000 001 002 ALIGNMENT-AWARE MODEL EXTRACTION ATTACKS ON LARGE LANGUAGE MODELS

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Paper under double-blind review

ABSTRACT

Model extraction attacks (MEAs) on large language models (LLMs) have received increasing attention in recent research. However, existing attack methods typically adapt the extraction strategies originally developed for deep neural networks (DNNs). They neglect the underlying inconsistency between the training tasks of MEA and LLM alignment, leading to suboptimal attack performance. To tackle this issue, we propose **Locality Reinforced Distillation (LoRD)**, a novel model extraction algorithm specifically designed for LLMs. In particular, LoRD employs a newly defined policy-gradient-style training task that utilizes the responses of victim model as the signal to guide the crafting of preference for the local model. Theoretical analyses demonstrate that I) The convergence procedure of LoRD in model extraction is consistent with the alignment procedure of LLMs, and II) LoRD can reduce query complexity while mitigating watermark protection through exploration-based stealing. Extensive experiments on domain-specific extractions validate the superiority of our method in extracting various state-of-the-art commercial LLMs. Our code is available at: <https://anonymous.4open.science/r/LoRD-MEA-1EF2/>.

1 INTRODUCTION

028 029 030 031 032 033 034 035 036 037 038 039 040 041 042 043 044 In recent years, we have witnessed the remarkable success of large language models (LLMs) such as ChatGPT [\(cha, 2024\)](#page-11-0), Gemini [\(Anil](#page-11-1) [et al., 2024\)](#page-11-1), and Claude [\(cla, 2024\)](#page-11-2), which are now widely employed in various consumer and industrial applications. Despite their success, these models may suffer from *model extraction attacks* (MEAs) [\(Krishna et al., 2020;](#page-13-0) [Rafi](#page-15-0) [et al., 2022;](#page-15-0) [Xu et al., 2022;](#page-15-1) [Li et al., 2023b\)](#page-13-1), where their knowledge could be at risk of being stolen by an adversary through a *local model* that learns on the data collected from the *victim model*. Besides of some "open-source" LLMs (e.g., Alpaca [\(Taori et al., 2023\)](#page-15-2)), which are trained on the chat history of GPT-4, cases of commercial model theft among companies have also been reported recently [\(Heath, 2023\)](#page-12-0).

045 046 047 048 049 050 Under such a real-world threat, instead of focusing on MEAs against conventional DNNs, which have been extensively studied theoretically [\(Saad & Solla, 1995;](#page-15-3) [Tian, 2020;](#page-15-4) [Zhou](#page-16-0) [et al., 2021\)](#page-16-0) and empirically [\(Jagielski et al.,](#page-12-1) [2020;](#page-12-1) [Tramèr et al., 2016;](#page-15-5) [Papernot et al., 2017\)](#page-14-0), a few recent works turn to explore model extrac-

Adversary End

Figure 1: Comparison between vanilla MEAs on conventional DNNs (left) and MEAs on LLMs with alignments (right).

051 052 053 tion algorithms and theorems for LLMs. For example, [Wallace et al.](#page-15-6) [\(2020\)](#page-15-6) propose a monolingualquery-based imitation attack framework to steal machine translation knowledge from generative language models such as GPT-2. [Li et al.](#page-13-1) [\(2023b\)](#page-13-1) investigate threats of stealing the code-related knowledge from LLMs. However, these studies inherit those MEA algorithms from traditional fields, **054 055 056 057 058 059 060** such as computer vision [\(Tramèr et al., 2016;](#page-15-5) [Papernot et al., 2017\)](#page-14-0), and train the local model via supervised learning like maximum likelihood estimation (MLE) [\(Bengio et al., 2000;](#page-11-3) [Myung, 2003\)](#page-14-1), while neglecting the inconsistency of training tasks between MEAs and the alignments [\(Ouyang](#page-14-2) [et al., 2022;](#page-14-2) [Glaese et al., 2022;](#page-12-2) [Bai et al., 2022a](#page-11-4)[;b;](#page-11-5) [Perez et al., 2023\)](#page-14-3) of modern LLMs. As shown in Figure [1,](#page-0-0) modern LLMs typically employ alignments using reinforced learning, which is missing in the local model training of conventional MEAs. As a result, these attacks usually suffer from poor performance.

061 062 In this paper, we challenge the effectiveness of MLE in stealing a reinforcement-learning-aligned LLM, by analyzing its potential drawbacks as follows:

063 064 065 066 Low query efficiency. Current LLM-oriented MEAs suffer from unacceptably significant query times because they must collect enough generated responses, which entails exponential complexity in terms of generated tokens, resulting in low query efficiency.

067 068 069 070 071 Vulnerability against defenses. Directly learning from the responses of victim models can cause local models to inadvertently incorporate those *watermarks* [\(Cong et al., 2022;](#page-11-6) [He et al., 2022;](#page-12-3) [Zhao et al., 2022;](#page-16-1) [He et al., 2021\)](#page-12-4) embedded in the output of victim models. The residue of such watermarks makes the extraction process less stealthy and even serves as provenance evidence of model theft.

072 073 074 075 076 077 078 079 080 081 082 Motivated by these limitations, we propose Locality Rein-forced Distillation (LoRD), a queryefficient and watermark-resistant model extraction attack under a training paradigm with LLM's alignments. Stealing LLMs via reinforcement learning paradigms is challenging. The main reason is that the key component in the alignment procedure of LLMs, *reinforcement learning with human feedback* (RLHF) [\(Bai et al., 2022a;](#page-11-4)[b;](#page-11-5) [Perez et al., 2023\)](#page-14-3), heavily relies on the feedback signal of *human annotators*, which is difficult to reproduce directly in the context of MEAs. To tackle this challenge, we develop a policy-gradient-style extraction procedure. This approach regards the *locality direction* between the generations of local models and victim models as the implicit reward signal. It can thus achieve a *human-feedback-free* reinforcement learning for our extraction attack. From the theoretical perspective, we show why those existing MEAs using *MLE* and *knowledge distillation (KD)* are inconsistent with the optimization procedure in LLMs' alignments. Along this way, we also demonstrate why LoRD can achieve stronger watermark resistance and higher query efficiency.

083 084 085 086 087 088 089 Extensive experiments on five downstream NLP tasks and ten datasets demonstrate that it is feasible to steal a commercial LLM with 175 billion parameters by a pre-trained local model with only 8 billion parameters under a given domain. The resulting local model performs statistically similar to the victim model for tasks not requiring extra knowledge (e.g., data-to-text), and only $0 \sim 3$ percentage lower for tasks requiring it (e.g., translation and QAs). This result poses an immediate threat of task-specific extraction on commercial LLMs. To further draw the capability boundary of such a threat, we also illustrate the "spectrum" in difficulties and upper bounds for extracting LLMs.

090 091 To summarize, the contributions of our paper are as follows:

092 093 094 New Perspective of LLM Alignment for MEAs. We present LoRD, a novel model extraction attack algorithm for LLMs. To our best knowledge, it is the first effective and realistic extraction algorithm that is compatible with the alignment procedure of LLMs.

095 096 097 Theoretical Guarantee. We theoretically prove that the convergence procedure of LoRD in MEAs is consistent with the alignments of LLMs. Furthermore, we demonstrate that LoRD can reduce query complexity while mitigating watermark protection through exploration-based stealing.

098 099 Systematical Evaluation. Extensive experiments on domain-specific extractions demonstrate that our method outperforms current extraction strategies across different downstream NLP tasks.

- **100 101**
- 2 BACKGROUND
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104 2.1 POLICY GRADIENT MODELS

106 107 Policy gradient models (PGM) are commonly used in reinforcement learning (RL) algorithms to optimize the agents based on the decided *action* of RL agents. Represented by TRPO [\(Schulman](#page-15-7) [et al., 2015\)](#page-15-7) and PPO [\(Schulman et al., 2017\)](#page-15-8), policy gradient models minimize the the following

108 109 objective function:

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$$
\mathcal{L}_{pg,j} = -\hat{\mathbb{E}}_j[p_j^r(\theta)A_j],\tag{1}
$$

111 112 113 114 where at each decision step j, $p_j^r(\theta) = \frac{\pi_{\theta}(a_j|s_j)}{\pi_{\theta_{old}}(a_j|s_j)}$ refers to the probability ratio defined by the optimized policy $\pi_{\theta}(a_j | s_j)$ and the initial policy $\pi_{\theta_{old}}(a_j | s_j)$, s_j denotes the *state* of the environment, a_j denotes the decided *action* of π_{θ} , and A_j is the *de-biased reward* of a_j . A_j is estimated by the Q -value minus the V -value, i.e.,

$$
A_j(s_j, a_j) = Q(s_j, a_j) - V(s_j).
$$
\n(2)

117 118 119 Intuitively, Q-value refers to the *reward* if employing action a_i at the given environment state s_i , which can be seen as the label of policy's decision. *V*-value represents the estimation of the expected reward at s_j . Consequently, A_j denotes the *surprise* when taking action a_j .

120 121 122 123 To alleviate the *off the cliff* phenomenon that a large bad gradient update occurred from Equation [1,](#page-2-0) PGMs, such as PPO and TRPO, add some regularization terms to avoid large gradients. Specifically, TRPO constrains the distribution between π_{θ} and $\pi_{\theta_{old}}$ with KL divergence, and PPO warps a "clip" function to constrain the bounds of $p_j^r(\theta)$.

125 2.2 LANGUAGE MODELING

126 127 128 129 130 Supervised Training (SFT). Given a pre-trained model with parameters θ , supervised training is essentially the *maximum likelihood estimation (MLE)* task [\(Bengio et al., 2000;](#page-11-3) [Myung, 2003\)](#page-14-1), which fine-tunes θ on the labeled dataset $\mathcal{D}_{tr}^s = \{(\mathbf{x}_i, \mathbf{y}_i)|i=1,2,...,N_{trs}\}$ by minimizing the following objective function:

$$
\mathcal{L}_{mle} = -\prod_{i}^{N_{trs}} P_{\theta}(\mathbf{y}_i|\mathbf{x}_i) = -\prod_{i}^{N_{trs}} \prod_{j}^{N} P_{\theta}(y_{i,j}|\mathbf{x}_i, \mathbf{y}_{i,j}),
$$
(3)

133 134 135 136 where N denotes the sequence length of y_i , $y_{i,j}$ denotes the j-th token in y_i , and $y_{i,\leq j}$ = {yi,0, ..., yi,j−1}. The logarithmic formula of Equation [3](#page-2-1) can also be seen as a *joint cross-entropy* loss function:

$$
\mathcal{L}_{ce} = -\sum_{i}^{N_{trs}} \log P_{\theta}(\mathbf{y}_i|\mathbf{x}_i) = -\sum_{i}^{N_{trs}} \sum_{j}^{N} \log P_{\theta}(y_{i,j}|\mathbf{x}_i, \mathbf{y}_{i,
$$

139 140 141 142 Equation [4](#page-2-2) is extensively utilized in LLM's pre-training and fine-tuning procedures. For instance, it can be applied to *instruction-following supervised fine-tuning (SFT)* with the training set \mathcal{D}_{tr} , wherein x_i encompasses the instruction and the task input, while y_i denotes the reference response.

143 144 145 146 147 Aligning LLMs merely by SFT is not always practical, as MLE tends to align the model with the one-hot distribution of y, making it challenging to draw a sufficient variety of examples due to the *"exponential explosion"* of tokens (see Section [4](#page-5-0) for more details). Moreover, providing standard answers for LLMs can sometimes be daunting for annotators, which further slows down and even degrades the alignment process through direct training.

148 149 Therefore, instead of "learning from answers" as in Equation [4,](#page-2-2) learning from *preferences* is proposed, which only requires the annotators to select a better response from a pair of texts generated by LLMs.

