# ONE2ALL: INDIVIDUAL REWEIGHTING FOR USER ORIENTED FAIRNESS IN RECOMMENDER SYSTEMS

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## ABSTRACT

Recommender systems often manifest biases toward a small user group, resulting in pronounced disparities in recommendation performance, i.e., the User-Oriented Fairness (UOF) issue. Existing research on UOF faces three major limitations, and no single approach effectively addresses all of them. Limitation 1: Post-processing methods fail to address the root cause of the UOF issue. Limitation 2: Some in-processing methods rely heavily on unstable user similarity calculations under severe data sparsity problems. Limitation 3: Other in-processing methods overlook the disparate treatment of individual users within user groups. In this paper, we propose a novel Individual Reweighting for User-Oriented Fairness framework, namely IR-UOF, to address all the aforementioned limitations. IR-UOF serves as a versatile solution applicable across various backbone recommendation models to achieve UOF. The motivation behind IR-UOF is to introduce an in-processing strategy that addresses the UOF issue at the individual level without the need to explore user similarities. We conduct extensive experiments on three real-world datasets using four backbone recommendation models to demonstrate the effectiveness of IR-UOF in mitigating UOF and improving recommendation fairness. The code of this paper is available at https://anonymous.4open.science/r/IR-UOF-D53B/

## 1 INTRODUCTION

Fairness is currently a critical research field in Recommender Systems (RSs) Deldjoo et al. (2022);
Chen et al. (2023a). RS is a complex domain involving frequent interactions between users and items Zheng et al. (2022); Li et al. (2022), leading to fairness issues arising from both the user Li et al. (2021); Rahmani et al. (2022) and item side Dash et al. (2021); Deldjoo et al. (2021b). In this paper, we focus on the fairness issue related to performance disparities among different user groups.

RSs often exhibit bias toward a small group of users, 037 resulting in significant unfairness in the quality of recommendations Li et al. (2021); Rahmani et al. (2022); Wen et al. (2022b), referred to as the User-Oriented 040 Fairness (UOF) issue. We define users who receive 041 more satisfying recommendation results as advan-042 taged users and other users as disadvantaged users, 043 following Li et al. (2021); Rahmani et al. (2022). 044 Existing research has shown that advantaged users constitute only a small proportion of the total user base Li et al. (2021), as many users suffer from the 046 data sparsity problem Han et al. (2023b) and fail to 047 receive satisfactory recommendations. Therefore, ad-048 dressing the UOF issue is crucial in RSs to enhance the overall quality of recommendation services. 050



Figure 1: Gradients come from different users in a training epoch of LightGCN in the Epinion dataset.

Existing research in addressing the UOF issue includes post-processing methods (directly adjusting the recommendation lists) and in-processing methods (adjusting the training process of recommendations).
 All these methods face three key limitations, and *none of the existing research can address all of them*. Limitation 1: Post-processing methods fail to address the root cause of the UOF issue. Some

existing research proposes post-processing methods Li et al. (2021); Rahmani et al. (2022) to re-rank
the calculated recommendation lists *after model training* to balance advantaged and disadvantaged
user groups. However, *the root cause of the UOF issue lies in the unfair training process*, where
the recommendation models are dominated by advantaged users Han et al. (2023a; 2024a). As
illustrated in Figure 1, the advantaged users, who make up only 5% of the population, contribute
17.2% of the gradients in a single training epoch. Post-processing methods cannot mitigate the unfair
training process and are thus unable to address the root cause of the UOF issue, resulting in limited
performance.

062 **Limitation 2**: Some in-processing methods rely heavily on unstable user similarity calculations 063 under severe data sparsity problems. Some studies Han et al. (2023a; 2024a;b) adopt in-processing 064 methods to mitigate unfair training processes in recommendation models. These approaches calculate user similarities based on user-item interactions. Then they aim to enhance the training process for 065 disadvantaged users by enabling them to learn from other similar users. However, disadvantaged 066 users often face severe data sparsity problems Li et al. (2021); Rahmani et al. (2022), and the sparse 067 interactions result in unstable similarity calculations based on user-item interactions. Consequently, 068 the performance of these methods is limited. 069

**Limitation 3**: Other in-processing meth-071 ods overlook the disparate treatment of individual users within user groups. Some 072 methods Wen et al. (2022b) propose strate-073 gies that enhance the importance of loss 074 values for the entire disadvantaged user 075 group during model training. However, 076 as illustrated in Figure 2, different users 077 within disadvantaged or advantaged users 078 also tend to be treated differently, i.e., 079 the under-representation problem Chai & Wang (2022). The lack of individualized 081 optimization strategies for each user reduces the effectiveness of these methods, resulting in less significant performance 083 improvement Han et al. (2024a). Over-084 all, none of the existing research fully ad-085 dresses all three of these limitations, leav-086 ing the UOF issue insufficiently resolved. 087



Figure 2: Distribution of user performance among advantaged and disadvantaged user groups, with LightGCN as the recommendation model.

088 In this paper, we propose a novel Individual Reweighting for User-Oriented Fairness framework, named IR-UOF, to address all the aforementioned limitations. IR-UOF serves as a versatile solution 089 applicable across various backbone recommendation models to achieve UOF. The motivation behind 090 IR-UOF is to introduce an in-processing strategy that addresses UOF issues at the individual level 091 without the need to explore user similarities based on user-item interactions. In detail, to tackle 092 Limitation 1, IR-UOF addresses the root cause of the UOF issue by introducing an in-processing 093 strategy to focus on mitigating the unfair training processes of recommendation models. To tackle 094 Limitation 2, IR-UOF avoids relying on user similarity calculations based on limited user-item interactions. Instead, IR-UOF focuses on the loss value of each user, as it directly reflects the quality 096 of the user's training. By adjusting the weights of losses for different users, the model's emphasis on various users can be modulated. To address Limitation 3, IR-UOF introduces an individual-level 098 reweighting method, transcending the constraints of group-level optimization. As illustrated in Figure2, it is not only disadvantaged users but also individual users among the advantaged group who 099 may be overlooked. IR-UOF adaptively adjusts the weight of the loss value for all users, providing 100 precise strategies tailored to each user's training situation. This approach allows IR-UOF to enhance 101 the training quality of every individual user who is dominated by recommendation models, achieving 102 overall fairness through individual optimization, i.e., One to All. 103

We conduct extensive experiments on three publicly available real-world datasets using four backbone
 recommendation models. The effectiveness of IR-UOF is comprehensively assessed using evaluation
 metrics from various perspectives. Experimental results demonstrate that IR-UOF outperforms all
 State-Of-The-Art (SOTA) methods across all datasets and backbone models.

We summarize our main contributions as follows: (1) We introduce an in-processing method to address the UOF issue. (2) We propose an individual reweighting strategy to achieve overall fairness by balancing the training process for different users. (3) We conduct extensive experiments to demonstrate the effectiveness of the proposed method.

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  - 2 RELATED WORK
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116 2.1 FAIRNESS IN MACHINE LEARNING

As outlined in Mehrabi et al. (2021), fairness in decision-making processes is broadly defined as the absence of bias or favoritism toward an individual or group based on their inherent or acquired characteristics. Research on machine learning fairness can be categorized from various perspectives into distinct domains.

