

Influence-driven Curriculum Learning for Pre-training on Limited Data

Anonymous ACL submission

Abstract

Curriculum learning, a training technique where data is presented to the model in order of example difficulty (e.g., from simpler to more complex documents), has shown limited success for pre-training language models. In this work, we investigate whether curriculum learning becomes competitive if we replace conventional human-centered difficulty metrics with one that more closely corresponds to example difficulty as observed during model training. Specifically, we experiment with sorting training examples by their *training data influence*, a score which estimates the effect of individual training examples on the model’s output. Models trained on our curricula are able to outperform ones trained in random order by over 10 percentage points in benchmarks, confirming that curriculum learning is beneficial for language model pre-training, as long as a more model-centric notion of difficulty is adopted.

1 Introduction

Curriculum learning, a training paradigm where the training data is presented to the model in non-random order (Bengio et al., 2009), has recently been explored extensively as a pretraining strategy for language models due to its potential to improve performance in low-resource settings (Timiryasov and Tastet, 2023), reduce training time (Platanios et al., 2019), or to make the training process more data-efficient and developmentally plausible (i.e., more similar to how humans acquire language; Warstadt et al., 2023a; Hu et al., 2024). A popular form of curriculum learning relies on heuristics that **sort training data by increasing difficulty** (e.g., lexical diversity trough type-token ratio: Mi, 2023). However, in low-resource language modeling, approaches that incorporate this curriculum learning strategy have not yielded the anticipated improvements and show no consistent positive effect on model performance (Hu et al., 2024). In this

work, we therefore investigate whether curriculum learning becomes competitive for language model pretraining, if we replace human-centered difficulty measures with one that better reflects training dynamics. Specifically, we derive a novel form of curriculum from **training data influence estimates**, that we obtain from a surrogate model trained with randomly ordered data: These estimates assign documents from the training data scores proportional to their impact on the model’s output. We adapt a *gradient similarity-based* influence score (Pruthi et al., 2020), where influence is measured by comparing loss-gradients of training and test instances, with higher similarity signifying greater influence. We experiment with 10 different sorting

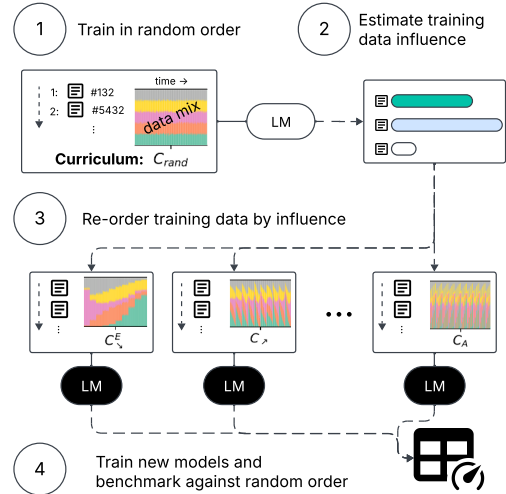


Figure 1: In our method, we extract training data influence estimates from models trained in random order, to create better-performing curricula.

strategies, all based on the **average influence** that a given training example exerts on the prediction of *other* examples sampled from the training data. We compare model performance under these curricula to both random training and curriculum learning using three human-centered difficulty heuristics. Through experiments with RoBERTa- (Liu et al.,

2019) and Llama models (Touvron et al., 2023), we demonstrate that our approach is more effective than handcrafted curricula, and analyze what ranking and coverage strategies are most effective. We find that source-difficulty curricula, a popular human-centered design that arranges datasets by their difficulty, are ineffective compared to alternative dataset coverage strategies, and we offer insights into the reasons for their low performance. Our **main contributions** are as follows:¹

- (1) We demonstrate that our curricula yield an increase of over 10 percentage points (pp) in accuracy for RoBERTa- and over 4 pp for Llama models on a popular challenge dataset for low-resource pre-training (BabyLM 10M-word dataset: Choshen et al., 2024).
- (2) We analyze the data mix of the generated curricula (e.g., child-directed speech, dialogue, etc.) and how it evolves over time;
- (3) Analyze loss trajectories to study how our curricula affect the model’s learning process;
- (4) Explore how example ordering within influence curricula relates to existing heuristics.

2 Related Work

Curriculum Learning can roughly be categorized into dynamic and static approaches. Dynamic designs incorporate difficulty heuristics directly into the training process, generating or updating the curriculum during training (e.g., Kumar et al., 2010; Sedova et al., 2023). Static curricula have recently proven popular in the *BabyLM challenge*, a competition promoting the creation of more developmentally plausible language models (Hu et al., 2024): Motivated by the observation that humans only require up to 100 million words to reach native levels in a language (Gilkerson et al., 2017), this challenge invites NLP researchers to explore human-centered learning strategies on a dataset of just 10M or 100M words. Participants have incorporated various sorting heuristics into curriculum learning schemes, such as sorting by increasing sentence length (Platanios et al., 2019; Ghanizadeh and Dousti, 2024; Borazjanizadeh, 2023; Spitkovsky et al., 2010), document- or sentence complexity (Oba et al., 2023; Oppen et al., 2023), lexical diversity (Mi, 2023; Ghanizadeh and Dousti, 2024), or dataset-level source difficulty by category

¹We make our code available at <https://anonymous.4open.science/r/cl-4B5C>, and will provide the links to the datasets and models hosted on the Hugging Face Hub upon acceptance (as they far exceed file size restrictions).

(Thoma et al., 2023; Huebner et al., 2021; Martinez et al., 2023; Oppen et al., 2023). However, static approaches following this framework have shown no consistent positive effect on model performance (Hu et al., 2024).

Our method is motivated by the assumption that children’s language learning proceeds from easy to complex input (Elman, 1993), but represents a middle ground between static and dynamic approaches: we generate static curricula, but base them on a score that reflects training dynamics.

Training Data Influence for CL Bejan et al. (2023) employ TracIn self-influence (Pruthi et al., 2020) for curriculum learning in the fine-tuning setting. For them, self-influence is defined as $\nabla \ell(w_t, z) \cdot \nabla \ell(w_t, z)$ (Pruthi et al., 2020), which does not relate to other data points in the training data, and effectively only quantifies magnitude for a given example. In contrast to our approach, their focus lies on improving performance by filtering outliers and up-weighting the most influential examples. Our approach incorporates more information, specifically pairwise influence scores between one example and *all* other examples in the training data, as outlined in Section 3.1.

Role of Example Difficulty in Learning Several authors have utilized measures of example difficulty to systematically study the effect of curriculum learning for supervised fine-tuning tasks and in the image domain (Hacohen and Weinshall, 2019; Wu et al., 2020; Jiang et al., 2021; Baldock et al., 2021). For instance, Wu et al. (2020), study whether examples of similar difficulty are learned at similar stages across architectures through comparing the *learned iteration* of examples across models, a metric defined as the first epoch at which the model correctly predicts them. Our setup differs in that we study the model’s downstream performance and operate within an unsupervised setting.

3 Methodology

In this work, we investigate the benefits of incorporating training data influence estimates into curriculum learning methods, particularly for low-data pre-training settings. We first introduce our approach for estimating example difficulty using training gradients. Then, we describe our curriculum designs and outline our experimental setup.

3.1 Training Data Influence Estimation

We define a new metric for measuring example difficulty in curriculum design that leverages training data influence estimates: We adapt TracInCP (Pruthi et al., 2020) for this, which in its original formulation estimates the *point-wise influence* $\phi_{\text{TracInCP}}(z, z')$ that training on an instance z had on the model, when predicting a test instance z' . The estimation process involves measuring the similarity between the gradients of the model’s loss function, when evaluated on z and z' respectively, w.r.t some set of parameters w_t , and is repeated at a series of checkpoints T :

$$\phi_{\text{TracInCP}}(z, z') = \sum_{\forall t \in T} \eta_t \nabla \ell(w_t, z) \cdot \nabla \ell(w_t, z') \quad (1)$$

Following Yeh et al. (2022), we let w_t be the model’s input embeddings at checkpoint t .² To leverage this point-wise influence score **for curriculum learning**, we propose to calculate the **average influence** $\phi_t(z, D)$ that a given training example exerts on the prediction of all other examples from the training data D . Omitting the learning rate η_t , for one training instance z , and one checkpoint t we calculate:

$$\begin{aligned} \phi_t(z, D) &= \frac{\sum_{\forall z' \in D} \nabla \ell(w_t, z) \cdot \nabla \ell(w_t, z')}{|D|} \quad (2) \\ &= \nabla \ell(w_t, z) \cdot \mathbb{E}_{z' \sim D} [\nabla \ell(w_t, z')] \quad (3) \end{aligned}$$

Doing so for all examples in the training dataset D , at regular checkpoints for a model trained in random order, yields a matrix $\Phi \in \mathbb{R}^{|D| \times |T|}$ like the one depicted in Figure 2, which we subsequently use for constructing curricula with various reordering functions. In initial experiments, we observed

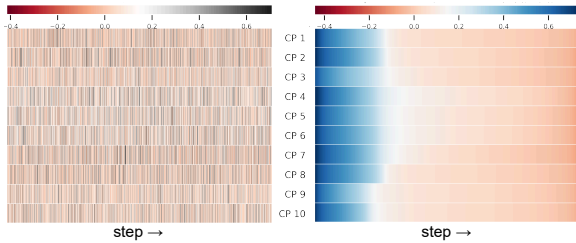


Figure 2: Left: measured influence on C_{rand} ; Right: anticipated influence if sorted according to C_{\searrow} .

that this score based on dot-product similarity was biased against longer examples, which was also

²Note that this score incorporates information about the full model, as the gradient chains through higher layers as well (Yeh et al., 2022).

observed by Xia et al. (2024). Thus, we **normalize the loss gradients** to reduce the impact of gradient magnitude on the similarity scores, effectively yielding cosine similarity (Hammoudeh and Lowd, 2022, 2024; Park et al., 2023; Xia et al., 2024).

3.2 Curriculum Design

This section introduces our 10 curriculum design methods based on influence estimates, as well as 4 baseline curricula. Our designs can be broadly categorized into two categories, characterized by their coverage strategy: the first group of curricula covers the full dataset every epoch, while the second group progressively increases example difficulty across epochs, consequently not re-visiting examples from early epochs in later ones.

Epoch-wise Dataset Coverage Strategies

In the curricula C_{\searrow} and C_{\nearrow} , we sort documents in descending (\searrow) or ascending (\nearrow) order of influence, measured using model checkpoints of a surrogate model trained in random order stored after each epoch t . We include an additional pair of curricula C_{\searrow}^{\sim} and C_{\nearrow}^{\sim} , where, in an attempt to increase data diversity during training, we additionally divide the curriculum into ordered subsets of 1000 documents, and then randomly shuffle the documents within these subsets. Similarly, motivated by the intuition that examples with lasting influence across epochs should be prioritized because they appear to have been more difficult for the surrogate model to learn, we add a re-weighting step to the two curricula $(C * h)_{\searrow}^{\sim}$ and $(C * h)_{\nearrow}^{\sim}$, where we convolve the influence estimates Φ with a lognormal filter h before the sorting step; this thus up-weights examples that remain influential in subsequent epochs: $(C * h)_{(t,i)} = \sum_{k=0}^T \Phi_{(t-k,i)} \cdot h(k)$.

Lastly, emulating prior works that used influence estimates for data cleaning and not solely for re-ordering (e.g., Bejan et al., 2023), we add a curriculum $C^{\{50\}}$ where we discard the 50% least influential examples in each epoch, while keeping the total number of words shown to the model constant. We shuffle once per epoch.

Cumulative Dataset Coverage Strategies

Source difficulty curricula (Martinez et al., 2023) are a curriculum learning strategy where models are trained on a collection of datasets that are manually sorted by difficulty (but the individual examples within these datasets are not). In C_{\searrow}^E and C_{\nearrow}^E , we design a similar coverage strategy, allowing us to

subsequently test whether curricula based on training data influence yield similar dataset mixtures as handcrafted ones: In contrast to the curriculum designs introduced so far, we aggregate the individual influence estimates for a given example across all T epochs to obtain a measure of its overall influence during training ($\phi_T(z, D) = \sum_{\forall t} \phi_t(z, D)$). We then sort examples by this score, either in ascending (\nearrow) or descending order (\searrow). Subsequently, we divide this ordered data into $m = 10$ segments, from which we then randomly sample to create m equal-length epochs with examples of increasing or decreasing difficulty respectively.

