Learning to Focus: Prioritizing Informative Histories with Structured Attention Mechanisms in Partially Observable Reinforcement Learning

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Abstract

Transformers have shown strong ability to model long-term dependencies and are increasingly adopted as world models in model-based reinforcement learning (RL) under partial observability. However, unlike natural language corpora, RL trajectories are sparse and reward-driven, making standard self-attention inefficient because it distributes weight uniformly across all past tokens rather than emphasizing the few transitions critical for control. To address this, we introduce structured inductive priors into the self-attention mechanism of the dynamics head: (i) per-head **memory-length priors** that constrain attention to task-specific windows, and (ii) **distributional priors** that learn smooth Gaussian weightings over past state–action pairs. We integrate these mechanisms into UniZero, a model-based RL agent with a Transformer-based world model that supports planning under partial observability. Experiments on the Atari 100k benchmark show that most efficiency gains arise from the Gaussian prior, which smoothly allocates attention to informative transitions, while memory-length priors often truncate useful signals with overly restrictive cut-offs. In particular, Gaussian Attention achieves a 77% relative improvement in mean human-normalized scores over UniZero. These findings suggest that in partially observable RL domains with non-stationary temporal dependencies, discrete memory windows are difficult to learn reliably, whereas smooth distributional priors flexibly adapt across horizons and yield more robust data efficiency. Overall, our results demonstrate that encoding structured temporal priors directly into self-attention improves the prioritization of informative histories for dynamics modeling under partial observability.[1]

1 Introduction

Reinforcement learning (RL) Sutton and Barto [2018] provides a principled framework for sequential decision making, but real-world tasks often violate the Markov assumption and exhibit only partial observability. Such settings are naturally modeled as Partially Observable Markov Decision Processes (POMDPs), which require agents to leverage observation–action histories to reduce uncertainty and achieve robust control Sondik [1971], Kaelbling et al. [1998].

Model-based RL addresses this challenge by learning an explicit world model of environment dynamics Sutton and Barto [2018], which can be used to plan or imagine future trajectories. A seminal example is MuZero Schrittwieser et al. [2020], which learns a joint representation, dynamics, and value model in latent space, paired with Monte Carlo Tree Search Kocsis and Szepesvári [2006] to achieve state-of-the-art performance in board games and Atari. More recently, UniZero Pu et al.

[1] Our code is publicly available in github.com/daniallegue/learning-to-focus

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[2025] replaced MuZero's recurrent dynamics with a Transformer backbone, using masked self-attention to capture long-range dependencies in latent state–action sequences and improve sample efficiency under partial observability.

Despite this architectural shift, UniZero often remains sample-inefficient in low-data regimes because it inherits assumptions from natural language modeling: namely, that sequential data are abundant, balanced, and richly interdependent. In reality, RL trajectories consist of long stretches of uninformative transitions, sparse rewards, skewed return distributions, and a limited number of interactions Janner et al. [2021], Andrychowicz et al. [2017]. In Transformer-based world models, standard self-attention treats all past tokens within the history as equally relevant, making it hard to identify the sparse transitions that actually drive reward. Unlike language modeling, where vast corpora make even rare dependencies learnable Brown et al. [2020], RL agents operate on scarce and noisy trajectories, requiring attention mechanisms that explicitly prioritize informative segments of history Ni et al. [2023].

To address this limitation, we enhance the UniZero world model by introducing two structured temporal priors into the self-attention layers of its dynamics head. The dynamics head predicts the next latent state z_{t+1} and immediate reward r_t based on attention-weighted histories. The first prior, a **memory-length prior**, restricts each attention head to a learnable contiguous window, approximating the minimal history required for accurate prediction. The second, a **distributional prior**, applies smooth Gaussian weighting over past tokens, emphasizing those most informative for immediate outcomes. We instantiate these as **Adaptive Attention** (memory-length prior), **Gaussian Attention** (distributional prior), and their combination, **Gaussian Adaptive Attention**.

On the Atari 100k benchmark, Gaussian Attention yields a 77% relative improvement in human-normalized mean score over UniZero's standard self-attention. This gain stems from its ability to allocate weight smoothly across past transitions, capturing relevant temporal dependencies without imposing sharp cutoffs. In contrast, Adaptive Attention often misestimates the true dependency horizon, either truncating important signals or including irrelevant ones, reducing sample efficiency. Combining the two mechanisms degrades performance: the hard span mask truncates Gaussian tails, negating its smooth weighting benefits. These results highlight a general guideline for model-based RL under partial observability: smooth distributional priors offer more robust and data-efficient dynamics modeling than rigid memory-length priors.

Our contributions are as follows:

- We propose two structured temporal priors for self-attention in world models: a memory-length prior enforcing per-head learnable look-back windows, and a distributional prior introducing smooth Gaussian weightings over histories.
- We integrate these mechanisms into the UniZero agent and demonstrate on Atari 100k that Gaussian Attention achieves substantial gains in human-normalized mean and median scores, with negligible computational overhead.
- We analyze the complementary behavior of hard and smooth priors, showing how Gaussian priors reliably capture diverse temporal dependencies while memory-length priors offer benefits in limited cases.
- Through systematic ablations across Atari games, we isolate the effects of each prior and its regularization, confirming robustness to initialization and low additional computational cost.

2 Background

MDPs and POMDPs. A Markov Decision Process (MDP) is defined by the tuple $(\mathcal{S}, \mathcal{A}, P, R, \gamma)$, where $\mathcal{S}$ is the state space, $\mathcal{A}$ is the action space, $P(s' \mid s, a)$ denotes the transition probability, $R(s, a)$ is the reward function, and $\gamma \in [0, 1)$ is the discount factor Sutton and Barto [2018]. The agent seeks a policy $\pi : \mathcal{S} \to \mathcal{A}$ that maximizes the expected discounted return $E[\sum_{t=1}^{\infty} \gamma^t R(s_t, a_t)]$, satisfying the Bellman optimality equation. A Partially Observable MDP (POMDP) extends this formulation with an observation space $\mathcal{O}$ and observation probabilities $O(o \mid s, a)$, since the true state is not directly observable, and thus is defined by $(\mathcal{S}, \mathcal{A}, \mathcal{O}, P, R, O, \gamma)$. To act under partial observability, the agent maintains a belief distribution b over states, updated after action a and observation o as $b_{a,o}(s') \propto O(o \mid s', a) \sum_s P(s' \mid s, a) b(s)$. Not all observations are equally informative, and a central objective in planning under partial observability is to identify a minimal subset of history

sufficient for predicting future transitions and rewards. Influence-Based Abstraction (IBA) formalizes this by identifying d-separating observation sets that render the future conditionally independent of the remaining history Oliehoek et al. [2012], echoing state-abstraction principles in RL Givan et al. [2003].