122 Groups Affected by Fairness Issues. Fairness research primarily addresses two aspects: group 123 fairness and individual fairness Mehrabi et al. (2021); Dai et al. (2022). Group fairness aims to ensure 124 equal treatment for users from different demographic groups. Key approaches in this domain include 125 Demographic Parity Kusner et al. (2017), Equalized Odds Hardt et al. (2016), Equal Opportunity Hardt 126 et al. (2016), Conditional Statistical Parity Corbett-Davies et al. (2017), and Treatment Equality Berk 127 et al. (2021). Individual fairness focuses on providing similar recommendations to similar individuals. Research areas include Fairness Through Unawareness Grgic-Hlaca et al. (2016), Fairness Through 128 Awareness Dwork et al. (2012), and Counterfactual Fairness Kusner et al. (2017). 129

Stages of the ML Process. Research on fairness can also be categorized according to different stages of the machine learning process: pre-processing methods, in-processing methods, and post-processing methods Mehrabi et al. (2021); Dai et al. (2022). Pre-processing methods aim to transform training data to eliminate underlying biases before model training d'Alessandro et al. (2017); Kang et al. (2020). In-processing methods incorporate fairness considerations into the training process to mitigate bias during model development Dai & Wang (2020); Bose & Hamilton (2019). Post-processing methods adjust the predictions of a trained model to ensure fairness Li et al. (2021).

In this paper, we introduce an in-processing framework specifically designed to ensure user-oriented fairness, a kind of group fairness in RSs.

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  - 2.2 FAIRNESS IN RECOMMENDER SYSTEMS

Fairness in RSs can be examined from three primary perspectives: user fairness, item fairness, and provider fairness Deldjoo et al. (2023).

145 User Fairness: Studies in this area aim to ensure that similar users receive comparable recommendation outcomes. Key considerations include ranking accuracy Deldjoo et al. (2021c), diversity 146 coverage Melchiorre et al. (2021), under-ranking Gorantla et al. (2021), and selection rate Sühr et al. 147 (2021). Item Fairness: The goal is to ensure that similar items receive equal exposure, regardless of 148 sensitive attributes Rastegarpanah et al. (2019); Deldjoo et al. (2021a); Dash et al. (2021) or previous 149 exposure history Biega et al. (2018), such as in cold-start scenarios. Provider Fairness: There is a 150 tendency for providers with a more extensive interaction history to be recommended more frequently, 151 creating a "superstar effect" Ferraro (2019); Gharahighehi et al. (2021). Efforts to mitigate exposure 152 disparities arising from the relationship between providers and items Sühr et al. (2021) and private 153 characteristics Shakespeare et al. (2020) are crucial for fostering an equitable market. 154

In this paper, we focus on the underexplored issue of user-oriented fairness (UOF), specifically addressing fairness among users with varying levels of activity.

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- **3 PROBLEM FORMULATION**
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- 161 This paper focuses on achieving fairness in RSs through individual reweighting. We categorize the problem into two main components: user-oriented fairness and individual reweighting.

# 162 3.1 USER-ORIENTED FAIRNESS

In RSs, let  $\mathcal{U}$  and  $\mathcal{I}$  represent the user set and the item set, respectively.  $N_{\mathcal{U}}$  and  $N_{\mathcal{I}}$  represent the number of users and items. Following prior research Li et al. (2021); Rahmani et al. (2022); Han et al. (2023a), users are divided into two groups: disadvantaged users ( $\mathcal{D}$ ) and advantaged users ( $\mathcal{A}$ ). The disadvantaged group  $\mathcal{D} = \{D_1, D_2, \dots, D_{N_{\mathcal{D}}}\}$  consists of users with fewer interactions, while the advantaged group  $\mathcal{A} = \{A_1, A_2, \dots, A_{N_{\mathcal{A}}}\}$  includes users with more frequent interactions. Here,  $N_{\mathcal{D}}$  and  $N_{\mathcal{A}}$  represent the number of users in each group. Users with more interactions are more likely to be advantaged. The goal is to minimize the performance disparity between  $\mathcal{D}$  and  $\mathcal{A}$ , thereby achieving UOF while maintaining overall recommendation quality.

UOF is a type of group fairness Hardt et al. (2016); Dwork et al. (2012), which ensures that groups of
users with different protected attributes are treated comparably. Specifically, UOF aims to provide
users with different activity levels with the same recommendation performance. The definition of
UOF is as follows Li et al. (2021); Rahmani et al. (2022); Han et al. (2023a):

**Definition 1** (User-Oriented Fairness (UOF)).

$$\mathbb{E}[\mathcal{M}(\mathcal{A})] = \mathbb{E}[\mathcal{M}(\mathcal{D})]. \tag{1}$$

Here,  $\mathcal{M}$  is a metric (e.g., NDCG and Hit Ratio) evaluating recommendation performance.  $\mathcal{M}(u)$ represents the recommendation performance for user u.

UOF aims to offer users with different activity levels the same recommendation performance, which is always impossible in real-world RSs. Therefore, researchers Li et al. (2021); Rahmani et al. (2022); Han et al. (2023a) calculate the difference in average recommendation performance for different user groups to evaluate the fairness of a model:

**Definition 2** (The UOF metric  $(\mathcal{M}_{UOF})$ ).

$$\mathcal{M}_{UOF}(\mathcal{D}, \mathcal{A}) = \left| \frac{1}{|\mathcal{A}|} \sum_{A_i \in \mathcal{A}} \mathcal{M}(A_i) - \frac{1}{|\mathcal{D}|} \sum_{D_i \in \mathcal{D}} \mathcal{M}(D_i) \right|.$$
(2)

The  $\mathcal{M}_{UOF}$  value is used to evaluate the fairness of a recommendation model. A lower  $\mathcal{M}_{UOF}$  indicates a fairer algorithm, aiming for equal treatment across different user activity groups. Note that some researchers Han et al. (2024a) have proposed alternative metrics for assessing UOF. However, these metrics often replicate the characteristics of standard metrics like NDCG or Hit Ratio, and thus, they fail to specifically address the fairness aspect. Therefore, we utilize the more widely accepted  $\mathcal{M}_{UOF}$  metric, as adopted by Li et al. (2021); Rahmani et al. (2022); Han et al. (2023a), which is better suited to evaluate fairness within RSs.