150 151 152 153 154 155 Aligning from Preferences. Employing reinforcement learning in LLMs typically consists of three stages. First, the annotators construct a preference dataset $\mathcal{D}^{pref} = \{(\mathbf{x}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)\}$ by chatting with LLMs and rating their responses, where y_i^+ and y_i^- denote the rated positive and negative responses of the dialogue context x_i , respectively. Then, a *reward model* $R_{\theta_{\phi}}(x, y) \to r$ is trained based on \mathcal{D}^{pref} to simulate the environment and predict the reward values of tokens in given texts. It is trained with a pair-wise loss,

$$
\mathcal{L}_r = -\sum_{(\mathbf{x}, \mathbf{y}^+, \mathbf{y}^-) \sim \mathcal{D}^{pref}} \sigma(R_{\theta_{\phi}}(\mathbf{x}, \mathbf{y}^+) - R_{\theta_{\phi}}(\mathbf{x}, \mathbf{y}^-)),\tag{5}
$$

158 159 160 where $\sigma(\cdot)$ denotes the sigmoid function. Based on the reward model $R_{\theta_{\phi}}(\mathbf{x}, \mathbf{y})$, we can finally train the language models P_{θ} by maximizing its reward, i.e.,

161
$$
\max_{\theta} \sum_{\mathbf{x} \sim \mathcal{D}_q} R_{\theta_{\phi}}(\mathbf{x}, \hat{\mathbf{y}}) - \beta \mathbb{D}_{KL}[P_{\theta}(\hat{\mathbf{y}}|\mathbf{x})||P_{\theta_{init}}(\hat{\mathbf{y}}|\mathbf{x})],
$$
 (6)

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Figure 2: The stealing procedure of LoRD.

175 176 177 178 179 where \mathcal{D}_q denotes the dataset of text inputs, $\hat{\mathbf{y}} \sim P_\theta(\mathbf{y}|\mathbf{x})$ denotes the sampled sequence of the training model, and θ_{init} is the initialized parameters of the model, e.g. the parameters after SFT. The Kullback-Leibler (KL) divergence term, $\beta \mathbb{D}_{KL}[P_{\theta}(\mathbf{y}|\mathbf{x})||P_{\theta_{init}}(\mathbf{y}|\mathbf{x})]$, introduced by TRPO [\(Schulman et al., 2015\)](#page-15-7), is incorporated to constrain the shift of distribution in generated texts \hat{y} , where β is the hyperparameter.

183 185 Consequently, SFT shown in Equation [4](#page-2-2) fine-tunes the pre-trained model with parameters θ_{pre} into an aligned model θ_{sft} through MLE, and RLHF outlined in Equation [6,](#page-2-3) further aligns θ_{sft} towards the target model θ_{vic} . As this procedure is not consistent with the conventional training framework of DNNs, it remains unclear whether current MEAs (detailed in Appendix [C.2\)](#page-23-0) are effective and efficient in stealing a LLM. Specifically, we will first put forward a new stealing method in Section [3,](#page-3-0) and compare it with current MEAs in Section [4.](#page-5-0)

3 LORD: LOCALITY REINFORCED DISTILLATION

3.1 OVERVIEW

191 192 193 194 195 196 197 198 199 200 201 202 203 204 205 In this subsection, we delve into the details of our model extraction framework, LoRD (Locality Reinforced Distillation). As described in Algorithm [1,](#page-26-0) LoRD follows a reinforcement learning paradigm, that is, it consists of several *periods*, and in each period, the model will learn to explore new responses and attempt to enhance the model trained in the last period. However, different from LLMs' alignments, the agent can neither obtain the reward from the reward model directly, nor label positive and negative responses manually. This motivates us to design a new RL method which can implicitly measure the reward for generated tokens under the guidance of victim model's responses.

206 207 208 Illustrated by Figure [2,](#page-3-1) LoRD first requires the model to sample two sentences randomly at period $t - 1$, which are denoted as y_{t-1}^+ and y_{t-1}^- ,

Figure 3: Determination of the positive and negative samples in LoRD. We sample y_{t-1}^+ and y_{t-1}^- from $P_{\theta_{t-1}}(\cdot|\mathbf{x})$, and compute their conditional probabilities. The response with a higher probability increment on θ_t is selected as the positive sample.

209 210 211 212 213 214 215 respectively. In a new period t , it first computes the changes of likelihoods for these two sentences, among the old model $P_{\theta_{t-1}}$ and the current model P_{θ_t} . These changes of likelihoods, denoted as Δ_t^+ and Δ_t^- , indicate whether a selected sentence is locally *isotropic* ($\Delta > 0$) to the optimization direction with victim model's response y_{vic} or not ($\Delta \le 0$), which can be seen as the feedback signal for P_{θ_t} in the current optimization step. For convenience, we may swap y_{t-1}^+ with y_{t-1}^- to make sure that $\Delta_t^+ > \Delta_t^-$ always holds. In this way, for pairs (x, y_{vic}) we can take y_{t-1}^+ as a *locality neighborhood* of y_{vic} and y_{t-1}^- as the negative sample, all of which can be utilized in the training of P_{θ_t} . Figure [3](#page-3-2) illustrates this procedure. Additionally, LoRD takes y_{t-1}^+ as the positive label under

216 217 218 the current scope only when Δ^+ or $P_{\theta_t}(\mathbf{y}_{t-1}^+|\mathbf{x})$ exceed their respective fixed thresholds τ_1 and τ_2 . If these conditions are not met, it will use \mathbf{y}_{vic} as a substitute for \mathbf{y}_{t-1}^+ to enable a cold start.

Based on y_{vic}, y_{t-1}^+ , and y_{t-1}^- , we now design LoRD's loss function.

221 3.2 DESIGN OF LOSS FUNCTIONS

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From Section [2.1,](#page-1-0) we know that the loss function of a policy gradient model can be expressed as an *objective function* to maximize the rewards of decisions (see Equation [1\)](#page-2-0) and a *regularization term* to ensure the stability of training. Following this paradigm, the loss function of LoRD could be

$$
\mathcal{L}_{\text{LoRD}} = \mathcal{L}_{obj} + \mathcal{L}_{reg}.\tag{7}
$$

Objective function \mathcal{L}_{obj} . Inspired by the reward model $R_{\theta_{\phi}}$ existed in Equation [6,](#page-2-3) which is trained to distinguish between positive and negative samples, we propose utilizing the logarithmic proportion of positive to negative samples as the means of achieving a de-biased reward, i.e.,

$$
\mathcal{L}_{obj} = -\sum_{\mathbf{x} \in \mathcal{D}_q} \log[\frac{P_{\theta_t}(\mathbf{y}_{t-1}^+|\mathbf{x})}{P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})}] = -\sum_{\mathbf{x} \in \mathcal{D}_q} [\log P_{\theta_t}(\mathbf{y}_{t-1}^+|\mathbf{x}) - \log P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})]. \tag{8}
$$

233 234 235 236 Equation [8](#page-4-0) exhibits similarities to previous studies on RL-enhanced LLM [\(Peters & Schaal, 2007;](#page-14-4) [Peng et al., 2019;](#page-14-5) [Go et al., 2023;](#page-12-5) [Korbak et al., 2022;](#page-13-2) [Rafailov et al., 2023\)](#page-14-6). We provide a theoretical explanation for its consistency with the learning procedure of RLHF and the deduction procedure, as detailed in Section [4](#page-5-0) and Appendix [B.1.](#page-20-0)

237 238 239 240 241 However, training the local model merely by \mathcal{L}_{obj} is ineffective due to two reasons: *i*) when $\mathcal{L}_{\text{LoRD}} :=$ \mathcal{L}_{obj} , no information from the victim model's responses is incorporated into the selection of y_{t-1}^+ beyond the cold start phase, resulting in a meaningless *self-reward-based learning* loop for the stealing procedure; *ii)* the convergence of the local model's training cannot be guaranteed.

242 To address these two issues simultaneously, we design the regularization term as follows.

243 244 245 Regularization loss \mathcal{L}_{reg} . Different from LLM's RLHF [\(Schulman et al., 2015;](#page-15-7) [Rafailov et al., 2023;](#page-14-6) [Bai et al., 2022a\)](#page-11-4) that typically constrain θ_t with initial model's generating distribution $P_{\theta_{init}}(\cdot|\mathbf{x})$ in RLHF, LoRD aims to directly constrain θ_t with victim model's distribution $P_{\theta_{vis}}(\cdot|\mathbf{x})$.

246 247 248 249 Unfortunately, $P_{\theta_{vic}}(\cdot|\mathbf{x})$ is typically **inaccessible** within the APIs of commercial LLMs and is not feasible for our black-box scenarios. Consequently, we incorporate the regularization techniques employed in PPO and TRPO but tailor our regularization as a bounded contrastive term between the likelihood of θ_t under the victim model's response and the negative sample, i.e.,

$$
\mathcal{L}_{reg} = -\sum_{\mathbf{x} \in \mathcal{D}_q} clip(\log[\frac{P_{\theta_t}(\mathbf{y}_{vic}|\mathbf{x})}{P_{\theta_t}(\mathbf{y}_{t-1}^{-}|\mathbf{x})}]) = -\sum_{\mathbf{x} \in \mathcal{D}_q} clip(\log P_{\theta_t}(\mathbf{y}_{vic}|\mathbf{x}) - \log P_{\theta_t}(\mathbf{y}_{t-1}^{-}|\mathbf{x})).
$$
 (9)

253 254 255 256 257 258 259 In Equation [9,](#page-4-1) we utilize PPO's $clip(\cdot)$ function to limit the value of the regularization term, as we expect the regularization term could only be used to avoid the *off the cliff* problem [\(Schulman](#page-15-8) [et al., 2017;](#page-15-8) [2015\)](#page-15-7) in RL's convergence. Besides, our contrastive term can be seen as a streamlined black-box variant of the KL divergence in TRPO. This simplification offers two advantages: *i)* it alleviates the necessity of loading the initial model's weights, leading to a substantial reduction in GPU memory usage; *ii*) it eliminates the need for $P_{\theta_t}(\cdot|\mathbf{x})$, which would otherwise necessitate an additional exponential operation of $log P_{\theta_t}(\cdot|\mathbf{x})$ that would slow down the forward computation process and increase extra consumption.^{[1](#page-0-1)}

Incorporating Equation [8](#page-4-0) with Equation [9,](#page-4-1) we can reshape the loss function of LoRD as

$$
\mathcal{L}_{\text{LoRD}} = \mathcal{L}_{obj} + \mathcal{L}_{reg} = \sum_{\mathbf{x} \in \mathcal{D}_q} \log[\frac{P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})}{P_{\theta_t}(\mathbf{y}_{t-1}^+|\mathbf{x})}] + clip(\log[\frac{P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})}{P_{\theta_t}(\mathbf{y}_{\text{vic}}|\mathbf{x})})].
$$
\n(10)

Finally, we wrap $\mathcal{L}_{\text{LoRD}}$ with a sigmoid function $\sigma(\cdot)$ to normalize the loss to the interval $(0, 1)$, which is

$$
\mathcal{L} = \sum_{\mathbf{x} \sim \mathcal{D}_q} \sigma(\log[\frac{P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})}{P_{\theta_t}(\mathbf{y}_{t-1}^+|\mathbf{x})}] + clip(\log[\frac{P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})}{P_{\theta_t}(\mathbf{y}_{vic}|\mathbf{x})}])).
$$
\n(11)

¹logsoftmax is preferred in the implementation of deep learning frameworks [\(tor\)](#page-11-7), as the exponential operation in *softmax* and the logarithmic operation in *cross-entropy* can be canceled out by each other.

270 271 4 THEORETICAL ANALYSIS

272 273 274 275 276 This section will compare LoRD with current model extraction methods from a theoretical perspective. We will first reveal the underlying inconsistency between the optimization procedure of LLMs, which typically involves RL-based alignments, and the previous model extraction approaches utilizing *MLE* and *knowledge distillation (KD)*. Subsequently, we will demonstrate in theory the reasons why LoRD can achieve stronger watermark resistance and higher query efficiency than existing methods.