Our last curriculum, C_A , is designed as a compromise between curricula with epoch-wise dataset coverage strategies and C^E : In this curriculum, we alternate between showing subsets of high influence scores and subsets of low influence scores, but shuffle the individual examples within each segment randomly. Specifically, we first sort examples by their aggregate score $\phi_T(z, D)$, and create $m = 10$ segments just as for C^E . We then assemble the curriculum from these segments by alternating between the highest-influence and lowest-influence ones until all are used. We train for 10 epochs in this order, randomly shuffling the examples within each segment before each pass.

Baseline Curricula

We include 4 baseline curricula C_{rand} , C_{source} , C_{MATTR} and C_{PPL} : In C_{rand} we emulate non-curriculum learning, performing one pass over the training data per epoch in random order. We train one model per dataset using this curriculum, storing regular checkpoints so that it can serve both as a surrogate model for extracting influence estimates and as a baseline.

Handcrafted *source-difficulty curricula* present datasets sorted by difficulty as distinct blocks (e.g., children’s books before Wikipedia articles). We define such a curriculum in C_{source} , by assigning the datasets in Table 1 to one of 5 stages (C1-C5), following previous work (Thoma et al., 2023; Huebner et al., 2021; Martinez et al., 2023; Oppen et al., 2023). Similar to C^{\nearrow} and C^{\searrow} , we train for two epochs per stage, randomly shuffling examples within each epoch.

C_{MATTR} is inspired by Mi’s (2023) use of *type-token ratio* (TTR) for curriculum learning. Here, we sort documents by increasing moving average type-token ratio (C_{MATTR} (with a window length

of 5); Covington et al., 2010).³ Lastly, for C_{PPL} , we sort in order of increasing perplexity under a static uni-gram model, as described in Martinez et al. (2023). With both C_{MATTR} and C_{PPL} , we train the model on full epochs in this order 10 times.

3.3 Datasets

We train models on three datasets:

- D_{2024} is the 10M word text-only dataset utilized in the 2024 and 2025 iterations of the BabyLM challenge (Choshen et al., 2024; Charpentier et al., 2025), which is composed of datasets of various levels of difficulty listed in Table 1.
- To facilitate analysis of source-difficulty curricula, we construct $D_{stratified}$, which has an equal number of words per stage. We sample from the same datasets underlying D_{2024} , but add sources to balance word counts (Table 1).
- As document length varies substantially by source, we additionally control for the number of words per document in a third dataset $D_{equitoken}$ (also stratified and balanced w.r.t stages); specifically, we create synthetic documents that are exactly 100 words long by concatenation.

Finally, we create a shared evaluation set for all D_* , sampled from the 100M word version of said BabyLM dataset ($|D_{eval}| = 0.05 \cdot |D_{2024}|$).

3.4 Models

Our experiments produce a total of 84 models, one RoBERTa- (126M params) and one Llama model (97.2M params), both with random initializations, for each combination of the 3 datasets and 14 curricula. We train on 4 NVIDIA H100 GPUs with an effective batch size of 2048, using the parameters summarized in Table 3 in Appendix A. Each curriculum includes at most 100 million words (e.g., 10 passes over a dataset of 10M tokens for C_{rand}).

4 Results and Analysis

This section presents and analyzes the results of our curriculum design experiments. Specifically, we: (1) present the benchmark performance of our models on downstream tasks; (2) compare the source composition of our curricula to those of the baselines; (3) analyze training- and evaluation loss trajectories; (4) and explore how example ordering in

³We choose to use MATTR over TTR as a metric to make our curricula more robust to variation in document length.

C1	Child Directed Speech CHILDES (MacWhinney, 2014)
C2	Unscripted Dialogue Switchboard Dialog Act Corpus (Stolcke et al., 2000) British National Corpus (BNC), dialogue portion (Consortium, 2007)
C3	Scripted Dialogue OpenSubtitles (Lison and Tiedemann, 2016)
C4	Wiki Simple Wiki (Warstadt et al., 2023a)
C5	Written English Standardized Project Gutenberg Corpus (Gerlach and Font-Clos, 2018)

C1	Child Directed Speech CHILDES (MacWhinney, 2014)
C2	Children’s Books Children Stories Text Corpus (Bensaid et al., 2021) Children’s Book Test (Hill et al., 2016)
C3	Dialogue Switchboard Dialog Act Corpus (Stolcke et al., 2000) British National Corpus (BNC), dialogue portion (Consortium, 2007) OpenSubtitles (Lison and Tiedemann, 2016)
C4	Educational Simple Wiki (Warstadt et al., 2023a) QED (Abdelali et al., 2014)
C5	Written English Standardized Project Gutenberg Corpus (Gerlach and Font-Clos, 2018) Wikipedia (Warstadt et al., 2023a)

Table 1: Curriculum stages in C_{source} . Stages for D_{2024} (left) differ from those in $D_{stratified}$ and $D_{equitoken}$ (right) to allow for a balanced split. We make all three datasets available under CC BY 4.0.

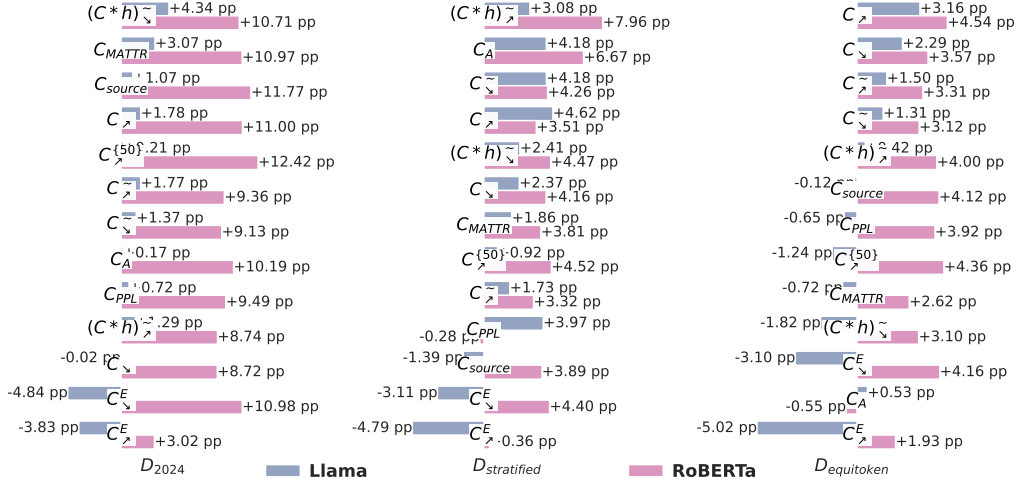


Figure 3: Average change in macro-accuracy across benchmark tasks w.r.t. training on the random curriculum. Sorted by average change across RoBERTa and Llama models.

the influence curricula correlates with the orderings of existing heuristics.

4.1 Benchmark Performance

Dataset	C_{rand} Llama	C_{rand} RoBERTa	Best Model
D_{2024}	0.541	0.466	
$D_{stratified}$	0.536	0.512	0.592
$D_{equitoken}$	0.523	0.492	

Table 2: Macro-Accuracy across tasks for C_{rand} and the best configuration (RoBERTa, $(C * h)_{\sim}$, $D_{stratified}$).

We evaluate our curricula by comparing their performance to models trained on the same data in random order. In Figure 3, we report the increase or decrease in macro-accuracy across individual benchmark tasks from BLiMP (Warstadt et al., 2020), BLiMP supplement (Warstadt et al., 2023b), EWOK (Ivanova et al., 2024), Super GLUE (Wang et al., 2019), as well as an entity tracking task (Kim and Schuster, 2023) and an adjective nominalization task (Hofmann et al., 2024), as implemented specifically for the BabyLM challenge (Charpentier

et al., 2025). Results for the individual benchmarks are provided in Appendix D.

In terms of raw performance, the RoBERTa model trained using $(C * h)_{\sim}$ (sorted by increasing influence, re-weighted with lognormal filter) on $D_{stratified}$ is the **best performing model overall** (0.592 macro-acc, +7.96 pp over C_{rand}), with the best Llama model being the one trained with $(C * h)_{\sim}$ (sorted by decreasing influence) on D_{2024} (0.584, +4.34 pp). RoBERTa models see higher absolute gains through the addition of curriculum learning than Llama models in our experiments. This can partially be attributed to their lower initial accuracy when trained in random order, with Llama models outperforming RoBERTa models by 7.5, 2.4, and 3.1 pp on the D_{2024} , $D_{stratified}$, and $D_{equitoken}$ datasets, respectively (Table 2). Notably, for RoBERTa models, the handcrafted source curriculum was effective on D_{2024} (+11.77 pp), and only two curricula lead to a decrease in performance, namely C_{PPL} on $D_{stratified}$ (-0.28 pp), and C_A on $D_{equitoken}$ (-0.55 pp). For Llama mod-

els, in contrast, the worst-performing curricula C_{\searrow}^E and C_{\nearrow}^E incur a considerable 3.10-5.02 pp decrease in accuracy over training in random order.

For both model architectures, the highest gains through curriculum learning are on D_{2024} followed by $D_{stratified}$ (equal number of words per stage), and $D_{equitoken}$ (equal number of documents per stage, and words per document).

Dataset Coverage Strategies

Models trained with handcrafted- (C_{source}) and synthetic source difficulty curricula (C_{\searrow}^E , C_{\nearrow}^E), both designed to increase difficulty gradually across epochs (cumulative coverage strategies), perform worse overall than the other designs, which perform one full pass over the data each epoch (per-epoch coverage strategies). C_A , where we alternate between showing subsets of high influence scores and subsets of low influence scores, shows significant improvements over training in random order for both Llama (+4.18 pp) and RoBERTa (+6.67 pp) on $D_{stratified}$ and D_{2024} for RoBERTa (+10.19 pp), but not for the remaining three models.

Sorting Direction and Shuffling Strategy

Surprisingly, our benchmark results do not conclusively show whether curricula sorted by ascending (\nearrow) or descending (\searrow) influence perform better; the ascending version of the same strategy does not consistently outperform the descending version (and vice versa). Curricula where we shuffle within stages (e.g., C_{\searrow}^E) similarly do not reliably outperform ones without, the same applies to curricula built from lognorm-filtered influence estimates ($((C * h)_{\searrow})$). We offer a potential explanation for this in Section 5.

4.2 Source Composition

The datasets we utilize are themselves composed of sources of varying difficulty; similar to previous work (Thoma et al., 2023) we have attributed each to one of five stages of increasing difficulty (C1-C5; from a human learning perspective) for constructing the handcrafted curricula (Table 1). Based on these labels, we plot the source compositions of the training data shown to the Llama models over time in Figure 4 and provide those of RoBERTa models in Appendix C.

We observe that our **influence curricula are highly sensitive to the source distribution of the dataset**. *C1: Child Directed Speech* and *C3: Dialogue*, the two largest stages in the unbalanced D_{2024} dataset, are scheduled first in the synthetic

source difficulty curriculum C_{\searrow}^E , with more than half of the training steps allocated to them. For $C^{\{50\}}$, where we discard the 50% least influential examples in each epoch, the share of child directed speech accounts for over 90% of examples throughout the training process, despite accounting for only roughly half of D_{2024} by number of documents.

