

000 001 002 003 004 005 006 007 008 009 010 011 012 013 014 015 016 017 018 019 020 021 022 023 024 025 026 027 028 029 030 031 032 033 034 035 036 037 038 039 040 041 042 043 044 045 046 047 048 049 050 051 052 053 PROVENANCE-ENABLED MULTI-VIEW DIABETIC RETINOPATHY DIAGNOSIS THROUGH INTERPRETABLE PROCESS MINING

Anonymous authors

Paper under double-blind review

ABSTRACT

Diabetic retinopathy (DR) is a leading cause of blindness among individuals with diabetes. Although the existing deep learning models have demonstrated potential in DR diagnosis, they still lack full-process interpretability. Specifically, these models suffer from three key challenges: reliance on single-source inputs, opaque and untraceable reasoning processes, and the absence of a mechanism for result verification. To meet the requirements of the medical scenario for a trustworthy diagnostic model, we propose a provenance-enabled concept-based framework for multi-view DR diagnostic (ProConMV). This work integrates DR lesion masks, clinical text and multi-view data, utilizing multimodal prompt analysis and visual-text concept interaction to learn the interpretable multi-source input. During the reasoning stage, the proposed framework introduces lesion concepts for causal reasoning chains combining clinical guidelines, and adds doctor intervention for human-machine collaboration. For dynamic fusion decision and verification in multi-view DR diagnosis, we derive via generalization theory that incorporating each view's lesion concept uncertainty and grading uncertainty reduces the generalization error upper bound. Accordingly, we design a dual uncertainty-aware module to enable provenance-based verification, ultimately enabling verifiable analysis of DR diagnostic results. Extensive experiments conducted on two public multi-view DR datasets demonstrate the effectiveness of our method.

1 INTRODUCTION

Diabetic retinopathy (DR) is a major cause of blindness among diabetic patients (Federation, 2021), posing a visual health error to the global working-age population. International DR severity is diagnosed by lesions like microaneurysms (MA), hemorrhage (HE), and exudation (EX), and classified into five grades (Grade 0-4): normal, mild, moderate, severe, and Proliferative Diabetic Retinopathy (PDR) (Wilkinson et al., 2003). With the development of artificial intelligence technology, traditional deep learning models (Liu et al., 2022a; 2024a) have demonstrated excellent performance in DR grading tasks, capable of quickly processing large amounts of images and providing grading results. However, their inherent limitations in practical application have gradually become bottlenecks in bridging the gap between AI technology and real-world medical needs.

A critical examination of existing DR diagnostic models (as in Section A.1 of appendix) reveals three core challenges that undermine their credibility and usability in clinical settings (Lin et al., 2025), as illustrated in Fig.1. First, single-source input limitations persist: most models rely solely on monomodal data and fail to integrate complementary information from lesion morphology and clinical text. Moreover, training on single-view databases (Decenciere et al., 2014; EyePACS, 2015) means the field of view (FOV) of input images covers only 20% of the observable fundus, increasing the error of missing critical pathological features. Second, "black-box" reasoning processes lack medical interpretability (Huang et al., 2024): the internal calculations of traditional models are opaque, and they cannot map image features to diagnostic results via clinically understandable logic. Third, insufficient result verification mechanisms (Luo et al., 2025): existing methods generally lack uncertainty quantification and traceable validation, making it impossible to assess the reliability of diagnostic outputs. This deficiency is particularly problematic in medical scenarios, where unreliable results may lead to misdiagnosis, missed diagnosis, or inappropriate clinical interventions.

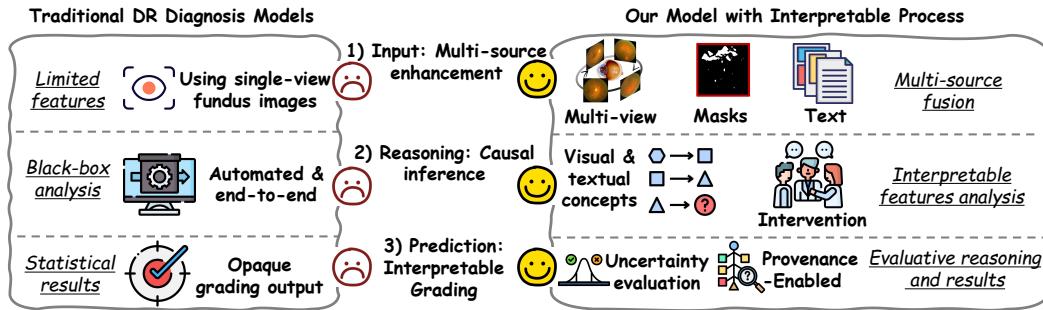


Figure 1: Our model with an interpretable process compared with traditional DR diagnosis models.

To address these critical issues and alleviate the credibility dilemma of DR diagnosis models in clinical practice, this study proposes a full-process interpretable framework for DR diagnosis, encompassing multi-source input fusion, interpretable causal reasoning, and verifiable result evaluation. Specifically, we integrate fundus image lesion masks, structured clinical texts, and multi-view fundus data to construct a rich input space. The proposed Hilbert RWKV encodes spatial features of images for precise lesion localization, while a large language model (LLM)-based text encoder (Achiam et al., 2023) extracts lesion-related semantic information from clinical texts, with cross-modal interaction enabled by a Visual-Text RWKV (VT-RWKV) module. For reasoning, we introduce lesion concepts (Wen et al., 2024) as intermediate units aligned with clinical guidelines. And incorporate real-time doctor intervention to build a human-machine collaborative causal reasoning chain, transforming "input-output" mapping into physician-understandable pathological logic.

Furthermore, multi-view fusion decision-making is crucial for the comprehensive DR diagnosis. However, due to varying cooperation among different patients during fundus examinations, the captured multi-view fundus images exhibit various variations. Most existing multi-view fusion methods (Hu et al., 2025) lack theoretical guarantees, which can lead to one-sided and inaccurate diagnostic results. To achieve reliable dynamic fusion, we demonstrate for the first time in a multi-view concept-based model that, from the perspective of generalization theory, when fusion weights are negatively correlated with both concept loss and grading loss, the upper bound of the generalization error for decision fusion will be reduced and outperforms that of static fusion methods. Meanwhile, the concept uncertainty and grading uncertainty of each view related to the decision are traceable, enabling verifiable analysis of DR diagnostic results. The main contributions of this full-process interpretable DR diagnosis framework are summarized as follows:

- The multimodal input mechanism is proposed to integrate DR lesion masks, clinical text, and multi-view data. Leveraging Hilbert RWKV encoding of image features and textual concept encoder extraction of text features to achieve cross-modal interaction, a semantically rich interpretable input foundation is provided for reasoning.
- A causal reasoning chain combining lesion concepts and clinical guidelines is constructed, with the simultaneous introduction of a doctor intervention link to form a human-machine collaborative reasoning mode, effectively solving the problem of opaque and untraceable reasoning processes in traditional models.
- In the dynamic fusion decision, we derive for the first time from the perspective of generalization that incorporating the lesion concept uncertainty and the grading uncertainty of each view can reduce the generalization error upper bound. Then, we design a dual uncertainty-aware module to realize provenance-enabled verification of diagnostic results.

2 METHOD

This framework takes the fusion of multi-source clinical data as its input foundation, uses medically logical causal reasoning as its core link, and employs a dual uncertainty-aware mechanism as its result guarantee.

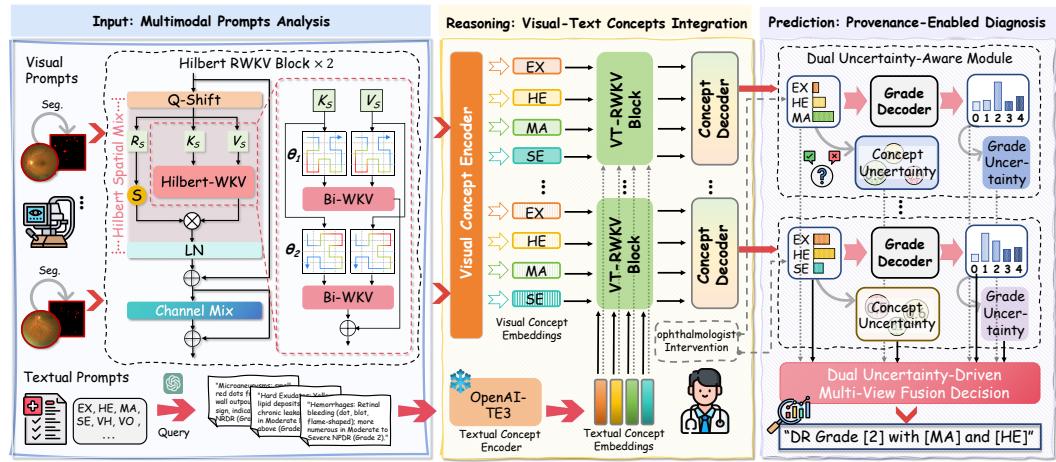


Figure 2: The framework of our proposed ProConMV model has three parts: multi-source input for the enhancement of interpretable features, visual-text concepts integration for causal reasoning, and provenance-enabled diagnosis using the dual uncertainty-aware module.

2.1 MULTI-VIEW CONCEPT REPRESENTATION LEARNING

Some studies (Xu et al., 2021; Shamshad et al., 2023) have demonstrated that existing Transformer-based multi-view methods (Xu et al., 2024; Gu et al., 2024) are less effective at fine-grained local concept perception, while incurring large parameter overhead and prolonged inference times. To capture multi-view fine-grained lesion concept features, we propose an RWKV-based backbone equipped with multi-directional Hilbert attention mechanism, which preserves linear complexity while ensuring continuity in fundus local representation learning. Specifically, the backbone first utilizes a stem (comprising two convolutional layers and downsampling) to extract shallow features for each view. Then, it optimizes the deep features using two Hilbert RWKV Blocks.

2.1.1 HILBERT RWKV BLOCK

This block mainly consists of two components: Hilbert spatial-mix and channel-mix. The spatial mixing is the core, while the channel mixing serves as a feed-forward network (FFN) to enhance channel features. Given the fundus representation of the v -th view $\mathbf{x}^{(v)} \in \mathbb{R}^{h \times w \times d}$, the block first transforms it into $p \times p$ patches, which are then projected into visual tokens of shape $\frac{h w}{p^2} \times d$. These tokens $\bar{\mathbf{x}}^{(v)}$ are fed into the Hilbert spatial-mix module. Similar to Vision-RWKV (Duan et al., 2025), we adopt the quad-directional token shift (Q-Shift) operation along with three parallel linear layers to obtain the matrices $\mathbf{R}_s, \mathbf{K}_s, \mathbf{V}_s \in \mathbb{R}^{\frac{h w}{p^2} \times d}$:

$$\mathbf{R}_s = \text{Q-Shift}_R(\bar{\mathbf{x}}^{(v)})W_R, \quad \mathbf{K}_s = \text{Q-Shift}_K(\bar{\mathbf{x}}^{(v)})W_K, \quad \mathbf{V}_s = \text{Q-Shift}_V(\bar{\mathbf{x}}^{(v)})W_V. \quad (1)$$

This Q-Shift operation enhances the attention mechanism by allowing tokens to shift and perform linear interpolation with neighboring tokens, thereby improving the receptive field of each token without increasing computational complexity. The following formula holds:

$$\begin{aligned} \text{Q-Shift}_{(*)}(\bar{\mathbf{x}}^{(v)}) &= \bar{\mathbf{x}}^{(v)} + (1 - \mu(*))\bar{\mathbf{x}}'^{(v)}, \quad \bar{\mathbf{x}}'^{(v)}[a, b] = \\ &\text{Concat}(\bar{\mathbf{x}}^{(v)}[a-1, b, 0: \frac{d}{4}], \bar{\mathbf{x}}^{(v)}[a+1, b, \frac{d}{4}: \frac{d}{2}], \bar{\mathbf{x}}^{(v)}[a, b-1, \frac{d}{2}: \frac{3d}{4}], \bar{\mathbf{x}}^{(v)}[a, b+1, \frac{3d}{4}: d]), \end{aligned} \quad (2)$$

where the subscript $(*) \in \{R, K, V\}$ represents the interpolation of $\bar{\mathbf{x}}^{(v)}$ and $\bar{\mathbf{x}}'^{(v)}$, controlled by the learnable vector $\mu(*)$. Subsequently, we design a novel linear attention mechanism with local continuity perception, Hilbert-WKV($\mathbf{K}_s, \mathbf{V}_s$), and a gating function $\sigma(\mathbf{R}_s)$ to obtain the output of the Hilbert spatial mixing module \mathbf{O}_s , as shown in the figure:

$$\mathbf{O}_s = \text{LN}(\sigma(\mathbf{R}_s) \odot \text{Hilbert-WKV}(\mathbf{K}_s, \mathbf{V}_s)W_{O_s}). \quad (3)$$

Here, σ represents the sigmoid function, \odot denotes element-wise multiplication, and LN refers to layer normalization. To achieve channel feature fusion, \mathbf{O}_s is passed into the channel-mix module.