#### 3.2 INDIVIDUAL REWEIGHTING

200 Individual reweighting aims to allocate different weights to each user's loss values, thereby giving 201 more weight to users who are likely to be disadvantaged by the recommendation models. Consider the 202 utility loss  $\mathcal{L} = \sum_{U_i \in \mathcal{U}} L(U_i)$  of a recommendation model, where  $L(U_i)$  represents the loss value for user  $U_i$ . For instance, this could be the cross-entropy loss. The individual reweighting strategy 203 involves calculating a set of weights  $\beta = {\beta_1, \beta_2, \dots, \beta_{N_u}}$  that maximize the total weighted loss: 204  $\max_{\beta} \mathcal{L} = \sum_{U_i \in \mathcal{U}} \beta_i L(U_i)$ . By amplifying the loss values of poorly trained users, this approach 205 ensures that the model pays more attention to these users, thereby enhancing their training process 206 and improving overall fairness. 207

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### 4 Methodology

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In this paper, we propose a novel Individual Reweighting for User-Oriented Fairness framework,
 named IR-UOF, to address the UOF issue in RSs. Designed as a versatile framework, IR-UOF can
 be integrated with any existing backbone recommendation model to enhance fairness. The key
 motivation behind IR-UOF is to introduce an in-processing framework that employs an individual level optimization strategy, thereby avoiding the need to calculate user similarities in sparse datasets
 and overcoming the three key limitations. *Firstly*, IR-UOF assigns reweighting ratios to advantaged

216 and disadvantaged user groups, thereby tailoring reweighting strengths based on the training qualities 217 of these groups. Secondly, IR-UOF provides a detailed calculation strategy for the individual 218 reweighting process within each user group. *Thirdly*, IR-UOF introduces a delayed updating strategy 219 to ensure the smooth optimization of the algorithm. 220

#### 4.1 REWEIGHTING RATIOS FOR DIFFERENT USER GROUPS

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As discussed in Section 1, users in both advantaged and disadvantaged groups can be adversely 223 affected by recommendation models. Therefore, reweighting both user groups is essential to enhance 224 overall fairness and improve recommendation performance. For the advantaged user group  $\mathcal A$  and 225 the disadvantaged user group  $\mathcal{D}$ , IR-UOF computes two weighting sets:  $\beta^{\mathcal{A}} = \{\beta_1^{\mathcal{A}}, \beta_2^{\mathcal{A}}, \dots, \beta_{N_{\mathcal{A}}}^{\mathcal{A}}\}$ 226 and  $\beta^{\mathcal{D}} = \{\beta_1^{\mathcal{D}}, \beta_2^{\mathcal{D}}, \dots, \beta_{N_{\mathcal{D}}}^{\mathcal{D}}\}$ . To ensure fairness and control the range of the loss function, these weights must be non-negative and capped. Hence, the weighting sets for these two groups must 227 228 satisfy the following conditions: 229

$$\sum_{\beta_i^{\mathcal{A}} \in \boldsymbol{\beta}^{\mathcal{A}}} \beta_i^{\mathcal{A}} = K_{\mathcal{A}}, \beta_i^{\mathcal{A}} \ge 0; \quad \sum_{\beta_i^{\mathcal{D}} \in \boldsymbol{\beta}^{\mathcal{D}}} \beta_i^{\mathcal{D}} = K_{\mathcal{D}}, \beta_i^{\mathcal{D}} \ge 0.$$
(3)

Here,  $K_A$  and  $K_D$  control the reweighting strengths for each user group. To prioritize reweighting in user groups that are more likely to be dominated by recommendation models, we calculate these values as follows:

$$K_{\mathcal{A}} = \frac{\sum_{A_i \in \mathcal{A}} L(A_i)}{\sum_{A_i \in \mathcal{A}} L(A_i) + \sum_{D_i \in \mathcal{D}} L(D_i)} K; \quad K_{\mathcal{D}} = \frac{\sum_{D_i \in \mathcal{D}} L(D_i)}{\sum_{A_i \in \mathcal{A}} L(A_i) + \sum_{D_i \in \mathcal{D}} L(D_i)} K, \quad (4)$$

where K is a hyperparameter that controls the overall reweighting scale. By calculating the reweighting ratios for different user groups, IR-UOF assigns greater weights to the user group which is more likely to be overlooked, ensuring balanced attention and enhanced fairness.

#### 4.2 CALCULATION OF INDIVIDUAL RWEIGHTING STRATEGY

Since the calculation of individual reweighting strategy is the same for advantaged and disadvantaged user groups, we take the disadvantaged user group as an example in this section. The individual 245 reweighting problem for disadvantaged users can be formulated as follows: 246

$$\max_{\boldsymbol{\beta}^{\mathcal{D}}} \mathcal{L}_{\mathcal{D}} = \sum_{D_i \in \mathcal{D}} \beta_i^{\mathcal{D}} L(D_i), \quad \text{s.t.} \sum_{\boldsymbol{\beta}_i^{\mathcal{D}} \in \boldsymbol{\beta}^{\mathcal{D}}} \beta_i^{\mathcal{D}} = K_{\mathcal{D}}, \; \beta_i^{\mathcal{D}} \ge 0.$$
(5)

Naturally, the optimal solution of  $\beta^{\mathcal{D}*}$  in Problem equation 5 is assigning 1 to the largest loss and 250 assigning 0 to all others. However, in order to tackle the UOF issue, consideration should be given to 251 individual users more likely to be neglected, not just the single most likely. Hence, we introduce a 252 regularization term and receive the following individual reweighting problem: 253

$$\max_{\boldsymbol{\beta}^{\mathcal{D}}} \mathcal{L}_{\mathcal{D}} = \sum_{D_i \in \mathcal{D}} \beta_i^{\mathcal{D}} L(D_i) - \alpha ||\boldsymbol{\beta}^{\mathcal{D}}||^2, \text{s.t.} \sum_{\boldsymbol{\beta}_i^{\mathcal{D}} \in \boldsymbol{\beta}^{\mathcal{D}}} \beta_i^{\mathcal{D}} = K_{\mathcal{D}}, \ \beta_i^{\mathcal{D}} \ge 0.$$
(6)

256 A higher value of the hyperparameter  $\alpha$  results in more positive weights. When  $\alpha$  reaches a sufficiently 257 large value, all samples will be assigned equal weights, and equation 6 will degenerate into the original 258 recommendation model training process. 259

Directly calculating the optimal value of  $\beta^{\mathcal{D}}$  through the optimization process is time consuming and 260 is not suitable for real practice. Therefore, we introduce the closed-form solution of adaptive weights  $\beta^{\mathcal{D}}$ . Due to space limitations, the detailed proof and calculation process are provided in **Appendix A**. 262

Assume the loss of each disadvantaged user is represented as  $l_i = L(D_i), D_i \in \mathcal{D}$ . Firstly, sort the 263 losses of all disadvantaged users in descending order, i.e.,  $l_i \ge l_j$ ,  $\forall i > j$ . Secondly, for i, calculate 264 the value  $\gamma$  following  $\sum_{j=1}^{\gamma} l_j - \gamma l_{\gamma+1} > 2\alpha K_{\mathcal{D}} > \sum_{j=1}^{\gamma} l_j - \gamma l_{\gamma}$ . Then, the optimal solution  $\beta^{\mathcal{D}*}$ 265 of Problem equation 6 is as follows: 266

$$\beta_i^{\mathcal{D}*} = \operatorname{ReLU}(\frac{\gamma l_i - \sum_{j=1}^{\gamma} l_j + 2\alpha K_{\mathcal{D}}}{2\alpha\gamma}).$$
(7)

We can follow a similar calculation process to get  $\beta^{\mathcal{A}*}$ .

