
Leveraging LLM-Generated Structural Prior for Causal Inference with Concurrent Causes

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Abstract

Causal inference with many potential concurrent causes presents significant challenges across various fields, from biomedicine to policy analysis. The core challenge lies in understanding how combinations of potential causes influence an outcome, which becomes exponentially more complex as the number of potential concurrent causes increases. To address this challenge, we propose to incorporate structural prior information that describes the interrelations between causes. Specifically, we use a large language model (LLM) to systematically curate this structural information, effectively reducing the complexity of the causal inference task. We validate our method using both a semi-synthetic dataset and a real-world case study from the film industry.¹

1 Introduction

Causal inference from observational data is a critical but challenging task. Traditional settings often focus on binary or continuous treatments [30, 10] while a lot of real-world situations involve complex treatments made up of many concurrent causes. This complexity arises in fields such as medicine, where the combined effects of multiple drugs are evaluated [41], or political science, where multiple policies are studied [6]. In the film industry, producers must understand how different combinations of actors (i.e. a cast) impact the box office performance, where each actor is a *concurrent cause* and a specific cast constitutes a *treatment*, with return on investment (ROI) as the *outcome*. **This illustrative example will be used throughout the paper to demonstrate our methodology.**

Many challenges arise in these novel settings. As the number of potential concurrent causes m increases, the possible combinations grow exponentially, making it infeasible to consider each combination independently. To mitigate this, a common approach is to assume a multilinear relationship between concurrent causes and the outcome [38, 31, 25]. However, this approach is complicated by imbalanced data, where certain causes are observed more frequently, resulting in a higher variance for less common causes. Furthermore, the fundamental problem of causal inference—the inability to observe counterfactual outcomes—becomes more intractable as the number of causes grows, further complicating the estimation of causal effects.

To address these challenges, a potential way is to incorporate prior knowledge to guide the estimation process. Large language models (LLM), which have shown exceptional reasoning abilities in recent years, present a promising solution for systematically curating this prior knowledge by extracting and synthesizing information from vast text corpora, such as Wikipedia. Inspired by recent work on the decomposition of complex tasks into simpler pairwise comparisons [44, 28], we propose a method that takes advantage of LLMs to construct a similarity graph representing the interrelationships

¹Our experiment code is openly available at <https://anonymous.4open.science/r/causal-inference-with-graph-prior-59B5>.

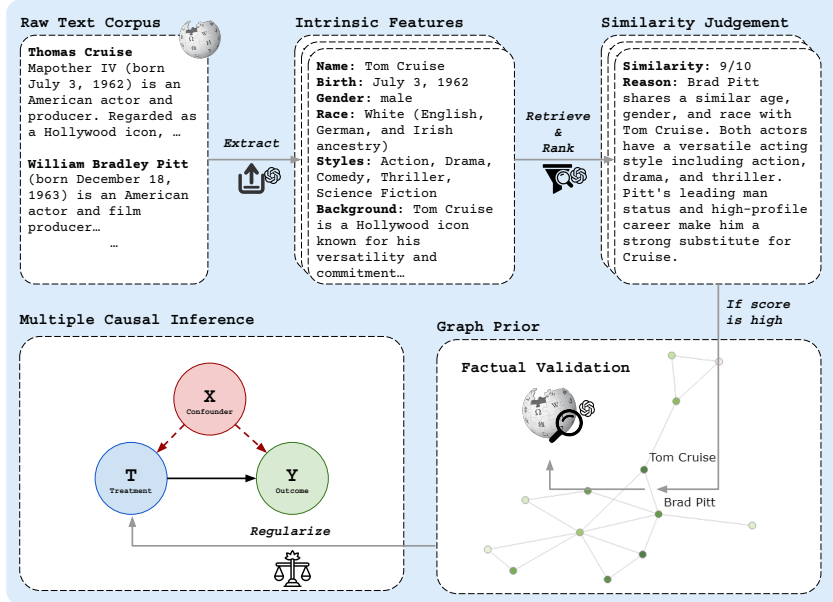


Figure 1: Overview of the proposed methodology for analyzing film ROI (outcome), where actors are considered as concurrent causes. LLMs are used to extract structured actor information from raw text sources (e.g., Wikipedia). Next, we prompt LLMs to retrieve and rank actor pairs based on similarity, constructing a similarity graph where nodes represent actors and edges indicate the belief that one actor can be replaced by another without impacting the film’s ROI. We assess the reliability of these similarity judgments using FActScore [24]. Finally, the similarity graph serves as prior information to regularize causal inference.

between potential concurrent causes. This graph serves as a structural prior that regularizes the estimation process in causal inference. Our methodology is illustrated in Figure 1.

2 Method

2.1 Causal inference with many potential concurrent causes

Traditional approaches of causal inference from observational data aim to estimate the distribution of potential outcomes Y given a binary treatment T , where T can take values $t \in \{0, 1\}$, in the presence of n confounders $\mathbf{x} \in \mathbb{R}^n$. The potential outcome function $Y_i(t)$ represents the outcome of subject i under treatment t . When multiple concurrent causes are considered, the treatment t is extended to a binary vector $\mathbf{v} \in \{0, 1\}^m$, where m represents the number of potential concurrent causes². Consequently, the dataset consists of tuples $\mathcal{D} = \{(\mathbf{v}_i, \mathbf{x}_i, y_i)\}_{i=1}^N$, where N denotes the number of observations.

