Interventional Probing in High Dimensions: An NLI Case Study

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Abstract

 Probing strategies have been shown to detect semantic features intermediate to certain frag- ments of NLI. In the case of natural logic, the relation between these features and the entail- ment label is explicitly known: as such, this provides a ripe setting for interventional studies on the NLI models' representations, allowing for stronger causal conjectures and a deeper critical analysis of interventional probing meth- ods. In this work, we carry out new and exist- ing vector-level interventions to investigate the 012 effect of these semantic features on NLI classi- fication: we perform *amnesic* probing (which removes features as directed by learned probes) and introduce the *mnestic* probing variation (which forgets all dimensions *except* the probe- selected ones). Furthermore, we delve into the limitations of these methods and outline pitfalls 019 that have been obscuring the effectivity of such **020** studies.

021 1 **Introduction**

 The *probing* paradigm has emerged as a useful in- terpretability methodology which has been shown to have reasonable information-theoretic underpin- nings [\(Pimentel et al.,](#page-8-0) [2020;](#page-8-0) [Voita and Titov,](#page-8-1) [2020;](#page-8-1) [Zhu and Rudzicz,](#page-8-2) [2020\)](#page-8-2), indicating whether a given feature is captured in the intermediate vector rep- resentations of neural models. It has been noted many times that this does not generally imply that the models are *using* these learnt features, and they may represent vestigial information from earlier [t](#page-8-4)raining steps [\(Ravichander et al.,](#page-8-3) [2021;](#page-8-3) [Elazar](#page-8-4) [et al.,](#page-8-4) [2020\)](#page-8-4).

 Only through interventional analyses can we start to make claims about which modelled fea- tures are used for a given downstream task: this is the aim of works such as [Elazar et al.](#page-8-4) [\(2020\)](#page-8-4) and [Geiger et al.](#page-8-5) [\(2021\)](#page-8-5). We refer to the case where the interventions are guided by trained probes as *interventional probing*.

It has been suggested in [Elazar et al.](#page-8-4) [\(2020\)](#page-8-4) that **041** if features are strongly detected by probes, one may **042** use debiasing methods such as *iterative nullspace* **043** *projection (INLP)* [\(Ravfogel et al.,](#page-8-6) [2020\)](#page-8-6) to inter- **044** vene on the corresponding vector representations **045** and effectively "remove" the features before re- **046** insertion into the given classifier. This methodol- **047** ogy is referred to as *amnesic probing* [\(Elazar et al.,](#page-8-4) **048** [2020\)](#page-8-4). Investigating the effect of these intervention **049** operations on the classifier performance could al- **050** low for stronger causal claims about the role of the **051** probe-detected features. **052**

In this work, we delve deeper into the amnesic **053** probing methodology with an NLI case study and **054** identify two key limitations. Firstly, there is an **055** issue of dimensionality: when the number of di- **056** mensions is high and the number of auxiliary fea- **057** ture classes is low, it seems that amnesic probing **058** is not sufficiently informative. In particular, we **059** cannot rely on the same control baselines to reach **060** the kind of conclusions discussed in [\(Elazar et al.,](#page-8-4) **061** [2020\)](#page-8-4), as nulling out small numbers of random **062** directions consistently has no impact on the down- **063** stream performance. Secondly, in the linguistic **064** settings explored in [Elazar et al.](#page-8-4) [\(2020\)](#page-8-4), we do 065 not have expectations for exactly *how* or even *if* **066** the explored features should be affecting the down- **067** stream task. This makes it difficult to explore the **068** effectivity of the methodology itself. **069**

To this end, we propose the use of a controlled **070** [s](#page-8-7)ubset of NLI called *Natural Logic* [\(MacCartney](#page-8-7) **071** [and Manning,](#page-8-7) [2007\)](#page-8-7). In this setting, the interme- **072** diate linguistic features of *context montonicity* and **073** *lexical relations* are already known to be highly **074** extractable from certain NLI models' hidden lay- **075** ers [\(Rozanova et al.,](#page-8-8) [2021b\)](#page-8-8), allowing us a certain **076** amount of understanding and control of these fea- **077** tures' representations in the latent space. Using **078** the deterministic and well-understood nature of the **079** problem space where we have concrete *expecta-* **080** *tions* about the theoretical interaction between the **081**

Figure 1: Workflow for Interventional Probing For NLI Models

082 intermediate features and the downstream label, we **083** may critically analyse the effectivity of interven-**084** tional probing.

