MASIMU: MULTI-AGENT SPEEDY AND INTER-PRETABLE MACHINE UNLEARNING

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Abstract

The regulatory landscape around the use of personal data to train AI/ML models is rapidly evolving to protect privacy of sensitive information like user locations or medical data and improve AI trustworthiness. Practitioners must now provide the capability to "unlearn" or "forget" data—the forget set—that was used to train an AI model, without triggering a full model re-train on the remaining data—the *retain set* to be computationally efficient. Existing unlearning approaches train via some combination of fine-tuning pre-trained AI models solely on the retain set, pruning model weights then unlearning, and model-sparsification-assisted unlearning. In our research paper, we use deep learning (DL), multi-agent reinforcement learning (MARL) and explainable AI (XAI) methods to formulate a faster, more robust and interpretable unlearning method than past works. Our method, multi-agent speedy and interpretable machine unlearning (MASIMU), fine-tunes a pre-trained model on the retain set, interpretably re-weighting the gradients of the fine-tuned loss function by computing the similarity influences of the *forget set* on the batched *retain set* based on weights generated by an XAI method. We add a MARL framework on top to address the challenge of high dimensional training spaces by having multiple agents learning to communicate positional beliefs and navigate in image environments. The per-agent observation spaces have lower dimensions, leading to the agents focusing on unlearning interpretable gradients of important superpixels that influence the target labels in the learning criteria. We provide extensive experiments on four datasets—CIFAR-10, MNIST, high resolution satellite images in RESISC-45, skin cancer images in HAM-10000 to unlearn for preserving medical privacy—computing robustness, interpretability, and speed relative to the dimensionality of the training features, and find that MASIMU outcompetes other unlearning methods.

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1 INTRODUCTION

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The large-scale adoption of Machine Learning models has led to emergence of legal opportunities where certain users would like their data to be forgotten in the training set of Artificial Intelligence (AI) models, as protected by the Right to be Forgotten (Chenou & Radu, 2019), granted by the 040 European Union to its residents. US residents are covered by medical privacy protection under the 041 HIPAA Federal Law (Ness et al., 2007) which is helpful to protect sensitive medical data like lung 042 cancer images (Bandyopadhyay et al., 2021) to train AI models for cancer prediction. This helps to 043 improve the trustworthiness of AI models. AI models will often have to follow copyright laws and 044 regulations (Grynbaum & Mac, 2023) which can lead to the models forgetting a part of the training dataset that is subject to these copyright laws. Machine unlearning applications include lifelong learning (Liu et al., 2022), toxicity mitigation in Large Language Models (Lu et al., 2022) along 046 with Reinforcement Learning applications (Nikishin et al., 2022; Ye et al., 2023; Guo et al., 2023). 047

The goal of Machine Unlearning is to effectively forget the influence of a portion of the training data, the *forget set*, on an AI model satisfying a specific objective like classification while retaining similar or better performance like the original AI model. Retraining the model from scratch on the held-out training data without including the *forget set*, called the *retain set*, takes a long time which may not be practically sustainable for AI models trained on big datasets that require high computational costs like many GPUs for training. The NeurIPS 2023 Machine Unlearning competition (Eleni Triantafillou, 2023) put forth machine unlearning evaluation criteria like unlearning taking

much less time than retraining and measuring similar performance of the unlearnt model to the orig-055 inal model. Another metric is success against Membership Inference Attacks (MIAs) to discern 056 examples in the *forget set* from those in the *test set*. Existing research works perform unlearning 057 mostly by fine-tuning pre-trained AI models on the retain set which poses the inherent challenge 058 of not considering the influence of the *forget set* on the *retain set*. Latest unlearning research by pruning model weights then unlearning and with model sparsification assisted unlearning (Jia et al., 2023) improves on multi-criteria performance unlearning for a few datasets like CIFAR-10. Other 060 unlearning related works are shared in Appendix A.1. Existing unlearning research poses signif-061 icant challenges like robustness, lack of interpretability. They also do not address the unlearning 062 problem with increasing dimensionality of training feature spaces in high-resolution images having 063 significant amounts of information, not related to the learning objective. 064

We propose a baseline Machine Unlearning (MU) Framework for image classification, fine-tuning 065 a pre-trained model on the retain set. For our Interpretable Machine Unlearning (IMU) Framework, 066 we compute the *forget set* influence on the *retain set* by interpretably re-weighting the gradients of 067 the fine-tuned loss function using similarity scores of XAI weights on the batched retain set and 068 the forget set. XAI weights from Local Interpretable Model-Agnostic Explanations (LIME) method 069 (Ribeiro et al., 2016), for both the retain set and the forget set, are generated faster compared to other XAI methods like SHAP scores (Lundberg & Lee, 2017) making it lucrative to be a component of 071 our Machine Unlearning paradigm. The underlying behavior of the LIME XAI method (Garreau 072 & Mardaoui, 2021a), like selecting local examples, identifying features and calculating weights 073 per feature, motivate our approach for using interpretable gradients to address machine unlearning, 074 including the use of cosine similarity and average feature weights for each label.

075 We formulate a Multi-agent Speedy gated recurrent unit (GRU) based Machine Unlearning 076 (MASMU) framework with agents communicating their pose beliefs. We compare its unlearning 077 speed with the Multi-Agent long-short term memory (LSTM) based Unlearning (MALMU). Past 078 work, using multiple agents to classify images (Mousavi et al., 2019a), compute a spatial state 079 positioned on each image which agents communicate to update local beliefs and policies. We combine MASMU with IMU to a Multi-Agent Speedy GRU based Interpretable Machine Unlearn-081 ing (MASIMU) framework comparing it with its corresponding LSTM framework of Multi-Agent LSTM based Interpretable Machine Unlearning (MASIMU) to address the challenge of higher dimensionality for high-resolution training image features, needed to train more accurate models e.g. 083 improving lung cancer detection (Daneshpajooh et al., 2021). The per-agent observation spaces 084 in the MASIMU framework is small, helping to unlearn gradients of important superpixels faster 085 that influence the probability distribution of prediction vectors in the learning criteria. We show our interpretable and robust results on the CIFAR-10, MNIST, and high resolution imagery from 087 satellites (RESISC-45 (Cheng et al., 2017a)) and skin cancer (HAM-10000 (Tschandl et al., 2018)) 088 data, showing improved unlearning performance with faster unlearning specially with more dimen-089 sionality on high resolution training image features using multiple agents. Our Machine Unlearning evaluation metrics (Nguyen et al., 2022) include completeness (closeness to the original model), 091 and timeliness (time cost of unlearning as opposed to retraining). Our IMU, MASMU, MALMU, 092 MASIMU and MALIMU unlearning frameworks are novel for high resolution image classification tasks.