Our goal is to estimate the average treatment effect (ATE) $\mu(\mathbf{v}) = \mathbb{E}[Y_i(\mathbf{v})]$ for any treatment \mathbf{v} . However, a naive Monte Carlo estimate of $\mu(\mathbf{v})$ are biased due to the *fundamental problem of causal inference*, expressed as

$$\mathbb{E}[Y_i(\mathbf{v})|T = \mathbf{v}] \neq \mathbb{E}[Y_i(\mathbf{v})]. \quad (1)$$

Given the assumptions of no unmeasured confounders, the Stable Unit Treatment Value Assumption (SUTVA), and overlap (a.k.a. positivity) [11], the ATE $\mu(\mathbf{v})$ can be identified using a plug-in estimator:

$$\tau(\mathbf{v}) = \mathbb{E}[\mathbb{E}[Y_i(\mathbf{v})|X, V = \mathbf{v}]] = \mu(\mathbf{v}). \quad (2)$$

²While our method is presented using binary causes and a continuous outcome, it can be generalized to accommodate continuous causes and discrete outcomes.

In practice, we approximate the inner expectation with a parametric function f_θ , often assumed to be linear [38, 31, 25], and estimate $\tau(\mathbf{v})$ via Monte Carlo sampling:

$$\hat{\tau}(\mathbf{v}) = \frac{1}{k} \sum_{j=1:k} f_\theta(\mathbf{x}_j, \mathbf{v}), \text{ where } f_\theta(\mathbf{x}, \mathbf{v}) = \mathbb{E}[Y_i(\mathbf{v})|X, V = \mathbf{v}] = \theta_x^\top \mathbf{x} + \theta_v^\top \mathbf{v} \quad (3)$$

Here k is the sample size, and \mathcal{X} represents the empirical distribution of covariates \mathbf{x} in \mathcal{D} . To learn f_θ , a straightforward method is to use ordinary least square (OLS) linear regression, which serves as our baseline.

2.2 Structural Prior Knowledge

Definition In practice, we often have access to prior information regarding the similarity between potential concurrent causes. This information is based on the belief that *substituting one cause for another is unlikely to significantly affect the potential outcome*. For instance, as illustrated in Figure 1, replacing Tom Cruise with Brad Pitt may not drastically alter a film’s box office. This pairwise similarity relationship can be effectively represented by an undirected graph $\mathcal{G} = (V, A)$ predetermined by domain expertise. Here, the node set $V = \{v_1, \dots, v_m\}$ comprises all potential causes, and the edges are encoded in an adjacency matrix A . We use an unweighted graph in the demonstration.

Graph-Based Regularization We use Laplacian regularization, a graph-based regularization technique that incorporates graph structure information into training, to regularize the linear regression in Eq 3. Laplacian regularization has wide applications in multiple machine learning fields, such as semi-supervised learning and graph learning [47, 46, 2, 40]. It introduces an explicit regularization term into the objective function, leveraging the graph Laplacian, $L = D - A$, where D is the diagonal degree matrix, to promote parameter similarity among strongly connected nodes. Therefore, the new objective is

$$\mathcal{L} = \frac{1}{N} \sum_{i=1}^N (f_\theta(\mathbf{x}_i, \mathbf{v}_i) - y_i)^2 + \lambda \theta_v^\top L \theta_v \quad (4)$$

Here, λ controls the strength of regularization. Intuitively, the Laplacian regularization penalizes the parameter discrepancies between connected nodes, thereby enforcing smoothness in the parameter space in accordance with the graph structure.

2.3 Prior Knowledge Generation with LLMs

Relying on domain experts to curate prior knowledge is often inefficient due to the significant time and financial costs involved. Inspired by recent advancements that leverage LLMs for atomic tasks such as pairwise comparison [44, 28], we propose LLMs to automate the curation of this prior knowledge. We illustrate our method through the aforementioned film example in Figure 1.

Information Retrieval and Intrinsic Feature Extraction To minimize hallucination, we integrate a simplified version of retrieval-augmented generation (RAG) for prior knowledge generation. We retrieve and process a collection of documents for each actor using the Wikipedia API. During the generation phase, these preprocessed documents are provided to LLMs accordingly. This approach enhances reproducibility and stability of the experiment and can be generalized or extended to other applications where domain-specific background information is accessible. However, the raw data retrieved from Wikipedia is not guaranteed to be free from confounding effects. For instance, actor biographies may include information about their collaborations with other actors, which could introduce bias. To address this issue, we employ LLMs to clean the prior information by filtering out extraneous details and preserving only those intrinsic characteristics. Only this refined information is used in subsequent steps.

Graph Construction and Factual Validation A straightforward graph construction process would involve pairwise evaluations of all actors. To reduce the number of API calls, we first prompt LLMs to retrieve the $k_{\text{retrieval}}$ most similar candidates for each actor without providing biographical information. Subsequently, biographical information is added, and LLMs are prompted again to narrow down

Model	MSE (SE.)	
	No Control	Control
Linear Regression	0.349 (0.001)	0.115 (0.003)
Laplacian Reg Linear Regression	0.231 (0.001)	0.018 (0.002)

Table 1: Performance comparison between the proposed method and the baseline under an ideal synthetic scenario (rich observations and accurate prior). Standard errors (in parentheses) are computed across 5 random seeds. The ‘‘Control’’ column indicates results when confounder control is applied using a plug-in estimator, while ‘‘No Control’’ represents the setting without this adjustment.

and re-rank these candidates to obtain at most k_{rank} final choices. A detailed example of this process can be found in Appendix D. To ensure the faithfulness of this process, we solicit both a similarity score and an explanation for each proposed similarity from the LLM. We then use FActScore [24] to evaluate the extent to which the rationale is supported by evidence from the curated documents, ensuring that the generated knowledge is accurate and reliable.

3 Semi-Synthetic Experiment Validation

In this section, we evaluate the effectiveness of the proposed regularization technique using a semi-synthetic dataset. Our goal is to estimate the underlying parameters, θ_v , assuming a linear data generation process. Since obtaining ground truth in real-world scenarios is challenging, we create a semi-synthetic dataset based on the TMDB5000 dataset³ for quantitative validation.