277 278

308 309 4.1 CONSISTENCY ANALYSIS REGARDING DIFFERENT LEARNING TASKS

279 280 281 282 Based on the analysis of the four objective functions for MLE, KD, RLHF and LoRD, we reach the proposition [1,](#page-5-1) and illustrate their convergence procedure exhibited in Figure [4.](#page-5-2) A detailed proof can be found in Appendix [B.1.](#page-20-0)

283 284 285 286 287 Proposition 1 (Consistency in Stealing Procedure). *The learning procedure for LLMs' alignments is consistent with the stealing procedure of LoRD, i.e., they both attempt to maximize the difference between the probabilities of positive and negative samples. Conversely, they are inconsistent with either MLE or KD. In MLE, the objective is maximizing the label probability, while KD aims to minimize the distance among all dimensions.*

288 289 290 291 Albeit the inconsistency in their *training procedures*, we put forward Proposition [2](#page-5-3) to demonstrate that *with enough samples*, all these methods will reach the same distribution results.

292 293 294 295 296 297 298 299 Proposition 2 (Equivalence when Converged). *Ideally, for any loss value of Equations [4,](#page-2-2) [5,](#page-2-4) [6,](#page-2-3) [10,](#page-4-2) or [11](#page-4-3) converging to* 0*, we have* $y^+ \equiv$ yvic*. Meanwhile, the local model's distribution* $P_{\theta}(\cdot|\mathbf{x})$ *will approach that of the victim model* $P_{\theta_{vis}}(\cdot|\mathbf{x})$ *on MEAs from all three discussed MEA methods, including LoRD, MLE, and KD.*

300 301 302 303 304 305 306 307 Proposition [2](#page-5-3) ensures that the local model will converge to the victim model regardless of the choice of MEA methods. So what is the benefit of LoRD? In Section [4.2,](#page-5-4) we will show that LoRD outperforms current MEAs with two aspects: the query time reduction (i.e., size of the query set \mathcal{D}_q), and the watermark resistance of the learned local model.

Figure 4: Illustrations for the converging procedure of probability distributions regarding four methods, namely MLE (a), KD (b), RLHF (c), and LoRD (d). Arrows indicate the expected optimization direction. We mark the distribution dimensions learned with labels in *blue*, and employ *pink* and *yellow* components to indicate the probabilities of positive and negative tokens, respectively.

4.2 COMPARATIVE ANALYSIS ON MODEL STEALING

310 311 312 313 314 315 316 Query Efficiency. Let N_Q and N_R denote the sequence lengths of the query text and the response text, respectively. For MLE, the *ideal* query numbers to populate the entire text space are given by $\mathcal{O}(V^{N_Q} \cdot V^{N_R})$, where V represents the size of the vocabulary. In contrast, LoRD possesses the capability to automatically explore the generation token space, thereby significantly reducing the query requirements about generation candidates to a constant level. Specifically, the complexity of LoRD's query requirements is $\mathcal{O}(V^{N_Q} \cdot C)$, where C is a constant that correlates with the capability of local models.

317 318 319 320 321 322 323 Based on the above analysis, a straightforward concern with employing MLE in LLMs' extraction is that, given the limited query times in real-world practices, it may suffer from incomplete learning, especially for text generation tasks. Consequently, the local model may tend to memorize some specific responses instead of achieving a broad understanding and generation. We call such a phenomenon *preference overfitting (PO)*, which indicates that the local model is only effective on a limited set of explored samples, and yet does not generalize well to unseen scenarios. In such cases, the local model usually exhibits a more "rugged" decision surface, which appears to *overfit* the preference sentences in \mathcal{D}_{tr} , as shown in Figure [11](#page-20-1) (b). Figure [10](#page-19-0) provides a visualization of it.

324		BLEU				BERTScore			Rouge-L			
325			$\overline{}$		4	Pre.	Rec.	F1.	Pre.	Rec.	F1.	
		Text to SQL: WikiSQL (Zhong et al., 2017) with 64 query samples										
326	Victim Model	54.1	41.4	32.1	24.4	86.9	93.5	90.1	58.9	62.1	59.7	
	Local Model	20.2 ± 0.2	14.5 ± 0.2	10.9 ± 0.1	8.1 ± 0.1	82.5 ± 0.0	92.4 ± 0.1	87.1 ± 0.0	22.6 ± 0.3	66.4 ± 0.4	33.2 ± 0.3	
327	$+MLE$	54.0 ± 1.6	37.5 ± 2.1	26.4 ± 2.0	18.8 ± 1.8	83.1 ± 0.2	92.9 ± 0.2	87.7 ± 0.2	56.2 ± 1.5	56.1 ± 0.9	55.8 ± 1.2	
	$+LoRD$	55.1 ± 2.3	39.0 ± 3.6	28.0 ± 4.0	20.4 ± 3.9	83.4 ± 0.4	92.9 ± 0.3	87.9 ± 0.4	57.7 ± 2.2	56.3 ± 2.0	56.7 ± 2.1	
328	Text to SOL: Spider (Zhong et al., 2017) with 64 query samples											
329	Victim Model	9.4	3.9	2.1	1.1	77.7	84.1	80.6	17.1	36.3	21.8	
	Local Model	6.4 ± 0.2	2.1 ± 0.1	0.9 ± 0.1	0.5 ± 0.0	80.0 ± 0.1	82.6 ± 0.1	81.2 ± 0.1	10.0 ± 0.3	21.5 ± 0.6	12.7 ± 0.4	
330	$+MLE$	6.2 ± 0.9	1.3 ± 0.5	0.6 ± 0.3	0.2 ± 0.2	76.4 ± 0.7	81.8 ± 0.4	78.9 ± 0.6	12.7 ± 1.6	18.3 ± 1.6	14.3 ± 1.6	
	$+LoRD$	9.1 ± 0.9	2.8 ± 0.5	1.3 ± 0.4	0.6 ± 0.2	77.7 ± 0.4	83.1 ± 0.5	80.2 ± 0.3	16.9 ± 0.1	24.1 ± 0.2	18.8 ± 0.1	
331	Data to Text: E2E NLG (Dušek et al., 2020) with 64 query samples											
	Victim Model	51.8	27.0	26.8	19.1	93.9	94.6	94.2	49.6	54.6	51.4	
332	Local Model	31.1 ± 0.1	20.1 ± 0.2	13.5 ± 0.2	8.9 ± 0.3	86.1 ± 0.1	92.4 ± 0.1	89.1 ± 0.1	29.0 ± 0.3	49.4 ± 0.4	35.9 ± 0.3	
333	$+MLE$	53.0 ± 0.9	38.0 ± 0.6	27.5 ± 0.5	19.9 ± 0.4	89.1 ± 0.0	94.5 ± 0.0	91.8 ± 0.0	48.3 ± 0.5	54.2 ± 1.4	50.4 ± 0.9	
	$+LoRD$	53.1 ± 1.1	38.2 ± 0.9	27.8 ± 0.7	20.2 ± 0.5	89.1 ± 0.1	94.5 ± 0.1	91.7 ± 0.1	48.3 ± 0.7	53.5 ± 1.4	50.2 ± 0.9	
334							Data to Text: CommonGen (Lin et al., 2020) with 64 query samples					
	Victim Model	33.3	18.5	11.1	6.9	91.3	92.1	91.7	33.6	40.7	36.1	
335	Local Model	12.2 ± 0.0	6.5 ± 0.1	3.8 ± 0.0	2.3 ± 0.0	83.0 ± 0.0	89.7 ± 0.0	86.2 ± 0.0	14.6 ± 0.1	46.2 ± 0.2	21.6 ± 0.0	
	$+MLE$	32.4 ± 2.0	18.3 ± 1.3	10.9 ± 1.0	6.6 ± 0.7	84.2 ± 0.1	91.7 ± 0.0	87.8 ± 0.0	31.7 ± 2.4	41.1 ± 0.4	35.1 ± 1.6	
336	$+LoRD$	32.1 ± 1.3	18.0 ± 0.9	10.7 ± 0.5	6.4 ± 0.3	84.1 ± 0.0	91.6 ± 0.1	87.7 ± 0.0	31.4 ± 1.1	40.3 ± 0.9	34.6 ± 0.9	
337	Victim Model	Summarization: TLDR (Kirk et al., 2023) with 64 query samples								18.4		
	Local Model	11.9 6.9 ± 0.0	5.0 3.2 ± 0.1	2.6 1.7 ± 0.0	1.5 1.0 ± 0.0	85.9 81.0 ± 0.1	88.4 87.6 ± 0.0	87.1 84.1 ± 0.0	13.4 10.5 ± 0.1	30.9 41.1 ± 0.1	16.4 ± 0.1	
338	$+MLE$	10.6 ± 0.5	4.8 ± 0.2	2.6 ± 0.1	1.6 ± 1.1	83.6 ± 0.7	88.4 ± 0.2	85.9 ± 0.5	14.3 ± 0.5	32.7 ± 1.1	18.9 ± 0.4	
	$+LoRD$	10.2 ± 0.3	4.5 ± 0.1	2.4 ± 0.1	1.4 ± 0.0	84.1 ± 0.1	88.3 ± 0.1	86.2 ± 0.1	12.8 ± 0.3	33.2 ± 0.9	18.0 ± 0.2	
339												
340	Summarization: CNN Daily Mail (Hermann et al., 2015) with 64 query samples Victim Model 20.4 10.8 6.4 4.1 86.4 87.8 87.1								22.4	40.8	28.2	
	Local Model	4.9 ± 0.0	3.6 ± 0.0	2.7 ± 0.0	2.1 ± 0.0	80.5 ± 0.0	88.3 ± 0.0	84.2 ± 0.0	10.9 ± 0.0	79.1 ± 0.1	18.8 ± 0.0	
341	$+MLE$	5.1 ± 0.5	3.7 ± 0.0	2.8 ± 0.0	2.2 ± 0.0	80.6 ± 0.0	88.3 ± 0.0	84.3 ± 0.0	11.3 ± 0.1	78.6 ± 0.1	19.3 ± 0.1	
	$+LoRD$	5.3 ± 0.0	3.9 ± 0.0	2.9 ± 0.0	2.3 ± 0.0	80.6 ± 0.0	88.4 ± 0.0	84.3 ± 0.0	11.3 ± 0.1	78.6 ± 0.2	19.1 ± 0.1	
342				Summarization: Samsum (Gliwa et al., 2019) with 64 query samples								
	Victim Model	20.7	11.4	6.9	4.4	88.1	91.7	89.8	24.2	50.5	31.6	
343	Local Model	8.9 ± 0.2	5.2 ± 0.1	3.3 ± 0.1	2.1 ± 0.1	80.9 ± 0.2	90.1 ± 0.1	85.2 ± 0.2	17.0 ± 0.3	61.8 ± 0.5	25.5 ± 0.4	
344	$+MLE$	16.9 ± 1.1	9.4 ± 0.7	5.8 ± 0.4	3.7 ± 0.3	83.9 ± 0.9	90.9 ± 0.6	87.3 ± 0.8	25.2 ± 0.8	49.8 ± 2.5	31.0 ± 1.7	
	$+LoRD$	18.4 ± 0.7	10.1 ± 0.3	6.0 ± 0.2	3.7 ± 0.1	84.9 ± 0.1	91.5 ± 0.1	88.1 ± 0.1	23.2 ± 0.8	49.7 ± 1.5	30.2 ± 0.6	
345												

Table 1: MEA comparison on three tasks, including structured text generation, data to text, and summarization. We use GPT-3.5-turbo as the victim model, and Llama3-8B [\(lla, 2024\)](#page-11-8) as the local initial model. The *intensity* of the red or blue color corresponds to the degree of underperformance or outperformance relative to the victim model. More experiments are in Table [2](#page-17-0) and Table [6.](#page-24-0)

351 352 353 354 355 356 Watermark Resistance. Another limitation of prevalent objective functions, such as MLE and KD, is their susceptibility to watermarks [\(Cong et al., 2022;](#page-11-6) [He et al., 2022;](#page-12-3) [2021;](#page-12-4) [Kirchenbauer et al.,](#page-13-5) [2023\)](#page-13-5) of output contents, i.e., while stealing knowledge from LLMs via responses y_{vic} , watermarks within them will also been passively inherited by the local model. Consequently, the generated sentences of the local model may possess some *residual* of watermarks, which might be detected as evidence of stealing.

357 358 359 360 Despite introducing current watermark removal techniques, we indicate that LoRD can mitigate the influences of watermarks naturally, as it does not learn the likelihood of victim models' responses $y_{vic} \sim \mathcal{D}_{tr}$ directly, but relies on y_{vic} to determine positive and negative labels from responses generated by the local model.