This **over-representation of child directed speech** in the majority of epochs may explain why these curricula perform worse in benchmark tasks than all other influence curricula across all datasets and model types: When controlling for the number of words per source ($D_{stratified}$), the effect is less extreme, yet, *C1: Child-Directed Speech*, *C3: Dialogue*, and *C4: Educational* are more frequently shown in early rather than in later epochs in C_{\searrow}^E , with *C5: Written English* following the opposite trend. For $D_{equitoken}$ however, where the model used for influence estimation sees an equal number of tokens and documents per stage, all trends are reversed, with C1 now shown more often in later epochs, and C5 in earlier ones. One possible explanation stems from the definition of our datasets, which sample based on a word-based budget rather than one based on the number of documents: In D_{2024} , C1 accounts for 54% of documents but only 28% of words, while C5 comprises 25% of words within just 6% of the dataset’s documents.⁴ Because our sorting relies on a *per-document average* influence measure, similarity to the larger subset C1 likely disproportionately impacts influence scores compared to similarity with C5. This suggests that our ranking method is **biased against smaller sources** (by number of documents).

Contrary to our initial expectation that the influence of child-directed speech would diminish in later epochs, the **source composition** of epoch-wise dataset coverage strategies (e.g., C_{\searrow}^E), **does not strongly vary over time**. To obtain a formal measure of how similar a curriculum’s source distribution over time is to the model-agnostic baselines, we split both curricula into $n = 1000$ segments, for which we then calculate the average Jensen-Shannon divergence⁵. We find that our curricula’s source distribution is closer to that of C_{rand} than to other baselines (i.e., our curricula retain the dataset’s source distribution, Figure 5). We therefore cannot explain the performance of influence

⁴the same pattern applies in $D_{stratified}$

⁵ $\mu_{JSD}(p_a || p_b) := \sum_{i=1}^n \frac{D_{KL}(p_a^i || p_b^i) + D_{KL}(p_b^i || p_a^i)}{2} / n$, where p_a^i and p_b^i are the source distributions of two segments

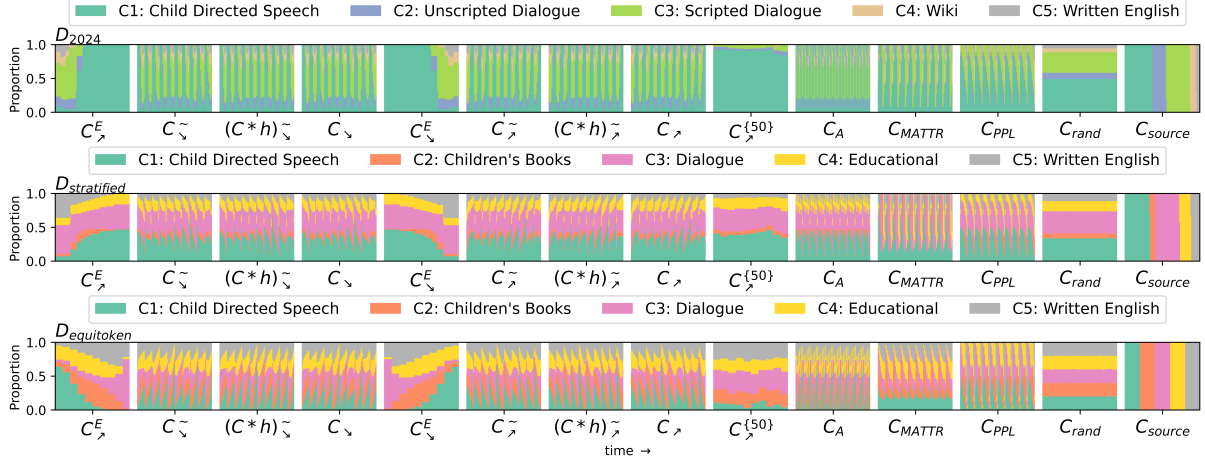


Figure 4: Dataset mix of curricula for Llama models. We trace back documents to the stages defined in Table 1.

curricula through their source distributions alone.

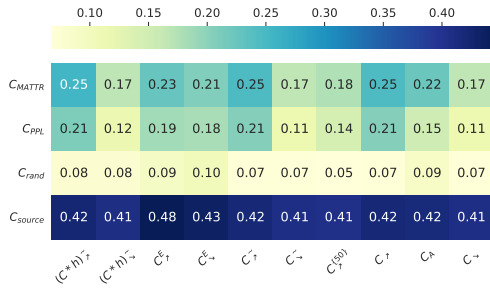


Figure 5: Average Jensen-Shannon divergence between curricula for Llama models. Lower values indicate more similar stage distributions.

4.3 Loss Trajectories

We provide training- and evaluation loss trajectories for a subset of our models in Figure 6, and the remaining ones in Appendix D. For one RoBERTa model (C^E_{\nearrow} on D_{2024}) and 9 Llama models (D_{2024} : $\{C^E_{\nearrow}, C_A, C_{source}, C_{MATTR}, C_{rand}\}$, $D_{stratified}$: $\{C^E_{\nearrow}, C^E_{\searrow}, C^{\{50\}}_{\nearrow}, C_{rand}\}$) we measure higher evaluation loss at the end of training compared to the beginning, suggesting training divergence.

We observe **substantial training loss spikes**, which in non-curriculum learning often indicates training instability (Li et al., 2022). However, as evident in Figure 6, the model that performs best in benchmarks ($(C * h)^{\nearrow}_{\nearrow}$, RoBERTa) exhibits more severe training loss-spikes than the worse performing C_{source} , C^E_{\searrow} or C_{random} . We extend this analysis to all 84 models, calculating the Spearman rank correlation between a curriculum’s gain in benchmark performance (over training in random order) and the *loss-ratio* (a measure of training instability; Li et al., 2022) in Appendix B. We find no sig-

nificant negative rank correlation for any dataset⁶, indicating that at least within the limited number of epochs we train for, training loss trajectories appear **less informative of downstream performance** compared to training in random order.

4.4 Document Order

We additionally explore how the ordering of examples under influence curricula correlates with ordering of existing heuristics. We use Kendall’s τ , calculated on a per-epoch basis as documents are shown multiple times during training.⁷ Curricula sorted by decreasing influence (C^{\sim}_{\searrow} , C^{\sim}_{\searrow} , $(C * h)^{\sim}_{\searrow}$) show significantly stronger correlations with both C_{MATTR} and C_{PPL} than curricula sorted by increasing influence (C_{MATTR} : +0.047*, C_{PPL} : +0.084*). This suggests that our influence measure **may be inversely related to example difficulty** as defined by these curricula (i.e., higher influence implies lower difficulty). Rank correlation between any type of influence curriculum and C_{rand} , as well as between influence curricula and C_{source} is negligible, which is to be expected as we shuffle these within epochs or stages respectively. Convolution with a log-norm filter before sorting ($(C * h)^{\sim}_{\searrow}$) has a marginal positive, but insignificant effect on the similarity to baselines (+0.016 w.r.t. C^{\sim}_{\searrow} for C_{MATTR} , +0.013 w.r.t. C_{PPL}).

5 Discussion

Our results indicate that curricula based on training data influence estimates can be viable from a per-

⁶ D_{2024} : 0.177, $D_{equitoken}$: 0.096, $D_{stratified}$: 0.197

⁷As documents may also be visited multiple times within an epoch, we use tau-b (Kendall, 1945) to account for ties. We truncate the longer of the two curricula where necessary.

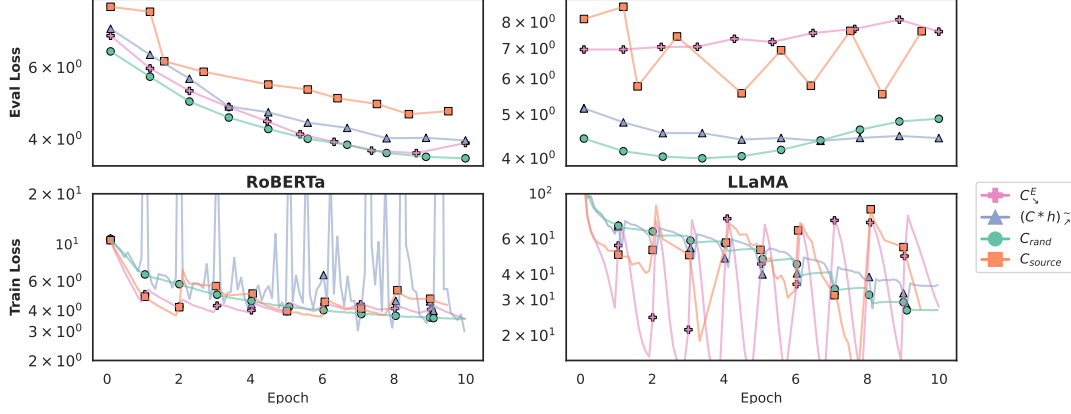


Figure 6: Train- and evaluation loss of baselines and influence curricula for $D_{stratified}$.

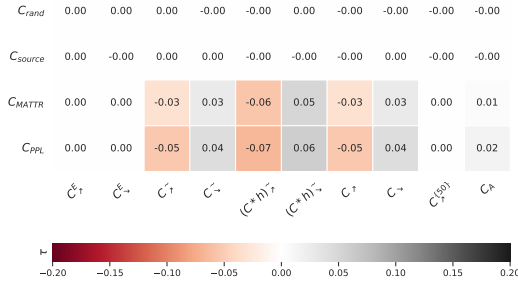


Figure 7: Rank-similarity between influence-curricula and baselines: Mean Kendall τ_b .

formance perspective; however, they are only so if paired with non-developmentally plausible coverage strategies (i.e., ones roughly inspired by how humans acquire language), in which the full training data is visited once per epoch: When specifically comparing the handcrafted- (C_{source}), and the two synthetic source-difficulty curricula (C_{\nearrow}^E , C_{\searrow}^E), it is evident that our sorting strategy based on training dynamics was unable to compensate for this less effective human-centered form of scheduling in terms of performance. Future work should therefore explore coverage strategies that more effectively balance model performance and developmentally plausible scheduling.

The observation that the ascending versions of the same strategy do not consistently outperform the descending versions (e.g., C_{\searrow} and C_{\nearrow}) and vice versa suggests that the observed increase in performance might not stem from the specific sorting order (by increasing or decreasing influence), but rather from an **improved grouping of examples**: examples of similar influence are more likely located in the same batch. This would also explain the competitive performance of sorting by the model-agnostic difficulty heuristic C_{MATTR}

on D_{2024} and $D_{stratified}$.

6 Conclusion

In this work, we study curriculum learning for language model pretraining and propose a novel type of curricula based on training data influence, which **outperforms training in random order** by up to 12.42 pp for RoBERTa models ($C_{\{50\}}$, D_{2024}) and up to 4.62 pp for Llama models (C_{\nearrow} , $D_{stratified}$). In contrast to recent experiments with handcrafted curricula, our results indicate that curriculum learning with our method has **potential to improve data efficiency in low-resource settings**.

Through an analysis of the data distribution in our curricula derived from influence estimates, we find that **their source composition does not strongly vary over time**, contrasting that of existing source-difficulty curricula, which are typically designed to decrease the proportion of child-directed speech in later epochs (replacing it with more complex text). Furthermore, by conducting an analysis of training- and evaluation loss trajectories, we have observed that the severe spikes in training loss seen with this form of curriculum learning are not significantly correlated with model performance on downstream benchmarks. Lastly, we explore how the ordering of examples with influence curricula correlates with existing sorting heuristics, finding that our measure is **inversely correlated to example difficulty** (i.e., higher influence implies lower difficulty). In conclusion, our results suggest that curricula based on training data influence estimates can be viable from a performance perspective, but, their success may be attributed to training dynamics rather than increased developmental plausibility.

Limitations

We use a two-step approach to estimating training data influence: we first pre-train a model in random order, and subsequently extract the loss-gradients we utilize for influence estimation (one example at a time). We opted for this implementation to simplify our experimental setup, as our primary focus was on studying curriculum learning rather than minimizing training time. To improve computational efficiency within our framework, one could reuse (mini-batch) gradients from model training for influence estimation. We provide additional details on runtime in Appendix A.

In Section 4.2, where we study the data mix of our curricula, we observe that our influence curricula are highly sensitive to the source distribution of the dataset. If future work has an intention to use a similar influence estimation method for data cleaning or selection (as we did in $C^{\{50\}}$), it should explore measures to ensure appropriate data balancing. In our setup, the failure to do so primarily results in lower benchmark performance for $C^{\{50\}}$.