Algori	thm 1: IR-UOF
Input	:User set $\mathcal{U}$ and item set $\mathcal{I}$ ; Advantaged user set $\mathcal{A}$ and Disadvantaged user set $\mathcal{D}$ ;
	Hyperparameters K and $\alpha$ ; Training round limit T; $t = 0$ .
Outpu	t:Final Recommention model;
while 7	t < T do
2   Ex	tract loss values $\{L(A_1), L(A_2), \dots, L(A_{N_A})\}$ and $\{L(D_1), L(D_2), \dots, L(D_{N_D})\};$
a Ca	lculate $\beta^{\mathcal{A}(t)*}$ and $\beta^{\mathcal{D}(t)*}$ according to problem equation 6;
Ge	t the value of $\beta^{\mathcal{A}(t)}$ and $\beta^{\mathcal{D}(t)}$ according to Equation equation 8;
5 Ca	lculate the final loss $L_{fairness}$ and do a gradient updation.
s end	·
Return	<b>1</b> trained recommendation model;

#### 4.3 DELAYED UPDATING STRATEGY FOR INDIVIDUAL REWEIGHTING

For such an individual reweighting method, directly replacing the value of  $\beta^{\mathcal{A}}$  and  $\beta^{\mathcal{D}}$  in each training round with the optimal one may result in unsteadiness. Therefore, we introduce a learning rate schedule to update  $\beta^{\mathcal{A}}$  and  $\beta^{\mathcal{D}}$  smoothly in the training round *t*:

$$\boldsymbol{\beta}^{\mathcal{A}(t)} = (1 - \eta_t)\boldsymbol{\beta}^{\mathcal{A}(t-1)} + \eta_t\boldsymbol{\beta}^{\mathcal{A}(t)*}, \boldsymbol{\beta}^{\mathcal{D}(t)} = (1 - \eta_t)\boldsymbol{\beta}^{\mathcal{D}(t-1)} + \eta_t\boldsymbol{\beta}^{\mathcal{D}(t)*},$$
(8)

where  $\eta^t = 1 - \frac{t}{T}$ , with T denoting the total training round. By doing so, IR-UOF avoids drastic changes to the individual weights and brings a more stable training process.

From the above discussion, we can find that both  $\alpha$  and K ( $K_A$  and  $K_D$  are calculated from K) have an impact on the values of  $\beta^A$  and  $\beta^D$ . We decide the values of these two hyperparameters according to the experimental results in Section 5.6.

#### 4.4 IN-PROCESSING TRAINING STRATEGY

299 As an in-processing framework, IR-UOF can be integrated with any existing backbone recom-300 mendation model to enhance fairness. In the training round t of a given recommendation model, 301 IR-UOF *firstly* extracts original training losses of advantaged users  $\{L(A_1), L(A_2), \ldots, L(A_{N_A})\}$ 302 and disadvantaged users  $\{L(D_1), L(D_2), \ldots, L(D_{N_D})\}$ . Secondly, IR-UOF calculates the optimal 303 individual reweighting sets  $\beta^{\mathcal{A}(t)*}$  and  $\beta^{\mathcal{D}(t)*}$  based on these loss values according to problem equa-304 tion 6. *Thirdly*, IR-UOF utilizes the delayed updating strategy to get the value of  $\hat{\beta}^{\mathcal{A}(t)}$  and  $\beta^{\mathcal{D}(t)}$  in 305 t-th training round. Finally, IR-UOF aggregates the final loss function with the fairness concern as 306 follows:

$$L_{fairness} = \sum_{A_i \in \mathcal{A}} \beta_i^{\mathcal{A}(t)} L(A_i) + \sum_{D_i \in \mathcal{D}} \beta_i^{\mathcal{D}(t)} L(D_i).$$
(9)

This loss function is used for the gradient update of the recommendation model. *To avoid overfitting to noisy user-item training pairs, the reweighting strategy is applied at the user level rather than at the individual training sample level.* We outlined the overall algorithm of IR-UOF in algorithm 1.

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### 5 EXPERIMENTS AND ANALYSIS

316 To comprehensively evaluate the effectiveness of the proposed IR-UOF framework, we conduct 317 extensive experiments on three real-world datasets to address the following Research Questions 318 (RQs): **RQ1**: How does IR-UOF compare with existing SOTA methods in tackling the UOF issue 319 and improving overall recommendation performance? **RQ2:** What is the impact of reweighting 320 different user groups on the performance of IR-UOF? RQ3: As an in-processing method, is IR-321 UOF time-efficient? **RQ4:** Can IR-UOF maintain satisfactory performance in extremely sparse datasets? **RQ5:** How do important hyperparameters affect the performance of IR-UOF? **RQ6:** How 322 robust is the generalizability of the IR-UOF framework when faced with variations in the classification 323 of advantaged and disadvantaged users?

# 324 5.1 DATASETS AND EXPERIMENTAL SETTINGS

<sup>326</sup> Due to space limitations, the details of this section are provided in **Appendix B**.

Dataset Description. We utilize three real-world datasets: Epinion Massa & Avesani (2007),
MovieLens Harper & Konstan (2015), and Gowalla Liu et al. (2017), which are commonly used to validate the UOF issueRahmani et al. (2022); Han et al. (2023a).

Baselines and Backbone Models. We compare IR-UOF with the SOTA UOF methods UFR (failing to tackle Limitation 1) Li et al. (2021), In-UCDS Han et al. (2023a), HyperUOF Han et al. (2024b), and II-GOOT Han et al. (2024a) (failing to tackle Limitation 2), S-DRO Wen et al. (2022a) (failing to tackle Limitation 3). Besides, we choose four different backbone recommendation models, including a traditional matrix factorization method (MF Koren et al. (2009)), two deep-learning-based methods (NeuMF He et al. (2017), VAECF Liang et al. (2018)), and a graph neural network-based method (LightGCN He et al. (2020)).

**Evaluation Protocols.** (1) User Grouping: Users are ranked by interaction counts, with the top 5% as advantaged and the rest as disadvantaged Li et al. (2021); Dai et al. (2022); Han et al. (2023a). (2) Performance Metrics: We adopt the widely-used Normalized Discounted Cumulative Gain (NDCG) Wang et al. (2013) and Hit Ratio (HR) Waters (1976) to evaluate the recommendation performance of each model. Besides, we utilize  $\mathcal{M}_{UOF}$  to evaluate the UOF level of a recommendation model, with a lower value means a fairer performance. (3) Statistical Robustness: Each evaluation is repeated 10 times, reporting average performance with significance testing (p-value < 0.05).

- <sup>345</sup> **Parameter Settings.** The details of this part are provided in **Appendix B**.
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- 5.2 OVERALL COMPARISON (RQ1)

To comprehensively evaluate the effectiveness of the proposed IR-UOF framework, we conduct
 extensive experiments on three publicly available real-world datasets using four backbone models.
 The results are detailed in Table 1. Across all datasets, IR-UOF consistently outperforms all SOTA
 methods, highlighting the importance of addressing all three critical limitations (introduced in Section
 in solving UOF.

(1) Tackling Limitation 1 (Compared with UFR). IR-UOF outperforms UFR across all datasets.
 Unlike the post-processing method UFR, IR-UOF effectively mitigates the training gap between advantaged and disadvantaged users, thereby addressing Limitation 1. UFR's failure to tackle the root cause of the UOF issue results in its generally poor performance compared with all baselines.