 Through the application of probe-based interven-086 tions in this setting, we show that blindly applying the amnesic probing argument structure leads to unexpected and contradictory conclusions: the two features which the final label is known to depend on are shown to have no influence on the final clas- sification (both jointly and independently). This further calls into question the suitability of these methods for situations where a small number of feature label classes and high dimensionality of representations is concerned.

 As a consequence, we introduce and study a variation which we call *mnestic* probing, which we show to be more informative in the high- dimensional, low-class-count setting: the core idea is to *keep only* the directions identified by the it- eratively trained probes. This allows us to anal- yse much lower dimension subspaces, and leads to more informative observations in line with ex-pected behaviour for natural logic.

105 In summary, the contributions of the paper are **106** as follows:

- **107** 1. We propose the setting of *natural logic* to be **108** ripe territory for exploration of interventional **109** probing strategies.
- **110** 2. We note two limitations of the amnesic prob-**111** ing methodology, demonstrating both dimen-**112** sionality limitations for the control baselines

[4.4](#page-6-0) and contradictory behaviour in the NLI **113** setting [4.2](#page-4-0) (namely that that the expected ef- **114** fects of semantic features on the downstream **115** NLI task are notably absent). **116**

- 3. Building upon previous interventional **117** methodologies, we introduce an additional **118** *mnestic* intervention operation based on probe **119** outputs, which uses the outputs of the INLP **120** process in the opposite way. **121**
- 4. We contrast the mnestic probing strategy with **122** the amnesic probing results, and demonstrate **123** it presents more informative results which are **124** aligned with the constructed expectations in **125** our high dimensional, low label class count **126** setting. **127**

2 Interventional Probing **¹²⁸**

We may summarise the general setup of interven- **129** tional probing as follows: suppose we start with **130** a classification model that may be decomposed as **131** $f \circ g : \mathcal{X} \to \mathbb{R}^n$, where g is an encoder module 132 which yields a representation that serves as an input to the classifier head f , and n is the number **134** of output classes of the final classifier. We aim **135** to intervene on the output of g and observe the **136** change in the performance of f (usually in comparison with some kind of random control baseline **138** intervention).

Linear probes are able to identify subspaces in **140** which a given feature set is best represented: these 141 may be used as a guide for vector-level interven- **142** tion on the representation space. This is the class of **143** interventions we are concerned with here: in partic- **144** ular, when the interventions are vector *projections* **145** guided by the learned probes which are indicative **146** of a given auxiliary feature. **147**

The exact nature of this intervention is inter- **148** changeable. We consider two in particular: the *am-* **149** *nesic* intervention introduced in [Elazar et al.](#page-8-4) [\(2020\)](#page-8-4) 150 (described further in section [2.2\)](#page-2-0) and our *mnes-* **151** *tic* variation of the same INLP techniques (section **152** [2.3\)](#page-2-1). **153**

2.1 What Should it Tell Us? **154**

The interventional probing steps are performed on **155** exactly the representation that would have been an **156** input to the classifier head f . We may re-insert the 157 intervened representations and re-calculate the clas- **158** sifier accuracy (note that the iterative projections **159**

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$$

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\frac{191}{100}
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160 in sections [2.2](#page-2-0) and [2.3](#page-2-1) maintain the original dimen-**161** sionality of the vector set but reduce the *rank*).

 We are looking to see if the downstream perfor- mance of the classifier f drops. If it does, the inter- ventions have removed information that was neces- sary for successful classification. However, as any projection would remove some information, these results must be viewed in the context of a control intervention: if the INLP process ends up removing **n** directions, a sample of *n* randomly chosen direc- tions is selected from the original representation, [Elazar et al.](#page-8-4) [\(2020\)](#page-8-4) argue that if the amnesic down- stream performance drops significantly more than the random removal control performance, we may conclude that the features were necessary for the final downstream classification. On the other hand, if the performance does not drop at all, the features were not useful for the classifier in the first place. In the ensuing sections and results, we demonstrate that this is not necessarily a valid conclusion.

