ_i that gives the greatest $\frac{\text{TPR}_i}{\text{FPR}_i}$ for sample x_i .

162 4 METHODS
163
164165 Privacy Déjà Vu Effect means a new fine-tuning round will expose the privacy of some training
166 samples in the previous fine-tuning rounds. For simplicity, we will look at the change in privacy risk
167 of a sample in S_k after the model is fine-tuned on S_{k+1} . Next, we will discuss the methods we use to
168 explore this effect.169
170 4.1 MODEL AND DATASETS
171
172

173 We start with our choice of datasets and models.

174 **Datasets.** We adopt two standard benchmarks: Tiny-ImageNet-200 (Le & Yang, 2015) and the IMDb
175 Large Movie Review corpus (Maas et al., 2011). To meet the domain-incremental setting in Section 3,
176 on each stage, fine-tuning sets shares the same label set but differs in input distribution. We therefore
177 merge original fine-grained labels into superclasses. Formally, let \mathcal{C} be the original class set and
178 $\mathcal{C}' = \{s_1, \dots, s_J\}$ a partition of \mathcal{C} . Tiny-ImageNet provides $|\mathcal{C}| = 200$ classes grouped into $|\mathcal{C}'| = 22$
179 semantic clusters (e.g., "Vehicle" superclass spans original classes "limo", "sportscar", "wagon", etc.
180 (Deng et al., 2009)). IMDb's ten rating buckets collapse into Neg={1–4} and Pos={7–10} (Maas
181 et al., 2011). For Tiny-ImageNet-200, we sample two fine-grained classes per superclass to form
182 $S_k \subset \mathcal{D}$; for IMDb, we sample one rating per superclass.183 **Models.** Experiments cover two foundation architectures: ViT-B/16 pretrained on ImageNet-21k
184 (Dosovitskiy et al., 2021) and BERT-base (uncased) (Devlin et al., 2019). We use the strategy
185 introduced in (Jagielski et al., 2023) to mimic domain-incremental fine-tuning: each model undergoes
186 two fine-tuning rounds: round 1 yields f_k , round 2 yields f_{k+1} , i.e., f_1 and f_2 . Both rounds use
187 the superclasses as labels, i.e., ViTs fit 22-classification tasks and BERTs fit binary-classification
188 tasks. The validation sets are drawn from the entire validation set according to the superclasses and
189 classes in the training sets. For instance, if superclass "Vehicle" in S_k contains "Limo", then the
190 corresponding validation set also contains "Limo". We adopt very small learning rates (3×10^{-6} for
191 ViT, 1×10^{-7} for BERT) and early stopping after three epochs without validation-loss improvement,
192 storing the best checkpoint—as in (Jagielski et al., 2023). This protocol attains 93.4% validation
193 accuracy on Tiny-ImageNet-200 and 94.2% on IMDb. In this paper, we fine-tune 500 f_k ($m = 500$)
194 to generate statistically significant estimation, which is suggested by (Gu et al., 2024). It takes 16.3
195 hours on 15 RTX-2080 Ti GPUs to finish all fine-tuning stages on ViT models, and 6.8 hours on
196 BERT models. All experiments in the paper takes around 900 hours.197
198 4.2 ESTIMATING PRIVACY RISK CHANGE
199200 To estimate the per-sample privacy risk change of samples in S_k , we need to compute the per-sample
201 privacy risk of samples in S_k on model f_k and f_{k+1} . As shown in Figure 7 in Appendix 1, this
202 estimation has three steps:203 1. Estimation over f_k : Following the LiRA-based per-sample $\frac{\text{TPR}}{\text{FPR}}$ estimation described in Section 3,
204 and also as shown in Figure 7 in Appendix 1, we fine-tune f_{k-1} to get m models $\{f_{j,k} \leftarrow \mathcal{T}(S_{j,k}) | j = 1, \dots, m\}$. Each sample in $S_{j,k}$ is randomly sampled with a probability of 0.5 from S_k . Thus, around
205 $\frac{m}{2}$ datasets contain sample $x_{i,k} \in S_k$. And for each sample-model pair, we have the ground
206 truth membership. We then use LiRA to attack the x_i on each of the models to get m predicted
207 memberships, with which we can compute the sample-level privacy risk $R_{i,k} = \frac{\text{TPR}_{i,k}}{\text{FPR}_{i,k}}$ of x_i on f_k .
208 2. Estimation over f_{k+1} : To estimate the privacy risk of each sample in S_k after the $(k+1)$ -th round
209 of fine-tuning, we simply fine-tune each $f_{j,k}$ on the fine-tuning set S_{k+1} and use the m fine-tuned
210 models $f_{j,k+1}$ to estimate the privacy risk $R_{i,k+1} = \frac{\text{TPR}_{i,k+1}}{\text{FPR}_{i,k+1}}$ of each sample $x_i \in S_k$ as step 1.
211 3. Estimating privacy risk change: For sample $x_i \in S_k$, we compute the privacy risk change as
212 $\Delta_i = R_{i,k+1} - R_{i,k}$. A greater positive Δ_i indicates the x_i 's privacy risk is enhanced more in f_{k+1} .
213 A negative Δ_i means the sample becomes safer.

216 4.3 STUDY THE PRIVACY DÉJÀ VU EFFECT
217

218 **Fine-tuning Strategies.** To assess the widespread nature of the Privacy Déjà Vu Effect, we implement
219 two contrasting data update strategies: *SGD-New* and *SGD-Full*, as introduced (Jagielski et al., 2023).
220 In *SGD-New*, the dataset S_{k+1} comprises only new samples, randomly drawn from $\mathcal{D} \setminus S_k$, with a size
221 set to half of $|S_k|$ to avoid the impact of dataset size difference between $S_{j,k}$ and S_{k+1} —specifically,
222 $|S_k| = 30,000$ for Tiny-ImageNet-200 and $|S_k| = 15,000$ for IMDb. In *SGD-Full*, S_{k+1} includes
223 both the new samples and all data from S_k , effectively duplicating the previous dataset.

224 Figure 1 illustrates that, for both BERT and ViT models, and under both strategies, certain samples
225 in S_k exhibit increased privacy risk after fine-tuning. Notably, the *SGD-New* strategy results in a
226 more pronounced Privacy Déjà Vu Effect compared to *SGD-Full*. We hypothesize that this difference
227 arises because duplicating old data in *SGD-Full* reduces the sensitivity of some samples, thereby
228 mitigating privacy risks. This observation aligns with findings by (Carlini et al., 2022c). We further
229 validate this hypothesis in Section 5.2.

230 These findings confirm that the Privacy Déjà Vu Effect is prevalent in practice and appears to be
231 influenced by the relationship between old and new data. Because the *SGD-New* setting avoid the
232 impact of overlap between S_k and S_{k+1} , to analyze the details of the effect, subsequent sections will
233 focus on the *SGD-New* setting.