361 362 363 364 365 As depicted in Equation [8,](#page-4-0) LoRD guides the local model to learn the likelihood of y_{t-1}^+ instead of y_{vic} , which means that it will not been influenced by watermarks contained in y_{vic} explicitly. However, the regularization term \mathcal{L}_{reg} , as well as the replacement $y_{t-1}^+ \leftarrow y_{vic}$ for a cold start, will indeed introduce watermarks from y_{vic} . To address this, we can reshape Equation [11](#page-4-3) into a convex combination of the objective function and the regularization, i.e.,

366 367 368 $\mathcal{L} = \mathbb{E}[(1 - \lambda_1) \cdot (\log P_{\theta_t}(\mathbf{y}_{t-1}^+|\mathbf{x}) - \log P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})) + \lambda_1 \cdot \operatorname{clip}(\log P_{\theta_t}(\mathbf{y}_{vic}|\mathbf{x}) - \log P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x}))],$ where $0 \leq \lambda_1 \leq 1$ is the hyperparameter.

369 370 371 372 373 374 When λ_1 is small, the convergence of LoRD will substantially focus on maximizing $P_{\theta_t}(\mathbf{y}_{t-1}^+|\mathbf{x})/P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})$, with which the local model will exhibit a strong watermark resistance ability. When λ_1 increases, LoRD will tend to rely more on the guidance of y_{vic} , resulting in a higher risk of introducing watermarks. In the case of $\lambda_1 = 1$, the local model will converge to the victim model without any exploration and watermark resistance, which might suffer from the same level of defense by watermarks.

375 376 377 From a global perspective, \mathcal{L}_{obj} represents the exploration and the locality learning ability of LoRD, which can mitigate the influences of watermarks. On the other hand, \mathcal{L}_{reg} ensures the stability of the training procedure. Therefore, $\mathcal L$ characterizes a trade-off via λ_1 between the stability and the diversity during stealing, and Equation [11](#page-4-3) can be seen as a special case of $\mathcal L$ with $\lambda_1 = 0.5$.

378 5 EXPERIMENTS

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5.1 SETTINGS

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383 384 385 386 387 388 389 390 Datasets. We evaluate MEAs on five mainstream natural language generation (NLG) tasks, including *machine translation*, *text summarization*, *question answering*, *structured text generation*, and *data-totext*. We select ten representative datasets: WMT16 [\(Bojar et al., 2016\)](#page-11-9), TLDR [\(Kirk et al., 2023\)](#page-13-4), CNN Daily Mail [\(Hermann et al., 2015\)](#page-12-7), Samsum [\(Gliwa et al., 2019\)](#page-12-8), WikiSQL [\(Zhong et al., 2017\)](#page-16-2), Spider [\(Yu et al., 2018\)](#page-15-9), E2E-NLG [\(Dušek et al., 2020\)](#page-12-6), CommonGen [\(Lin et al., 2020\)](#page-13-3), PIQA [\(Bisk](#page-11-10) [et al., 2020\)](#page-11-10), and TruthfulQA [\(Lin et al., 2021\)](#page-13-6) as benchmarks for our domain-specific evaluation. These datasets cover most of the downstream tasks in natural language generation. We compare not only the stealing efficacy of different MEA methods, but also the stealing difficulty across different downstream tasks. Table [5](#page-23-1) lists all datasets and backbones used in the paper.

391 392 393 394 395 Baselines. As described in Section [2.2](#page-2-5) and [4.1,](#page-5-5) we compare LoRD with two types of model extraction methods: maximum likelihood estimation (MLE) and knowledge distillation (KD). For MLE and LoRD, we conduct MEAs under pure **black-box attack settings** (see Appendix [D](#page-24-1) for more details of the threat model). For KD, the predicted distributions are used specifically under grey-box settings.

396 397 398 399 Metrics. For text generation tasks, we evaluate extracted models with a semantic-level and two lexical-level metrics, BERTScore [\(Zhang et al., 2020\)](#page-15-10), BLEU [\(Papineni et al., 2002\)](#page-14-7), and Rouge-L [\(Lin, 2004\)](#page-13-7), all of which are commonly used in the NLG evaluation. Regarding reasoning tasks (e.g., QA), we use Precision, Recall, Accuracy, and F1 score as their evaluation metrics.

400 401 402 403 404 405 406 407 408 409 410 Implementation Details. We use Llama3-8B as the local model to learn the outputs generated by victim models. We set sequence length varying 128 to 4096 depending on the selected tasks, and learning rate 3 × 10⁻⁵. Our experiments run on 2 × 80GB Nvidia Tesla A100. We execute each training five times and record the mean values and standard variances in the following sections. For LoRD, we set τ_1 and τ_2 to 0.8 and -0.1, respectively. Besides, we set the period number N_t to 512, and use $\lambda_1 = 0.5$ as the default formation of the loss function. The victim model's response, y_{vic} , is generated by token sampling with a temperature of 1, the default setting for current LLM APIs. The local model also uses token sampling, but with a temperature of 0.8 and Top-P probability clipping [\(Holtzman et al., 2019\)](#page-12-9) at 0.98. We use this setting to enhance the stability of generation in local models. Note that we have not incorporated *sampling strategies* with their corresponding hyperparameters into the design of LoRD. We believe that MEAs considering sampling strategies could inspire more powerful MEA methods, and we leave these improvements for future work.

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5.2 STEALING DOMAIN-SPECIFIC KNOWLEDGE

414 415 416 417 418 419 420 421 422 423 424 425 We first select GPT-3.5-turbo, a checkpoint of ChatGPT, as the basic victim model. This is because its API provides *probabilities* of candidate words when generating responses. We employ Llama3- 8B [\(lla, 2024\)](#page-11-8), a small LLM with only a 4.5% fraction of parameters than the victim model as our initial local model. Though this LaViSH (Large-Victim-Small-Heist) setting contradicts previous assumptions [\(Tramèr et al., 2016;](#page-15-5) [Papernot et al., 2017;](#page-14-0) [Jagielski et al., 2020\)](#page-12-1) in MEA that the copy model should usually be "wider" or "larger" than the victim model to contain its knowledge, we believe this setting is more applicable in real world scenarios [\(Li et al., 2023b\)](#page-13-1). Appendix [D](#page-24-1) provides more detail for this setting. Besides, the number of query times selected in this section is less than 100, a significant degradation compared to previous studies [\(Li et al., 2023b\)](#page-13-1). This is because, in our experiments, copy models can easily learn the knowledge with a few training samples and then exhibit only slight improvements afterward. More discussions on query times can be found in Appendix [A.1.1.](#page-17-1)

426 427 428 429 430 431 Fidelity and limits on stealing. We first examine the fidelity and limits of a small LLM to steal commercial LLMs. As shown in Table [1,](#page-6-0) we list the performance of the victim model and the local model on three tasks, and provide two MEA methods, local model fine-tuned with MLE (+MLE) and LoRD (+LoRD), respectively. In Table [1,](#page-6-0) cells highlighted in *red* indicate poorer outcomes compared to the victim model, whereas *blue* signifies results that are on par or potentially superior to the victim model. The *intensity* of the red or blue color corresponds to the degree of underperformance or outperformance relative to the victim model.

432 433 434 435 436 437 438 439 440 We can see that the original performance of the local model is significantly lower than the victim model, i.e., with a 50% decrease in BLEU-4 or $10 \sim 25$ decrease in Rouge-L. Once we employ MEAs in the local model, its performance rapidly boosts to nearly the same as the victim model, with $0 \sim 40\%$ points of gaps in BERTScore. These gaps are negligible (e.g. $< 1\%$ in summarization) in some tasks, but remain eminent in other tasks such as reasoning, structured text generation, and machine translation. This phenomenon indicates that domain-specific model extractions can effectively learn domain-specific abilities from victim models but may perform poorly if downstream tasks require extra knowledge, such as machine translation and QA. We provide a stealing comparison among different local models in Table [9.](#page-18-0)

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442 Comparison among stealing methods. Tables [1,](#page-6-0) [6,](#page-24-0) and [2](#page-17-0) compare the stealing efficacy be-

443 444 445 446 447 448 449 450 451 452 453 454 455 tween MLE and our LoRD. The results consistently show that LoRD significantly outperforms MLE under the same MEA settings. Besides, for challenging tasks such as reasoning and translation, LoRD exhibits much higher improvements, which demonstrates that it can address the preference overfitting problem discussed in Section [4.2](#page-5-4) and do enable the local model to learn the task ability from victim models. However, we also observe that for some tasks (e.g., summarization), LoRD shows no statistical difference from MLE, probably because these tasks are relatively simple, where merely MLE has already achieved comparable results to victim models.

456 457 458 459 460 461 462 Tasks difficulties comparison. Based on previous analysis, we observe that the performance and limitations of MEA depend on the category of tasks. Additionally, sometimes datasets in the same task exhibit significant differences in stealing. We put forward two metrics to measure task difficulties: the *fidelity* that measures extraction

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Figure 5: Spectrum of the fidelity and performanceup on extracting different downstream tasks. Current datasets can be divided into three groups: high fidelity and high performance-up (HFHP), high fidelity but low performance-up (HFLP), and low fidelity but high performance-up (LFHP).

463 464 465 466 efficacy compared to victim models, and the *performance-up*, which assesses the performance gain before and after stealing for a given local model. Formally, given a test set $\mathcal{D}_{te} = \{(\mathbf{x}, \mathbf{y})\}$ and a corresponding metric $\mathcal{M}(hypothesis, reference)$, the fidelity (F) and performance-up (P) of the local model θ_{N_t} can be defined as:

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P = \frac{\sum\limits_{\mathbf{x},\mathbf{y}\in\mathcal{D}_{te}}\mathcal{M}(\mathbf{y}_{N_t},\mathbf{y})}{\sum\limits_{\mathbf{x},\mathbf{y}\in\mathcal{D}_{te}}\mathcal{M}(\mathbf{y}_{vic},\mathbf{y})}, P = \frac{\sum\limits_{\mathbf{x},\mathbf{y}\in\mathcal{D}_{te}}\mathcal{M}(\mathbf{y}_{N_t},\mathbf{y})}{\sum\limits_{\mathbf{x},\mathbf{y}\in\mathcal{D}_{te}}\mathcal{M}(\mathbf{y}_0,\mathbf{y})},
$$
(12)

470 471 472 473 474 where $\mathbf{y}_{N_t} \sim P_{\theta_{N_t}}(\cdot|\mathbf{x}), \mathbf{y}_0 \sim P_{\theta_0}(\cdot|\mathbf{x}),$ and $\mathbf{y}_{vic} \sim P_{\theta_{vic}}(\cdot|\mathbf{x})$ denote the sampled responses from the trained local model (θ_{N_t}) , the initial local model (θ_0) , and the victim model (θ_{vic}) , respectively. In Figure [5,](#page-8-0) we illustrate a "spectrum" of extracting various downstream tasks based on these two metrics defined in Equation [12.](#page-8-1) The figure can assist in recognizing and defending commercial LLM's knowledge.

475 476 477 From Figure [5,](#page-8-0) we observe five tasks forming the following three scenario groups and datasets coming from the same tasks are mostly in the same group:

- High fidelity and high performance-up (HFHP). These tasks are challenging for a pre-trained model but can be effectively learned with the guidance of victim models. This group includes two tasks: data-to-text and structured text generation.
- High fidelity but low performance-up (HFLP). The initial local model already achieves a comparable performance to the victim model. QAs and summarization are in this group.
- **483 484 485** • Low fidelity but high performance-up (LFHP). While MEAs significantly improve the local model's performance, gaps between the local and victim models remain difficult to bridge with domain-specific extraction alone. Machine translation is a representative task whose reasons are explained in Section [5.2.](#page-7-0)

486 487 5.3 RESISTANCE TO WATERMARKS

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489 490 491 492 493 494 495 496 497 Current LLM watermarking methods have been shown [\(Kirchenbauer et al., 2023\)](#page-13-5) to be robust against commonly used erasing strategies (e.g., rephrasing), making watermark removal a distinct challenge. In this section, we validate the inherent resistance of LoRD to watermarks, suggesting that LoRD is preliminarily resistant to text watermarking. As described in Section [4,](#page-5-0) we highlight that LoRD can extract the victim models' knowledge with two terms: the straightforward likelihood learning term $log P_{\theta_t}(\mathbf{y}_{vic}|\mathbf{x}) - log P_{\theta_t}(\mathbf{y}_{t-1}^{-}|\mathbf{x})$ and the exploration term $log P_{\theta_t}(\mathbf{y}_{t-1}^{+}|\mathbf{x}) - log P_{\theta_t}(\mathbf{y}_{t-1}^{-}|\mathbf{x})$, where we can tune the hyperparameter λ_1 as shown in L to trade off the exploration and the convergence speed. Typically, a lower λ_1 encourages the model for conducting a slower but more diverse and localized exploration from its own generated text y_{t-1}^+ , potentially enhancing watermark resistance. In this subsection, we evaluate this analysis empirically.