180 2.2 The Amnesic Intervention

We follow the procedure in [\(Elazar et al.,](#page-8-4) [2020\)](#page-8-4) (in turn based on *iterative nullspace projection* [\(Ravfogel et al.,](#page-8-6) [2020\)](#page-8-6)): given a set X of encoded representations for the textual input (with dimensions num_examples \times embedding_dimension), we iteratively train linear SVM classifiers according to a set of auxiliary feature labels. For each INLP step i , This yields a linear transformation $W_iX + B$, where the vectors of W_i define directions onto which the probe projects the representations for auxiliary label classification (i.e., these are the chosen directions most aligned with auxiliary class separation). For each step i , an orthogonal basis denoted R_i is found for this rowspace. The projection to the intersection of the nullspaces is given by a matrix

$$
PX = (I - (R_0 + \dots + R_n))X.
$$

181 The matrix product PX is a matrix in the original dimensions of X, but with reduced rank by the number of iteration steps (as each projection "flat-tens out" the representation in these directions).

 Projection to the intersection of nullspaces is thus the removal of any information pertaining to the auxiliary feature labels (or at least, the infor- mation which allows high performance for a linear probe). The training terminates these auxiliary task classifiers start consistently performing at the ma- jority class baseline, indicating that there is no fur-ther linearly information to be extracted from the

remaining representation. As such, the resulting **193** representation is treated as an altered representation **194** where this feature is *removed* or forgotten. **195**

2.3 A Variation: The Mnestic Intervention **196**

[Elazar et al.](#page-8-4) [\(2020\)](#page-8-4) perform a series of experi- **197** ments on various linguistic features which had pre- **198** viously been shown to be well-captured in language **199** model representations and use the amnesic prob- **200** ing methodology to distinguish between features **201** that are *used* by the model and those that are not **202** by comparing post-intervention downstream task **203** performance to a baseline of randomly removed **204** directions. 205

Rather than projecting the embedded representa- **206** tions to the intersection of nullspaces of the trained **207** probes (removing the target property), we project **208** them to the *union of the rowspaces* with the trans- **209** formation: **210**

$$
(I - P)X = (I - (I - (R_0 + ... + R_n)))X
$$

= (R_0 + ... + R_n)X 212

This has the opposite effect: we use projection to **213** null out *everything except* the directions identified **214** by the probes as indicative of the target feature. As **215** such, we "remember" only that feature rather than **216** forgetting it. **217**

3 Experimental Setup **²¹⁸**

In this study, we use interventional methods $\frac{1}{1}$ $\frac{1}{1}$ $\frac{1}{1}$ to study the internal behaviour of NLI models. **220** We compare amnesic and mnestic variations of **221** the INLP strategy, evaluating intermediate feature **222** probing performance and downstream NLI perfor- **223** mance after every step of the intervention process. 224

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For each auxiliary feature label and and model, **225** we perform the *interventional probing* as outlined **226** in figure [1.](#page-1-0) **227**

3.1 Dataset **228**

Our setting for this study is a fragment of NLI **229** called *Natural Logic* [\(MacCartney and Manning,](#page-8-7) **230** [2007\)](#page-8-7). In particular, we focus on single-step nat- **231** ural logic inferences in which entailment exam- **232** ples are generated by replacing a noun phrase in a **233** sentence with a hyponym, hypernym or unrelated **234** noun phrase. The context of the substituted term **235**

¹We reuse much of the code included with [\(Elazar et al.,](#page-8-4) [2020\)](#page-8-4), but we include our data and reproducible experimental code in *anonymized github repo*.

 is either *upward* or *downward* monotone, as de- termined by the composition of negation markers, generalized quantifiers or determiners present in the context. The entailment label of the example is a consequence of this feature and the lexical relation between the substituted terms.

 We use the NLI_XY dataset from [\(Rozanova](#page-8-8) [et al.,](#page-8-8) [2021b,](#page-8-8)[a\)](#page-8-9). By construction, the NLI_XY dataset consists of NLI examples which rely on exactly these two abstract features: context mono- tonicity and the lexical relation of the substituted **247** terms.

248 We perform two flavours of probe-based inter-**249** ventions (described fully in section [2\)](#page-1-1) with four **250** feature label sets (described next).