244 Figure 1: Descendingly ordered Δ with different continual fine-tuning strategies. Note that each set
245 of results is sorted independently. Both models show that SGD-New causes more intense privacy risk
246 increases for old samples. We omit samples with $\Delta(\frac{\text{TPR}}{\text{FPR}}) \leq 0$, which cover roughly 68% of the
247 ViT cases and 62.5% of the BERT cases.

248 **Simulating Distribution Shifting.** The results in Figure 1 suggest that Privacy Déjà Vu Effect
249 intensifies with the correlation between the old data S_k and the new data S_{k+1} , which is related to
250 subpopulation distribution shifting. As shown by (Jagielski et al., 2023), simulating the subpopulation
251 distribution shifting in continual fine-tuning is a proper way to study the correlation among data. We
252 use the BREEDS framework (Santurkar et al., 2021) to simulate the subpopulation shifting, which
253 works with a hierarchy of classes and samples similar classes in the superclass.

254 For ViTs, we first build S_k by sampling two classes per superclass from Tiny-ImageNet-200 and
255 train the f_k . For BERTs, we randomly choose one class per superclass from IMDb. To simulate
256 a focused subpopulation shifting within a target superclass $s^* \in \mathcal{C}'$, define the remaining pool of
257 classes $C_{\text{rem}} = \{\mathcal{C} \setminus \{\text{classes in } S_k\}\}$ and let $n = |\{C_{\text{rem}} \cap s^*\}|$. Then we form S_{k+1} by sampling
258 examples from $\alpha \times n$ classes chosen at random from $\{C_{\text{rem}} \cap s^*\}$, where $\alpha \in (0, 1]$ controls
259 shifting strength. We choose α from $\{0.2, 0.4, 0.6, 0.8\}$ for Tiny-ImageNet-200 and $\{0.4, 0.7, 1\}$
260 for IMDb. Fine-tuning f_k on S_{k+1} thus implements a BREEDS-style subpopulation shifting in the
261 target superclass s^* , isolating its impact on the Privacy Déjà Vu effect. In our experiments, we repeat
262 experiments by trying each superclass as the target superclass and conclude our results.

264 4.4 ANALYZING THE DEJAVU EFFECT WITH DIFFERENT DATA SIMILARITY MEASURES
265

266 As the Privacy Déjà Vu Effect is similar to how people recall similar memories, we use two sample-
267 to-sample similarity measures between the samples S_k and S_{k+1} to study the factors that cause
268 the effect: **Structural Similarity (SSIM)** (Wang et al., 2004) – a perceptual, pixel-space measure
269 that reflects how humans compare images. **Gradient Dot-Product (NTK-similarity)** (Jacot et al.,

270 2018) – a parameter-space measure that reflects how the model perceives the similarity between two
 271 samples.

272 **SSIM.** SSIM applies only to images, so we use it on ViTs. For every image $x \in S_k$, we compute its
 273 mean SSIM against S_{k+1} . We sort the images by their SSIM score and split them into 10 equal-sized
 274 quantiles. The quantiles with greater ID indicate that the old data is more similar to the S_{k+1} .

275 **NTK-similarity.** The neural tangent kernel compares inputs by the angle of their parameter-gradient
 276 “fingerprints.” High similarity implies that training on one example produces a large first-order effect
 277 on another. We show the detailed computation of the NTK-similarity in Appendix. Analogous to
 278 SSIM, we sort samples in S_k by the NTK-similarity and divide into 10 equal-sized quantiles.

280 281 5 RESULTS

282 In this section, we study the two questions through our experimental results: (1) How does the Privacy
 283 Déjà Vu Effect perform in subpopulation distribution shifting scenarios? (Section 5.1) (2) What are
 284 the causes of the Privacy Déjà Vu Effect? (Section 5.2)

285 286 287 5.1 PRIVACY DÉJÀ VU EFFECT IN SUBPOPULATION DISTRIBUTION SHIFTING



298 Figure 2: Violin graph of privacy risk change Δ of multiple strength of distribution shifting. The
 299 vertical line indicates the range of privacy risk change Δ across samples, and the bulge indicates the
 300 density. Results of the target superclass show samples with larger privacy risk increases than samples
 301 in other superclasses. Greater α causes more significant Privacy Déjà Vu Effect.

302 **Trend with Distribution Shifting Strength.** We show how the subpopulation shifting strength
 303 α impacts the Privacy Déjà Vu Effect in Figure 2a. We use the violin graph to more intuitively
 304 understand the impacts of fine-tuning on privacy risk changes. The vertical span shows the full range
 305 of the Δ . Each violin shape represents the probability density over the y-axis. The narrow shape
 306 means most points are around zero (no dramatic privacy risk change). As the parameter α increases,
 307 the overall range of privacy change Δ —as indicated by the vertical span of the violins in Figure 2—is
 308 larger for both the target superclass and other superclasses, in both BERT and ViT models. The
 309 pronounced bulges near $\Delta \approx 0$ reflect that many samples experience little change in privacy risk.



311 312 313 314 315 316 317 318 319 320 321 322 323 Figure 3: The privacy risk changes for the samples in the target superclass are more affected by the
 324 distribution shifting strength α . With stronger shifting (larger α), less samples in target superclasses
 325 show positive privacy risk change δ , while which in other superclasses do not show obvious trends.
 326 We also show the results with different α in Appendix 3.

324 **Fraction of Positively Changed Samples.** To better understand this pattern, we inspect the population
 325 of samples with positive or negative Δ . We quantify this by:

$$326 \quad r^+ = \frac{|\{x \in S_k : \Delta(x) > 0\}|}{|S_k|}, \quad r^- = 1 - r^+.$$

327 where r^+ indicates the population of the samples that become more risky and r^- indicates the
 328 population of safer samples in S_k .

329 Figure 3 shows that for other superclasses, r^+ converges to about 0.5 as α increases, whereas for the
 330 target class, r^+ decreases. In other words, the Privacy Déjà Vu Effect in the target superclasses only
 331 shows in a smaller number of highly vulnerable examples, not a uniform change across all samples.

332 Combining Figure 2 and 3, the phenomenon is a striking analogy with human memory: just as a few
 333 new examples can cue recall of related past items, a small fine-tuning set “reminds” the models of
 334 old samples. Imagine a person who glimpses a handful of cars drawn from many makes (small α);
 335 they instinctively recall vehicles across all brands. But if they then see dozens of cars from a single
 336 marque (large α), their recall narrows to that one brand and neglects other brands (the vertical span).
 337 This metaphor inspired us to understand the Privacy Déjà Vu Effect from the perspective of similarity
 338 between old and new data. Intuitively, the new data will remind the model of some similar old data.