498 499 500 501 502 503 504 505 506 507 508 509 510 511 Watermarking Details. Unlike previous experimental settings in Section [5,](#page-7-1) here we cannot utilize commercial LLMs as victim models due to the inability to control token sampling inside LLMs. Instead, we employ Llama3-70B as the victim model and watermark its outputs based on *"green" tokens selection*. Following prior research [\(Kirchenbauer et al., 2023\)](#page-13-5), we separate the predicted vocabulary into a *green word set* and a *red word set* , assigning them randomly with the seed derived from the hash of generated tokens at the last generation step. Subsequently, we sample the next token exclusively from the green set, determined by a certain probability.

512 513 514 515 In this way, given the hypothesis H_0 that *texts are generated without the knowledge of the green word set*, we can estimate the probability H⁰ occurs (*P-value*) and the *Z-score* of it for these texts. A high P-value, among with a low

Figure 6: Comparison of watermarks resistance.

516 517 Z-score, indicates stronger watermark resistance for MEA algorithms.

518 519 520 521 522 523 524 525 526 527 528 Result Analysis. As depicted in Figure [6,](#page-9-0) we evaluate the watermark resistance for both MLE and LoRD, and demonstrate how LoRD's performance varies with different values of λ_1 . The Z-score of LoRD witnesses a consistent increase as λ 1 arises, indicating that the "confidence" in rejecting the hypothesis, i.e., the risk to be suspected, arises when λ_1 increases. This finding coincides with the analysis in Section [4.](#page-5-0) However, $\lambda_1 = 0$ is a *abnormal* point in WMT (de-en), which might be because it disables the regularization term of LoRD's loss function. For tasks the local model does not own enough enough knowledge, it will lead to a significant performance degradation. Besides, we observe that the P-values of LoRD are generally higher than those of MLE when λ_1 is below 0.8, indicating that LoRD typically exhibits stronger watermarking resistance than MLE in most situations. It is noteworthy that this enhanced resistance seems not a "tax" of MEAs efficacy, as the Rouge-L (F1) scores of LoRD consistently surpass those of MLE and do not exhibit a significant negative correlation with their P-values.

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6 CONCLUSION

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535 536 537 538 539 In this paper, we have focused on the extraction problem of commercial large language models. We proposed LoRD, a practical and realistic extraction algorithm which is consistent with the alignment procedure of large language models. Our analysis proved that LoRD can reduce the query time significantly and mitigate the certification of current watermarks naturally, surpassing existing MEA algorithms' capabilities. Extensive experiments on domain-specific stealing demonstrated the superiority of our method.

7 ETHICAL CONSIDERATIONS

 As discussed in Section [1,](#page-0-2) MEAs are becoming increasingly prevalent in industrial settings and have already been executed, yet there remains a critical gap in understanding which specific tasks are more susceptible and what capabilities are necessary for effective executions. This lack of knowledge exacerbates the challenges faced by LLM maintainers in safeguarding their systems. Our research can contribute to that. Besides, the theoretical problem we address (as shown in Section [4\)](#page-5-0) offers a novel and insightful perspective on the nature of this threat. Based on these two points, we believe the benefits of our paper outweigh potential harms, which aligns with the principles of the *Menlo Report* [\(Bailey et al., 2012\)](#page-11-11) on ethics. Additionally, we have submitted an anonymous version of the paper to the maintainers of the victim models used in our study to assist in improving their model security.

 It is important to acknowledge, however, that the algorithms we propose could inadvertently enhance the efficiency of illicit extraction efforts by adversaries. To mitigate this risk, we have introduced and analyzed two defensive strategies in Appendix [8,](#page-10-0) assessing both their effectiveness and potential vulnerabilities under adaptive attack scenarios. This ensures a comprehensive approach to bolstering the security of LLMs.

8 POTENTIAL DEFENSES

 Query Detection. One approach to effectively prevent the attack of LoRD is by detecting the distribution of query texts. This is because LoRD, similar to current MEA algorithms, makes no improvements to query samples, indicating that it can be detected by analyzing the statistical information of the adversary's queries, such as the number of queries, distribution of query contents, and so on. However, this defense is usually resource-consuming, as it requires the LLM provider to store all query texts of each user. Besides, the potential for false positives could adversely affect the user experience.

 More Powerful Watermarks. While we highlight the watermark resistance of LoRD, watermarking remains one of the most effective solutions to mitigate MEAs. For example, some model-level watermarks, such as backdoor-based watermarking [\(Jia et al., 2021;](#page-13-8) [Lv et al., 2024\)](#page-14-8), can effectively certify the theft of DNNs. While model-level (e.g. backdoor-based) watermarks on pre-trained models raised increasing concerns recently [\(Peng et al., 2023a;](#page-14-9) [Gu et al., 2022;](#page-12-10) [Li et al., 2023a\)](#page-13-9), model-level watermarking on LLMs remains preliminary. Besides, this technique might not work when the adversary only steals a subset of knowledge in which no backdoor is embedded.

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Figure 7: Comparison of query efficiency between MLE and LoRD on PiQA, where the *green horizontal line* represents the performance of the initialized local model. We increase query times for each method until reaching their bottlenecks. It can be found that the model extracted by LoRD typically performs a higher accuracy than MLE under the same number of queries. At the same time, LoRD reaches bottlenecks significantly earlier, reducing about 87% query cost compared with MLE.

A SUPPLEMENTAL EXPERIMENTS

A.1 SCALING THE STEALING

937 938 939 940 941 942 943 In this subsection, we explore essential capacities to steal domain-specific knowledge from LLMs. We first analyze the influence of query times for the adversary, then compare the efficacy when utilizing different sizes of the local model, and finally compare the fidelity among different victim and local models.

A.1.1 QUERY TIMES

946 947 948 949 950 951 952 We first investigate the influence of query numbers on MEAs. Specifically, we sample query examples randomly from the query dataset, starting from 4, and incrementally increase it until the performance of the learned model stabilizes. Figure [7](#page-17-2) illustrates the stealing efficacy of LoRD and MLE on PiQA.

We observe that the scores of MLE and LoRD

Table 2: MEA comparison on WMT16 [\(Bojar et al.,](#page-11-9) [2016\)](#page-11-9) among MLE and our LoRD methods, where we use GPT-3.5-turbo as the victim model, and Llama3-8B [\(lla, 2024\)](#page-11-8) as the local initial model.

954 955 956 957 958 959 consistently increase as the query number rises, showing that a larger query number can improve stealing efficacy steadily until reaching their empirical upper bounds. Additionally, LoRD typically obtains a higher score than MLE with the same number of queries, and reaches bottlenecks earlier, which can reduce the required query numbers by 87% compared to MLE. Moreover, in Figure [7,](#page-17-2) the performance of LoRD exhibits a relatively lower standard variance than MLE, indicating a more

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A.1.2 SCALES OF LOCAL MODELS

stable training procedure.

963 964 965 966 967 968 969 As shown in our threat model (see Appendix [D\)](#page-24-1), we assume the adversary is stealing existing commercial LLMs with a small local model. This raises the question of selecting an appropriate interval of the local model's size. To address this concern, we illustrate the correlation between the local model's size and extraction efficacy on two machine translation tasks, Russian-to-English (ru-en) and German-to-English (de-en), as shown in Figure [8.](#page-18-1) Here, we employ seven OPT models [\(Zhang](#page-15-11) [et al., 2022\)](#page-15-11) as local models, with parameters ranging from 125 million to 30 billion, to minimize the interruptions of factors other than model size.

970 971 Figure [8](#page-18-1) shows a sharp distinction between two machine translation tasks. In the de-en task, the performance of the local model increases steadily with model size, while this trend is not evident in the ru-en task with model size smaller than 30 billion. Nevertheless, the performance of a

Figure 8: Experiments varying different model parameter scales.

989 990 991 992 993 994 995 996 997 30 billion parameter learned local model in ru-en cannot even be comparable to that of a 1.3 billion parameter local model in the de-en task. This phenomenon suggests that for tasks requiring commonsense knowledge, such as machine translation, the local model should at least possess foundational knowledge of the task (e.g., pre-trained on Russian texts) to learn from victim models effectively. Besides, experiments in BERTScore (F1) show that sometimes LoRD may underperform MLE when the local model has fewer than 1 billion parameters, demonstrating that it is challenging to bootstrap LoRD's exploration with a very small local model. By summarizing the increase in LoRD's curves, a model with 2.7 billion appears sufficient to steal domain-specific knowledge from commercial LLMs.

A.1.3 FIDELITY UNDER DIFFERENT VICTIM AND LOCAL MODELS

1000 1001 1002 1003 1004 1005 1006 1007 We then evaluate the fidelity of extracting different victim models using various pre-trained local models. Specifically, we select GPT-3.5, GPT-4, and GPT-4o as victim models, and employ five state-of-the-art open-source models, Phi-3 (3.8B), OPT (6.7B), Qwen-2 (7B), Mistral-V3 (7B), and Llama-3 (8B), as local models, as shown in Figure [9.](#page-18-0)

1008 1009 1010 1011 1012 1013 1014 1015 1016 1017 Horizontally, while GPT-4 exhibits a consistently lower extracted fidelity compared to the other two victim models, vulnerabilities of the three victim models are generally similar. Vertically, fidelity of different local models can be significantly impacted by their performance. For instance, OPT (6.7B) shows a noticeably lower score compared to the other four models, which indicates that the initial performance of the local model will affect the performance of MEAs. Besides, Phi-3 (3.8B) achieves a comparable fi-

Figure 9: Fidelity of extracted models with different victim models (GPT-3.5-turbo, GPT-4, and GPT-4o) and different local models (Phi-3, OPT, Qwen2, MistralV3, and Llama3).

1018 1019 1020 delity to larger models like Llama-3 (8B), demonstrating that the size of a local model does not influence final fidelity in domain-specific stealing after 2.7 billion, which corroborates the observation in Appendix [A.1.2.](#page-17-3)

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1022 A.2 VISUALIZATION OF DISTRIBUTIONS

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1024 1025 We also investigate the *probability distributions* in the generation procedure among different extraction methods. Specifically, we visualize these distributions for four models, the victim model (GPT-3.5turbo), the initial local model (llama3-8B), and the learned local models with MLE and LoRD.

1026			DiaSafety			SafeRLHF					
102.	Model	Toxicity	Insult	Profanity	Severe Toxity	Threat	Toxicity	Insult	Profanity	Severe Toxity	Threat
	Llama3-8B (initial)	14.20	7.94	8.35	1.58	າ າດ	7.92		2.80	0.30	.49
1028	+MLE	8.31	3.69	4.31	0.83	.50	4.87	.98	.66	0.16	l.02
	+LoRD	6.45	2.81	3.56	0.71	1.34	3.55		2.84	0.38	0.79

Table 4: Comparison on safety alignment extraction tasks.

1033 1034 1035 1036 1037 1038 As plotted in Figure [10,](#page-19-0) each row in the subfigures refers to the distribution when generating the i-th token, with each column element indicating the *probability* predicted for the corresponding token index. We limit the visualization to no more than five token probabilities as currently only GPT-3.5-turbo provides the token prediction probabilities during generation, with a maximum of 5 candidate tokens [\(ope\)](#page-11-12).