Transformers. Transformers Vaswani et al. [2017] have emerged as powerful alternatives to recurrent neural networks (RNNs) for long-sequence modeling. Given an input sequence of length N, each token is projected into queries $Q \in \mathbb{R}^{N \times d_k}$, keys $K \in \mathbb{R}^{N \times d_k}$, and values $V \in \mathbb{R}^{N \times d_v}$. Self-attention then aggregates contextual information via:

$$\text{Attention}(Q, K, V) = \text{softmax}\Big(\frac{QK^\top}{\sqrt{d_k}}\Big)V. \tag{1}$$

Since self-attention is permutation-invariant, positional encodings, either fixed or learned, are added to token embeddings to inject order information Devlin et al. [2019]. By combining global context aggregation with positional encodings, Transformers effectively capture long-range dependencies that truncated RNNs fail to model Dai et al. [2019]. This has made Transformer architectures compelling candidates for world models in RL, where long-horizon planning and memory are critical Ni et al. [2023], Robine et al. [2023].

MuZero. MuZero Schrittwieser et al. [2020] achieves superhuman performance in board games and Atari by integrating Monte Carlo Tree Search (MCTS) with a learned latent dynamics model. At each time step t, MuZero employs:

1. **Encoder:** $z_t^0 = h_\theta(o_{1:t})$, mapping the observation history to a latent state.
2. **Dynamics head:** $(z_{t+1}, r_t) = g_\theta(z_t, a_t)$, unrolling latent states and predicting rewards recurrently.
3. **Prediction head:** $(\pi_t, v_t) = f_\theta(z_t)$, producing policy logits and value estimates.

Although powerful, MuZero's recurrent dynamics suffer from vanishing gradients and a fixed unroll horizon, which limit its ability to capture long-range dependencies Bengio et al. [1994].

UniZero. UniZero Pu et al. [2025] retains MuZero's overall world model tuple $W = (h_\theta, g_\theta, f_\theta)$ but parameterizes g_θ and f_θ with a Transformer backbone. Unlike MuZero, whose encoder produces only a single latent state summarizing the entire history, UniZero encodes each observation individually as $z_i = h_\theta(o_i)$, yielding a sequence $z_{1:t}$. The sequence of observation–action pairs $\big[(z_1, a_1), \ldots, (z_t, a_t)\big]$ is then processed by L stacked Transformer layers, each with h attention heads. Masked self-attention ensures that token i attends only to past tokens, preventing future leakage (see Figure 1).

The outputs from all heads are concatenated and projected through a final linear layer, integrating the diverse subspaces captured by each head. This allows UniZero to capture dependencies far beyond MuZero's fixed horizon, though at quadratic complexity in the sequence length, the number of layers L, and the number of heads h. Moreover, because self-attention initially treats all past tokens as equally relevant, the model must learn relevance weights during training, often leading to sample inefficiency.

The final Transformer layer outputs the next latent state z_{t+1} and immediate reward r_t, which are passed to the unchanged prediction head f_θ to produce π_t and v_t. UniZero, like MuZero, is trained via joint model–policy optimization, maintaining a soft-target world model $\hat{W} = (\hat{h}_\theta, \hat{g}_\theta, \hat{f}_\theta)$ to stabilize learning Eysenbach et al. [2022]. By leveraging global temporal context, UniZero improves long-horizon performance, but its uniform attention weighting motivates the structured temporal priors we introduce in this work.

3 Related Work

RL in POMDPs. Under partial observability, model-free methods typically rely on recurrent networks to infer hidden states Hausknecht and Stone [2015], whereas model-based approaches learn latent world models for planning. Early frameworks such as predictive state representations Littman and Sutton [2001] have evolved into deep generative models such as Dreamer, which combine variational inference and recurrent state-space models to compactly represent belief states and enable efficient long-horizon planning Ha and Schmidhuber [2018], Hafner et al. [2020].

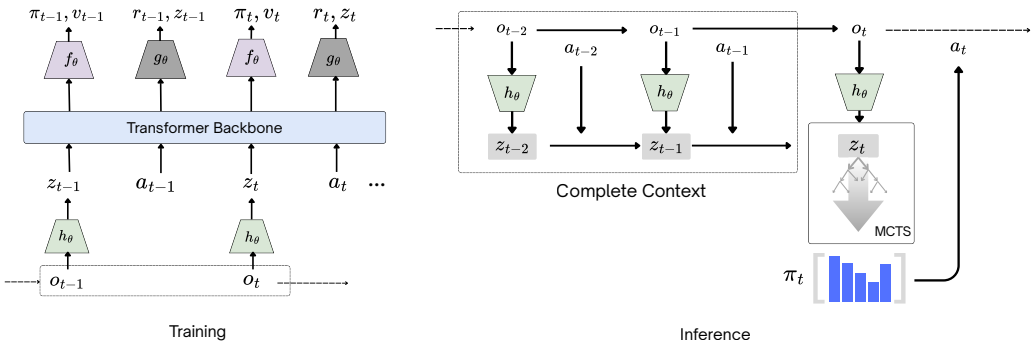

Figure 1: UniZero architecture. Overview of the UniZero world model $W = (h_\theta, g_\theta, f_\theta)$. The encoder h_θ maps observations o_t to latent states z_t. The dynamics head g_θ (a Transformer with masked self-attention) consumes past latent state-action pairs to predict the next state z_{t+1} and reward r_t. The prediction head f_θ outputs the policy π_t and value v_t for MCTS planning.

Memory Mechanisms in DRL. Many deep RL methods explicitly incorporate memory to handle partial observability. Simple approaches stack the last k frames Mnih et al. [2015], recurrent architectures summarize the entire action–observation history into fixed-size states Hausknecht and Stone [2015], and external differentiable memories further expand capacity but often introduce training instability Graves et al. [2016]. Influence-Aware Memory (IAM), inspired by Influence-Based Abstraction (IBA) Oliehoek et al. [2012], learns gating mechanisms that selectively retain past observations predictive of future outcomes Suau et al. [2022].

Transformer-based World Models. Recent Transformer adaptations in RL leverage self-attention to capture long-range dependencies, but most do not incorporate inductive priors tailored to RL sequences. On the model-free side, methods such as GTrXL and Transformer-XL stabilize attention via gating and relative encodings Parisotto et al. [2020], Dai et al. [2019], Decision Transformer reframes control as return-conditioned masked attention over past trajectories Chen et al. [2021], and Adaptive Span Transformer reduces computation by learning per-head context lengths without building an explicit dynamics model Kumar et al. [2020]. On the model-based side, hybrids such as IRIS Micheli et al. [2023] and TransDreamer Chen et al. [2022] integrate Transformers into latent world models, rolling out imagined trajectories for planning to achieve strong sample efficiency. However, most existing Transformer-based world models in RL rely on fixed or NLP-inspired positional encodings (e.g., sinusoidal or relative embeddings), which emphasize computational efficiency rather than task relevance. In contrast, we introduce structured temporal priors to better align attention with reward-relevant dependencies.