Settings The original TMDB5000 dataset includes data of 901 actors, each having appeared in at least 9 movies, along with revenue information for 2,828 movies. The movies in this dataset span 18 genres and are delivered in 58 languages. In our semi-synthetic dataset, we utilize the genre information as confounders, thus representing each film i with covariates $\mathbf{x}_i \in \{0, 1\}^{18}$. We then generate the treatments \mathbf{v}_i based on the confounders \mathbf{x}_i , and create the true parameters θ from a uniform distribution. The outcomes y_i are generated using a linear relationship as defined in Eq.3. The graph prior is constructed according to pairwise similarity within $\theta_v + \epsilon$, where ϵ is noise that controls the accuracy of the prior. Further details on the data generation process can be found in Appendix C. We report the mean squared error (MSE) between the learned parameters $\hat{\theta}_v$ and the true parameters θ_v .

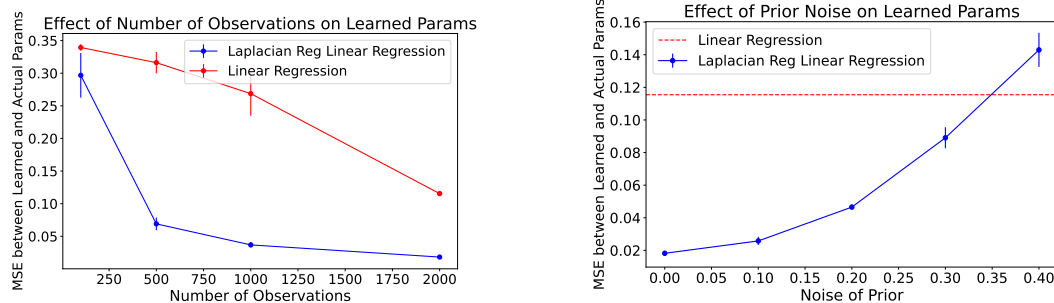


Figure 2: The effects of dataset properties on performance of the models. Error bars indicate the standard error derived by 5 different random seeds. **Left:** The performance of the models vs. the number of observation. **Right:** The performance of graph regularization method vs. the level of noise. The x-axis indicates the standard error of noise σ_θ .

Results We evaluate our methods under three scenarios. (a) In the ideal scenario, the number of observations $N = 2,828$ is large, and the prior information (represented by \mathcal{G}) is accurate. As shown in Table 1, the proposed method significantly outperforms the baseline, yielding more accurate

³<https://www.kaggle.com/tmdb>

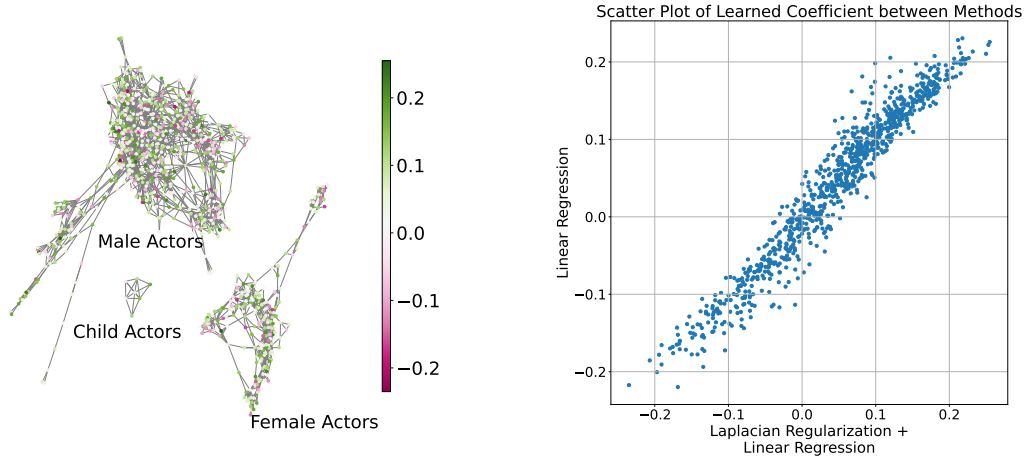


Figure 3: **Left:** Graph prior generated by LLM, showing connections among 901 actors. The presence of an edge indicates the two connected actors are similar. Node colors indicate learned parameters (green: positive; red: negative). **Right:** Coefficients learned by two methods. Despite a very small regularization, certain data points are affected significantly.

estimates of θ_v regardless of whether confounder control is applied. (b) Next, we vary the number of observations to evaluate the performance of both methods under sparse data conditions. Figure 2 (Left) shows that our method consistently outperforms the baseline. The graph prior proves especially useful when the number of observations is moderate, as nodes with limited data benefit from similar neighboring nodes. However, when the number of observations is reduced to as few as 100, the performance gap between the two methods narrows due to the limited data available for accurate prediction. Conversely, when the number of observations is abundant, the performance of graph regularization saturates, reducing the disparity between the methods. (c) Finally, we investigate the robustness of the graph regularization method under varying levels of noise in the graph prior. Specifically, we examine scenarios where the noise standard deviation σ_ϵ is adjusted. Given that the standard deviation of θ_v is $\sigma_\theta = 1/\sqrt{3} \approx 0.58$, the injected noise is substantial compared to the scale of the ground truth parameters. As seen in Figure 2 (Right), our approach continues to outperform basic linear regression until σ_ϵ reaches 0.4, demonstrating its resilience in noisy environments.

4 Real-World Case Study

In this section, we demonstrate the effectiveness of the proposed pipeline through a real-world case study using the original TMDb5000 dataset.

4.1 Prior Knowledge Generation with LLMs

Graph Construction and Validation We follow the pipeline described in Sec 2.3 to generate the graph prior. For each actor, intrinsic features such as *gender*, *birth*, *race*, *acting styles*, and *background* information are extracted from Wikipedia. We set $k_{\text{retrieval}} = 10$ and $k_{\text{rank}} = 5$ during graph construction, utilizing the gpt-4o-2024-05-13 model for all experiments⁴.