339 5.2 CAUSES OF THE PRIVACY DÉJÀ VU EFFECT

340 In this section, we study how the Privacy Déjà Vu Effect relates to data similarity.



341 Figure 4: Violin graph of Δ within ascendingly ordered SSIM quantiles when $\alpha = 0.8$. The rightmost
 342 is the quantile with the greatest similarity. The results do not show obvious relationship between
 343 SSIM similarity and the Privacy Déjà Vu Effect.

344 **Structural Similarity (SSIM) vs. Δ .** Following the method in Section 4.4, we begin by asking
 345 whether raw image-level similarity between old and new samples correlates with the privacy risk
 346 change Δ in ViT models. In Figure 4a and Figure 4b, we draw the violin graph of Δ within each
 347 SSIM quantile when $\alpha = 0.8$. If higher visual similarity drove larger privacy risk changes, one would
 348 expect a higher Δ in the quantiles with greater ID. However, both panels exhibit no clear upward
 349 trend—raw image-based SSIM fails to predict which samples exhibit large Δ . When we try various
 350 α , there is also no obvious correlation between SSIM and Δ . We show the results in Appendix 3.

351 Does this observation indicate that similarity is not correlated to Δ variability? Our answer is no.
 352 The key problem is the mismatch between *human-perceptual* and *model-perceptual* similarity: SSIM
 353 mimics our visual judgments, whereas ViTs base their decisions on latent feature representations.

354 **NTK-similarity vs. Δ .** As introduced in Section 4.4, NTK-similarity captures the similarity from
 355 the perspective of machine learning model. Figure 5 shows the violin graph of Δ versus ascending
 356 NTK-similarity quantiles for $\alpha = 0.8$ (ViT) and $\alpha = 1$ (BERT). Figure 5a exhibits a clear upward
 357 trend: in the ViT models, the higher NTK similarity leads to more dramatic change of risks, including
 358 both larger increases and larger decreases for some sample in the target superclass. In the other
 359 superclasses, Figure 5b and 5d show downward trends, which means that higher NTK-similarity in
 360 other superclasses mitigates the sensitivity of old data. This is because they have a different label,
 361 which is a typical example of catastrophic forgetting in continual fine-tuning (De Lange et al., 2021).
 362 That is, the model f_{k+1} will re-link new data to a label, which will impact the model’s performance
 363 on some similar data in S_k with different labels. For instance, assume a blue sport car image in S_k
 364 was labeled as “sport car” and then the label was changed to “blue” in S_{k+1} , f_{k+1} will link the data

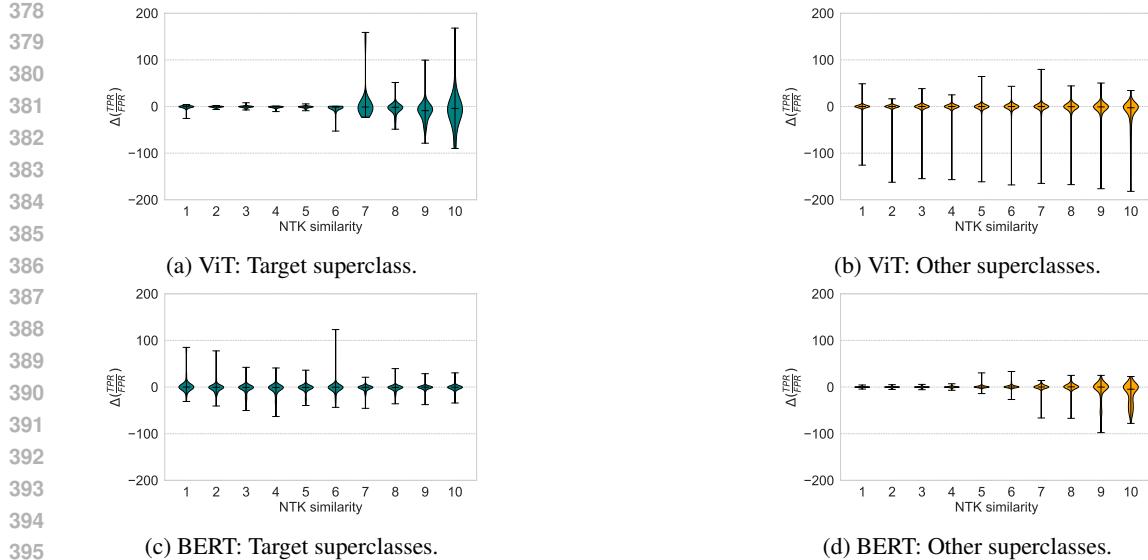


Figure 5: Violin graph of Δ within ascendingly ordered NTK-similarity quantiles. The rightmost is the quantile with the greatest similarity. ViT: $\alpha = 0.8$; BERT: $\alpha = 1$. The Privacy Déjà Vu Effect show clear correlation with NTK-similarity in ViTs. However, the trends is abnormal in BERTs. We visualize the samples in Tiny-ImageNet-200 with the greatest Δ and corresponding top-10 similar samples in S_{k+1} in Appendix 5.

to class "blue" and forget the link to the class "sport car". Moreover, in Appendix 4, we show that increasing α amplifies these trends, demonstrating that stronger subpopulation shifting intensifies the model's reminder of old samples. Intuitively, exposing the model to more new examples strengthens their pull on related old representations. This behavior aligns with the patterns in Figure 1.

However, we also observe two unexpected phenomena: (1) In Figure 5a, even in the highest-similarity quantile, some old data become safer with negative Δ . (2) In BERT, Figure 5c shows that in the target superclass, with increased NTK-similarity, the Privacy Déjà Vu Effect is unchanged or even slightly weakened, which is a reversed pattern compared to the image data on ViT.

To further explore these anomaly patterns, we examine the details of sample similarity levels. Inspired by (Carlini et al., 2022a), who have already hinted that duplicating an image in the training set lowers LiRA's accuracy for each of the duplicated samples. We therefore hypothesize that extremely high similarity between S_{k+1} and a vulnerable point in S_k can act as a privacy shield.

To probe the idea, we run a controlled duplication test. For model f_k , we first identify the most and least vulnerable sample (samples with the greatest and smallest risk R_k). The most sensitive sample has $R_k = 129.36$ in ViT and $R_k = 91.74$ in BERT. Then we pick the top-100 samples in \mathcal{D} (the entire Tiny-ImageNet-200 or IMDb training set) that are similar to the most sensitive sample in S_k , and sort them into 10 shards, $\{\text{Shard}_{i,k+1} | i = 0, \dots, 9\}$. $\text{Shard}_{0,k+1}$ is the most similar shard consisting of the 10 most similar samples. Each shard is used for fine-tuning in step $k+1$ instead, i.e., $S_{k+1} \in \{\text{Shard}_{i,k+1} | i = 0, \dots, 9\}$. Similarly, we also pick the top-100 samples in \mathcal{D} most similar to the least vulnerable sample and conduct the fine-tuning.