Lastly, our experiments are based on relatively small language models and datasets due to the lack of large-scale pre-training datasets that both cover and categorize examples across different difficulty levels. However, with D_{2024} we include a dataset that is widely used and studied through the BabyLM challenge (see Charpentier et al., 2025).

References

- Ahmed Abdelali, Francisco Guzman, Hassan Sajjad, and Stephan Vogel. 2014. [The AMARA Corpus: Building Parallel Language Resources for the Educational Domain](#). In *Proceedings of the Ninth International Conference on Language Resources and Evaluation (LREC'14)*, pages 1856–1862, Reykjavik, Iceland. European Language Resources Association (ELRA).
- Robert Baldock, Hartmut Maennel, and Behnam Neyshabur. 2021. [Deep Learning Through the Lens of Example Difficulty](#). In *Advances in Neural Information Processing Systems*, volume 34, pages 10876–10889. Curran Associates, Inc.
- Irina Bejan, Artem Sokolov, and Katja Filippova. 2023. [Make Every Example Count: On the Stability and Utility of Self-Influence for Learning from Noisy NLP Datasets](#). In *Proceedings of the 2023 Conference on Empirical Methods in Natural Language Processing*, pages 10107–10121, Singapore. Association for Computational Linguistics.
- Yoshua Bengio, Jérôme Louradour, Ronan Collobert, and Jason Weston. 2009. [Curriculum learning](#). In *Proceedings of the 26th Annual International Conference on Machine Learning, ICML '09*, pages 41–48, New York, NY, USA. Association for Computing Machinery.
- Eden Bensaid, Mauro Martino, Benjamin Hoover, and Hendrik Strobelt. 2021. [FairyTailor: A Multimodal Generative Framework for Storytelling](#). *arXiv preprint*. ArXiv:2108.04324 [cs].
- Nasim Borazjanizadeh. 2023. [Optimizing GPT-2 Pre-training on BabyLM Corpus with Difficulty-based Sentence Reordering](#). In *Proceedings of the BabyLM Challenge at the 27th Conference on Computational Natural Language Learning*, pages 356–365, Singapore. Association for Computational Linguistics.
- Lucas Charpentier, Leshem Choshen, Ryan Cotterell, Mustafa Omer Gul, Michael Hu, Jaap Jumelet, Tal Linzen, Jing Liu, Aaron Mueller, Candace Ross, Raj Sanjay Shah, Alex Warstadt, Ethan Wilcox, and Adina Williams. 2025. [BabyLM Turns 3: Call for papers for the 2025 BabyLM workshop](#). *arXiv preprint*. ArXiv:2502.10645 [cs].
- Leshem Choshen, Ryan Cotterell, Michael Y. Hu, Tal Linzen, Aaron Mueller, Candace Ross, Alex Warstadt, Ethan Wilcox, Adina Williams, and Chengxu Zhuang. 2024. [\[Call for Papers\] The 2nd BabyLM Challenge: Sample-efficient pretraining on a developmentally plausible corpus](#). *arXiv preprint*. ArXiv:2404.06214.
- B. N. C. Consortium. 2007. [British National Corpus, XML edition](#). Accepted: 2018-07-27 Artwork Medium: Digital bitstream Interview Medium: Digital bitstream Publisher: University of Oxford.
- Michael A. Covington, , and Joe D. McFall. 2010. [Cutting the Gordian Knot: The Moving-Average Type-Token Ratio \(MATTR\)](#). *Journal of Quantitative Linguistics*, 17(2):94–100. Publisher: Routledge _eprint: <https://doi.org/10.1080/09296171003643098>.
- Jeffrey L. Elman. 1993. [Learning and development in neural networks: the importance of starting small](#). *Cognition*, 48(1):71–99.
- Martin Gerlach and Francesc Font-Clos. 2018. [A standardized Project Gutenberg corpus for statistical analysis of natural language and quantitative linguistics](#). *arXiv preprint*. ArXiv:1812.08092 [cs].
- Mohammad Amin Ghanizadeh and Mohammad Javad Dousti. 2024. [Towards Data-Efficient Language Models: A Child-Inspired Approach to Language Learning](#). In *The 2nd BabyLM Challenge at the 28th Conference on Computational Natural Language Learning*, pages 22–27, Miami, FL, USA. Association for Computational Linguistics.
- Jill Gilkerson, Jeffrey A. Richards, Steven F. Warren, Judith K. Montgomery, Charles R. Greenwood, D. Kimbrough Oller, John H. L. Hansen, and Terrance D.

688	Paul. 2017. Mapping the early language environment using all-day recordings and automated analysis . <i>American Journal of Speech-Language Pathology</i> , 26(2):248–265.	744
689		745
690		746
691		
692	Guy Hacohen and Daphna Weinshall. 2019. On The Power of Curriculum Learning in Training Deep Networks . <i>arXiv preprint</i> . ArXiv:1904.03626 [cs].	747
693		748
694		749
695	Zayd Hammoudeh and Daniel Lowd. 2022. Identifying a Training-Set Attack’s Target Using Renormalized Influence Estimation . In <i>Proceedings of the 2022 ACM SIGSAC Conference on Computer and Communications Security, CCS ’22</i> , pages 1367–1381, New York, NY, USA. Association for Computing Machinery.	750
696		751
697		752
698		
699		
700		
701		
702	Zayd Hammoudeh and Daniel Lowd. 2024. Training data influence analysis and estimation: a survey . <i>Machine Learning</i> , 113(5):2351–2403.	753
703		754
704		755
705	Felix Hill, Antoine Bordes, Sumit Chopra, and Jason Weston. 2016. The Goldilocks Principle: Reading Children’s Books with Explicit Memory Representations . <i>arXiv preprint</i> . ArXiv:1511.02301 [cs].	756
706		
707		
708		
709	Valentin Hofmann, Leonie Weissweiler, David Mortensen, Hinrich Schütze, and Janet Pierrehumbert. 2024. Derivational Morphology Reveals Analogical Generalization in Large Language Models . <i>arXiv preprint</i> . ArXiv:2411.07990 [cs].	757
710		758
711		759
712		760
713		761
714	Michael Y. Hu, Aaron Mueller, Candace Ross, Adina Williams, Tal Linzen, Chengxu Zhuang, Ryan Cotterell, Leshem Choshen, Alex Warstadt, and Ethan Gotlieb Wilcox. 2024. Findings of the Second BabyLM Challenge: Sample-Efficient Pretraining on Developmentally Plausible Corpora . <i>arXiv preprint</i> . ArXiv:2412.05149 [cs] version: 1.	762
715		763
716		764
717		765
718		766
719		767
720		768
721	Philip A. Huebner, Elior Sulem, Fisher Cynthia, and Dan Roth. 2021. BabyBERTa: Learning More Grammar With Small-Scale Child-Directed Language . In <i>Proceedings of the 25th Conference on Computational Natural Language Learning</i> , pages 624–646, Online. Association for Computational Linguistics.	769
722		770
723		771
724		772
725		773
726		774
727	Anna A. Ivanova, Aalok Sathe, Benjamin Lipkin, Unnathi Kumar, Setayesh Radkani, Thomas H. Clark, Carina Kauf, Jennifer Hu, R. T. Pramod, Gabriel Grand, Vivian Paulun, Maria Ryskina, Ekin Akyürek, Ethan Wilcox, Nafisa Rashid, Leshem Choshen, Roger Levy, Evelina Fedorenko, Joshua Tenenbaum, and Jacob Andreas. 2024. Elements of World Knowledge (EWOK): A cognition-inspired framework for evaluating basic world knowledge in language models . <i>arXiv preprint</i> . ArXiv:2405.09605 [cs] version: 1.	775
728		776
729		777
730		778
731		779
732		780
733		781
734		782
735		783
736		784
737		
738	Ziheng Jiang, Chiyuan Zhang, Kunal Talwar, and Michael C. Mozer. 2021. Characterizing Structural Regularities of Labeled Data in Overparameterized Models . In <i>Proceedings of the 38th International Conference on Machine Learning</i> , pages 5034–5044. PMLR. ISSN: 2640-3498.	785
739		786
740		787
741		788
742		789
743		790
		791
	M. G. Kendall. 1945. THE TREATMENT OF TIES IN RANKING PROBLEMS . <i>Biometrika</i> , 33(3):239–251.	792
		793
		794
		795
		796
		797
		798
	Najoung Kim and Sebastian Schuster. 2023. Entity Tracking in Language Models . In <i>Proceedings of the 61st Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)</i> , pages 3835–3855, Toronto, Canada. Association for Computational Linguistics.	
	M. Kumar, Benjamin Packer, and Daphne Koller. 2010. Self-Paced Learning for Latent Variable Models . In <i>Advances in Neural Information Processing Systems</i> , volume 23. Curran Associates, Inc.	
	Conglong Li, Minjia Zhang, and Yuxiong He. 2022. The Stability-Efficiency Dilemma: Investigating Sequence Length Warmup for Training GPT Models . <i>Advances in Neural Information Processing Systems</i> , 35:26736–26750.	
	Pierre Lison and Jörg Tiedemann. 2016. OpenSubtitles2016: Extracting Large Parallel Corpora from Movie and TV Subtitles . In <i>Proceedings of the Tenth International Conference on Language Resources and Evaluation (LREC’16)</i> , pages 923–929, Portorož, Slovenia. European Language Resources Association (ELRA).	
	Yinhan Liu, Myle Ott, Naman Goyal, Jingfei Du, Mandar Joshi, Danqi Chen, Omer Levy, Mike Lewis, Luke Zettlemoyer, and Veselin Stoyanov. 2019. RoBERTa: A Robustly Optimized BERT Pretraining Approach . <i>arXiv preprint</i> . ArXiv:1907.11692 [cs].	
	Brian MacWhinney. 2014. <i>The ChILdes Project</i> , 0 edition. Psychology Press.	
	Richard Diehl Martinez, Hope McGovern, Zebulun Goriely, Christopher Davis, Andrew Caines, Paula Buttery, and Lisa Beinborn. 2023. CLIMB – Curriculum Learning for Infant-inspired Model Building . In <i>Proceedings of the BabyLM Challenge at the 27th Conference on Computational Natural Language Learning</i> , pages 112–127, Singapore. Association for Computational Linguistics.	
	Maggie Mi. 2023. Mmi01 at The BabyLM Challenge: Linguistically Motivated Curriculum Learning for Pretraining in Low-Resource Settings . In <i>Proceedings of the BabyLM Challenge at the 27th Conference on Computational Natural Language Learning</i> , pages 269–278, Singapore. Association for Computational Linguistics.	
	Miyu Oba, Akari Haga, Akiyo Fukatsu, and Yohei Oseki. 2023. BabyLM Challenge: Curriculum learning based on sentence complexity approximating language acquisition . In <i>Proceedings of the BabyLM Challenge at the 27th Conference on Computational Natural Language Learning</i> , pages 290–297, Singapore. Association for Computational Linguistics.	

A Implementation Details

Influence Estimation

To enable influence estimation for the RoBERTa models, which are trained with dynamic masking (tokens are masked differently at each epoch), we implement a custom *Data Collator* for use with the Hugging Face *Trainer*. This collator makes masking reproducible by computing a hash based on the document and the epoch number.

Runtime

Pre-training of all 84 models took 195 hours on 4 NVIDIA H100 GPUs (approximately 2h20m per model). The runtime of the influence estimation step, which is only required once per dataset, depends on the number of documents. Note that while one can run computation for individual model checkpoints in parallel, sequential runtime would amount to 7h45h for $D_{equitoken}$, 109h for D_{2024} (both ran on NVIDIA H100 GPUs), and 149h30min on $D_{stratified}$ (ran on a lower-spec NVIDIA V100 GPUs), totaling 266 GPU hours overall.