Graph Validation We use FActScore [24] as a measurement of the trustworthiness of the LLM-generated graph prior. It decomposes the LLM generation into atomic facts and checks the average groundedness of each atomic fact against a trusted corpus. In our case, we evaluate the FActScore of the reasoning provided along with the similarity judgement. Using the RAG, our final average score for the generation is 89.5%, indicating most of the statements are supported by facts⁵.

⁴The prompt and sample response from the LLM are provided in Appendix D.

⁵The implementation details of FActScore are shown in Appendix E.

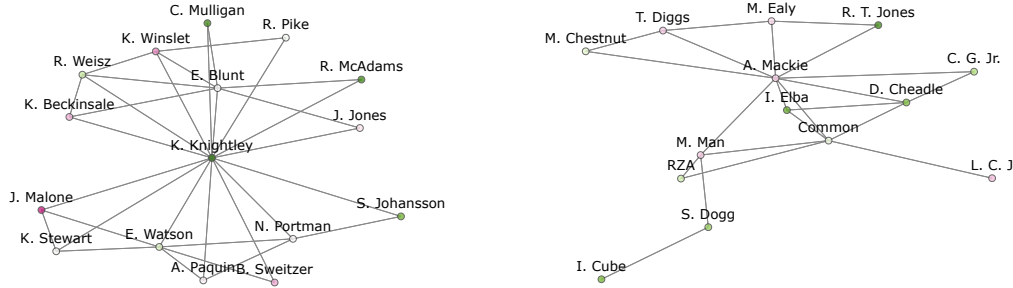


Figure 4: Ego networks of actors with high discrepancy in coefficients. Node colors indicate learned parameters (same as Figure 3). **Left:** 1-hop ego graph centered on Keira Knightley. **Right:** 2-hop ego graph centered on Method Man.

Results The extracted graph prior is visualized in Figure 3 (Left), comprising 2078 edges with an average node degree of 2.31. Notably, the graph features three major components corresponding to male, female, and child actors, suggesting that it effectively captures essential information on actor similarity. A few isolated nodes are also present, such as Aasif Mandvi, who is the only actor in the dataset with an Indian background, demonstrating his irreplaceability.

4.2 Comparison Study

Settings Utilizing the generated graph prior, we apply Laplacian regularization to linear regression and compare it with standard linear regression without regularization. A small regularization weight of $\lambda = 0.001$ is chosen to ensure that the scale of the learned coefficients remains largely unaffected.

Results Figure 3 (Right) shows the disparity in the learned coefficients between the two methods, with a Pearson correlation of 0.97. Despite the minimal regularization applied, there is a noticeable difference in the coefficients attributed to specific actors. We present case studies of two actors with notable coefficient discrepancies between standard and Laplacian-regularized linear regressions. Figure 4 (Left) shows Keira Knightley’s ego graph, where her positive coefficient in the standard regression is significantly reduced under the graph-regularized model by 0.099. This reduction reflects the lower coefficients of her neighbors, with regularization penalizing her value accordingly. In contrast, Method Man’s coefficient increases with regularization by 0.071, influenced by positive coefficients of nearby actors like RZA and Richard T. Jones, shown in Figure 4 (Right). Notably, Method Man is recognized more for his contributions to hip hop than acting, leading to fewer collaborations with prominent directors. The directors of his notable films, including Mike Devine and Jonathan Levine, are not widely recognized. This highlights a possible neglect of important confounding variables, such as a movie’s director, underscoring the necessity for additional control measures in the analysis.

5 Discussion

Conclusion We propose a graph-based method for causal inference with multiple concurrent causes. By using LLMs to extract prior knowledge and construct the graph, we enhance the model’s ability to capture complex relationships that traditional methods overlook. This approach demonstrates the value of LLMs in enriching causal inference with structured, context-aware insights.

Limitations and Future Work One limitation of the current approach lies in the similarity judgment by LLM, which requires inputting the full list of actors into the LLM’s context window. For larger datasets, this can exceed the LLM’s context limit, though this issue could potentially be mitigated by splitting the list across multiple windows. Additionally, the proposed method assumes a linear data generation process, which may not fully capture the complexities of real-world scenarios. A promising direction for future work is to extend the approach by using the graph prior for data augmentation, enabling the model to better handle non-linear relationships and more intricate causal structures.

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A Visualization of Graph Prior

We use `graph-tool`'s Hierarchical community detection algorithm to plot the visualization of the extracted graph prior, shown in Figure 5.

B Related Work

Multiple Causal Inference Multiple causal inference is a topic of interest, spurred by a plethora of applications that have garnered attention in the machine learning community, inclusive of genome-wide association studies (GWAS), recommender systems, and polypharmacy [39, 32, 29, 31]. Numerous studies have been conducted in the realm of causal inference with multiple versions of treatments, where a single chosen treatment is administered to a subject per observation [3, 43, 10, 45, 22, 21, 29, 35, 17]. Alternatively, some studies focus on combinatorial treatments, where multiple treatments can be administered concurrently to a subject [15, 38, 27, 31]. The latter type of study is generally more complex due to the expanded treatment space and is therefore more challenging to approach. Our work also falls into this category. [31] explores the extension of G-computation, inverse propensity score estimation, and the double robust estimator with respect to four concurrent treatments. [39] proposes a novel algorithm "deconfounder" to tackle the problem of unobserved confounders in multiple causal inference scenarios. [27] seeks to address severe data scarcity by utilizing data augmentation techniques.

Causal Inference Incorporating Graph Structure A substantial body of work on causal inference involves the integration of graph structures or graph data. Some studies consider subject networks and corresponding network effects that potentially violate the basic assumptions of causal inference from observational data [12, 1, 7, 18, 13, 26, 34, 8]. For instance, [12] elucidates the limitations of standard graph machine learning models in estimating causal effects on networked observational data. Other research efforts have focused on estimating the causal effects of graph-structured treatments. As an example, [9] takes into account the graph structure of drug chemicals and employs a Graph Neural Network (GNN) to learn the representation of graph treatments. However, none of the existing work explores the setting where multiple treatments are modeled through a graph structure to estimate causal effects.