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2 RETAIN AND FORGET DATASETS

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In machine unlearning, the forget dataset D_f consists of a set of data items within the training dataset D_{tr} for an AI model M for which the influence of the data items in the *forget set* must be removed ("or unlearnt") from M without full retraining on the remaining training data items, defined as the retain dataset D_r . Fully retraining M on D_r is computationally expensive for deep learning models. A major challenge in Machine Unlearning is to learn the influence of the *forget set* on the *retain set* and to efficiently remove them from the pre-trained AI model. In our proposed MASIMU framework, we compute the influence of *forget set* and *retain set* and efficiently unlearn the influence on the pre-trained model.

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We experiment on the CIFAR-10 dataset (Krizhevsky et al., 2009) with 32 × 32 color images having
 10 labels like vehicles and animals. We also consider the MNIST dataset (Deng, 2012) with 28 × 28 gray-scale images of digits from 0 to 9 and their corresponding 10 labels. Finally, we unlearn AI

models on high resolution 256×256 satellite imagery in the RESISC-45 dataset (Cheng et al., 2017b) with 45 labels like mountains, houses and 450×450 skin-cancer images in the HAM-10000 dataset (Tschandl et al., 2018) with 7 labels including melanoma and melanocytic nevi, investigating unlearning of sensitive data like locations and medical records. Our train/test and the retain/forget data splits for all the datasets are provided in Table 3.

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3 INTERPRETABLE MACHINE UNLEARNING

116 Feature-based XAI methods like Locally Interpretable Model-agnostic Explanations (LIME) 117 (Ribeiro et al., 2016) are useful to explain the influence of training features on the output of an 118 AI model, post training. LIME works by taking examples and constructing an interpretable approx-119 imate linear model around which samples are taken. For each training feature, LIME calculates n120 weights in the following manner, where n is the number of local samples used to generate the ex-121 planation as in Equation 1. LIME outputs on RESISC-45 in Figure 1 and HAM-10000 in Figure 2 122 show segmented superpixels on interpretable LIME masks which helps to identify similar retain and forget images. 123

$$w_i = e^{\frac{1}{2b^2} cosdist(\mathbf{1}, x_i)^2} \quad \forall i \le n \tag{1}$$

Here, b is a bandwidth parameter, x_i is a local sample selected by LIME, and cosdist is the cosine distance between 2 vectors. LIME coefficients segment an image to super-pixels that can help in improving the unlearning efficiency by calculating their influence on the learning criteria.

129 For our baseline Machine Unlearning Framework (MU), we fine-tune the pre-trained training model 130 on the *retain set* only, which poses the problem of not computing the influence of the *forget set* 131 on the retain set. We define our Interpretable Machine Unlearning Framework (IMU) Algorithm weighing the influence of the LIME coefficients of the *forget set* on the batched *retain set* during fine-132 tuning and removing the influence of these interpretable LIME weights on the computed gradients 133 of the super-pixels in our *retain set*. This is based on the intuition that LIME coefficient outputs are 134 similar to the sum of the integrated gradients of the training input superpixels for AI models that are 135 sufficient smooth in comparison to their training datasets (Garreau & Mardaoui, 2021b). 136

We calculate the LIME coefficient weights for each superpixel in each image and average them over 137 each label. Then we use the pcs function defined in the IMU Algorithm to compute pair-wise cosine 138 similarity of LIME weight of every batched image in the *retain set* for batches b with the LIME 139 weights of all f forget set images. This leads to a $b \times f$ cosine similarity matrix. We average along the 140 rows for non-zero cosine similarity values to only compute rsim the influence of forget set images 141 which are more similar with *retain set* images. Then we average the similarity weightage of all the 142 batched retain images in crsim which is our interpretable weight I_w highlighting the importance 143 of the training superpixels generated by LIME. During the backpropagation of the loss function, 144 when gradients of the loss function are computed, we update the gradients with this interpretable 145 weight and remove their influence from the original gradients by subtraction. The computation 146 of cosine similarity on the interpretable approximately linear LIME coefficient weights, is helpful 147 to ensure the differentiability of the gradients of the loss function. For the unlearning problem of image classification models, we use the widely used multi-class classification loss function of Cross 148 Entropy Loss in Equation 2. There, x is a given example, n is the number of classes, y_i is the truth 149 label, and $p_i(x) = \frac{e^{x_i}}{\sum_{j=1}^n e^{x_j}}$ is the softmax probability of x being class i. 150

 $L_{CE}(x) = -\sum_{i=1}^{n} y_i \log p_i(x)$ (2)

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4 MULTI-AGENT INTERPRETABLE MACHINE UNLEARNING

A Multi-Agent (MA) Machine Unlearning (MAMU) framework has been devised in Algorithm 1
where multiple agents traverse a limited observation space based on learning the underlying belief
and decision Recurrent Neural Networks (RNN) (Rumelhart et al., 1986). The RNN can be configured as either a Long Short-Term Memory (LSTM) (Hochreiter & Schmidhuber, 1997) or a Gated
Recurrent Unit (GRU) (Chung et al., 2014) in the MALMU (Multi-Agent LSTM based Machine
Unlearning) framework or the MASMU (Multi-Agent Speedy GRU based Machine Unlearning)

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with its LIME coefficient vector and that of the original image having the highest cosine similarity (g) Lakes Image from RESISC-45 forget set with its LIME coefficient vector and that of the original 188 image having the lowest cosine similarity. 189

191 framework. We use the RNN to represent belief that is propagated across the agents per step with 192 the incentive of speeding up image unlearning using MA-REINFORCE algorithm. For unlearning, 193 we load the model trained with MA-REINFORCE algorithm on the entire dataset and fine-tune it 194 using the retain set with MA-REINFORCE to unlearn the forget set images. This MA framework 195 can improve unlearning for high resolution images, e.g. RESISC-45 satellite images, reducing the 196 dimensionality with less observation dimensions per agent. MALMU and MASMU are inspired 197 by the training of MARL algorithms (Mousavi et al., 2019b) using LSTM RNNs classifying high resolution images. 199