 Auxiliary Feature Labels We begin with the two relevant intermediate features (respectively, con- text monotonicity and lexical relation) which are already known to correlate with stronger perfor- [m](#page-8-8)ance on the downstream NLI_XY task [\(Rozanova](#page-8-8) [et al.,](#page-8-8) [2021b\)](#page-8-8). We will refer to this as *single-feature* interventional probing, as the probing and inter- vention steps are only applied to one feature set at a time. Next, we combine the two features in a cross product, creating a new feature label set with all possible combinations of these interme- diate features (in the dataset, they are completely [i](#page-8-9)ndependent variables by construction [\(Rozanova](#page-8-9) [et al.,](#page-8-9) [2021a\)](#page-8-9)). We refer to this as the *composite feature label*.

 Lastly, we also consider the *entailment label* itself (the downstream task label) as an input to the interventional probing process. The latter is particularly useful as a diagnostic sanity check, and aids the critical nature of our findings.

271 3.2 NLI Models and Encoding

 We compare a selection of BERT [\(Devlin et al.,](#page-7-0) [2019\)](#page-7-0) and RoBERTa [\(Liu et al.,](#page-8-10) [2019\)](#page-8-10) models trained for NLI classification. Firstly, we include a pair of models trained respectively on the MNLI [\(Williams et al.,](#page-8-11) [2018\)](#page-8-11) and SNLI [\(Bowman et al.,](#page-7-1) [2015\)](#page-7-1) benchmark datasets. In [\(Rozanova et al.,](#page-8-8) [2021b\)](#page-8-8) and [\(Rozanova et al.,](#page-8-9) [2021a\)](#page-8-9), it is shown that when roberta-large-mnli (a model which performs well on benchmarks but poorly 280 on the targeted NLI_XY challenge set) receives **281** additional training on the adversarial HELP dataset **282** [\(Yanaka et al.,](#page-8-12) [2019\)](#page-8-12) it improves in NLI_XY **283** performance and *begins to show high probing* **284** *performance for the relevant intermediate features*, **285** context monotonicity and lexical relations: this is **286** the necessary precondition for doing interventional **287** probing. We include two of their models with this **288** property: roberta-large-mnli-help and **²⁸⁹** roberta-large-mnli-double-finetuning, **²⁹⁰** with the other models included for a contextual 291 comparison. **292**

We perform probing and intervention on the final **293** representation that precedes the NLI classification **294** head: in the case of BERT and RoBERTa, this is **295** the [CLS] token of the final layer. **²⁹⁶**

The initial input is a tokenized NLI exam- **297** ple from the NLI_XY dataset. The findings in **298** [\(Rozanova et al.,](#page-8-8) [2021b\)](#page-8-8) show that the intermedi- **299** ate feature labels (context monotonicity and lexical **300** relations) are detectable in the concatenated tokens **301** of the substituted noun phrases: however, for in- **302** terventional purposes, we perform the probing and **303** intervention steps on the [CLS] token which serves 304 as an input to the NLI classifier head: we have **305** found that the same features are detectable to a **306** comparable standard, and this is the only position **307** at which we are able to make a sensible interven- **308** tion that would allow conclusions about the final **309** classifier head only. **310**

3.3 Evaluation **311**

The significant metrics for these interventional **312** probing paradims are the *probing accuracy* before **313** and after the iterative nullspace projection steps (a **314** decline to random performance indicates the fea- **315** ture is being "removed" from the representation in **316** the sense that it is no longer detectable by linear **317** probes) and the *downstream classification accu-* **318** *racy* on the NLI task the model's were trained for **319** (in our case, we report the accuracy on the NLI_XY **320** task). **321**

For amnesic probing, we report the performance **322** deltas for both the probing and downstream tasks. **323** However, for mnestic probing, a slightly more nu- **324** anced and qualitative view is helpful: it can be **325** assumed that eventually mnestic probing will reach **326** comparable performance to the untouched vector **327** representations, but we are interested in the com- **328** parative rates at which this happens. As the inter- **329**

Table 1: Amnesic probing performance deltas across models and target feature labels: first listed is the performance on the probing task with respect to the indicated feature, and then the accuracy on the downstream NLI-XY task. We note the results pre-intervention and the ensuing change in accuracy.

 ventions are iterative, we may feed the intervened representations into the classifier head at *each step* of the intervention process - we use this to provide a step-wise presentation of results in linear plots in figure [3.](#page-5-0)

 While the tabulated deltas in table [1](#page-4-1) results are sufficient to present our observations on amnesic probing, for comparison we also include the step-wise graphical presentations in the appendix.