(2) Tackling Limitation 2 (Compared with In-UCDS, HyperUOF, and II-GOOT). IR-UOF consistently outperforms In-UCDS, HyperUOF, and II-GOOT across all datasets, especially on the sparser Gowalla dataset. These methods rely heavily on identifying essential similarities among users based on user-item interactions, a process that is unstable under severe data sparsity. As a result, their performance is limited, particularly in sparser datasets. IR-UOF focuses on reweighting loss values for each user, directly reflecting their training quality, making it a more stable and direct solution to the UOF issue.

(3) Tackling Limitation 3 (Compared with S-DRO). Compared to S-DRO, IR-UOF achieves
 fairer models with better recommendation performance. S-DRO sorely assign more weight to the
 entire disadvantaged user group, overlooking the different treatments individual users within this
 group receive. This inability to target users individually limits its performance. IR-UOF adaptively
 reweights each user's loss value, providing unique treatment to each user and accurately improving
 the training of users dominated by recommendation models. Thus, IR-UOF can narrow the training
 gap across the entire user group, naturally improving both fairness and recommendation performance.

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5.3 ABLATION STUDY (RQ2)

We conduct an ablation study to analyze the impact of reweighting different user groups on the performance of IR-UOF, using LightGCN as the backbone model. As illustrated in Table 2, "Re-Adv" indicates reweighting only in the advantaged user group (setting  $K_A = K$ ), while "Re-Dis" indicates reweighting only in the disadvantaged user group (setting  $K_D = K$ ).

				Epi	inion			Mov	ieLens			Gov	walla	
			Over.	Adv.	Dis.	$\mathcal{M}_{UOF}$	Over.	Adv.	Dis.	$\mathcal{M}_{UOF}$	Over.	Adv.	Dis.	$\mathcal{M}_{UOF}$
		Original	0.361	0.387*	0.359	0.028	0.394	0.453*	0.391	0.062	0.356	0.458*	0.350	0.108
		S-DRO	0.364	0.376	0.364	0.012	0.396	0.431	0.394	0.037	0.357	0.433	0.352	0.080
	ß	UFR	0.362	0.382	0.361	0.021	0.399	0.429	0.397	0.032	0.361	<u>0.440</u>	0.357	0.083
	ĕ	In-UCDS	0.368	0.381	0.367	0.014	0.410	0.439	0.408	0.030	0.357	0.433	0.353	0.080
	z	HyperUOF	0.366	0.380	0.365	0.015	0.403	0.440	0.401	0.038	0.360	0.434	0.356	<u>0.078</u>
		II-GOOT	0.370	0.380	0.370	0.010	0.404	0.443	0.402	0.040	0.361	0.437	0.357	0.080
Π		IR-UOF	0.377*	0.382	0.377*	0.005*	0.412*	0.433	0.411*	0.022*	0.373*	<u>0.440</u>	0.369*	0.071*
2		Original	0.460	0.513*	0.457	0.057	0.474	0.548*	0.470	0.077	0.432	0.593*	0.424	0.169
		S-DRO	0.462	<u>0.511</u>	0.460	0.051	0.475	0.531	0.472	0.059	0.437	0.572	0.430	0.142
	~	UFR	0.460	0.513*	0.457	0.056	0.472	0.521	0.470	0.052	0.447	0.581	<u>0.440</u>	0.142
	Ĥ	In-UCDS	0.462	0.507	0.460	0.047	0.485	0.530	0.483	0.047	0.447	0.571	0.440	0.131
		HyperUOF	0.462	0.510	0.460	0.050	0.484	0.530	0.482	0.048	0.443	0.570	0.436	0.134
		II-GOOT	0.465	0.509	0.463	0.046	0.487	0.532	0.485	0.047	0.442	0.573	0.435	0.138
		IR-UOF	0.478*	0.509	0.477*	0.033*	0.489*	0.531	0.486*	0.044*	0.464*	0.584	0.458*	0.126*
		Original	0.369	0.393*	0.368	0.025	0.404	0.484*	0.400	0.084	0.376	0.467*	0.371	0.096
		S-DRO	0.373	0.386	0.372	0.014	0.398	0.465	0.394	0.071	0.376	0.459	0.372	0.086
	ß	UFR	0.371	0.390	0.370	0.020	0.403	0.480	0.399	0.081	0.380	0.461	0.376	0.085
	ğ	In-UCDS	0.374	0.389	0.374	0.015	0.408	0.476	0.405	0.072	0.384	0.460	0.381	0.080
	z	HyperUOF	0.371	0.390	0.370	0.020	0.407	0.479	0.403	0.076	0.384	0.459	0.380	0.079
ц		II-GOOT	0.376	0.390	0.376	<u>0.014</u>	<u>0.414</u>	<u>0.480</u>	0.410	<u>0.070</u>	0.383	0.459	0.379	0.081
Μ		IR-UOF	0.381*	<u>0.392</u>	0.380*	0.012*	0.423*	<u>0.480</u>	0.420*	0.060*	0.401*	0.460	0.398*	0.062*
Nei		Original	0.472	0.522*	0.469	0.053	0.481	0.576*	0.476	0.101	0.441	0.601*	0.433	0.168
		S-DRO	0.470	0.515	0.468	0.046	0.484	0.569	0.479	0.090	0.442	0.586	0.434	0.151
	К	UFK	0.471	0.510	0.469	0.041	0.4/6	0.569	0.4/1	0.098	0.441	0.583	0.434	0.150
	Н	In-UCDS	0.482	0.515	0.480	0.036	0.505	0.571	0.502	0.069	0.446	0.587	0.438	0.149
		HyperUOF	0.475	0.514	0.474	0.040	0.504	0.571	0.500	0.071	0.445	0.589	0.437	0.152
		II-GOUI	0.475	0.515	0.475	0.041	0.507	0.575	0.504	0.009	0.445	0.591	0.455	0.130
		IR-UUF	0.490*	0.405*	0.489*	0.029*	0.514*	0.572	0.511*	0.001*	0.470*	0.462*	0.403*	0.131*
		Original S DDO	0.374	0.405*	0.372	0.033	0.416	0.492	0.412	0.080	0.399	0.465*	0.396	0.067
		S-DKU	0.374	0.397	0.373	0.024	0.421	0.490*	0.417	0.079	0.415	0.455	0.410	0.045
	Ş	UFK In LICDS	0.372	0.400	0.370	0.050	0.410	0.483	0.412	0.073	0.399	0.454	0.390	0.058
	ĝ	HumarLIOF	0.382	0.398	0.381	0.010	0.433	0.490	0.429	0.000	0.400	0.434	0.404	0.051
	_	IL COOT	0.381	0.398	0.284	0.018	0.432	0.489	0.429	0.000	0.403	0.433	0.400	0.054
СF			0.301*	0.400	0.301*	0.013	0.434	0.491	0.430	0.000	0.402	0.430	0.399	0.037
ÅE		Original	0.391*	0.527*	0.391*	0.010**	0.435**	0.409	0.454	0.05/*	0.427	0.504*	0.410	0.175
Ż		S-DRO	0.475	0.527*	0.472	0.033	0.400	0.509*	0.454	0.114	0.427	0.594*	0.419	0.175
		UER	0.476	0.519	0.473	0.040	0.463	0.555	0.405	0.090	0.431	0.584	0.423	0.140
	Щ	In-UCDS	0.470	0.524	0.475	0.031	0.405	0.500	0.430	0.101	0.431	0.504	0.425	0.101
	Η	HyperLIOF	0.407	0.521	0.403	0.030	0.470	0.559	0.475	0.000	0.433	0.581	0.423	0.156
		ILGOOT	0.409	0.520	0.407	0.035	0.479	0.556	0.476	0.085	0.432	0.584	0.424	0.150
		IR-UOF	0.491	0.520	0.405	0.031	0.486*	0.501	0.497*	0.083	0.428	0.564	0.420	0.104
		Original	0 300	0.440	0 307	0.043	0.483	0.520	0.480	0.002	0.403	0.486*	0 300	0.087
		S-DRO	0.399	0.440	0.397	0.045	0.405	0.529	0.404	0.049	0.405	0.400	0.399	0.067
	~ 7	J-DKU	0.401	0.438	0.399	0.039	0.490	0.552*	0.494	0.038	0.417	0.480	0.414	0.009
	Ŋ	ULK In LICDS	0.400	0.440	0.398	0.042	0.488	0.525	0.480	0.037	0.407	0.480	0.405	0.077
	ĝ	HumarLIOF	0.400	0.430	0.403	0.031	0.501	0.528	0.499	0.028	0.418	0.484	0.414	0.070
7	-	HyperUOF	0.400	0.438	0.404	0.034	0.501	0.52/	0.500	0.027	0.400	0.480	0.402	0.077
ģ		II-GOUI	<u>0.408</u> 0.416*	0.45/ 0.441*	<u>0.40/</u> 0.414*	0.030	0.304 0.515*	0.529	0.502	0.020	0.409	0.482	0.400	0.0//
htG		IK-UUF	0.410*	0.550	0.414*	0.02/*	0.515*	0.610	0.515*	0.014*	0.423*	0.604*	0.420*	0.121
Ligh		original	0.479	0.559	0.475	0.084	0.549	0.619	0.545	0.074	0.480	0.604*	0.475	0.151
Γ		S-DRO	0.483	0.553	0.479	0.074	0.558	0.617	0.554	0.062	0.486	0.596	0.480	0.110
	К	UFK	0.480	0.553	0.476	0.077	0.550	0.615	0.546	0.069	0.486	0.598	0.480	0.118
	Η	in-UCDS	0.484	0.554	0.480	0.074	0.566	0.620	0.563	0.057	0.482	0.593	0.476	0.116
		HyperUOF	0.485	0.555	0.481	0.074	0.555	0.614	0.552	0.062	0.484	0.597	0.478	0.119
		II-GOOT	0.488	0.557	<u>0.484</u>	0.073	0.569	0.619	0.566	0.053	0.481	0.595	0.475	0.119
		IR-UOF	0.502*	0.560*	0.499*	0.061*	0.582*	0.621*	0.580*	0.040*	0.503*	0.602	0.498*	0.104*