We model our MAMU frameworks, MALMU and MASMU, as Partially Observable Markov De-200 cision Processes (POMDPs). For an agent classifying an image I, the state consists of the position 201 of the center of the agent on I, as well as the history of the belief RNN and the decision RNN. 202 When GRUs are used to compute the beliefs, only a hidden state is updated. Actions available to the 203 agent are to move the position a pixel up, down, left or right. This is constrained by the requirement 204 that the agent's observation window fits entirely within I. Using a window size reduces the dimen-205 sionality of the observation space when supplied with high-resolution images like in RESISC-45 206 or HAM-10000. Transitions come from policy function π conditioned on the hidden cell state of 207 the decision RNN in the case of updates to the spatial state (position), and from the output of a parameterized function supplied with the previous state and information input in the case of the be-208 lief and decision RNNs. Differentiable rewards across classification model network parameters are 209 calculated by taking the difference of a random loss and cross entropy loss at each step. A detailed 210 mathematical discussion on computing LSTM and GRU based belief RNNs along with correspond-211 ing decision RNNs to sample actions based on the policy gradients of MA-REINFORCE algorithm 212 has been shared in the Appendix A.4. 213

For an image I with ground truth label $i \in \{1 \dots M\}$, to incentive speedy unlearning, rewards for 214 a particular trajectory with positive probability τ are calculated by grouping the various parameters 215 in our algorithm into one single parameter Θ . The differentiable reward across network parameters



Figure 2: (a) (Melanoma Image from HAM-10000 *retain set* (d) A Melanoma Image from HAM-10000 *forget set* for which its LIME coefficient vector and that of the original image has the highest cosine similarity (g) Melanocytic Nevi Image from HAM-10000 *forget set* for which its LIME coefficient vector and that of the original image has the lowest cosine similarity.

 r_{τ} is computed in Equation 3 to follow the aggregate prediction of the agents where e_i is the unit vector along the ground truth's direction.

$$r_{\tau} = -L(\bar{p} - e_i) \tag{3}$$

Our multi-agent learning paradigms use a LSTM RNN in MALMU similar to the same MA-REINFORCE approach as (Mousavi et al., 2019a) with also while using a GRU RNN in MASMU. For MALIMU and MASIMU, we update the parametric gradients of the loss function, used to compute the differentiable rewards for MA-REINFORCE algorithm, by subtracting, thereby removing the interpretable weight of similar super-pixels in the retain set and the forget set which is computed using LIME interpretable AI method as shown in Algorithm 2. Our goal is to adjust the parameters of our system Θ in such a way that we maximize the objective function in Equation 4.

$$J(\Theta) = \mathbb{E}_{\tau \in \mathcal{T}}[r_{\tau}] \tag{4}$$

T is the set of possible trajectories for our agents. The original REINFORCE algorithm (Sutton et al., 2000), extended to MA-REINFORCE, computes gradients of the objective function in Equation 5.

$$\nabla J(\Theta) = \mathbb{E}[\sum_{\tau \in \mathcal{T}} \nabla(\log p_{\tau})r_{\tau} + \nabla r_{\tau}]$$
(5)

which can be approximated with an unbiased estimator for J, obtained by sampling N trajectories:

$$\hat{J}(\Theta) = \frac{1}{N} \sum_{i=1}^{N} (\log p_{\tau_i}) r_{\tau_i}^d + r_{\tau_i} \implies \mathbb{E}[\nabla \hat{J}(\Theta)] = \nabla J(\Theta)$$
(6)