4 Dynamics Modelling with Self-Attention Priors

In UniZero's world model, the dynamics function aggregates past latents and actions up to time t into a history h_t, and predicts the next latent and reward:

$$(\hat{z}_{t+1}, \hat{r}_t) = g_\theta(z_{\leq t}, a_{\leq t}) = g_\theta(h_t), \tag{2}$$

where relevance is computed via self-attention with weights $\{\alpha_{ij}\}_{j=1}^{i}$ (with i the current query and j the key). Under partial observability, however, only a limited window of context and a sparse set of key events truly drive accurate predictions. To better align attention with these reward-relevant dependencies, we introduce two structured temporal priors into the attention mechanism: (i) a **memory-length prior** that enforces a learnable finite look-back span, and (ii) a **distributional prior** that softly emphasizes tokens according to a Gaussian saliency distribution. Our goal is to bias self-attention toward histories that matter most for predicting dynamics and rewards, thereby improving sample efficiency in low-data, partially observable RL settings. Figure 2 illustrates the different attention priors described in this section.

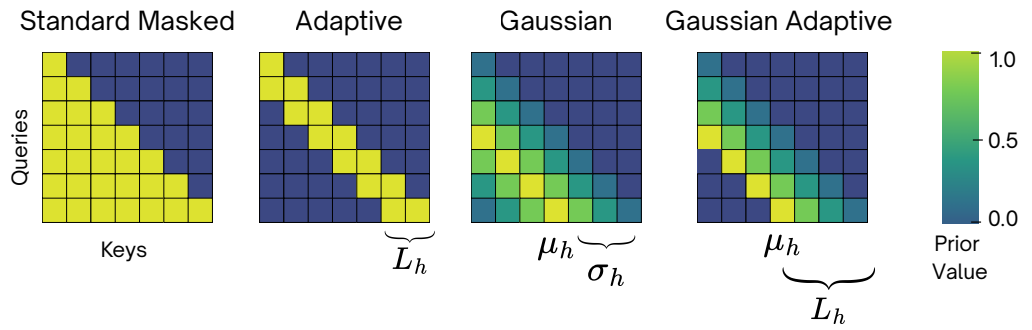

Figure 2: Attention priors. Visualization of the attention prior matrices described in Eqs. (5)–(9). Rows correspond to queries i (current timestep) and columns to keys j (past tokens). (From left to right) standard causal masking, the memory-length prior (Eq. 4), the Gaussian distributional prior (Eq. 7), and their combination (Eq. 9). Yellow indicates high prior bias, dark blue zero bias. Together, these priors constrain α_{ij} to emphasize reward-relevant temporal context $c_t^{(h)}$.

4.1 Memory-Length Prior

Many partially observable environments admit a finite effective memory: only the most recent n steps are needed to predict the next reward Littman and Sutton [2001], Mnih et al. [2016]. Imposing this prior focuses the model on a minimal history window, reducing redundant computation over distant tokens. Formally,

$$\mathbb{E}[r_t \mid h_{1:t}, a_t] \;=\; \mathbb{E}[r_t \mid h_{t-n+1:t}, a_t]. \tag{3}$$

We implement this using **Adaptive Attention** Sukhbaatar et al. [2019]. Each head h learns a scalar parameter s_h, transformed via softplus into a positive span $L_h = \mathrm{softplus}(s_h)$. A hard mask over relative positions is then constructed:

$$M_{ij}^{(h)} = \begin{cases} 0, & i - j \le L_h, \\ -\infty, & i - j > L_h, \end{cases} \tag{4}$$

so that queries at i can only attend within their learned look-back span. Attention weights become

$$\mathrm{Attention}^{(h)} = \mathrm{softmax}\big(\tfrac{Q^{(h)} K^{(h)\top}}{\sqrt{d_k}} + M^{(h)}\big). \tag{5}$$

To prevent trivial solutions where all spans grow without bound, we apply an ℓ_1 penalty, encouraging the model to learn minimal but sufficient spans Tibshirani [1996], Givan et al. [2003]. Each attention head h produces a context vector

$$c_t^{(h)} = \sum_{j=1}^{t} \alpha_{tj}^{(h)} [z_j; a_j], \tag{6}$$

where α_{tj} are the learned attention weights that determine the relative importance of past steps when computing the context, and $[z_j; a_j]$ denotes the concatenated latent state and action at step j. By constraining spans L_h, different heads specialize at distinct temporal scales, yielding a multi-scale representation when their context vectors are combined into h_t.

4.2 Distributional Prior

In partially observable settings, only a sparse subset of tokens carries predictive signal for $(\hat{z}_{t+1}, \hat{r}_t)$. We capture this *distributional prior* by learning a Gaussian positional kernel.

Each head h learns parameters $\mu_h, \sigma_h > 0$, defining

$$G_{ij}^{(h)} = -\frac{(i - j - \mu_h)^2}{2\sigma_h^2}. \tag{7}$$

This is added to the scaled dot-product logits:

$$\text{Attention}^{(h)} = \text{softmax}\Big(\frac{Q^{(h)}K^{(h)\top}}{\sqrt{d_k}} + G^{(h)}\Big), \tag{8}$$

so that queries at i privilege tokens at offset μ_h with sharpness σ_h Ioannides et al. [2024]. Unlike spans, μ_h and σ_h are unconstrained: σ_h may expand to broad attention or shrink to narrow focus, thereby giving each head a smooth, learned saliency profile through $G^{(h)}$. Different heads capture different offsets and spreads, producing complementary temporal filters that are concatenated into h_t.

4.3 Combining Priors

Finally, we combine the two priors by defining

$$B_{ij}^{(h)} = G_{ij}^{(h)} + M_{ij}^{(h)}, \tag{9}$$

and apply it within the attention mechanism by adding $B^{(h)}$ as a bias term to the scaled dot-product before the softmax. This **Gaussian Adaptive Attention** enforces a finite horizon while retaining smooth saliency within it, thereby combining the strengths of memory-length and distributional priors.

5 Experiments

We evaluate our Transformer-based world model augmented with attention priors on the Atari 100k benchmark, a widely used testbed for sample efficiency in model-based reinforcement learning. This suite spans diverse reward densities, horizon lengths, and stochastic dynamics. Our evaluation considers both aggregate performance and the contribution of each prior through controlled ablations.