Table 1: Overall experimental result.

<sup>\*</sup> Over. indicates overall performance. Adv. and Dis. indicate the performance of advantaged and disadvantaged users, respectively.

\* The results of IR-UOF are highlighted in bold. The best results are marked with \*. The second-best results are underlined.

\* All outcomes pass the significance test, with a p-value below the significance threshold of 0.05.

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Overall, IR-UOF achieves the best performance 423 compared to the ablation methods, demonstrat-424 ing that reweighting both advantaged and dis-425 advantaged user groups is necessary to improve 426 fairness and recommendation performance. This 427 is because some users in both groups may re-428 ceive poor training results. Reweighting only ad-429 vantaged or disadvantaged users neglects some poorly trained users. Since disadvantaged users 430

Table 2: Ablation study.

-		Epinion		Movi	eLens	Gowalla		
		Overall	$\mathcal{M}_{UOF}$	Overall	$\mathcal{M}_{UOF}$	Overall	$\mathcal{M}_{UOF}$	
	Original	0.399	0.043	0.483	0.049	0.403	0.087	
NDCC	Re-Adv	0.402	0.046	0.492	0.058	0.413	0.095	
NDCG	Re-Dis	0.411	0.032	0.510	0.021	0.419	0.069	
	IR-UOF	0.416	0.027	0.515	0.014	0.423	0.064	
	Original	0.479	0.084	0.549	0.074	0.480	0.131	
LID	Re-adv	0.483	0.099	0.552	0.082	0.486	0.152	
пк	Re-dis	0.500	0.069	0.571	0.054	0.491	0.114	
	IR-UOF	0.502	0.061	0.582	0.040	0.503	0.104	

are more likely to be dominated by recommen-

dation models, Re-Dis achieves significantly better performance than Re-Adv.

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5.4 MODEL EFFICIENCY (RQ3)

Epinion, MovieLens, and Gowalla.

This section aims to analyze the efficiency of IR-UOF. As an in-processing framework, it is crucial to demonstrate that it does not impose excessive additional time costs on the original models' training process. We compare the training time of IR-UOF with all in-processing methods. The experimental results are presented in Figure 3. *Our analysis reveals that IR-UOF maintains a time cost comparable to the original backbone model, incurring only a slight additional time cost*. The additional time expenditure associated with IR-UOF is primarily due to sorting the loss values of users, which has a time complexity of  $\mathcal{O}(N_U \log N_U)$ . This sorting process is time-efficient and depends solely on the size of the datasets. Consequently, when applied to more complex and time-intensive backbone models (e.g., LightGCN), the relative increase in training time due to IR-UOF becomes less significant. This observation underscores IR-UOF's applicability and practicality, especially in scenarios where backbone models are inherently resource-intensive.

Figure 3: Training time of the original backbone model, S-DRO, In-UCDS, II-GOOT, and IR-UOF in datasets

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# 430 5.5 SPARSE TEST (RQ4)

460 This section aims to demonstrate the supe-461 rior performance of IR-UOF on extremely 462 sparse datasets, thus highlighting the ne-463 cessity of addressing Limitation 2. Disad-464 vantaged users frequently encounter severe 465 data sparsity issues. The capability of a model to handle sparse datasets is crucial 466 for effectively tackling the UOF challenge. 467 To validate this, we simulate sparser en-468 vironments by randomly omitting various 469 ratios of interactions within each dataset 470 and subsequently conducting experiments. 471 As outlined in Section 1, the user similar-472 ity calculation processes in In-UCDS, Hy-473 perUOF, and II-GOOT become unstable 474 in sparse datasets, limiting these methods' 475 performance. Therefore, we compare the

performance of IR-UOF with these meth-



Figure 4: Sparse test with LightGCN as the backbone model.

dots. The experimental results are provided in Figure 4, with the "Sparse ratio" representing thepercentage of interactions omitted.

The experimental findings unequivocally indicate that *IR-UOF consistently surpasses In-UCDS*, *HyperUOF, and II-GOOT across all levels of dataset sparsity, achieving superior recommendation performance and fairness.* Notably, the advantage of IR-UOF becomes more pronounced as the sparsity of the datasets increases. This is because, as datasets become sparser, the unstable user similarity calculation process for In-UCDS, HyperUOF, and II-GOOT significantly hampers their performance, leading to a faster rate of performance decline. In contrast, IR-UOF focuses on users' loss values, which can consistently and accurately reflect the user's training level, thereby making its performance more robust.