Figure 6a shows that the most similar shard will "shield" the old most sensitive sample, and then the "shield" becomes weaker when shards consists of less similar samples. It explains why there are some samples with negative Δ existing in quantile 10 in Figure 5a. In contrast, Figure 6b shows that for the lowest privacy-risk sample, its less similar samples in S_{k+1} will increase the privacy risk more. This explains why the positive Δ is small in Figure 5c.

Why are the bursty privacy-risk changes in Figure 5a for ViT models not observed in Figure 5c for BERT models? We suspect that the IMDb data has low diversity within the superclass, and the distributional shifts are not so obvious between fine-tuning steps. As a result, the step $k+1$ uses a similar dataset to step k , leading to small changes in privacy risks. Table 1 partially supports our conjecture. The IMDb batches in target superclasses have much higher NTK-similarity.



Figure 6: The most similar shard will “shield” the old most sensitive sample. This partially explains two abnormal phenomena. X-axis is the shard ID. The leftmost index means S_{k+1} consists of the most similar shard. The most sensitive sample has $R_k = 129.36$ in ViT and $R_k = 91.74$ in BERT. The least sensitive sample has $R_k = 0.99$ in ViT and $R_k = 0.986$ in BERT. We visualize the samples in the Appendix 6.

Dataset (model)	Target superclass	Other superclass
Tiny-ImageNet-200 (ViT)	0.4484 ± 0.0175	0.3731 ± 0.0188
IMDb (BERT)	0.8791 ± 0.0094	0.1224 ± 0.0172

Table 1: Normalized NTK-similarity (mean \pm std) for target vs. other superclasses. The IMDb batches in target superclasses have much higher NTK-similarity, which partially implies the IMDb data has low diversity within superclasses.

In summary, the Privacy Déjà Vu Effect is rather a local phenomenon: a few similar samples in the new batch trigger the dramatic privacy risk changes of a few old samples. However, as shown in Figure 1, the model is still forgetting legacy data generally. Whether an old example becomes riskier or safer depends chiefly on *feature-level* neighbours it gains in the new round and on the intrinsic complexity of the dataset. Some may question that this may be due to the model re-learning the old sample. However, the old sample will not appear in S_{k+1} . Moreover, in our Appendix, we show that both f_k and f_{k+1} do not overfit on the sample with the greatest Δ . Thus, the effect cannot be concluded as re-memorization. Meanwhile, the relationship is not monotonic: If the old sample is sensitive, initially its risk drops as similarity of newcomer increases—new examples “cover” it better—until a similarity threshold beyond which additional resemblance no longer helps; if the old sample is safe, fine-tuning with similar data raises its privacy risk, but this effect also stop increasing past a certain threshold. Pinpointing those similarity thresholds depends on the model’s capacity and the complexity of the dataset, and how to identify them remains an open challenge.

6 CONCLUSION

Our study of the Privacy Déjà Vu Effect reveals critical implications for privacy protection in continual fine-tuning systems. We summarize our observations and then propose possible solutions.

Reassessing “Safe” Legacy Data. Many studies suggest that catastrophic forgetting can ease the risk of old samples being breached by privacy attacks (Wang et al., 2025). However, we observe that fine-tuning on new data with high feature-level similarity can *rehabilitate* sensitive aspects of old samples, triggering renewed privacy exposure. This Privacy Déjà Vu Effect means that prioritizing the protection of only new data can leave old data unexpectedly vulnerable; privacy mechanisms must therefore guard across all fine-tuning rounds, not just the most recent one.

Open Questions. While our work focuses on domain-incremental fine-tuning, it remains an open question whether the Privacy Déjà Vu Effect manifests in other fine-tuning paradigms, where the label space also evolves. Meanwhile, constrained by the heavy computational cost, we can only show the existence of the effect in two rounds of fine-tuning on representative models. However, our initial observations indicate that other models and additional rounds of fine-tuning are likely to have this effect as well, which will be verified in future work.

486 REFERENCES
487

488 Michael Aerni, Jie Zhang, and Florian Tramèr. Evaluations of machine learning privacy defenses
489 are misleading. In *Proceedings of the 2024 on ACM SIGSAC Conference on Computer and*
490 *Communications Security*, pp. 1271–1284, 2024.

491 Reza Akbarian Bafghi, Nidhin Harilal, Claire Monteleoni, and Maziar Raissi. Parameter efficient
492 fine-tuning of self-supervised vits without catastrophic forgetting. In *Proceedings of the IEEE/CVF*
493 *Conference on Computer Vision and Pattern Recognition (CVPR) Workshops*, pp. 3679–3684, June
494 2024.

495 Jaydeep Borkar, Matthew Jagielski, Katherine Lee, Niloofar Mireshghallah, David A Smith, and
496 Christopher A Choquette-Choo. Privacy ripple effects from adding or removing personal informa-
497 tion in language model training. *arXiv preprint arXiv:2502.15680*, 2025.

498 Nicholas Carlini, Steve Chien, Milad Nasr, Shuang Song, Andreas Terzis, and Florian Tramer.
499 Membership inference attacks from first principles. In *2022 IEEE Symposium on Security and*
500 *Privacy (SP)*, pp. 1897–1914. IEEE, 2022a.

501 Nicholas Carlini, Daphne Ippolito, Matthew Jagielski, Katherine Lee, Florian Tramer, and Chiyuan
502 Zhang. Quantifying memorization across neural language models. In *The Eleventh International*
503 *Conference on Learning Representations*, 2022b.

504 Nicholas Carlini, Matthew Jagielski, Chiyuan Zhang, Nicolas Papernot, Andreas Terzis, and
505 Florian Tramer. The privacy onion effect: Memorization is relative. In S. Koyejo,
506 S. Mohamed, A. Agarwal, D. Belgrave, K. Cho, and A. Oh (eds.), *Advances in Neu-*
507 *ral Information Processing Systems*, volume 35, pp. 13263–13276. Curran Associates, Inc.,
508 2022c. URL https://proceedings.neurips.cc/paper_files/paper/2022/file/564b5f8289ba846ebc498417e834c253-Paper-Conference.pdf.

509 Ajesh Koyatan Chathoth, Clark P Necciai, Abhyuday Jagannatha, and Stephen Lee. Differentially
510 private federated continual learning with heterogeneous cohort privacy. In *2022 IEEE International*
511 *Conference on Big Data (Big Data)*, pp. 5682–5691, 2022a. doi: 10.1109/BigData55660.2022.
512 10021082.

513 Ajesh Koyatan Chathoth, Clark P Necciai, Abhyuday Jagannatha, and Stephen Lee. Differentially
514 private federated continual learning with heterogeneous cohort privacy. In *2022 IEEE International*
515 *Conference on Big Data (Big Data)*, pp. 5682–5691. IEEE, 2022b.