³³⁹ 4 Results and Discussion

340 4.1 Single Feature Amnesic Probing

 The results for the standard amnesic probing pro- cedure are in table [1.](#page-4-1) In particular, the single fea- ture results are in the rows with features labelled *insertion relation* and *context monotonicity*. The amnesic operation is successful - the respective probing accuracies approach and reach the majority class baseline. The length of this iterative process is indicative of the number of dimensions removed to reach this baseline: it can also be considered a proxy for the strength of the feature presence in the representations, or rather, the dimension of the semantic subspace corresponding to the target features.

354 The second phase of this process, i.e. the resub-

stitution of the modified representations as inputs **355** to the NLI classifier head, can be seen in the right **356** hand portion of table [1,](#page-4-1) labelled *NLI-XY Perfor-* **357** *mance*. The result is unexpected: for each of these **358** features, *the downstream task performance appears* **359** *to be unaffected after their removal.* This is surpris- **360** ing when the dataset is explicitly controlled to rely 361 only on these two features. **362**

4.2 Multi Feature Amnesic Probing **363**

The results for the amnesic probing procedure uti- **364** lizing *both* auxiliary feature label sets and the en- **365** tailment gold label are in the rows of table [1](#page-4-1) with **366** labels *composite* and *entailment label* respectively. **367** We observe that once again, the downstream task **368** performance is mostly unaffected. Unlike the un- **369** expected result in the previous section, it's difficult **370** to argue away the fact that this is somewhat con- **371** tradictory: while single feature removal may be **372** subject to some confounding bias, the removal of 373 both features exhausts the variables on which this **374** classification depends. This is highly unexpected, **375** and suggests a point of failure for the amnesic prob- **376** ing process. Naturally, we cannot be without doubt **377** that despite all our best efforts to work with a con- **378** trolled dataset that relies only on these two know **379** (but still complex) features, a model may yet find **380**

Figure 3: Downstream Task Performance After Mnestic Intervention

 unrelated heuristics to exploit that may correlate so strongly with the downstream task label that it may perform well without representing and using these intermediate features. However, we imagine this to be a rather low probability scenario to be that the model simultaneously learns such heuris- tics but simultaneously learn representations that create strong clusters for the known intermediate features *without using them at all*. The models which we have observed to perform more less well on NLI-XY (such as roberta-large-mnli) are indeed estimated to be using sub-par heuristics, but this also comes with poor probing results for the inter- mediate features - naturally, this in itself does not imply anything conclusive, but certainly adds to our convictions.

 On a seprate note, it is noted in [Elazar et al.](#page-8-4) [\(2020\)](#page-8-4) that there is no control for the number of dimensions removed, while there is a clear correla- tion between downstream task performance and the number of label classes (and thus removed probe directions) are in play. Our feature sets have only 2 and 3 classes respectively. In the most analagous result in [\(Elazar et al.,](#page-8-4) [2020\)](#page-8-4) where the auxiliary

features had very few classes and no change on **405** the downstream performance was observed, it was **406** concluded that the features must have no effect on **407** the outcome. It is very likely that *too little informa-* **408** *tion* is being removed in this process to observe any **409** impact on the downstream task performance. This **410** could potentially be pointing to high redundancy in **411** the representations which the amnesic intervention **412** may struggle to remove appropriately. **413**

4.3 Mnestic Probing 414 414

Given the possible dimensionality problem, the al- 415 ternative method of *mnestic* probing seems promis- **416** ing: many dimensions are removed and few remain, **417** so it appears to be a ripe setting for observing and **418** comparing effects on downstream NLI accuracy. **419** The results for the *mnestic* probing procedure are **420** in figure [3.](#page-5-0) There is a clear increase in NLI perfor- **421** mance with subsequent addition of probe-chosen 422 directions to the representations, but these results **423** especially need to be viewed in the context of sec- **424** tion [4.4,](#page-6-0) where we compare the performance to **425** random choices of included directions. **426**

We observe that the *composite* label and the gold **427**

 entailment label are reflected as expected in the mnestic probing experiments: the inclusion of the probe-selected dimensions with respect to these la- bels introduces a sharp and immediate increase in the NLI classifier performance. This is significantly steeper than the baseline increase observed in ran- dom addition of representation directions. Simi- larly, the increase is nearly as sharp for the lexical relation label. However, although an increase is observed during the iterative mnestic probing in- tervention for context montonicity, this increase is not at a dramatically higher rate than adding subsequently more directions from the original rep- resentation. For monotonicity specifically, this is not enough to conclude that the feature (or at least, the corresponding probe-selected dimensions) are critical to the final classifier.