#### 486 5.6 EFFECT OF HYPERPARAMETERS (RQ5) 487

488 In this section, we conduct experiments to 489 analyze the effects of hyperparameters  $\alpha$ and K within the proposed IR-UOF frame-490 work. Due to space constraints, we present 491 the experimental results using LightGCN 492 as the backbone model in Figure 5. 493

494 **Effect of**  $\alpha$ **.** As depicted in Figure 5, the 495 IR-UOF framework achieves peak perfor-496 mance in terms of recommendation quality 497 and UOF optimization when  $\alpha$  is set to 10. 498 The parameter  $\alpha$  controls the importance





of the regularization term. A value of  $\alpha$  that is too small will result in IR-UOF assigning positive 499 weights to only a few users, thereby neglecting too many individuals. Conversely, a value of  $\alpha$  that is 500 too large will cause IR-UOF to degenerate into average weighting. 501

502 Effect of K. Figure 5 shows that IR-UOF attains optimal recommendation performance and UOF 503 optimization when K is set to 1000. This parameter controls the scale of weights assigned to each 504 individual user in IR-UOF. A larger value of K can better represent the differences in loss values 505 among users, making recommendation models focus more on users who are often neglected. However, an excessively large value of K causes the recommendation models to focus too much on specific 506 users, thereby reducing the model's generalization ability.

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#### 6 GENERALIZABILITY OF IR-UOF (RQ6)

511 The level of data sparsity varies across dif-512 ferent datasets, leading to a dynamic nature 513 in how advantaged and disadvantaged users 514 are categorized. To prove the generalizabil-515 ity of IR-UOF, we adopt LightGCN as the 516 backbone model and modify the percentage of advantaged users from 5% to 50% 517 within the Gowalla Dataset. The outcomes 518 are presented in Figure 6. The experimen-519 tal results indicate that the ratio of advan-520 taged to disadvantaged users does not sig-521 nificantly affect the overall model perfor-522 mance. This is because IR-UOF reweights 523 samples within both user groups, rather 524 than a specific group. As the threshold in-525 creases, the overall activity level difference



Figure 6: The above results illustrate how the overall performance and  $\mathcal{M}_{UOF}$  of IR-UOF and the original model change in response to variations in the categorization of advantaged and disadvantaged users. Due to space limitations, we take LightGCN as the backbone model and Gowalla as the experimental dataset.

526 between the two user groups decreases, resulting in a reduced disparity in UOF gap. The results prove that IR-UOF has strong generalizability in narrowing the recommendation gap across various 527 user distributions. 528

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#### 530 7 CONCLUSION

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This paper addresses the User-Oriented Fairness (UOF) issue in Recommender Systems (RSs), 533 specifically focusing on narrowing the recommendation gap between advantaged and disadvantaged 534 user groups. We introduce a novel framework, Individual Reweighting for User-Oriented Fairness, referred to as IR-UOF, designed to overcome three significant limitations that existing research has not adequately addressed. IR-UOF adaptively reweights the loss values of each user, ensuring 537 that no users are dominated by the recommendation models. As a result, IR-UOF enhances the training quality for each individual user, achieving overall fairness and improving recommendation 538 performance through individualized optimization, i.e., One to All. We conduct extensive experiments on three real-world datasets to demonstrate the efficacy of IR-UOF.

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## A DETAILED PROOF AND CALCULATION OF INDIVIDUAL REWEIGHING STRATEGY

The optimization of  $\beta^{\mathcal{D}}$  in problem equation 6 can be formulated as

$$\max_{\beta^{\mathcal{D}}} \mathcal{L}_{\mathcal{D}} = \sum_{D_i \in \mathcal{D}} L(D_i) - \alpha ||\beta^{\mathcal{D}}||^2, \text{s.t.} \sum_{\beta_i^{\mathcal{D}} \in \beta^{\mathcal{D}}} \beta_i^{\mathcal{D}} = K_{\mathcal{D}}, \beta_i^{\mathcal{D}} \ge 0.$$

Denote the loss of each sample as  $l_i = L(D_i), D_i \in D$ , the optimization problem can be written as

$$\min_{\beta^{\mathcal{D}}} - \sum_{i} l_{i} \beta_{i}^{\mathcal{D}} + \alpha \|\beta^{\mathcal{D}}\|^{2}, \text{ s.t. } \sum_{\beta_{i}^{\mathcal{D}} \in \beta^{\mathcal{D}}} \beta_{i}^{\mathcal{D}} = K_{\mathcal{D}}, \beta_{i}^{\mathcal{D}} \ge 0.$$
(10)

Consider the Lagrangian dual of problem equation 10, we employ the KKT conditions Boyd & Vandenberghe (2004) to optimize equation 10 via its Lagrangian:

$$L(\beta^{\mathcal{D}}, \lambda, \nu) = -\sum_{i} l_{i}\beta_{i}^{\mathcal{D}} + \alpha \sum_{i} \beta_{i}^{\mathcal{D}^{2}} - \sum_{i} \lambda_{i}\beta_{i}^{\mathcal{D}} + \nu(\sum_{i} \beta_{i} - K_{\mathcal{D}}).$$
(11)

From the KKT conditions, we have

$$\nabla_{\beta_i^{\mathcal{D}}} L(\beta^{\mathcal{D}}, \lambda, \nu) = -l_i + 2\alpha \beta_i^{\mathcal{D}} - \lambda_i + \nu = 0,$$
(15a)

$$\lambda_i \beta_i^{\mathcal{D}} = 0, \beta_i^{\mathcal{D}} \ge 0, \lambda_i \ge 0, i = [1, N_D], \tag{15b}$$

$$\sum_{i} \beta_i^{\mathcal{D}} = K_D. \tag{15c}$$

<sup>725</sup> Combining equation 15a and equation 15b, since  $\alpha > 0$ , we can derive that

$$\begin{cases} l_i - \nu > 0 \Rightarrow 2\alpha \beta_i^{\mathcal{D}} = l_i - \nu, \lambda_i = 0, \\ l_i - \nu \le 0 \Rightarrow 2\alpha \beta_i^{\mathcal{D}} = 0, \lambda_i = \nu - l_i. \end{cases}$$
(13)

Hence, we get  $\beta_i^{\mathcal{D}} = (\frac{l_i - \nu}{2\alpha})_+ = \max\{\frac{l_i - \nu}{2\alpha}, 0\}$ . Then equation 15c can be written as

$$\sum_{i} (l_i - \nu)_+ = 2\alpha K_{\mathcal{D}}.$$
(14)

Here,  $\nu$  can be calculated through solving equation 14. Firstly, we consider that  $\sum_i l_i \le 2\alpha K_D$ , the unique solution is

$$\nu = (2\alpha K_{\mathcal{D}} - \sum_{i} l_{i})/N_{\mathcal{D}}.$$
(15)