	RoBERTa	LLaMA
Vocabulary size	52k	
Hidden size	768	
Number of layers	12	
Number of attention heads	12	
Initializer range	0.02	
Tie word embeddings	True	
Max position embeddings	514	256
Intermediate (FFN) size	3072	2048
Norm epsilon	1e-5	1e-6
Attention dropout	0.1	0
Activation function	gelu	silu
Hidden dropout	0.1	-
FP16	False	
Per Device Batch Size	32	
Gradient Accumulation Steps	16	
GPUs	4	
Adam β_1	0.9	
Adam β_2	0.98	
Adam ϵ	1e-6	
Weight Decay ϵ	0.01	
Learning rate	5e-4	7e-4
Scheduler	polynomial	cosine

Table 3: Training parameters used for all models.

this adds significant overhead during training. To analyze whether training loss spikes are still indicative of training instability for curriculum learning, i.e. whether their severity ultimately impacts benchmark performance, we employ the *loss ratio* metric proposed by Li et al. (2022), as a measure of training instability, which compares the loss at the current step s to the lowest loss achieved in any prior step: $lr(s) = \frac{\ell(s)}{\min_{s' < s} \ell(s')}$. Intuitively (if training in random order), one would expect models with high loss ratios to have lower benchmark performance. However, an analysis of the correlation between a curriculum’s gain in benchmark performance (over training in random order) and this loss-ratio indeed does not reveal a significant negative Spearman rank correlation for any dataset: D_{2024} : 0.177; $D_{equitoken}$: 0.096; $D_{stratified}$: 0.197.

B Loss Trajectories

Our curricula sort examples based on their influence, which may inadvertently reduce example diversity within training batches. We hypothesize that this led to the substantial training loss spikes observed. While one can measure loss during training with a separate evaluation set (as we have done),

C Complementary Figures

This section presents complementary figures for RoBERTa or Llama models, with the respective other model type included in the main body of our paper.

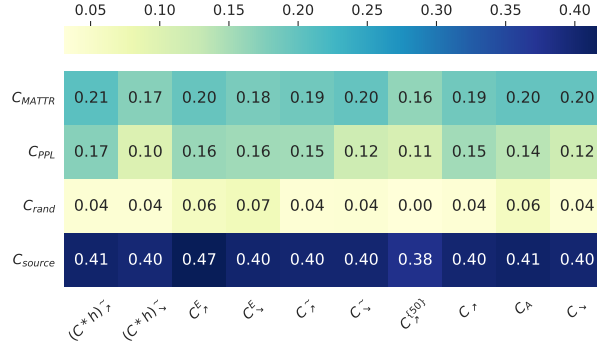


Figure 8: Comparison of curriculum stage distributions: Average Jensen-Shannon divergence between 1000 segments of two given curricula for RoBERTa models. Lower values indicate more similar stage distributions.

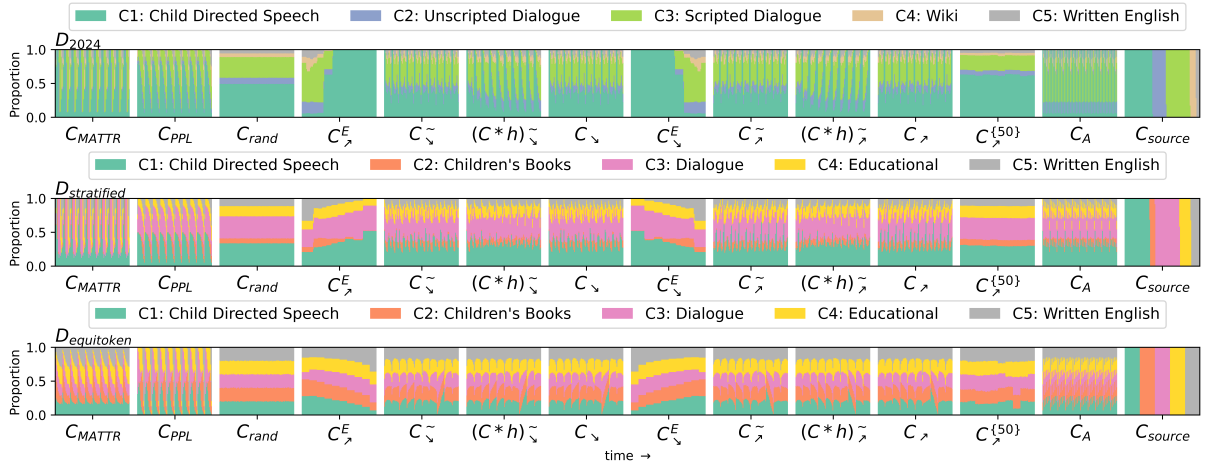


Figure 9: Dataset mix of curricula for RoBERTa models. We trace back documents to the stages defined in Table 1.

D Full Benchmark Results and Loss Trajectories

Table 4: Macro-average gain in accuracy over the corresponding random curriculum.

Curriculum	Dataset	Architecture	Improvement	p-val	Model acc	Random acc
C_{rand}	D_{2024}	RoBERTa	+0.00 pp	-	0.466	-
C_{rand}	$D_{deutoken}$	RoBERTa	+0.00 pp	-	0.492	-
C_{rand}	$D_{stratified}$	RoBERTa	+0.00 pp	-	0.512	-
C_{rand}	$D_{deutoken}$	Llama	+0.00 pp	-	0.523	-
C_{rand}	$D_{stratified}$	Llama	+0.00 pp	-	0.536	-
C_{rand}	D_{2024}	Llama	+0.00 pp	-	0.541	-
C_{\rightarrow}^E	$D_{deutoken}$	Llama	-5.02 pp**	0.033	0.473	0.523
C_{\rightarrow}^E	D_{2024}	Llama	-4.84 pp***	0.004	0.493	0.541
C_{\rightarrow}^E	$D_{stratified}$	Llama	-4.79 pp***	0.005	0.488	0.536
C_{\rightarrow}^E	D_{2024}	Llama	-3.83 pp*	0.065	0.503	0.541
C_{\rightarrow}^E	$D_{stratified}$	Llama	-3.11 pp***	0.002	0.504	0.536
C_{\rightarrow}^E	$D_{deutoken}$	Llama	-3.10 pp	0.100	0.492	0.523
$(C * h)_{\sim}$	$D_{deutoken}$	Llama	-1.82 pp	0.400	0.505	0.523

Continued on next page

Continued from previous page

Curriculum	Dataset	Architecture	Improvement	p-val	Model acc	Random acc
C_{source}	$D_{stratified}$	Llama	-1.39 pp	0.167	0.522	0.536
$C_{\{50\}}$	$D_{equitoken}$	Llama	-1.24 pp	0.504	0.511	0.523
C_{MATTR}	$D_{equitoken}$	Llama	-0.72 pp	0.293	0.516	0.523
C_{PPL}	$D_{equitoken}$	Llama	-0.65 pp	0.431	0.517	0.523
C_A	$D_{equitoken}$	RoBERTa	-0.55 pp	0.726	0.487	0.492
C_{PPL}	$D_{stratified}$	RoBERTa	-0.28 pp	0.877	0.510	0.512
C_{source}	$D_{equitoken}$	Llama	-0.12 pp	0.856	0.522	0.523
C_{\searrow}	D_{2024}	Llama	-0.02 pp	0.991	0.541	0.541
C_A	D_{2024}	Llama	+0.17 pp	0.796	0.543	0.541
$C_{\{50\}}$	D_{2024}	Llama	+0.21 pp	0.918	0.543	0.541
C_{\nearrow}^E	$D_{stratified}$	RoBERTa	+0.36 pp	0.801	0.516	0.512
$(C * h)_{\nearrow}$	$D_{equitoken}$	Llama	+0.42 pp	0.848	0.527	0.523
C_A	$D_{equitoken}$	Llama	+0.53 pp	0.813	0.528	0.523
C_{PPL}	D_{2024}	Llama	+0.72 pp	0.317	0.548	0.541
$C_{\{50\}}$	$D_{stratified}$	Llama	+0.92 pp	0.619	0.545	0.536
C_{source}	D_{2024}	Llama	+1.07 pp	0.242	0.552	0.541
$(C * h)_{\nearrow}$	D_{2024}	Llama	+1.29 pp	0.504	0.554	0.541
C_{\searrow}	$D_{equitoken}$	Llama	+1.31 pp	0.150	0.536	0.523
C_{\searrow}	D_{2024}	Llama	+1.37 pp	0.477	0.555	0.541
C_{\nearrow}	$D_{equitoken}$	Llama	+1.50 pp	0.494	0.538	0.523
C_{\nearrow}	$D_{stratified}$	Llama	+1.73 pp***	0.007	0.553	0.536
C_{\nearrow}	D_{2024}	Llama	+1.77 pp	0.362	0.559	0.541
C_{\nearrow}	D_{2024}	Llama	+1.78 pp	0.371	0.559	0.541
C_{MATTR}	$D_{stratified}$	Llama	+1.86 pp**	0.029	0.554	0.536
C_{\nearrow}^E	$D_{equitoken}$	RoBERTa	+1.93 pp	0.236	0.512	0.492
C_{\searrow}	$D_{equitoken}$	Llama	+2.29 pp***	0.006	0.546	0.523
C_{\searrow}	$D_{stratified}$	Llama	+2.37 pp***	0.002	0.559	0.536
$(C * h)_{\searrow}$	$D_{stratified}$	Llama	+2.41 pp***	0.001	0.560	0.536
C_{MATTR}	$D_{equitoken}$	RoBERTa	+2.62 pp	0.138	0.518	0.492
C_{\nearrow}^E	D_{2024}	RoBERTa	+3.02 pp	0.124	0.496	0.466
C_{MATTR}	D_{2024}	Llama	+3.07 pp***	0.000	0.572	0.541
$(C * h)_{\nearrow}$	$D_{stratified}$	Llama	+3.08 pp	0.122	0.566	0.536
$(C * h)_{\searrow}$	$D_{equitoken}$	RoBERTa	+3.10 pp	0.123	0.523	0.492
C_{\searrow}	$D_{equitoken}$	RoBERTa	+3.12 pp*	0.079	0.523	0.492
C_{\nearrow}	$D_{equitoken}$	Llama	+3.16 pp	0.142	0.555	0.523
C_{\nearrow}	$D_{equitoken}$	RoBERTa	+3.31 pp*	0.077	0.525	0.492
C_{\nearrow}	$D_{stratified}$	RoBERTa	+3.32 pp	0.166	0.546	0.512
C_{\nearrow}	$D_{stratified}$	RoBERTa	+3.51 pp	0.140	0.548	0.512
C_{\searrow}	$D_{equitoken}$	RoBERTa	+3.57 pp**	0.050	0.528	0.492
C_{MATTR}	$D_{stratified}$	RoBERTa	+3.81 pp	0.126	0.551	0.512
C_{source}	$D_{stratified}$	RoBERTa	+3.89 pp	0.120	0.551	0.512
C_{PPL}	$D_{equitoken}$	RoBERTa	+3.92 pp**	0.032	0.531	0.492
C_{PPL}	$D_{stratified}$	Llama	+3.97 pp***	0.000	0.575	0.536
$(C * h)_{\nearrow}$	$D_{equitoken}$	RoBERTa	+4.00 pp*	0.050	0.532	0.492
C_{source}	$D_{equitoken}$	RoBERTa	+4.12 pp*	0.052	0.533	0.492
C_{\searrow}^E	$D_{equitoken}$	RoBERTa	+4.16 pp**	0.041	0.534	0.492
C_{\searrow}	$D_{stratified}$	RoBERTa	+4.16 pp*	0.079	0.554	0.512
C_A	$D_{stratified}$	Llama	+4.18 pp***	0.000	0.577	0.536
C_{\searrow}	$D_{stratified}$	Llama	+4.18 pp***	0.000	0.577	0.536
C_{\searrow}	$D_{stratified}$	RoBERTa	+4.26 pp*	0.094	0.555	0.512
$(C * h)_{\searrow}$	D_{2024}	Llama	+4.34 pp**	0.028	0.584	0.541
$C_{\{50\}}$	$D_{equitoken}$	RoBERTa	+4.36 pp**	0.039	0.536	0.492
C_{\nearrow}^E	$D_{stratified}$	RoBERTa	+4.40 pp*	0.052	0.556	0.512
$(C * h)_{\searrow}$	$D_{stratified}$	RoBERTa	+4.47 pp*	0.072	0.557	0.512
$C_{\{50\}}$	$D_{stratified}$	RoBERTa	+4.52 pp*	0.067	0.558	0.512
C_{\nearrow}	$D_{equitoken}$	RoBERTa	+4.54 pp**	0.031	0.538	0.492
C_{\nearrow}	$D_{stratified}$	Llama	+4.62 pp***	0.000	0.582	0.536
C_A	$D_{stratified}$	RoBERTa	+6.67 pp***	0.004	0.579	0.512
$(C * h)_{\nearrow}$	$D_{stratified}$	RoBERTa	+7.96 pp***	0.000	0.592	0.512
C_{\searrow}	D_{2024}	RoBERTa	+8.72 pp***	0.004	0.553	0.466
$(C * h)_{\nearrow}$	D_{2024}	RoBERTa	+8.74 pp***	0.002	0.553	0.466
C_{\searrow}	D_{2024}	RoBERTa	+9.13 pp***	0.002	0.557	0.466
C_{\nearrow}	D_{2024}	RoBERTa	+9.36 pp***	0.000	0.559	0.466

