

# Raker: A Relation-aware Knowledge Reasoning Model for Inductive Relation Prediction

Anonymous ACL submission

## Abstract

Inductive relation prediction, an important task for knowledge graph completion, is to predict the relations between entities that are unseen at the training stage. The latest methods use pre-trained language models (PLMs) to encode the paths between the head entity and tail entity and achieve state-of-the-art prediction performance. However, these methods cannot well handle no-path situations and are also unable to learn comprehensive relation representations for distinguishing different relations to overcome the difficulty of inductive relation prediction. To tackle this issue, we propose a novel **Relation-aware knowledge reasoning model** entitled Raker which introduces an adaptive reasoning information extraction method to identify relation-aware reasoning neighbors of entities in the target triple to handle no-path situations, and enables the PLM to be more aware of the possible relations by the relation-specific soft prompting. Raker is evaluated on three public datasets and achieves SOTA performance in inductive relation prediction when compared with the baseline methods. Notably, the absolute improvement of Raker is even more than 10% on the FB15k-237 dataset in the inductive setting. Moreover, Raker also demonstrates its superiority in transductive and few-shot settings. The code of Raker is available at <https://anonymous.4open.science/r/Raker-9234>.

## 1 Introduction

Knowledge graphs (KGs) are usually heterogeneous graphs consisting of different nodes as entities and different types of edges as relations. KGs play an essential role in a wide range of applications such as recommendation systems (Zhang et al., 2021) and intelligent question answering (Yasunaga et al., 2021; Saxena et al., 2022). However, most KGs suffer from incompleteness, making predicting missing relations between entities in KGs

a popular research problem (Ji et al., 2021; Chen et al., 2023; Liang et al., 2022).

Given an incomplete knowledge graph, the general relation prediction task is to score the probability that the target triple  $(h, r, t)$  is true, where  $h$  and  $t$  denote the head and tail entities, respectively, and  $r$  refers to a certain relation. Specifically, inductive relation prediction is to predict the relations between entities that are unseen at the training stage (Hubert et al., 2023). Existing methods for relation prediction can be roughly divided into 4 categories, i.e., *embedding-based methods*, *rule-based methods*, *graph-based methods*, and *PLM-based methods* (Ji et al., 2021; Chen et al., 2023). Embedding-based methods, e.g., TransE (Bordes et al., 2013) and RoateE (Sun et al., 2019), encode the entities and relations into a semantic space, and design a score function to measure the possibility of the target triple based on the encoded representations. These approaches achieve good performance on some knowledge graph completion (KGC) benchmarks but are limited to the transductive setting which requires all entities and relations to be seen at the training stage (Chen et al., 2022). Rule-based methods (Meilicke et al., 2018) extract logical rules from KGs to infer whether the target triple is correct. Graph-based methods (Teru et al., 2020; Mai et al., 2021) mainly use Graph Neural Networks (GNNs) to encode the graph structures of KGs for inferring relations between entities. PLM-based methods, e.g., BERTRL (Zha et al., 2022) and KRST (Su et al., 2023), feed the KG structure information and the textual embeddings of entities and relations into PLMs for target triple prediction, and achieve state-of-the-art performance in inductive relation prediction.

Particularly, the latest PLM-based methods, e.g., BERTRL and KRST, extract the paths between entities as reasoning information to predict the target triple and are thus highly dependent on the connectivity of KGs. However, KGs often suffer from

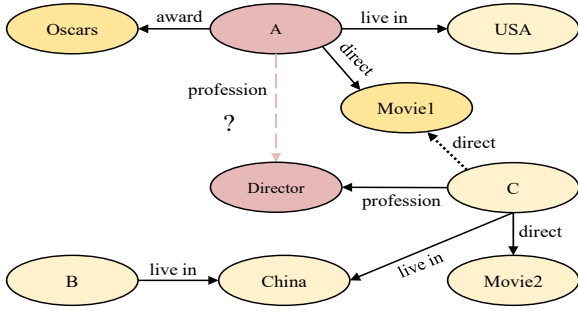


Figure 1: An example of knowledge subgraph.

high incompleteness and sparsity, and there could be no paths between entities. For example, about 12% of entity pairs have no path connection in the widely used knowledge graph dataset FB15k-237. Without paths connecting the head entity  $h$  and the tail entity  $t$ , inferring the target triple becomes difficult. In this case, a natural idea is to add effective relational neighbor triples around entities to enrich the reasoning information for prediction. For example, as illustrated in Figure 1, we wish to predict the target triple  $(A, \textit{profession}, \textit{Director})$ , and assume that the *direct* relation between  $C$  and  $\textit{Movie1}$  is missing. By analyzing the associated triples of  $A$ , e.g.,  $(A, \textit{direct}, \textit{Movie1})$  and  $(A, \textit{award}, \textit{Oscars})$ , we can infer that the target triple is likely correct. Therefore, analyzing the relations surrounding the entities is helpful to infer the target triple. However, the contributions of neighbors associated with the head and tail entities are not equal. Some neighbors can provide strong support information for the target triple prediction, while others may be noisy and unhelpful. For example, the neighbor triple  $(A, \textit{live in}, \textit{USA})$  of entity  $A$  cannot provide strong clues for predicting  $(A, \textit{profession}, \textit{Director})$ . Therefore, identifying effective relational neighbors is an important yet challenging task.

In addition, inductive relation prediction needs rich information about the target relations because the associated entities are unseen at the training stage. PLM-based methods like BERTRL and KRST use hard prompts to directly input the relation names into PLMs, and cannot learn comprehensive representations for relations, which could impede PLMs’ ability to be aware of the target relations in KGs. Moreover, these inherently inflexible hard prompts cannot adapt to different types of relations of similar textual tokens. For example, in the FB15k-237 dataset, the names of different relations may share common textual tokens, such as the rela-

tions named ‘/location/location/partially\_contains’ and ‘/location/location/contains’. The high reliance on textual tokens within hard prompts could lead to confusion for the PLM, thus hindering its ability to accurately differentiate textually similar relations.

To address the above issues, we propose the **Relation-aware knowledge reasoning model** entitled Raker. Raker introduces an adaptive reasoning information extraction method to adaptively extract reasoning information, i.e., reasoning paths and relation-aware reasoning neighbors, for relation prediction. In addition, Raker designs a soft prompting approach to dynamically learn comprehensive and semantic relation representations. Finally, we combine the learned relation representations, hard prompts and extracted reasoning information as the input sequence of PLMs for fine-tuning and relation prediction.

In sum, we make the following contributions:

- We propose a relation-aware knowledge reasoning model Raker for inductive relation prediction and adaptively extract reasoning information to address the issue of no-path connection between entities in PLM-based methods.
- We propose the relation-aware reasoning neighbors extraction method to effectively identify those neighbors that are helpful for target relation prediction, and design a relation-specific soft prompting method to learn comprehensive representation for the target relation.
- We conduct extensive experiments on three public datasets. Raker outperforms the strong baseline methods by a large margin in inductive relation prediction, and also demonstrates its superiority in transductive and few-shot settings.

## 2 Related Work

More details about the four categories of relation prediction methods in KGs are provided below.