$\mathbf{R}_c, \mathbf{K}_c, \mathbf{V}_c \in \mathbb{R}^{\frac{hw}{p^2} \times d}$ are obtained similarly to spatial-mix by \mathbf{O}_s . In the channel-mix module, \mathbf{V}_c is the linear projection of \mathbf{K}_c after applying the activation function SquaredReLU, controlled by a gating mechanism $\sigma(\mathbf{R}_c)$. The output \mathbf{O}_c is the linear projection of the resulting value:

$$\mathbf{O}_c = \sigma(\mathbf{R}_c) \odot (\text{SquaredReLU}(\mathbf{K}_c)W_V)W_{O_c}. \quad (4)$$

2.1.2 HILBERT-WKV ATTENTION MECHANISM

Inspired by the filling curve (Chen et al., 2023) and the bidirectional attention mechanism Bi-WKV (Duan et al., 2025), we design the Hilbert-WKV, a multi-directional attention mechanism grounded in the Hilbert curve. Our proposed Hilbert-WKV has two advantages in multi-view fundus representation learning, as shown in Fig. 2, it preserves the continuity of token arrangement, and the local scanning characteristic of the Hilbert curve window outperforms the default strip scanning.

Specifically, after dividing into $\frac{hw}{p^2}$ tokens of size $p \times p$, the arrangement order of the tokens is determined based on the 2D Hilbert curve:

$$H_n(a, b) = \begin{cases} 4 \cdot H_{n-1}(b, a) & (a, b) \in Q_0, \\ 4 \cdot H_{n-1}(a, b) + 4^{n-1} & (a, b) \in Q_1, \\ 4 \cdot H_{n-1}(a, b) + 2 \cdot 4^n & (a, b) \in Q_2, \\ 4 \cdot H_{n-1}(N - 1 - b, N - 1 - a) + 3 \cdot 4^{n-1} & (a, b) \in Q_3. \end{cases} \quad (5)$$

Here, $H_n(a, b)$ represents the Hilbert sequence position of the token located at (a, b) , with $N = 2^n = \frac{1}{p}\sqrt{hw}$ and $H_n(0, 0) = 0$. Q_0 to Q_3 represent the four quadrants formed by dividing the area of $N/2$ into four sections: Q_0 (lower-left), Q_1 (upper-left), Q_2 (upper-right), and Q_3 (lower-right). We denote the Hilbert Transform as η and its inverse as η^{-1} . The proposed Hilbert-WKV attention mechanism constructs attention mechanisms with vertical and horizontal direction priorities:

$$\text{Hilbert-WKV}(\mathbf{K}_s, \mathbf{V}_s) = \underbrace{\eta^{-1}(\text{Bi-WKV}(\bar{\mathbf{K}}_s, \bar{\mathbf{V}}_s))}_{\text{Vertical Attention}} + \underbrace{\eta^{-1}(\text{Bi-WKV}(\bar{\mathbf{K}}_s^\top, \bar{\mathbf{V}}_s^\top))^\top}_{\text{Horizontal Attention}}, \quad (6)$$

where $\bar{\mathbf{K}}_s = \eta(\mathbf{K}_s)$, $\bar{\mathbf{V}}_s = \eta(\mathbf{V}_s)$,

where \top is the transpose. The Bi-WKV attention calculation for the t -th token is formulated as follows:

$$wkv_t = \text{Bi-WKV}(\mathbf{K}_s, \mathbf{V}_s)_t = \frac{\sum_{i=0, i \neq t}^{T-1} e^{-(|t-i|-1)/T \cdot w + k_i} v + e^{u+k_t} v_t}{\sum_{i=0, i \neq t}^{T-1} e^{-(|t-i|-1)/T \cdot w + k_i} + e^{u+k_t}}, \quad (7)$$

where, $T = \frac{hw}{p^2}$ represents the total number of tokens. w and u are two D -dimensional learnable vectors representing channel-wise spatial decay and the current token, respectively. k_t and v_t denote the t -th feature of \mathbf{K}_s and \mathbf{V}_s . Compared to the self-attention, the Hilbert-WKV attention achieves linear computational complexity $O(n \times T \times D)$, where n is a constant.

2.1.3 VISUAL CONCEPT ENCODER

Following the shared backbone processing, each view obtains its latent representation $\bar{\mathbf{h}}^{(v)} \in \mathbb{R}^{n_h}$. Our model then feeds $\bar{\mathbf{h}}^{(v)}$ into a concept-specific fully connected layer, which learn the lesion concept embedding in \mathbb{R}^{n_z} , namely $\mathbf{z}_j^{(v)} = \sigma(W_j \bar{\mathbf{h}}^{(v)} + b_j)$. Here, $\mathbf{z}_j^{(v)}$ denotes the j -th concept embedding in the i -th view, while σ , W_j , and b_j correspond to the LeakyReLU activation function, weight paremeters, and bias term of the j -th concept layer, which are shared across all views. In this way, the fundus visual feature is mapped into lesion concept representations for each view.

2.1.4 TEXTUAL CONCEPT ENCODER

We use GPT-4 (Achiam et al., 2023) to obtain medical knowledge descriptions for each DR lesion concept, focusing on their characteristics and occurrence stages. **This description text is a curated knowledge base for retinal diagnosis, which provides a unified textual description for all samples as a shared semantic anchor point.** The text is fed into a frozen text encoder text-embedding-3-large (TE3) to generate the textual concept embedding $\mathbf{t}_j \in \mathbb{R}^{n_t}$, where j denotes the j -th concept.

216 2.2 MULTI-VIEW VISUAL-TEXT CONCEPT INTEGRATION
217

218 To efficiently align multi-view lesion concept representations with human clinical knowledge and
219 improve reasoning interpretability, we propose a visual-text RWKV (VT-RWKV) block, a multi-
220 model driven concept enhancement method based on RWKV.

221 Specially, for view v , our model considers the concatenated representation of the concept visual em-
222 bedding $\mathbf{z}^{(v)} = [\mathbf{z}_1^{(v)}, \mathbf{z}_2^{(v)}, \dots, \mathbf{z}_M^{(v)}]$ and its corresponding textual embedding $\mathbf{t} = [\mathbf{t}_1, \mathbf{t}_2, \dots, \mathbf{t}_M]$
223 as input, where M denotes the number of lesion concepts. The multi-modal embeddings are then
224 projected through three parallel linear layers to obtain the matrices $\mathbf{R}_{con}, \mathbf{W}_{con}, \mathbf{K}_{con} \in \mathbb{R}^{m \times n_z}$:
225

$$226 \quad \mathbf{R}_{con} = W_r \mathbf{z}^{(v)}, \quad \mathbf{K}_{con} = W_k \mathbf{t}, \quad \mathbf{V}_{con} = W_v \mathbf{t}, \quad (8)$$

227 where W_r, W_k , and W_v are learnable parameters. Here, the VT-RWKV operator improves concept
228 visual representations by fusing them with aligned textual features. The key and value matrices
229 \mathbf{K}_{con} and \mathbf{V}_{con} , computed from \mathbf{t} , are fed into a linear complexity bidirectional attention module,
230 Bi-WKV, to obtain the attention output $ckv \in \mathbb{R}^{M \times n_z}$. Meanwhile, the visual embedding $\mathbf{z}^{(v)}$
231 generates a gating matrix $\sigma(\mathbf{R}_{con})$, which modulates the attention output. The enhanced concept
232 representation $\bar{\mathbf{z}}^{(v)}$ is computed as:

$$233 \quad \bar{\mathbf{z}}^{(v)} = (\sigma(\mathbf{R}_{con}) \odot ckwv) W_z, \quad ckwv = \text{Bi-WKV}(\mathbf{K}_{con}, \mathbf{V}_{con}), \quad (9)$$

234 where W_z is a learnable projection matrix, σ denotes the sigmoid function, and \odot represents
235 element-wise multiplication. Through this fusion, the model obtains each view's lesion concept
236 embeddings that are aligned with both visual information and diagnostic knowledge, thereby en-
237 hancing the interpretability and predictive accuracy of the concepts.

238 In reasoning, the view-shared concept decoder C transforms the enhanced concept representation of
239 each view into its corresponding concept predictions, which are then passed to the grade decoder G
240 to produce the final grading result for that view. For view v , the procedure can be derived as:

$$241 \quad \hat{\mathbf{c}}^{(v)} = C(\bar{\mathbf{z}}^{(v)}) \in \mathbb{R}^M, \quad \hat{\mathbf{y}}^{(v)} = G(\hat{\mathbf{c}}^{(v)}) \in \mathbb{R}^K. \quad (10)$$

243 Here, $\hat{\mathbf{c}}^{(v)}$ denotes the concept prediction vector of view v with M concepts, and $\hat{\mathbf{y}}^{(v)}$ represents the
244 corresponding grading vector with K DR grades. In this way, the model completes the entire process
245 from input to concept analysis and finally to grading output for each view, i.e., $\mathbf{x}^{(v)} \rightarrow \hat{\mathbf{c}}^{(v)} \rightarrow \hat{\mathbf{y}}^{(v)}$.

246 2.3 DUAL UNCERTAINTY-AWARE INTERPRETABLE MULTI-VIEW DR DIAGNOSIS
247

248 In the traditional interpretable concept reasoning pipeline, we find that the final grading prediction
249 cannot fully capture the reliability of each view. This limitation arises because the lesion concepts,
250 which serve as the input to the $c \rightarrow g$ stage, play a critical role in determining both the interpretabil-
251 ity and the accuracy of the reasoning process for each view. Thus, we propose a dynamic fusion
252 method with dual uncertainty awareness in concept prediction and grading.

254 2.3.1 GENERALIZATION THEORY IN MULTI-VIEW CONCEPT-BASED MODELS
255

256 We integrate the generalization theory into the multi-view concept-based framework. This enables
257 us to formalize the reasoning process, analyze grading prediction loss, and validate dynamic weight
258 design, as detailed in the following setting and derivation.