2/11:Input: retain data D_r of size r , pre-trained model M 272:Training Parameters: epochs e_r , batches on retain data b_r loss function L_f , optimizer O , batch2743:Initialize $M_u = M$ 2754:for $i = 1$ to e do2765:for $j = 1$ to b do2776:for $k = 1$ to g do2787:for $v = 1$ to N do2798:Initialize $s_v(0)$ on a random pixel in image I_k 2809:Initialize $s_v(0) = 0$, $c_w(0) = 0$ 28110:for $w = 1$ to $ N_v $ do28211: $m_w(0) = 0$ 28312:end for284for $t = 0$ to $T - 1$ do285for $v = 1$ to N do28613:end for28113:end for283for $t = 0$ to $T - 1$ do284for $t = 0$ to $T - 1$ do285for $v = 1$ to N do286for $v = 1$ to N do286for $t = 0$ to $T - 1$ do287for $v = 1$ to N do288Get fature extraction $b_v(t) = b_{a_v}(v_v(t))$ 289For minformation input $u_v(t) = b_{a_v}(v_v(t))$ 291Calculate aggregate message $\overline{d}_v(t) = \frac{1}{n:deg(v)} \sum_{n=1}^{N-1} d_n(t)$ 292For minformation input $u_v(t) = mo_{a_v}(s_v(t))$ 293Run decision RNN using $u_v(t)$ as input294294Update policy π on $\pi_{a_v}(\cdot, h_v(t+1))$ 295Get action $a_v(t + 1)$ from π 206Go to new spatial state $s_v(t + 1)$ er	270	Alg	porithm 1 Multi-Agent Machine Unlearning (MAMU) (for both MALMU and MASMU)
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276 5: for $j = 1$ to j do 277 6: for $k = 1$ to g do 278 7: for $v = 1$ to N do 279 8: Initialize $s_v(0)$ on a random pixel in image I_k 280 9: Initialize $h_v(0) = 0$, $c_v(0) = 0$ 281 10: $m_w(0) = 0$, $c_v(0) = 0$ 281 11: $m_w(0) = 0$ 281 22: end for 284 14: for $t = 0$ to $T - 1$ do 285 15: for $v = 1$ to N do 286 16: Make observation $o_v(t) = \text{observe}(I_k, s_v(t))$ 287 17: Get feature extraction $b_v(t) = \mathbf{b}_{\theta_4}(o_v(t))$ 288 18: Get state representation $q_v(t) = \mathbf{d}_{\theta_5}(s_v(t))$ 289 19: Calculate aggregate message $\overline{d}_v(t) = \frac{1}{\mathbf{h}_{eq}(v)} \sum_{n=1}^{N} d_n(t)$ 291 20: Form information input $u_v(t) = [b_v(t)^T q_v(t)^T \overline{d}_v(t)^T]$ 292 21: Run belief RNN using $u_v(t)$ as input 293 23: Run decision RNN using $u_v(t)$ as input 294 24: Update policy π on $\pi_{\theta_5}(\cdot, \hat{h}_v(t + 1))$ 295 35: Get action $a_v(t + 1)$ from π 296 Go to new spatial state $s_v(t + 1) = \text{transition}(s_v(t), a_v(t + 1))$ 297 298: end for 298: end for 299 29: for $v = 1$ to N do 300: Generate prediction vector p_v 311: end for 321: Calculate mean prediction vector \bar{p} 332: Calculate mean prediction vector \bar{p} 343: end for 354: end for 355: end for 355: end for 355: end for 355: end for 356: end for 357: return M_u	275	4:	for $i = 1$ to e do
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7: for $v = 1$ to N do 7: initialize $s_v(0)$ on a random pixel in image I_k 7: initialize $h_v(0) = 0, c_v(0) = 0$ 7: for $w = 1$ to $ \mathcal{N}_v $ do 7: for $w = 1$ to $ \mathcal{N}_v $ do 7: for $v = 1$ to $ \mathcal{N}_v $ do 7: for $v = 1$ to N do 7: for for in formation $v_v(t) = \mathbf{b}_{\theta_0}(v_v(t))$ 7: for in formation input $u_v(t) = \mathbf{q}_{\theta_0}(s_v(t))$ 7: form in formation input $u_v(t) = \mathbf{l}_{v_v}(t)^T \overline{d}_v(t)^T$ 7: form in formation input $u_v(t)$ a in jou 7: form in formation $u_v(t)$ a in jou 7: for in for in for in $n = \sqrt{n} \sqrt{n} \sqrt{n} (t + 1)$ 7: for in for $n = \sqrt{n} \sqrt{n} \sqrt{n} (t + 1)$ 7: for $v = 1$ to N do 7: for $v = 1$ for	277	6:	for $k = 1$ to g do
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13:end for14:for $t = 0$ to $T - 1$ do15:for $v = 1$ to N do16:Make observation $o_v(t) = observe(I_k, s_v(t))$ 17:Get feature extraction $b_v(t) = \mathbf{b}_{\theta_4}(o_v(t))$ 18:Get state representation $q_v(t) = \mathbf{q}_{\theta_5}(s_v(t))$ 19:Calculate aggregate message $\bar{d}_v(t) = \frac{1}{\ln \cdot \deg(v)} \sum_{n=1}^{N} d_n(t)$ 20:Form information input $u_v(t) = [b_v(t)^T q_v(t)^T \bar{d}_v(t)^T]$ 21:Run belief RNN using $u_v(t)$ as input22:Generate message $m_v(t) = \mathbf{m}_{\theta_2}(h_v(t))$ 23:Run decision RNN using $u_v(t)$ as input24:Update policy π on $\pi_{\theta_5}(\cdot, \hat{h}_v(t + 1))$ 25:Get action $a_v(t + 1)$ from π 26:Go to new spatial state $s_v(t + 1) = transition(s_v(t), a_v(t + 1))$ 27:end for28:end for29:Si for $v = 1$ to N do30:Generate prediction vector p_v 31:end for32:Calculate mean prediction vector \bar{p} 33:Compute discounted differentiable rewards with MA-REINFORCE policy gradients in Equation (6) and update parameters34:end for35:end for36:end for37:return M_u	283	12:	end for
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290 20: Form information input $u_v(t) = [b_v(t)^T q_v(t)^T \overline{d}_v(t)^T]$ 21: Run belief RNN using $u_v(t)$ as input 22: Generate message $m_v(t) = \mathbf{m}_{\theta_2}(h_v(t))$ 23: Run decision RNN using $u_v(t)$ as input 24: Update policy π on $\pi_{\theta_5}(\cdot, \hat{h}_v(t+1))$ 25: Get action $a_v(t+1)$ from π 26: Go to new spatial state $s_v(t+1) = \text{transition}(s_v(t), a_v(t+1))$ 27: end for 28: end for 29: for $v = 1$ to N do 30: Generate prediction vector p_v 301 31: end for 302 32: Calculate mean prediction vector \bar{p} 303 33: Compute discounted differentiable rewards with MA-REINFORCE policy gradients in Equation (6) and update parameters 34: end for 35: end for 36: end for 37: return M_u	289	19:	Calculate aggregate message $\bar{d}_v(t) = \frac{1}{\ln deg(v)} \sum_{n=1}^N d_n(t)$
291201Form minimum and $u_v(t)$ $[v_v(t) + v_v(t) + u_v(t) $	290	20.	Form information input $u_{\nu}(t) = [b_{\nu}(t)^T a_{\nu}(t)^T \bar{d}_{\nu}(t)^T]$
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294 24: Update policy π on $\pi_{\theta_5}(\cdot, \hat{h}_v(t+1))$ 295 25: Get action $a_v(t+1)$ from π 296 26: Go to new spatial state $s_v(t+1) = \text{transition}(s_v(t), a_v(t+1))$ 297 27: end for 298 28: end for 299 29: for $v = 1$ to N do 300 30: Generate prediction vector p_v 301 31: end for 302 32: Calculate mean prediction vector \bar{p} 303 33: Compute discounted differentiable rewards with MA-REINFORCE policy gradients in Equation (6) and update parameters 304 34: end for 305 35: end for 306 36: end for 307 37: return M_u	293	23:	Run decision RNN using $u_{a}(t)$ as input
295 25: Get action $a_v(t+1)$ from π 296 26: Go to new spatial state $s_v(t+1) = \text{transition}(s_v(t), a_v(t+1))$ 297 27: end for 298 28: end for 299 29: for $v = 1$ to N do 300 30: Generate prediction vector p_v 301 31: end for 302 32: Calculate mean prediction vector \bar{p} 303 33: Compute discounted differentiable rewards with MA-REINFORCE policy gradients in Equation (6) and update parameters 304 34: end for 305 35: end for 306 36: end for 307 37: return M_u	294	24.	Undate policy π on π_{e} (\hat{h} $(t+1)$)
296 26: Go to new spatial state $s_v(t+1)$ = transition $(s_v(t), a_v(t+1))$ 297 27: end for 298 28: end for 299 29: for $v = 1$ to N do 300 30: Generate prediction vector p_v 301 31: end for 302 32: Calculate mean prediction vector \bar{p} 303 33: Compute discounted differentiable rewards with MA-REINFORCE policy gradients in Equation (6) and update parameters 304 34: end for 305 35: end for 306 36: end for 307 37: return M_u	295	21.	Get action $a_{0}(t+1)$ from π
297 27: end for 298 28: end for 299 29: for $v = 1$ to N do 300 30: Generate prediction vector p_v 301 31: end for 302 32: Calculate mean prediction vector \bar{p} 303 33: Compute discounted differentiable rewards with MA-REINFORCE policy gradients in Equation (6) and update parameters 304 34: end for 305 35: end for 306 36: end for 307 37: return M_u	296	25.	Go to new spatial state $s_{i}(t+1) = \text{transition}(s_{i}(t), a_{i}(t+1))$
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307 37: return M_u	306	36:	end for
	307	37:	return M_u