516 Xiaoyi Chen, Siyuan Tang, Rui Zhu, Shijun Yan, Lei Jin, Zihao Wang, Liya Su, Zhikun Zhang,
517 XiaoFeng Wang, and Haixu Tang. The janus interface: How fine-tuning in large language models
518 amplifies the privacy risks. In *Proceedings of the 2024 on ACM SIGSAC Conference on Computer*
519 *and Communications Security*, pp. 1285–1299, 2024.

520 Matthias De Lange, Rahaf Aljundi, Marc Masana, Sarah Parisot, Xu Jia, Aleš Leonardis, Gregory
521 Slabaugh, and Tinne Tuytelaars. A continual learning survey: Defying forgetting in classification
522 tasks. *IEEE transactions on pattern analysis and machine intelligence*, 44(7):3366–3385, 2021.

523 Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale
524 hierarchical image database. In *2009 IEEE conference on computer vision and pattern recognition*,
525 pp. 248–255. Ieee, 2009.

526 Pradnya Desai, Phung Lai, NhatHai Phan, and My T Thai. Continual learning with differential
527 privacy. In *Neural Information Processing: 28th International Conference, ICONIP 2021, Sanur,*
528 *Bali, Indonesia, December 8–12, 2021, Proceedings, Part VI 28*, pp. 334–343. Springer, 2021.

529 Jacob Devlin, Ming-Wei Chang, Kenton Lee, and Kristina Toutanova. Bert: Pre-training of deep
530 bidirectional transformers for language understanding. In *Proceedings of the 2019 conference of*
531 *the North American chapter of the association for computational linguistics: human language*
532 *technologies*, volume 1 (long and short papers), pp. 4171–4186, 2019.

533 Jinshuo Dong, Aaron Roth, and Weijie J Su. Gaussian differential privacy. *Journal of the Royal*
534 *Statistical Society Series B: Statistical Methodology*, 84(1):3–37, 2022.

540 Alexey Dosovitskiy, Lucas Beyer, Alexander Kolesnikov, Dirk Weissenborn, Xiaohua Zhai, Thomas
 541 Unterthiner, Mostafa Dehghani, Matthias Minderer, Georg Heigold, Sylvain Gelly, Jakob Uszkoreit,
 542 and Neil Houlsby. An image is worth 16x16 words: Transformers for image recognition at scale.
 543 *ICLR*, 2021.

544 Cynthia Dwork. Differential privacy. In *International colloquium on automata, languages, and*
 545 *programming*, pp. 1–12. Springer, 2006.

546 European Data Protection Board. Opinion 28/2024 on certain data protec-
 547 tion aspects related to the processing of personal data in the context of ai
 548 models. EDPB Website, December 2024. URL https://www.edpb.europa.eu/our-work-tools/our-documents/opinion-board-art-64/opinion-282024-certain-data-protection-aspects_en. [Online; accessed
 549 May 2025].

550 Farhad Farokhi and Henrik Sandberg. Fisher information as a measure of privacy: Preserving
 551 privacy of households with smart meters using batteries. *IEEE Transactions on Smart Grid*, 9(5):
 552 4726–4734, 2017.

553 Yuechun Gu, Jiajie He, and Keke Chen. Demo: Ft-privacyscore: Personalized privacy scoring service
 554 for machine learning participation. In *Proceedings of the 2024 on ACM SIGSAC Conference on*
 555 *Computer and Communications Security*, CCS ’24, pp. 5075–5077, New York, NY, USA, 2024.
 556 Association for Computing Machinery. ISBN 9798400706363. doi: 10.1145/3658644.3691366.
 557 URL <https://doi.org/10.1145/3658644.3691366>.

558 Raia Hadsell, Dushyant Rao, Andrei A Rusu, and Razvan Pascanu. Embracing change: Continual
 559 learning in deep neural networks. *Trends in cognitive sciences*, 24(12):1028–1040, 2020.

560 Ahmad Hassanzadeh, Majid Moradikia, Bian Yang, Ahmed Abdelhadi, Christoph Busch, and Julian
 561 Fierrez. Differential privacy preservation in robust continual learning. *IEEE Access*, 10:24273–
 562 24287, 2022. doi: 10.1109/ACCESS.2022.3154826.

563 Tyler L Hayes, Kushal Kafle, Robik Shrestha, Manoj Acharya, and Christopher Kanan. Remind your
 564 neural network to prevent catastrophic forgetting. In *European conference on computer vision*, pp.
 565 466–483. Springer, 2020.

566 IBM Cloud. Algorithm version and training. IBM Cloud Documentation,
 567 2023. URL <https://cloud.ibm.com/docs/watson-assistant?topic=watson-assistant-algorithm-version>. [Online; accessed May 2025].

568 Arthur Jacot, Franck Gabriel, and Clément Hongler. Neural tangent kernel: Convergence and
 569 generalization in neural networks. *Advances in neural information processing systems*, 31, 2018.

570 Matthew Jagielski, Jonathan Ullman, and Alina Oprea. Auditing differentially private machine
 571 learning: How private is private sgd? *Advances in Neural Information Processing Systems*, 33:
 572 22205–22216, 2020.

573 Matthew Jagielski, Stanley Wu, Alina Oprea, Jonathan Ullman, and Roxana Geambasu. How to
 574 combine membership-inference attacks on multiple updated machine learning models. *Proceedings*
 575 *on Privacy Enhancing Technologies*, 2023.

576 Peter Kairouz, Sewoong Oh, and Pramod Viswanath. The composition theorem for differential
 577 privacy. In *International conference on machine learning*, pp. 1376–1385. PMLR, 2015.

578 Ya Le and Xuan S. Yang. Tiny imagenet visual recognition challenge. In *CS231N: Convolutional Neu-*
 579 *ral Networks for Visual Recognition*, 2015. URL <https://tiny-imagenet.herokuapp.com/>. Stanford University.

580 Andrew L. Maas, Raymond E. Daly, Peter T. Pham, Dan Huang, Andrew Y. Ng, and Christopher
 581 Potts. Learning word vectors for sentiment analysis. In *Proceedings of the 49th Annual Meeting*
 582 *of the Association for Computational Linguistics: Human Language Technologies*, pp. 142–
 583 150, Portland, Oregon, USA, 2011. Association for Computational Linguistics. URL <https://aclanthology.org/P11-1015/>.

594 James L McClelland, Bruce L McNaughton, and Randall C O'Reilly. Why there are complementary
 595 learning systems in the hippocampus and neocortex: insights from the successes and failures of
 596 connectionist models of learning and memory. *Psychological review*, 102(3):419, 1995.

597

598 Michael McCloskey and Neal J Cohen. Catastrophic interference in connectionist networks: The
 599 sequential learning problem. In *Psychology of learning and motivation*, volume 24, pp. 109–165.
 600 Elsevier, 1989.