259 **Setting.** In conjunction with Equation (10), we define $\mathbf{c}^{(v)}$ and $\mathbf{y}^{(v)}$ as the concept label and the
260 grading (class prediction) label of view v , respectively. According to the reasoning pipeline $\mathbf{x}^{(v)} \rightarrow$
261 $\hat{\mathbf{c}}^{(v)} \rightarrow \hat{\mathbf{y}}^{(v)}$, The view-shared concept predictor C and grading predictor G are specified in the
262 hypothesis spaces \mathcal{C} and \mathcal{G} . The final prediction of the late-fusion multi-view method is formulated as
263 $\hat{\mathbf{y}} = \sum_{v=1}^V w_v \hat{\mathbf{y}}^{(v)}$, where $w_v \in (0, 1)$ denotes the fusion weight of view v , satisfying $\sum_{v=1}^V w_v =$
264 1. Unlike the static fusion weight w_v^s , dynamic weight w_v^d is dependent on the input. To provide a
265 provable dynamic weight design for multi-view concept-based models, we introduce generalization
266 theory. The generalization error of grading (classification) prediction in multi-view concept-based
267 models L_y can be expressed as:

$$268 \quad L_y := \mathbb{E}_{(\mathbf{x}^{(1:V)}, \mathbf{c}^{(1:V)}, \mathbf{y}) \sim \mathcal{D}} \left[\ell_y \left(\sum_{v=1}^V w_v G(\hat{\mathbf{c}}^{(v)}), \mathbf{y} \right) \right], \quad (11)$$

270 where \mathbb{E} is the expectation, \mathcal{D} is the unknown joint distribution, and ℓ_y represents the cross-entropy
 271 loss function with convexity. **Our objective is to search for dynamic w_v^d that minimizes the upper
 272 bound of L_y as much as possible, and to prove that it is always superior to the static fusion
 273 weight $w_v^s = 1/V$.**

274 **Theorem 1** (Generalization Bound of Decision Fusion in Multi-View Concept-based Models)

275 Given a training set $\mathcal{D}_{\text{train}} = \left\{ \left(\mathbf{x}_i^{(1:V)}, \mathbf{c}_i^{(1:V)}, \mathbf{y}_i \right) \right\}_{i=1}^N$, we derive the generalization error bound
 276 of Multi-View Concept-based Models using Rademacher complexity (Bartlett & Mendelson, 2002),
 277 and for $1 > \delta > 0$, with probability at least $1 - \delta$, it holds that

$$\begin{aligned}
 L_y \leq & \underbrace{\sum_{v=1}^V \mathbb{E}[w_v] \hat{L}_y^{(v)} + \sum_{v=1}^V \mathbb{E}[w_v] L_g^{(v)} \hat{L}_c^{(v)}}_{\text{Term-L (average empirical loss of prediction and concept)}} + \underbrace{\sum_{v=1}^V \mathbb{E}[w_v] \mathfrak{R}_N(\mathcal{G}) + \sum_{v=1}^V \mathbb{E}[w_v] L_g^{(v)} \mathfrak{R}_N(\mathcal{C})}_{\text{Term-C (average complexity of prediction and concept)}} \\
 & + \underbrace{\sum_{v=1}^V \text{Cov}(w_v, \ell_y(G(\mathbf{c}^{(v)}), \mathbf{y})) + \sum_{v=1}^V L_g^{(v)} \text{Cov}(w_v, \|\hat{\mathbf{c}}^{(v)} - \mathbf{c}^{(v)}\|_1)}_{\text{Term-Cov (covariance between fusion weights and losses)}} + 2P \underbrace{\sqrt{\frac{\ln(V/\delta)}{N}}}_{\text{concentration term}}, \quad (12)
 \end{aligned}$$

290 where $\hat{L}_y^{(v)}$ and $\hat{L}_c^{(v)}$ denote the empirical prediction error (evaluated under true concepts) and the
 291 empirical concept error, respectively, $\mathfrak{R}_N(\mathcal{G})$ and $\mathfrak{R}_N(\mathcal{C})$ denote the Rademacher complexities esti-
 292 mated with N samples, $L_g^{(v)} > 0$ is the Lipschitz constant of G with respect to its concept input (i.e.,
 293 the sensitivity bound of the prediction loss with respect to the concept), $\text{Cov}(\cdot, \cdot)$ denotes the covari-
 294 ance, and $P > 0$ is an absolute constant determined by the boundedness of the loss. In particular,
 295 when $w_v = w_v^s = 1/V$, the Term-Cov becomes 0.

296 First, since $\hat{L}_y^{(v)}$, $\hat{L}_c^{(v)}$, $L_g^{(v)}$, $\mathfrak{R}_N(\mathcal{G}_v)$, and $\mathfrak{R}_N(\mathcal{H}_v)$ are trained within the same loss function class
 297 and are independent of w_v , for $0 < \delta < 1$, with probability at least $1 - \delta$, to ensure that the
 298 generalization bound L_y under w_v^d is smaller than that under w_v^s , it is required that:

$$\underbrace{\mathbb{E}[w_v^d] \equiv w_v^s}_{\text{always holds}}, \quad \text{Cov}(w_v, \ell_y(G(\mathbf{c}^{(v)}), \mathbf{y})) \leq 0, \quad \text{Cov}(w_v, \|\hat{\mathbf{c}}^{(v)} - \mathbf{c}^{(v)}\|_1) \leq 0. \quad (13)$$

303 Although $\ell_y(G(\mathbf{c}^{(v)}), \mathbf{y})$ denotes the prediction loss obtained from the true concepts,
 304 $\ell_y(G(\mathbf{c}^{(v)}), \mathbf{y})$ and $\ell_y(G(\hat{\mathbf{c}}^{(v)}), \mathbf{y})$ are positively correlated, since a smaller deviation between $\hat{\mathbf{c}}^{(v)}$
 305 and $\mathbf{c}^{(v)}$ leads to closer prediction behavior of $G(\hat{\mathbf{c}}^{(v)})$ and $G(\mathbf{c}^{(v)})$, which in turn results in similar
 306 values of the two losses. In addition, the concept loss (L1loss) is required to be negatively correlated
 307 with w_v . Thus, we present the following corollary:

309 **Corollary 1** When fusion weight $w_v = w_v^d$ is negatively correlated with both the prediction loss and
 310 the concept loss of the view, the generalization bound of multi-view decision fusion can be reduced.

311 Inspired by (Zhang et al., 2023), the concept loss and grading prediction loss are observed to be pos-
 312 itively correlated with uncertainty, and together with Corollary 1, we propose the dual uncertainty-
 313 driven multi-view fusion decision.

315 2.3.2 DUAL UNCERTAINTY-AWARE MODULE

317 For each view, we quantify concept- and grading-level uncertainty under the evidential framework
 318 of Subjective Logic, which parameterizes belief masses via a Dirichlet distribution (Shafer, 1976;
 319 Han et al., 2022). For concept-level modeling, we treat each concept as a binary classification. The
 320 evidence vector $\mathbf{e}_{v,c_j} = [e_{v,c_j}^+, e_{v,c_j}^-] = \text{softplus}(\hat{\mathbf{c}}^{(v)})$ yields Dirichlet parameters $\alpha_{v,c_j}^+ = e_{v,c_j}^+ + 1$
 321 and $\alpha_{v,c_j}^- = e_{v,c_j}^- + 1$. The belief masses and uncertainty for concept j in view v are:

$$b_{v,c_j}^+ = \frac{\alpha_{v,c_j}^+ - 1}{S_{v,c_j}}, \quad b_{v,c_j}^- = \frac{\alpha_{v,c_j}^- - 1}{S_{v,c_j}}, \quad \psi_{v,c_j}^{\text{con}} = \frac{2}{S_{v,c_j}}, \quad (14)$$

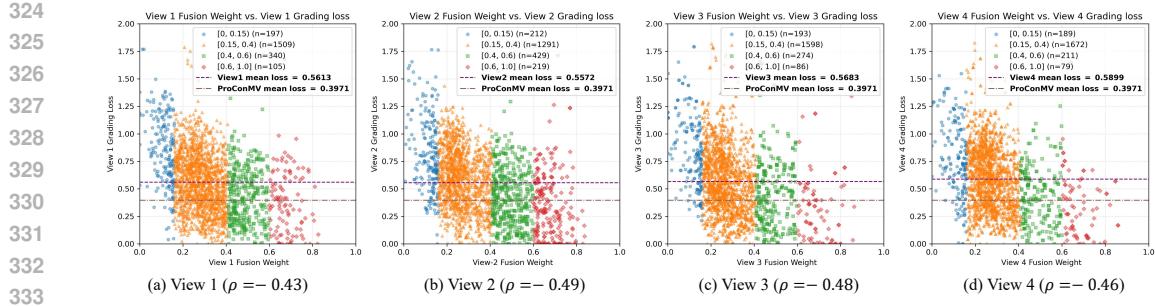


Figure 3: Scatter plots of per-view grading loss versus dual-uncertainty fusion weights on the MFIDDR test set, where ρ denotes their Pearson correlation coefficient (Benesty et al., 2009).

where $S_{v,cj} = \alpha_{v,cj}^+ + \alpha_{v,cj}^-$. The overall concept uncertainty for view v is averaged over all m concepts: $\Psi_v^{\text{con}} = \frac{1}{m} \sum_{j=1}^m \psi_{v,cj}^{\text{con}}$. For grading-level modeling with K classes, the evidence vector $\mathbf{e}_v^{\text{gr}} = [e_v^{(1)}, \dots, e_v^{(K)}] = \text{softplus}(\hat{\mathbf{y}}^{(v)})$ gives $\alpha_v^{(i)} = e_v^{(i)} + 1$. The belief mass for grade i and the grading uncertainty are:

$$b_v^{(i)} = \frac{\alpha_v^{(i)} - 1}{S_v^{\text{gr}}}, \quad \Psi_v^{\text{gr}} = \frac{K}{S_v^{\text{gr}}}, \quad (15)$$

with total strength $S_v^{\text{gr}} = \sum_{i=1}^K \alpha_v^{(i)}$, satisfying $\sum_{i=1}^K b_v^{(i)} + \Psi_v^{\text{gr}} = 1$.

2.3.3 MULTI-VIEW DECISION-MAKING UNDER DUAL UNCERTAINTIES

To construct a fully interpretable multi-view fundus decision model, our method exploits the uncertainties Ψ_v^{con} and Ψ_v^{gr} to assess view reliability, which in turn guides the dynamic fusion of outputs across views. In particular, the final grading decision $\hat{\mathbf{y}}$ is obtained by summing the view-specific outputs $\hat{\mathbf{y}}^{(v)}$, each weighted by a reliability score that combines concept- and grading-level certainties, $(1 - \Psi_v^{\text{con}})$ and $(1 - \Psi_v^{\text{gr}})$, with a learnable parameter $W_c = \frac{e^{-\eta}}{1+e^{-\eta}} > 0$ controlling their trade-off:

$$\hat{\mathbf{y}} = \sum_{i=1}^V [W_c(1 - \Psi_v^{\text{con}}) + (1 - W_c)(1 - \Psi_v^{\text{gr}})] \odot \hat{\mathbf{y}}^v. \quad (16)$$

This inverse dual-uncertainty design dynamically reduces the contribution of views with high uncertainty and low interpretability. As shown in Fig. 3, scatter plots and Pearson correlation coefficient ρ intuitively demonstrate the correlation between per-view grading loss and dual-uncertainty fusion weights. This indicates that dual uncertainty can reduce the interference of unreliable perspectives on the final diagnosis and provide interpretable evidence for multi-view diagnosis.

2.4 LOSS FUNCTION

The training objective combines concept-level supervision for each view and the overall grading supervision. Specifically, we minimize

$$\mathcal{L} = - \sum_{j=1}^n (1 - \hat{\mathbf{y}}_j)^\gamma \mathbf{y}_j \log \hat{\mathbf{y}}_j - \frac{\alpha}{V} \sum_{i=1}^V \sum_{j=1}^N \left[\mathbf{c}_j^{(v)} \log \hat{\mathbf{c}}_j^{(v)} + (1 - \mathbf{c}_j^{(v)}) \log (1 - \hat{\mathbf{c}}_j^{(v)}) \right]. \quad (17)$$

Here, the first term corresponds to the *Focal Loss* (with focusing parameter γ) for class-imbalanced DR grading, and the second term corresponds to the *Binary Cross-Entropy Loss* for concept prediction, with α balancing the two. By jointly optimizing both terms, the model is encouraged to learn faithful concept representations while simultaneously improving the final grading performance. Detailed hyperparameter experiments are presented in Fig. 8.