738 When  $0 < 2\alpha K_{\mathcal{D}} < \sum_{i} l_{i}$ , there exist  $l_{\max} > \nu \ge 0$  such that  $\sum_{i} (l_{i} - \nu)_{+} = 2\alpha K_{\mathcal{D}}$  holds 739 true. Without loss of generality, suppose that the loss vector l is sorted in descending order, i.e., 740  $l_{\max} = l_{1} > l_{2} > \cdots > l_{N_{\mathcal{D}}} = l_{\min}$ , there exists a  $\gamma \in [1, N_{\mathcal{D}}]$  that satisfies  $l_{\gamma} > \nu > l_{\gamma+1}$ . The 741 problem equation 14 can be expressed as

$$\sum_{i} (l_i - \nu)_+ = \sum_{i=1}^{\gamma} l_i - \gamma \nu = 2\alpha K_{\mathcal{D}},$$

$$\Rightarrow \nu = \frac{\sum_{i=1}^{\gamma} l_i - 2\alpha K_{\mathcal{D}}}{\gamma}.$$
(16)

Moreover, with the expression of  $\nu$ , it can be derived that the index  $\gamma$  satisfies

$$\sum_{i=1}^{\gamma} l_i - \gamma l_{\gamma+1} > 2\alpha K_{\mathcal{D}} > \sum_{i=1}^{\gamma} l_i - \gamma l_{\gamma}.$$
(17)

Combining equation 15 and equation 16, the optimal solution of weight  $\beta$  is

$$\beta_i^{\mathcal{D}*} = \left(\frac{l_i - \left(\sum_{i=1}^{\gamma} l_i - 2\alpha K_{\mathcal{D}}\right)/\gamma}{2\alpha}\right)_+ = \operatorname{ReLU}\left(\frac{\gamma l_i - \sum_{j=1}^{\gamma} l_j + 2\alpha K_{\mathcal{D}}}{2\alpha\gamma}\right),\tag{18}$$

where  $\gamma$  satisfies equation 17. When  $\sum_{i} l_i \leq 2\alpha K_D$ , let  $\gamma = N_D$ .

## <sup>756</sup> B DATASETS AND EXPERIMENTAL SETTINGS

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Dataset Description. We utilize three publicly available real-world datasets: Epinion Massa & Avesani (2007), MovieLens Harper & Konstan (2015), and Gowalla Liu et al. (2017), representing different domains (opinions, movies, and points of interest). These datasets are commonly used to validate the performance of models addressing the UOF issueRahmani et al. (2022); Han et al. (2023a). Table 3 provides the statistics of these datasets.

764 Overall, we select these datasets for

three specific reasons in order to
demonstrate the scalability, efficiency,
and effectiveness of IR-UOF. (1) Domain Diversity: The datasets originate from different domains, providing a comprehensive evaluation of IR-

Table 3: The statistics of datasets.

Dataset	Users	Items	Interactions	Sparsity	Domain
Epinion	2,677	2,060	103,567	98.12%	Opinion
MovieLens	5,738	3,627	760,814	96.34%	Movie
Gowalla	33,699	123,587	1,011,694	99.98%	POI

ing a comprehensive evaluation of IR UOF's performance. (2) Sparsity Variation: The datasets vary in sparsity levels, which directly impacts the UOF issue due to differences in user activity. (3) Scalability Testing: The datasets differ in size, allowing us to demonstrate IR-UOF's scalability.

774 Baselines and Backbone Models. We compare IR-UOF with the SOTA UOF methods UFR (failing to tackle Limitation 1) Li et al. (2021), In-UCDS Han et al. (2023a), HyperUOF Han et al. (2024b), 775 and II-GOOT Han et al. (2024a) (failing to tackle Limitation 2 and Limitation 3), S-DRO Wen 776 et al. (2022a) (failing to tackle Limitation 3). (1) UFR: A post-processing re-ranking method that 777 modifies recommendation results of a given backbone model. (2) In-UCDS: An in-processing 778 method that allows disadvantaged users to learn from advantaged users based on dominant sets. (3) 779 HyperUOF: An in-processing strategy that utilizes hypergraph to explore high-order correlations among advantaged and disadvantaged users. (4) II-GOOT: An in-processing framework that narrows 781 the training gap between advantaged and disadvantaged users through intra- and inter-group stages. 782 (5) **S-DRO** An in-processing method that minimizes the loss function value for disadvantaged users 783 during training.

784 To fully evaluate the performance of IR-UOF and SOTA methods, we choose four different backbone 785 recommendation models, including a traditional matrix factorization method (MF), two deep-learning-786 based methods (NeuMF, VAECF), and a graph neural network-based method (LightGCN). (1) 787 **MF** Koren et al. (2009): Matrix Factorization maps both users and items to a joint latent factor 788 space and calculates the similarities among users and items. (2) NeuMF He et al. (2017): Neural 789 Collaborative Filtering introduces a deep neural network with non-linear activation functions to train 790 a user and item matching function. (3) VAECF Liang et al. (2018): Variational Autoencoders for Collaborative Filtering proposes a generative model with multinomial likelihood and uses Bayesian 791 inference for parameter estimation. (4) LightGCN He et al. (2020): Light Graph Convolution 792 Network simplifies the design of GCN by including only the most essential component in GCN 793 neighborhood aggregation — for collaborative filtering. 794

795 **Evaluation Protocols.** (1) User Grouping: Users are ranked by interaction counts, with the top 5% 796 as advantaged and the rest as disadvantaged Li et al. (2021); Dai et al. (2022); Han et al. (2023a). (2) 797 Dataset Spilting: Using the Leave-One-Out (LOO) strategy Chen et al. (2023b); He et al. (2017), 798 we split data into training, validation, and testing sets. (3) Performance Metrics: We adopt the widely-used Normalized Discounted Cumulative Gain (NDCG) Wang et al. (2013) and Hit Ratio 799 (HR) Waters (1976) to evaluate the recommendation performance of each model. A higher value 800 indicates superior recommendation performance, with a predicted cut-off of topK = 10 Li et al. 801 (2021); Dai et al. (2022); Han et al. (2023a). Besides, we utilize  $\mathcal{M}_{UOF}$  to evaluate the UOF level of 802 a recommendation model, with a lower value of  $\mathcal{M}_{UOF}$  means a fairer performance. (4) Statistical 803 Robustness: Each evaluation is repeated 10 times, reporting average performance with significance 804 testing (p-value < 0.05). 805

Parameter Settings. (1) For IR-UOF: Hyperparameters K and α are set according to Section 5.6.
(2) For UFR, In-UCDS, HyperUOF, and II-GOOT: We use the code provided by authors and leave the parameters as their default values. (3) For S-DRO: Implemented as recommended in Wen et al. (2022b), with hidden layer dimensions (128, 64) and temperature τ set to 0.07. (4) For backbone models: We set the dimension of user and item embeddings to 64 for all of them, and adopt their

810 811 812	parameters as suggested in their original paper. We adopt the Adam optimizer Kingma & Ba (2014) with a learning rate of 0.0001 and ensure convergence through 200 training epochs for all models.
813 814	<b>Experiments Compute Resources.</b> We conducted our experiments on a GPU server equipped with 8 CPUs and an NVIDIA RTX 3090 (24G).
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