LLMs and Graph Creation As large language models emerge these years, they are applied to various downstream tasks, including graph construction in different contexts. One such kind of graphs are the knowledge graphs [14, 23], where LLMs serve as domain experts to develop ontology and build graphs that represent real-world knowledge. In causal inference, previous studies also leverage LLMs to explore causal relationships for directed acyclic graphs (DAG) engineering [19]. For instance, [16] opens the frontier by utilizing LLMs to determine pair-wise causal relationships. Despite the high accuracy of this approach, it actually has some drawbacks, such as cyclic graph structure [36], the $O(N^2)$ complexity [4] and false information [20, 33]. To mitigate these problems, other works also investigate the role of LLMs in causal discovery [42, 20, 37, 5], which focuses on

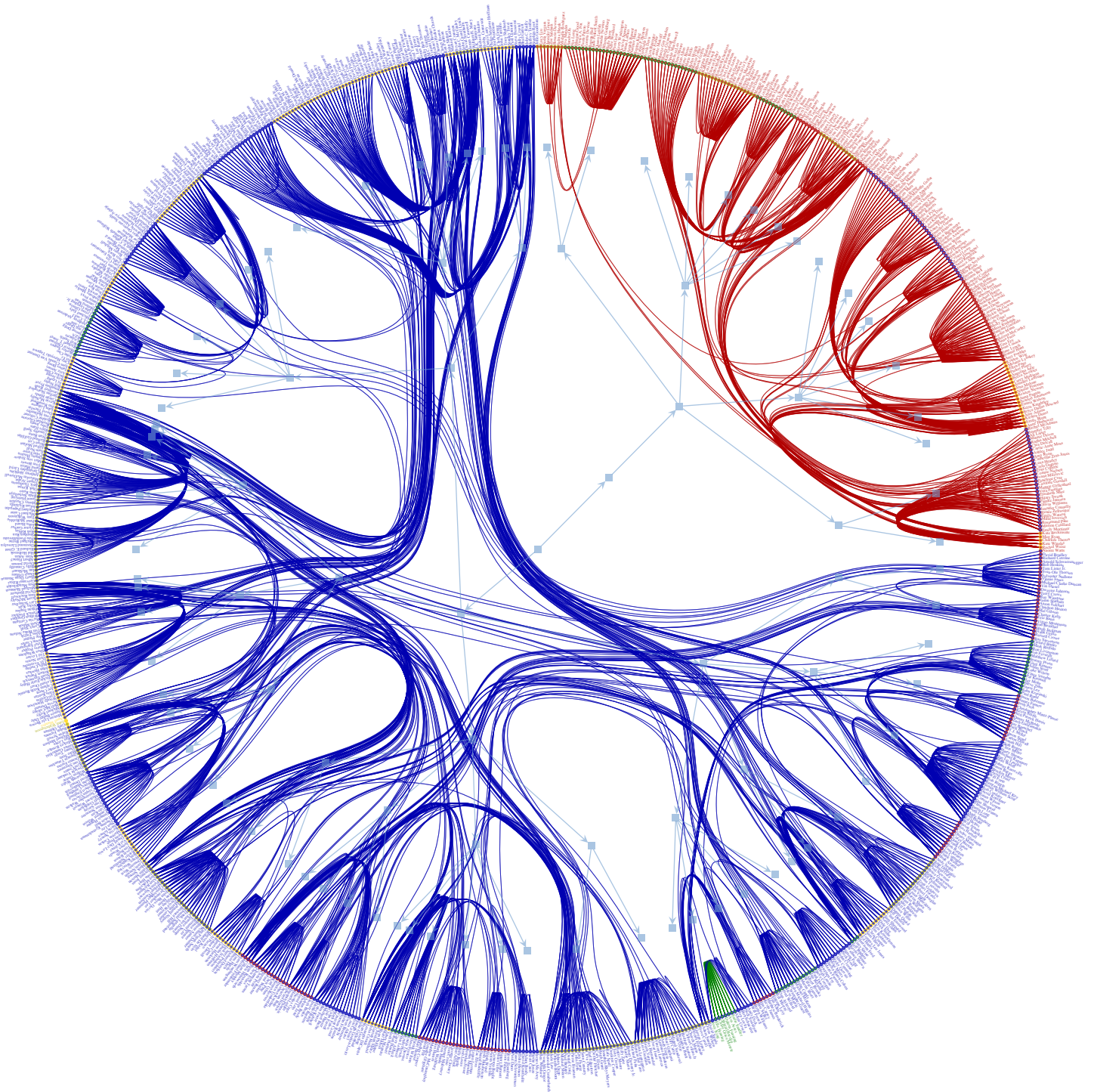


Figure 5: Graph prior that represents actor similarity relationships, generated using prior knowledge from ChatGPT, showing connections among 901 actors. Each edge indicates a similarity between the connected actors. Blue nodes represent male actors, red nodes represent female actors, and green nodes represent child actors. Two isolated nodes are highlighted in yellow and olive.