Continued on next page

Continued from previous page

Curriculum	Dataset	Architecture	Improvement	p-val	Model acc	Random acc
C_{PPL}	D_{2024}	RoBERTa	+9.49 pp***	0.000	0.561	0.466
C_A	D_{2024}	RoBERTa	+10.19 pp***	0.001	0.568	0.466
$(C * h) \searrow$	D_{2024}	RoBERTa	+10.71 pp***	0.000	0.573	0.466
C_{MATTR}	D_{2024}	RoBERTa	+10.97 pp***	0.000	0.575	0.466
C_{\searrow}^E	D_{2024}	RoBERTa	+10.98 pp***	0.000	0.576	0.466
C_{\nearrow}	D_{2024}	RoBERTa	+11.00 pp***	0.000	0.576	0.466
C_{source}	D_{2024}	RoBERTa	+11.77 pp***	0.000	0.583	0.466
$C_{\nearrow}^{\{50\}}$	D_{2024}	RoBERTa	+12.42 pp***	0.000	0.590	0.466
E_{mixed}	ext	gpt-bert	-	-	0.498	-
E_{causal}	ext	gpt-bert	-	-	0.502	-
E_{masked}	ext	gpt-bert	-	-	0.504	-
E_{gpt2}	ext	-	-	-	0.551	-

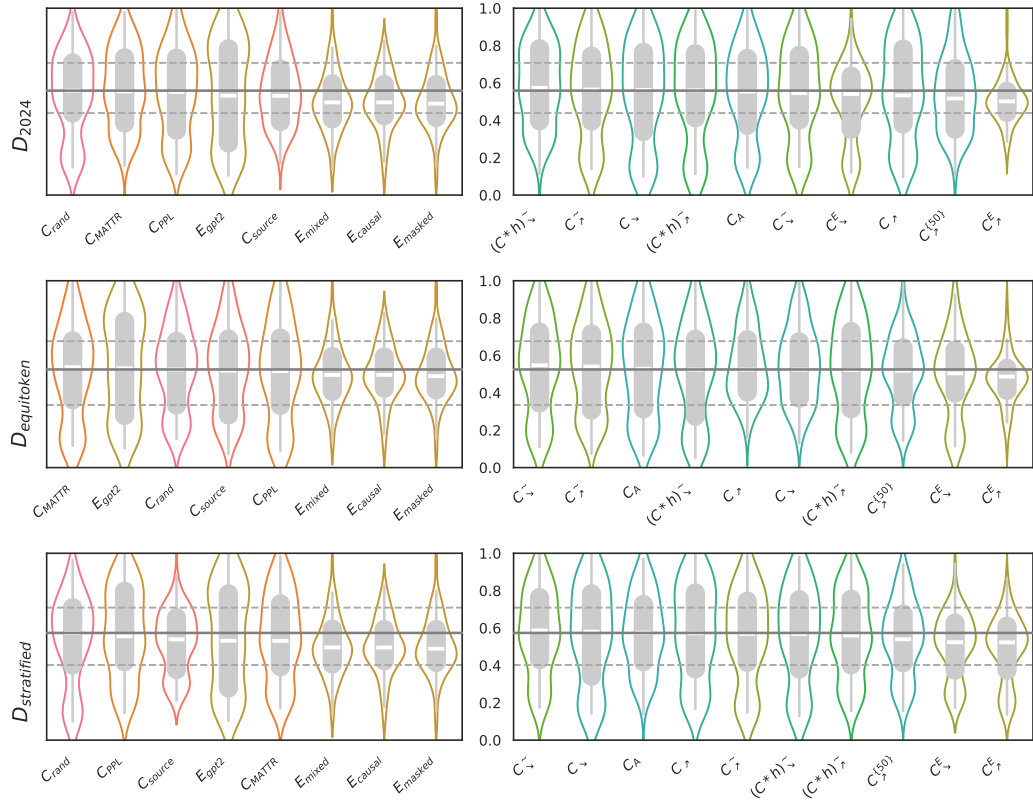


Figure 10: Benchmark results for Llama models.

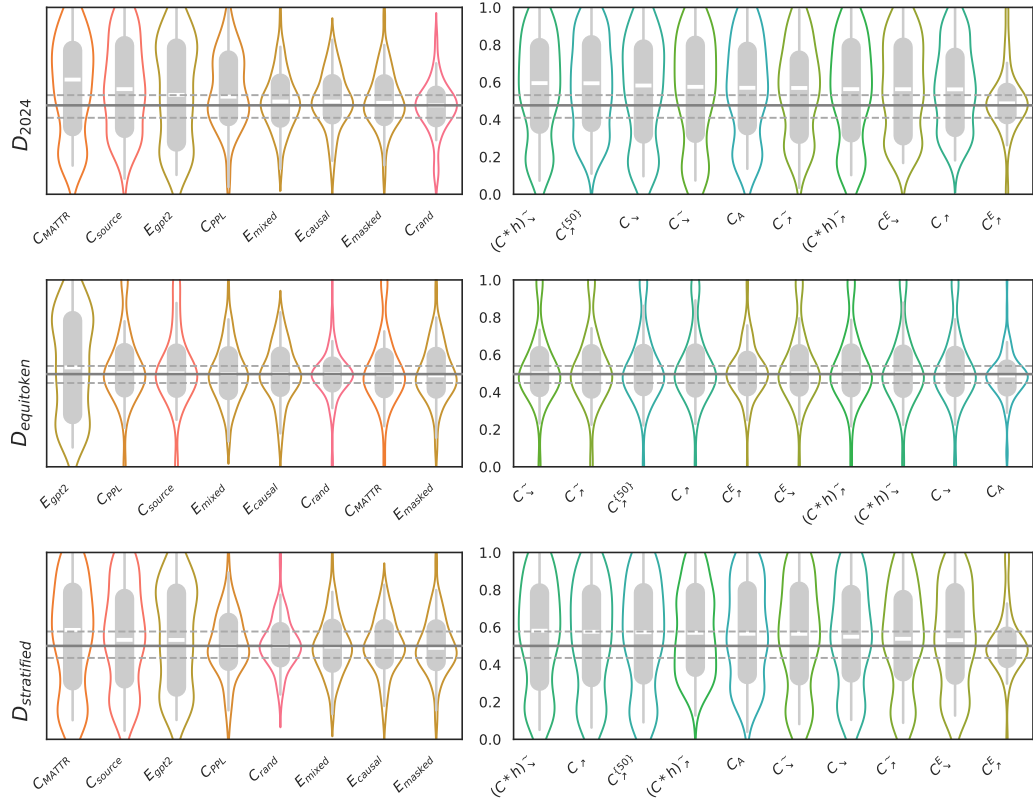


Figure 11: Benchmark results for RoBERTa models.

Table 5: Macro accuracy for Llama models across tasks, per benchmark and overall. E_{opt2} denotes baseline models from the BabyLM challenge, the fine-tuning evaluation pipeline fails for the E_{opt2} model.

Curriculum	Dataset	(Super) GLUE	blimp_filtered	supplement_filtered	entity_tracking	ewok_filtered	wug_adj_nominalization	Macro acc
$(C * h) \sim$	D_{2024}	0.579	0.688	0.559	0.302	0.509	0.570	0.584
$C \nearrow$	$D_{\text{stratified}}$	0.573	0.715	0.546	0.208	0.503	0.600	0.582
C_A	$D_{\text{stratified}}$	0.575	0.675	0.575	0.306	0.507	0.560	0.577
$C \sim$	$D_{\text{stratified}}$	0.573	0.695	0.558	0.242	0.519	0.495	0.577
C_{PPL}	$D_{\text{stratified}}$	0.573	0.696	0.532	0.239	0.510	0.480	0.575
$C_{MATT R}$	D_{2024}	0.573	0.671	0.551	0.295	0.507	0.550	0.572
$(C * h) \sim$	$D_{\text{stratified}}$	0.572	0.678	0.567	0.245	0.501	0.540	0.566
$(C * h) \sim$	$D_{\text{stratified}}$	0.573	0.691	0.542	0.169	0.507	0.510	0.560
$C \nearrow$	$D_{\text{stratified}}$	0.567	0.694	0.533	0.164	0.512	0.420	0.559
$C \sim$	D_{2024}	0.575	0.686	0.566	0.184	0.506	0.500	0.559
$C \sim$	D_{2024}	0.571	0.683	0.566	0.184	0.506	0.565	0.559
$C \nearrow$	D_{2024}	0.571	0.679	0.571	0.176	0.506	0.500	0.555
$C \nearrow$	$D_{\text{equitoken}}$	0.575	0.618	0.514	0.389	0.489	0.555	0.555
$C_{MATT R}$	$D_{\text{stratified}}$	0.571	0.663	0.539	0.227	0.516	0.495	0.554
$(C * h) \sim$	D_{2024}	0.570	0.692	0.536	0.136	0.511	0.515	0.554
$C \nearrow$	$D_{\text{stratified}}$	0.568	0.684	0.514	0.169	0.499	0.535	0.553
$C \sim$	D_{2024}	0.576	0.628	0.503	0.336	0.505	0.560	0.552
E_{opt2}	ext	nan	0.673	0.591	0.189	0.498	0.390	0.551
C_{PPL}	D_{2024}	0.582	0.655	0.508	0.226	0.499	0.655	0.548
$C \nearrow$	$D_{\text{equitoken}}$	0.577	0.615	0.528	0.336	0.501	0.685	0.546
$C \nearrow$	$D_{\text{stratified}}$	0.575	0.633	0.540	0.267	0.510	0.635	0.545
C_A	D_{2024}	0.573	0.660	0.520	0.178	0.506	0.635	0.543
$C \nearrow$	D_{2024}	0.572	0.618	0.541	0.314	0.497	0.635	0.543
C_{rand}	D_{2024}	0.572	0.658	0.497	0.193	0.500	0.440	0.541
$C \nearrow$	D_{2024}	0.573	0.674	0.521	0.133	0.500	0.530	0.541
$C \nearrow$	$D_{\text{equitoken}}$	0.577	0.634	0.561	0.234	0.503	0.465	0.538
C_{rand}	$D_{\text{stratified}}$	0.576	0.662	0.517	0.142	0.500	0.550	0.536
$C \nearrow$	$D_{\text{equitoken}}$	0.578	0.650	0.514	0.179	0.502	0.620	0.536
C_A	$D_{\text{equitoken}}$	0.577	0.634	0.547	0.184	0.492	0.625	0.528
$(C * h) \sim$	$D_{\text{equitoken}}$	0.577	0.638	0.559	0.168	0.495	0.485	0.527
C_{rand}	$D_{\text{equitoken}}$	0.579	0.615	0.548	0.215	0.493	0.625	0.523
C_{source}	$D_{\text{equitoken}}$	0.577	0.609	0.480	0.244	0.499	0.615	0.522
C_{source}	$D_{\text{stratified}}$	0.577	0.593	0.479	0.286	0.518	0.570	0.522
C_{PPL}	$D_{\text{equitoken}}$	0.582	0.635	0.490	0.129	0.498	0.610	0.517
$C_{MATT R}$	$D_{\text{equitoken}}$	0.579	0.627	0.529	0.141	0.498	0.665	0.516
$C \nearrow$	$D_{\text{equitoken}}$	0.579	0.592	0.535	0.228	0.503	0.495	0.511
$(C * h) \sim$	$D_{\text{equitoken}}$	0.578	0.610	0.542	0.136	0.502	0.520	0.505
E_{masked}	ext	0.665	0.508	0.483	0.419	0.502	0.965	0.504