**Embedding-based methods.** Embedding-based methods, e.g., TransE(Bordes et al., 2013), TransR(Lin et al., 2015), RoateE(Sun et al., 2019), Complex(Trouillon et al., 2016), ConvE(Dettmers et al., 2018), and TuckER(Balazevic et al., 2019), encode entities and relations as low-dimensional vectors to learn their semantic and structural information and design certain score functions to evaluate the possibility of the target triples based on

the encoded vectors. These methods are effective for transductive relation prediction (Li et al., 2023). However, they cannot generalize to unseen entities, making them unsuitable for inductive relation prediction.

**Rule-based methods.** Rule-based methods uncover logical rules to infer the correctness of the target triple. For example, AMIE (Galárraga et al., 2013) and RuleN (Meilicke et al., 2018) extract the inference patterns for relation prediction. NeuralLP (Yang et al., 2017) and DRUM (Sadeghian et al., 2019) employ an end-to-end approach to learn the differentiable rules, and use the rules to predict the target triple.

**Graph-based methods.** Graph-based methods (Das et al., 2018; Schlichtkrull et al., 2018; Li et al., 2022) exploit the structure information of knowledge graphs to infer the relations between entities. For example, GraIL (Teru et al., 2020) and CoMPiLE (Mai et al., 2021) extract the subgraph that encompasses the target triple and leverages GNN message passing to achieve relation prediction. DeepPath (Xiong et al., 2017) and MINERVA (Das et al., 2018) identify the paths that connect the head and tail entities of the target triple and use them to predict the missing relation. However, according to (Zhang et al., 2022), the aggregation mechanisms in GNNs are not effective for KGs.

**PLM-based methods.** The pre-trained language models (PLMs) like BERT (Devlin et al., 2018), T5 (Raffel et al., 2020), and GPT-3 (Brown et al., 2020) have revolutionized natural language processing, and are widely used for knowledge graph completion (Gesese et al., 2022). For example, KG-BERT (Yao et al., 2019) fine-tunes BERT with the descriptions of entities and relations to predict the missing relations. PKGC (Lv et al., 2022) uses PLMs to encode the definition and attributes of head and tail entities for predicting the target triple. BERTRL (Zha et al., 2022) employs BERT to encode the reasoning paths between head and tail entities to predict the target triple. KRST (Su et al., 2023) further introduces path extraction metrics, i.e., relation path coverage and confidence, to select relevant paths for the target triple. Specifically, BERTRL and KRST capture both structural and semantic information in knowledge graphs and achieve SOTA performance for inductive relation prediction. However, they still struggle to infer the target triple  $(h, r, t)$  when there are no paths between entities  $h$  and  $t$ .

### 3 Methodology

Figure 2 illustrates the framework of Raker which proposes the adaptive reasoning information extraction method to address the no-path issue and the relation-specific soft prompting method to make PLMs aware of the predicted relation’s semantic representation. Concretely, given the target triple  $(h, r, t)$ , Raker tries to extract the paths between entities  $h$  and  $t$  to obtain reasoning information. If there are no paths between the two entities, Raker extracts relation-aware reasoning neighbors as the reasoning information. Meanwhile, Raker designs a soft prompt to learn comprehensive representations for the target relation, thereby guiding the PLMs to focus on the relevant information for relation inference. Finally, Raker fine-tunes PLMs for relation prediction with the learned relation representations and extracted reasoning information.

#### 3.1 Adaptive Reasoning Information Extraction

Given the target triple  $(h, r, t)$ , Raker first tries to extract the paths between entities  $h$  and  $t$  since these paths provide effective reasoning information to evaluate the relation  $r$  (Zha et al., 2022; Su et al., 2023). If the two entities are disconnected, Raker uses the relation-aware reasoning neighbors extraction method to accurately identify those neighbor triples that are helpful for the relation prediction. In this way, we can achieve adaptive reasoning information extraction. Note that, the reasoning paths and relation-aware reasoning neighbors usually contain duplicate reasoning information. For example, to predict triple  $(A, profession, Director)$  in Figure 1, the reasoning path  $A \xrightarrow{direct} Movie1 \xleftarrow{direct} C \xrightarrow{profession} Director$  between  $A$  and  $Director$  covers the reasoning neighbor  $A \xrightarrow{direct} Movie1$ . Thus, Raker only uses the reasoning paths if head and tail entities are connected to reduce redundancy.

For easy representation, we denote a KG as  $G=(E, R, D)$ , where  $E$  and  $R$  represent the sets of entities and relations, respectively, and  $D=\{(h, r, t)|h, t \in E, r \in R\}$  represents all the triples in  $G$ .

##### 3.1.1 Reasoning Paths Extraction

Reasoning paths can be formulated as the logic rules for knowledge reasoning. For example, we can easily infer  $(C, mother\ of, B)$

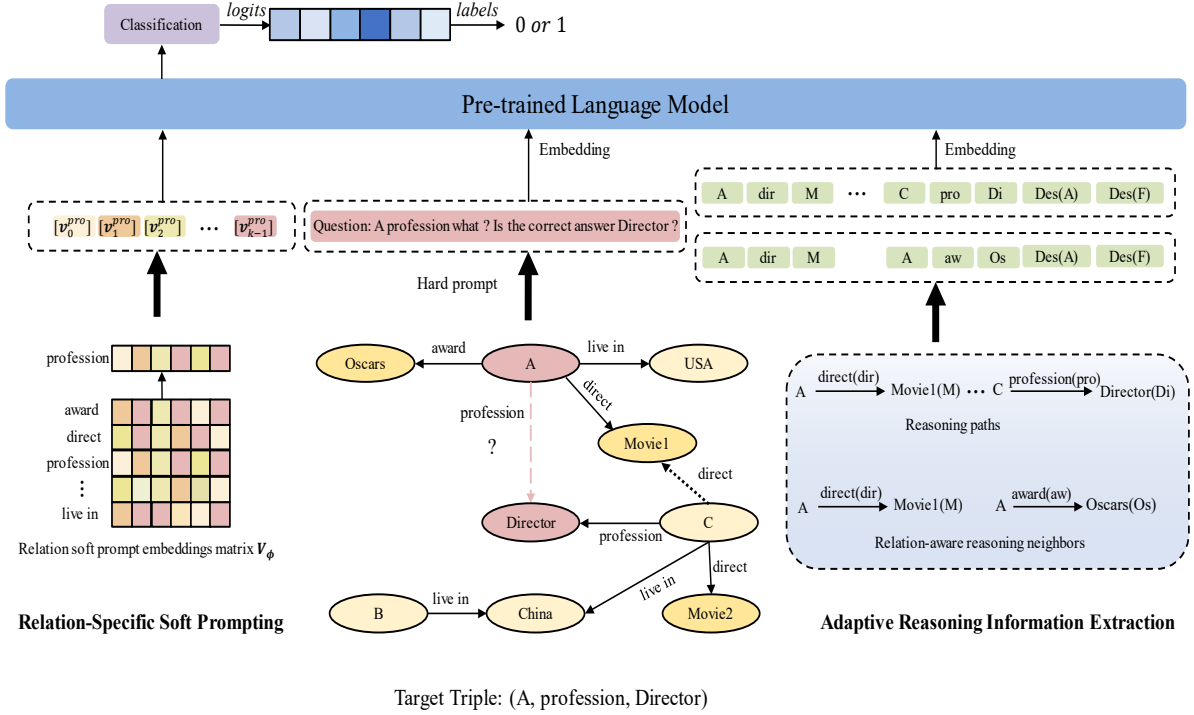


Figure 2: The framework of Raker which extracts adaptive reasoning information, generates relation-specific prompts from learnable embeddings and hard prompts, and fine-tunes the PLM for relation prediction with the reasoning information and generated prompts.

from rule  $(A, \text{father of}, B) \wedge (C, \text{married}, A) \rightarrow (C, \text{mother of}, B)$ . Therefore, the paths between head and tail entities show great reasoning power for inductive relation prediction. Following BERTRL (Zha et al., 2022) and KRST (Su et al., 2023), Raker directly uses the Breadth-First Search algorithm to extract the reasoning paths between head and tail entities.