³¹⁰ $r_{\tau_i}^d$ in Equation 6 denotes the reward of sampled trajectory τ_i detached from the computational graph and treated as a scalar, as in (Mousavi et al., 2019a).

The resilient performance with increasing dimensionality of high resolution training images, allows 313 our MASMU framework to be applicable in scenarios requiring the unlearning of very detailed 314 and therefore potentially extremely sensitive images. This also motivates our framework of Multi-315 Agent Speedy and Interpretable Machine Unlearning (MASIMU) as described in Algorithm 2, in-316 terpretably unlearning the influence of specific super-pixels in high resolution sensitive images by 317 re-weighting the gradient weights during fine-tuning just like in the IMU Algorithm without multiple 318 agents. After the agents are initialized, MASIMU algorithm goes through a number of steps where 319 information is exchanged between agents through the use of a RNN structure like LSTM or GRU. 320 Using this information as well as an observation of the immediate environment (pixels of the image 321 in the neighborhood of the agent), the agent makes a prediction of an image's class and then takes an action. After each batch of predictions, losses are calculated for the policy-based actor deciding 322 which action to take and the critic network assigning values to the actions taken by each agent, and 323 their weights are updated accordingly.

Alg	gorithm 2 Multi-Agent Interpretable Unlearning (MAIMU) (for both MALIMU and MASIMU)
1:	Input: training data D_{tr} of size tr , test data D_{te} of size te , retain data D_r of size r , forget
	data D_f of size f, LIME coefficients on retain data I_{D_r} , LIME coefficients on forget data I_{D_f} ,
	baseline model M
2:	Note: $f = tr - r$
3:	Training Parameters: epochs e , batches on retain data b , loss function L_f , batch size g , agents
	N, steps T
4:	$M_u = M$
5:	repeat
6:	for $i = 1$ to e do
7:	repeat
8:	$\mathbf{IOr} \ i = 1 \ \mathbf{IO} \ b \ \mathbf{OO}$
9:	Use N agents to run an episode of MA-REINFORCE as in Algorithm 1
10:	Obtains batch input features $D_r^{(r)}$ and target labels $D_r^{(r)}$ for b_r batched images
11:	Obtains LIME scores for batched images $I_{D_r^b}$
12:	Note: LIME scores are \sum of interpretable gradients over batched superpixels
13:	circuites gradients of parameters in <i>M</i> tracked by O
14:	$sim = \text{pcs}(I_{D_r^b}, I_{D_f})$
15:	$rsim = rowwise_average(sim for sim \neq 0)$
10:	$Crsim = \text{columnwise}_a \text{verage}(rsim)$
17:	$T_w = CFS(M)$ (interpretable weight of similar super-pixels in retain & forget sets)
10:	$\begin{aligned} u_u p_u &= M_u (D_r^{*}) \\ loss &= I_s (output D^{bt}) \end{aligned}$
19. 20·	$D_{f}(uiput, D_{r})$ Compute gradients $\nabla(loss)$ on the loss function during backward propagation
20.21	Note: There are p parameters in the pre-trained model
22:	Note: Interpretably unlearning influence of retain set on the forget set
23:	repeat
24:	for $i = 1$ to p do
25:	$\nabla_p(loss) = \nabla_p(loss) - I_w * \nabla_p(loss)$
26:	end for
27:	until all $\nabla_p(loss)$ are updated
28:	end for
29:	until all b batches are processed
30:	end for
31:	until all e epochs are updated
32:	Returns M_u unlearnt model

360 We measure the unlearning accuracy and loss (as in Equation 2) on AI models classifying each 361 dataset to measure the quality and accuracy of our unlearning frameworks. For successful unlearn-362 ing, it is good for the accuracy of the unlearned model on the *forget set* to be close to the accuracy of the unlearned model on the test set, as it indicates that the "forgotten" examples have never been 363 seen by the model to begin with, just like the test samples. Similarly, unlearned model on the retain 364 set should have a similar accuracy to the training accuracy of the original model. We also measure 365 completeness (Cao & Yang, 2015) of how close the unlearned model is to the original model. A high 366 completeness indicates better unlearning where the unlearned model is less distinguishable from the 367 original model when evaluated on unseen examples. We use the accuracy of Membership Infer-368 ence Attacks (MIAs) (Shokri et al., 2017), to measure how successfully we can guess that a given 369 example is part of retain set or forget set. Details of the above metrics are described in Appendix 370 A.5.