Continued on next page

Continued from previous page

Curriculum	Dataset	(Super) GLUE	blimp_filtered	supplement_filtered	entity_tracking	ewok_filtered	wug_adj_nominalization	Macro acc
C^E	$D_{stratified}$	0.576	0.577	0.535	0.242	0.500	0.555	0.504
C^E_{\rightarrow}	D_{2024}	0.570	0.518	0.499	0.412	0.506	0.925	0.503
E_{causal}	ext	0.654	0.514	0.449	0.412	0.502	0.770	0.502
E_{mixed}	ext	0.660	0.505	0.459	0.414	0.500	0.780	0.498
C^E	D_{2024}	0.577	0.586	0.486	0.152	0.512	0.635	0.493
C^E_{\rightarrow}	$D_{equitoken}$	0.576	0.587	0.507	0.148	0.502	0.590	0.492
C^E_{\rightarrow}	$D_{stratified}$	0.573	0.562	0.510	0.201	0.505	0.640	0.488
C^E_{\rightarrow}	$D_{equitoken}$	0.570	0.471	0.502	0.415	0.502	0.685	0.473

Table 6: Macro accuracy for RoBERTa models across tasks, per benchmark and overall. E_{\rightarrow} denotes baseline models from the BabyLM challenge, the fine-tuning evaluation pipeline fails for the E_{gpt2} model.

Curriculum	Dataset	(Super) GLUE	blimp_filtered	supplement_filtered	entity_tracking	ewok_filtered	wug_adj_nominalization	Macro acc
$(C * h)_{\rightarrow}^{\sim}$	$D_{stratified}$	0.650	0.694	0.535	0.307	0.507	0.570	0.592
$C^{\{50\}}$	D_{2024}	0.634	0.700	0.578	0.268	0.501	0.690	0.590
C^{\rightarrow}_{source}	D_{2024}	0.635	0.683	0.563	0.290	0.507	0.670	0.583
C^A	$D_{stratified}$	0.629	0.698	0.555	0.238	0.497	0.460	0.579
C^{\rightarrow}	D_{2024}	0.643	0.664	0.535	0.309	0.504	0.780	0.576
C^E	D_{2024}	0.641	0.689	0.530	0.237	0.500	0.655	0.576
C^{MATT_R}	D_{2024}	0.642	0.701	0.556	0.186	0.505	0.715	0.575
$(C * h)_{\rightarrow}^{\sim}$	D_{2024}	0.645	0.702	0.570	0.171	0.500	0.680	0.573
C^A	D_{2024}	0.636	0.691	0.529	0.187	0.505	0.675	0.568
C^{\rightarrow}_{PPL}	D_{2024}	0.633	0.614	0.534	0.402	0.500	0.620	0.561
$C^{\rightarrow}_{\{50\}}$	D_{2024}	0.639	0.658	0.567	0.239	0.501	0.715	0.559
$C^{\rightarrow}_{\{50\}}$	$D_{stratified}$	0.647	0.690	0.571	0.126	0.503	0.650	0.558
C^{\rightarrow}	D_{2024}	0.637	0.692	0.561	0.117	0.502	0.775	0.557
$(C * h)_{\rightarrow}^{\sim}$	$D_{stratified}$	0.650	0.689	0.538	0.140	0.502	0.560	0.557
C^E	$D_{stratified}$	0.647	0.680	0.563	0.162	0.499	0.530	0.556
C^{\rightarrow}	$D_{stratified}$	0.638	0.690	0.556	0.128	0.503	0.460	0.555
C^{\rightarrow}	$D_{stratified}$	0.643	0.679	0.559	0.149	0.500	0.610	0.554
C^{\rightarrow}	D_{2024}	0.639	0.675	0.565	0.149	0.501	0.765	0.553
$(C * h)_{\rightarrow}^{\sim}$	D_{2024}	0.626	0.675	0.571	0.148	0.511	0.745	0.553
C^{MATT_R}	$D_{stratified}$	0.648	0.683	0.535	0.127	0.502	0.505	0.551
C^{\rightarrow}_{source}	$D_{stratified}$	0.636	0.668	0.560	0.177	0.499	0.560	0.551
E_{gpt2}	ext	nan	0.673	0.591	0.189	0.498	0.390	0.551
C^{\rightarrow}	$D_{stratified}$	0.644	0.677	0.530	0.125	0.499	0.715	0.548

Continued on next page

Curriculum	Dataset	(Super) GLUE	blimp_filtered	supplement_filtered	entity_tracking	ewok_filtered	wug_adj_nominalization	Macro acc
C_{\rightarrow}^{\sim}	$D_{stratified}$	0.638	0.677	0.535	0.123	0.502	0.540	0.546
C_{\rightarrow}^{\sim}	$D_{equitoken}$	0.611	0.575	0.476	0.409	0.501	0.925	0.538
$C_{\rightarrow}^{\{50\}}$	$D_{equitoken}$	0.605	0.575	0.488	0.409	0.500	0.690	0.536
C_{\rightarrow}^E	$D_{equitoken}$	0.600	0.573	0.485	0.406	0.502	0.720	0.534
C_{source}^{\sim}	$D_{equitoken}$	0.609	0.569	0.488	0.407	0.500	0.855	0.533
$(C * h)_{\rightarrow}^{\sim}$	$D_{equitoken}$	0.612	0.570	0.471	0.409	0.498	0.690	0.532
C_{PPL}^{\sim}	$D_{equitoken}$	0.605	0.566	0.486	0.411	0.501	0.770	0.531
C_{\rightarrow}^{\sim}	$D_{equitoken}$	0.606	0.564	0.475	0.409	0.496	0.690	0.528
C_{\rightarrow}^{\sim}	$D_{equitoken}$	0.602	0.558	0.484	0.411	0.500	0.720	0.525
C_{\rightarrow}^{\sim}	$D_{equitoken}$	0.612	0.559	0.450	0.409	0.491	0.600	0.523
$(C * h)_{\rightarrow}^{\sim}$	$D_{equitoken}$	0.614	0.557	0.484	0.406	0.501	0.495	0.523
C_{MATTR}^{\sim}	$D_{equitoken}$	0.603	0.552	0.455	0.409	0.499	0.525	0.518
C_{\rightarrow}^E	$D_{stratified}$	0.594	0.550	0.462	0.414	0.492	0.400	0.516
C_{rand}^{\sim}	$D_{stratified}$	0.591	0.542	0.467	0.408	0.504	0.520	0.512
C_{\rightarrow}^E	$D_{equitoken}$	0.605	0.531	0.506	0.411	0.501	0.795	0.512
C_{PPL}^{\sim}	$D_{stratified}$	0.645	0.535	0.488	0.411	0.497	0.195	0.510
E_{masked}^{\sim}	ext	0.665	0.508	0.483	0.419	0.502	0.965	0.504
E_{causal}^{\sim}	ext	0.654	0.514	0.449	0.412	0.502	0.770	0.502
E_{mixed}^{\sim}	ext	0.660	0.505	0.459	0.414	0.500	0.780	0.498
C_{\rightarrow}^E	D_{2024}	0.591	0.516	0.459	0.407	0.497	0.540	0.496
C_{rand}^{\sim}	$D_{equitoken}$	0.595	0.506	0.438	0.418	0.494	0.660	0.492
C_A	$D_{equitoken}$	0.597	0.501	0.441	0.413	0.489	0.510	0.487
C_{rand}^{\sim}	D_{2024}	0.601	0.462	0.465	0.409	0.507	0.490	0.466

Table 7: Average % R^2 gain for Llama models in the reading benchmarks (not included in the main paper). E denotes baseline models from the BabyLM challenge.

Curriculum	Dataset	Eye Tracking Score	Self-Paced Reading Score	Avg
E_{causal}	ext	0.102	0.029	0.065
E_{masked}	ext	0.103	0.027	0.065
E_{mixed}	ext	0.099	0.025	0.062
C_{\nearrow}^E	$D_{equitoken}$	0.024	0.009	0.016
C_{\nearrow}^E	D_{2024}	0.021	0.010	0.016
C_{source}	$D_{stratified}$	0.011	0.001	0.006
C_{\searrow}^E	$D_{stratified}$	0.012	0.000	0.006
C_{\searrow}^E	D_{2024}	0.009	0.001	0.005
C_{source}	D_{2024}	0.006	0.001	0.003
$C_{\nearrow}^{\{50\}}$	$D_{equitoken}$	0.006	0.000	0.003
C_{rand}	$D_{equitoken}$	0.005	0.001	0.003
C_{source}	$D_{equitoken}$	0.005	0.001	0.003
C_{rand}	D_{2024}	0.005	0.001	0.003
C_{\searrow}	$D_{stratified}$	0.006	0.001	0.003
C_{\searrow}	$D_{equitoken}$	0.005	0.000	0.003
C_{\searrow}	D_{2024}	0.005	0.000	0.003
C_{PPL}	$D_{equitoken}$	0.006	0.001	0.003
C_{MATTR}	$D_{equitoken}$	0.005	0.000	0.003
$C_{\nearrow}^{\{50\}}$	$D_{stratified}$	0.005	0.001	0.003
$(C * h)_{\nearrow}$	D_{2024}	0.003	0.002	0.003
C_{\nearrow}	$D_{stratified}$	0.005	0.000	0.003
$(C * h)_{\nearrow}$	$D_{stratified}$	0.005	0.001	0.003
$(C * h)_{\searrow}$	$D_{equitoken}$	0.007	0.000	0.003
C_{\searrow}	$D_{equitoken}$	0.006	0.000	0.003
C_{PPL}	$D_{stratified}$	0.003	0.000	0.002
$(C * h)_{\searrow}$	D_{2024}	0.004	0.001	0.002
$(C * h)_{\searrow}$	$D_{stratified}$	0.005	0.000	0.002
C_{rand}	$D_{stratified}$	0.004	0.000	0.002
C_{\searrow}^E	$D_{equitoken}$	0.004	0.000	0.002
C_{\searrow}	D_{2024}	0.003	0.000	0.002
C_{\searrow}	$D_{equitoken}$	0.004	0.000	0.002
C_{\searrow}	$D_{stratified}$	0.005	0.000	0.002
C_{\searrow}	D_{2024}	0.004	0.000	0.002
C_{PPL}	D_{2024}	0.003	0.001	0.002
C_{\searrow}	$D_{stratified}$	0.004	0.000	0.002
C_A	$D_{stratified}$	0.003	0.001	0.002
C_A	$D_{equitoken}$	0.004	0.000	0.002
C_A	D_{2024}	0.005	0.000	0.002
$(C * h)_{\searrow}$	$D_{equitoken}$	0.005	0.000	0.002
C_{\nearrow}	$D_{equitoken}$	0.004	0.000	0.002
C_{\nearrow}	D_{2024}	0.002	0.000	0.001
C_{MATTR}	$D_{stratified}$	0.002	0.000	0.001
C_{MATTR}	D_{2024}	0.003	0.000	0.001
C_{\nearrow}^E	$D_{stratified}$	0.002	0.000	0.001
E_{gpt2}	ext	0.001	0.000	0.001
$C_{\nearrow}^{\{50\}}$	D_{2024}	0.001	0.002	0.001

Table 8: Average % R^2 gain for RoBERTa models in the reading benchmarks (not included in the main paper). E denotes baseline models from the BabyLM challenge.