### 3.1.2 Relation-aware Reasoning Neighbors Extraction

To predict a target triple, the contributions of neighbors associated with the head and tail entities are not equal. As discussed previously, some neighbors can provide strong support information for the target triple, while others may be noisy and unhelpful. Therefore, we propose a relation-aware reasoning neighbors extraction method to identify those neighbors associated with the head and tail entities of the target triple that are helpful to the relation prediction.

Given the target triple  $(h, r, t)$ , relation-aware reasoning neighbors refer to these triples that contain  $h$  or  $t$ , and their relations could help to predict the target relation  $r$ . To identify these relation-aware reasoning neighbors, we first calculate the relative frequency of relations for all entities in

the entire KG, and then calculate the contribution score of each relation associated with the head and tail entities. Finally, the relation-aware reasoning neighbors are extracted based on the contribution scores.

For entity  $e$ , all the relations associated with  $e$  are denoted as  $R^e$ . For each relation  $r \in R^e$ , the relative frequency  $f_r^e$  is calculated as below.

$$f_r^e = \frac{n_r^e}{\sum_{r_i \in R^e} n_{r_i}^e} \quad (1)$$

where  $n_r^e$  is the frequency of relation  $r$  associated with  $e$ . For example, we have  $f_{direct}^C = 1/3$  for entity  $C$  and relation  $direct$  in Figure 1. Then, for each entity  $e$ , we can obtain a vector  $\mathbf{F}^e$  consisting of the relative frequencies of all the relations associated with  $e$ . The vectors for all entities form a matrix  $\mathbf{F}$ .

For the target relation  $r$ , we extract the entities that are heads of  $r$  in KG  $G$  and analyze the distributions of relations associated with these entities. Concretely, we define  $D_r$  as the set of triples containing relation  $r$ ,  $D_r^h$  as the set of triples that contain relation  $r$  and have  $h$  as their head entities, and  $E_r^H$  as the set of head entities appearing in  $D_r$ . In addition, we define  $R_r^H$  as the set

of relations associated with entities in  $E_r^H$ , i.e.,  
 $R_r^H = \bigcup_{h_i \in E_r^H} R^{h_i}$ .

For target relation  $r$ , we calculate the contribution score  $p(r | r_i)$  of each relation  $r_i \in R_r^H$  to  $r$ , i.e.,

$$p(r | r_i) = \frac{p(r)p(r_i | r)}{\sum_{r_k \in R} p(r_k)p(r_i | r_k)} \quad (2)$$

$$p(r) = \frac{|D_r|}{\sum_{r_i \in R} |D_{r_i}|} \quad (3)$$

where  $p(r)$  is the appearance probability of relation  $r$  in KG  $G$ , and  $|D_r|$  denotes the number of triples in  $D_r$ . Intuitively, given relation  $r_i$ ,  $p(r | r_i)$  means the probability that the head entity of  $r_i$  also has the relation  $r$ . The item  $p(r_i | r)$  in Eq. (3) is calculated as below.

$$p(r_i | r) = \sum_{h_i \in E_r^H} s_{(r,r_i)}^{h_i} \quad (4)$$

where  $s_{(r,r_i)}^h = f_{r_i}^h \times f_{inv}$ ,  $f_{r_i}^h$  is the relative frequency of relation  $r_i$  associated with entity  $h \in E_r^H$ , and  $f_{inv}$  is the inverse frequency, i.e., the logarithm of the ratio between the total number of entities and the number of entities having relation  $r_i$ .

For example, in Figure 1, only triple  $(C, profession, Director)$  contains target relation *profession*. Therefore, we have  $E_{pro}^H = \{C\}$  and  $R_{pro}^H = \{profession, direct, live\}$ , and just need to analyze the relations associated with  $C$ . Specifically, for relation *direct*, we have  $f_{dir}^C = 1/3$  and  $f_{inv} = \log(8/2)$  since the example KG has 8 entities among which 2 entities have relation *direct* if the relation *direct* between entities  $C$  and *Movie1* is missing. Finally, we have  $p(pro | dir) = s_{(pro,dir)}^C = 1/3 \times \log(8/2) = 0.462$ .

After calculating the contribution score  $p(r | r_i)$  for each relation  $r_i \in R_r^H$ , we use a threshold  $\alpha$  to filter out those relations in  $R_r^H$  with contribution scores lower than  $\alpha$  to get the helpful relations  $R_r^{H'}$  associated with head entities for relation  $r$ . In addition, we also calculate the helpful relations, i.e.,  $R_r^{T'}$ , associated with tail entities for relation  $r$  in the same way.

Then, we further calculate the specific helpful relations  $R^{h'}$  and  $R^{t'}$  for the head entity  $h$  and tail entity  $t$ , respectively, in the target triple, i.e.,

$$R^{h'} = R^h \cap R_r^{H'}, R^{t'} = R^t \cap R_r^{T'} \quad (5)$$

where  $R^h$  and  $R^t$  are the sets of relations associated with entities  $h$  and  $t$ , respectively.

Finally, if both  $R^{h'}$  and  $R^{t'}$  are not empty, we extract the relation-aware reasoning neighbors  $RN$  for the target triple  $(h, r, t)$  as below.

$$RN = (\bigcup_{r_h \in R^{h'}} D_{r_h}^h) \cup (\bigcup_{r_t \in R^{t'}} D_{r_t}^t) \quad (6)$$

For the implementation details of relation-aware reasoning neighbors extraction, please refer to appendix A.

### 3.2 Relation-specific Soft Prompting

Existing PLM-based relation prediction methods usually use hard prompts to encode the target entities and relations, e.g., "Question: **[head entity] [relation]** what ? Is the correct answer **[tail entity]** ?". Only using these hard prompts struggle to be aware of the target relation and cannot adapt to diverse triples. Furthermore, these inherently inflexible hard prompts are limited to a pre-defined set of instructions, rendering them incapable of interacting with reasoning information and discriminating textually similar relations. To overcome these limitations, we propose the relation-specific soft prompting method.

For each relation  $r$ , the corresponding relation-specific soft prompt  $v^r$  comprises  $k$  trainable vectors  $[v_0^r; v_1^r; \dots; v_{k-1}^r]$ , where  $v_i^r \in \mathbb{R}^m$  and  $[\cdot]$  denotes the vector concatenation operation. The soft prompts for all relations forms the matrix  $V_\phi \in \mathbb{R}^{|R| \times k \times m}$ , where  $|R|$  denotes the number of distinct relations, and  $m$  is the dimension of trainable vectors and set to 768.