1039 1040 1041 1042 1043 1044 1045 1046 1047 1048 1049 1050 1051 1052 1053 1054 From Figure [10,](#page-19-0) we can see that both MLE and LoRD successfully redistribute the generation of the initial local model into a distribution similar to the victim model's, where probabilities, especially Top-1 tokens, have been well inherited in the extraction. This phenomenon supports our analysis in Proposition [2.](#page-5-3) However, distributions of MLE extracted models are consistently sharper than LoRD's, which aligns with our analysis in Section [4.2,](#page-5-4) where we claim that MLE leads local models to overfit to the preferred sentences (i.e., Top-1 tokens), namely *PO*, and thus to disrupt the original distributions, leveraging unusual low probabilities for other token indexes. The reason why LoRD can be resistant watermarks, i.e., tokens in Top-1, can also be derived from this discovery.

1055 1056 1057 To compare MLE and LoRD accurately, we quantize the *entropy* of these distributions, and compute the KL divergence (\mathbb{D}_{KL}) , and the

Figure 10: Token generation distributions of four models, namely the victim model, the (initial) local model, and the local model learned through LoRD and MLE, respectively. We visualize their logarithmic probability on examples sampled from the train set and test set, where a deeper color indicates a higher probability.

1058 1059 1060 1061 1062 *Spearman Correlation (Spear. Corr.)* with respect to the victim and initial local model. As shown in Table [3,](#page-19-1) while the MLE extracted model exhibits a lower KL divergence (i.e., high distribution similarity) with the victim model than LoRD's on the training dataset, its KL divergence becomes comparable to LoRD's on the test set. Meanwhile, its Spearman correlation significantly decreases from 0.78 to 0.27, which shows that MLE cannot effectively imitate prediction behaviors of the victim model when encountering data beyond the training dataset.

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1065 A.3 STEALING SAFETY ALIGNMENTS

1066 1067 1068 1069 1070 1071 1072 1073 1074 1075 1076 Besides of the domain-specific model extraction, we also propose the safety alignment extraction. Specifically, we select two popular safety alignment datasets for the experiments, namely SafeRLHF [\(Ji et al., 2024\)](#page-13-10) and DiaSafety [\(Sun](#page-15-12) [et al., 2022\)](#page-15-12), to assess the safety of the gener-ated responses. We employed PerspectiveAPI^{[2](#page-0-1)} to automatically evaluate the safety of the responses. We select five key aspects of safety probabilities: Toxicity, Insult, Profanity, Severe Toxicity, and Threat. In these categories, a lower score indicates better safety performance. For

Table 3: Quantization analysis on distributions. A low KL divergence or a high Spearman correlation indicates a high similarity.

1077 1078 the LoRD model, we have retained the same hyper-parameters as those used in our domain-specific experiments to ensure consistency.

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2 https://perspectiveapi.com/

1092 1093 1094 1095 1096 1097 1098 Figure 11: Comparison of learned joint *prediction distributions* among the victim model (a), local models are learned with MLE (b) and LoRD (c). Simply obtaining the tokens from the victim model (solid black squares), MLE may only memorize specific responses and build a complicated decision surface, resulting in *preference overfitting*. In contrast, LoRD further explores the candidate generation paths (dashed arrows and squares) under the guidance of the victim's generation, which is expected to better approximate the victim model in terms of generalization ability, especially under a limited query budget.

1100 1101 1102 As shown in Table [4,](#page-19-2) we can see that both MLE and LoRD significantly reduce the harmful information after the stealing procedure. However, LoRD consistantly outperforms MLE on most of the indicators, suggesting that it can achieve better performance in the alignment task.

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1104 B PROOFS

1106 B.1 PROOFS OF PROPOSITION [1](#page-5-1)

1108 1109 1110 1111 As we described in Section [2,](#page-1-1) both existing methods and LoRD are learned from the victim model's response y_{vic} and the corresponding probability distribution $P_{\theta_{vic}}(\cdot|\mathbf{x}) \in \mathbb{R}^V$, where V denotes the vocabulary size. Therefore, we first investigate how the local model is learned to emulate the distribution of the victim model, $P_{\theta_{vis}}(\cdot|\mathbf{x})$, under the following three stealing strategies.

1112 1113 Expected Distribution of MLE. We can first reshape the MLE loss into a special formation of Kullback-Leibler divergence with labels of one-hot distributions, that is,

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$$
\mathcal{L}_{ce} = -\sum_{\mathbf{x}, \mathbf{y} \sim \mathcal{D}_{tr}} \log P_{\theta}(\mathbf{y}_{vic}|\mathbf{x}) = \sum_{\mathbf{x}, \mathbf{y} \sim \mathcal{D}_{tr}} \sum_{j}^{N} \mathbb{D}_{KL}[\mathbf{1}_{y_{vic,j}} || P_{\theta}(\cdot|\mathbf{x}, \mathbf{y}_{vic,(13)
$$

1117 1118 1119 where $\mathbf{1}_{y_{vic,j}}$ is a one-hot vector in which only $\mathbf{1}_{y_{vic,j}}[y_{vic,j}] = 1$ and all the other elements are 0. Equation [13](#page-20-2) demonstrates that MLE learns to maximize the probability of $y_{vic,j}$, without explicit constraints on probabilities across other dimensions.

1120 1121 1122 Expected Distribution of KD. Following a previous work [\(Hinton et al., 2015\)](#page-12-11), the objective function of KD is

$$
\mathcal{L}_{kd} = \mathbb{D}_{KL}[P_{\theta_{vic}}(\cdot|\mathbf{x})||P_{\theta}(\cdot|\mathbf{x})] + T^2 \cdot \mathbb{D}_{KL}[\text{SM}(P_{\theta_{vic}}(\cdot|\mathbf{x})/T)||\text{SM}(P_{\theta}(\cdot|\mathbf{x})/T)],\tag{14}
$$

1123 1124 1125 1126 1127 where $SM(\cdot)$ represents the *softmax function*, and $T > 1$ denotes the temperature to smooth the targeted distribution $P_{\theta_{vis}}(\cdot|\mathbf{x})$. As described in Equation [14,](#page-20-3) knowledge distillation aims to align $P_{\theta}(\cdot|\mathbf{x})$ with $P_{\theta_{vis}}(\cdot|\mathbf{x})$ in both the original and the smoothed probability across all dimensions, which is exceptionally comprehensive among these methods.

1128 1129 Expected Distribution of Alignments. Replacing Equation [6](#page-2-3) with Equation [5,](#page-2-4) we can merge the optimization target of LLMs' alignments as

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\n
$$
\min_{\theta*} - \sum_{(\mathbf{x}, \mathbf{y}^+, \mathbf{y}^-) \sim \mathcal{D}^{pref}} \sigma \left(\log \frac{P_{\theta*}(\mathbf{y}^+|\mathbf{x})/P_{\theta*}(\mathbf{y}^-|\mathbf{x})}{P_{\theta_{init}}(\mathbf{y}^+|\mathbf{x})/P_{\theta_{init}}(\mathbf{y}^-|\mathbf{x})} \right)
$$
\n(15)

$$
\Rightarrow \max_{\theta*} \sum_{(\mathbf{x}, \mathbf{y}^+, \mathbf{y}^-) \sim \mathcal{D}^{pref}} \log P_{\theta*}(\mathbf{y}^+|\mathbf{x}) - \log P_{\theta*}(\mathbf{y}^-|\mathbf{x}),
$$

1134 1135 where θ ^{*} denotes the expected parameters of the models as

$$
P_{\theta*}(\mathbf{y}|\mathbf{x}) = \frac{1}{Z(x)} P_{\theta_{init}}(\mathbf{y}|\mathbf{x}) \cdot e^{\frac{1}{\beta}R_{\phi}(\mathbf{x}, \mathbf{y})}.
$$
 (16)

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1139 1140 1141 1142 We provide a detailed derivation for Equation [16](#page-21-0) in Appendix [B.2.](#page-21-1) By replacing Equation [15](#page-20-4) with Equation [16,](#page-21-0) the expected distribution can be represented as $\mathbf{r}_{i,j} \cdot P_{\theta_{init}}(\cdot|\mathbf{x})$, in which $\mathbf{r}_{i,j}$ indicates the wrapped distribution gain. This distortion aims to maximize the ratio $P_\theta(y_j^+|\mathbf{x}, \mathbf{y}_{< j}^+) / P_\theta(y_j^-|\mathbf{x}, \mathbf{y}_{< j}^-)$, and leave the probabilities in other dimensions unconstrained directly.

1143 1144 1145 1146 1147 1148 1149 Expected Distribution of LoRD. Similar to alignments, the expected converging procedure by the objective function \mathcal{L}_{obj} is also intended to maximize the ratio between positive samples and negative samples, i.e., $P_{\theta_t}(\mathbf{y}_{t-1}^+|\mathbf{x})/P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})$. Meanwhile, the regularization term $P_{\theta_t}(\mathbf{y}_{vic}|\mathbf{x})/P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})$ will guide the models to maximize the ratio between y_{vic} and y_{t-1}^- . As the "standard response" to be learned, y_{vic} can be viewed sufficiently as a positive example. Therefore, we can derive that the optimization target of LoRD is consistent with RLHF's optimization, i.e., both encourage local models to maximize the probability proportion between positive and negative samples.

1150 1151 1152 1153 1154 1155 Similar to Equation [16](#page-21-0) in which the optimized model can be seen as the distortion of the original model $P_{\theta_{init}}$, in LoRD the optimized model can be regarded as the distortion of the local model P_{θ_0} , with $P_{\theta_t}(\cdot|\mathbf{x}) = \mathbf{r}_{i,j}^t P_{\theta_{t-1}}(\cdot|\mathbf{x})$ at each step t, where the distortion term $\mathbf{r}_{i,j}^t$ is intended to jointly maximize $P_{\theta_t}(\mathbf{y}_{t-1}^+|\mathbf{x})/P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})$ and $P_{\theta_t}(\mathbf{y}_{vic}|\mathbf{x})/P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})$, while leaving the probabilities in other dimensions unconstrained directly.

1156 1157 B.2 THE DEDUCTION OF EQUATION [16](#page-21-0) IN PROPOSITION [1](#page-5-1)

1158 From Equation [6,](#page-2-3) we can get that

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$$
\frac{\log \sum_{\mathbf{x} \sim \mathcal{D}_q} R_{\theta_{\phi}}(\mathbf{x}, \hat{\mathbf{y}}) - \beta \mathbb{D}_{KL}[P_{\theta}(\mathbf{y}|\mathbf{x})||P_{\theta_{init}}(\mathbf{y}|\mathbf{x})]
$$
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$$
\frac{\partial}{\partial} \sum_{\mathbf{x} \sim \mathcal{D}_q} \sum_{\mathbf{y} \sim P_{\theta}(\cdot|\mathbf{x})} -\frac{1}{\beta} R_{\theta_{\phi}}(\mathbf{x}, \mathbf{y}) + \log \frac{P_{\theta}(\mathbf{y}|\mathbf{x})}{P_{\theta_{init}}(\mathbf{y}|\mathbf{x})}
$$
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1173 If we define a partition function $Z(\mathbf{x})$ with the formation of

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$$

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$$

 $Z(\mathbf{x}) = \sum$ y $P_{init}(\mathbf{y}|\mathbf{x})$ exp $(\frac{1}{\varphi})$ $\frac{1}{\beta}R_{\theta_{\phi}}(\mathbf{x}, \mathbf{y})),$ (17)

1178 we can reformat the optimization target as

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$$

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$$
\min_{\theta} \sum_{\mathbf{x} \sim \mathcal{D}_q} \sum_{\mathbf{y} \sim P_{\theta}(\cdot \mid \mathbf{x})} \log \frac{P_{\theta}(\mathbf{y} \mid \mathbf{x})}{\exp(\frac{1}{\beta} R_{\theta_\phi}(\mathbf{x}, \mathbf{y})) \cdot P_{\theta_{init}}(\mathbf{y} \mid \mathbf{x})}
$$