445 Nevertheless, we have been able to make clearer **446** observations than were possible in the amnesic **447** probing setting.

448 4.4 Control Comparison

Figure 5: Amnesic control experiment: Downstream NLI accuracy upon the *removal* of n random directions of the original representation.

 We contextualise all the preceding results with a set of control experiments both for amnesic (figure [5\)](#page-6-1) and mnestic (figure [6\)](#page-6-2) probing. Note in partic- ular that even with very few random dimensions kept, downstream performance starts approaching comparable levels to the full representations. As such, a single random baseline as in [Elazar et al.](#page-8-4) [\(2020\)](#page-8-4) can be misleading: there is enough variabil- ity in the random direction results so as to allow for a false claim of feature irrelevance by simply getting lucky; as few as 3 dimensions can perform at the original model's performance level or arbi-trarily lower.

Figure 6: Mnestic control experiment: Downstream NLI accuracy upon the *selection* of n random directions of the original representation.

Lastly, we compare to the mnestic probing re- **462** sults in figure [3:](#page-5-0) with the probe-selected mnestic 463 dimension choices, the increase in downstream per- 464 formance does seem to happen faster and in a more **465** consistent fashion, while the selection of n ran- 466 domly chosen directions introduces very haphaz- **467** ard performance spikes. This suggests the probe- **468** selected dimensions are consistently adding to the **469** model's access to the relevant information, amd **470** this may be stronger evidence for the usefulness of **471** the examined features for the final classification. **472**

5 Related Work **⁴⁷³**

The use of probing as an interpretability strategy 474 dates back as far as works such as [Alain and Bengio](#page-7-2) **475** [\(2018\)](#page-7-2) and [\(Conneau et al.,](#page-7-3) [2018\)](#page-7-3), but a core set of **476** work on the detailed development of the method- **477** [o](#page-7-4)logy includes [Hewitt and Liang](#page-8-13) [\(2019\)](#page-8-13); [Belinkov](#page-7-4) **478** [and Glass](#page-7-4) [\(2019\)](#page-7-4); [Voita and Titov](#page-8-1) [\(2020\)](#page-8-1); [Pimentel](#page-8-0) **479** [et al.](#page-8-0) [\(2020\)](#page-8-0). For a full survey, see [Belinkov](#page-7-5) [\(2022\)](#page-7-5). **480**

The application of probing strategies to natural **481** [l](#page-8-8)ogic components has been explored in [Rozanova](#page-8-8) **482** [et al.](#page-8-8) [\(2021b\)](#page-8-8) and [Geiger et al.](#page-8-14) [\(2020\)](#page-8-14). In [Rozanova](#page-8-8) **483** [et al.](#page-8-8) [\(2021b\)](#page-8-8), probing experiments have proven **484** effective in detecting the presence or absence of **485** features such as *context monotonicity* and *phrase-* **486** *pair relations* in the internal representations of NLI **487** models. **488**

Regarding interventions as interpretability tools **489** for machine learning classifiers, there are two broad **490** categories: those that modify the raw input (such **491** as image or text) in a controlled way, and those that **492** modify the hidden/latent vector representations of **493** the data at various stages of the models' input pro- **494** cessing. While input-level interventions are more **495** common as they are usually easier to control and **496**