We prepend  $v^r$  to the prefix of the PLM's input. In the self-attention process of the PLM, the soft prompt vector interacts with the textual information in the input sequence, thus making the model focus on the textual content that is relevant to the specific relation. Concretely, given a pre-trained language model  $LM_\theta$  parametrized by  $\theta$ , the input sentence embedding generated by Raker is  $z = [e([\text{CLS}]) \ v \ e(q) \ e([\text{SEP}]) \ e(c)]$  which fuses the embedding of [CLS], the relation-specific soft prompt  $v$ , the embedding of hard prompt  $q$  for the target triple, the embedding of [SEP] and the embedding of adaptive reasoning information  $c$ , where  $e(\cdot)$  denoted as embedding operation.

During the training, the  $i^{\text{th}}$  input  $l_i^j$  for the  $j^{\text{th}}$  layer of the PLM in Raker is calculated as below.

$$l_i^j = \begin{cases} z_i & (j = 0) \\ LM_\theta(l_i^{j-1}) & \text{Otherwise} \end{cases} \quad (7)$$

where  $j = 0$  corresponds to the input layer and

$LM_\theta(\cdot)$  is the forward function of language model layer.

Raker leverages the trainable matrix  $V_\phi$  to dynamically learn comprehensive representations of relations. By combining the soft prompts with hard prompts, Raker can enhance PLMs’ awareness of the target relation for better prediction.

### 3.3 Triple Prediction via PLM

#### 3.3.1 Input Sentence Formation

Raker combines prompts and adaptive reasoning information to generate the input sentence for the PLM, i.e.,

$$z = [e([\text{CLS}]) \ v \ e(q) \ e([\text{SEP}]) \ e(c)]$$

Adaptive reasoning information  $c$  can be  $c_p$  or  $c_n$ , where  $c_p$  represents the reasoning paths and  $c_n$  represents the relation-aware reasoning neighbors.

Take the target triple ( $A$ , *profession*, *Director*) in Figure 1 as an example, we have

$$z = [e([\text{CLS}]) \ v^{pro} \ e(q) \ e([\text{SEP}]) \ e(c)]$$

$q = \text{Question: A profession what? Is the correct answer Director?}$

$c = [c_p \ \text{or} \ c_n]$

$c_p = \text{A direct Movie1; C direct Movie1; C profession Director [SEP] Des(A) [SEP] Des(Director)}$

$c_n = \text{A direct Movie1; A award Oscars [SEP] Des(A) [SEP] Des(Director)}$

where  $\text{Des}(\cdot)$  is the textual description of the entity that is used to augment the reasoning information for the target triple (Yao et al., 2019; Wang et al., 2022). If the relation *direct* between entities  $C$  and *Movie1* exists, we have  $c = c_p$ , otherwise  $c = c_n$ .

#### 3.3.2 Relation Prediction

After input sentence formation, Raker uses one linear layer on top of [CLS] to score the target triple’s correctness, which can be regarded as a binary classification task. If reasoning paths are used, following BERTRL and KRST, Raker takes each reasoning path as a separate input to the PLM. We define  $z(c_{p_i})$  as the input sentence embedding using the  $i^{\text{th}}$  reasoning path, and the corresponding prediction probability is  $pro_i$ , i.e.,

$$pro_i = pro(y|z(c_{p_i})), \ i = 1, 2, \dots, N \quad (8)$$

where  $y \in \{0, 1\}$  is class label, and  $N$  is the number of reasoning paths. Then, the final score of target triple ( $h, r, t$ ) is calculated as below.

$$\text{score}(h, r, t) = \max_{i=1,2,\dots,N} pro(y = 1 | z(c_{p_i})) \quad (9)$$

If relation-aware reasoning neighbors are used as the reasoning information, we have  $\text{score}(h, r, t) = pro(y|z(c_n))$ .

We follow the negative sampling strategy in BERTRL to produce negative samples, i.e., randomly sampling entities from the common 3-hop entities of head and tail entities to corrupt the head or tail of each positive triple.

Raker is trained based on the cross entropy loss, i.e.,

$$\mathcal{L} = - \sum_{\tau} (y_{\tau} \log p + (1 - y_{\tau}) \log (1 - p)) \quad (10)$$

where  $y_{\tau} \in \{0, 1\}$  is the label,  $p$  is the triple score,  $\tau \in D^+ \cup D^-$ ,  $D^+$  is the positive triple set, and  $D^-$  is the negative triple set.

## 4 Experiments

### 4.1 Datasets

We conducted extensive experiments on three widely used knowledge graph completion datasets, i.e., FB15k-237 (Toutanova et al., 2015), WN18RR (Dettmers et al., 2018), and NELL-995 (Xiong et al., 2017). Table 1 presents the details of three datasets. We use the inductive, transductive, few-shot subsets of these three datasets according to the setting in BERTRL (Zha et al., 2022).

Table 1: Statistics of three datasets.

Dataset	KG	Relations	Entities	Triples	Avg. degree
WN18RR	train	9	2746	6670	4.86
	train-2000	9	1970	2002	2.03
	train-1000	9	1362	1001	1.47
	test-transductive	7	962	638	1.32
	test-inductive	8	922	1991	4.32
FB15k-237	train	180	1594	5223	6.56
	train-2000	180	1280	2008	3.14
	train-1000	180	923	1027	2.23
	train-rel50	50	1310	3283	5.01
	train-rel100	100	1499	3895	5.20
	test-transductive	102	550	492	1.79
test-inductive	142	1093	2404	4.40	
NELL-995	train	88	2564	10063	7.85
	train-2000	88	1346	2011	2.99
	train-1000	88	893	1020	2.28
	test-transductive	60	1936	968	1.00
	test-inductive	79	2086	6621	6.35

### 4.2 Experiment Settings

Raker is implemented based on the bert-base-uncased using PyTorch, and trained on two NVIDIA GeForce RTX 3090 GPUs. Following the evaluation in Grail (Teru et al., 2020) and BERTRL (Zha et al., 2022), we measure the Mean

Table 2: Results of transductive and inductive relation prediction.