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$$
\Rightarrow \min_{\theta} \sum_{\mathbf{x} \sim \mathcal{D}_q} \sum_{\mathbf{y} \sim P_{\theta}(\cdot | \mathbf{x})} \log \frac{Z(\mathbf{x}) \cdot P_{\theta}(\mathbf{y} | \mathbf{x})}{\exp(\frac{1}{\beta} R_{\theta_{\phi}}(\mathbf{x}, \mathbf{y})) \cdot P_{\theta_{init}}(\mathbf{y} | \mathbf{x})}
$$

$$
1185 - 4J \cdot 16 \cdot |x\rangle - \log Z(\mathbf{x}).
$$

If we mark $\frac{1}{Z(\mathbf{x})} \exp(\frac{1}{\beta} R_{\theta_{\phi}}(\mathbf{x}, \mathbf{y})) \cdot P_{\theta_{init}}(\mathbf{y}|\mathbf{x})$ as $P_{\theta *}(\mathbf{y}|\mathbf{x})$, then we have

$$
\begin{array}{c} 1189 \\ 1190 \end{array}
$$

$$
\min_{\theta} \sum_{\mathbf{x} \sim \mathcal{D}_q} \sum_{\mathbf{y} \sim P_{\theta}(\cdot \mid \mathbf{x})} \log \frac{Z(\mathbf{x}) \cdot P_{\theta}(\mathbf{y} \mid \mathbf{x})}{\exp(\frac{1}{\beta} R_{\theta_\phi}(\mathbf{x}, \mathbf{y})) \cdot P_{\theta_{init}}(\mathbf{y} \mid \mathbf{x})} - \log \! Z(\mathbf{x})
$$

$$
\begin{array}{c} 1191 \\ 1192 \end{array}
$$

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$$
\Rightarrow \min_{\theta} \sum_{\mathbf{x} \sim \mathcal{D}_q} \sum_{\mathbf{y} \sim P_{\theta}(\cdot|\mathbf{x})} \log \frac{P_{\theta}(\mathbf{y}|\mathbf{x})}{P_{\theta*}(\mathbf{y}|\mathbf{x})} - \log Z(\mathbf{x}).
$$

1195 Because $Z(\mathbf{x})$ is independent to y, we can deduct that

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$$
\min_{\theta} \sum_{\mathbf{x} \sim \mathcal{D}_q} \sum_{\mathbf{y} \sim P_{\theta}(\cdot | \mathbf{x})} \log \frac{P_{\theta}(\mathbf{y} | \mathbf{x})}{P_{\theta*}(\mathbf{y} | \mathbf{x})} - \log Z(\mathbf{x})
$$
\n
$$
\Rightarrow \min_{\theta} \sum_{\mathbf{x} \sim \mathcal{D}_q} \left[\sum_{\mathbf{y} \sim P_{\theta}(\cdot | \mathbf{x})} \log \frac{P_{\theta}(\mathbf{y} | \mathbf{x})}{P_{\theta*}(\mathbf{y} | \mathbf{x})} \right] - \log Z(\mathbf{x}) \tag{18}
$$
\n
$$
\Rightarrow \min_{\theta} \sum_{\mathbf{x} \sim \mathcal{D}_q} \mathbb{D}_{KL}[P_{\theta}(\mathbf{y} | \mathbf{x}) || P_{\theta*}(\mathbf{y} | \mathbf{x})] - \log Z(\mathbf{x}).
$$

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1207 1208 1209 As we know that $Z(x)$ does not contain θ , the above optimization target actually minimizes the KL-divergence between the distribution of P_θ and $P_{\theta*}$, demonstrating that $\theta*$ is the optimal value of θ that satisfies

 $\mathbf{x} \sim \mathcal{D}_q$

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$$
P_{\theta*}(\mathbf{y}|\mathbf{x}) = \frac{1}{Z(\mathbf{x})} \exp(\frac{1}{\beta} R_{\theta_{\phi}}(\mathbf{x}, \mathbf{y})) \cdot P_{\theta_{init}}(\mathbf{y}|\mathbf{x}).
$$
\n(19)

,

1214 1215 Based on equation [19,](#page-22-0) we can see that the optimal distribution of θ is built upon $P_{\theta_{init}}$ with a distortion, as we discussed in Section [4.1.](#page-5-5)

1217 B.3 PROOFS OF PROPOSITION [2](#page-5-3)

1219 1220 Guarantee of MLE. From Equation [13](#page-20-2) we can obtain that when \mathcal{L}_{ce} decreases to 0, the KL divergence between $P_{\theta}(\cdot|\mathbf{x})$ and $P_{\theta_{vis}}(\cdot|\mathbf{x})$ decreases to 0, indicating that $P_{\theta}(\cdot|\mathbf{x})$ equals to $P_{\theta_{vis}}(\cdot|\mathbf{x})$.

1221 1222 1223 1224 Guarantee of KD. As we know, $\mathbb{D}_{KL}(p,q) \geq 0 \ \forall \ p$ and q. Therefore, if \mathcal{L}_{kd} shown in Equation [14](#page-20-3) equals to 0, then both $\mathbb{D}_{KL}[P_{\theta}(\cdot|\mathbf{x})||P_{\theta_{visc}}(\cdot|\mathbf{x})]$ and $\mathbb{D}_{KL}[\text{SM}(P_{\theta}(\cdot|\mathbf{x})/T)||\text{SM}(P_{\theta_{visc}}(\cdot|\mathbf{x})/T)]$ equal to 0. For the latter one, we have

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$$
\mathbb{D}_{KL}[\text{SM}(P_{\theta_{vis}}(\cdot|\mathbf{x})/T)||\text{SM}(P_{\theta}(\cdot|\mathbf{x})/T)]
$$
\n
$$
= \mathbb{E}_{\mathbf{y} \sim P_{\theta_{vis}}(\cdot|\mathbf{x})} \mathbb{E}_{y \in \mathbf{y}} \left[\log \frac{\exp(P_{\theta}(y|\mathbf{x}, \mathbf{y}_p)/T)/\sum_{y' \in \mathbf{y}} \exp(P_{\theta_{vis}}(y|\mathbf{x}, \mathbf{y}_p)/T)}{\exp(P_{\theta_{vis}}(y|\mathbf{x}, \mathbf{y}_p)/T)/\sum_{y' \in \mathbf{y}} \exp(P_{\theta}(y|\mathbf{x}, \mathbf{y}_p)/T)} \right]
$$
\n
$$
= \mathbb{E}_{\mathbf{y} \sim P_{\theta_{vis}}(\cdot|\mathbf{x})} \mathbb{E}_{y \in \mathbf{y}} \left[\log \frac{\exp((P_{\theta}(y|\mathbf{x}, \mathbf{y}_p) - P_{\theta_{vis}}(y|\mathbf{x}, \mathbf{y}_p))/T)}{\sum_{y' \in \mathbf{y}} \exp(P_{\theta_{vis}}(y|\mathbf{x}, \mathbf{y}_p)/T)/\sum_{y' \in \mathbf{y}} \exp(P_{\theta}(y|\mathbf{x}, \mathbf{y}_p)/T)} \right]
$$

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1232 1233 1234 where we can observe that only when $P_{\theta}(\cdot|\mathbf{x})$ equals to $P_{\theta_{vic}}(\cdot|\mathbf{x})$ can this term reduce to 0. Integrating the analysis of these two terms, we can obtain that $\mathcal{L}_{kd} = 0$ represents the local model's distribution converge to that of the victim model.

1235 1236 1237 1238 1239 1240 1241 Guarantee of LoRD. When $\mathcal L$ shown in Equation [11](#page-4-3) equals to 0, the proportion of $P_{\theta_t}(\mathbf{y}_{vic}|\mathbf{x})/P_{\theta_t}(\mathbf{y}_{t-1}^{-}|\mathbf{x})$ and $P_{\theta_t}(\mathbf{y}_{t-1}^{+}|\mathbf{x})/P_{\theta_t}(\mathbf{y}_{t-1}^{-}|\mathbf{x})$ should limit to $-\infty$. As we know that *i*) in a distribution $\sum P_{\theta_t}(\cdot|\mathbf{x}) = 1$ and *ii*) \mathbf{y}_{t-1}^+ is a dynamic positive response generated at each period, we can deduct that when $\mathcal{L} = 0$ there must be $y_{vic} = y_{t-1}^+$, i.e., $P_{\theta_t}(y_{vic}|\mathbf{x}) = P_{\theta_t}(y_{t-1}^+|\mathbf{x}) = 1$ and $P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x}) = 0$. Note that this is merely a theoretical limit that cannot be reached, because $\mathbf{y}_{t-1}^$ will not be sampled if its probability is 0, and y_{t-1}^+ usually doesn't exhibit a significant distinction to y_{t-1}^- when sampling.

Table 5: Datasets and pre-trained model checkpoints used in the paper.

1259 C SUPPLEMENTAL RELATED WORKS

1261 C.1 HUMAN-FEEDBACK-FREE ALIGNMENTS

1263 1264 1265 1266 1267 1268 1269 There are several alternatives to the standard RLHF approach. [Lee et al.](#page-13-11) [\(2023\)](#page-13-11) propose reinforcement learning with AI feedback (RLAIF) as a means to diminish the annotation burden associated with the preference assessments. Besides, there are some approaches, such as direct preference optimization (DPO) [\(Rafailov et al., 2023\)](#page-14-6), that conceptualize the language model itself as the reward model and thus consolidate Equation [5](#page-2-4) and Equation [6](#page-2-3) into a unified supervised and preference-based training task. Since they do not change the primary targets (i.e., maximizing rewards) and optimization strategies of LLM's alignments, we only consider the standard formation of alignments for simplicity in our theoretical analysis.

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1272 C.2 LANGUAGE MODELS EXTRACTION

1273 1274 1275 1276 Studies to steal language models originated from the natural language understanding (NLU) models, such as BERT[\(Devlin et al., 2019\)](#page-12-12), and then evolved to generative language models, especially large language models recently.

1277 1278 1279 1280 1281 1282 1283 [Krishna et al.](#page-13-0) [\(2020\)](#page-13-0) highlights early recognition of model extraction threats in language models. By constructing text inputs with randomly vocabulary sampling, they successfully extract the weights from BERT-based APIs. Besides, [Rafi et al.](#page-15-0) [\(2022\)](#page-15-0) investigate the feasibility of side-channel model extraction attacks, revealing that by analyzing extra signals from GPU kernels, one could accurately steal the model architecture and its parameters. Subsequent research [\(Xu et al., 2022\)](#page-15-1) has thoroughly investigated the strategy of ensembling victim models to train a competitor model that surpasses its teachers.

1284 1285 1286 1287 1288 1289 1290 1291 1292 1293 1294 1295 The exploration of generative language model extraction is still in its infant stage, with only a handful of studies thus far. [Wallace et al.](#page-15-6) [\(2020\)](#page-15-6) investigate imitation attacks on natural language models. By designing monolingual query texts and collecting responses, they successfully extract the knowledge from a simulated machine translation model under the black-box settings. This research exhibits that slight architectural differences will not influence the extraction between language models. [Li](#page-13-1) [et al.](#page-13-1) [\(2023b\)](#page-13-1) also explores the potential risks of stealing the code-generation abilities of LLMs into smaller downstream models. Unlike previous research [\(Wallace et al., 2020\)](#page-15-6), this is the first study that selects LLMs as targets. By collecting large-scale domain-specific samples, they fine-tune a 7-billion local pre-trained model with them and show the similarity between the victim and local models in both performances and adversarial samples. However, these two studies employ the MLE loss (Equation [3\)](#page-2-1) as the MEA method, neither considering whether MLE is compatible with LLMs's training, especially the alignment procedure shown in Section [2.2,](#page-2-5) nor addressing optimizations related to query efficiency and the watermark resistance. Besides, the scope of these studies is limited to stealing specific knowledge in a few downstream domains. At the same time, most of the critical

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	Model/Metric	Accuracy	Precision	Recall	F1 Score						
1297	PIQA (Bisk et al., 2020) with 64 query samples										
1298	Victim Model	0.828	0.828	0.827	0.827						
1299	Local Model	0.622	0.638	0.621	0.609						
	+MLE (baseline)	0.760 ± 0.02	0.771 ± 0.01	0.760 ± 0.02	0.757 ± 0.03						
1300	$+KD$ (gre-box)	0.759 ± 0.02	0.760 ± 0.02	0.759 ± 0.02	0.759 ± 0.02						
1301	$+LoRD$ (ours)	0.785 ± 0.01	0.795 ± 0.01	0.785 ± 0.01	0.783 ± 0.02						
1302	TruthfulOA (Lin et al., 2021) with 64 query samples										
	Victim Model	0.414	0.500	0.207	0.293						
1303	Local Model	0.391	0.500	0.195	0.281						
1304	+MLE (baseline)	0.381 ± 0.17	0.500 ± 0.00	0.190 ± 0.09	0.266 ± 0.09						
1305	$+KD$ (gre-box)	0.463 ± 0.03	0.500 ± 0.00	0.232 ± 0.01	0.316 ± 0.01						
1306	$+LoRD$ (ours)	0.408 ± 0.05	0.500 ± 0.00	0.204 ± 0.03	0.289 ± 0.03						

1307 1308 Table 6: MEA comparison on QA tasks among MLE and our LoRD methods, where we use GPT-3.5 turbo as the victim model, and Llama3-8B [\(lla, 2024\)](#page-11-8) as the local initial model.