2.5 MULTI-VIEW TEST TIME INVENTION

Building upon our reasoning chain and dual-uncertainty decision paradigm, we propose a multi-view intervention mechanism that enables physicians to intervene on either a single view or a specific

378 Table 1: Comparison of Accuracy, Specificity, Kappa, and Macro F1-score on MFIDDR and DRTiD
 379 (Unit: %), and inference time (Unit: ms) for different models on DR grading. The best results are
 380 highlighted in bold, and “(MV)” means transforming into a multi-view method.

| 382 Method | 383 Venue | 384 Backbone | MFIDDR (four views) | | | | DRTiD (two views) | | | | 385 Infer. 386 Time ↓ |
|---|-----------|---------------------|---------------------|--------------|--------------|--------------|-------------------|--------------|--------------|--------------|--------------------------|
| | | | 387 Acc.↑ | 388 Spe.↑ | 389 Kap.↑ | 390 F1↑ | 391 Acc.↑ | 392 Spe.↑ | 393 Kap.↑ | 394 F1↑ | |
| 395 Non-interpretable Multi-View DR Diagnosis Methods | | | | | | | | | | | |
| CrossFit | BIBM’22 | Resnet-50 | – | – | – | – | 72.73 | 86.63 | 57.60 | 70.53 | – |
| ETMC | TPAMI’22 | Resnet-50 | 81.54 | 83.44 | 64.76 | 79.74 | 65.48 | 78.14 | 44.79 | 61.35 | 6.61 |
| MVCINN | AAAI’23 | Resnet-50+ViT | 80.10 | 83.32 | 62.45 | 78.86 | 68.18 | 85.78 | 51.39 | 66.83 | 31.31 |
| CVSRA-ViT | PR’25 | VGG+ViT | 82.61 | 86.77 | 68.57 | 81.94 | 70.62 | 88.91 | 55.74 | 69.97 | 71.53 |
| SMVDR | AAAI’25 | Mamba | 84.01 | 91.30 | 71.36 | 83.69 | 74.52 | 92.29 | 61.38 | 72.86 | 65.71 |
| WMIMVDR | ICME’25 | Resnet-50+ViT | 84.15 | 89.95 | 71.16 | 83.59 | 73.23 | 90.58 | 58.87 | 70.62 | 25.44 |
| 396 Interpretable Multi-View DR Diagnosis Methods | | | | | | | | | | | |
| Multi-Task | TKDE’21 | Resnet-50 | 83.73 | 89.06 | 70.24 | 83.12 | 72.79 | 89.32 | 56.98 | 70.12 | 8.24 |
| MVCBM | ICML’22 | Resnet-50 | 83.22 | 88.22 | 69.12 | 82.43 | 71.54 | 85.02 | 57.89 | 68.50 | 19.67 |
| CEM (MV) | NIPS’22 | Resnet-50 | 84.12 | 88.77 | 70.83 | 83.45 | 74.55 | 91.67 | 61.42 | 72.06 | 21.25 |
| PCBM (MV) | ICML’23 | Resnet-50 | 83.52 | 91.19 | 70.35 | 83.29 | 74.73 | 90.26 | 60.68 | 71.99 | 17.56 |
| SSMVCBM | MIA’24 | Resnet-50 | 82.75 | 85.81 | 67.55 | 81.51 | 73.98 | 91.74 | 60.01 | 70.81 | 20.71 |
| CLAT (MV) | TMI’25 | ViT | 82.89 | 86.66 | 68.16 | 81.88 | 74.55 | 91.33 | 61.03 | 72.77 | 33.02 |
| ProConMV (Ours) | – | Hilbert-RWKV | 86.75 | 92.79 | 76.05 | 86.35 | 76.77 | 93.77 | 64.47 | 74.64 | 8.77 |

397 concept. Our method not only retains the ability of single-view CBMs to intervene on concepts to
 398 influence single-view decisions, but also leverages dual uncertainties at both the concept and grading
 399 levels to increase the contribution of the corresponding view to the overall decision. Specifically,
 400 taking view i as an example, if an ophthalmologist corrects the result $\hat{\mathbf{c}}^{(v)}$ of lesion concepts in this
 401 view, the DR grading can first be re-inferred and updated as $\hat{\mathbf{y}}^{(v)}$, after which the dual uncertainties
 402 of the view are updated accordingly, thereby influencing the fused diagnostic outcome $\hat{\mathbf{y}}'$.
 403

404 Table 2: Comparison of AUPR, AUC, Accuracy, Macro F1-score, Ranking Loss, and Hamming
 405 Loss on MFIDDR and DRTiD for different models on lesion concept classification. The best results
 406 are highlighted in bold, and “(MV)” means transforming into a multi-view method. (Unit: %)

| 408 Method | MFIDDR | | | | | DRTiD | | | | | 410 |
|-----------------|--------------|--------------|--------------|-------------|-------------|--------------|--------------|--------------|-------------|-------------|-----|
| | 411 AUPR↑ | 412 ACC↑ | 413 F1↑ | 414 RL↓ | 415 HL↓ | 416 AUPR↑ | 417 ACC↑ | 418 F1↑ | 419 RL↓ | 420 HL↓ | |
| Multi-Task | 54.69 | 93.87 | 51.69 | 3.73 | 5.54 | 47.32 | 87.31 | 43.90 | 7.88 | 12.69 | |
| MVCBM | 61.56 | 94.22 | 59.10 | 3.21 | 5.36 | 48.50 | 88.82 | 41.88 | 5.56 | 11.18 | |
| CEM (MV) | 65.47 | 94.74 | 60.42 | 2.86 | 5.21 | 48.50 | 89.95 | 44.63 | 6.12 | 11.05 | |
| PCBM (MV) | 68.12 | 94.85 | 66.08 | 1.91 | 4.96 | 52.59 | 90.46 | 47.24 | 4.52 | 9.54 | |
| SSMVCBM | 66.25 | 94.42 | 63.34 | 2.17 | 5.02 | 53.52 | 90.35 | 47.15 | 4.25 | 9.65 | |
| CLAT (MV) | 63.89 | 94.63 | 59.15 | 2.98 | 5.45 | 51.83 | 89.97 | 46.82 | 4.71 | 10.02 | |
| ProConMV (Ours) | 72.26 | 95.42 | 68.43 | 1.45 | 4.47 | 55.86 | 90.83 | 48.00 | 3.42 | 9.17 | |

421 3 EXPERIMENTS

422 3.1 EXPERIMENTAL SETTINGS

423 **Datasets.** We evaluate our method on the two publicly available multi-view DR grading datasets,
 424 MFIDDR (Luo et al., 2023) and DRTiD (Hou et al., 2022). MFIDDR contains 34,452 images from
 425 4,344 patients, annotated with five DR grades across four standard views (macula-centered,
 426 optic disc-centered, and superior/inferior tangent to the optic disc). DRTiD consists of 3,100 paired
 427 macula- and optic disc-centered images from 1,550 eyes. To enable concept-based reasoning, oph-
 428 thalmologists annotate six lesion concepts in the fundus images of each dataset, which serve as con-
 429 cept prediction labels: hard exudates (EX), hemorrhages (HE), microaneurysms (MA), soft exudates
 430 (SE), vitreous hemorrhage (VH), and vitreous opacity (VO). For fair comparison, we follow the of-
 431 ficial data split protocols provided by each dataset, respectively. Detailed statistics of the dataset
 432 distributions are summarized in Section A.3. [And lesion masks are generated by the HACDR-Net](#)
 433 ([Xu et al., 2024](#)) pre-trained on DDR [Li et al. \(2019\)](#) dataset.

432 **Evaluation Metric and Compared Methods.** In this section, we evaluate multi-view DR diagnosis
 433 on two tasks: multi-view DR grading and lesion concept classification. Grading is assessed using
 434 accuracy (Acc.), precision (Prec.), sensitivity (Sens.), specificity (Spe.), kappa, macro-F1, and AUC
 435 (Trevethan, 2017), while the lesion concept classification uses AUPR, AUC, Acc., macro-F1, ranking
 436 loss (RL), and Hamming loss (HL). We also report inference time. Baselines are divided into
 437 two categories: (i) non-interpretable multi-view DR diagnosis methods, including CrossFit (Hou
 438 et al., 2022), ETMC (Han et al., 2022), MVCINN (Luo et al., 2023), Retfound (Zhou et al., 2023),
 439 CVSRA-ViT (Lin et al., 2025), SMVDR (Luo et al., 2025), and WMIMVDR (Hu et al., 2025), and
 440 (ii) interpretable multi-view DR diagnosis methods, including Multi-Task (Zhang & Yang, 2022),
 441 MVCBM (Klimiene et al., 2022), CEM (Espinosa Zarlenga et al., 2022), PCBh (Yuksekgonul
 442 et al., 2023), SSMVCBM (Marcinkevič et al., 2024), and CLAT (Wen et al., 2024).

443 **Implementation Details.** All experiments are implemented with PyTorch and conducted on an
 444 NVIDIA RTX 4090 GPU. We resize the images and labels to a resolution of 256×256 . The batch
 445 size and number of epochs are set to 8 and 100, respectively. The Adam optimizer is used with an
 446 initial learning rate of 10^{-5} , which is dynamically adjusted by a cosine annealing scheduler. We
 447 select the model achieving the best grading performance on the validation set as the final model,
 448 which is then used for subsequent testing and analysis.

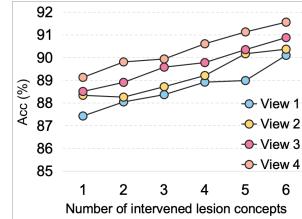
449 3.2 EXPERIMENTAL ANALYSIS

450 **Comparison with Advanced Methods.** We compare our method with 12 state-of-the-art multi-
 451 view methods on two datasets. As shown in Table 1, our ProConMV achieves the best performance
 452 in multi-view DR grading on both datasets. Specifically, ProConMV improves accuracy by 2.6% on
 453 the four-view dataset and by 2.04% on the two-view dataset, with the highest Kappa improvement
 454 of 4.69 on MFIDDR. As presented in Table 2, our method also achieves the best results in lesion
 455 concept classification on both datasets. The AUPR is improved by 4.14% and 2.34% on MFIDDR
 456 and DRTiD, respectively, while RL and HL are significantly reduced. Benefiting from the linear
 457 complexity of Hilbert-RWKV, our method also ranks among the top in single-image inference time.
 458 Overall, our method achieves the highest accuracy in both grading and concept prediction for the
 459 diagnostic task, while also delivering superior inference efficiency compared to most existing inter-
 460 pretable and non-interpretable multi-view diagnostic methods.

461 **Analysis of Test-time Intervention Capability.** As a concept-based
 462 model, our approach enables interventions from both the view and
 463 lesion perspectives. Specifically, ophthalmologists can revise the
 464 diagnosis of a particular view, a specific lesion type, or the same le-
 465 sion type across multiple views, and such interventions directly re-
 466 fine the final DR grading outcome. As shown in Fig. 4, the overall
 467 grading accuracy increases proportionally with the number of inter-
 468 viewed views and lesion concepts. When all erroneous concepts are
 469 corrected, the grading accuracy reaches 91.56%, yielding a 4.81%
 470 improvement over the non-intervention setting. This verifies the ef-
 471 ffectiveness of the proposed intervention method.

472 3.3 ABLATION STUDY

473 **Ablation Results of Hilbert-RWKV.** We first compare Hilbert-RWKV with existing state-of-the-
 474 art backbones, as shown in Table 4. Compared to ResNet-50 (He et al., 2016), ViT-Big (Dosovitskiy
 475 et al., 2021), VMamba-Tiny (Liu et al., 2024b), Swin v1-S Liu et al. (2021) and Swin v2-S Liu
 476 et al. (2022b), our method achieves consistent improvements in DR grading and lesion classifica-
 477 tion with lower parameter counts and shorter inference times. For example, our method surpasses
 478 ResNet-50 by 1.03% Acc. and 2.27% F1 in DR grading, and by 2.80% AUPR and 2.80% F1 in
 479 lesion classification, while requiring significantly fewer parameters (6.70M vs. 25.26M) and less
 480 inference time (8.77ms vs. 10.16ms). Subsequently, as presented in Table 5, we evaluate different
 481 scanning strategies for the RWKV architecture. Compared with Hilbert scanning, sweep, zigzag,
 482 and unidirectional scanning lead to drops of 0.78% and 2.18% in F1 scores for DR grading and
 483 lesion classification, respectively. These results substantiate the superiority of the Hilbert-RWKV
 484 design in both DR diagnostic reasoning and computational efficiency.