		Transductive			Inductive		
		WN18RR	FB15k-237	NELL-995	WN18RR	FB15k-237	NELL-995
MRR	RuleN	0.669	0.674	0.736	0.780	0.462	0.710
	GRAIL	0.676	0.597	0.727	0.799	0.469	0.675
	MINERVA	0.656	0.572	0.592	-	-	-
	TuckER	0.646	0.682	0.800	-	-	-
	KG-BERT	-	-	-	0.547	0.500	0.419
	BERTRL	0.683	0.695	0.781	0.792	0.605	0.808
	KRST	0.899	0.720	0.800	0.890	0.716	0.769
	Raker	<b>0.912</b>	<b>0.784</b>	<b>0.813</b>	<b>0.930</b>	<b>0.817</b>	<b>0.835</b>
	Absolute Imp.	<b>1.3%↑</b>	<b>6.4%↑</b>	<b>1.3%↑</b>	<b>4.0%↑</b>	<b>10.1%↑</b>	<b>2.7%↑</b>
Hits@1	RuleN	0.646	0.603	0.636	0.745	0.415	0.638
	GRAIL	0.644	0.494	0.615	0.769	0.390	0.554
	MINERVA	0.632	0.534	0.553	-	-	-
	TuckER	0.600	0.615	0.729	-	-	-
	KG-BERT	-	-	-	0.436	0.341	0.244
	BERTRL	0.655	0.620	0.686	0.755	0.541	0.715
	KRST	0.835	0.639	0.694	0.809	0.600	0.649
	Raker	<b>0.853</b>	<b>0.701</b>	<b>0.730</b>	<b>0.888</b>	<b>0.729</b>	<b>0.748</b>
	Absolute Imp.	<b>1.8%↑</b>	<b>6.2%↑</b>	<b>3.6%↑</b>	<b>7.9%↑</b>	<b>12.9%↑</b>	<b>3.3%↑</b>

Reciprocal Rank (MRR) and Hits@1 of one positive triple among 50 samples with 49 negative triples. MRR calculates the average reciprocal rank of all positive triples and Hits@1 calculates the percentage of cases where the positive triple appears as the top-1 ranked triple. Following BERTRL, we randomly generate negative triples and use them for training and validation. For a fair comparison, we directly use the negative triples provided by BERTRL for testing. Each experiment is run twice and the mean results are reported. We set the learning rate, the length of relation-specific soft prompts  $k$  and relation-aware reasoning neighbors filtering threshold  $\alpha$  to  $5 \times 10^{-5}$ , 10, and 0.1, respectively.

### 4.3 Results of Transductive and Inductive Relation Prediction

Table 2 presents the results of both transductive and inductive relation prediction. Since the WN18RR dataset has only 9 relations, and the paths between entities could be highly redundant, we employ the path filtering strategy in KRST to reduce such redundancy.

According to the results in Table 2, Raker achieves the best performance among all methods, and largely outperforms the baselines. Especially, the improvement of Raker is more than 10% on the FB15k-237 inductive subset which has the largest number of distinct relations among three datasets, and has many entity pairs that are not connected. The relation-specific soft prompting and relation-aware-reasoning neighbors together contribute to such improvement.

We also evaluated the performance of Raker ,

BERTRL, and KRST in terms of Hits@3 and Hits@10 on three inductive datasets. The results are summarized in Appendix C.

### 4.4 Results of Few-shot Relation Prediction

For few-shot relation prediction, Raker follows BERTRL to extract reasoning paths on the sub-graphs and Raker\* follows KRST to extract reasoning paths on the entire KG graph. According to the results in Table 3, Raker and Raker\* outperform most baseline methods over three datasets. In general, Raker\* performs better than Raker because extracting reasoning paths from the entire KG graph could learn more information about the target triple. KRST performs best on the NELL-995 dataset for transductive relation prediction since most entity pairs in this dataset are connected and the contribution from relation-aware reasoning neighbors is thus limited.

### 4.5 Unseen Relation Prediction

Raker leverages a pre-trained language model for relation prediction, and has the potential to predict unseen relations. Table 4 presents the results of unseen relation prediction on the subsets of FB15k-237 with a zero-shot setting introduced by BERTRL. Following BERTRL, we use the triples with different numbers of relation types for training, and testing on the FB15k-237 inductive dataset. According to the results, Raker largely outperforms BERTRL and KRST since it can extract more reasoning information for relation prediction.

Table 3: Results of few-shot relation prediction.

		Transductive						Inductive					
		WN18RR		FB15k-237		NELL-995		WN18RR		FB15k-237		NELL-995	
		1000	2000	1000	2000	1000	2000	1000	2000	1000	2000	1000	2000
MRR	RuleN	0.567	0.625	0.434	0.577	0.453	0.609	0.681	0.773	0.236	0.383	0.334	0.495
	GRAIL	0.588	0.673	0.375	0.453	0.292	0.436	0.652	0.799	0.380	0.432	0.458	0.462
	MINERVA	0.125	0.268	0.198	0.364	0.182	0.322	-	-	-	-	-	-
	TuckER	0.258	0.448	0.457	0.601	0.436	0.577	-	-	-	-	-	-
	KG-BERT	-	-	-	-	-	-	0.471	0.525	0.431	0.460	0.406	0.406
	BERTRL	0.662	0.673	0.618	0.667	0.648	0.693	0.765	0.777	0.526	0.565	0.736	0.744
	KRST	<u>0.871</u>	<u>0.882</u>	<u>0.696</u>	0.701	<b>0.743</b>	<b>0.781</b>	0.886	0.878	<u>0.679</u>	0.680	<u>0.745</u>	<u>0.738</u>
	Raker	0.810	0.850	0.670	<u>0.728</u>	0.673	<u>0.757</u>	<b>0.892</b>	<b>0.917</b>	0.637	<u>0.687</u>	<b>0.750</b>	<b>0.783</b>
	Raker*	<b>0.877</b>	<b>0.887</b>	<b>0.731</b>	<b>0.736</b>	<u>0.718</u>	0.751	<u>0.891</u>	<u>0.910</u>	<b>0.701</b>	<b>0.723</b>	0.662	0.727
Hits@1	RuleN	0.548	0.605	0.374	0.508	0.365	0.501	0.649	0.737	0.207	0.344	0.282	0.418
	GRAIL	0.489	0.633	0.267	0.352	0.198	0.342	0.516	0.769	0.273	0.351	0.295	0.298
	MINERVA	0.106	0.248	0.170	0.324	0.152	0.284	-	-	-	-	-	-
	TuckER	0.320	0.415	0.407	0.529	0.392	0.520	-	-	-	-	-	-
	KG-BERT	-	-	-	-	-	-	0.364	0.404	0.288	0.317	0.236	0.236
	BERTRL	0.621	0.637	0.517	0.583	0.526	0.582	0.713	0.731	0.441	0.493	0.622	0.628
	KRST	<u>0.790</u>	<u>0.810</u>	<u>0.611</u>	0.602	<b>0.628</b>	<b>0.678</b>	0.811	0.793	<u>0.537</u>	0.524	<u>0.637</u>	<u>0.629</u>
	Raker	0.745	0.783	0.590	<u>0.629</u>	0.545	<u>0.657</u>	<b>0.835</b>	<b>0.864</b>	0.531	<u>0.578</u>	<b>0.641</b>	<b>0.683</b>
	Raker*	<b>0.815</b>	<b>0.823</b>	<b>0.621</b>	<b>0.632</b>	<u>0.589</u>	0.637	<u>0.819</u>	<u>0.850</u>	<b>0.566</b>	<b>0.593</b>	0.505	0.598

Table 4: Results of unseen relation prediction.

Method		30 relations	50 relations	70 relations	100 relations	130 relations
MRR	KG-BERT	-	-	-	-	-
	BERTRL	0.574	0.580	0.610	0.612	0.621
	KRST	0.642	0.660	0.677	0.692	0.694
	Raker	<b>0.651</b>	<b>0.714</b>	<b>0.770</b>	<b>0.769</b>	<b>0.788</b>
Hits@1	KG-BERT	-	0.266	-	0.450	-
	BERTRL	0.519	0.534	0.573	0.585	0.577
	KRST	0.509	0.551	0.555	0.560	0.557
	Raker	<b>0.537</b>	<b>0.619</b>	<b>0.671</b>	<b>0.678</b>	<b>0.690</b>

## 4.6 Ablation Study

Table 5 shows the results of Raker after removing the relation-aware reasoning neighbors extraction method and the relation-specific soft prompting method. Obviously, after removing either of the two components, the performance of Raker decreases dramatically, which indicates the effectiveness and necessity of the two components.