5.1 Experimental Setup

Agents are trained on 26 Atari environments for $100k$ steps, with performance averaged over five random seeds (1–5) and reported as human-normalized scores following Łukasz Kaiser et al. [2020]. We utilize Single-Task (ST) training (separate model per environment) to isolate the effects of attention priors. Unless noted, we adopt UniZero's default hyperparameters from Pu et al. [2025]. Full details, configurations, and reproduction instructions are in Appendix A.

Attention Prior Initialization. We initialize all attention priors to align with typical temporal dependencies in Atari trajectories. For Adaptive Attention, each head begins with a span of $L_h^0 = 0.3\,L_{\max} \approx 6$, following the recommendations of Kumar et al. [2020]. Gaussian Attention is initialized with mean offset $\mu_h = 6$ and standard deviation $\sigma_h = 1$, while Gaussian Adaptive Attention learns both μ_h and σ_h but applies a hard cutoff at $L_h^0 = 10$. To ensure comparable starting conditions, initial distributional logits are sampled from $\mathcal{N}(\mu_h, \sigma_h^2)$, exactly matching the Gaussian prior.

Baselines. We compare against two established model-based RL baselines implemented in the LightZero framework Niu et al. [2023]: (i) *MuZero* Schrittwieser et al. [2020], which combines latent dynamics with Monte Carlo Tree Search, and (ii) *UniZero* Pu et al. [2025], which replaces MuZero's recurrent core with a Transformer backbone. Both baselines are trained for 100k steps per environment under identical hyperparameters, ensuring that performance differences arise solely from the proposed priors.

5.2 Performance Results

Table 1 reports Atari 100k results against UniZero (ST) and MuZero. Gaussian UniZero delivers the best overall performance, improving HNS from 0.13 to 0.23 (+77%) and HMS from 0.05 to 0.10 (+100%), outperforming the baseline in 19 of 26 games. Adaptive and Gaussian Adaptive variants yield inconsistent or weaker results, with Adaptive only matching the baseline on HMS. Overall, smooth Gaussian priors provide consistent sample-efficiency gains, while rigid span cutoffs hurt performance. Full learning curves can be found in Appendix B. .

Gaussian Attention consistently outperforms alternatives because it distributes weights smoothly across short- and mid-range temporal offsets, effectively capturing both immediate and moderately

Table 1: Raw Atari 100k scores comparing our attention-biased UniZero variants against reproduced UniZero and MuZero baselines. MuZero results are from LightZero reproductions in Pu et al. [2025] (three seeds), while Random and Human scores are from Pu et al. [2025]. All "Ours" results are averaged over five seeds. **Bold** entries denote the superior method between the *UniZero ST* baseline and our attention-biased methods, while underlined values indicate the overall best-performing method.

Game	Random	Human	MuZero	UniZero ST (Baseline)	Adaptive UniZero (Ours)	Gaussian UniZero (Ours)	Gaussian Adaptive UniZero (Ours)
Alien	227.8	7127.7	300.0	468.5	**570.6**	483.3	509.6
Amidar	5.8	1719.5	90.0	57.2	57.9	**71.2**	53.4
Assault	222.4	742.0	609.0	341.9	423.5	**486.8**	333.7
Asterix	210.0	8503.7	1400.0	495.3	500.1	**619.9**	333.6
BankHeist	14.2	753.1	223.0	91.3	13.3	**165.1**	0.7
BattleZone	2360.0	37187.5	7587.0	**6000.0**	5872.5	5361.6	5297.6
Boxing	0.1	12.1	20.0	0.1	−9.5	**2.4**	−11.3
Breakout	1.7	30.5	3.0	3.7	0.8	**5.1**	0.5
ChopperCommand	811.0	7387.8	1050.0	1169.0	872.5	**1263.4**	735.2
CrazyClimber	10780.5	35829.4	22060.0	7418.9	4326.6	**7966.6**	2020.0
DemonAttack	152.1	1971.0	4601	236.3	187.4	**267.0**	166.4
Freeway	0.0	29.6	12.0	0.0	0.7	0.1	**2.6**
Frostbite	65.2	4334.7	260.0	239.8	**261.2**	236.7	162.2
Gopher	257.6	2412.5	346.0	606.7	646.4	**798.8**	240.0
Hero	1027.0	30826.4	3315.0	1483.0	1422.2	699.6	**2414.4**
Jamesbond	29.0	302.8	90.0	201.7	156.7	**362.0**	75.9
Kangaroo	52.0	3035.0	200.0	842.6	488.6	**1636.4**	367.9
Krull	1598.0	2665.5	5191.0	2539.8	2647.5	**3108.8**	1964.0
KungFuMaster	258.5	22736.3	6100.0	2019.0	8546.5	**9424.5**	644.3
MsPacman	307.3	6951.6	1010.0	643.9	**1103.3**	726.6	394.7
Pong	−20.7	14.6	−15.0	−14.5	−19.6	**−7.1**	−20.3
PrivateEye	24.9	69571.3	100.0	**93.3**	−60.1	57.6	80.0
Qbert	163.9	13455.0	1700.0	677.2	941.5	**1741.8**	356.3
RoadRunner	11.5	7845.0	4400.0	1941.3	**2164.5**	1948.4	1400.0
Seaquest	68.4	42054.7	466.0	384.1	293.2	**485.7**	273.3
UpNDown	533.4	11693.2	1213.0	2018.0	1374.7	**2373.8**	1246.4
Normalized Mean	0.000	1.000	0.44	0.13	0.095	**0.23**	0.00
Normalized Median	0.000	1.000	0.13	0.05	0.05	**0.10**	0.02

delayed dependencies Ni et al. [2023]. By contrast, Adaptive Attention's hard spans often misestimate the relevant horizon, either truncating delayed yet informative signals or incorporating irrelevant context. Combining Gaussian weighting with a hard cutoff further degrades performance: truncating the Gaussian kernel removes useful tails and produces conflicting priors. Together, these findings suggest a general guideline for model-based RL under partial observability: smooth, learnable positional priors offer a more robust and flexible mechanism for temporal modeling than rigid memory windows. Future directions include extending Gaussian priors to multi-task settings, where shared temporal structure across games could further improve generalization.

5.3 Ablation Studies

To isolate the contributions of each prior, we conduct ablations on four representative Atari games: Pong, MsPacman, Jamesbond, and Freeway, which span diverse observation complexities, reward structures, and temporal dependencies.

Regularization Ablation. We compare three penalties on the learned span vector L_h, each with penalty coefficient $\lambda = 0.025$ as in Kumar et al. [2020]:

① Max-norm $\ell_{\max}$: enforces $\|L_h\|_\infty \leq c$, restricting each head to the most recent tokens Srivastava et al. [2014].

② ℓ_1: adds $\lambda \sum_j L_{h,j}$, encouraging sparsity by driving many spans to zero while letting a few grow.