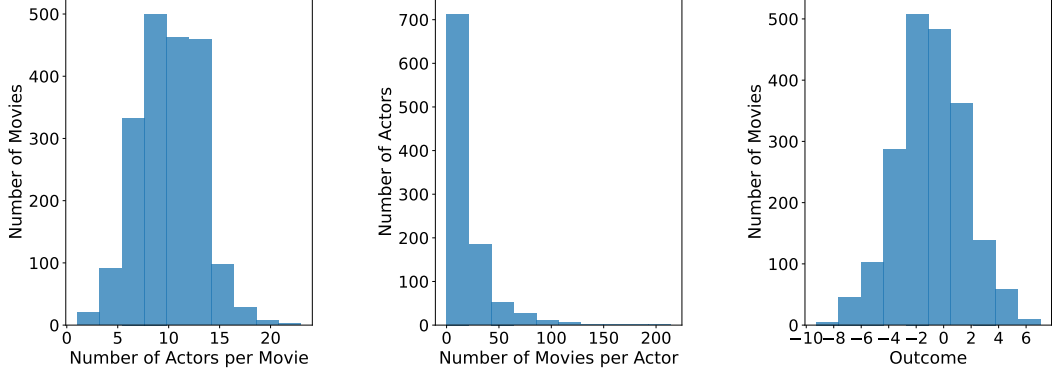


Figure 6: Statistical Distribution Characteristics of the Synthetic Dataset. The dataset mirrors real-world distributions, with both the number of actors and ground truth outcomes adhering to a normal distribution. Furthermore, the distribution of movies per actor indicates that most actors participate in a limited number of movies, paralleling real-world trends.

recovering instead of generating causal graphs. While most of the previous research is focusing on causal discovery, our research is trying to expand the boundaries of LLMs in graph-guided causal estimation, as a reliable foundation model for structural prior retrieval.

C Constructing the Semi-synthetic Dataset

When generating the semi-synthetic dataset, we use the genres of a movie in the original dataset as the confounder, i.e. $x \in \{0, 1\}^{18}$. The actors are the causes and the outcome of interest Y is the ROI of a movie. Only the confounders are from the real-world distribution, both treatments and outcomes are generated. We suppose there are $m = 1000$ actors in total so a treatment is a binary vector $v \in \{0, 1\}^{1000}$ indicating whether 1000 actors are in the movie or not. The relation of the confounder genre and the cause actors is defined by a preference matrix W :

$$p_v = \alpha \cdot \text{softmax}(Wx) \quad (5)$$

where $W \in \mathbf{R}^{n \times m}$ and each element of it follows the normal distribution $\mathcal{N}(0, 1)$. The probability of an actor j appeared in the movie is then $P[v_j = 1] = p_{v_j}$. We sample the actors of a movie from the Bernoulli distribution $\mathcal{B}(p_{v_j})$ accordingly. α is the expected number of actors per movie so that given a movie, $E[\sum_{j=1}^m v_j] = \alpha$. We set α to be 10 in our experiments to be reasonably close to a real-world setting. The ground truth causal and confounder effect θ_v and θ_x are generated from a uniform distribution $\mathcal{U}(-1, 1)$. We then define the linear outcome model:

$$y_i = \theta_v^T v_i + \theta_x^T x_i + \epsilon_y \quad (6)$$

as we assume the linear model and $\epsilon_y \sim \mathcal{N}(0, 1)$. With the ground truth causal effect, we use the Gaussian kernel to measure the similarity between the actors to create a binary graph prior A :

$$A_{ij} = \mathbb{1} \left[\exp \frac{(\tilde{\theta}_{v_i} - \tilde{\theta}_{v_j})^2}{2\sigma_v^2} \geq T \right] \quad (7)$$

where σ_v and T are parameters to control the density of the graph. In particular, the prior is usually expected to be noisy. Therefore, we set $\tilde{\sigma}_v = \sigma_v + \epsilon$ where $\epsilon \sim \mathcal{N}(0, \sigma_\epsilon)$ and control σ_ϵ to inject noise of different scale in our semi-synthetic setting.

D Prior Information Graph Construction Detail

D.1 Prompts

The following section shows the complete prompts used to generate the prior information graph in this paper.

D.1.1 Intrinsic Feature Extraction

You will be provided with an introduction of <ACTOR_NAME> and your task is to summarize the following information from the text:

1. gender
2. birth
3. race
4. acting styles
5. other background information that demonstrates the intrinsic characteristics.

Each section should be less than a few sentences. Think step by step and present your final answer in JSON format.

Information

The information for <ACTOR_NAME> is provided here:
<DESCRIPTION>

JSON Format

The JSON format should be as follows:

```
{
  "name": "<name>",
  "birth": "<birthday>",
  "gender": "<gender>",
  "race": "<race>",
  "styles": "<styles>",
  "background": "<background>"
}
```

Example of an output JSON

```
{
  "name": "Actor A",
  "birth": "October 1, 1970",
  "gender": "male",
  "race": "white",
  "styles": "Method acting, Classical theatre, Comedy",
  "background": "Actor A was born in a small town in the Midwest. He discovered his passion for acting in high school theatre and went on to study drama at a prestigious performing arts school. Known for his versatility, he has performed in a variety of roles ranging from Shakespearean plays to modern comedies."
}
```

D.1.2 Candidates Retrieval

Context

You are an expert in the film industry, with a deep understanding of actors and actresses, including their characteristics and connections within the industry. Your task is to identify which 5 actors or actresses are most similar to <ACTOR_NAME>, excluding <ACTOR_NAME> themselves. This is to suggest that a director could potentially replace <ACTOR_NAME> with one of these five

individuals without significantly impacting the movie's outcome. Consider factors such as their acting style, genres they typically work in, gender, age, nationality, ethnicity, and other relevant traits. Additionally, you may weigh their professional experiences and past collaborations. These suggestions are merely guidelines; you may rely on other evidence if you believe it more accurately supports your analysis.

We provide the information for <ACTOR_NAME>:
<DESCRIPTION>

Please follow the steps below:

1. Provide a description of <ACTOR_NAME> with at least three sentences. Outline your criteria for similarity, explaining what factors you believe are most critical for this comparison.
2. From the provided 'Actor List', preliminarily select 10 candidates. At this stage, a detailed explanation for each choice is not required, and they do not need to be ranked or meticulously filtered for relevance.

Verify the presence of your candidates in the 'Actor List'. If any selected individuals do not appear on this list, they should be excluded from further consideration.

Return the final result in JSON format.