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5 Results

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 We train our Machine Unlearning (MU), Interpretable Machine Unlearning (IMU), Multi-Agent
 Speedy MU (MASMU) and Multi-Agent Speedy IMU (MASIMU) frameworks using a stochastic
 gradient descent (SGD) optimizer, a learning rate of 0.1 and a cross-entropy loss function. A comparative analysis of the unlearning performance for IMU and MU frameworks on the low-dimensional

EXPERIMENT	DATASET	MIA	Сомр
MU	RESISC-45	0.532	0.817
IMU	RESISC-45	0.536	0.813
MU	HAM-10000	0.640	0.781
IMU	HAM-10000	0.640	0.760
MU	CIFAR-10	0.503	0.832
IMU	CIFAR-10	0.513	0.849
MU	MNIST	0.545	0.998
IMU	MNIST	0.545	0.995

Table 1: Unlearning Results for Baseline Unlearning (MU) and our Interpretable Unlearning IMU
 Experiments (Exp) on Completeness (Comp) and Membership-Inference Attack (MIA) metrics

images in MNIST and the high-dimensional satellite images in RESISC-45 datasets indicates improved unlearning with increasing accuracy and decreasing loss across 25 epochs for IMU in Figure 3 when the gradients are interpretably re-weighted. Table 1 indicates that IMU framework is better for unlearning, increasing the completeness measure and taking the MIA accuracy score closer to 0.5 in comparison to MU. MASIMU computes local beliefs with GRU. Local beliefs are also computed with LSTMs in MALIMU framework for comparative analysis. Figure 5 shows that the benefits of using Multiple agents on unlearning time scale with the dimensionality of the dataset. MASIMU and MALIMU outperform all other frameworks on the very high dimensional HAM-10000 dataset and are not far behind in the high dimensional RESISC-45 dataset. Comparison of with retraining on retain set from scratch can be found in Table 4 showing that retraining from scratch is slower.



Figure 3: Machine Unlearning (MU) and Interpretable MU (IMU) Accuracy and Loss Plots

For our MASMU & MASIMU experiments, we use 3 agents, 5 steps per episode, an observation window size of 6, and a learning rate of 1 · 10⁻³, for the low-resolution MNIST images. On higher resolution images like RESISC-45, we use 16 agents, 16 steps per episode, an observation window size of 12, and a learning rate of 1 · 10⁻⁴. We reduce the learning rate for our multi-agent frameworks to make smaller learning steps by multiple agents for the optimal solution. This leads to the MASIMU and MASMU comparison over 5 epochs in Figure 4 on MNIST and RESISC-45 datasets

Table 2: Unlearning Results for our Baseline Multi-Agent Speedy Machine Unlearning (MASMU)
and our Multi-Agent Speedy and Interpretable Machine Unlearning Framework (MASIMU) on
Completeness (Comp), and Membership-Inference Attack (MIA) metrics.

EXPERIMENT	t Dataset	BELIEF	MIA	Сомр
MALMU	RESISC-45	LSTM	0.531	0.615
MASMU	RESISC-45	GRU	0.531	0.596
MALIMU	RESISC-45	LSTM	0.538	0.595
MASIMU	RESISC-45	GRU	0.533	0.603
MALMU	HAM-10000	LSTM	0.640	0.828
MASMU	HAM-10000	GRU	0.640	0.807
MALIMU	HAM-10000	LSTM	0.640	0.814
MASIMU	HAM-10000	GRU	0.640	0.838
MALMU	CIFAR-10	LSTM	0.498	0.645
MASMU	CIFAR-10	GRU	0.501	0.647
MALIMU	CIFAR-10	LSTM	0.498	0.648
MASIMU	CIFAR-10	GRU	0.501	0.636
MALMU	MNIST	LSTM	0.545	0.756
MASMU	MNIST	GRU	0.545	0.729
MALIMU	MNIST	LSTM	0.545	0.770
MASIMU	MNIST	GRU	0.545	0.732

showing a trend of MASIMU being better at unlearning in comparison to MASMU. Completeness increases and MIA values are closer to 0.5 in case of MASIMU as shown in Table 2.



Figure 4: Multi-Agent Unlearning Accuracy and Loss Plots

486 The accuracy on the *forget set* is comparable with that on the *test set* for the interpretative unlearning 487 frameworks, showing robustness for IMU, MALIMU or MASIMU. This achieves a major part of 488 the unlearning objective, which is that a member of the *forget set* should be evaluated as if the model 489 had never seen it in the first place. Unlearning time significantly reduces for MASMU, MALMU, 490 MASIMU and MALIMU, on the HAM-10000 and RESISC-45 datasets with respect to IMU and MU as shown in Figure 5. For HAM-10000, GRU-based MASMU is faster than LSTM-based MALMU 491 while MASIMU is slightly faster than MALIMU. For RESISC-45, MASMU and MALMU have 492 comparable unlearning times and so do MALIMU and MASIMU with MALMU being slightly 493 faster than MASMU. More importantly, unlearning time significantly decreases for MALIMU and 494 MASIMU in comparison to MALMU and MASU, even with the additional computational cost of 495 interpretatively re-weighting gradients during back-propagation in the fine-tuning process. Multiple 496 agents reduce observation space dimensionality per agent, leading to faster unlearning which is 497 important for AI applications sensitive to latency like disaster management detecting satellite images 498 (e.g. RESISC-45) or protecting medical privacy in skin cancer images (e.g. HAM-10000). 499



Figure 5: Unlearning Time Plots comparing our Frameworks

6 CONCLUSION AND FUTURE WORK

We have presented a Machine Unlearning (MU) framework with an interpretative component (IMU) 518 that we have extended with multiple agents (MA) in MALMU, MASMU, MALIMU and MASIMU 519 frameworks. Interpretation is important for providing insights into the behavior of the unlearned 520 model so that we understand how our model is unlearning by forgetting the influence of major 521 superpixels of images in the *forget set*, a part of the original training set. Our results show that Inter-522 pretable Machine Unlearning (IMU) is better than fine-tuning on the retain set (MU) when it comes 523 to completeness and accuracy on an MIA. When it comes to increased dimensionality with high 524 resolution training examples, MALIMU, MASIMU, MALMU and MASMU frameworks are sig-525 nificantly faster than IMU and MU for the MNIST and RESISC-45 datasets, which is an important 526 factor in weighing the compute costs and benefits of unlearning versus retraining a model. Notably 527 MASIMU and MALIMU are both faster than MALMU and MASMU, even with added compute 528 cost for interpretability, showing that multiple agents unlearn faster by reducing observation space 529 per agent. Furthermore, both IMU, MALIMU and MASIMU share the desirable robustness property 530 that an unlearned model has similar accuracy on the *forget set* and the test set, leading to a decreased probability that an adversary can use performance of the model on a member of the *forget set* to 531 infer membership in the training set. In future, we hope to explore how state-of-the-art cooperative 532 decision making algorithms such as Proximal Policy Optimization (PPO) (Schulman et al., 2017) 533 and Multi-Agent PPO (MAPPO) (Yu et al., 2022) along with single agent algorithms like self-play 534 (Bai et al., 2020) can be used to further increase the unlearning performance of MASIMU. 535