③ ℓ_2: adds $\lambda \sum_j L_{h,j}^2$, softly shrinking spans while preserving long-range context.

In practice, max-norm favors purely short-term attention; ℓ_1 produces a bimodal mix of very short and very long spans; and ℓ_2 encourages balanced recency while retaining moderate long-range dependencies. Figure 3 illustrates these effects: max-norm performs best in short-horizon tasks, ℓ_2 dominates in mid-horizon settings, and ℓ_1 occasionally excels in long-horizon environments by retaining sparse but wide spans. Overall, ℓ_2 generalizes most robustly, striking a balance between stability and flexibility.

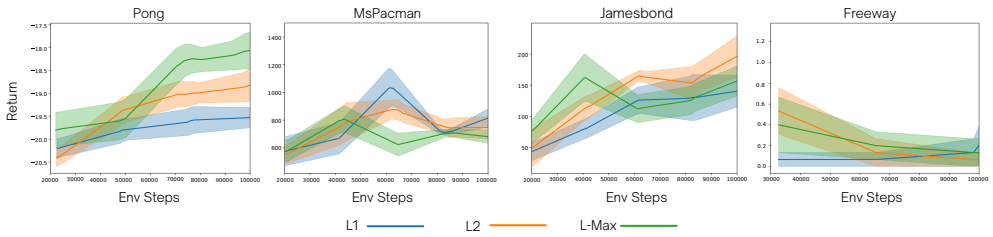

Figure 3: Regularization ablation. Comparison of ℓ_1 (blue), ℓ_2 (orange), and max-norm (green) penalties across four Atari games over five seeds. Shaded regions denote standard error. Each scheme exhibits task-specific strengths, but ℓ_2 achieves the most consistent performance overall.

Initial Parameter Sensitivity. As shown in Table 2, sensitivity analysis reveals robustness to initial spans (L_h) and Gaussian centers (μ_h), which adapt quickly. However, the Gaussian width σ_h is critical: narrower priors ($\sigma_h = 1$) consistently yield superior results, whereas wider priors ($\sigma_h = 3$) underperform. This indicates that a tight positional prior is essential for a strong inductive initial distribution.

Table 2: Ablation on initialization of attention priors. Mean $\pm$ standard error over five seeds on four Atari games. Varying initial spans L_h or offsets μ_h has little effect, while narrow Gaussian widths ($\sigma_h = 1$) consistently improve performance. **Bold** entries mark the best result per game.

	Pong	**MsPacman**	**Jamesbond**	**Freeway**
$L_h = 2$	-18.5 ± 0.4	716.7 ± 58.9	180.0 ± 49.8	2.2 ± 2.1
$L_h = 6$	-19.6 ± 0.4	$\mathbf{1103.3 \pm 345.8}$	156.7 ± 29.8	0.7 ± 0.6
$L_h = 10$	-18.7 ± 0.5	633.3 ± 47.4	130.0 ± 34.7	$\mathbf{2.7 \pm 2.1}$
$\mu_h = 2$	$\mathbf{-6.9 \pm 1.8}$	805.3 ± 112.6	293.3 ± 49.6	0.0 ± 0.0
$\mu_h = 6$	-7.9 ± 1.0	726.7 ± 98.2	$\mathbf{362.1 \pm 53.1}$	0.1 ± 0.1
$\mu_h = 10$	-10.5 ± 1.0	894.7 ± 101.8	290.0 ± 58.4	0.1 ± 0.1
$\sigma_h = 1$	-7.9 ± 1.0	726.7 ± 98.2	$\mathbf{362.1 \pm 53.1}$	0.1 ± 0.1
$\sigma_h = 3$	-15.1 ± 0.7	638.7 ± 47.6	196.7 ± 24.4	0.0 ± 0.0

Limitations. Our evaluation is restricted to Atari, leaving open whether the proposed attention priors generalize to continuous-control or multi-task settings. In addition, the learned look-back spans require regularization to avoid collapse to trivial extremes, which may limit adaptability in environments with highly variable temporal dependencies. Future work should investigate more flexible temporal priors and evaluate their robustness across broader RL domains, including continuous-control benchmarks such as Tassa et al. [2018].

6 Conclusion

In NLP, Transformers benefit from massive, balanced corpora where long-range dependencies recur frequently, allowing self-attention to capture them implicitly. In contrast, model-based RL agents must identify the few reward-relevant dependencies hidden within sparse and correlated trajectories under limited supervision. This mismatch makes standard self-attention sample-inefficient, as it spreads its focus across many uninformative transitions rather than concentrating on the critical ones. We addressed this by incorporating two inductive priors into UniZero's dynamics head: a **memory-length prior**, restricting each head to a finite span, and a **distributional prior**, implemented as a smooth Gaussian positional prior.

Experiments on Atari-100k demonstrate that Gaussian positional priors substantially improve sample efficiency, delivering a 100% relative gain in human-normalized median score, while hard span cutoffs degrade performance by truncating delayed yet informative signals. These results suggest a broader principle: smooth, learnable temporal priors align better with the irregular dependency structure of RL trajectories than rigid memory windows. Looking ahead, structured temporal priors in self-attention promise to improve robustness and data efficiency in Transformer world models, with potential benefits extending beyond Atari to continuous control, multi-task learning, and other domains with complex temporal dependencies.

References

Marcin Andrychowicz, Filip Wolski, Alex Ray, Jonas Schneider, Rachel Fong, Peter Welinder, Bob McGrew, Josh Tobin, OpenAI Pieter Abbeel, and Wojciech Zaremba. Hindsight experience replay. *Advances in Neural Information Processing Systems*, 30, 2017.

Yoshua Bengio, Patrice Simard, and Paolo Frasconi. Learning long-term dependencies with gradient descent is difficult. *IEEE Transactions on Neural Networks*, 5(2):157–166, 1994.

Tom Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared D Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, et al. Language models are few-shot learners. *Advances in Neural Information Processing Systems*, 33:1877–1901, 2020.

Chang Chen, Yi-Fu Wu, Jaesik Yoon, and Sungjin Ahn. Transdreamer: Reinforcement learning with transformer world models. *arXiv preprint arXiv:2202.09481*, 2022.

Lili Chen, Kevin Lu, Aravind Rajeswaran, Kimin Lee, Aditya Grover, Misha Laskin, Pieter Abbeel, Aravind Srinivas, and Igor Mordatch. Decision transformer: Reinforcement learning via sequence modeling. *Advances in Neural Information Processing Systems*, 34:15084–15097, 2021.

Zihang Dai, Zhilin Yang, Yiming Yang, Jaime Carbonell, Quoc Le, and Ruslan Salakhutdinov. Transformer-XL: Attentive language models beyond a fixed-length context. In *Proceedings of the 57th Annual Meeting of the Association for Computational Linguistics*, pages 2978–2988. Association for Computational Linguistics, 2019.