475 Figure 4: Performance eval-
 476 uation of the multi-view
 477 test-time intervention.

486
487
488
489 Table 3: Ablation studies of key modules on MFIDDR. ‘ \times ’ and ‘ \checkmark ’ denote the absence and presence
490 of each module. The first row corresponds to the baseline, MVCBM. (Unit: %)

| 491 | 492 | 493 | 494 | 495 | 496 | 497 | Mask | Text | Hilbert-RWKV | VT-RWKV | DU-MVFD | Grading Acc | Grading Kappa | Concept Pred. AUPR | Concept Pred. F1 |
|-----|-----|-----|-----|-----|-----|-----|--------------|--------------|--------------|--------------|--------------|-------------|---------------|--------------------|------------------|
| | | | | | | | \checkmark | \checkmark | \times | \times | \times | 83.22 | 69.12 | 61.56 | 59.10 |
| | | | | | | | \checkmark | \checkmark | \checkmark | \times | \times | 85.72 | 74.31 | 62.90 | 63.87 |
| | | | | | | | \checkmark | \checkmark | \times | \checkmark | \times | 85.45 | 74.29 | 64.72 | 62.61 |
| | | | | | | | \checkmark | \checkmark | \times | \times | \checkmark | 84.15 | 71.57 | 60.87 | 58.92 |
| | | | | | | | \checkmark | \checkmark | \checkmark | \checkmark | \times | 86.23 | 75.23 | 70.69 | 67.89 |
| | | | | | | | \checkmark | \checkmark | \checkmark | \times | \checkmark | 85.68 | 74.43 | 70.12 | 64.39 |
| | | | | | | | \checkmark | \checkmark | \times | \checkmark | \checkmark | 85.12 | 72.68 | 67.71 | 66.12 |
| | | | | | | | \checkmark | \times | \checkmark | \checkmark | \checkmark | 85.68 | 74.43 | 70.12 | 64.39 |
| | | | | | | | \times | \checkmark | \checkmark | \checkmark | \checkmark | 85.21 | 73.98 | 68.59 | 66.26 |
| | | | | | | | \checkmark | \checkmark | \checkmark | \checkmark | \checkmark | 86.75 | 76.05 | 72.26 | 68.43 |

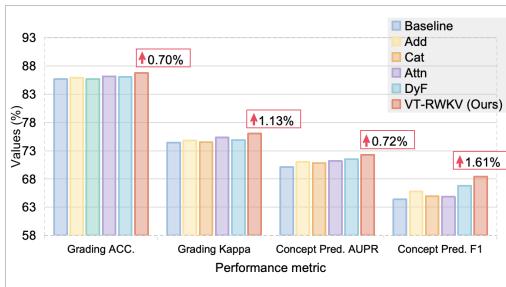
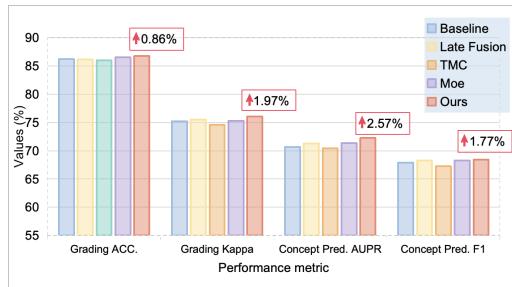
498
499 Table 4: Comparison of backbones. (Unit: %)

| 501 Backbone | Grading Acc. | Grading F1 | Concept Pred. AUPR | Concept Pred. F1 | Params (M) | Infer. (ms) |
|--------------|--------------|--------------|--------------------|------------------|-------------|-------------|
| VGG-16 | 85.63 | 85.26 | 67.69 | 66.88 | 15.29 | 6.93 |
| ResNet-50 | 85.72 | 84.08 | 67.71 | 66.12 | 25.26 | 10.16 |
| ViT-B | 85.82 | 85.44 | 55.01 | 52.81 | 86.61 | 12.09 |
| Swin v1-S | 86.09 | 86.03 | 66.65 | 60.09 | 49.56 | 18.65 |
| Swin v2-S | 86.33 | 85.76 | 61.47 | 57.52 | 37.93 | 26.95 |
| VMamba | 83.03 | 82.29 | 59.43 | 52.15 | 14.60 | 9.27 |
| Ours | 86.75 | 86.35 | 72.26 | 68.92 | 6.70 | 8.77 |

500
501 Table 5: Comparison of scanning strategies on MFIDDR. (Unit: %)

| 502 Strategy | Grading Acc. | Grading F1 | Concept Pred. F1 | Concept Pred. AUPR |
|--------------|--------------|--------------|------------------|--------------------|
| Sweep | 86.29 | 85.94 | 65.24 | 69.61 |
| Horizontal | 86.24 | 86.05 | 64.93 | 70.97 |
| Vertical | 86.10 | 85.96 | 64.75 | 70.46 |
| Zigzag | 86.24 | 85.70 | 63.89 | 67.60 |
| Ours | 86.75 | 86.35 | 68.92 | 72.26 |

502
503
504
505
506
507
508 **Ablation Results of VT-RWKV and multi-view fusion method.** As shown in Fig. 5(a), we compare different interaction strategies for VT-RWKV, where Cat denotes channel-wise fusion, Attn applies cross-attention, and DyF (Xue & Marculescu, 2023) uses dynamic multimodal fusion. VT-RWKV consistently outperforms these designs, achieving improvements of +0.70% ACC, +1.13% Kappa, +0.72% AUPR, and +1.61% F1, confirming the superiority of our image-text concept interaction. For multi-view fusion (Fig. 5(b)), our dual-uncertainty module achieves the best performance, outperforming Baseline (Concat), Late Fusion (Average add), TMC, and Moe (Cao et al., 2023) with gains of +0.86% Acc, +1.97% Kappa, +2.57% AUPR, and +1.77% F1. This demonstrates the effectiveness of uncertainty modeling for multi-view decision fusion.

527
528 (a) Comparison of experimental results of different
529 image-text concept interaction methods.530
531 (b) Comparison of experimental results of different
532 ways of multi-view fusion decision.

533 Figure 5: Ablation studies on VT-RWKV and DU-MVFD on the MFIDDR dataset.

534
535

4 CONCLUSION

536 This paper proposes a full-process interpretable model, ProConMV. It achieves deep extraction and
537 fusion of multi-source features, introduces lesion concepts to construct a causal reasoning chain,
538 and incorporates real-time physician intervention. Moreover, the proposed multi-view decision-
539 making approach theoretically reduces generalization error and achieves traceability through a dual
540 uncertainty module. The evaluation results show that it achieves state-of-the-art performance and
541 high clinical credibility in DR grading. Future research will focus on weakly-supervised learning
542 with sparse data and conduct large-scale studies involving physician users.

540 REFERENCES
541

542 Josh Achiam, Steven Adler, Sandhini Agarwal, Lama Ahmad, Ilge Akkaya, Florencia Leoni Ale-
543 man, Diogo Almeida, Janko Altenschmidt, Sam Altman, Shyamal Anadkat, et al. Gpt-4 technical
544 report. *arXiv preprint arXiv:2303.08774*, 2023.

545 Peter L Bartlett and Shahar Mendelson. Rademacher and gaussian complexities: Risk bounds and
546 structural results. *Journal of machine learning research*, 3(Nov):463–482, 2002.

547

548 Jacob Benesty, Jingdong Chen, Yiteng Huang, and Israel Cohen. Pearson correlation coefficient. In
549 *Noise reduction in speech processing*, pp. 1–4. Springer, 2009.

550

551 Bing Cao, Yiming Sun, Pengfei Zhu, and Qinghua Hu. Multi-modal gated mixture of local-to-global
552 experts for dynamic image fusion. In *ICCV*, pp. 23555–23564, 2023.

553

554 Aditya Chattpadhyay, Anirban Sarkar, Prantik Howlader, and Vineeth N Balasubramanian. Grad-
555 cam++: Generalized gradient-based visual explanations for deep convolutional networks. In
556 *WACV*, pp. 839–847. IEEE, 2018.

557

558 Hugh Chen, Scott M Lundberg, and Su-In Lee. Explaining a series of models by propagating shapley
559 values. *Nature communications*, 13(1):4512, 2022.

560

561 Wanli Chen, Xufeng Yao, Xinyun Zhang, and Bei Yu. Efficient deep space filling curve. In *ICCV*,
562 pp. 17525–17534, 2023.

563

564 Gabriele Ciravegna, Pietro Barbiero, Francesco Giannini, Marco Gori, Pietro Lió, Marco Maggini,
565 and Stefano Melacci. Logic explained networks. *Artificial Intelligence*, pp. 103822, 2022.

566

567 Etienne Decenciere, Xiwei Zhang, Guy Cazuguel, Bruno Lay, Beatrice Cochener, Caroline Trone,
568 Philippe Gain, Richard Ordonez, Pascale Massin, Ali Erginay, Beatrice Charton, and Jean-Claude
569 Klein. Feedback on a publicly distributed database: the messidor database. *Image Analysis
570 Stereology*, 33(3):231–234, 2014.

571

572 Alexey Dosovitskiy, Lucas Beyer, Alexander Kolesnikov, Dirk Weissenborn, Xiaohua Zhai, Thomas
573 Unterthiner, Mostafa Dehghani, Matthias Minderer, Georg Heigold, Sylvain Gelly, Jakob Uszkoreit,
574 and Neil Houlsby. An image is worth 16x16 words: Transformers for image recognition at
575 scale. In *ICLR*, 2021.

576

577 Yuchen Duan, Weiyun Wang, Zhe Chen, Xizhou Zhu, Lewei Lu, Tong Lu, Yu Qiao, Hongsheng
578 Li, Jifeng Dai, and Wenhui Wang. Vision-RWKV: Efficient and scalable visual perception with
579 RWKV-like architectures. In *ICLR*, 2025.

580

581 Mateo Espinosa Zarlenga, Pietro Barbiero, Gabriele Ciravegna, Giuseppe Marra, Francesco Gian-
582 nini, Michelangelo Diligenti, Zohreh Shams, Frederic Precioso, Stefano Melacci, Adrian Weller,
583 et al. Concept embedding models: Beyond the accuracy-explainability trade-off. *NeurIPS*, 35:
584 21400–21413, 2022.

585

586 EyePACS. Kaggle-eyepacs. [https://www.kaggle.com/c/
587 diabetic-retinopathy-detection/data](https://www.kaggle.com/c/diabetic-retinopathy-detection/data), 2015. Accessed: 2025-09-28.

588

589 International Diabetes Federation. Idf diabetes atlas, 10th edn. [https://www.
590 diabetesatlas.org](https://www.diabetesatlas.org), 2021. Accessed: 2025-09-27.

591

592 Tiancheng Gu, Kaicheng Yang, Xiang An, Ziyong Feng, Dongnan Liu, Weidong Cai, and Jiankang
593 Deng. Rwkv-clip: A robust vision-language representation learner. In *EMNLP*, 2024.

594

595 Zongbo Han, Changqing Zhang, Huazhu Fu, and Joey Tianyi Zhou. Trusted multi-view classi-
596 fication with dynamic evidential fusion. *IEEE transactions on pattern analysis and machine
597 intelligence*, 45(2):2551–2566, 2022.

598

599 Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recog-
600 nition. In *CVPR*, pp. 770–778, 2016.

594 Qingdong He, Jiangning Zhang, Jinlong Peng, Haoyang He, Xiangtai Li, Yabiao Wang, and
 595 Chengjie Wang. Pointrwkv: Efficient rwkv-like model for hierarchical point cloud learning. In
 596 *AAAI*, volume 39, pp. 3410–3418, 2025.