Curriculum	Dataset	Eye Tracking Score	Self-Paced Reading Score	Avg
E_{causal}	ext	0.102	0.029	0.065
E_{masked}	ext	0.103	0.027	0.065
E_{mixed}	ext	0.099	0.025	0.062
C_{\nearrow}^E	$D_{stratified}$	0.076	0.015	0.046
C_{\nearrow}^E	D_{2024}	0.074	0.014	0.044
C_{rand}	$D_{stratified}$	0.070	0.016	0.043
C_{\nearrow}	$D_{stratified}$	0.075	0.009	0.042
C_{PPL}	$D_{stratified}$	0.071	0.012	0.041

Continued on next page

Continued from previous page

Curriculum	Dataset	Eye Tracking Score	Self-Paced Reading Score	Avg
C_{rand}	D_{2024}	0.064	0.011	0.037
C_{PPL}	D_{2024}	0.060	0.007	0.033
C_{\nearrow}^{\sim}	$D_{stratified}$	0.051	0.007	0.029
C_{\nearrow}^E	$D_{equitoken}$	0.045	0.011	0.028
C_{\nearrow}	D_{2024}	0.050	0.006	0.028
C_A	$D_{equitoken}$	0.045	0.012	0.028
C_{rand}	$D_{equitoken}$	0.041	0.012	0.027
$(C * h)_{\searrow}^{\sim}$	$D_{stratified}$	0.046	0.005	0.026
C_{\searrow}^E	$D_{stratified}$	0.043	0.004	0.024
C_{\searrow}^E	D_{2024}	0.045	0.003	0.024
C_{\searrow}^{\sim}	D_{2024}	0.039	0.007	0.023
$(C * h)_{\searrow}^{\sim}$	D_{2024}	0.039	0.005	0.022
C_{source}	D_{2024}	0.039	0.003	0.021
C_{\nearrow}^{\sim}	D_{2024}	0.035	0.007	0.021
C_A	D_{2024}	0.036	0.005	0.021
C_{\searrow}	$D_{stratified}$	0.036	0.003	0.020
$C_{\nearrow}^{\{50\}}$	$D_{stratified}$	0.034	0.004	0.019
C_A	$D_{stratified}$	0.034	0.003	0.018
C_{\searrow}^{\sim}	$D_{stratified}$	0.033	0.003	0.018
C_{\searrow}	D_{2024}	0.030	0.005	0.017
$C_{\nearrow}^{\{50\}}$	D_{2024}	0.033	0.002	0.017
$(C * h)_{\nearrow}^{\sim}$	$D_{stratified}$	0.031	0.002	0.016
C_{MATR}	D_{2024}	0.029	0.003	0.016
C_{source}	$D_{stratified}$	0.024	0.003	0.014
$(C * h)_{\nearrow}^{\sim}$	D_{2024}	0.019	0.001	0.010
C_{\searrow}	$D_{equitoken}$	0.015	0.003	0.009
$(C * h)_{\searrow}^{\sim}$	$D_{equitoken}$	0.015	0.003	0.009
C_{\nearrow}^{\sim}	$D_{equitoken}$	0.015	0.003	0.009
C_{source}	$D_{equitoken}$	0.016	0.003	0.009
C_{MATR}	$D_{stratified}$	0.018	0.001	0.009
$(C * h)_{\nearrow}^{\sim}$	$D_{equitoken}$	0.014	0.003	0.008
$C_{\nearrow}^{\{50\}}$	$D_{equitoken}$	0.012	0.002	0.007
C_{PPL}	$D_{equitoken}$	0.011	0.003	0.007
C_{\nearrow}	$D_{equitoken}$	0.011	0.002	0.007
C_{\searrow}^{\sim}	$D_{equitoken}$	0.012	0.002	0.007
C_{\searrow}^E	$D_{equitoken}$	0.012	0.002	0.007
C_{MATR}	$D_{equitoken}$	0.011	0.002	0.007
E_{gpt2}	ext	0.001	0.000	0.001

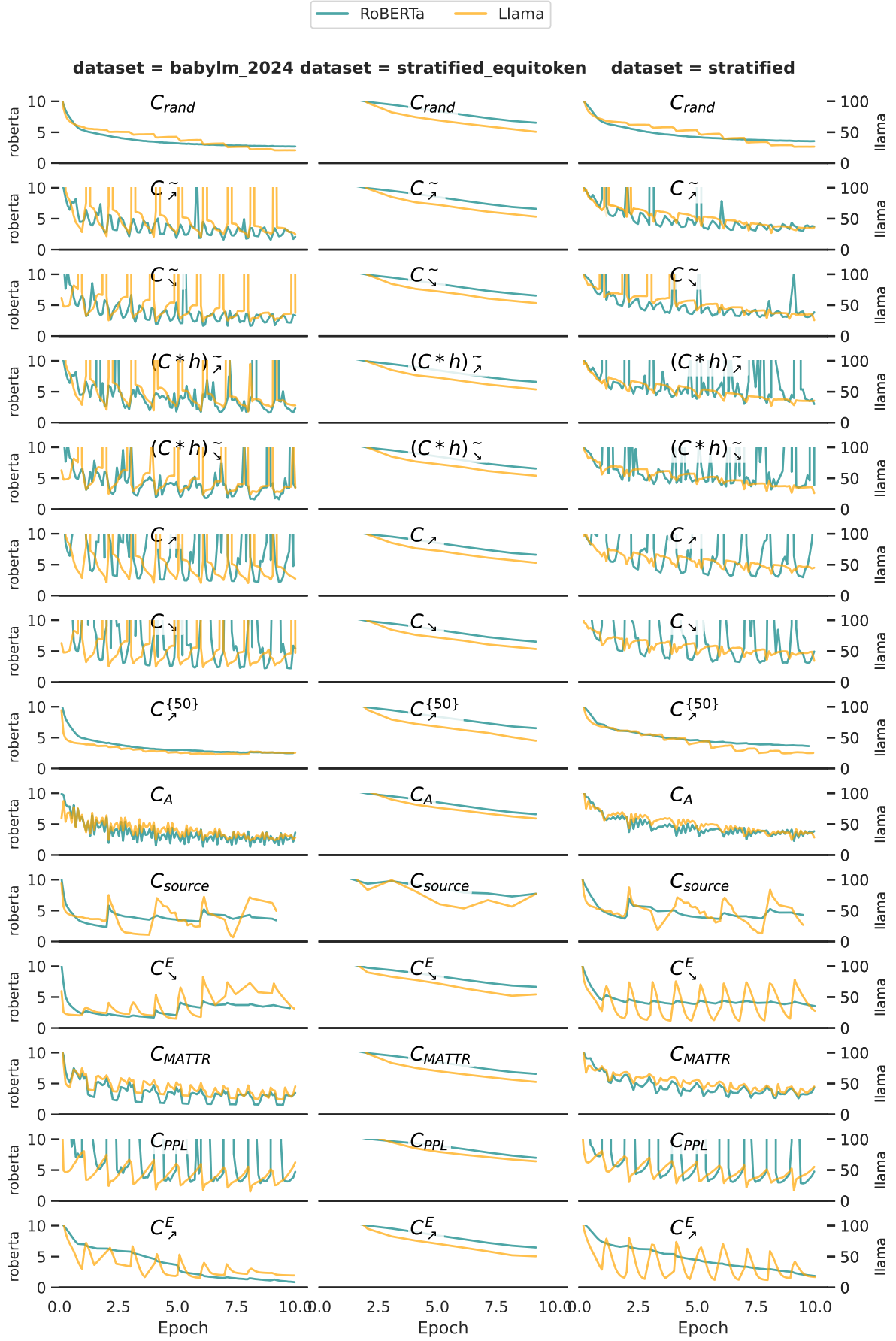


Figure 12: Training loss trajectories under different curricula.

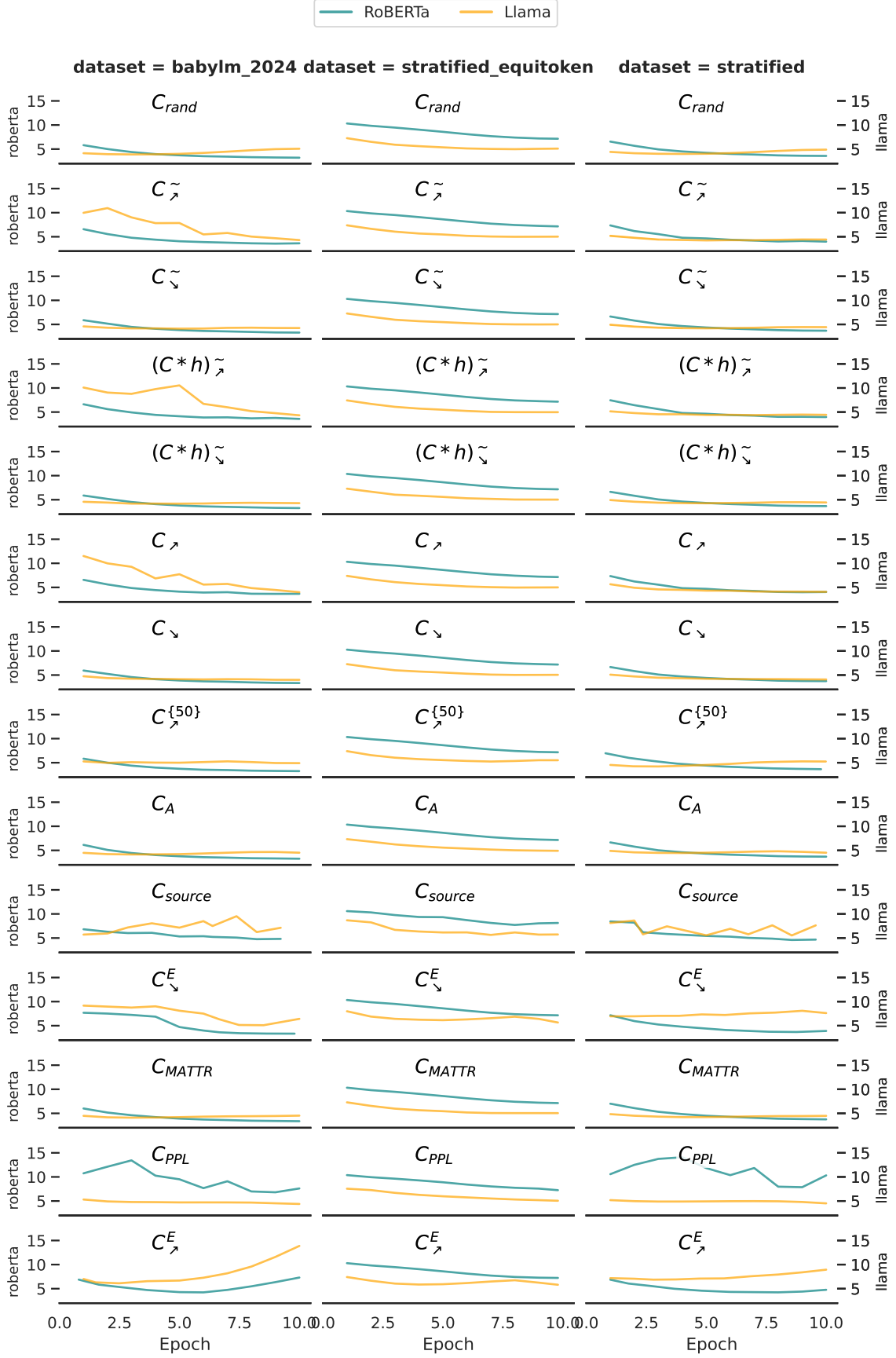


Figure 13: Evaluation loss trajectories under different curricula. We construct an evaluation set by sampling the 100M word 2024 BabyLM dataset (D_{2024} is the 10M version; Choshen et al., 2024). $|D_{eval}| = 0.05 \cdot |D_{2024}|$.