Jacob Devlin, Ming-Wei Chang, Kenton Lee, and Kristina Toutanova. BERT: Pre-training of deep bidirectional transformers for language understanding. In *Proceedings of the 2019 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, Volume 1 (Long and Short Papers)*, pages 4171–4186. Association for Computational Linguistics, 2019.

Benjamin Eysenbach, Alexander Khazatsky, Sergey Levine, and Russ R Salakhutdinov. Mismatched no more: Joint model-policy optimization for model-based rl. *Advances in Neural Information Processing Systems*, 35:23230–23243, 2022.

Robert Givan, Thomas Dean, and Matthew Greig. Equivalence notions and model minimization in markov decision processes. *Artificial intelligence*, 147(1-2):163–223, 2003.

Alex Graves, Greg Wayne, Malcolm Reynolds, Tim Harley, Ivo Danihelka, Agnieszka Grabska-Barwińska, Sergio Gómez Colmenarejo, Edward Grefenstette, Tiago Ramalho, John Agapiou, et al. Hybrid computing using a neural network with dynamic external memory. *Nature*, 538(7626): 471–476, 2016.

David Ha and Jürgen Schmidhuber. World models. *arXiv preprint arXiv:1803.10122*, 2018.

Danijar Hafner, Timothy Lillicrap, Jimmy Ba, and Mohammad Norouzi. Dream to control: Learning behaviors by latent imagination. In *International Conference on Learning Representations*, 2020.

Nicklas Hansen, Hao Su, and Xiaolong Wang. Td-mpc2: Scalable, robust world models for continuous control. *arXiv preprint arXiv:2310.16828*, 2023.

Matthew J Hausknecht and Peter Stone. Deep recurrent q-learning for partially observable mdps. In *AAAI fall symposia*, volume 45, page 141, 2015.

Dan Hendrycks and Kevin Gimpel. Gaussian error linear units (gelus). *arXiv: Learning*, 2016.

Georgios Ioannides, Aman Chadha, and Aaron Elkins. Gaussian adaptive attention is all you need: Robust contextual representations across multiple modalities. *CoRR*, 2024.

Michael Janner, Qiyang Li, and Sergey Levine. Offline reinforcement learning as one big sequence modeling problem. In *Advances in Neural Information Processing Systems*, volume 34, pages 1273–1286, 2021.

Leslie Pack Kaelbling, Michael L Littman, and Anthony R Cassandra. Planning and acting in partially observable stochastic domains. *Artificial intelligence*, 101(1-2):99–134, 1998.

Levente Kocsis and Csaba Szepesvári. Bandit based monte-carlo planning. In *Machine Learning: ECML 2006*, pages 282–293. Springer Berlin Heidelberg, 2006.

Shakti Kumar, Jerrod Parker, and Panteha Naderian. Adaptive transformers in rl. *arXiv preprint arXiv:2004.03761*, 2020.

Michael Littman and Richard S Sutton. Predictive representations of state. *Advances in Neural Information Processing Systems*, 14, 2001.

Ilya Loshchilov and Frank Hutter. Decoupled weight decay regularization. In *International Conference on Learning Representations*, 2019.

Vincent Micheli, Eloi Alonso, and François Fleuret. Transformers are sample-efficient world models. In *The Eleventh International Conference on Learning Representations*, 2023.

Volodymyr Mnih, Koray Kavukcuoglu, David Silver, Andrei A Rusu, Joel Veness, Marc G Bellemare, Alex Graves, Martin Riedmiller, Andreas K Fidjeland, Georg Ostrovski, et al. Human-level control through deep reinforcement learning. *Nature*, 518(7540):529–533, 2015.

Volodymyr Mnih, Adria Puigdomenech Badia, Mehdi Mirza, Alex Graves, Timothy Lillicrap, Tim Harley, David Silver, and Koray Kavukcuoglu. Asynchronous methods for deep reinforcement learning. In *International Conference on Machine Learning*, pages 1928–1937. PMLR, 2016.

Tianwei Ni, Michel Ma, Benjamin Eysenbach, and Pierre-Luc Bacon. When do transformers shine in rl? decoupling memory from credit assignment. *Advances in Neural Information Processing Systems*, 36:50429–50452, 2023.

Yazhe Niu, Yuan Pu, Zhenjie Yang, Xueyan Li, Tong Zhou, Jiyuan Ren, Shuai Hu, Hongsheng Li, and Yu Liu. Lightzero: A unified benchmark for monte carlo tree search in general sequential decision scenarios. *Advances in Neural Information Processing Systems*, 36:37594–37635, 2023.

Frans Oliehoek, Stefan Witwicki, and Leslie Kaelbling. Influence-based abstraction for multiagent systems. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 26, pages 1422–1428, 2012.

Emilio Parisotto, Francis Song, Jack Rae, Razvan Pascanu, Caglar Gulcehre, Siddhant Jayakumar, Max Jaderberg, Raphael Lopez Kaufman, Aidan Clark, Seb Noury, et al. Stabilizing transformers for reinforcement learning. In *International Conference on Machine Learning*, pages 7487–7498. PMLR, 2020.

Yuan Pu, Yazhe Niu, Zhenjie Yang, Jiyuan Ren, Hongsheng Li, and Yu Liu. Unizero: Generalized and efficient planning with scalable latent world models. *Transactions on Machine Learning Research*, 2025. ISSN 2835-8856.

Jan Robine, Marc Höftmann, Tobias Uelwer, and Stefan Harmeling. Transformer-based world models are happy with 100k interactions. In *The Eleventh International Conference on Learning Representations*, 2023.

Julian Schrittwieser, Ioannis Antonoglou, Thomas Hubert, Karen Simonyan, Laurent Sifre, Simon Schmitt, Arthur Guez, Edward Lockhart, Demis Hassabis, Thore Graepel, et al. Mastering atari, go, chess and shogi by planning with a learned model. *Nature*, 588(7839):604–609, 2020.

Edward Jay Sondik. *The optimal control of partially observable markov processes*. PhD thesis, Stanford University, Stanford, CA, 1971.

Nitish Srivastava, Geoffrey Hinton, Alex Krizhevsky, Ilya Sutskever, and Ruslan Salakhutdinov. Dropout: a simple way to prevent neural networks from overfitting. *The journal of machine learning research*, 15(1):1929–1958, 2014.

Miguel Suau, Jinke He, Elena Congeduti, Rolf A. N. Starre, Aleksander Czechowski, and Frans A. Oliehoek. Influence-aware memory architectures for deep reinforcement learning in pomdps. *Neural Computing and Applications*, 37(19):13145–13161, 2022. doi: 10.1007/s00521-022-07691-7.