597 Junlin Hou, Jian Xu, Fan Xiao, Rui-Wei Zhao, Yuejie Zhang, Haidong Zou, Lina Lu, Wenwen
 598 Xue, and Rui Feng. Cross-field transformer for diabetic retinopathy grading on two-field fundus
 599 images. In *BIBM*, pp. 985–990, 2022.

600 Yongting Hu, Yuxin Lin, Chengliang Liu, Xiaoling Luo, Xiaoyan Dou, Qihao Xu, and Yong
 601 Xu. Wavelet-based global-local interaction network with cross-attention for multi-view diabetic
 602 retinopathy detection. *arXiv preprint arXiv:2503.19329*, 2025.

603 Yijin Huang, Junyan Lyu, Pujin Cheng, Roger Tam, and Xiaoying Tang. Ssit: Saliency-guided self-
 604 supervised image transformer for diabetic retinopathy grading. *IEEE Journal of Biomedical and*
 605 *Health Informatics*, 28(5):2806–2817, 2024.

606 Ugne Klimiene, Ričards Marcinkevičs, Patricia Reis Wolfertstetter, Ece Ozkan, Alyssia Paschke,
 607 David Niederberger, Sven Wellmann, Christian Knorr, and Julia E Vogt. Multiview concept bot-
 608 tleneck models applied to diagnosing pediatric appendicitis. In *ICML*, 2022.

609 Pang Wei Koh, Thao Nguyen, Yew Siang Tang, Stephen Mussmann, Emma Pierson, Been Kim, and
 610 Percy Liang. Concept bottleneck models. In *ICML*, pp. 5338–5348. PMLR, 2020.

611 Tao Li, Yingqi Gao, Kai Wang, Song Guo, Hanruo Liu, and Hong Kang. Diagnostic assessment of
 612 deep learning algorithms for diabetic retinopathy screening. *Information Sciences*, 501:511–522,
 613 2019.

614 Yuxin Lin, Xiaoyan Dou, Xiaoling Luo, Zhihao Wu, Chengliang Liu, Tianyi Luo, Jie Wen, Bingo
 615 Wing-kuen Ling, Yong Xu, and Wei Wang. Multi-view diabetic retinopathy grading via cross-
 616 view spatial alignment and adaptive vessel reinforcing. *Pattern Recognition*, 164:111487, 2025.

617 Chengliang Liu, Zhihao Wu, Jie Wen, Yong Xu, and Chao Huang. Localized sparse incomplete
 618 multi-view clustering. *IEEE Transactions on Multimedia*, 25:5539–5551, 2022a.

619 Chengliang Liu, Jie Wen, Yabo Liu, Chao Huang, Zhihao Wu, Xiaoling Luo, and Yong Xu.
 620 Masked two-channel decoupling framework for incomplete multi-view weak multi-label learn-
 621 ing. *NeurIPS*, 36, 2024a.

622 Yue Liu, Yunjie Tian, Yuzhong Zhao, Hongtian Yu, Lingxi Xie, Yaowei Wang, Qixiang Ye, Jianbin
 623 Jiao, and Yunfan Liu. Vmamba: Visual state space model. *NeurIPS*, 37:103031–103063, 2024b.

624 Ze Liu, Yutong Lin, Yue Cao, Han Hu, Yixuan Wei, Zheng Zhang, Stephen Lin, and Baining Guo.
 625 Swin transformer: Hierarchical vision transformer using shifted windows. In *CVPR*, pp. 10012–
 626 10022, 2021.

627 Ze Liu, Han Hu, Yutong Lin, Zhuliang Yao, Zhenda Xie, Yixuan Wei, Jia Ning, Yue Cao, Zheng
 628 Zhang, Li Dong, et al. Swin transformer v2: Scaling up capacity and resolution. In *CVPR*, pp.
 629 12009–12019, 2022b.

630 Xiaoling Luo, Chengliang Liu, Waikeung Wong, Jie Wen, Xiaopeng Jin, and Yong Xu. Mvcinn:
 631 multi-view diabetic retinopathy detection using a deep cross-interaction neural network. In *AAAI*,
 632 volume 37, pp. 8993–9001, 2023.

633 Xiaoling Luo, Qihao Xu, Zhihua Wang, Chao Huang, Chengliang Liu, Xiaopeng Jin, and Jianguo
 634 Zhang. A lesion-fusion neural network for multi-view diabetic retinopathy grading. *IEEE Journal*
 635 *of Biomedical and Health Informatics*, 2024.

636 Xiaoling Luo, Qihao Xu, Huisi Wu, Chengliang Liu, Zhihui Lai, and Linlin Shen. Like an oph-
 637 thalmologist: Dynamic selection driven multi-view learning for diabetic retinopathy grading. In
 638 *AAAI*, volume 39, pp. 19224–19232, 2025.

639 Ričards Marcinkevičs, Patricia Reis Wolfertstetter, Ugne Klimiene, Kieran Chin-Cheong, Alyssia
 640 Paschke, Julia Zerres, Markus Denzinger, David Niederberger, Sven Wellmann, Ece Ozkan, et al.
 641 Interpretable and intervenable ultrasonography-based machine learning models for pediatric ap-
 642 pendicitis. *Medical image analysis*, 91:103042, 2024.

648 Bo Peng, Eric Alcaide, Quentin Anthony, Alon Albalak, Samuel Arcadinho, Stella Biderman,
 649 Huanqi Cao, Xin Cheng, Michael Chung, Matteo Grella, et al. Rwkv: Reinventing rnns for
 650 the transformer era. *arXiv preprint arXiv:2305.13048*, 2023.

651

652 Alvin E Roth. *The Shapley value: essays in honor of Lloyd S. Shapley*. Cambridge University Press,
 653 1988.

654

655 Ramprasaath R Selvaraju, Michael Cogswell, Abhishek Das, Ramakrishna Vedantam, Devi Parikh,
 656 and Dhruv Batra. Grad-cam: Visual explanations from deep networks via gradient-based local-
 657 ization. In *ICCV*, pp. 618–626, 2017.

658

659 Sangwoo Seo, Sungwon Kim, and Chanyoung Park. Interpretable prototype-based graph informa-
 660 tion bottleneck. *NeurIPS*, 36:76737–76748, 2023.

661

662 Glenn Shafer. *A Mathematical Theory of Evidence*. Princeton University Press, 1976.

663

664 Fahad Shamshad, Salman Khan, Syed Waqas Zamir, Muhammad Haris Khan, Munawar Hayat,
 665 Fahad Shahbaz Khan, and Huazhu Fu. Transformers in medical imaging: A survey. *Medical*
 666 *image analysis*, 88:102802, 2023.

667

668 Chung-En Sun, Tuomas Oikarinen, Berk Ustun, and Tsui-Wei Weng. Concept bottleneck large
 669 language models. In *ICLR*, 2025.

670

671 R. Trevethan. Sensitivity, specificity, and predictive values: Foundations, pliabilities, and pitfalls in
 672 research and practice. *Frontiers in Public Health*, 5:307, 2017.

673

674 Chi Wen, Mang Ye, He Li, Ting Chen, and Xuan Xiao. Concept-based lesion aware transformer for
 675 interpretable retinal disease diagnosis. *IEEE Transactions on Medical Imaging*, 2024.

676

677 Charles P Wilkinson, Frederick L Ferris III, Ronald E Klein, Paul P Lee, Carl David Agardh,
 678 Matthew Davis, Diana Dills, Anselm Kampik, R Pararajasegaram, Juan T Verdague, et al.
 679 Proposed international clinical diabetic retinopathy and diabetic macular edema disease sever-
 680 ity scales. *Ophthalmology*, 110(9):1677–1682, 2003.

681

682 QiHao Xu, Xiaoling Luo, Chao Huang, Chengliang Liu, Jie Wen, Jialei Wang, and Yong Xu. Hacdr-
 683 net: Heterogeneous-aware convolutional network for diabetic retinopathy multi-lesion segmenta-
 684 tion. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 38, pp. 6342–6350,
 685 2024.

686

687 Yufei Xu, Qiming Zhang, Jing Zhang, and Dacheng Tao. Vitae: Vision transformer advanced by
 688 exploring intrinsic inductive bias. *Neruips*, 34:28522–28535, 2021.

689

690 Zihui Xue and Radu Marculescu. Dynamic multimodal fusion. In *CVPR*, pp. 2575–2584, 2023.

691

692 Haobo Yuan, Xiangtai Li, Lu Qi, Tao Zhang, Ming-Hsuan Yang, Shuicheng Yan, and Chen Change
 693 Loy. Mamba or rwmk: Exploring high-quality and high-efficiency segment anything model. *arXiv*
 694 *preprint arXiv:2406.19369*, 2024.

695

696 Mert Yuksekgonul, Maggie Wang, and James Zou. Post-hoc concept bottleneck models. In *ICLR*,
 697 2023.

698

699 Qingyang Zhang, Haitao Wu, Changqing Zhang, Qinghua Hu, Huazhu Fu, Joey Tianyi Zhou, and
 700 Xi Peng. Provable dynamic fusion for low-quality multimodal data. In *ICML*, pp. 41753–41769.
 701 PMLR, 2023.

702

703 Rui Zhang, Xingbo Du, Junchi Yan, and Shihua Zhang. The decoupling concept bottleneck model.
 704 *IEEE Transactions on Pattern Analysis and Machine Intelligence*, pp. 1–13, 2024.

705

706 Yu Zhang and Qiang Yang. A survey on multi-task learning. *IEEE Transactions on Knowledge and*
 707 *Data Engineering*, 34(12):5586–5609, 2022.

708

709 Yukun Zhou, Mark A Chia, Siegfried K Wagner, Murat S Ayhan, Dominic J Williamson, Robbert R
 710 Struyven, Timing Liu, Moucheng Xu, Mateo G Lozano, Peter Woodward-Court, et al. A founda-
 711 tion model for generalizable disease detection from retinal images. *Nature*, 622(7981):156–163,
 712 2023.

702 **A APPENDIX**703 **A.1 RELATED WORK**704 **A.1.1 DNN-BASED METHODS FOR MULTI-VIEW DIABETIC RETINOPATHY DIAGNOSIS**

705 Recently, multi-view approaches for DR diagnosis have attracted increasing attention. Luo et al.
 706 (Luo et al., 2023) first proposed MVCINN, a multi-view DR diagnosis network that integrates CNNs
 707 and Transformers. Subsequently, several works (Luo et al., 2024; Lin et al., 2025; Hu et al., 2025)
 708 have leveraged visual cues, such as vessel and DR lesion masks derived from segmentation models,
 709 to improve diagnostic accuracy. Others (Hou et al., 2022; Luo et al., 2025) focused on inter-view
 710 information exchange and backbone design to further strengthen diagnostic representations. Never-
 711 theless, interpretability for this task has not been adequately explored, particularly in terms of textual
 712 explanations and transparent diagnostic workflows, which are of great significance in clinical medi-
 713 cal diagnosis.

714 **A.1.2 INTERPRETABLE MACHINE LEARNING MODELS IN COMPUTER VISION**

715 Interpretability methods have achieved remarkable success in computer vision, which enhances hu-
 716 man understanding of model predictions. Early studies on interpretability mainly focused on post-
 717 hoc explanations of black-box models, such as Shapley (Roth, 1988; Chen et al., 2022), Grad-CAM
 718 (Selvaraju et al., 2017; Chattopadhyay et al., 2018), and Prototypes (Seo et al., 2023). However, these
 719 methods lack human-comprehensible reasoning processes and are therefore fundamentally unable
 720 to provide reasonable explanations for downstream vision applications. To this end, Koh et al. (Koh
 721 et al., 2020) proposed the Concept Bottleneck Model (CBM), an interpretable framework that first
 722 predicts visual concepts and then uses them to generate the final prediction. There is a diverse set
 723 of CBM variants (Espinosa Zarlenga et al., 2022; Zhang et al., 2024; Wen et al., 2024; Ciravegna
 724 et al., 2022; Sun et al., 2025), each tackling the problem from a different perspective. To the best of
 725 our knowledge, SSMVCBM (Marcinkevičs et al., 2024) is the only work on interpretable multi-view
 726 classification. In contrast to prior concept-based studies, grounded in the perspective of interpretable
 727 multi-view vision task, our work 1) introduces a multimodal RWKV module to enhance concept rep-
 728 resentations, and 2) proposes a dual-uncertainty-aware fusion strategy that explicitly accounts for
 729 both concept and outcome uncertainties in multi-view decision-making.