601 Milad Nasr, Jamie Hayes, Thomas Steinke, Borja Balle, Florian Tramèr, Matthew Jagielski, Nicholas
 602 Carlini, and Andreas Terzis. Tight auditing of differentially private machine learning. In *32nd*
 603 *USENIX Security Symposium (USENIX Security 23)*, pp. 1631–1648, 2023.

604

605 Reddit, Inc. What are home feed recommendations?
 606 <https://support.reddithelp.com/hc/en-us/articles/440228477364-What-are-home-feed-recommendations>. Reddit Help Cen-
 607 ter, updated Nov 06, 2024.

608

609 Shibani Santurkar, Dimitris Tsipras, and Aleksander Madry. Breeds: Benchmarks for subpopulation
 610 shift. In *International Conference on Learning Representations*, 2021.

611

612 Joan Serra, Didac Suris, Marius Miron, and Alexandros Karatzoglou. Overcoming catastrophic
 613 forgetting with hard attention to the task. In *International conference on machine learning*, pp.
 614 4548–4557. PMLR, 2018.

615

616 Reza Shokri, Marco Stronati, Congzheng Song, and Vitaly Shmatikov. Membership inference attacks
 617 against machine learning models. In *2017 IEEE symposium on security and privacy (SP)*, pp. 3–18.
 618 IEEE, 2017.

619

620 Amy Stapleton. IBM Fine-Tunes LLMs for Customer Service with IBM Watsonx.ai. Opus
 621 Research Blog (July 17, 2023). URL <https://opusresearch.net/2023/07/17/ibm-fine-tunes-llms-for-customer-service-with-ibm-watsonx-ai/>.

622

623 Thomas Steinke, Milad Nasr, and Matthew Jagielski. Privacy auditing with one (1) training run.
 624 *Advances in Neural Information Processing Systems*, 36, 2024.

625

626 Florian Tramer, Andreas Terzis, Thomas Steinke, Shuang Song, Matthew Jagielski, and Nicholas
 627 Carlini. Debugging differential privacy: A case study for privacy auditing. *arXiv preprint*
 628 *arXiv:2202.12219*, 2022.

629

630 Gido M Van de Ven and Andreas S Tolias. Three scenarios for continual learning. *arXiv preprint*
 631 *arXiv:1904.07734*, 2019.

632

633 Liyuan Wang, Xingxing Zhang, Hang Su, and Jun Zhu. A comprehensive survey of continual learning:
 634 Theory, method and application. *IEEE Transactions on Pattern Analysis and Machine Intelligence*,
 635 2024.

636

637 Zhenyi Wang, Enneng Yang, Li Shen, and Heng Huang. A comprehensive survey of forgetting in
 638 deep learning beyond continual learning. *IEEE Transactions on Pattern Analysis and Machine*
 639 *Intelligence*, 47(3):1464–1483, 2025. doi: 10.1109/TPAMI.2024.3498346.

640

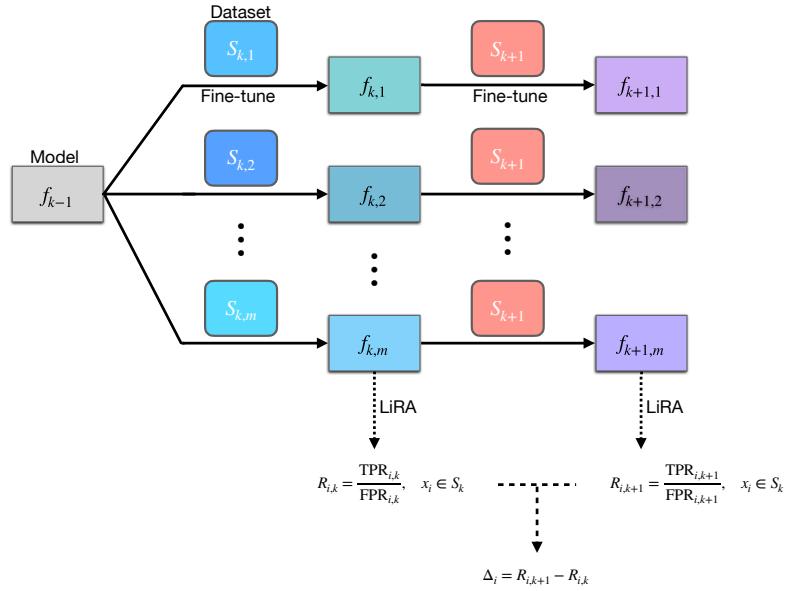
641

642 Zhou Wang, A.C. Bovik, H.R. Sheikh, and E.P. Simoncelli. Image quality assessment: from error
 643 visibility to structural similarity. *IEEE Transactions on Image Processing*, 13(4):600–612, 2004.
 644 doi: 10.1109/TIP.2003.819861.

645

646

647

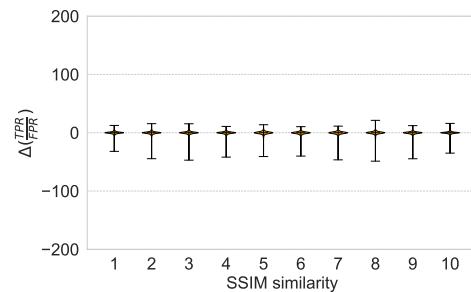
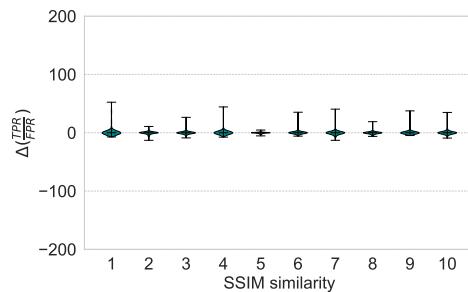
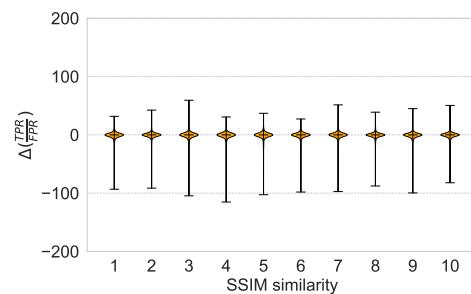
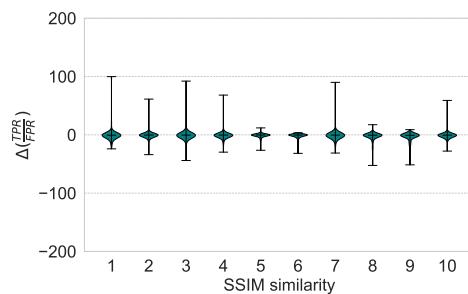
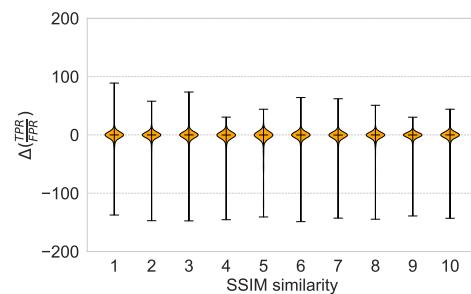
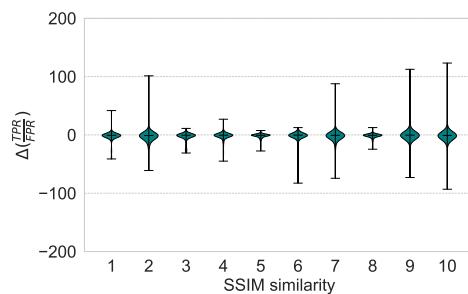
648
649
A APPENDIX650
651
A.1 ILLUSTRATION OF FINE-TUNING MODELS AND ESTIMATION OF PRIVACY SCORE671
672
Figure 7: Fine-tune models and estimate per-sample privacy scores difference Δ_i . $S_{k,m} \subset S_k$,
673
 $S_k \cap S_{k+1} = \emptyset$.674
675
A.2 NTK-SIMLARITY676
677
Let $g_k(x) = \nabla_\theta f_k(x)$ be the gradient of the fine-tuned round- k model with respect to input x and
678
define