Sainbayar Sukhbaatar, Edouard Grave, Piotr Bojanowski, and Armand Joulin. Adaptive attention span in transformers. In *Proceedings of the 57th Annual Meeting of the Association for Computational Linguistics*, pages 331–335. Association for Computational Linguistics, 2019.

Richard S. Sutton and Andrew G. Barto. *Reinforcement learning: An introduction*. MIT Press, Cambridge, MA, second edition, 2018.

Yuval Tassa, Yotam Doron, Alistair Muldal, Tom Erez, Yazhe Li, Diego de Las Casas, David Budden, Abbas Abdolmaleki, Josh Merel, Andrew Lefrancq, et al. Deepmind control suite. *arXiv preprint arXiv:1801.00690*, 2018.

Robert Tibshirani. Regression shrinkage and selection via the lasso. *Journal of the Royal Statistical Society Series B: Statistical Methodology*, 58(1):267–288, 1996.

Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N Gomez, Łukasz Kaiser, and Illia Polosukhin. Attention is all you need. *Advances in Neural Information Processing Systems*, 30, 2017.

Łukasz Kaiser, Mohammad Babaeizadeh, Piotr Miłos, Błażej Osiński, Roy H Campbell, Konrad Czechowski, Dumitru Erhan, Chelsea Finn, Piotr Kozakowski, Sergey Levine, Afroz Mohiuddin, Ryan Sepassi, George Tucker, and Henryk Michalewski. Model based reinforcement learning for atari. In *International Conference on Learning Representations*, 2020.

A Implementation Details

Encoder Archictecture. We adopt the UniZero encoder architecture Pu et al. [2025], which builds on the convolutional backbone of LightZero Niu et al. [2023] and adds a final linear projection to produce a 768-dimensional (D) latent state. To improve training stability under partial observability, we incorporate simplicial normalization (SimNorm) Hansen et al. [2023], which normalizes each latent segment via a learnable temperature-controlled mappings.

Transformer Backbone and Prediction Heads. Our Transformer backbone follows the nanoGPT architecture described in Pu et al. [2025], stacking multiple self-attention and feed-forward layers to process sequences of timestep inputs. All of our proposed inductive biases are implemented directly within the self-attention module of each Transformer layer. At each step, the latent state (after SimNorm) and the corresponding action are embedded into a common D-dimensional space via learnable `nn.Embedding` (or a linear layer for continuous actions) and summed with learnable positional embeddings. The Transformer outputs context-enriched representations that are sent to two separate two-layer MLPs with GELU Hendrycks and Gimpel [2016] activations: the dynamics head predicts the next latent state (of dimension D, followed by SimNorm) and the reward distribution (discrete support size), while the decision head predicts policy logits (action-space size) and value distribution (support size).

Training Details. All reported results are averaged over 5 random seeds, with error bars as described in Appendix B. Atari environments are provided through the ALE interface (Gymnasium 0.28, sticky actions enabled), ensuring consistency with prior work. All experiments were conducted with a configuration of a single NVIDIA Tesla A100 / V100 GPU, $15-20$ CPU cores, and $60-80$ GB of total RAM. Training an Atari agent for $100{,}000$ environment steps requires approximately $4-5$ hours, with agent evaluations every $10{,}000$ steps (starting after the $20{,}000$th step). We observed stable results across A100 and V100 GPUs. Training configurations can be found in the `zoo/atari/config` directory, where each attention model has a different configuration file within UniZero. See README file in the codebase for details on how to train an agent.

Compute and Memory Overhead. All proposed priors incur negligible overhead, with at most a 0.002% increase in MFLOPs per forward pass. Table 3 shows that parameter counts and FLOPs remain effectively unchanged relative to UniZero, demonstrating that the efficiency gains of adaptive and Gaussian attention come at no meaningful computational cost.

Table 3: Overhead analysis. Parameter counts (in millions), MFLOPs per Transformer forward pass, and relative increase over the vanilla UniZero baseline.

Model	Total Parameters (M)	Transformer Parameters (M)	MFLOPs	Δ MFLOPs (%)
Baseline	20.77	14.18	454.611	—
Adaptive	20.77	14.18	454.615	**+0.001**
Gaussian	20.77	14.18	454.619	**+0.002**
Gaussian Adaptive	20.77	14.18	454.619	**+0.002**

Hyperparameters and Environments. Table 4 summarizes all architectural and training parameters used in our experiments. Most values such as latent dimension, Transformer depth, MCTS settings, and optimizer configuration are inherited from UniZero Pu et al. [2025], with additional entries for our attention-bias hyperparameters. All Atari environments are provided through the ALE interface via Gymnasium v0.28, using the standard `NoFrameskip` variants with sticky actions enabled, matching the settings in the UniZero framework. We select the environments from the Atari 100k benchmark Łukasz Kaiser et al. [2020].

Table 4: Key Hyperparameters. The values are aligned with those in Pu et al. [2025] for Atari environments. The section on **Attention** refers to the newly added parameters.

Hyperparameter	Value
Planning	

(continued)

Hyperparameter	Value
Number of MCTS Simulations (sim)	50
Inference Context Length (H_{infer})	4
Temperature	0.25
Dirichlet Noise (α)	0.3
Dirichlet Noise Weight	0.25
Coefficient c_1	1.25
Coefficient c_2	19652
Environment and Replay Buffer	
Replay Buffer Capacity	1,000,000
Sampling Strategy	Uniform
Observation Shape (Atari)	(3, 64, 64) (stack1)
Reward Clipping	True
Number of Frames Stacked	1 (stack1)
Frame Skip	4
Game Segment Length	400
Data Augmentation	False
Architecture	
Latent State Dimension (D)	768
Number of Transformer Heads	8
Number of Transformer Layers (N)	2
Dropout Rate (p)	0.1
Activation Function	LeakyReLU (encoder); GELU (others)
Reward/Value Bins	101
SimNorm Dimension (V)	8
SimNorm Temperature (τ)	1
Optimization	
Training Context Length (H)	10
Replay Ratio	0.25
Buffer Reanalyze Frequency	1/50
Batch Size	64
Optimizer	AdamW Loshchilov and Hutter [2019]
Learning Rate	1×10^{-4}
Next Latent State Loss Coefficient	10
Reward Loss Coefficient	1
Policy Loss Coefficient	1
Value Loss Coefficient	0.5
Policy Entropy Coefficient	1×10^{-4}
Weight Decay	10^{-4}
Max Gradient Norm	5
Discount Factor	0.997
Soft Target Update Momentum	0.05
Hard Target Network Update Frequency	100
Temporal Difference (TD) Steps	5
Evaluation Frequency	10k Collector Steps
Attention	
Attention Type	*causal*, *gaussian*, *adaptive* or *gaam*
Rotary Positional Embeddings	False
Initial Gaussian Mean Offset μ_0^h (`init_adaptive_mu`)	6.0 (Varied across ablations)
Initial Gaussian Standard Deviation σ_0^h (`init_adaptive_sigma`)	1.0 (Varied across ablations)