JSON Format

The JSON format should be as follows:

```
[{"name": <name>, "id": <id>}, ...]
```

Actor List

<ACTOR_LIST>

1) Provide description and outline evaluation similarity criterion	<p>Description of Tom Cruise</p> <p>Tom Cruise is a renowned Hollywood actor born on July 3, 1962. He is known for his versatility across various genres, including action, drama, comedy, thriller, and science fiction...</p> <p>Criteria for Similarity</p> <ol style="list-style-type: none"> 1. Acting Style and Genres: Actors who have demonstrated versatility across action, drama, comedy, thriller, and science fiction. 2. Gender and Age: Male actors who are relatively close in age to Tom Cruise. 3. Nationality and Ethnicity: Primarily American or actors who have a significant presence in Hollywood. 4. Professional Experience: Actors with a substantial body of work and a history of high-profile roles. 5. Physicality and Stunt Work: Actors known for performing their own stunts or having a strong physical presence in their roles. 										
2) Retrieve 10 candidates from the provided list	<p>Preliminary Selection of 10 Candidates</p> <table border="0"> <tr> <td>1. Brad Pitt (id: 280)</td> <td>6. Robert Downey Jr. (id: 61)</td> </tr> <tr> <td>2. Leonardo DiCaprio (id: 161)</td> <td>7. Hugh Jackman (id: 195)</td> </tr> <tr> <td>3. Christian Bale (id: 20)</td> <td>8. Will Smith (id: 130)</td> </tr> <tr> <td>4. Matt Damon (id: 433)</td> <td>9. Johnny Depp (id: 5)</td> </tr> <tr> <td>5. Keanu Reeves (id: 392)</td> <td>10. Mark Wahlberg (id: 226)</td> </tr> </table>	1. Brad Pitt (id: 280)	6. Robert Downey Jr. (id: 61)	2. Leonardo DiCaprio (id: 161)	7. Hugh Jackman (id: 195)	3. Christian Bale (id: 20)	8. Will Smith (id: 130)	4. Matt Damon (id: 433)	9. Johnny Depp (id: 5)	5. Keanu Reeves (id: 392)	10. Mark Wahlberg (id: 226)
1. Brad Pitt (id: 280)	6. Robert Downey Jr. (id: 61)										
2. Leonardo DiCaprio (id: 161)	7. Hugh Jackman (id: 195)										
3. Christian Bale (id: 20)	8. Will Smith (id: 130)										
4. Matt Damon (id: 433)	9. Johnny Depp (id: 5)										
5. Keanu Reeves (id: 392)	10. Mark Wahlberg (id: 226)										
3) Select 5 final candidates, provide score and explanation	<pre>{ "name": "Brad Pitt", "id": 280, "similarity_score": 9, "explanation": "Brad Pitt shares a similar age, gender, and race with Tom Cruise. Both actors have a versatile acting style and have starred in a wide range of genres, including action, drama, and thriller. Pitt's leading man status and high-profile career make him a strong substitute for Cruise." }, ...</pre>										

Figure 7: Illustration of leveraging LLM (ChatGPT) to generate a graph prior for actors from TMDB5000. A three-step dialogue is used to identify five actors similar to Tom Cruise. The prompting process are detailed in Appendix D

D.1.3 Candidates Reranking

Context

You are an expert in the film industry, with a deep understanding of actors and actresses, including their characteristics and connections within the industry. Your task is to identify which 5 actors or actresses are most similar to <ACTOR_NAME> from the candidates list, excluding <ACTOR_NAME> themselves. This is to suggest that a director could potentially replace <ACTOR_NAME> with one of these five individuals without significantly impacting the movie's outcome. Consider factors such as their acting style, genres they typically work in, gender, age, nationality, ethnicity, and other relevant traits. Additionally, you may weigh their professional experiences and past collaborations. These suggestions are merely guidelines; you may rely on other evidence if you believe it more accurately supports your analysis.

Please follow the steps below:

1. Narrow your selection down to the 5 most suitable candidates based on the initial criteria.
2. Present your final selection in JSON format, listing each actor's name, ID (as indicated in the 'Actor List'), similarity score (on a scale of 1-10), and a brief explanation of why each actor or actress is considered similar to <ACTOR_NAME>.

JSON Format

The JSON format should be as follows:

```
[
  {
    "name": "<name>",
    "id": <id>,
    "similarity_score": <similarity_score>,
    "explanation": "...",
  },
  ...
]
```

Example of Scoring Standard

An example is provided below to indicate how the similarity score should be interpreted. This is only a guide, and you may use your own judgment to assign scores.

```
[
  {
    "name": "Actor A",
    "id": 123,
    "similarity_score": 3,
    "explanation": "Actor A shares the action genre with <ACTOR_NAME> but has a distinctly different acting style, focusing more on physical prowess than nuanced emotional expression. Additionally, there's a significant age difference, limiting role interchangeability."
  },
  {
    "name": "Actor B",
    "id": 456,
    "similarity_score": 5,
    "explanation": "Actor B and <ACTOR_NAME> have both thrived in drama films and share a similar acting range. However, Actor B has primarily been cast in supporting roles, and their physical appearance is quite different, which might affect
```

```

        audience acceptance in leading roles traditionally played by <
        ACTOR_NAME>."
    },
    {
        "name": "Actor C",
        "id": 789,
        "similarity_score": 8,
        "explanation": "Actor C is very similar to <ACTOR_NAME> in age,
            acting style, and the types of characters portrayed,
            particularly in romantic comedies. While there's a slight
            difference in their career trajectories, Actor C could
            seamlessly step into roles typically associated with <
            ACTOR_NAME>."
    },
    {
        "name": "Actor D",
        "id": 1011,
        "similarity_score": 10,
        "explanation": "Actor D is almost indistinguishable from <
            ACTOR_NAME> in terms of physical appearance, acting range, and
            genre specialization. They have even been considered for the
            same roles in the past, making Actor D an ideal substitute for
            <ACTOR_NAME> in virtually any project."
    }
}
]