Table 5: Results of ablation studies on FB15k-237-inductive dataset.

Method	MRR	Hits@1	Hits@3	Hits@10
w/o Relation-aware reasoning neighbors	0.720	0.643	0.771	0.892
w/o Relation-specific soft prompts	0.746	0.646	0.809	0.939
Raker	<b>0.817</b>	<b>0.729</b>	<b>0.873</b>	<b>0.978</b>

## 5 Conclusion

In this work, we propose the relation-aware knowledge reasoning model Raker for inductive relation prediction, and adaptively extract reasoning information to address the issue of no-path connection

between entities. Raker introduces the relation-aware reasoning neighbors extraction method to effectively identify those neighbors that are helpful for target relation prediction, and designs a relation-specific soft prompting method to learn comprehensive representation for the target relation. According to the experiment results under different settings, Raker largely outperforms the baseline methods in both inductive relation prediction and transductive relation prediction, and also achieves good performance for few-shot setting and unseen relation prediction.

## Limitations

Although Raker can well address the issue of no-path connection between entities and largely outperforms baseline methods, it still has two limitations. First, Raker extracts paths and neighbors for each triple, and could be of high computational complexity if applied to predict missing entities. Second, reasoning paths and neighbors are used alternately in Raker, and better integration methods



575	are expected to take their advantage while avoiding	6th International Conference on Learning Representations, ICLR 2018, Vancouver, BC, Canada, April 30 - May 3, 2018, Conference Track Proceedings.	631
576	redundancy.	OpenReview.net.	632
			633
			634
577	<b>References</b>		
578	Ivana Balazevic, Carl Allen, and Timothy M. Hospedales. 2019. Tucker: Tensor factorization for	Tim Dettmers, Pasquale Minervini, Pontus Stenetorp, and Sebastian Riedel. 2018. Convolutional 2d knowledge graph embeddings. In Proceedings of the Thirty-Second AAAI Conference on Artificial Intelligence, (AAAI-18), the 30th innovative Applications of Artificial Intelligence (IAAI-18), and the 8th AAAI Symposium on Educational Advances in Artificial Intelligence (EAAI-18), New Orleans, Louisiana, USA, February 2-7, 2018, pages 1811–1818. AAAI Press.	635
579	knowledge graph completion. In Proceedings of the 2019 Conference on Empirical Methods in Natural Language Processing and the 9th International Joint Conference on Natural Language Processing, EMNLP-IJCNLP 2019, Hong Kong, China, November 3-7, 2019, pages 5184–5193. Association for Computational Linguistics.		636
580			637
581			638
582			639
583			640
584			641
585			642
586			643
587	Antoine Bordes, Nicolas Usunier, Alberto García-Durán, Jason Weston, and Oksana Yakhnenko. 2013. Translating embeddings for modeling multi-relational data. In Advances in Neural Information Processing Systems 26: 27th Annual Conference on Neural Information Processing Systems 2013. Proceedings of a meeting held December 5-8, 2013, Lake Tahoe, Nevada, United States, pages 2787–2795.	Jacob Devlin, Ming-Wei Chang, Kenton Lee, and Kristina Toutanova. 2018. Bert: Pre-training of deep bidirectional transformers for language understanding. arXiv preprint arXiv:1810.04805.	644
588			645
589			646
590			647
591		Luis Antonio Galárraga, Christina Teflioudi, Katja Hose, and Fabian M. Suchanek. 2013. AMIE: association rule mining under incomplete evidence in ontological knowledge bases. In 22nd International World Wide Web Conference, WWW '13, Rio de Janeiro, Brazil, May 13-17, 2013, pages 413–422. International World Wide Web Conferences Steering Committee / ACM.	648
592			649
593			650
594			651
595	Tom B. Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Aspell, Sandhini Agarwal, Ariel Herbert-Voss, Gretchen Krueger, Tom Henighan, Rewon Child, Aditya Ramesh, Daniel M. Ziegler, Jeffrey Wu, Clemens Winter, Christopher Hesse, Mark Chen, Eric Sigler, Mateusz Litwin, Scott Gray, Benjamin Chess, Jack Clark, Christopher Berner, Sam McCandlish, Alec Radford, Ilya Sutskever, and Dario Amodei. 2020. Language models are few-shot learners. In Advances in Neural Information Processing Systems 33: Annual Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12, 2020, virtual.	Genet Asefa Gesese, Harald Sack, and Mehwish Alam. 2022. RAILD: towards leveraging relation features for inductive link prediction in knowledge graphs. In Proceedings of the 11th International Joint Conference on Knowledge Graphs, IJCKG 2022, Hangzhou, China, October 27-28, 2022, pages 82–90. ACM.	652
596			653
597			654
598			655
599			656
600			657
601			658
602			659
603			660
604			661
605			662
606			663
607			664
608			665
609			666
610	Mingyang Chen, Wen Zhang, Yuxia Geng, Zezhong Xu, Jeff Z. Pan, and Huajun Chen. 2023. Generalizing to unseen elements: A survey on knowledge extrapolation for knowledge graphs. In Proceedings of the Thirty-Second International Joint Conference on Artificial Intelligence, IJCAI 2023, 19th-25th August 2023, Macao, SAR, China, pages 6574–6582. ijcai.org.	Nicolas Hubert, Pierre Monnin, and Heiko Paulheim. 2023. Beyond transduction: A survey on inductive, few shot, and zero shot link prediction in knowledge graphs. CoRR, abs/2312.04997.	667
611			668
612			669
613			670
614			671
615			672
616			673
617			674
618	Mingyang Chen, Wen Zhang, Yushan Zhu, Hongting Zhou, Zonggang Yuan, Changliang Xu, and Huajun Chen. 2022. Meta-knowledge transfer for inductive knowledge graph embedding. In SIGIR '22: The 45th International ACM SIGIR Conference on Research and Development in Information Retrieval, Madrid, Spain, July 11 - 15, 2022, pages 927–937. ACM.	Ren Li, Yanan Cao, Qiannan Zhu, Guanqun Bi, Fang Fang, Yi Liu, and Qian Li. 2022. How does knowledge graph embedding extrapolate to unseen data: A semantic evidence view. In Thirty-Sixth AAAI Conference on Artificial Intelligence, AAAI 2022, Thirty-Fourth Conference on Innovative Applications of Artificial Intelligence, IAAI 2022, The Twelveth Symposium on Educational Advances in Artificial Intelligence, EAAI 2022 Virtual Event, February 22 - March 1, 2022, pages 5781–5791. AAAI Press.	675
619			676
620			677
621			678
622			679
623			680
624			681
625			682
626	Rajarshi Das, Shehzaad Dhuliawala, Manzil Zaheer, Luke Vilnis, Ishan Durugkar, Akshay Krishnamurthy, Alex Smola, and Andrew McCallum. 2018. Go for a walk and arrive at the answer: Reasoning over paths in knowledge bases using reinforcement learning. In	Rui Li, Xu Chen, Chaozhuo Li, Yanming Shen, Jianan Zhao, Yujing Wang, Weihao Han, Hao Sun, Weiwei Deng, Qi Zhang, and Xing Xie. 2023. To copy rather than memorize: A vertical learning paradigm for knowledge graph completion. In Proceedings of the 61st Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers), ACL	683
627			684
628			685
629			686
630			687