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A APPENDIX

667 A.1 ADDITIONAL RELATED WORKS

669 Machine Unlearning is a formulated as a problem (Nguyen et al., 2022) where there is a dataset D, a forget set $D_f \subset D$, and a model trained on the dataset A(D) passed into an unlearning algorithm 670 $U(\cdot)$. The unlearning algorithm returns a model where the influence of the members of D_f on the 671 output of the model has been reduced. Reasons are given to motivate the task of machine unlearn-672 ing, namely the removal of sensitive data from models used in sensitive industries such as healthcare 673 and finance. Several challenges arise when tackling machine unlearning, such as the stochasticity 674 of many training methods and reduction in performance for models that have been unlearned. The 675 survey also posits some desired properties of unlearning algorithms: having similar accuracy to the 676 original model (completeness) and being fast enough to justify not retraining the model (timeliness). 677 These two properties have a trade-off that must be considered when deciding whether to retrain or 678 unlearn a model. A summary and comparison of many unlearning methods is provided, covering 679 different types of methods (model-agnostic, model-intrinsic, data-driven), scenarios where the meth-680 ods can be applied (few-shot, zero-shot, zero-glance, exact, approximate), properties of the methods (completeness, timeliness, etc.) and the kinds of data that can be unlearned (items, features, etc.). 681 No reinforcement-learning based or multi-agent unlearning method was mentioned in this survey, 682 unlike our novel multi-agent reinforcement learning frameworks. 683

- 684 Machine unlearning has been applied to a wide variety of settings, including lifelong learning (Liu 685 et al., 2022) and toxicity mitigation in Large Language Models (Lu et al., 2022). This includes 686 applying it to Reinforcement Learning (Nikishin et al., 2022) (Ye et al., 2023) (Guo et al., 2023). Unlike prior work, however, we are focused on using Reinforcement Learning to forget examples 687 from a subset of a training set rather than having agents unlearn deleterious behavior learned early 688 on in training, attempting to forget an environment, or mitigating attacks by a trojan agent. Multi-689 objective Reinforcement Learning has been discussed as a possible future direction for machine 690 unlearning (Kassem et al., 2023) but has not yet been attempted as far as we are aware. 691
- (Laroche & Tachet Des Combes, 2022) address the issue of unlearning bad convergences when
 making policy updates in Reinforcement Learning. It does not really have anything to do with
 machine unlearning as the problem is formulated in works like (Nguyen et al., 2022). Nonetheless,
 it proposes to speed up the unlearning process through a modified cross-entropy-based approach, in
 contrast to traditional policy gradient updates.
- In order to address the problem of models that deal with outdated, irrelevant, or private data, (Shaik
 et al., 2023) introduce FRAMU, a framework that uses Reinforcement Learning and Federated
 Learning to achieve machine unlearning. Attention-based Machine Unlearning using Federated
 Reinforcement Learning. FRAMU can work with both single-modal and multi-modal data, and is
 suited for situations where the data distribution is dynamic. However, FRAMU is not very scalable
 and is computationally complex.

There have been attempts to apply machine unlearning to multi-modal data with potentially dynamic data distributions (Shaik et al., 2023) but so far they have not been scalable or computationally complex. As we value time complexity, we only consider single-modal data.

An approach to machine unlearning by sparsifying model parameters is posited by (Jia et al., 2023). While this research work achieves good results in metrics such as accuracy and Membership Inference attacks using resnet18 models and the CIFAR-10 dataset, the time cost associated with making the models sparse makes it less appealing as an unlearning method, given the possibility of retraining the model from scratch if time is not a concern. Furthermore, unlearning through making models sparse is not interpretable. These unlearning methods are not applicable for high resolution image classification tasks.

A.2 STATISTICS OF RETAIN AND FORGET SETS

Table 3: Statistics on the train, retain, forget and test datasets

DATASET	TRAIN	RETAIN	Forget	Test
RESISC-45	26775	24098	2677	4725
HAM-10000	8512	7661	851	1503
CIFAR-10	50000	45000	5000	10000
MNIST	60000	54000	6000	10000

ALGORITHM FOR INTERPRETABLE MACHINE UNLEARNING A.3

A.4 COMMUNICATION IN MULTI-AGENT MACHINE UNLEARNING

For MASMU, our agents are represented via vertices in a directed graph \mathcal{G} for N agents denoted by $\{1, ..., N\}$, the state of agent $i \in N$ at step t by $s_i(t)$, the observation of agent i at step t by $o_i(t)$, and the sampled action of agent i at time step t by $a_i(t)$. The set of edges in G is given by $\mathcal{E} \subset \{(i,j) : i \neq j\}$, where $(i,j) \in \mathcal{E}$ represents that *i* communicates messages to *j*. We let \mathcal{N}_i denote the set of neighbors of i, i.e., $\mathcal{N}_i = \{j : (i, j) \in \mathcal{E}\}$. An RNN is used to calculate the belief of the agent as it progresses through the task. We denote the hidden state of agent *i*'s belief LSTM at time step t via $h_i(t)$, and similarly denote the cell state (if the RNN is an LSTM) with $c_i(t)$. The hidden state of the belief RNN is used to create a message in Equation 7

$$m_i(t) = \mathbf{m}_{\theta_1}(h_i(t)) \tag{7}$$

where \mathbf{m}_{θ_1} is a function parameterized on θ_1 . This message is shared with agents in \mathcal{N}_i . An agent receives its messages from its neighbors and decodes them via a trainable parameterized function

$$d_i(t) = \mathbf{d}_{\theta_2}(m_i(t)) \tag{8}$$

with θ_2 parameters on d, aggregated by averaging to get

$$\bar{d}_i(t) = \frac{1}{indeg(i)} \sum_{j=1}^N d_j(t)$$
(9)

where indeg(i) is the number of nodes in G pointing to i. Features are extracted from the local observation by a trainable function

$$b_i(t) = \mathbf{b}_{\theta_3}(o_i(t)) \tag{10}$$

where θ_3 represents the parameters of **b**. We prepare the position of *i* for input to the belief RNN through parameterized mapping and thereby update the belief RNN.

$$q(t) = \mathbf{q}_{\theta_4(s_i(t))}.\tag{11}$$

If the RNN is an LSTM, it is updated according to the Equation 12.