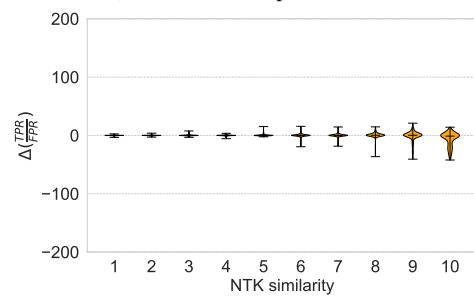
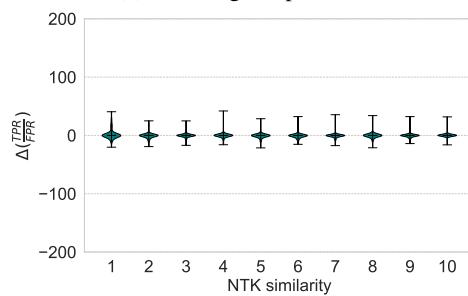
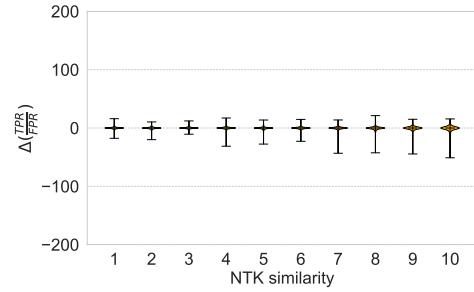
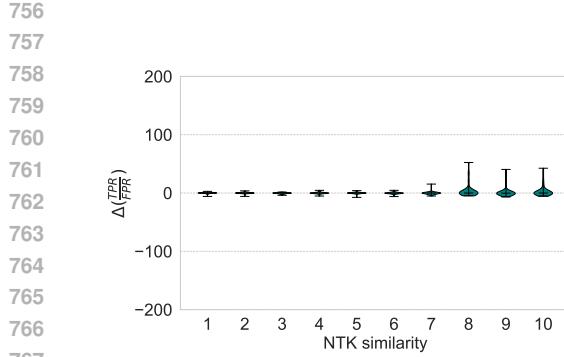
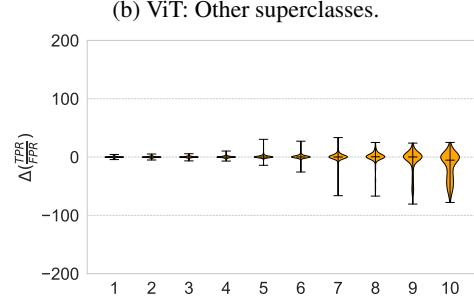
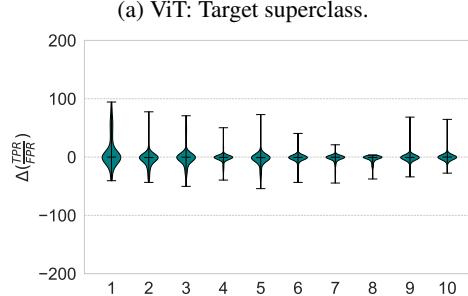
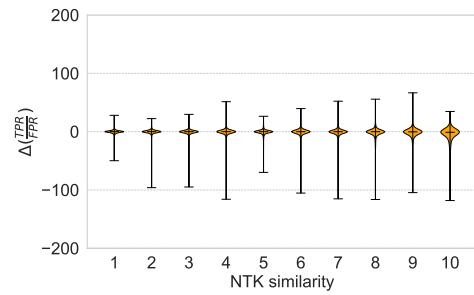
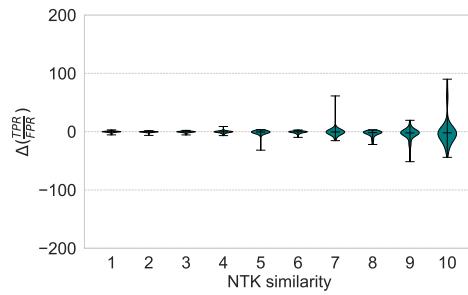
679
680
$$K(x, x') = \langle g_k(x), g_k(x') \rangle.$$

681
682
For every $x \in S_k$ we compute its mean similarity to the new set:

683
684
$$\bar{K}(x) = \frac{1}{|S_{k+1}|} \sum_{x' \in S_{k+1}} K(x, x').$$

685
686
A.3 SSIM AND Δ : VARIOUS α 687
688
We show the correlation between SSIM-similarity and Δ in various α settings. Figure-8 to 10 show
689
no significant correlations.690
691
A.4 NTK-SIMILARITY AND Δ : VARIOUS α 692
693
We show the correlation between NTK-similarity and Δ in various α settings. Figure-11 to 13 show
694
apparent correlations.695
696
697
698
699
700
701

Figure 8: SSIM vs. Δ : $\alpha = 0.2$ Figure 9: SSIM vs. Δ : $\alpha = 0.4$ Figure 10: SSIM vs. Δ : $\alpha = 0.6$

Figure 11: Violin graph of each quantile. ViT: $\alpha = 0.2$; BERT: $\alpha = 0.4$.Figure 12: Violin graph of each quantile. ViT: $\alpha = 0.4$; BERT: $\alpha = 0.7$.