688	2023, Toronto, Canada, July 9-14, 2023, pages 6335–6347. Association for Computational Linguistics.	Michael Sejr Schlichtkrull, Thomas N. Kipf, Peter Bloem, Rianne van den Berg, Ivan Titov, and Max Welling. 2018. <a href="#">Modeling relational data with graph convolutional networks</a> . In <i>The Semantic Web - 15th International Conference, ESWC 2018, Heraklion, Crete, Greece, June 3-7, 2018, Proceedings</i> , volume 10843 of <i>Lecture Notes in Computer Science</i> , pages 593–607. Springer.	745 746 747 748 749 750 751 752
690	Ke Liang, Lingyuan Meng, Meng Liu, Yue Liu, Wenxuan Tu, Siwei Wang, Sihang Zhou, Xinwang Liu, and Fuchun Sun. 2022. Reasoning over different types of knowledge graphs: Static, temporal and multi-modal. <i>arXiv preprint arXiv:2212.05767</i> .	Zhixiang Su, Di Wang, Chunyan Miao, and Lizhen Cui. 2023. <a href="#">Multi-aspect explainable inductive relation prediction by sentence transformer</a> . In <i>Thirty-Seventh AAAI Conference on Artificial Intelligence, AAAI 2023, Thirty-Fifth Conference on Innovative Applications of Artificial Intelligence, IAAI 2023, Thirteenth Symposium on Educational Advances in Artificial Intelligence, EAAI 2023, Washington, DC, USA, February 7-14, 2023</i> , pages 6533–6540. AAAI Press.	753 754 755 756 757 758 759 760 761
695	Yankai Lin, Zhiyuan Liu, Maosong Sun, Yang Liu, and Xuan Zhu. 2015. <a href="#">Learning entity and relation embeddings for knowledge graph completion</a> . In <i>Proceedings of the Twenty-Ninth AAAI Conference on Artificial Intelligence, January 25-30, 2015, Austin, Texas, USA</i> , pages 2181–2187. AAAI Press.	Zhiqing Sun, Zhi-Hong Deng, Jian-Yun Nie, and Jian Tang. 2019. <a href="#">Rotate: Knowledge graph embedding by relational rotation in complex space</a> . In <i>7th International Conference on Learning Representations, ICLR 2019, New Orleans, LA, USA, May 6-9, 2019</i> . OpenReview.net.	762 763 764 765 766 767
701	Xin Lv, Yankai Lin, Yixin Cao, Lei Hou, Juanzi Li, Zhiyuan Liu, Peng Li, and Jie Zhou. 2022. <a href="#">Do pre-trained models benefit knowledge graph completion? a reliable evaluation and a reasonable approach</a> . In <i>Findings of the Association for Computational Linguistics: ACL 2022</i> , pages 3570–3581.	Komal K. Teru, Etienne G. Denis, and William L. Hamilton. 2020. <a href="#">Inductive relation prediction by subgraph reasoning</a> . In <i>Proceedings of the 37th International Conference on Machine Learning, ICML 2020, 13-18 July 2020, Virtual Event</i> , volume 119 of <i>Proceedings of Machine Learning Research</i> , pages 9448–9457. PMLR.	768 769 770 771 772 773 774
707	Sijie Mai, Shuangjia Zheng, Yuedong Yang, and Haifeng Hu. 2021. <a href="#">Communicative message passing for inductive relation reasoning</a> . In <i>Thirty-Fifth AAAI Conference on Artificial Intelligence, AAAI 2021, Thirty-Third Conference on Innovative Applications of Artificial Intelligence, IAAI 2021, The Eleventh Symposium on Educational Advances in Artificial Intelligence, EAAI 2021, Virtual Event, February 2-9, 2021</i> , pages 4294–4302. AAAI Press.	Kristina Toutanova, Danqi Chen, Patrick Pantel, Hoi-fung Poon, Pallavi Choudhury, and Michael Gamon. 2015. <a href="#">Representing text for joint embedding of text and knowledge bases</a> . In <i>Proceedings of the 2015 Conference on Empirical Methods in Natural Language Processing, EMNLP 2015, Lisbon, Portugal, September 17-21, 2015</i> , pages 1499–1509. The Association for Computational Linguistics.	775 776 777 778 779 780 781 782
716	Christian Meilicke, Manuel Fink, Yanjie Wang, Daniel Ruffinelli, Rainer Gemulla, and Heiner Stuckenschmidt. 2018. <a href="#">Fine-grained evaluation of rule- and embedding-based systems for knowledge graph completion</a> . In <i>The Semantic Web - ISWC 2018 - 17th International Semantic Web Conference, Monterey, CA, USA, October 8-12, 2018, Proceedings, Part I</i> , volume 11136 of <i>Lecture Notes in Computer Science</i> , pages 3–20. Springer.	Théo Trouillon, Johannes Welbl, Sebastian Riedel, Éric Gaussier, and Guillaume Bouchard. 2016. <a href="#">Complex embeddings for simple link prediction</a> . In <i>Proceedings of the 33rd International Conference on Machine Learning, ICML 2016, New York City, NY, USA, June 19-24, 2016</i> , volume 48 of <i>JMLR Workshop and Conference Proceedings</i> , pages 2071–2080. JMLR.org.	783 784 785 786 787 788 789 790
725	Colin Raffel, Noam Shazeer, Adam Roberts, Katherine Lee, Sharan Narang, Michael Matena, Yanqi Zhou, Wei Li, and Peter J. Liu. 2020. <a href="#">Exploring the limits of transfer learning with a unified text-to-text transformer</a> . <i>J. Mach. Learn. Res.</i> , 21:140:1–140:67.	Liang Wang, Wei Zhao, Zhuoyu Wei, and Jingming Liu. 2022. <a href="#">Simkgc: Simple contrastive knowledge graph completion with pre-trained language models</a> . In <i>Proceedings of the 60th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers), ACL 2022, Dublin, Ireland, May 22-27, 2022</i> , pages 15321–15331.	791 792 793 794 795 796 797 798
730	Ali Sadeghian, Mohammadreza Armandpour, Patrick Ding, and Daisy Zhe Wang. 2019. <a href="#">DRUM: end-to-end differentiable rule mining on knowledge graphs</a> . In <i>Advances in Neural Information Processing Systems 32: Annual Conference on Neural Information Processing Systems 2019, NeurIPS 2019, December 8-14, 2019, Vancouver, BC, Canada</i> , pages 15321–15331.	Apoorv Saxena, Adrian Kochsiek, and Rainer Gemulla. 2022. <a href="#">Sequence-to-sequence knowledge graph completion and question answering</a> . In <i>Proceedings of the 60th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers), ACL 2022, Dublin, Ireland, May 22-27, 2022</i> , pages 2814–2828. Association for Computational Linguistics.	799 800 801

the 2017 Conference on Empirical Methods in Natural Language Processing, EMNLP 2017, Copenhagen, Denmark, September 9-11, 2017, pages 564–573. Association for Computational Linguistics.