 $\begin{bmatrix} h_i(t+1) \\ c_i(t+1) \end{bmatrix} = \mathbf{f}_{\theta_5}(\begin{bmatrix} h_i(t) \\ c_i(t) \end{bmatrix}, u_i(t))$ (12)

Alg	gorithm 3 Interpretable Machine Unlearning (IMU)
1:	Input: training data D_{tr} , test data D_{te} , retain data $D_r \subseteq D_{tr}$, forget data $D_f = D_{tr} \setminus D_r$,
	LIME coefficients on retain data I_{D_r} , LIME coefficients on forget data I_{D_f} , baseline model M.
2:	Training Parameters: epochs e , batches on retain data b , loss function L_f , learning rate sched-
	uler LS, optimizer O
3:	$M_u = M$
4:	repeat
5:	for $i = 1$ to e do
6:	repeat
7:	for $i = 1$ to b do
8:	Obtains batch input features D_r^{bf} and target labels D_r^{bt} for b_r batched images
9:	Obtains LIME scores for batched images $I_{D_r^b}$
10:	Note: LIME scores are \sum of interpretable gradients over batched superpixels
11:	Clears gradients of parameters in M tracked by O
12:	$sim = \operatorname{pcs}(I_{D_r^b}, I_{D_f})$
13:	$rsim = rowwise_average(sim \text{ for } sim \neq 0)$
14:	$crsim = $ columnwise_average $(rsim)$
15:	$I_w = crsim$ (Interpretable weight of similar super-pixels in retain & forget sets)
16:	$output = M_u(D_r^{o_J})$
17:	$loss = L_f(output, D_r^{ol})$
18:	Computes gradients $V(loss)$ on the loss function during backward propagation
19:	Note: There are p parameters in the pre-trained model
20:	Note: Interpretably unlearning influence of retain set on the forget set
21:	for $i = 1$ to n do
22. 23.	$\nabla_{\alpha}(loss) = \nabla_{\alpha}(loss) - I_{\alpha} * \nabla_{\alpha}(loss)$
$\frac{23}{24}$	end for
25:	until all $\nabla_r(loss)$ are updated
26:	end for
27:	until all b batches are processed
28:	end for
29:	until all e epochs are updated
30:	Returns M_u unlearnt model

If the RNN is a GRU then the update question will take the form:

$$h_i(t+1) = \mathbf{f}_{\theta_5}(h_i(t), u_i(t)) \tag{13}$$

where \mathbf{f}_{θ_5} is a trainable function, $u_i(t) = [b_i(t)^T \bar{d}_i(t)^T q_i(t)^T]$ consists of a three-part information input containing extracted features from the local observation, a representation of the agent's position within the example image, and the aggregate of the messages received by *i*. A decision LSTM with hidden state $\hat{h}_i(t)$ and cell state $c_i(t)$ is used for updating the policy.

$$\pi(a) = \pi_{\theta_6}(a, \hat{h}_i(t+1)) \tag{14}$$

for action $a \in A$. The decision LSTM is updated using the same information as the belief LSTM in Equation 15.

If a decision GRU is used instead of an LSTM, we only need to update the hidden state with Equation16.

- $\hat{h}_i(t+1) = \mathbf{f}_{\theta_7}(h_i(t)u_i(t))$ (16)
- We can sample an action $a_i(t)$ from the action space using π , and update our spatial state $s_i(t+1)$ accordingly. Each agent generates a raw prediction vector per step, with a value for each class using

parameterized mapping $p_i = \mathbf{p}_{\theta_8}(c_i(T))$. Finally, we calculate the shared prediction vector by averaging the raw prediction vectors across the agents. Thus our agents collaborate to form a final prediction vector.

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A.5 MULTI-AGENT MACHINE UNLEARNING EVALUATION

In order to evaluate the Multi-Agent Machine Unlearning frameworks, we compute the accuracy of the AI models, on the *retain set* D_{ret} , the *forget set* D_f , the *test set* D_{te} and the training set D_{tr} . For a given dataset D and AI model M, we calculate accuracy by calculating the number of correct predictions by M on D and then dividing it by the number of examples in D. Multi-label classification losses on each dataset are calculated using standard Cross Entropy Loss in Equation 2.

Another important comparison to make is the predictions of the unlearned model itself with those of the original model using distance metrics to quantify how "close" these two models are. To assess how often the predictions made by the original model M align with the predictions made by an unlearned model U, we calculate the "completeness" of the unlearned model in Equation 17. There, X is the *test set* of examples and $1_{\{C(U(x))\}}C(M(x))$ is the indicator function equal to one when the predicted class of the unlearned model U is the same as that of the original model M, and zero otherwise.

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857 858 859 $completeness(U, M) = \frac{\sum_{x \in X} \mathbf{1}_{\{C(U(x))\}} C(M(x))}{|X|}$ (17)

830 The concept of computing the accuracy of Membership Inference Attacks (MIA) (Shokri et al., 831 (2017) lends itself naturally to unlearning, where given a model M and a combination of examples 832 from the forget set D_f , and test set D_{te} , we see how accurately we can distinguish examples used 833 to train the model (members of the forget set) and examples not seen by the model during training 834 (the test set). Intuitively, we want the MIA's accuracy closer to 0.5 (a random guess). Our baseline 835 models fine-tuned on the *retain set* D_r are scored in Equation 18 with a simple MIA attack consisting of 10-fold cross-validation score for a simple logistic regression model trained on losses from 836 samples of D_f and D_{te} and categorized based on their inclusion in the training set (i.e. members of 837 the *forget set* are also in the training set, whereas member of the *test set* are not). 838

$$MIA(SL, inTrain) = CV_{10}(LR, SL, inTrain)$$
⁽¹⁸⁾

where $SL \in \mathbb{R}^n$ is a set of losses for *n* examples, $inTrain \in \{0, 1\}^n$ is a set of 0s and 1s categorizing whether the example is in the training set (1) or not (0), LR is a logistic regression model, and CV_{10} is a standard 10-fold cross validation procedure that returns an accuracy score of how well the logistic regression model distinguishes the members of the *forget set* from the *test set* based on their example losses.

A.6 RETRAINING TIME ON RETAIN SET

Dataset	Multi-Agent Retraining Time (seconds)
RESISC-45	5291.96
HAM10000	3556.20

Table 4: Multi-Agent Retraining Time on Retain Set re-training from scratch (25 Epochs)

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