	Intervention	Tested Effect	Feature Characterisation	Requires Intermediate Labels	Intervention Linked to Concept Interpretation	Domain
Amnesic Probing / INLP (Elazar et al., 2020)	Debiasing / Feature Removal	Downstream Classifier Accuracy	Linear Classifier	Yes	No	Language Modelling
CausaLM: Causal Model Explanation (Feder et al., 2021) Through Counterfactual Language Models	Re-Training Model Copy For Counterfactual Representation	Text representation-based individual treatment effect (TReITE)	Retrained Base Model	Yes	Yes	Sentiment Analysis
Causal Concept Effect	Generative Modeling	Average Causal Effect Measure	VAE	Yes	Yes	Vision Classification
Concept Activation Vectors (TCAV) (Kim et al., 2018)	Value Shift in Vector Direction	Custom Gradient Sensitivity Measure	Linear Classifier	Yes	Yes	Vision Classification
Latent Space Explanation by Intervention	VAE Input Discretization and Reconstruction	Reconstruction Quality	VAE	No	Qualitative Judgement (Vision Only)	Vision Classification
Meaningfully Explaining Model Mistakes Using Conceptual Counterfactuals	Weighted Combination of Concept Vectors	Difference Between Concept Addition and Removal Effect	Linear Classifier	Yes	Yes	Vision Classification

Table 2: Related Work on Latent Concept Interventions

 are strongly interpretable, they don't allow us to explore and conjecture about exact high-level rep- resentational mechanisms in the latent space. We tabulate a few relevant interventional interpretabil- ity methods in table [2.](#page-7-6) Note in particular the varia- tion in the *generation* step for the intervened input; some use generative modelling for counterfactual examples, while we use cheaper linear probes.

 The only other work in which interventional methods have been applied to natural logic is [Geiger et al.](#page-8-5) [\(2021\)](#page-8-5): a similar problem setting is considered, but at a finer granularity. Our work focuses more on the summarised abstract notion of context monotonicity as a single feature, rather than the intermediate tree nodes that determine its final monotonicity profile. The interventions used in this work are vector *interchange* interventions; partial representations from transformed inputs are used, as opposed to direct manipulations of the encoded vectors.

⁵¹⁷ 6 Conclusion and Future Work

 Our expiremental setting has shown significant lim- itations of amnesic probing in high-dimensional settings where there are few label classes (and con- sequently fewer dimension modified), even if these classes are strongly detectable. Our results point out that it is misguided to concluded that a given feature is not used when post-amnesic-intervention downstream performance fails to drop, especially in our example amnesic probing studies of a) the gold donwstream feature label and b) the compos- ite of two labels that jointly determine the entail- ment label. This may be due to a dimension/rank confounder variable and high redundancy of in- formation in the representations. It remains to be checked whether high performance in the random control directions corresponds to strong alignment with these probe-selected directions: we propose an analysis of the *dot products* with the fixed set of probe-selected dimensions, which indicates a shared directionality measure (0 for orthogonal vec-tors and 1 for codirectional ones).

We have introduced a modification of the am- **539** nesic probing paradigm which we call *mnestic* prob- **540** ing which uses the same INLP process but consid- **541** ers the opposite intervention: using the union of **542** projection rowspaces to keep *only* the directions the **543** probes have identified to be modelling the target **544** information. This strategy presents results that are **545** more aligned with theoretical expectations, possi- **546** bly because we are now able to make comparisons **547** in a lower rank setting and also work with more **548** useful control baselines. **549**

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A Expended Amnesic Intervention **⁶⁸⁰** Results **⁶⁸¹**

(a) Lexical Relation Probing Performance During Iterative Amnesic Intervention Process

(c) Context Monotonicity Probing Performance During Iterative Amnesic Intervention Process

Downstream Task (NLI) Accuracy

 0.6 $_{0.4}$ $\overline{0}$. Step $\sqrt{2}$ \bar{z} 10 15 $_{20}$ 25 30

(b) Downstream Performance On NLI_XY After Amnesic Intervention (Removing Lexical Relation Information)

(d) Downstream Performance On NLI_XY After Amnesic Intervention (Removing Context Monotonicity Information)

(a) Probing Performance On NLI_XY After Composite Label Amnesic Intervention

(b) Downstream Performance On NLI_XY After Composite Label Amnesic Intervention

Figure 8: Composite Feature Label Amnesic Probing

 0.2

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 $\mathbf{0}$

Probing Accuracy

(a) Probing Performance On NLI_XY After Entailment Label Amnesic Intervention

 40

60

 20

(b) Downstream Performance On NLI_XY After Entailment Label Amnesic Intervention

Figure 9: Sanity Check: Entailment Gold Label Amnesic Probing

Step

80