```

```

# Candidate list
Make your selection based on the list below. The descriptions for the
actors are also provided for your reference:
<candidates_info>

```

D.2 EXAMPLE RESPONSE

```

{
    "name": "Sam Worthington",
    "birth": "August 2, 1976",
    "gender": "male",
    "race": "white",
    "styles": "Method acting, Action roles, Dramatic roles",
    "background": "Sam Worthington is an Australian actor born to
        English parents in Surrey, UK, and moved to Australia as an
        infant. He studied drama but did not finish high school and
        began his career through construction work before gaining a
        scholarship to the National Institute of Dramatic Art. Known for
        his lead roles in the Avatar franchise and Terminator Salvation
        , Worthington has received critical acclaim in both film and
        television, and is also recognized for his work in video games."
}

```

Description of Sam Worthington

Sam Worthington is an Australian actor born on August 2, 1976, known for his method acting and roles in action and dramatic films. He gained international fame for his lead roles in the "Avatar" franchise and "Terminator Salvation." Worthington's background includes a mix of English and Australian influences, and he has received critical acclaim in both film and television, as well as recognition for his work in video games.

Criteria for Similarity

1. ****Acting Style****: Method acting, action roles, dramatic roles.
2. ****Genres****: Primarily action and drama.
3. ****Gender****: Male.

4. ****Age Range****: Born between 1970 and 1985.
5. ****Nationality/Ethnicity****: Preferably Australian or actors with a similar Western background.
6. ****Professional Experience****: Experience in high-profile action and dramatic films, possibly with some involvement in franchises or video games.
7. ****Past Collaborations****: Actors who have worked with similar directors or in similar types of projects.

Preliminary Selection of 10 Candidates

1. ****Orlando Bloom**** (ID: 6)
2. ****Christian Bale**** (ID: 20)
3. ****Tom Hardy**** (ID: 24)
4. ****Liam Neeson**** (ID: 29)
5. ****Ben Mendelsohn**** (ID: 30)
6. ****Chris Hemsworth**** (ID: 62)
7. ****Jeremy Renner**** (ID: 66)
8. ****Daniel Craig**** (ID: 15)
9. ****Jake Gyllenhaal**** (ID: 298)
10. ****Gerard Butler**** (ID: 421)

Verification and Final Result

All selected candidates are present in the provided 'Actor List'. Here is the final result in JSON format:

```

'''json
[
  {"name": "Orlando Bloom", "id": 6},
  {"name": "Christian Bale", "id": 20},
  {"name": "Tom Hardy", "id": 24},
  {"name": "Liam Neeson", "id": 29},
  {"name": "Ben Mendelsohn", "id": 30},
  {"name": "Chris Hemsworth", "id": 62},
  {"name": "Jeremy Renner", "id": 66},
  {"name": "Daniel Craig", "id": 15},
  {"name": "Jake Gyllenhaal", "id": 298},
  {"name": "Gerard Butler", "id": 421}
]
'''

```

Based on the provided criteria and the candidate list, here are the five actors most similar to Sam Worthington:

```

'''json
[
  {
    "name": "Chris Hemsworth",
    "id": 62,
    "similarity_score": 9,
    "explanation": "Chris Hemsworth and Sam Worthington share a similar physical presence and have both starred in action-packed roles. Hemsworth's work in the Marvel Cinematic Universe as Thor aligns well with Worthington's roles in Avatar and Clash of the Titans. Both actors are Australian, which adds to their similarity in terms of accent and cultural background."
  },
  {
    "name": "Gerard Butler",
    "id": 421,
    "similarity_score": 8,
    "explanation": "Gerard Butler and Sam Worthington have both taken on roles in action and historical epics. Butler's performance

```



```

    in 300 is comparable to Worthington's in Clash of the Titans.
    Both actors have a rugged, commanding screen presence and have
    worked in similar genres, making Butler a suitable
    replacement."
  },
  {
    "name": "Tom Hardy",
    "id": 24,
    "similarity_score": 7,
    "explanation": "Tom Hardy and Sam Worthington share a penchant for
    intense, physically demanding roles. Hardy's versatility and
    experience in action films like Mad Max: Fury Road align well
    with Worthington's filmography. Although Hardy is known for
    his method acting, their overall acting styles and genre
    preferences are quite similar."
  },
  {
    "name": "Jeremy Renner",
    "id": 66,
    "similarity_score": 7,
    "explanation": "Jeremy Renner and Sam Worthington have both
    excelled in action and thriller genres. Renner's roles in the
    Bourne series and the Marvel Cinematic Universe showcase his
    ability to handle intense, action-oriented characters, similar
    to Worthington's roles in Avatar and Terminator Salvation."
  },
  {
    "name": "Jake Gyllenhaal",
    "id": 298,
    "similarity_score": 6,
    "explanation": "Jake Gyllenhaal and Sam Worthington both have a
    versatile range, though Gyllenhaal leans more towards dramatic
    and psychological roles. However, Gyllenhaal's performances
    in action-thrillers like Source Code and End of Watch
    demonstrate his capability to take on roles similar to those
    of Worthington."
  }
]
'''

```

These actors were selected based on their similarities in acting style, genre preferences, physical presence, and professional experiences, making them suitable replacements for Sam Worthington.

E FActScore Implementation

The FActScore evaluation is basically performed using the original implementation in <https://github.com/shmsw25/FActScore>. For each edge in the replacement graph, we retrieve the documents relevant to the two actors involved from wikipedia database, and prompt GPT-4o-mini for groundedness evaluation. We just skip the evaluation for certain edge if the document for either of the involved actor does not exist.

We evaluated 4161 reasonings in total. The average number of atomic facts contained in each edge reasoning is 11.20. The resulting FActScore is 85.4% with a length penalty $\gamma = 10$, which means the generation will be penalized if it is shorter than 2 sentences. Without this penalty, the FActScore is 89.5%.