810
811
812
813
814
815
816
817
818
819
820
821
822
823
824
825
826
827
828
829
830

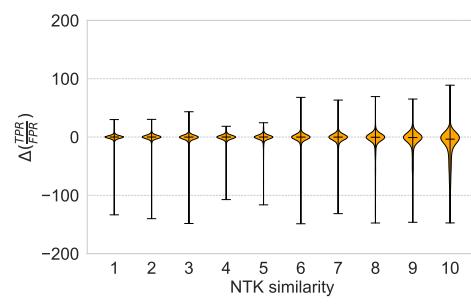
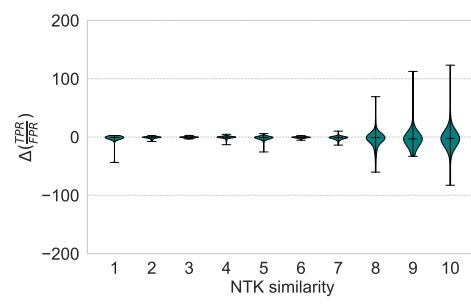


Figure 13: Violin graph of each quantile. ViT: $\alpha = 0.6$.

864
865A.5 VISUALIZATION OF SAMPLES WITH THE GREATEST Δ 866
867
868
869
870
871
872

We show the old samples with the greatest Δ (circled by red rectangle), and their nearest neighbors with the greatest NTK-similarity in this section. Figure 14 shows the old sample from the target superclass "mammal". We have tested the sample whose privacy risk increases most, e.g., the circled sample in Figure 14, on all models and found that f_k 's accuracy is 89.3% and f_{k+1} 's is 87.5%. In comparison, the average fine-tuning accuracy of fine-tuning set on the models is 97.3%. Thus, the most sensitive sample appears not to be overfitted by f_k and f_{k+1} . Furthermore, models seem to perform worse after seeing more new samples.

873
874

Figure 14 shows the old sample from one of the other superclasses, "instrumentality".

875
876
877
878
879880
881
882

Figure 14: Sample from target superclass with greatest $\Delta = 147.3$ and the most similar samples in S_{k+1} . Target superclass = "mammal".

883
884
885
886
887
888
889890
891
892

Figure 15: Sample from other superclass with greatest $\Delta = 92.2$ and the most similar samples in S_{k+1} . Target superclass = "mammal". Superclass of sample = "instrumentality".

893
894
895

A.6 VISUALIZATION OF THE TOP-100 MOST NTK-SIMILAR SAMPLES OF THE TARGET OLD SAMPLE

896
897
898
899

We show the old samples with the greatest and smallest R_k (circled by red rectangle) in this section. Figure 16 shows the sample with the greatest R_k and its top-100 most NTK-similar samples. Figure 17 shows the sample with the smallest R_k and its top-100 most NTK-similar samples.

900
901
902
903
904
905
906
907
908
909
910
911
912
913
914
915
916
917

918
 919
 920
 921
 922
 923
 924
 925
 926
 927
 928
 929
 930
 931
 932
 933
 934
 935
 936
 937
 938
 939
 940
 941
 942
 943
 944
 945
 946
 947
 948
 949
 950
 951
 952
 953
 954
 955
 956
 957
 958
 959
 960
 961
 962
 963
 964
 965
 966
 967
 968
 969
 970
 971

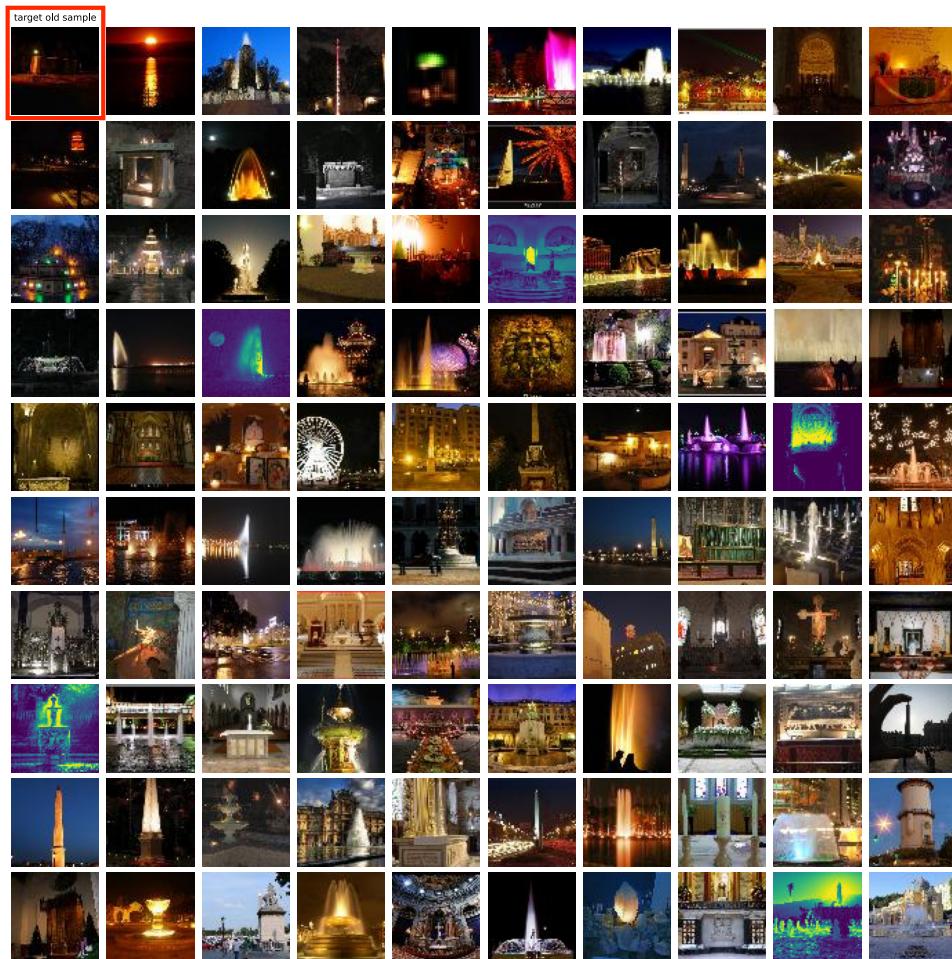


Figure 16: Visualized most sensitive old sample (top left). Figures from left to right have smaller similarity. Some may not be visually similar, but with high NTK-similarity.

972
 973
 974
 975
 976
 977
 978
 979
 980
 981
 982
 983 **target old sample**
 984 
 985 
 986 
 987 
 988 
 989 
 990 
 991 
 992 
 993 
 994 
 995 
 996 
 997 
 998 
 999 
 1000 
 1001 
 1002 
 1003 
 1004 
 1005 
 1006
 1007
 1008
 1009
 1010
 1011
 1012
 1013
 1014
 1015
 1016
 1017
 1018
 1019
 1020
 1021
 1022
 1023
 1024
 1025

Figure 17: Visualized most vulnerable old sample (top left). Figures from left to right have smaller similarity. The bottom right figure has the least NTK-similarity.