Fan Yang, Zhilin Yang, and William W. Cohen. 2017. Differentiable learning of logical rules for knowledge base reasoning. In *Advances in Neural Information Processing Systems 30: Annual Conference on Neural Information Processing Systems 2017, December 4-9, 2017, Long Beach, CA, USA*, pages 2319–2328.

Liang Yao, Chengsheng Mao, and Yuan Luo. 2019. KG-BERT: BERT for Knowledge Graph Completion. *arXiv preprint*. ArXiv:1909.03193 [cs].

Michihiro Yasunaga, Hongyu Ren, Antoine Bosselut, Percy Liang, and Jure Leskovec. 2021. QA-GNN: reasoning with language models and knowledge graphs for question answering. In *Proceedings of the 2021 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, NAACL-HLT 2021, Online, June 6-11, 2021*, pages 535–546. Association for Computational Linguistics.

Hanwen Zha, Zhiyu Chen, and Xifeng Yan. 2022. Inductive relation prediction by BERT. In *Thirty-Sixth AAAI Conference on Artificial Intelligence, AAAI 2022, Thirty-Fourth Conference on Innovative Applications of Artificial Intelligence, IAAI 2022, The Twelveth Symposium on Educational Advances in Artificial Intelligence, EAAI 2022 Virtual Event, February 22 - March 1, 2022*, pages 5923–5931. AAAI Press.

Ningyu Zhang, Qianghuai Jia, Shumin Deng, Xiang Chen, Hongbin Ye, Hui Chen, Huaixiao Tou, Gang Huang, Zhao Wang, Nengwei Hua, and Huajun Chen. 2021. Alicg: Fine-grained and evolvable conceptual graph construction for semantic search at alibaba. In *KDD '21: The 27th ACM SIGKDD Conference on Knowledge Discovery and Data Mining, Virtual Event, Singapore, August 14-18, 2021*, pages 3895–3905. ACM.

Zhanqiu Zhang, Jie Wang, Jieping Ye, and Feng Wu. 2022. Rethinking graph convolutional networks in knowledge graph completion. In *WWW '22: The ACM Web Conference 2022, Virtual Event, Lyon, France, April 25 - 29, 2022*, pages 798–807. ACM.

## A Implementation of Relation-aware Reasoning Neighbors Extraction

Algorithm 1 provides the implementation details of the relation-aware reasoning neighbors extraction method.

---

### Algorithm 1 Relation-aware Reasoning Neighbors Extraction

---

**Input:** KG  $G$ , target triple  $(h, r, t)$ , and  $\alpha$

**Output:** Relation-aware reasoning neighbors

```

1: Get  $R_r^H$  and  $E_r^H$ , initialize  $R_r^{H'}$  and  $R_r^{T'}$  as list()
2: Calculate  $F$  as Eq. (1)
3: for  $h \in E_r^H$  do
4:   for  $r_i \in F[h]$  do
5:     //  $len(F[e][r_i])$  denotes numbers of entities has relation  $r_i$ 
6:      $f_{inv} = \log(len(F)/len(F[e][r_i]))$ 
7:      $p(r_i | r) += f_{r_i}^h \times f_{inv}$ 
8:   end for
9: end for
10: for  $r_i \in R_r^H$  do
11:   Calculate score  $p(r | r_i)$  as Eq. (2)
12:   if  $p(r | r_i) \geq \alpha$  then
13:      $R_r^{H'}.append(r_i)$ 
14:   end if
15: end for
16: Repeat step 3-15 for calculating  $R_r^{T'}$ 
17: Calculate  $R^{h'}$  and  $R^{t'}$  as Eq. (5)
18: if  $R^{h'}$  is not empty and  $R^{t'}$  is not empty then
19:   return  $RN$  as Eq. (6)
20: else
21:   return empty list()
22: end if

```

---

## B Case Study

Table 6 presents a case study on FB15k-237 inductive dataset using Raker, KRST, and BERTRL. For instance, for the test triplet (Don Henley, person profession, Drummer-GB), Raker achieves a rank of 1 with a score of 0.8264, significantly outperforming the second-ranked triplet (Don Henley, person profession, Animation Director) with a score of 0.0314. Due to the absence of a path between Don Henley and Drummer-GB, KRST and BERTRL assign a rank of 50 to the target entity Drummer-GB. This demonstrates the effectiveness of Raker’s approach of incorporating relation-aware neighbors.

Table 6: Case study on FB15k-237 inductive dataset.

Triple to predict	Ground Truth	BERTRL	KRST	Raker
(Don Henley, person profession, ?)	Drummer-GB	<b>Rank: 50</b>	<b>Rank: 50</b>	<b>Rank: 1</b> (Drummer-GB,0.8264) (Animation Director,0.0314) (Diploma,0.000574); (Kappei Yamaguchi,0.0002915);
(Freddie Mercury, profession, ?)	Singer-songwriter-GB	<b>Rank: 50</b>	<b>Rank: 50</b>	<b>Rank: 1</b> (Singer-songwriter-GB,0.0633) (Storyboard Artist,0.0483); (Newcastle upon Tyne,0.000237); (Sex comedy,0.000231);

### C Hits@3 and Hits@10 of Inductive Relation Prediction

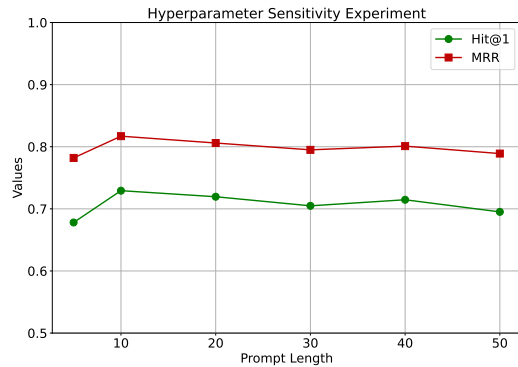
We present Hits@3 and Hits@10 of Inductive Relation Prediction in Table 7. On Hits@3 and Hits@10, Raker achieves state-of-the-art performance on the FB15k-237 dataset and demonstrates strong performance on the WN18RR and NELL-995 datasets.

Table 7: Hits@3 and Hits@10 of inductive relation prediction.

		WN18RR	FB15k-237	NELL-995
Hits@3	BERTRL	0.824	0.653	<b>0.913</b>
	KRST	0.965	0.803	0.818
	Raker	<b>0.968</b>	<b>0.873</b>	0.901
Hits@10	BERTRL	0.824	0.693	0.968
	KRST	<b>1.000</b>	0.932	0.912
	Raker	0.977	<b>0.978</b>	<b>0.978</b>

### D Prompt Length Sensitivity Experiment

To investigate the impacts of different soft prompt lengths on Raker, we conducted a prompt length sensitivity experiment under the FB15K-237 inductive setting as Figure 3. Experimental results show that the variation of  $k$  has little effect on the model’s performance. Considering both computational efficiency and model performance, we choose 10 for  $k$ .

Figure 3: Prompt length  $k$  sensitivity experiment on the FB15K-237 dataset with inductive setting.