1311 1312 aspects of LLMs and the required extraction capabilities, such as query numbers and local model scales, remain unresolved.

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1314 C.3 TEXT WATERMARKS

1315 1316 1317 1318 1319 1320 1321 1322 1323 In contrast to stealing LLMs, IP protection methods have received considerable attention recently. By sampling a stealthy but representative "greed word set" on the vocabulary distribution, these methods [\(Cong et al., 2022;](#page-11-6) [He et al., 2022;](#page-12-3) [2021;](#page-12-4) [Kirchenbauer et al., 2023\)](#page-13-5) can remap the generated words into their synonyms or add the "watermarked" token automatically, and thus effectively certify the output. Besides, strategies such as integrating embeddings into the representation as the backdoor [\(Peng et al., 2023b\)](#page-14-10) or manipulating the probabilities with crafted sinusoidal noises [\(Zhao et al.,](#page-16-1) [2022;](#page-16-1) [2023\)](#page-16-3) are also proposed. However, these approaches often presume more stringent conditions regarding the victim and the suspected models. This paper will further assess the effectiveness of LoRD and current MEAs in evading these black-box watermarking strategies.

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1325 D A DETAILED THREAT MODEL

1327 1328 1329 1330 1331 1332 Adversary's Objective. The adversary's objective is to steal the targeted knowledge from LLMs. Specifically, we select machine translation, reasoning, data-to-text, structured text generation, and summarization as the downstream domain-specific tasks. The adversary aims to develop a *queryefficient* MEA algorithm, since the amount of input and generated tokens will be counted as the costs. Additionally, the MEA methods are expected to be *watermark-resistant*, i.e., they are highly desired to reduce the risks of exposure to unauthorized stealing.

1333 1334 1335 1336 1337 1338 Targeted Models. We select Llama3-70B, GPT-3.5-turbo, and GPT-4o as the victim models in this paper. Unlike previous works that only deployed simulated local victim models (e.g., OPT [\(Zhang](#page-15-11) [et al., 2022\)](#page-15-11)), our selections aim to expose the stealing threat on realistic AI services. Besides, our target models are specifically constrained to LLMs fine-tuned with alignment methods (e.g., RLHF) since they are not only state-of-the-art solutions now but also more valuable due to their human-based alignments.

1339 1340 1341 1342 1343 1344 1345 Adversary's Capabilities. In accordance with the LLM-based AI service APIs, we identify two attack scenarios: black-box and grey-box attacks. In the black-box scenario, only textual responses the adversary is allowed to obtain. At the same time, all other information, such as the temperature, sampling strategies, and the hidden states of LLMs, are unseen and inaccessible. On the contrary, a grey-box attack allows the adversary to access the generation probabilities distribution of tokens. Notice that both MLE and our LoRD method are under black-box settings, and we only adopt grey-box settings on some particular stealing methods, such as knowledge distillation.

1346 1347 1348 1349 Besides, this paper posits that the adversary usually has worse training conditions than the victims. Specifically, query times and the scale of the local model available to the adversary are much smaller than the victims' training datasets and model parameters. This setting has been adopted in previous LLMs' extraction [\(Li et al., 2023b\)](#page-13-1). We call it a LaViSH (Large-Victim-Small-Heist) framework, which allows us to estimate the upper bound of MEA risks empirically. For adversaries with more

 Task Instruction
WMT16 Please tran WMT16 Please translate the sentence from [source language] to English.
PiQA & TruthfulQA Please select the correct answer for the "Question" of Users. Qu Please select the correct answer for the "Question" of Users. Question: [question] Selection 1: [Selection1] Selection 2:[Selection2]. E2E NLG Please translate the information to a sentence in natural language. CommonGen Please generate a sentence based on the words provided by Users.
WikiSQL& Spider Please return to me the SQL sentence based on the text (i.e., Ques Please return to me the SQL sentence based on the text (i.e., Question) and the table information (i.e., Table) provided by the User. TLDR& SamSUM | Please **summarize** the content given by the user. CNN Daily Mail Please **summarize** the content given by the user. Table 7: Instructions used in the different downstream datasets. substantial resources, they can train more powerful MEA-based LLMs by leveraging MEA algorithms under our LaViSH settings. E LIMITATIONS AND FUTURE WORKS MEAs on Multi-modal Models. While this paper delves into MEAs for large language models, it acknowledges the oversight of the multi-modal attribution of current commercial models [\(Anil et al.,](#page-11-1) [2024;](#page-11-1) [Achiam et al., 2024\)](#page-11-13) that integrate various forms of data such as text, images, voice, and so on. The challenge of extending MEA algorithms to accommodate these models, which requires extra considerations on the unified representation of concepts, remains unexplored. Future work could focus on developing MEA methodologies sensitive to multi-modal data nuances. Capacities beyond LaViSH Settings. We utilize the LaViSH setting to describe the model capacity of adversaries in our threat model (see Appendix [D\)](#page-24-1). However, sometimes, the adversary might possess comparable or superior training resources to the victims. Though this paper posits that our MEA algorithms and theoretical analysis are still compatible with such conditions, we concede that concrete experimental validation and results beyond LaViSH settings are not presented here. Lower-level Extractions. This study evaluates MEAs at the performance level, i.e., it measures the extraction effectiveness simply through task performance metrics, or the similarity of learned distributions to the victim model. This setting is justified, as performance metrics are essential for evaluating task-related knowledge and the practical application of LLMs. However, it does not consider the lower-level similarities between the victim and local models. Can we achieve neuronlevel alignments in LLM's MEAs? How does a LaViSH setting hurt LLM's MEAs? Is it compatible to extract a MoE (Mix-of-the-Expert) [\(Shazeer et al., 2017\)](#page-15-13) victim model with a dense local model? These questions are not addressed in this research.

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1405 1406 1407 1408 1409 1410 1411 1412 1413 1414 1415 1416 1417 1418 1419 1420 1421 1422 1423 1424 1425 1426 1427 1428 1429 1430 1431 1432 1433 1434 1435 1436 1437 1438 1439 1440 1441 1442 1443 1444 1445 1446 1447 1448 1449 1450 1451 1452 1453 Algorithm 1 LoRD Algorithm 1: **Input:**Query dataset \mathcal{D}_q , local language model θ_{init} , interface of the victim model $P_{\theta_{vic}}(\cdot|\cdot)$, train period number N_t , threshold values τ_1 and τ_2 . 2: // Initialization. 3: $\theta_0 \leftarrow \theta_{init}, \mathcal{D}_{tr} \leftarrow \emptyset, \mathcal{D}_0^+ \leftarrow \emptyset, \mathcal{D}_0^- \leftarrow \emptyset, t \leftarrow 0;$ 4: // Query the victim model. 5: for $\mathbf{x} \sim \mathcal{D}_q$ do 6: $\mathbf{y}_{vic} \leftarrow P_{\theta_{vic}}(\cdot|\mathbf{x});$ 7: $\mathcal{D}_{tr} \leftarrow \mathcal{D}_{tr} \cup \{(\mathbf{x}, \mathbf{y}_{vic}, P_{\theta_{vic}}(\mathbf{y}_{vic}|\mathbf{x}))\};$ 8: end for 9: // Train local model. 10: // Initialize the positive and negative datasets. 11: $\mathcal{D}_0^+ \leftarrow \mathcal{D}_q$; 12: for $(\mathbf{x}, \mathbf{y}_{vic}, P_{\theta_{vic}}(\mathbf{y}_{vic}|\mathbf{x})) \sim \mathcal{D}_{tr}$ do $13:$ $\overline{\rho}_0 \sim P_{\theta_t}(\cdot | \mathbf{x});$ 14: $\mathcal{D}_0^- \leftarrow \mathcal{D}_0^- \cup \{ (\mathbf{x}, \mathbf{y}_0^-, P_{\theta_0}(\mathbf{y}_0^-|\mathbf{x})) \};$ 15: end for 16: while $t < N_t$ do 17: $t \leftarrow t + 1;$ 18: $\theta_t \leftarrow \theta_{t-1};$
19: **for** (**x**, **y**_{vic} for $(\mathbf{x}, \mathbf{y}_{vic}, P_{\theta_{vic}}(\mathbf{y}_{vic}|\mathbf{x})) \sim \mathcal{D}_{tr}$ do $20:$ $t^+, \mathbf{y}_t^- \sim P_{\theta_t}(\cdot|\mathbf{x});$ $21:$ $t_t^+ \leftarrow \mathcal{D}_t^+ \cup \{(\mathbf{x}, \mathbf{y}_t^+)\};$ $22:$ $\overline{t}_t^- \leftarrow \mathcal{D}_t^- \cup \{(\mathbf{x}, \mathbf{y}_t^-)\};$ 23: end for 24: // Forward. 25: **for x**, $\mathbf{y}_{vic}, \mathbf{y}_{t-1}^+, \mathbf{y}_{t-1}^- \sim (\mathcal{D}_{tr}, \mathcal{D}_{t-1}^+, \mathcal{D}_{t-1}^-)$ **do** 26: $\Delta^+ \leftarrow \log P_{\theta_t}(\mathbf{y}_{t-1}^+ | x) - \log P_{\theta_{t-1}}(\mathbf{y}_{t-1}^+ | x);$ 27: $\Delta^- \leftarrow \log P_{\theta_t}(\mathbf{y}_{t-1}^- | x) - \log P_{\theta_{t-1}}(\mathbf{y}_{t-1}^- | x);$ 28: **if** $\Delta^+ < \Delta^-$ then 29: $swap(y_{t-1}^+, y_{t-1}^-);$ 30: swap $(\Delta^+, \Delta^-);$ 31: end if 32: **if** $P_{\theta_t}(\mathbf{y}_{t-1}^+ | x) < \tau_1 \&\& \Delta^+ < \tau_2$ then $33:$ $t_{t-1}^+ \leftarrow \mathbf{y}_{vic};$ 34: end if 35: // Compute loss with Equation [10](#page-4-2) or [11.](#page-4-3) 36: $\mathcal{L} \leftarrow \log[\frac{P_{\theta_t}(\mathbf{y}_{t-1}^-|\mathbf{x})}{P_{\theta_t}(\mathbf{x}_t^+|\mathbf{x})}]$ $\frac{P_{\theta_t}(\mathbf{y}_{t-1}^{-}|\mathbf{x})}{P_{\theta_t}(\mathbf{y}_{t-1}^{+}|\mathbf{x})}]+clip(\text{log}[\frac{P_{\theta_t}(\mathbf{y}_{t-1}^{-}|\mathbf{x})}{P_{\theta_t}(\mathbf{y}_{\text{vic}}|\mathbf{x})}]$ $\frac{\theta_t(\mathbf{y}_{t-1}|\mathbf{x})}{P_{\theta_t}(\mathbf{y}_{\text{vic}}|\mathbf{x})})$; 37: // Backward. 38: $\theta_t \leftarrow \text{stepUpdate}(\theta_t, \mathcal{L});$
39: **end for** end for 40: end while 41: return θ_t

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