730 **A.1.3 RECEPTANCE WEIGHTED KEY VALUE**

731 Receptance Weighted Key Value (RWKV) (Peng et al., 2023) is a neural network architecture that
 732 combines the parallel training ability of Transformers with the efficient recurrence of RNNs, char-
 733 acterized by its linear complexity and effectiveness in modeling long sequences. Recently, RWKV
 734 has gained renewed attention in vision tasks, as its core WKV attention mechanism has demon-
 735 strated superior performance compared to self-attention (Dosovitskiy et al., 2021) in some vision
 736 domains. Duan et al. proposed Vision-RWKV (Duan et al., 2025), first introducing a bidirectional
 737 WKV attention mechanism and a quad-directional token shift method to adapt RWKV for image
 738 classification tasks. Building upon RWKV and Vision-RWKV, a series of variants have been intro-
 739 duced for diverse vision-related tasks, including RWKV-SAM (Yuan et al., 2024) for segmentation,
 740 RWKV-CLIP (Gu et al., 2024) for vision-language representation learning, and Point-RWKV (He
 741 et al., 2025) for 3D point cloud learning. However, these works overlook the problem of spatial
 742 locality loss introduced by token serialization in image modeling.

743 **A.2 PROOF OF THEOREM 1**

744 According to the definitions and settings mentioned above, based on the convexity of the prediction
 745 loss $\ell_y^{(v)}(\cdot, \cdot)$ and the normalization property of w_v , we can derive:

$$\ell_y \left(\sum_{v=1}^V w_v G(\hat{\mathbf{c}}^{(v)}), \mathbf{y} \right) \leq \sum_{v=1}^V w_v \ell_y(G(\hat{\mathbf{c}}^{(v)}), \mathbf{y}) \quad (18)$$

746 Using the Lipschitz constraint, we decompose $\ell_y(G(\hat{\mathbf{c}}^{(v)}), \mathbf{y})$ as follows:

$$\ell_y(G(\hat{\mathbf{c}}^{(v)}), \mathbf{y}) \leq \ell_y(G(\mathbf{c}^{(v)}), \mathbf{y}) + L_g^{(v)} \|\hat{\mathbf{c}}^{(v)} - \mathbf{c}^{(v)}\|_1 \leq \ell_y(G(\mathbf{c}^{(v)}), \mathbf{y}) + L_g^{(v)} \ell_c^{(v)}. \quad (19)$$

756 By combining Equation (18) and (19), the upper bound of L_y can be rewritten as:
 757

$$758 \quad 759 \quad 760 \quad L_y \leq \sum_{v=1}^V \mathbb{E} \left[w_v \ell_y(G(\hat{\mathbf{c}}^{(v)}), y) \right] \leq \sum_v \mathbb{E} \left[w_v \ell_y(G(\mathbf{c}^{(v)}), \mathbf{y}) \right] + \sum_{v=1}^V L_g^{(v)} \mathbb{E} \left[w_v \ell_c^{(v)} \right]. \quad (20)$$

761 According to the property of expectation, for any random variables A and B , $\mathbb{E}[AB] = \mathbb{E}[A]\mathbb{E}[B] +$
 762 $\text{Cov}(A, B)$.
 763

$$764 \quad 765 \quad 766 \quad 767 \quad 768 \quad 769 \quad L_y \leq \sum_{v=1}^V (\mathbb{E}[w_v] \mathbb{E}[\ell_y(G(\mathbf{c}^{(v)}), \mathbf{y})]) + \sum_{v=1}^V (\mathbb{E}[w_v] L_g^{(v)} \mathbb{E}[\ell_c^{(v)}]) \\ + \sum_{v=1}^V \text{Cov}(w_v, \ell_y(G(\mathbf{c}^{(v)}), \mathbf{y})) + \sum_{v=1}^V L_g^{(v)} \text{Cov}(w_v, \ell_c^{(v)}). \quad (21)$$

770 To simplify Equation (21), we take $\mathbb{E}[\ell_y(G(\mathbf{c}^{(v)}), \mathbf{y})]$ as an example and invoke Rademacher
 771 complexity theory, which establishes that with a confidence level $1 - \delta$, where $0 < \delta < 1$, the following
 772 holds:
 773

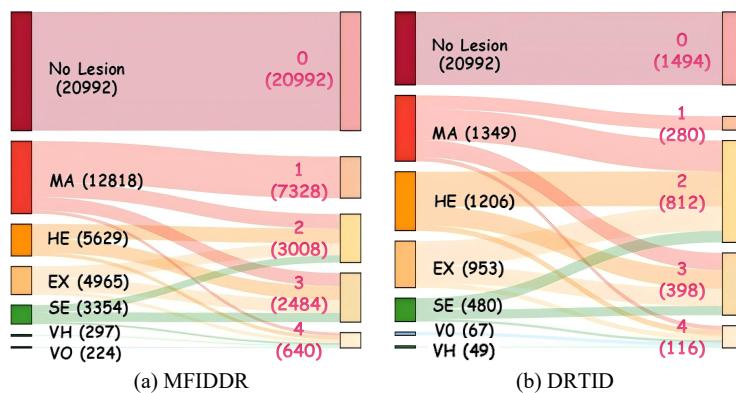
$$\mathbb{E}[\ell_y(G(\mathbf{c}^{(v)}), \mathbf{y})] \leq \hat{L}_y^{(v)} + \mathfrak{R}_N(\mathcal{G}) + P \sqrt{\frac{\ln(V/\delta)}{N}}. \quad (22)$$

774 Where $\hat{L}_y^{(v)}$ denotes the empirical prediction error under correct concepts. Similarly, it can be de-
 775 rived that: $\mathbb{E}[\ell_c^{(v)}] \leq \hat{L}_c^{(v)} + \mathfrak{R}_N(\mathcal{H}_v) + P \sqrt{\frac{\ln(V/\delta)}{N}}$. In summary, we can obtain the final
 776 theorem:
 777

$$778 \quad 779 \quad 780 \quad 781 \quad 782 \quad 783 \quad 784 \quad 785 \quad 786 \quad 787 \quad L_y \leq \underbrace{\sum_{v=1}^V \mathbb{E}[w_v] \hat{L}_y^{(v)} + \sum_{v=1}^V \mathbb{E}[w_v] L_g^{(v)} \hat{L}_c^{(v)}}_{\text{Term-L (average empirical loss of prediction and concept)}} + \underbrace{\sum_{v=1}^V \mathbb{E}[w_v] \mathfrak{R}_N(\mathcal{G}) + \sum_{v=1}^V \mathbb{E}[w_v] L_g^{(v)} \mathfrak{R}_N(\mathcal{C})}_{\text{Term-C (average complexity of prediction and concept)}} \\ + \underbrace{\sum_{v=1}^V \text{Cov}(w_v, \ell_y(G(\mathbf{c}^{(v)}), \mathbf{y})) + \sum_{v=1}^V L_g^{(v)} \text{Cov}(w_v, \ell_c^{(v)})}_{\text{Term-Cov (covariance between fusion weights and losses)}} + 2P \underbrace{\sqrt{\frac{\ln(V/\delta)}{N}}}_{\text{concentration term}}. \quad (23)$$

788 A.3 STATISTICAL INFORMATION OF TWO DATASETS

790 In Fig. 6, we list the detailed information of two DR diagnosis datasets used in our experiments.
 791 The relationships represented by the Sankey diagram capture underlying DR diagnostic rules, which
 792 in turn validate the rationality and interpretability of our reasoning model.
 793



806 Figure 6: The data correlation and distribution of lesion concepts and DR grades in the two benchmarks.
 807 On the left are lesion concepts, and on the right are DR grades. The text indicates the class
 808 name, and the number in parentheses denotes the number of samples in each class.
 809

810
811
812
813
814
815
816
817
818
819
820
821
822
823
824
825
826
827
828
829
830
831
832
833
834
835
836
837
838
839
840
841
842
843
844
845
846
847
848
849
850
851
852
853
854
855
856
857
858
859
860
861
862
863
Table 6: Comparison of Precision and Macro F1-score of different methods for DR 0-4 grades on MFIDDR. The best results are highlighted in bold, and “(MV)” means transforming into a multi-view method. (Unit: %)

| Method | Grade 0 | | Grade 1 | | Grade 2 | | Grade 3 | | Grade 4 | | Avg. | |
|-----------------|------------------|---------------|------------------|---------------|------------------|---------------|------------------|---------------|------------------|---------------|------------------|---------------|
| | Prec. \uparrow | F1 \uparrow |
| ETMC | 86.79 | 91.85 | 73.26 | 63.72 | 66.41 | 55.41 | 64.41 | 70.15 | 0.12 | 0.87 | 58.20 | 56.40 |
| MVCINN | 86.71 | 91.26 | 68.25 | 56.43 | 57.44 | 59.26 | 70.00 | 68.06 | 68.42 | 44.83 | 70.16 | 63.98 |
| Retfound | 80.11 | 87.47 | 50.20 | 35.92 | 54.41 | 46.39 | 65.79 | 66.67 | 90.00 | 36.73 | 68.10 | 54.64 |
| SMVDR | 93.48 | 93.52 | 71.15 | 71.70 | 60.00 | 60.33 | 69.41 | 74.21 | 99.99 | 30.43 | 78.81 | 66.04 |
| WMIMVDR | 92.26 | 93.49 | 71.02 | 71.41 | 63.98 | 59.88 | 71.87 | 74.68 | 87.50 | 29.79 | 77.33 | 65.85 |
| Multi-Task | 91.43 | 93.24 | 71.60 | 69.87 | 64.12 | 61.76 | 69.81 | 72.31 | 87.50 | 29.79 | 76.89 | 65.39 |
| MVCBM | 90.55 | 93.31 | 75.77 | 67.08 | 57.58 | 59.84 | 67.44 | 72.50 | 87.50 | 29.79 | 75.77 | 64.50 |
| CEM (MV) | 91.10 | 93.46 | 73.53 | 70.18 | 63.64 | 62.40 | 71.61 | 73.27 | 84.75 | 35.40 | 76.93 | 66.94 |
| PCBM-h (MV) | 93.44 | 93.94 | 71.72 | 71.03 | 52.82 | 56.82 | 71.13 | 69.66 | 94.44 | 35.42 | 76.71 | 65.37 |
| SSMVCBM | 88.66 | 92.78 | 73.63 | 66.09 | 64.23 | 55.00 | 66.48 | 72.78 | 99.99 | 30.43 | 78.60 | 63.42 |
| CLAT (MV) | 89.30 | 92.68 | 73.17 | 66.18 | 64.42 | 60.69 | 67.24 | 72.67 | 99.99 | 26.67 | 78.83 | 63.78 |
| ProConMV (Ours) | 94.61 | 95.35 | 77.85 | 78.63 | 63.19 | 63.01 | 71.14 | 71.38 | 88.89 | 33.00 | 79.14 | 68.27 |

A.4 SUPPLEMENTARY COMPARATIVE EXPERIMENTAL RESULTS

To better evaluate our proposed method, we compare it against 12 existing methods on MFIDDR dataset. Notably, We adapt RETFound to multi-view fundus image data by designing a multi-channel network to extract features from multiple views, which are then concatenated and fed into the classifier. As shown in Fig. 6, our method achieves the best performance on Grade 0 and Grade 1, with improvements of 1.13%, 1.41%, 2.08%, and 6.93% over the second-best results in Grade 0 precision, Grade 0 F1-score, Grade 1 precision, and Grade 1 F1-score. Moreover, the proposed method achieves competitive results on Grade 2 and Grade 3. However, it does not attain the best performance on Grade 4, possibly due to sample imbalance. Overall, our method achieves improvements of 5.68% in average precision and 4.76% in average F1-score compared to the mean values of the other twelve methods. Additionally, the visualization of the inference process of our proposed ProConMV model is shown in Fig. 9.