(continued)

Hyperparameter	**Value**
Max Adaptive Span (`max_adaptive_span`)	20.0
Initial Adaptive Span L_h^0 (`init_adaptive_span`)	6.0 (Adaptive), 10.0 (Gaussian Adaptive)
Adaptive Span Regularization Parameter (`adapt_span_loss`)	0.025
Adaptive Span Ramp R (`adapt_span_ramp`)	3.0

B Learning Curves and Learned Priors

Figure 4: Learning Curves for Attention-Biased UniZero. Each panel plots the mean evaluation return (solid line) and standard error (shaded band) over five random seeds for three variants: Gaussian attention (blue), Adaptive attention (orange), and Gaussian Adaptive attention (green). The grey dotted horizontal line in each subplot marks the UniZero baseline's final return at the 100,000th environment step.

In Pong, the learned parameters reveal clear differences between the inductive priors (Figure 5).

Adaptive attention. The learned memory spans L_h (initialized at 6) drift inconsistently across heads and layers. Some collapse to very short horizons, while others expand far beyond the relevant dependency range. This instability indicates that Adaptive attention struggles to capture Pong's narrow but stable temporal dependencies.

Gaussian attention. By contrast, Gaussian attention learns mean offsets μ_h that remain close to the initialization ($\mu \approx 6$), while widths σ_h expand moderately beyond 1.0. This produces smooth, head-specific kernels that emphasize a few recent steps but still leverage informative tails. These stable parameters align well with Pong's true dependency horizon and explain the stronger performance of this variant.

Gaussian Adaptive attention. This mechanism combines both priors, but the hard cutoff imposed by L_h (initialized at 10) often truncates the Gaussian kernel. Although the learned μ_h and σ_h resemble those of Gaussian attention, the span clips the tails, removing the soft weighting needed to capture delayed signals. As a result, Gaussian Adaptive inherits the instability of Adaptive rather than the robustness of Gaussian.

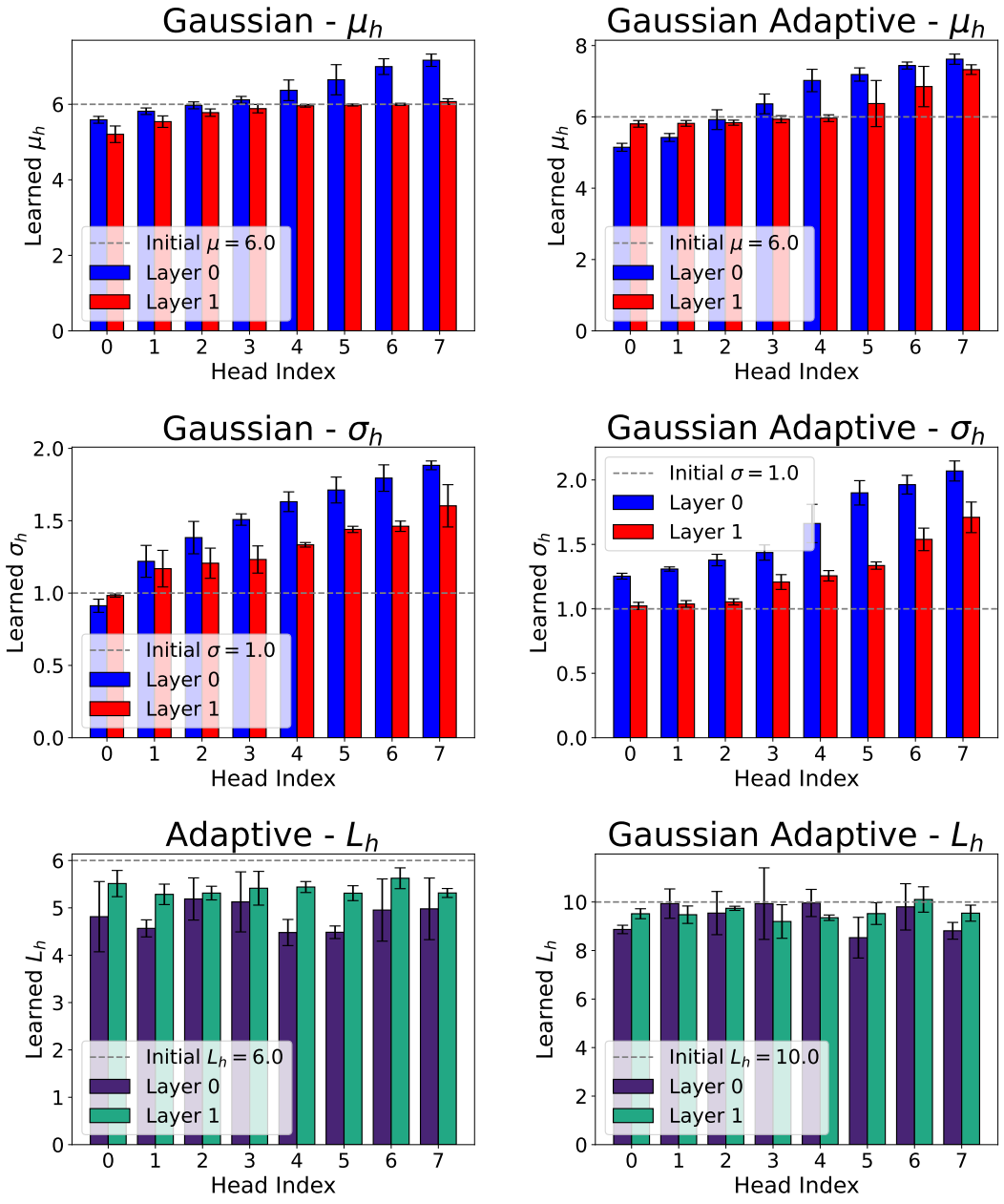

Figure 5: Learned adaptive and Gaussian-based attention parameters in Pong. The six subplots report the learned values across attention heads and layers, compared against their initialization (dashed lines). Top row: learned Gaussian mean offsets (μ_h) for Gaussian (left) and Gaussian Adaptive (right) attention. Middle row: learned Gaussian standard deviations (σ_h) for Gaussian (left) and Gaussian Adaptive (right) attention. Bottom row: learned adaptive memory lengths (L_h) for Adaptive (left) and Gaussian Adaptive (right) attention. Each bar shows the mean over 5 random seeds, with error bars indicating standard deviations. These plots illustrate how different inductive biases (Gaussian, Adaptive, and Gaussian Adaptive) evolve during training and how learned parameters adapt relative to their initial values.

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