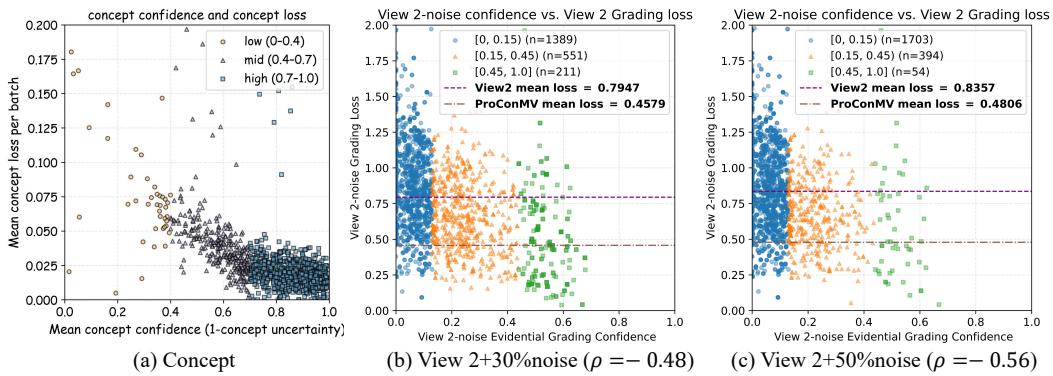


Figure 7: (a) Scatter plot of concept confidence versus loss. (b) Scatter plot of confidence versus loss for View 2 after adding 30% Gaussian noise. (c) Scatter plot of confidence versus loss for View 2 after adding 50% Gaussian noise on MFIDDR test set. Here, ρ denotes their Pearson correlation coefficient (Benesty et al., 2009).

A.5 ANALYSIS OF DUAL-UNCERTAINTY-AWARE MULTI-VIEW FUSION

We provide scatter plots of the concept loss versus its confidence (1-concept uncertainty). Based on the Pearson correlation coefficient $\rho = -0.34$ and the trend observed in Fig. 7, we can see that they are negatively correlated. In addition, we evaluate the sensitivity of uncertainty and the rationality of our module design under noisy conditions. Under noise perturbations, the grading loss of View 2 increases, while its confidence drops significantly. The number of views with confidence in the

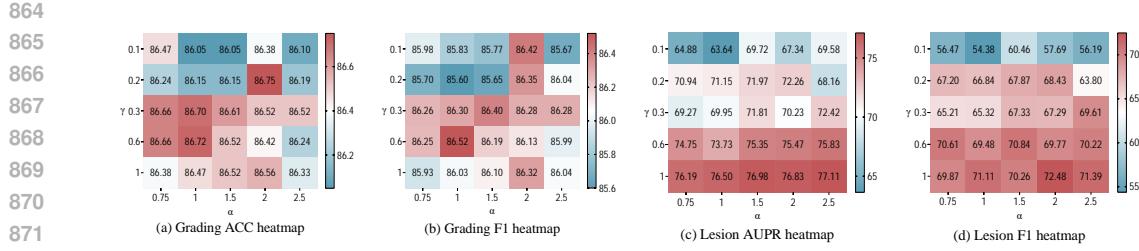


Figure 8: Results of the ablation study on the hyperparameters α and γ . The figure presents grading accuracy, grading F1-score, concept prediction accuracy, and concept prediction F1-score under different values of α and γ . The best results are indicated by the warmest colors.

range $[0, 0.15]$ also increases significantly as the noise level rises from 30% to 50%, as shown in Fig. 3 and Fig. 7. Overall, these results demonstrate the reliability of our dual-uncertainty-aware multi-view fusion method.

A.6 HYPERPARAMETER ANALYSIS

The hyperparameters α and γ respectively control the weight of the concept prediction loss and the focusing parameter in the grading loss. To analyse the impact of these hyperparameters, we conduct a two-dimensional ablation study by systematically varying both α and γ . As shown in Fig. 8, when α increases, the contribution of the concept prediction loss becomes more prominent, resulting in higher concept prediction accuracy. However, a larger value of α reduces grading accuracy, which contradicts our goal of achieving optimal grading performance. Therefore, there is a trade-off between these two hyperparameters. Based on this analysis, we select $\alpha = 0.2$ and $\gamma = 2.0$ as the optimal hyperparameter settings.

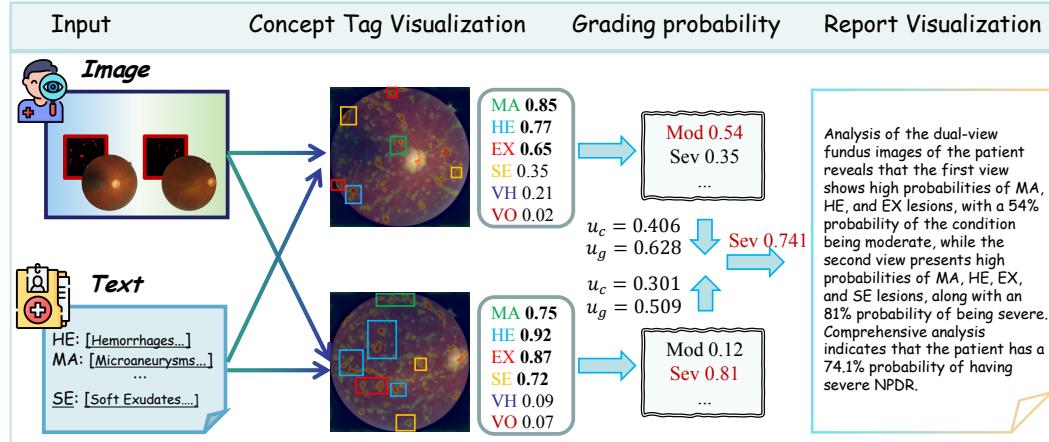


Figure 9: Visualization display of our ProConMV model’s Inference Process.

A.7 INTERPRETABILITY ANALYSIS

Fig. 9 illustrates that our model provides a fine-grained and clinically meaningful interpretation of its diagnostic workflow. For each fundus view, the model first localizes lesion regions and assigns concept tags (e.g., MA, HE, EX, SE, VH, VO) with calibrated probabilities, which are consistent with the accompanying textual descriptions of hemorrhages, microaneurysms, and soft exudates. In the first view, high probabilities of MA, HE, and EX lead to a moderate grading score, whereas in the second view, simultaneously elevated MA, HE, EX, and SE scores support a severe grade. The dual-uncertainty-aware fusion module then combines per-view concept and grading confidences to produce a final severe NPDR probability of 0.741, explicitly revealing how each view contributes to

918 the outcome. Finally, the system generates a natural-language report that summarizes the detected
 919 lesions, per-view severity, and overall diagnostic conclusion, allowing clinicians to verify the pre-
 920 diction step by step. Together, these visual and textual explanations show that the model’s decision
 921 is driven by clinically interpretable lesion patterns rather than opaque global features.
 922

923

924  Briefly describe Hemorrhages’ fundus appearance, key characteristics, and the DR stage(s) in which they most commonly
 925 occur (in 2–3 sentences each).

926 **Hemorrhages**
 927 Retinal bleeding (dot, blot, flame-shaped) caused by ruptured microaneurysms or fragile capillaries. They appear as
 928 multiple deep red lesions in the inner retinal layers and increase in number and size as diabetic retinopathy progresses.
 929 According to standard grading rules, scattered hemorrhages are common in Moderate NPDR (Grade 2), while extensive
 930 hemorrhages in all four quadrants are a hallmark of Severe NPDR (Grade 3) under the ‘4-2-1’ rule.
 931 

932  Briefly describe Hard Exudates’ fundus appearance, key characteristics, and the DR stage(s) in which they most
 933 commonly occur (in 2–3 sentences each).

934 **Hard Exudates**
 935 Yellow, well-defined lipid deposits resulting from chronic leakage of serum lipoproteins from incompetent retinal
 936 vessels or microaneurysms. They often cluster in circinate (ring-like) patterns around leaking points and can accumulate
 937 in the macula, threatening central vision. In grading, the presence of hard exudates is typical of Moderate NPDR and
 938 more advanced stages (Grade ≥ 2), and when located near the fovea, they are used to identify clinically significant
 939 macular edema in some grading schemes.
 940 

941  Briefly describe Microaneurysms’ fundus appearance, key characteristics, and the DR stage(s) in which they most
 942 commonly occur (in 2–3 sentences each).

943 **Microaneurysms**
 944 Small, round red dots produced by focal outpouching of capillary walls, representing the earliest clinically visible sign of
 945 diabetic retinopathy. They are usually located in the posterior pole and may be isolated or accompanied by minimal
 946 hemorrhages. In most grading systems, the presence of microaneurysms with few or no additional lesions corresponds to
 947 Mild NPDR (Grade 1), and increasing numbers of microaneurysms signal progression toward more severe stages.
 948 

949  Briefly describe Soft Exudates’ fundus appearance, key characteristics, and the DR stage(s) in which they most
 950 commonly occur (in 2–3 sentences each).

951 **Soft Exudates**
 952 White, fluffy ‘cotton-wool’ spots arising from focal ischemia and axoplasmic flow stasis in the nerve fiber layer. They
 953 indicate localized retinal infarction and are often associated with widespread capillary non-perfusion. In diagnostic
 954 grading, the occurrence of multiple soft exudates together with extensive hemorrhages, venous beading, or intraretinal
 955 microvascular abnormalities (IRMA) supports a diagnosis of Severe NPDR (Grade 3) according to the ‘4-2-1’ rule.
 956 

957  Briefly describe Vitreous Hemorrhages’ fundus appearance, key characteristics, and the DR stage(s) in which they most
 958 commonly occur (in 2–3 sentences each).

959 **Vitreous Hemorrhages**
 960 Blood leakage into the vitreous cavity or preretinal space from fragile neovascular vessels that break through the internal
 961 limiting membrane. Clinically, they present as sudden vision loss or floaters and may partially or completely obscure the
 962 fundus. In grading systems, the presence of vitreous or preretinal hemorrhage due to neovascularization is a defining
 963 sign of proliferative diabetic retinopathy (PDR, Grade 4) and identifies high-risk eyes that require urgent treatment.
 964 

965  Briefly describe Vitreous Opacities’ fundus appearance, key characteristics, and the DR stage(s) in which they most
 966 commonly occur (in 2–3 sentences each).

967 **Vitreous Opacities**
 968 Cloudy or hazy areas within the vitreous caused by suspended blood, fibrous tissue, or fibrovascular membranes
 969 following recurrent hemorrhage and neovascular proliferation. These opacities can produce persistent floaters, reduced
 970 contrast sensitivity, and significant vision loss if they obscure the macula. In severity grading, marked vitreous opacities
 971 are characteristic of advanced PDR (Grade 4) and often indicate fractional changes that may progress to retinal
 972 detachment if not properly managed.
 973 

Figure 10: The generation of concept text.

A.8 CONCEPT TEXT GENERATION

969 We obtain the concept descriptions of DR lesions through a six-round dialogue with GPT-4 (Achiam
 970 et al., 2023). In each round, the model extracts specific feature information about a lesion, ultimately
 971 generating an accurate medical text description. The generated text includes the lesion’s typical
 972 appearance, key features, and its manifestations at different stages of DR, as shown in Fig. 10.

972 A.9 LLM USAGE STATEMENT
973974 In this paper, an LLM is used solely for text polishing. All research ideas, methods, experiments,
975 and conclusions are conducted without the assistance of any LLMs.
976
977
978
979
980
981
982
983
984
985
986
987
988
989
990
991
992
993
994
995
996
997
998
999
1000
1001
1002
1003
1004
1005
1006
1007
1008
1009
1010
1011
1012
1013
1014
1015
1016
1017
1018
1019
1020
1021
1022
1023
1024
1025